



A Stomatal Model of Anatomical Tradeoffs Between Gas Exchange and Pathogen Colonization

Christopher D. Muir*

School of Life Sciences, University of Hawai'i, Honolulu, HI, United States

Stomatal pores control leaf gas exchange and are one route for infection of internal plant tissues by many foliar pathogens, setting up the potential for tradeoffs between photosynthesis and pathogen colonization. Anatomical shifts to lower stomatal density and/or size may also limit pathogen colonization, but such developmental changes could permanently reduce the gas exchange capacity for the life of the leaf. I developed and analyzed a spatially explicit model of pathogen colonization on the leaf as a function of stomatal size and density, anatomical traits which partially determine maximum rates of gas exchange. The model predicts greater stomatal size or density increases the probability of colonization, but the effect is most pronounced when the fraction of leaf surface covered by stomata is low. I also derived scaling relationships between stomatal size and density that preserves a given probability of colonization. These scaling relationships set up a potential anatomical conflict between limiting pathogen colonization and minimizing the fraction of leaf surface covered by stomata. Although a connection between gas exchange and pathogen defense has been suggested empirically, this is the first mathematical model connecting gas exchange and pathogen defense via stomatal anatomy. A limitation of the model is that it does not include variation in innate immunity and stomatal closure in response to pathogens. Nevertheless, the model makes predictions that can be tested with experiments and may explain variation in stomatal size and density among plants. The model is generalizable to many types of pathogens, but lacks significant biological realism that may be needed for precise predictions.

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*Correspondence:

Christopher D. Muir
cdmuir@hawaii.edu

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INTRODUCTION

Stomata evolved to regulate gas exchange in and out of the leaf (Hetherington and Woodward, 2003; Berry et al., 2010; Chater et al., 2017), but many foliar pathogens take advantage of these chinks in the leaf cuticular armor to infect prospective hosts (Zeng et al., 2010; McLachlan et al., 2014; Melotto et al., 2017). The stomatal and mesophyll conductance to CO₂ are two major limits to photosynthesis (Flexas et al., 2018; Lawson et al., 2018) that are partially determined by stomatal anatomy. Since CO₂ conductance limits photosynthesis (Farquhar and Sharkey, 1982; Jones, 1985) and pathogen infection can reduce fitness (Gilbert, 2002), this sets up a potential tradeoff between increased photosynthesis and defense against pathogens mediated by stomatal anatomy (McKown et al., 2014; Dutton et al., 2019; Fetter et al., 2019; Tateda et al., 2019). For example, plants could increase photosynthetic rate by developing more stomata, but more stomata could result in more

pathogen colonization. The optimal stomatal density, size, and arrangement on the leaf will depend on the fitness gains from increased gas exchange and fitness losses imposed by foliar pathogens, both of which depend on the environment. In the next two paragraphs I will review the relationship between stomatal anatomy, gas exchange, and foliar pathogen colonization. Then I will discuss why two anatomical traits, stomatal size and density, might be crucial components of a broader tradeoff between photosynthesis and pathogen defense.

The stomatal density and maximum pore area set an anatomical upper limit on stomatal conductance (Brown and Escombe, 1900; Parlange and Waggoner, 1970; Franks and Farquhar, 2001; Franks and Beerling, 2009b; Lehmann and Or, 2015; Sack and Buckley, 2016; Harrison et al., 2019), but stomatal shape, distribution, and patterning also affect gas exchange. Smaller guard cells and dumbbell-shaped stomata of grasses can respond faster to environmental changes (Drake et al., 2013), but responsiveness is further modulated by subsidiary cell anatomy and physiology (Franks and Farquhar, 2007; Raissig et al., 2017; Gray et al., 2020). Stomatal clustering reduces gas exchange and photosynthesis because adjacent stomata interfere with one another (Dow et al., 2014b), diffusion shells overlap (Lehmann and Or, 2015), and limitations on lateral diffusion of CO₂ in the mesophyll (Lawson and Blatt, 2014 and references therein). However, sparse clusters of small stomata could allow a leaf with low rates of gas exchange to have faster stomatal response compared to a leaf with large, low-density stomata (Papanatsiou et al., 2017). Leaves with stomata on both lower and upper surfaces (amphistomatous) supply more CO₂ to the mesophyll than hypostomatous leaves that only have stomata on the lower surface (Parkhurst, 1978; Gutschick, 1984; Parkhurst and Mott, 1990; Oguchi et al., 2018). In addition to anatomy, the pore area shrinks and expands in response to internal and external factors to regulate gas exchange dynamically (Buckley, 2019). For example, stomata typically open during the day and close at night in C₃/C₄ plants, but the opposite is true for CAM plants. Shade, high vapor pressure deficits, dry soil and other factors can cause stomata to (partially) close even in the middle of the day. Variation in how stomata respond to internal and external signals may explain as much of the variation in gas exchange across leaves as anatomy (Lawson and Blatt, 2014).

Many types of foliar pathogens, including viruses (Murray et al., 2016), bacteria (Melotto et al., 2006; Underwood et al., 2007), protists (Fawke et al., 2015), and fungi (Hoch et al., 1987; Zeng et al., 2010) use stomatal pores to gain entry into the leaf. For example, rust fungi hyphae recognize the angle at which guard cells project from the leaf surface and use it as a cue for appressorium formation (Allen et al., 1991). Oomycete pathogens can target open stomata on a leaf (Kiefer et al., 2002). Plants can limit colonization through innate immunity, called stomatal defense (recently reviewed in Melotto et al., 2017), by closing stomata after they recognize microbe-associated molecular patterns (MAMPs) on pathogen cells. Some bacterial pathogens have responded by evolving the ability to prevent stomatal closure, increasing their colonization of the leaf interior (Melotto et al., 2006). In addition to stomatal closure, anatomical changes in stomatal density and/or size might

provide another layer of defense against pathogen colonization. For example, infection increases in leaves with higher stomatal density (McKown et al., 2014; Dutton et al., 2019; Fetter et al., 2019; Tateda et al., 2019). The positive effect of stomatal density on infection suggests that infection is limited by the number or size of locations for colonization, meaning that many individual pathogens must usually be unable to find stomata or other suitable locations for colonization. This is actually somewhat surprising given the ability of some pathogens to search for and sense stomata (see above).

Stomatal anatomy could be a key link between gas exchange and pathogen colonization. Although many anatomical factors and stomatal movement affect gas exchange (see above), here I focus on the density and size of stomata in a hypostomatous leaf. Stomatal size refers to both the area of guard cells when fully open, from which one can calculate the pore area for gas exchange (see Model). For simplicity, I model a hypostomatous leaf, but consider the implications for amphistomatous leaves in the Discussion. Stomatal size and density not only determine the theoretical maximum stomatal conductance ($g_{s,max}$), but are also proportional to the operational stomatal conductance ($g_{s,op}$) in many circumstances (Franks et al., 2009, 2014; Dow et al., 2014a; McElwain et al., 2016; Murray et al., 2019). $g_{s,op}$ is the actual stomatal conductance of plants in the field and is almost always below $g_{s,max}$ because stomata are usually not fully open. Although they are not the same, the strong empirical relationship between $g_{s,max}$ and $g_{s,op}$ means that anatomical $g_{s,max}$ can be used as a proxy for $g_{s,op}$ without explicitly modeling dynamic changes in stomatal aperture (see Discussion). Stomatal size and density have also been measured on many more species than stomatal responsiveness, which may make it easier to test predictions.

After a pathogen reaches a host, it must survive on the leaf surface and colonize the interior (Beattie and Lindow, 1995; Tucker and Talbot, 2001). For analytical tractability, I restrict the focus here to colonization by a pathogen using a random search on a leaf without stomatal defense (i.e., a leaf that cannot recognize pathogens and close stomata). Obviously, these simplifications ignore a lot of important plant-pathogen interaction biology. In the Discussion, I delve further into these limitations and suggest future work to overcome these limitations. In order for pathogen-mediated selection on stomatal anatomy, I assume that the pathogen reduces host fitness once it colonizes (Gilbert, 2002). Susceptible hosts can lose much of their biomass or die, but even resistant hosts must allocate resources to defense or reduce photosynthesis because of defoliation, biotrophy, or necrosis around sites of infection (Bastiaans, 1991; Mitchell, 2003).

The purpose of this study is to develop a theoretical framework to test whether variation in stomatal size and density arises from a tradeoff between gas exchange and pathogen colonization. Since stomatal size and density affect both gas exchange and pathogen colonization, selection to balance these competing demands could shape stomatal size-density scaling relationships. Botanists have long recognized that stomatal size and density are inversely correlated (Weiss, 1865; Tichá, 1982; Hetherington and Woodward, 2003; Sack et al., 2003; Franks and Beerling, 2009a; Brodribb et al., 2013; Boer et al., 2016),

but the evolutionary origin of this relationship is not yet known. Here I argue that deleterious effects of pathogen infection could shape selection on this relationship. Explanations for inverse size-density scaling are usually cast in terms of preserving $g_{s,max}$ and/or stomatal cover (f_s), defined as the fraction of epidermal area allocated to stomata (Boer et al., 2016), because there are many combinations of stomatal size and density that have same $g_{s,max}$ or same f_s :

$$g_{s,max} = bmDS^{0.5} \quad (1)$$

$$f_s = DS. \quad (2)$$

D and S are stomatal density and size, respectively (see **Table 1** for a glossary of mathematical symbols and units). b and m are assumed to be biophysical and morphological constants, *sensu* (Sack and Buckley, 2016; see **Supplementary Material**). f_s is proportional to the more widely used stomatal pore area index (Sack et al., 2003; see **Supplementary Material**). If size and density also affect pathogen colonization, then selection from foliar pathogens could significantly alter the size-density scaling relationship. The empirical size-density scaling relationship is linear on a log-log scale, determined by an intercept α and slope β :

$$D = e^\alpha S^{-\beta}; \quad (3)$$

$$d = \alpha - \beta S. \quad (4)$$

For brevity, $d = \log(D)$ and $s = \log(S)$. Rearranging Equations 1 and 2, a scaling relationship where $\beta = 0.5$ preserves $g_{s,max}$ while $\beta = 1$ preserves f_s .

TABLE 1 | Glossary of mathematical symbols.

Symbol	R	Units	Description
D	D	mm^{-2}	Stomatal density
d	d	mm^{-2}	Stomatal density (log-scale, $d = \log D$)
f_s	f_s	none	Stomatal cover ($f_s = DS$)
$g_{s,max}$	g_smax	$\text{mol m}^{-2} \text{s}^{-1}$	Theoretical maximum stomatal conductance
$g_{s,op}$	g_sop	$\text{mol m}^{-2} \text{s}^{-1}$	Operational stomatal conductance
H	H	μm^{-1}	Death rate of pathogen on leaf surface
R	R	μm	Stomatal radius ($S = \pi R^2$)
S	S	μm^2	Stomatal size
s	s	μm^2	Stomatal size (log-scale, $s = \log S$)
θ_i	theta_i	radians	Angles between pathogen (x_p, y_p) and lines tangent to the circumference of stomate i
U	U	μm	Interstomatal distance
v_i	v_i	μm	Distance between pathogen (x_p, y_p) and stomate i
x_i, y_i	x_i, y_i	μm	Position of stomate i
x_p, y_p	x_p, y_p	μm	Starting position of pathogen

The columns indicate the mathematical symbol used in the paper, the associated symbol used in R scripts, scientific Units, and a verbal description.

How would adding pathogens alter these predicted scaling relationships? For simplicity, consider two environments, one without foliar pathogens and one with lots. In the absence of foliar pathogens, we expect size-density scaling to preserve $g_{s,max}$, f_s , or some least-cost combination of them. What happens when we introduce pathogens? If stomatal size and density increase pathogen colonization, then selection will favor reduced size and/or density. This would change the intercept α but not the slope. The effect of foliar pathogens on the slope depends on the relationship between size, density, and probability of colonization. If the probability of colonization is proportional to the product of linear stomatal size ($S^{0.5}$) and density ($\propto DS^{0.5}$ as for $g_{s,max}$) then it has the same effect on the slope as $g_{s,max}$ because there are many combinations of D and $S^{0.5}$ that have same probability of colonization. If the probability of colonization is proportional to the product of areal stomatal size (S) and density ($\propto DS$ as for f_s) then it has the same effect on the slope as f_s because there are many combinations of D and S that have same probability of colonization. Alternatively, the probability of colonization may have a different scaling relationship (neither 0.5 nor 1) or may be non-linear on a log-log scale. Unlike $g_{s,max}$ and f_s , we do not have theory to predict a stomatal size-density relationship that preserves the probability of colonization.

In summary, the physical relationship between stomatal size, density, and conductance is well-established (Harrison et al., 2019). Size and density also likely affect the probability of pathogen colonization, but we do not have a theoretical model that makes quantitative predictions. The inverse stomatal size-density relationship has usually been explained in terms of preserving stomatal conductance and/or stomatal cover, but selection by pathogens might alter scaling. To address these gaps, the goals of this study are to (1) introduce a spatially explicit model pathogen colonization on the leaf surface; (2) use the model to predict the relationship between $g_{s,max}$, f_s , and the probability of colonization; (3) work out what these relationships predict about stomatal size-density scaling. I analyzed an idealized, spatially explicit Model of how a pathogen lands on a leaf and finds a stomate to colonize the leaf using a random search. To my knowledge, this is the first model that makes quantitative predictions about the relationship between stomatal anatomy, the probability of colonization, and their impact on stomatal size-density scaling.

MODEL

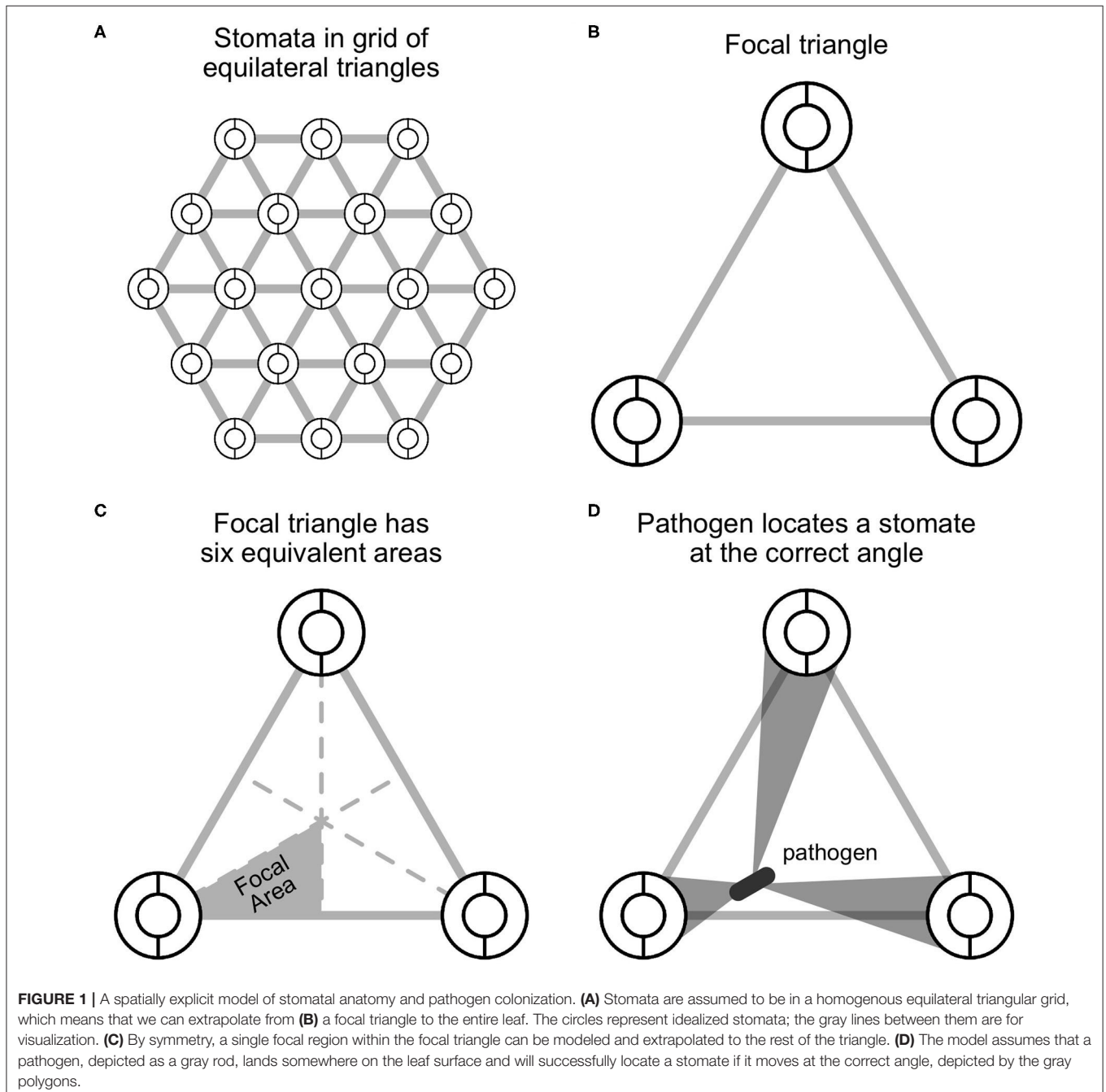
For generality, I refer to a generic “pathogen” that lands on leaf and moves to a stomate. The model is agnostic to the type of pathogen (virus, bacterium, fungus, etc.) and the specific biological details of how it moves. For example, motile bacterial cells can land and move around (Beattie and Lindow, 1995) whereas fungi may germinate from a cyst and grow until they form an appressorium for infection (Tucker and Talbot, 2001). These very different tropic movements on the leaf are treated identically here. I do not model photosynthesis explicitly, but assume that stomatal conductance limits carbon fixation, even

though the relationship is non-linear. I used Sympy version 1.6.1 (Meurer et al., 2017) for symbolic derivations.

Spatial Representation of Stomata

Stomata develop relatively equal spacing to minimize resistance to lateral diffusion (Morison et al., 2005), allow space between stomata (Dow et al., 2014b), and prevent stomatal interference (Lehmann and Or, 2015). Here I assume that stomata are arrayed in an equilateral triangular grid with a density D and size (area) S on the abaxial surface only, since most leaves are hypostomatous

(Muir, 2015; but see Discussion). This assumption ignores veins, trichomes, and within-leaf variation in stomatal density. Stomata are therefore arrayed in an evenly spaced grid (**Figure 1A**). The interstomatal distance U , measured as the distance from the center of one stomata to the next, is the maximal diagonal of the hexagon in μm that forms an equal area boundary between neighboring stomata. The area of a hexagon is $A_{\text{hexagon}} = \frac{\sqrt{3}}{2} U^2$. By definition the stomatal density is the inverse of this area, such that $D = A_{\text{hexagon}}^{-1} = \frac{2}{\sqrt{3}} U^{-2}$. Therefore, interstomatal distance can be derived from the stomatal density as:



$$D = \frac{2}{\sqrt{3}} U^{-2}$$

$$U = \left(\frac{2}{\sqrt{3}} D^{-1} \right)^{0.5}$$

For example, if the density is $D = 10^2 \text{ mm}^{-2} = 10^{-4} \text{ } \mu\text{m}^{-2}$, then U is $107.5 \text{ } \mu\text{m}$. Parkhurst (1994) described this result previously. I also make the simplifying assumption that stomata are perfectly circular with radius R when fully open. This may be approximately true for fully open stomata with kidney-shaped guard cells (Sack and Buckley, 2016 and references therein). Although I assume stomata are circular here, in calculating $g_{s,\text{max}}$, I assume typical allometric relationships between length, width, and pore area (Sack and Buckley, 2016; see **Supplementary Material**).

Spatial Representation of Pathogen Search

Since stomata are arrayed in a homogeneous grid, we can focus on single focal triangle (**Figures 1B,C**). Suppose that an individual pathogen (e.g., bacterial cell or fungal spore) lands at a uniform random position within the focal triangle and must arrive at a stomate to colonize. If it lands on a stomate, then it infects the leaf with probability 1; if it lands between stomata, then it infects the leaf with probability p_{locate} . This is the probability that it locates a stomate, which I will derive below. The probabilities of landing on or between a stomate are f_S and $1 - f_S$, respectively. Hence, the total probability of

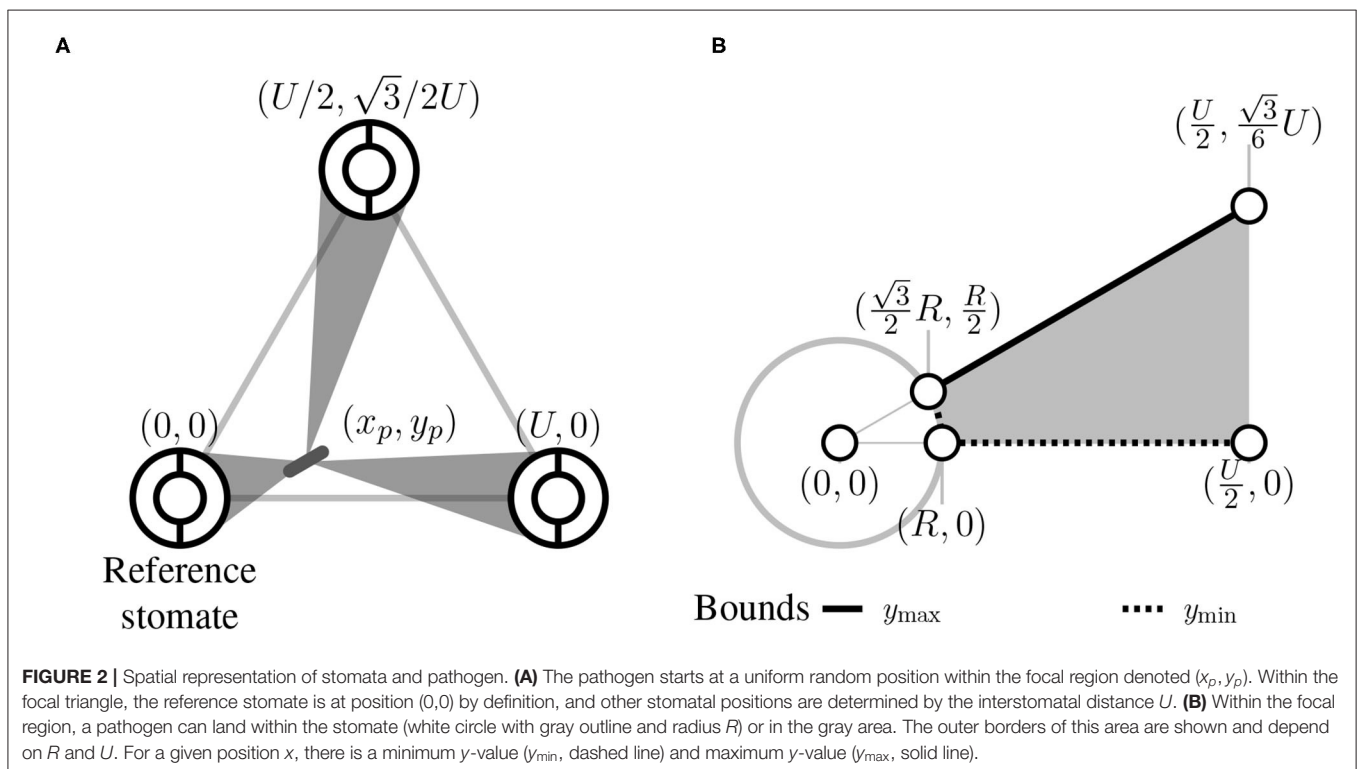
colonization is:

$$p_{\text{colonize}} = f_S + (1 - f_S)p_{\text{locate}}. \quad (5)$$

I assume that the pathogen cannot sense where stomata are and orients at random, thereafter traveling in that direction. If it successfully locates a stomate, it colonizes the leaf, but otherwise does not infect. If there is a high density of stomata and/or large stomata, the probability of locating a stomate increases. By assuming that stomata form an equilateral triangular grid (see above), we can extrapolate what happens in the focal triangle (**Figure 1B**) by symmetry. Further, since an equilateral triangle can be broken up into six identical units (**Figure 1C**), we can simply calculate p_{locate} in this focal area. This implicitly assumes that the probability of colonizing stomata outside the focal area is 0 because they are too far away. This assumption may be unrealistic for larger pathogens, such as fungi, whose hyphae can travel longer distances on the leaf surface (Brand and Gow, 2012). In **Appendix 1: Spatially Implicit Model** I derive a simpler, but spatially *implicit* model that relaxes the assumption the pathogens must colonize a stomate within their focal triangle.

Consider a pathogen that lands in position (x_p, y_p) within the triangle. The centroid of the triangle is at position (x_c, y_c) and a reference stomate is at position $(0, 0)$ (**Figure 2A**). Therefore $x_c = U/2$ and $y_c = \sqrt{3}U/6$. The other stomata are at positions $(U/2, \sqrt{3}U/2)$ and $(U, 0)$ (**Figure 2**). x_p and y_p are defined as the horizontal and vertical distances, respectively, from the pathogen to the reference stomate at position $(0, 0)$.

Given that the pathogen starts at position (x_p, y_p) , what's the probability of contacting one of the stomata at the vertices of the



focal triangle? I assume the probability of contacting a stomate is equal to the proportion of angular directions that lead to a stomate (**Figure 1D**). I solved this by finding the angles ($\theta_1, \theta_2, \theta_3$) between lines that are tangent to the outside of the three stomata and pass through (x_p, y_p) (**Figure 2A**). If stomate i is centered at (x_i, y_i) , the two slopes of tangency as function of pathogen position are:

$$t_{i,1}(x_p, y_p) = \frac{-Re_{i,2}(x_p, y_p) + e_{i,3}(x_p, y_p)}{e_{i,1}(x_p, y_p)} \quad (6)$$

$$t_{i,2}(x_p, y_p) = \frac{Re_{i,2}(x_p, y_p) + e_{i,3}(x_p, y_p)}{e_{i,1}(x_p, y_p)} \quad (7)$$

where

$$e_{i,1}(x_p, y_p) = (R^2 - x_i^2 + 2x_i x_p - x_p^2), \quad (8)$$

$$e_{i,2}(x_p, y_p) = \sqrt{-e_{i,1} + (y_i - y_p)^2}, \quad (9)$$

$$e_{i,3}(x_p, y_p) = -x_i y_i + x_i y_p + x_p y_i - x_p y_p. \quad (10)$$

Note that $i \in \{1, 2, 3\}$, indexing the three stomata in the focal triangle. The angle in radians between $t_{i,1}(x_p, y_p)$ and $t_{i,2}(x_p, y_p)$ is:

$$\theta_i(x_p, y_p) = \arctan\left(\frac{t_{i,1}(x_p, y_p) - t_{i,2}(x_p, y_p)}{1 + (t_{i,1}(x_p, y_p)t_{i,2}(x_p, y_p))}\right) \quad (11)$$

I further assumed that the longer distance a pathogen must travel, the less likely it would be to locate a stomate. For example, if stomata are at very low density, then a pathogen may die before it reaches a stomate because of UV, desiccation, or another factor. I included this effect by assuming the probability of reaching a stomate declines exponentially at rate H with the Euclidean distance $v_i(x_p, y_p)$ between the pathogen location and the edge of stomata i , which is distance R from its center at x_i, y_i :

$$v_i(x_p, y_p) = \sqrt{(x_i - x_p)^2 + (y_i - y_p)^2} - R. \quad (12)$$

The probability of locating a stomate as a function of pathogen position (x_p and y_p) is the sum of the angles divided by 2π , discounted by their distance from the stomate:

$$f_{\text{locate}}(x_p, y_p) = \frac{1}{2\pi} \sum_{i=1}^3 e^{-Hv_i(x_p, y_p)} \theta_i(x_p, y_p) \quad (13)$$

When there is no pathogen death ($H = 0$), p_{locate} is the fraction of angles that lead from (x_p, y_p) to a stomate. When $H > 0$, p_{locate} is proportional to this fraction, but less than it depending on stomatal density, size, and starting location of the pathogen.

To obtain the average p_{locate} , we must integrate $f_{\text{locate}}(x_p, y_p)$ over all possible starting positions (x_p, y_p) within the focal area. The focal area is a 30–60–90 triangle with vertices at the center of the reference stomate (0, 0), the midpoint of baseline ($U/2, 0$), and the centroid of the focal triangle ($U/2, \sqrt{3}/6U$) (**Figure 1C**). Colonization occurs with probability 1 if the pathogen lands in

the reference stomate, so we need to integrate the probability of colonization if it lands elsewhere. This region extends from the edge of the stomate, at $\sqrt{3}/2R$ to $U/2$ (**Figure 2B**). At any x , we integrate from the bottom of the focal area (y_{min}) to the top (y_{max}):

$$y_{\text{min}} = f(x) = \begin{cases} \sqrt{R^2 - x^2}, & \text{if } \frac{\sqrt{3}}{2}R < x < R \\ 0, & \text{if } R \leq x \leq \frac{U}{2} \end{cases} \quad (14)$$

$$y_{\text{max}} = f(x) = \frac{\sqrt{3}}{3}x \quad (15)$$

The integral is:

$$p_{\text{locate}} = \frac{1}{a_{\text{focal}}} \int_{\frac{\sqrt{3}}{2}R}^{U/2} \int_{y_{\text{min}}}^{y_{\text{max}}} f_{\text{locate}}(x, y) dx dy \quad (16)$$

a_{focal} is the area of the focal region depicted in gray in **Figure 2B**:

$$a_{\text{focal}} = \frac{U^2}{8\sqrt{3}} - \frac{\pi R^2}{12}$$

MATERIALS AND METHODS

The Model calculates a probability of host colonization (Equation 5) as a function of stomatal density, size, and position of a pathogen on the leaf. I solved p_{colonize} by importing symbolic derivations from Sympy into R with **reticulate** version 1.16 (Ushey et al., 2020) and used the `integrate2()` function in the **pracma** package version 2.2.9 (Borchers, 2019) for numerical integration. I used R version 4.0.2 (R Core Team, 2020) for all analyses and wrote the paper in **rmarkdown** version 2.3 (Xie et al., 2018; Allaire et al., 2020). Citations for additional R software packages are in **Appendix 2**. Source code is deposited on GitHub (<https://github.com/cdmuir/stomata-tradeoff>) and archived on Zenodo (<https://doi.org/10.5281/zenodo.4102283>).

What Is the Relationship Between Stomatal Size, Density, and Colonization?

I calculated p_{colonize} over a biologically plausible grid of stomatal size and density for hypostomatous species based on Boer et al. (2016). Stomatal density (D) ranges from 10^1 to $10^{3.5}$ mm^{-2} ; stomatal size (S) ranges from 10^1 to $10^{3.5}$ μm^2 . I only considered combinations of size and density where stomatal cover (f_s) was $< 1/3$, which is close to the upper limit in terrestrial plants (Boer et al., 2016). I crossed stomatal traits with three levels of $H \in \{0, 0.01, 0.1\}$. When $H = 0$, a pathogen persists indefinitely on the leaf surface. $H = 0.01$ and $H = 0.1$ correspond to low and high death rates, respectively. These values are not necessarily realistic, but illustrate qualitatively how a hostile environment on the leaf surface alters model predictions.

How Do Pathogens Alter Optimal Stomatal Size-Density Scaling?

The stomatal size-density scaling relationship can be explained in terms of preserving a constant stomatal conductance ($g_{s,\text{max}}$)

that is proportional to $DS^{0.5}$ when bm is constant (Equation 1). In other words, there are infinitely many combinations of D and $S^{0.5}$ with the same $g_{s,max}$. If $g_{s,max}$ is held constant at C_g , then the resulting size-density scaling relationship on a log-log scale is:

$$d = c_g - 0.5s$$

where lowercase variables are log-transformed equivalents of their uppercase counterparts (Table 1). The scaling exponent $\beta_g = 0.5$ preserves C_g .

Next, suppose there is a scaling exponent β_p that preserves $p_{colonize}$ for the product DS^{β_p} . If $\beta_p = 0.5$, then $p_{colonize}$ is always proportional to $g_{s,max}$. If $\beta_p > 0.5$, small, densely packed stomata would be more resistant to colonization (lower $p_{colonize}$) compared to larger, sparsely spaced stomata with the same $g_{s,max}$. If $\beta_p < 0.5$, small, densely packed stomata would be less defended (higher $p_{colonize}$) compared to larger, sparsely spaced stomata with the same $g_{s,max}$. I refer to the three outcomes ($\beta_p = 0.5$, $\beta_p < 0.5$, and $\beta_p > 0.5$) as iso-, hypo-, and hyper-conductance, respectively. I was unable to solve analytically for β_p , so I numerically calculated isoclines of $p_{colonize}$ over the grid of D and S values described in the preceding subsection. I numerically calculated the scaling relationships at a constant $p_{colonize} \in \{0.025, 0.1, 0.4\}$ for $H \in \{0, 0.01, 0.1\}$.

RESULTS

Non-linear Relationships Between Colonization, Stomatal Cover, and Conductance

The probability of colonization ($p_{colonize}$) is not simply proportional to stomatal cover (f_s). At low f_s , $p_{colonize}$ increases rapidly relative to f_s at first (Figure 3A). At higher f_s , $p_{colonize}$ increases linearly with f_s . When pathogens persist indefinitely ($H = 0$), any combination of stomatal size (S) and density (D) with the same f_s have the same effect on $p_{colonize}$. When $H > 0$, pathogens are less likely to land close enough to a stomate to infect before dying, so $p_{colonize}$ is closer to f_s (Figure 3A). The maximum $p_{colonize}$ under the range of parameters considered was ~ 0.6 when $H = 0$ and f_s is at its maximum value of $1/3$. When f_s is low, $p_{colonize}$ is also low. The relationship between $p_{colonize}$, f_s , and $g_{s,max}$ is qualitatively similar in the spatially implicit model, but the values for $p_{colonize}$ are substantially higher because pathogens can potentially colonize any stomate on the leaf rather than only those in the focal triangle (see Appendix 1: Spatially Implicit Model for more detail). Bear in mind that this is the probability for a single individual searching randomly; if enough individuals reach the leaf and/or they can actively find stomata, it's almost certain that at least some will colonize the leaf. However, reducing $p_{colonize}$ may help plants limit the damage since fewer total individual pathogens will colonize the leaf interior.

$p_{colonize}$ is not directly proportional to f_s because it depends on D and S in quantitatively different ways (Supplementary Figure 1). For the same f_s , leaves with greater D have higher $p_{colonize}$ (Figure 3A). Holding f_s constant,

leaves with lower D and higher S will have a greater distance (v_i) between a pathogen and its stomata. When $H > 0$, this extra distance leads more pathogens to die before they can find a stomate. However, this result is inconsistent with the spatially implicit model (Appendix 1) because S and D have identical effects on f_s .

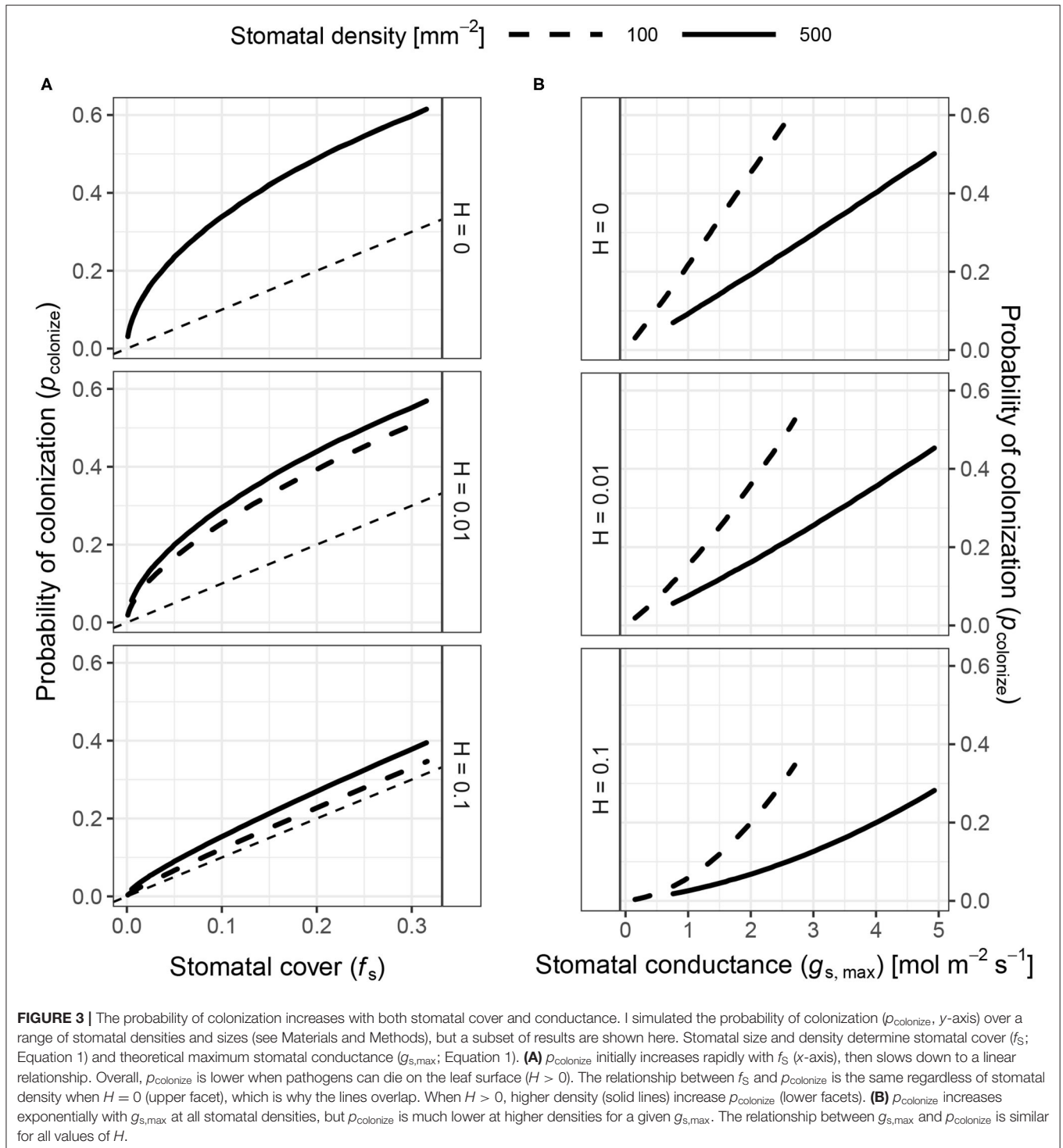
In contrast to f_s , $p_{colonize}$ increases at a greater than linear rate with stomatal conductance ($g_{s,max}$). Greater D (smaller S) is associated with lower $p_{colonize}$ for a given value of $g_{s,max}$ (Figure 3B). This happens because $p_{colonize}$ increases approximately linearly with S whereas $g_{s,max}$ is proportional to $S^{0.5}$. Therefore, $p_{colonize}$ increases exponentially with $g_{s,max}$ at all stomatal densities, but the rate of growth is lower at greater D for a given value of $g_{s,max}$.

Hyper-Conductance Size-Density Scaling

The scaling relationship between S and D that preserves $p_{colonize}$ is always >0.5 (hyper-conductance), but usually <1 . When $H = 0$, the scaling relationship is essentially 1 (Figure 4), which means that an increase f_s leads to a proportional increase in $p_{colonize}$. Because the scaling relationship is >0.5 , leaves with greater stomatal density will have lower $p_{colonize}$ than leaves lower stomatal density but the same $g_{s,max}$. In other words, increasing D and lowering S allows plants to reduce $p_{colonize}$ while maintaining $g_{s,max}$. The scaling relationship is slightly <1 , but still >0.5 , when $H > 0$ (Figure 4). In this area of parameter space, lower stomatal density can reduce f_s while $p_{colonize}$ is constant, but this will still result in lower $g_{s,max}$. In the spatially implicit model, the size-density scaling exponent was always exactly 1 except when $H = 0$ (Appendix 1).

DISCUSSION

Stomatal density and size set the upper limit on gas exchange in leaves (Harrison et al., 2019) and is often closely related to operational stomatal conductance in nature (Murray et al., 2019). Despite the fact that many foliar pathogens infect through stomata, the relationship between stomatal anatomy and resistance to foliar pathogens is less clear than it is for gas exchange. I used a spatially explicit model of a pathogen searching for a stomate to colonize a host. From this Model, I derived predictions about the relationship between stomatal anatomy and the probability of colonization, a component of disease resistance. The model predicts that the probability of colonization is not always proportional to the surface area of leaf covered by stomata (f_s), as one might intuitively predict. If the leaf surface is a hostile environment and pathogens have a limited time to search, lower stomatal density decreases the probability of colonization even if f_s is constant. However, $g_{s,max}$ decreases proportionally more than the probability of colonization. The model highlights the potential for conflicting demands of minimizing pathogen colonization, minimizing stomatal cover, and maintaining stomatal conductance. Including the effect of anatomy on pathogen colonization therefore has the potential to change our understanding of how stomatal size-density scaling evolves in land plants.



The model predicts that in most cases, increasing stomatal cover should lead to a proportional increase in colonization, which agrees with empirical studies (e.g., McKown et al., 2014; Dutton et al., 2019; Fetter et al., 2019; Tateda et al., 2019). It also makes new, testable predictions that are less intuitive (Table 2). At very low f_s , there is a rapid increase in

colonization (Figure 3A). If there are no stomata, the probability of colonization is 0, so the first few stomata dramatically increase the probability. This is less likely to be significant for abaxial (lower) leaf surfaces, which usually have most of the stomata (Salisbury, 1928; Metcalfe and Chalk, 1950; Mott et al., 1984; Peat and Fitter, 1994; Jordan et al., 2014; Muir, 2015; Bucher

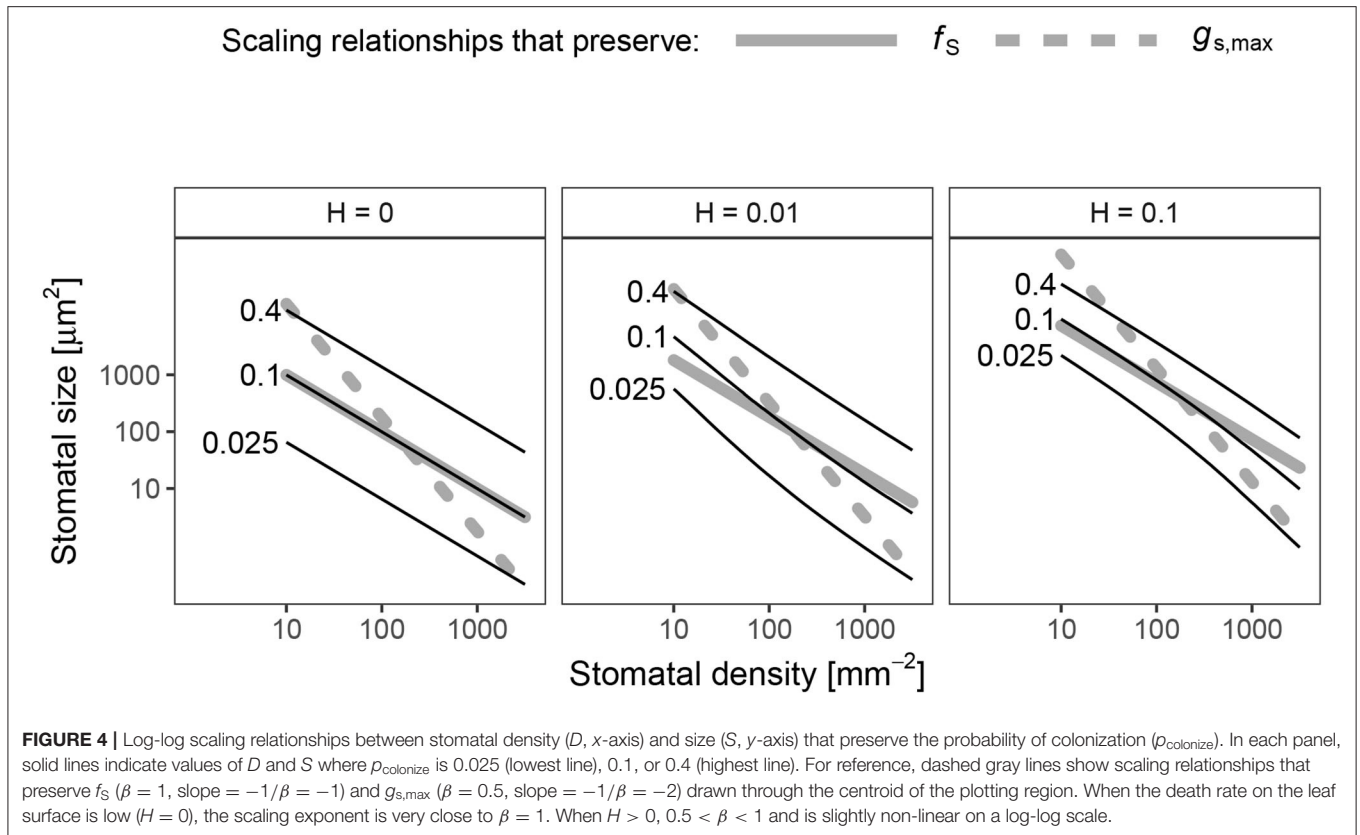


TABLE 2 | New testable model predictions and suggested experiments to test them.

Model prediction	How to test it
Increasing stomatal size and/or density will have a larger effect on pathogen colonization in leaves with low stomatal cover.	Compare the effect of changing stomatal size and/or density on pathogen colonization in leaves with low and high stomatal cover.
Increasing stomatal size and/or density will have a smaller effect on pathogen colonization in epiphytic environments more hostile to pathogens.	Compare the effect of changing stomatal size and/or density on pathogen colonization in more hostile environments (e.g., drier, higher light)
When selection against pathogen colonization is stronger, the stomatal size-density scaling exponent should be lower	Measure stomatal anatomy in environments that differ in pathogen colonization using comparative or experimental approaches

et al., 2017; Drake et al., 2019). However, many adaxial (upper) leaf surfaces have zero or very few stomata. Using adaxial leaf surfaces, it should be possible to test if small changes in stomatal size or density have a larger effect on pathogen colonization when f_S is low. Such experiments could use natural genetic variation (McKown et al., 2014) or mutant lines (Dow et al., 2014b). The non-linear increase in $p_{colonize}$ is less apparent when $H > 0$ (Figure 3A). A more hostile microenvironment (e.g., drier, higher UV) should therefore reduce the effect of increased size or density at low f_S . If true, the diminishing marginal effect

of f_S on colonization could explain why stomatal ratio on the upper and lower surface is bimodal (Muir, 2015). The initial cost of adaxial (upper) stomata is relatively high, but if the benefits outweigh the costs, then equal stomatal densities on each surface maximize CO_2 supply for photosynthesis (Parkhurst, 1978; Gutschick, 1984; Parkhurst and Mott, 1990). The costs and benefits will certainly vary with environmental conditions as well. Future work should extend this model, which considered hypostomatous leaves, to address stomatal size and density in amphistomatous leaves, since leaf surfaces may differ in the type of pathogens present and microenvironment (McKown et al., 2014; Fetter et al., 2019).

An effect of stomatal size and density on foliar pathogen colonization could change our understanding of stomatal size-density scaling. Since allocating leaf epidermis to stomata may be costly (Assmann and Zeiger, 1987; Franks and Farquhar, 2007; Dow et al., 2014b; Lehmann and Or, 2015; Baresch et al., 2019), selection should favor leaves that achieve a desired $g_{s,max}$ while minimizing f_S (Boer et al., 2016). Because of their different scaling exponents (Equation 1, 2), smaller, densely packed stomata can achieve the same $g_{s,max}$ at minimum f_S . However, many leaves have larger, sparsely packed stomata. Incorporating pathogen colonization may explain why. If pathogens have a limited time to find stomata before dying ($H > 0$), then the scaling exponent between size and density that keeps $p_{colonize}$ constant is between 0.5 and 1, the scaling exponents for $g_{s,max}$ and f_S , respectively (Figure 4). Greater density of smaller stomata can increase $g_{s,max}$ while keeping $p_{colonize}$ constant, but this will

increase f_s . Conversely, f_s could decrease while keeping p_{colonize} constant, but this will decrease $g_{s,\text{max}}$. This sets up the potential for conflict between competing goals. The optimal stomatal size and density will therefore depend on the precise costs and benefits of infection, stomatal conductance, and stomatal cover. This may explain why many leaves have large, sparsely packed stomata despite the fact that they could achieve the same $g_{s,\text{max}}$ and lower f_s with smaller, more densely packed stomata.

The model examines the probability of colonization for a single pathogen. The calculated probabilities of colonization should not be interpreted as exact predictions, but rather as depicting qualitative relationships between stomatal anatomy and infection severity. The energetic cost and lost photosynthetic capacity (closed stomata, necrosis, etc.) of dealing with a pathogen is assumed to be proportional to the amount of infection. The actual fitness cost will be modulated by the number of pathogens landing on the leaf and the cost of infection, all else being equal. In environments with fewer or less virulent pathogens, the fitness cost of infection will be less than in environments with more abundant, virulent pathogens. The model is less relevant to very susceptible host plants that can be severely damaged or killed by a small number of colonizations that spread unchecked throughout the host tissue.

CONCLUSION

The model makes two non-intuitive predictions. First, the effect of increased stomatal density or size on susceptibility to foliar pathogens is greatest when stomatal cover is very low. Second, maximizing disease resistance sets up a potential conflict between minimizing stomatal cover and maximizing stomatal conductance. The first prediction is consistent with results in *Populus trichocarpa* (McKown et al., 2014) and may be relatively straightforward to test experimentally with adaxial (upper) stomata that occur at low and moderate densities within the same or closely related species (Muir et al., 2014; Fetter et al., 2019). The second prediction about size-density scaling is more complex because we would need to know the relationships

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between colonization, stomatal cover, stomatal conductance, and fitness in natural conditions. There is growing evidence that stomata mediate tradeoffs between photosynthesis and defense in *Populus trichocarpa* (McKown et al., 2019), but testing these predictions in a variety of species will help determine whether pathogens have played an important role shaping stomatal anatomy in land plants.

DATA AVAILABILITY STATEMENT

Source code is deposited on GitHub (<https://github.com/cdmuir/stomata-tradeoff>) and archived on Zenodo (<https://doi.org/10.5281/zenodo.4102283>).

AUTHOR CONTRIBUTIONS

The author confirms being the sole contributor of this work and has approved it for publication.

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SUPPLEMENTARY MATERIAL

The Supplementary Material for this article can be found online at: <https://www.frontiersin.org/articles/10.3389/fpls.2020.518991/full#supplementary-material>

Appendix 1 | Supplemental methods and spatially implicit model.

Appendix 2 | Additional R packages.

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Conflict of Interest: The author declares that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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