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RECEIVED 21 March 2023

ACCEPTED 25 April 2023

PUBLISHED 25 May 2023

CITATION

Diao E, He Y, Liu X, Tong Q, Yang T, Liu X
and Lewis JP (2023), First principles data-
driven potentials for prediction of iron
carbide clusters.

Front. Quantum Sci. Technol. 2:1190522.
doi: 10.3389/frqst.2023.1190522

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First principles data-driven potentials for prediction of iron carbide clusters

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Many have reported the use of quantum chemistry approaches for evaluating the catalytic properties of iron carbide clusters. Unfortunately, structural energy calculations are computationally expensive when using density functional theory. The computational cost is prohibitive for high-throughput simulations with large length and time scales. In this paper, we generate data from 177 k clusters and choose state-of-the-art machine learning models within physical chemistry to train the features of this data. The generated potential gives a very high prediction accuracy on the order of the structure stability and achieves better adaptability/tolerance to poor structures of clusters. In addition, we use the machine learning potential to assist in high-throughput data collection and the prediction of hydrogen adsorption sites on cluster surfaces. We achieve more stable adsorption locations of the hydrogen atom more rapidly compared with traditional quantum chemical calculations.

KEYWORDS

iron carbide clusters, machine learning potentials, adsorbate prediction, cluster optimization, high-throughput data analysis

1 Introduction

Iron-based catalysts have been widely adopted in many chemical processes such as ammonia synthesis (Emmett and Brunauer, 1934; Emmett and Brunauer, 1937), Fischer-Tropsch synthesis (FTS) (Fischer and Tropsch, 1923; Fischer and Tropsch, 1926), CO oxygenation (Li et al., 2003; Qiao et al., 2011), and propane dehydrogenation (Sun et al., 2015; Tan et al., 2016). Among them, iron carbides are commonly utilized within the catalyst systems. Particularly, in FTS, which converts syngas to hydrocarbons, iron carbides (ϵ -Fe₂C, ϵ' -Fe_{2,2}C, χ -Fe₅C₂, θ -Fe₃C, and Fe₇C₃) (de Smit and Weckhuysen, 2008; de Smit et al., 2009; Liu et al., 2017) are usually regarded as the active phases. However, under practical conditions, the catalysts are usually present as mixture phases and exhibit a wide range of nanocluster size distributions (Herranz et al., 2006; Chang et al., 2018). Iron particles are also active as catalysts for carbon nanotube preparation, which is a highly promising material for application as catalyst substrates or energy conversion systems (Baughman et al., 2002; Kumar and Ando, 2010; Pant et al., 2021).

For the bulk iron carbides, the structures are usually observed as a distorted metal lattice, with the carbon atoms located at interstitial sites determined by geometric and electronic factors (Oyama, 1992). In θ -Fe₃C (cementite), χ -Fe₅C₂ (Hägg carbide), and Fe₇C₃, carbon atoms are in the trigonal prismatic interstices (de Smit and Weckhuysen, 2008), while ε -Fe₂C and ε' -Fe_{2.2}C possess structures with carbon atoms occupying the octahedral interstices. For small Fe_xC_y clusters [e.g., FeC, FeC₂, FeC_n ($n = 3-6$), and Fe_nC_m ($n = 1, 2, 3$ and $m = 2-8$)], extensive experimental work has found a variety of compositions, structures, and even catalytic properties from the mass spectra and gas phase ion chromatograph (Fan and Wang, 1994; Drechsler et al., 1995; von Helden et al., 1994; Steglich et al., 2014; Pilgrim and Duncan, 1993). Computationally, the detailed structures and bond strength of iron carbide clusters are determined by energetic calculations (Nash et al., 1996; Tzeli and Mavridis, 2002; Gutsev and Bauschlicher, 2003; Noya et al., 2003; Ryzhkov et al., 2005; Ryzhkov et al., 2008; Largo et al., 2009; Ryzhkov and Delley, 2012; Li et al., 2013; Chen and Xie, 2014). For example, the ground states for FeC₂₋₄ are fan-like structures, while linear and cyclic geometries are more stable structures for FeC₅ and FeC₆₋₁₀, respectively (Zhu and Li, 2009). Zheng et al. (2016) investigated Fe_xC_y ($x \leq 8$; $y \leq 8$) clusters combining structure searching and optimization by density functional theory and found that carbon chains are energetically preferred in carbon rich clusters. In addition, the catalytic reaction mechanisms on the clusters are also estimated with calculated energies (Li et al., 2015). However, in various catalysis systems, a huge class of iron carbides with varying element numbers and configurations should be calculated to fully represent the potential structures that exist, especially in FTS where thousands of possible elementary reactions and complex catalyst components occur. Fast and accurate methods are desperately needed to reduce the expensive structural

explorations. The community needs an advanced high-throughput calculator to explore metal carbide/oxide cluster systems.

Machine learning (ML) has emerged as a powerful new tool in chemistry (Butler et al., 2018; Xie and Grossman, 2018; Ye et al., 2018), driven in part by the advent of large material datasets from high-throughput electronic structure calculations. To the best of our knowledge, differently from some famous benchmarks in molecules (such as QM9, with 134 k molecules) and crystals (such as MatBench, which contains many datasets, with 132 k samples at most), no cluster benchmark has been published for iron carbides. Therefore, we must first develop a cluster dataset to provide the necessary exploration framework.

The scientific community has developed a wide variety of molecular representation methods for machine learning approaches to structure optimization—for example, SIFF (Structural Information Filtered Features) developed by Lewis et al. (Zeledon et al., 2020), SMILES (Simplified Molecular Input Line Entry Specification) (Weininger et al., 1989), SOAP (Smooth Overlap of Atomic Positions) (Bartók et al., 2013), CM (Coulomb Matrix) (Rupp et al., 2012), pymatgen (Python Materials Genomics) (Ong et al., 2013), and others. As an integral part of the ML architecture, the representation or defined features of molecular entities play a vital role in how accurately the ML model predicts the desired properties. Many machine learning approaches have been developed with an aim toward drug discovery (Yang et al., 2019; Chen et al., 2019; Feinberg et al., 2018; Schütt et al., 2018). Many approaches have focused on organic molecules, which mainly contain C, H, O, and N. However, for heterogeneous catalysis, we need representations that are appropriate for clusters containing transition metal atoms. Therefore, we evaluate the performance on cluster prediction using state-of-the-art machine

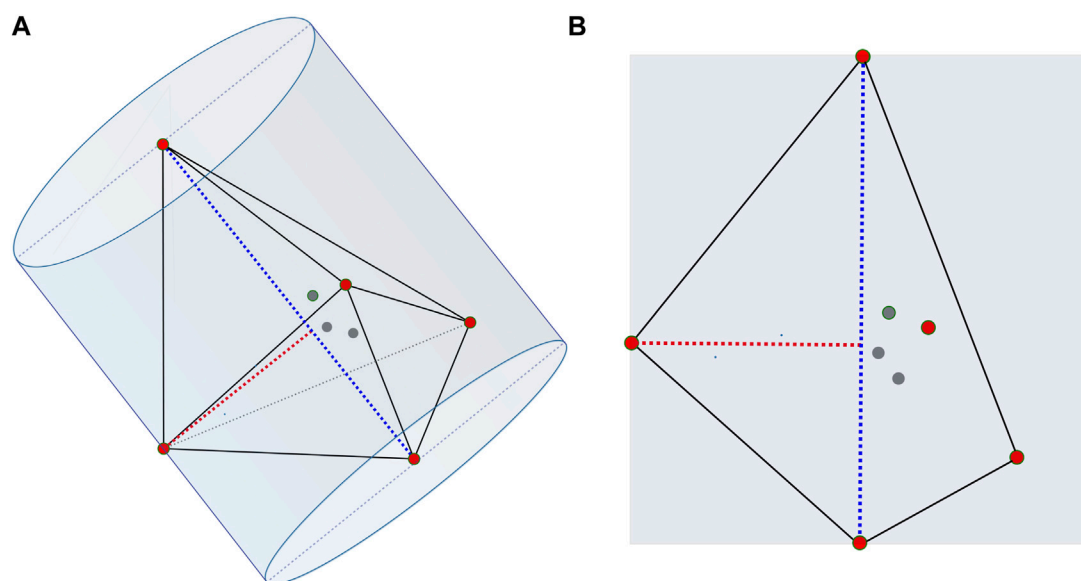


FIGURE 1

Long and short axes calculation of a certain Fe₄C₄. The blue dotted line, the long axis, is the farthest distance between the two atoms. The red dotted line, the short axis, is the farthest distance from the atom to the long axis. The central axis of the cylinder is the long axis, and the short axis is the radius. (B) is a cross-section of (A).

TABLE 1 Classification of Datasets.

Clusters	FeC _x	Fe ₂ C _x	Fe ₃ C _x	Fe ₄ C _x	Fe ₅ C _x	Fe ₆ C _x	Fe ₇ C _x	Fe ₈ C _x	Fe ₉ C _x
Counts	29,181	32,806	26,508	27,442	23,452	19,280	14,853	3,659	155

Number of structures located in each grouping of the composite dataset. The dataset is divided according to the stoichiometric count of iron atoms within the cluster.

learning models such as graph networks, MEGNet (Chen et al., 2019), or the continuous-filter convolutional neural network SchNet (Schütt et al., 2018).

In this work, we use the structure generation software combined with a first-principles calculator to search the structure of iron carbide clusters. We generate an Fe-C machine learning potential that is data driven from the high-throughput calculations of many clusters. There are several advantages of machine learning potentials compared to purely traditional quantum chemistry calculations for cluster structure optimization. The relative energy will determine the thermodynamic stability of different structures, and the equilibrium geometric configurations are found more rapidly using machine learning potentials. There is a demonstrated significant improvement in calculation speed for machine learning algorithms. Our work was released as an open-source code within a GitHub repository located at https://github.com/tony-dd/FeC_prediction.

2 Computational methodology

2.1 Clusters generation

In our dataset, we generate iron carbide clusters using the Crystal Structure Analysis by Particle Swarm Optimization (CALYPSO) code (Lv et al., 2012; Wang et al., 2012). The geometry optimization and energy calculations come from the Vienna Ab-initio Simulation Package (VASP) (Kresse and Furthmüller, 1996a; Kresse and Furthmüller, 1996b). Within these calculations, the electron-ion interactions are described from projector augmented wave (PAW) (Blöchl, 1994; Kresse and Joubert, 1999) potentials, and the electron exchange and correlation energy are treated by the Perdew–Burke–Ernzerhof (PBE) function, including spin polarization (Perdew et al., 1996). All calculations are performed within a box size of 15 Å to simulate a cluster calculation. The cut-off energy of 400 eV and Gaussian smearing with the width of 0.1 eV with the Gamma k-point sampling ensure accurate energies for the Fe-C clusters.

2.2 Clusters energy prediction

We have generated over 177 thousand structures and divided the entire dataset into nine parts according to the stoichiometric count of the iron atoms within the cluster. Detailed distributions of each group within the dataset are provided in Table 1.

MEGNet and SchNet are proven to work well with the QM9, MD17, and ISO17 datasets; hence, we choose these methods to predict our Fe-C clusters. The molecular representation, or features, of MEGNet is in the pymatgen format. We label the molecular

representation of SchNetPack as ‘SchNet’, because SchNetPack does not report the format of its molecular representation. We first use the ASE package to process each cluster structure and then fit structural representations of all the clusters to the two different feature representations—pymatgen and SchNet. During the training of our data, we use the default parameters that are found within MEGNet and SchNetPack. A cross-validation training strategy yields the best results by randomly shuffling and training all but one of the nine datasets and testing on the final dataset. This approach reduces the influence of the data proximity and thereby generalizes the performance of the models. The validation error is monitored, and the training is stopped when the validation error does not improve for 20 consecutive epochs. The models are trained on Nvidia RTX 3080 GPUs. Most models reach convergence within 500 epochs. On average, the training process takes 50 s and 80 s per epoch for each model, respectively. All chemistry structure calculations are handled using the Atomic Simulation Environment (ASE) (Larsen et al., 2017). Finally, we get nine trained models, and we develop the average predicted results to fit the final potential function.

2.3 Hydrogen adsorption prediction

The machine learning models need retraining from a new dataset when modeling the location of hydrogen adsorption on the Fe-C clusters. We apply the SchNet model to assist VASP in optimizing structures to generate a new dataset, which reduces a lot of the computing and time cost. More specifically, we select two structures with the largest variation in shape for each stoichiometry of the Fe_xC_y structure. The variation is defined by comparing the proportions of the long and short axes of the cluster. Figure 1 shows the calculation of the long and short axes of one structure. The convex hulls of the selected structures are calculated using SciPy. We introduce hydrogen atoms randomly on the planes parallel to the convex hulls and at 1 Å, as shown in Figure 2. The potentials of Fe and C are trained from the previous models, so the machine learning models can be used to optimize iron and carbon atoms in the new Fe-C clusters. The models optimize the structures, which significantly shortens the optimization calculation time. Finally, the structures processed by the models are optimized by VASP to obtain the final dataset.

The final trained models from the new datasets will predict the adsorption position of hydrogen atoms on the surface of the Fe-C clusters. As a demonstration of our approach, we have selected a stable Fe₅C₂ cluster from our initial dataset and randomly introduced a hydrogen atom on the surface. Fixing iron and carbon atoms in the structure, we conduct the following computational steps:

- (1) Optimize the hydrogen absorption by VASP.

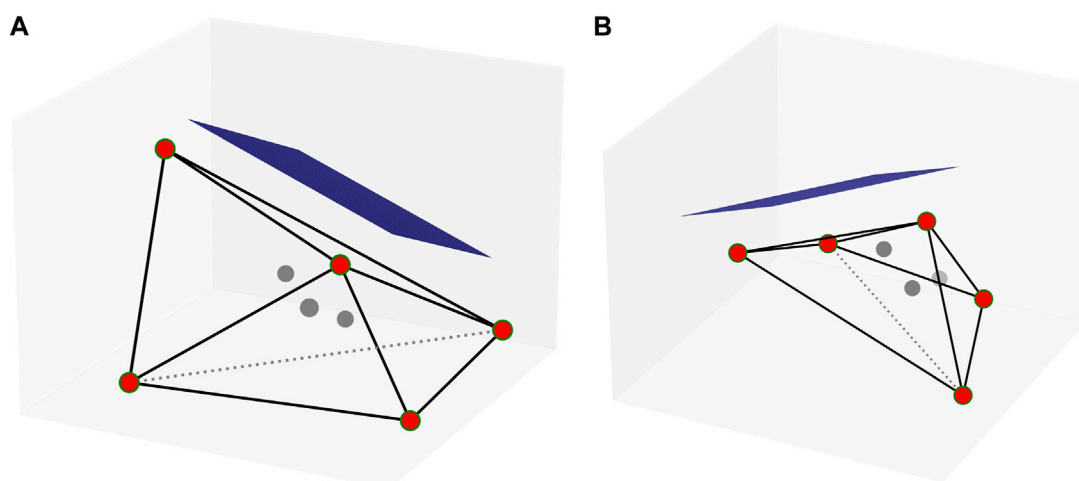


FIGURE 2

Convex hull of a certain Fe_4C_4 from two perspectives. The red circles are on the convex hull, and the gray circle is inside the convex hull. The blue planes are parallel to the surfaces of the convex hull, and the quantity is equal to the number of convex hull surfaces. The hydrogen atoms are randomly selected on the blue planes.

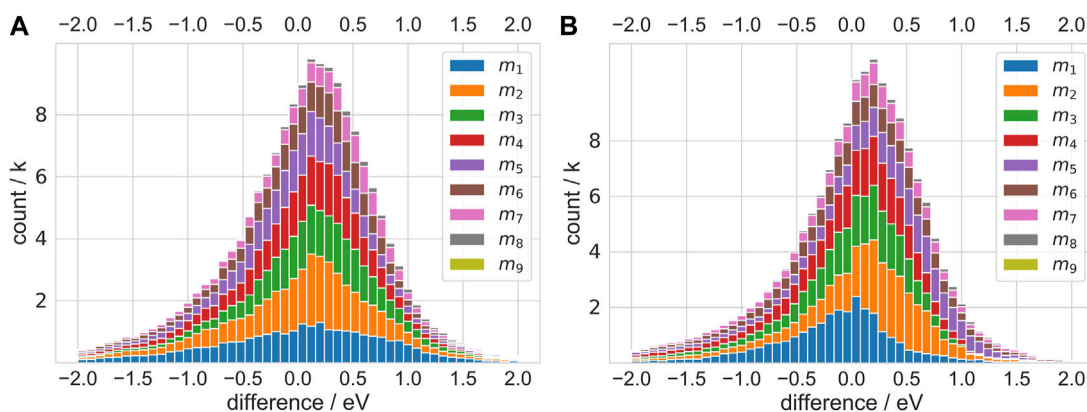


FIGURE 3

Error distribution histogram. The difference refers to the difference between the predicted value and the DFT calculated values for each structure. The m_i ($1 \leq i \leq 9$) means Fe_iC_j for test and others for training.

- (II) Optimize it next by SchNet and VASP and use the conjugate gradient method for SchNet local optimization.
- (III) Optimize it also by SchNet and VASP but use the Broyden–Fletcher–Goldfarb–Shanno (BFGS) algorithm and SchNet local optimization

We utilize both the conjugate gradient and BFGS to show the influence of different optimization algorithms on the results.

3 Results and discussion

The distribution of the difference between the predicted values and actual values will provide an evaluation of the predicted

accuracy of our machine learning models. We plot these results in Figure 3. The different colors represent the different testing sets. The average errors between the predicted values and the actual value are within 0.5 eV. In addition to the absolute values of prediction, the relative order accuracy (ROA) of the results represents a more significant evaluation of the model accuracy. The relative order accuracy evaluates the final optimized structure directly by using energy as a convergence condition. We sort the test data according to the DFT calculated values, shown in Figure 3, and assign each dataset an identifier: m_1, m_2, \dots , etc. We reorder the test data according to the potential energy predicted by the model and calculate the inversion number I of each set and rearrange each set according to the inversion number (as discussed in the Supplementary Material).

TABLE 2 Energy Prediction Results.

Id	Train	Test	\overline{CNT}	MEGNet		SchNet	
				E (eV)	ROA (%)	E (eV)	ROA (%)
m ₁	Fe ₂ C _x ~ Fe ₉ C _x	Fe ₁ C _x	7.597	0.722	97.8	0.507	98.5
m ₂	Fe ₁ C _x , Fe ₃ C _x ~ Fe ₉ C _x	Fe ₂ C _x	7.253	0.571	98.1	0.513	98.4
m ₃	Fe ₁ C _x ~ Fe ₂ C _x , Fe ₄ C _x ~ Fe ₉ C _x	Fe ₃ C _x	7.598	0.546	98.0	0.465	98.1
m ₄	Fe ₁ C _x ~ Fe ₃ C _x , Fe ₅ C _x ~ Fe ₉ C _x	Fe ₄ C _x	7.880	0.581	97.8	0.597	97.9
m ₅	Fe ₁ C _x ~ Fe ₄ C _x , Fe ₆ C _x ~ Fe ₉ C _x	Fe ₅ C _x	8.387	0.628	97.3	0.659	97.1
m ₆	Fe ₁ C _x ~ Fe ₅ C _x , Fe ₇ C _x ~ Fe ₉ C _x	Fe ₆ C _x	8.713	0.721	96.2	0.792	95.9
m ₇	Fe ₁ C _x ~ Fe ₆ C _x , Fe ₈ C _x ~ Fe ₉ C _x	Fe ₇ C _x	9.099	0.847	94.8	0.868	94.5
m ₈	Fe ₁ C _x ~ Fe ₇ C _x , Fe ₉ C _x	Fe ₈ C _x	9.396	0.930	91.8	1.017	91.7
m ₉	Fe ₁ C _x ~ Fe ₈ C _x	Fe ₉ C _x	10.000	1.310	86.2	1.545	86.4
AVG				0.776	95.3	0.773	95.4

\overline{CNT} means the average atoms count in each sub-dataset, E (eV) is the prediction error (MAEs) in eV, and ROA is the percentage of successful order prediction between any test case pair in each test dataset.

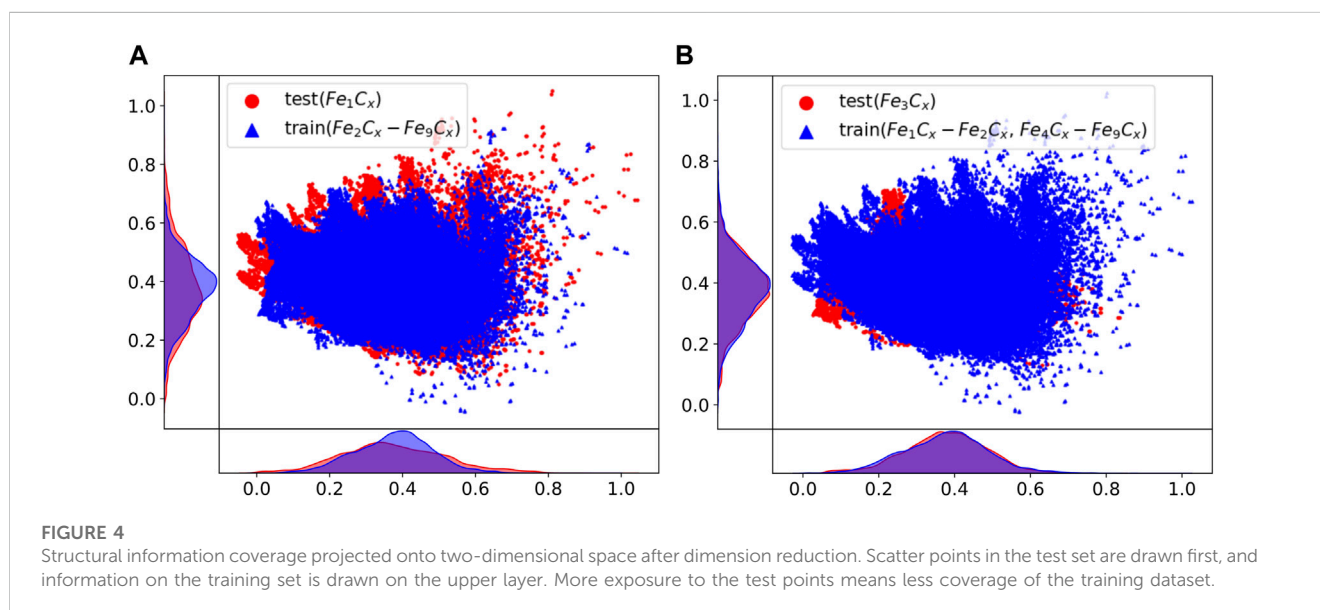


FIGURE 4

Structural information coverage projected onto two-dimensional space after dimension reduction. Scatter points in the test set are drawn first, and information on the training set is drawn on the upper layer. More exposure to the test points means less coverage of the training dataset.

Table 2 shows the comparison of the prediction results with the DFT calculated values, including the mean absolute errors (MAEs) and ROAs for MEGNet and SchNet. The average MAEs of the results are below 0.8 eV, and the average ROAs of prediction are above 95%. It can be seen that the ability of machine learning models to predict the ROA is excellent, which can ensure the reliability of the structural optimization. It is interesting that potential energy prediction MAE of m_3 is the smallest. We suggest the deviation of potential energy prediction is related to the average atoms count in the test and the coverage of the training set on the test set. In m_i ($i \leq 3$), we output the intermediate vectors predicted by MEGNet to verify the relationship between the MAEs and the coverage of the training set on the test set. Figure 4 shows the results after the

intermediate vector dimension reduction. Through comparison, we find that the coverage of m_3 training data on the test data exceeds m_1 significantly, which can explain the previous observation to a certain extent. In m_j ($j \geq 4$), the deviation of potential energy prediction increases with the average number of atoms. When the average number of atoms in the test set exceeds 8, the MAEs are mainly affected by that.

The high accuracy of the relative order shows that machine learning models have excellent performance in judging structural stability. To further demonstrate this point, we apply models to predict the relationship between the potential energy and the Fe-C distances, comparing the results with the calculation results of VASP. Detail information is shown in Figure 5. The distance

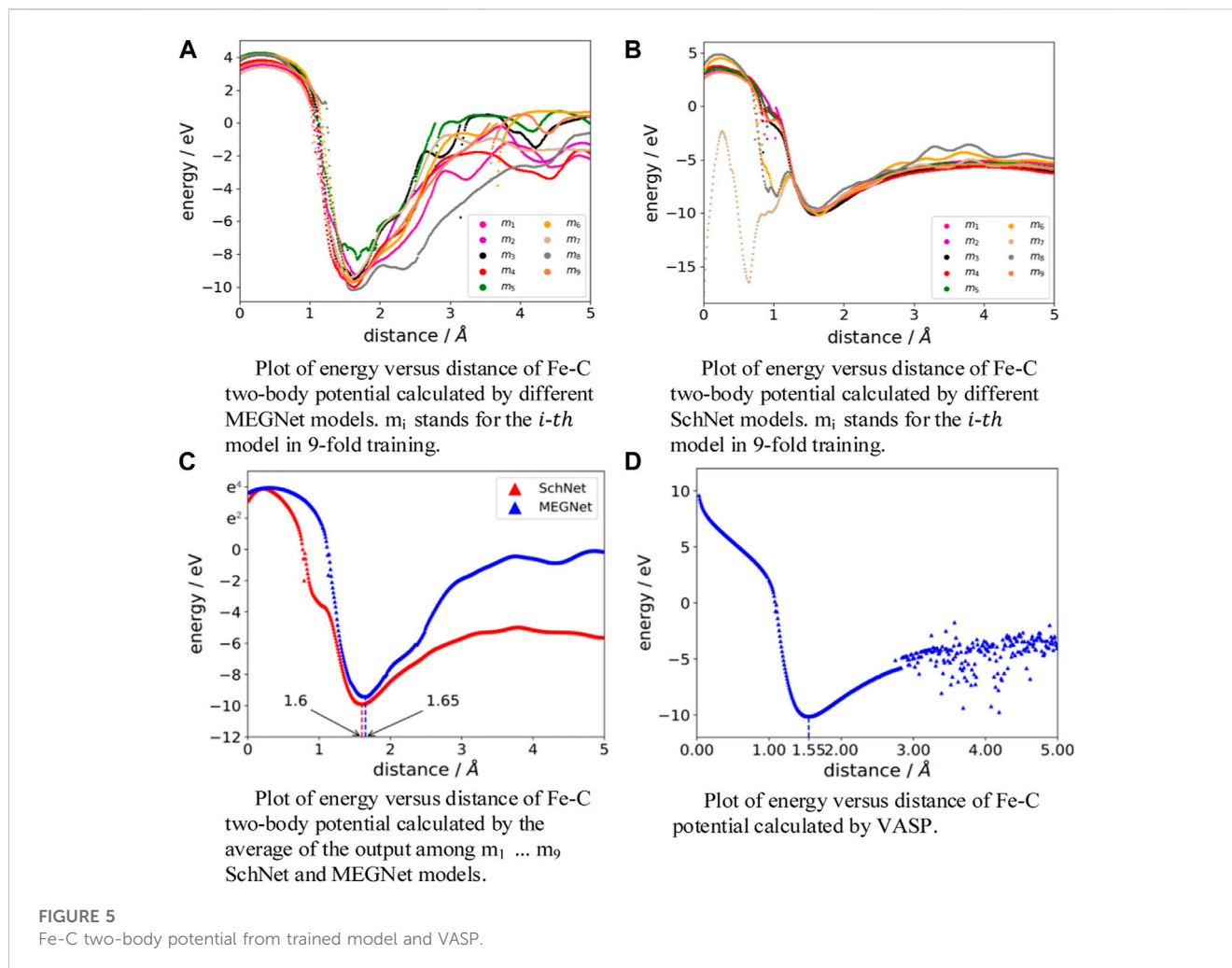


TABLE 3 Structural Optimization Results.

Id	T_{SchNet} (s)	T_{VASP} (s)	E_{SchNet} (eV)	E_{VASP} (eV)
(I)		2.05×10^3		1.62
(II)	4.30–16.07	1.27×10^3 – 2.33×10^3	5.44–7.30	0.79–2.81
(III)	16.89–321.04	1.63×10^3 – 1.92×10^3	3.94–7.10	0.99–3.19

T_{SchNet} (s) means the time consumed by the SchNet model optimization, and T_{VASP} (s) means the time consumed by VASP optimization. E_{SchNet} (eV) means the decrease of potential energy after the SchNet model optimization, and E_{VASP} (eV) means the decrease of potential energy after VASP optimization. All potential energy reductions are achieved by a single-point calculation of VASP.

between Fe and C is 0–5 Å, and the step length is 0.01 Å. Therefore, there are 500 points in each curve that show the relationship between the Fe-C distance and the potential energy. We focus on the trend of the curves and the lowest points representing the most stable distances. The trend and the lowest points of the curves predicted by MEGNet and SchNet are roughly the same throughout Figures 5A, B. We average the results of the MEGNet and SchNet models and visualize this average in Figure 5C. The result of the VASP calculation is shown in Figure 5D as a reference. According to the calculation of VASP, the change of the potential energy is no longer apparently regular when the distance of Fe-C exceeds 3 Å. The most stable distance of Fe-C predicted by MEGNet and SchNet

differs from VASP by 0.1 Å and 0.05 Å, respectively, as observed in Figures 5C, D.

We randomly generate 100 Fe_5C_5 poor initial structures to investigate the adaptability of models in structural optimization. These initial structures are considered poor in that VASP cannot optimize these structures. Traditional quantum chemical calculators such as VASP can effectively predict cluster geometries with a high level of accuracy. However, poor guesses from the user will add costly computational cycles in the performance, and these quantum chemistry tools struggle with out-of-the-box initial geometries. We test these 100 Fe_5C_5 poor initial structures so that we can obtain an understanding of the performance of VASP in extreme cases and

compare them with our machine learning approach. We also generate several typical Fe₅C₅ clusters to verify the performance of the structure optimization of the SchNet machine learning models. The SchNet model is treated as a ‘calculator’ of ASE, and BFGSLineSearch is used for local optimization. After about 100 steps of optimization, the potential energy of structures decreases rapidly by more than 10 eV while each step takes less than one second (as seen in [Supplementary Figure S4](#)). We find stable structures in a short time without expensive first-principles calculations.

Based on this, we generate 10 k new Fe_xC_yH data by the method in [Section 2.3](#) and use VASP to perform a single point calculation for most of these structures with the same parameters as [Section 2.1](#). We continue to train previous machine learning models with the new dataset to predict the adsorption position of hydrogen atoms. [Table 3](#) shows the results of structural optimization of the hydrogen absorption calculations with iron and carbon atoms fixed in [Section 2.3](#). In (I), the potential energy of the structure is reduced by 1.62 eV. In (II), the SchNet model can more rapidly reduce the potential energy of the structure by more than three times in less than 1% optimization time compared with VASP. In (II) and (III), the difference of the final structural potential energy is within 1 eV after VASP optimization to convergence. As a result, different local optimization algorithms have little effect on the results. Meanwhile, our results show that the model will optimize the structure to a more stable state than VASP in a much shorter time, and SchNet can also assist VASP in finding the most stable adsorption position by improving the initial guesses.

4 Conclusion

To conclude, we use CALYPSO and VASP for iron carbide cluster generation and apply state-of-the-art molecular properties prediction networks to the potential energy prediction of clusters and structural optimization. Although there are errors between machine learning models and DFT calculation methods in cluster potential energy prediction, the performance of models in judging structural stability is excellent. As a result, machine learning models can provide reliable structural optimization. In terms of cluster structure optimization, the machine learning models can obtain a more stable structure than VASP in a shorter time. Further, they can be used to assist VASP in finding the most stable adsorption position on the cluster surface in the catalytic process. This work is helpful in exploring the essential control factors of catalytic reaction activity and selectivity and realizing the regulation of catalyst activity and selectivity.

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Author contributions

All authors listed have made a substantial, direct, and intellectual contribution to the work and approved it for publication. All authors contributed to the article and approved the submitted version.

Funding

This project was supported by the National Natural Science Foundation of China (No. 22002008), National Key R&D Program of China (No. 2021YFB2600600), and the Ningxia Key Research and Development Project (No. 2022BEE03002). Additional funding was provided to the Institute of Data Science for promoting the development of universities for key research and cultivation projects (No. 2121YJPY225) and for building innovation capacity for scientific research institutions.

Conflict of interest

Author JL was employed by Synfuels China Co. Ltd.—SynCat@ Beijing and Author JL was employed by Hong Kong Quantum AI Laboratory, Ltd.

The remaining authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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Supplementary material

The Supplementary Material for this article can be found online at: <https://www.frontiersin.org/articles/10.3389/frqst.2023.1190522/full#supplementary-material>

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