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Detection of infrared light through stimulated four-wave mixing process

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Infrared optical measurement has a wide range of applications in industry and science, but infrared light detectors suffer from high costs and inferior performance than visible light detectors. Four-wave mixing (FWM) process allows detection in the infrared range by detecting correlated visible light. We experimentally investigate the stimulated FWM process in a hot ⁸⁵Rb atomic vapor cell, in which a weak infrared signal laser at 1,530 nm induces the FWM process and is amplified and converted into a strong FWM light at 780 nm, the latter can be detected more easily. We find the optimized single- and two-photon detunings by studying the dependence of the frequency of input laser on the generated FWM light. What's more, the power gain increases rapidly as the signal intensity decreases, which is consistent with our theoretical analysis. As a result, the power gain can reach up to 500 at a signal laser power of 0.1 μW and the number of detected photons increased by a factor of 250. Finally, we experimentally prove that our amplification process can work in a broad band in the frequency domain by exploring the response rate of our stimulated FWM process.

KEYWORDS

amplification, infrared detection, conversion, stimulated, four-wave mixing

1 Introduction

Infrared optical measurement is an important technique for applications in scientific research and industrial production. However, infrared light detectors in infrared optical devices have higher dark count rates, lower specific detectivities, and higher cost than the detector in the visible range, and often need to be cooled (Griffiths and de Haseth, 2007). For this dilemma, researchers correlate infrared light with visible light through nonlinear optical phenomena, and measure infrared light by detecting visible light with visible light detectors (Kalashnikov et al., 2016; Paterova et al., 2018). Four-wave mixing (FWM) is a common method for generating high-power visible light (Lavoute et al., 2010) and converting infrared light to visible light (Ding et al., 2012a, d, e), the latter is investigated in our work.

Four-wave mixing process is one of the prominent nonlinear optical phenomena (Yariv and Pepper, 1977) and originates from the third-order optical nonlinear effects in the interaction of optical fields with a nonlinear medium. In atomic system, the FWM process has been explored extensively due to its wide applications such as observing optical parametric amplification in the process of degenerate stimulated four-photon interaction (Carman et al., 1966) and optical precursors phenomena (Ding et al., 2015); generating non-classical correlated photon pairs (Ding et al., 2012c; Liu et al., 2012; Dong et al., 2017; Yu et al., 2018) via the spontaneous FWM process for use in long-distance quantum communication (Duan et al., 2001) and optical quantum information processing (Zhang et al., 2020a); observing squeezed light (Slusher et al., 1985) and strong relative intensity squeezing (McCormick et al., 2007); exhibiting localized entanglement of twin images (Boyer et al., 2008); and converting frequency of the optical field (Radnaev et al., 2010; Ding et al., 2012b). The FWM process has been realized in atomic system with various energy-level configurations such as double-ladder type (Lee et al., 2016; Lee and Moon, 2017a), double-lambda type (Ding et al., 2013b; Zhang et al., 2018; Yu et al., 2020), diamond type (Ding et al., 2013a; Shi et al., 2020) and inverted-Y type (Wen et al., 2008). In this paper, we focus on a four-level system with a diamond-type configuration.

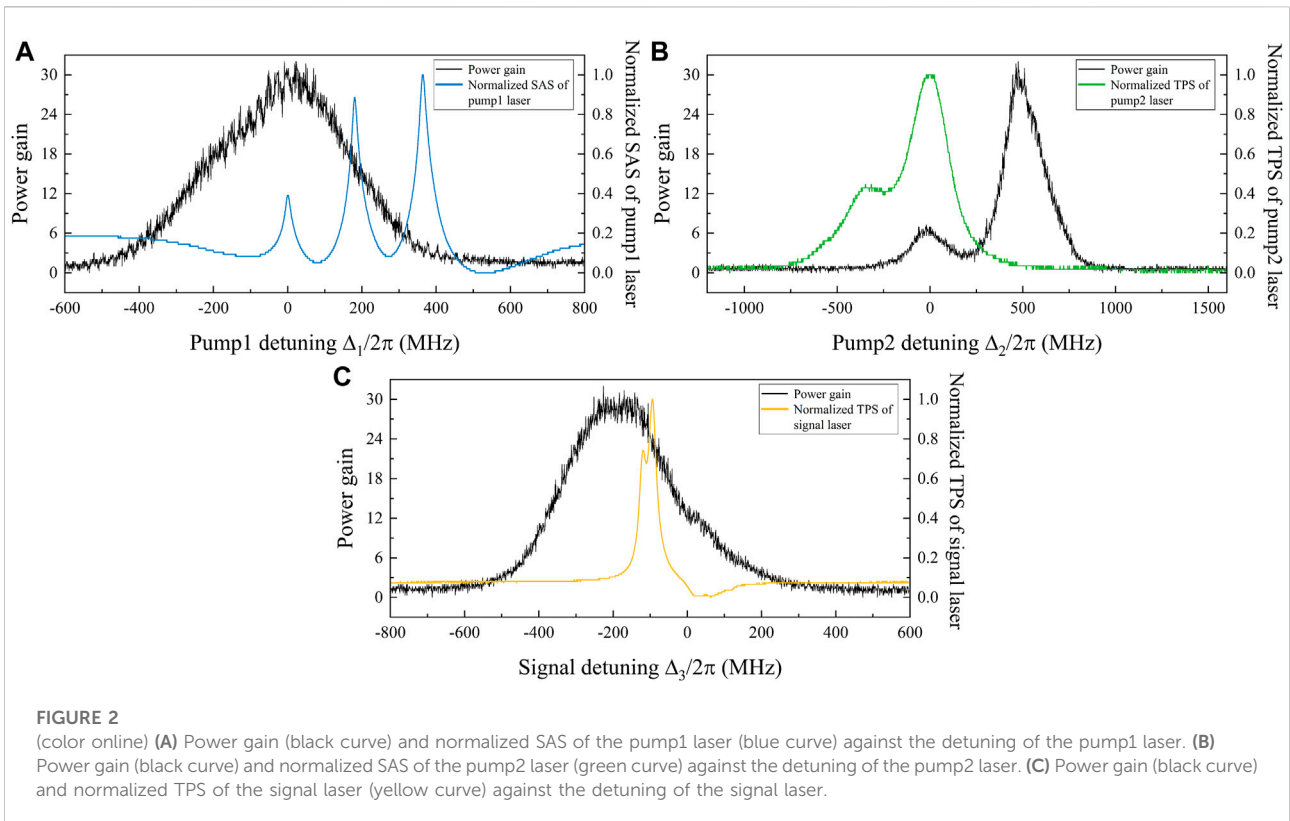
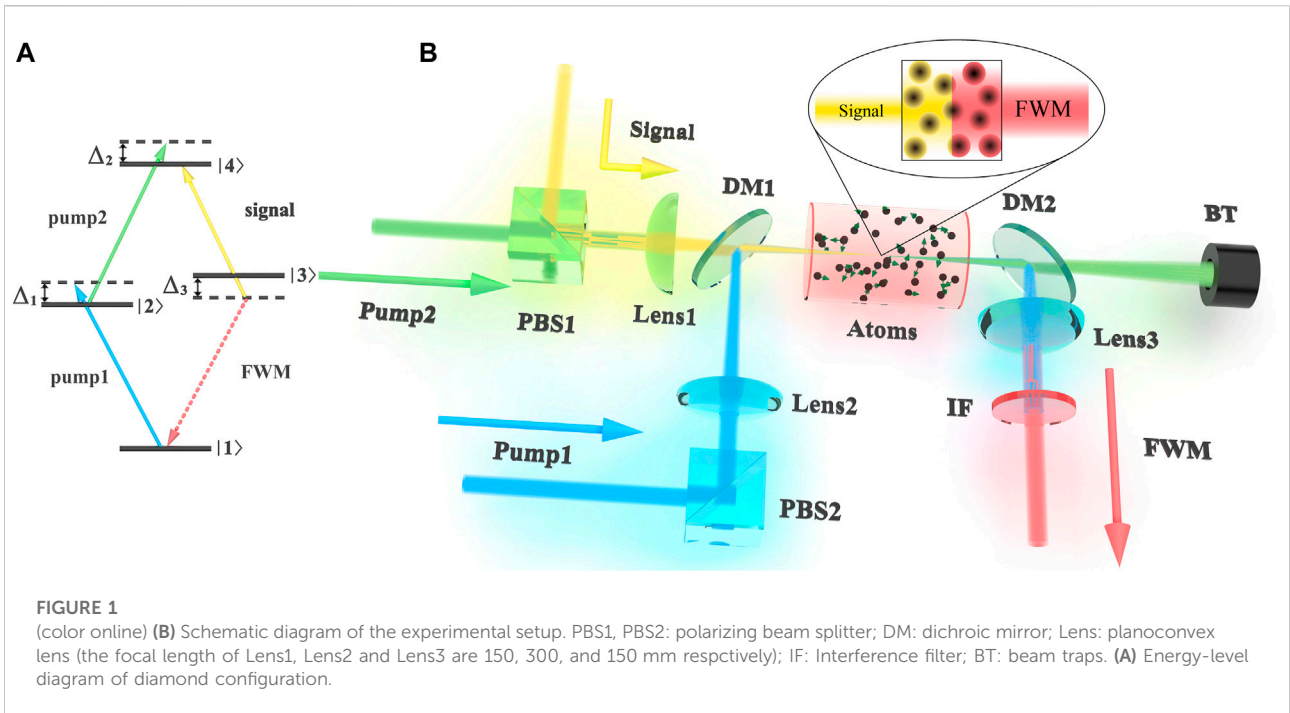
The stimulated FWM process with a four-level atomic system is an extensively researched topic in a double-ladder or diamond configuration. This phenomenon requires the interaction of three optical fields with the atoms in which two strong fields excite the atoms to a higher excited state (such as 5D or 4D state in rubidium atomic system) and a weak seed (driving) field induces the atoms to generate a strong FWM field. This process is also referred to as seeded FWM in some works (Zhang et al., 2020b). To date, the stimulated FWM process in a ladder-type atomic system has been studied to investigate the effects of atomic coherence on the FWM spectrum (Lee and Moon, 2016) or the relationship between three-photon electromagnetically induced absorption and FWM (Lee and Moon, 2017b). The biphoton spectral wave form of photon pairs emitted from a cascade-type atomic ensemble also can be measured by using the stimulated FWM process (Jeong et al., 2019). Recently, the amplified spontaneous emission induced self-stimulated FWM process and the stimulated FWM process have been exploited in the diamond-type atomic system (Zhang et al., 2020b), and the stimulated nondegenerate FWM phenomenon without amplified spontaneous emission has been realized in cesium atoms with a power of the generated FWM light up to 1.2 mW (Wu et al., 2022). The stimulated FWM process has also been investigated in rubidium atoms via Rydberg states (Kölle et al., 2012). To put it briefly, the stimulated FWM is generally utilized to explore precision spectroscopic measurements, atomic coherence, and efficient generation of FWM light.

In this paper, we report on an experimental exploration of the stimulated FWM process in a diamond-type ^{85}Rb atomic ensemble. Realizing the amplified detection of the infrared laser by converting the weak infrared signal light into the strong visible FWM light. In this work, the atoms are excited and populated in the upper state by inputting two strong pump lasers and we make an infrared beam as a seed light to induce atoms to efficiently generate the FWM light. Specifically, we find that we can achieve the purpose of amplifying and detecting the infrared signal by detecting the strong visible FWM signal which is induced by this infrared signal. In addition, in order to investigate the response properties of the amplifier, we compare the waveforms between the input signal and the output signal for various rising edge cases.

2 Experimental setup

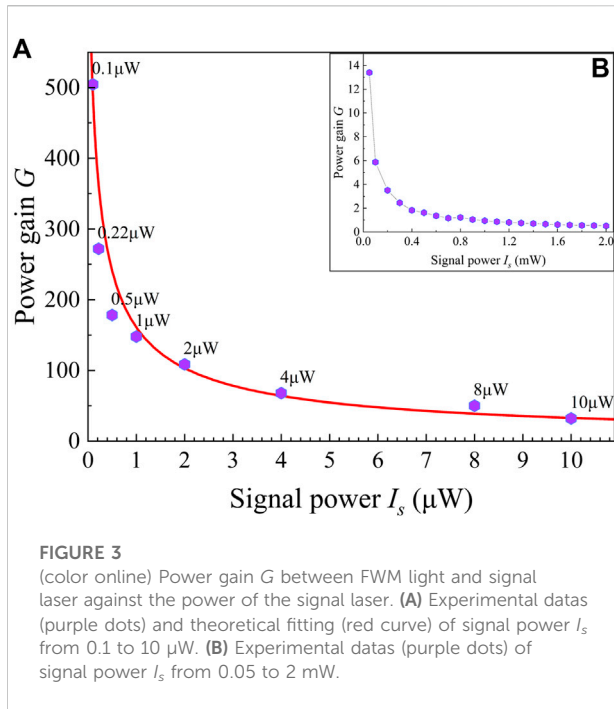
We experimentally realized the amplified detection of infrared signal through a stimulated FWM process in hot ^{85}Rb atomic vapor with a four-levels diamond configuration as shown in Figure 1A. It consists of one ground state $|1\rangle$ ($5S_{1/2}(F=2)$), one excited state $|4\rangle$ ($4D_{3/2}(F''=3)$), and two intermediate states $|2\rangle$ and $|3\rangle$ ($5P_{1/2}(F'=2)$ and $5P_{3/2}(F'=3)$). The pump1 (795 nm) and pump2 (1,475 nm) lasers excite the atoms from $|1\rangle$ to $|2\rangle$ and $|2\rangle$ to $|4\rangle$ respectively, then the atoms decay into the ground state $|1\rangle$ through the intermediate state $|3\rangle$. Since the difference between the spontaneous decay rates (Γ_{43}) from $|4\rangle$ to $|3\rangle$ and the spontaneous decay rates (Γ_{31}) from $|3\rangle$ to $|1\rangle$ satisfies the relation $\Gamma_{43} = 0.1\Gamma_{31}$, the populations of $|4\rangle$ and $|3\rangle$ are not significantly inversed and the FWM process cannot occur obviously in the absence of the signal laser (Zhang et al., 2020b). So that we input the signal (1,530 nm) laser which interacts with the $|3\rangle - |4\rangle$ transition to induce the FWM, and the FWM (780 nm) light can be generated strongly in the transition from $|3\rangle$ to $|1\rangle$ under the phase-matching condition of wave-vector conservation and energy conservation. Through this stimulated FWM process, a weak signal laser can be converted into a strong FWM light to achieve the amplification of the infrared signal laser. The detuning frequencies of the pump1, pump2, and signal lasers correspond to Δ_1 , Δ_2 and Δ_3 respectively.

The experimental setup is schematically depicted in Figure 1B, where pump 1, pump2 and signal lasers are continuous waves (CW) and overlap in a 5-cm-long ^{85}Rb cell that is heated to 140°C. The horizontally polarized pump2 beam and vertically polarized signal beam are focused into the center of the cell with the same diameter of 126 μm . The vertically polarized pump1 beam is superimposed with the pump2 beam and the signal beam through a dichromatic mirror (DM1), and has a diameter of



141 μm in the focal spot. The strong pump2 laser and signal laser are filtered out by the DM2, and the pump1 laser is blocked by a subsequent interference filter (IF). A

photomultiplier tube (PMT) with an adjustable attenuation collects the generated FWM light in the direction which is colinear with the pump1 laser in our system.



3 Experimental results and theoretical analysis

A critical metric to characterize the performance of our system is the power gain ($G = I_F/I_s$) defined as the ratio of the FWM light power (I_F) and the signal laser power (I_s). **Figure 2** shows the variation of the power gain (three black curves) with the detuning frequencies of pump1, pump2, and signal lasers (Δ_1 , Δ_2 and Δ_3), where the powers of the signal, pump1 and pump2 lasers are 10 μW , 110 and 110 mW respectively. In **Figure 2A**, the power gain are measured when we scan the detuning frequency of pump1 Δ_1 laser and the detuning frequency of pump2 Δ_2 (signal Δ_3) laser is fixed at $475 \times 2\pi$ MHz ($-190, \times, 2\pi$ MHz). The maximum power gain approaches 30 when the Δ_1 is equal to 0, $\times, 2\pi$ MHz, and the blue curve is the saturated absorption spectrum (SAS) of the pump1 field. We can find that the power gain has two peaks when the pump1 laser is resonant with the $|1\rangle - |2\rangle$ transition and the frequency of the signal laser is satisfied with $\Delta_3 = -190, \times, 2\pi$ MHz, as shown in **Figure 2B**. It is due to another two peaks which are corresponded to the transitions of $5S_{1/2}(F=2) - 5P_{1/2}(F'=3) - 4D_{3/2}(F''=3)$ and $5S_{1/2}(F=2) - 5P_{1/2}(F'=2) - 4D_{3/2}(F''=3)$ in the normalized two photons spectrum (TPS) of pump2 laser (green curve) and the maximum power gain occurs at the condition of $\Delta_2 = 475 \times 2\pi$ MHz. **Figure 2C** displays the power gain and the normalized TPS of the signal laser (yellow curve) when we scan the Δ_3 of the signal laser under the conditions of $\Delta_1 = 0, \times, 2\pi$ MHz and $\Delta_2 = 475 \times 2\pi$ MHz. It is obvious from **Figure 2** that the single-photon detunings of pump and signal fields significantly affect the value

of the power gain. The maximum point of the power gain reaches 30 when the Δ_1 , Δ_2 , and Δ_3 are fixed at 0, $\times, 2\pi$ MHz, $475 \times 2\pi$ MHz, and $-190, \times, 2\pi$ MHz respectively.

In **Figure 3**, we plot the power gain as a function of the signal power I_s under the optimal experimental conditions we mentioned above, and the power is measured with a power meter instead of the PMT. Due to the strong pump1 and pump2 lasers, the atoms are mostly populated at the state $|4\rangle$ via two-photon excitation. Meanwhile, the weak signal laser is converted and amplified into a strong FWM light. We can fetch the information from **Figure 3** that the power gain increases rapidly with the decrease of the signal power. **Figure 3A** indicates that the power gain exceeds 100 when the power of the signal laser is less than 2 μW , and the power gain can be reached up to 500 in the case of $I_s = 0.1 \mu\text{W}$. The amplification effect exhibits a tendency to saturation when the signal power intensity is beyond 1 mW, which is illustrated in **Figure 3B**. We also can define the photon-number gain (or detection gain) G_{photon} in this amplification process as the ratio of the number of output visible photons to the number of input infrared photons. Considering that the energy of a photon is inversely proportional to its wavelength, we can obtain the relationship $G_{\text{photon}} = 0.5G$ between photon-number gain and power gain. Similarly, the photon-number gain can reach 250 at the case of $I_s = 0.1 \mu\text{W}$ according to **Figure 3B**, which means that the number of photons detected by a detector is increased from 1 to 250.

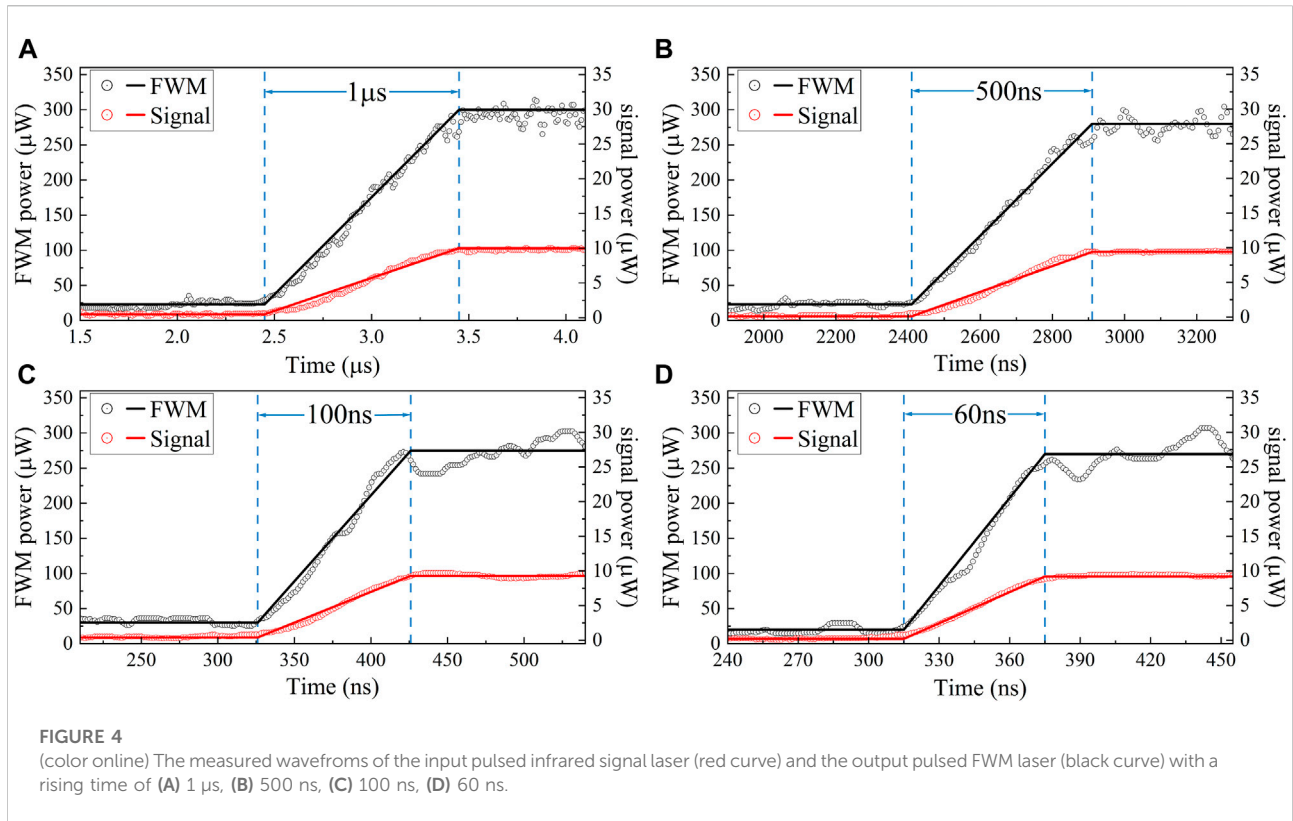
To explain the amplification of signal laser in the stimulated FWM process, we theoretically calculate the relation between power gain and signal power in an atomic diamond-type energy-level system. The equation of motion can be described as (Boyd, 2003).

$$\frac{\partial \rho_{ij}}{\partial t} = -\frac{i}{\hbar} \sum_k [H_{ik} \rho_{kj} - \rho_{ik} H_{kj}] - \Gamma_{ij} \rho_{ij} - \gamma_{ij} \rho_{ij} \quad (1)$$

where ρ_{ij} is the density-matrix element and H_{ij} is the effective interaction Hamiltonian. The subscript indices i and j indicate the $|i\rangle$ and $|j\rangle$ states respectively. Γ_{ij} denotes the population spontaneous relaxation rate from state $|i\rangle$ to state $|j\rangle$ while $\gamma_{ij} = (\Gamma_{ii} + \Gamma_{jj})/2$ denotes the relaxation rates of the coherences. For ^{85}Rb , the spontaneous decay rates are $\Gamma_{33} = 6 \times 2\pi$ MHz, $\Gamma_{22} = \Gamma_{33}$, $\Gamma_{44} = 0.35\Gamma_{33}$, $\Gamma_{43} = 0.1\Gamma_{33}$, and $\Gamma_{42} = 0.25\Gamma_{33}$. The matrix of the effective interaction Hamiltonian \hat{H} can be represented as

$$\hat{H} = \frac{\hbar}{2} \begin{pmatrix} 0 & \Omega_{21}^* & 0 & 0 \\ \Omega_{21} & -2\Delta_1 & 0 & \Omega_{42}^* \\ 0 & 0 & 2(\Delta_3 - \Delta_2 - \Delta_1) & \Omega_{43}^* \\ 0 & \Omega_{42} & \Omega_{43} & -2(\Delta_1 + \Delta_2) \end{pmatrix} \quad (2)$$

where Ω_{21} , Ω_{42} and Ω_{43} are the Rabi frequency of pump1, pump2, and signal laser respectively. We can then deduce the steady-state optical coherence ρ_{13} from Eqs 1, 2 as (Sun et al., 2004):



$$\rho_{31} = -\frac{i\Omega_{21}\Omega_{42}\Omega_{43}^*}{[2i(\Delta_1 - \gamma_{21})][2i(\Delta_1 + \Delta_2) - \gamma_{41}][2i(\Delta_1 + \Delta_2 - \Delta_3) - \gamma_{31}]} \quad (3)$$

The amplitude of the FWM light wave E_{FWM} is proportional to the third-order optical polarization $P_{FWM}^{(3)}$ (Parniak and Wasilewski, 2015):

$$E_{FWM} \propto P_{FWM}^{(3)} = N\mu_{31}^*\rho_{31} + \text{H.c.} \quad (4)$$

where N is the number density of atoms and μ_{31}^* is the transition dipole moment between states $|1\rangle$ and $|3\rangle$. In our system, the third-order optical polarization can be represented as $E_{FWM} \propto P_{FWM}^{(3)} = \epsilon_0\chi^{(3)}E_{p1}E_{p2}E_s^*$, where $\chi^{(3)}$ denotes the third-order susceptibility; ϵ_0 is the vacuum permittivity; E_{p1} , E_{p2} and E_s are amplitudes of the pump1, pump2 and the signal electric fields, respectively. We can obtain the power conversion efficiency $\eta \propto E_{FWM}^2/E_s^2$ between signal light and FWM light by calculating $\chi^{(3)}$.

Considering the stimulated amplified process of signal light, we treat the state $|3\rangle$ and the state $|4\rangle$ equivalents as a simple two-level atomic system for the signal field. The stimulated emission from the interaction between this two-level atomic system and signal field can enhance the input signal light with a gain factor of $G_{factor} = I_{sout}/I_s$ (I_{sout} is the power of the amplified signal light), and G_{factor} is satisfied by the following equation which is described in references (Riehle, 2004; Pan et al., 2018):

$$I_s(G_{factor} - 1) + 2A \ln G_{factor} = \frac{1}{2}B. \quad (5)$$

with $A = \pi\omega_s^2 I_{sat} \frac{\Delta_s^2 + \Gamma_{43}^2}{\Gamma_{43}}$ and $B = \alpha N\pi\omega_s^2 h\nu L$, where ω_s is the waist of signal light, ν is the frequency of the signal light at 1530nm, L is the length of the ^{85}Rb vapor cell, $I_{sat} = \pi h c \Gamma_{43} / (3\lambda^3)$ is the saturation intensity, and $\alpha = 1/\tau_{cyc}$ represents the pumping rate with $\tau_{cyc} = \frac{1}{\Omega_{43}} + \frac{1}{\Gamma_{43}} + \frac{1}{\Gamma_{31}}$ being the atomic cycling time (Zhang et al., 2013). We obtain the power gain

$$G = \eta G_{factor} \quad (6)$$

by considering that the stimulated FWM process consists of an amplification process and a frequency conversion process, where η is a constant and G_{factor} is a function of I_s . We then fit our experimental data with the deduced function and the result is shown in Figure 3A. The theoretical analysis agrees with our experimental results.

Finally, for amplified detection of an infrared signal, we should also pay attention to the response rate in this conversion process. As illustrated in Figure 4, we replace the CW signal laser with a pulsed signal laser. Figures 4A–D compare the signal pulse with the generated FWM pulse at a rising time of 1 μ s, 500 ns and 60 ns, respectively. It can be concluded that the rising time of the input signal light and output FWM light are almost identical and the response time of this conversion process is faster than 60 ns. The study of higher response rate is mainly restricted by the shortest achievable rising time of the acoustic optical modulator (AOM) in our setup, which is 55 ns.

4 Conclusion

In conclusion, we have demonstrated the amplified detection of an infrared signal via a stimulated FWM process based on an atomic diamond-type configuration. What's more, the generated FWM light is in the visible range, which can be detected more efficiently. We find that the power gain increases sharply as the power of the signal laser decreases, and the experimental data is in good agreement with our theoretical fitting. We also investigate the dependence of power gain on the detunings of the three input lasers. Simultaneously, we experimentally confirm that the response rate of the FWM process is faster than 60 ns, therefore it can be applied to the detection of the weak infrared signals in specific situations.

Data availability statement

The raw data supporting the conclusion of this article will be made available by the authors, without undue reservation.

Author contributions

D-SD and B-SS coordinated the research project. W-HZ performed the experimental fabrication, measurements and analyzed the data. All authors discussed the manuscript.

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Conflict of interest

The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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