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*CORRESPONDENCE Masaomi Tanaka, ⊠ mtanaka@artsci.kyushu-u.ac.jp

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Unveiling radii and neutron skins of unstable atomic nuclei via nuclear collisions

Masaomi Tanaka¹*, Wataru Horiuchi^{2,3,4,5} and Mitsunori Fukuda^{6,7}

¹Faculty of Arts and Science, Kyushu University, Fukuoka, Japan, ²Department of Physics, Osaka Metropolitan University, Osaka, Japan, ³Nambu Yoichiro Institute of Theoretical and Experimental Physics (NITEP), Osaka Metropolitan University, Osaka, Japan, ⁴RIKEN Nishina Center, Wako, Japan, ⁵Department of Physics, Hokkaido University, Sapporo, Japan, ⁶Department of Physics, Osaka University, Osaka, Japan, ⁷SLiCS Center, Osaka University, Osaka, Japan

Total reaction, interaction, and charge-changing cross sections, which are kinds of cross sections standing for total nuclear collision probability in medium-to high-energy region from a few to several hundred MeV, have been extensively utilized to probe nuclear sizes especially for unstable nuclei. In this mini review, experimental techniques and recent findings from these cross sections are briefly overviewed. Additionally, two new methods to extract neutron skin thickness solely from the above cross sections are explained: One is utilizing the energy and isospin dependence of the total reaction cross sections, and the other is the combination of the total reaction and charge-changing cross section measurements.

KEYWORDS

total reaction cross sections, interaction cross sections, charge-changing cross sections, root-mean-square radii, neutron skin thickness, unstable nuclei

1 Introduction

In neutron-rich nuclei, a thick neutron skin forms, reflecting both the nuclear structure and the bulk properties of nuclear matter. The neutron skin thickness Δr_{np} , which is defined as the difference between the root-mean-square (RMS) radii of the point-neutron and point-proton density distributions, r_n and r_p :

$$\Delta r_{\rm np} = r_{\rm n} - r_{\rm p}.\tag{1}$$

This quantity is particularly anticipated as a promising observable to determine the slope parameter, *L*, of the symmetry energy $c_{\rm sym}(\rho)$ at the saturation density ρ_0 in the equation of state (EoS) of nuclear matter [1], where ρ is the density. This parameter is defined as $L \equiv 3\rho_0 \times \left. \frac{dc_{\rm sym}}{d\rho} \right|_{\rho_0}$ playing a crucial role in extrapolating the EOS for symmetric nuclear matter to that for asymmetric nuclear matter. Although significant efforts have been made to determine the neutron skin thickness, $\Delta r_{\rm np}$, in neutron-rich stable nuclei using various experimental techniques [2–16], a consistent value for *L* has not yet been determined. Recent compilations report the range of *L* values as 58.9 ± 16.5 MeV [17], 58.7 ± 28.1 MeV [18], and 40–60 MeV [19].

Determining Δr_{np} of neutron-rich unstable nuclei has the advantage of constraining the parameter *L*, as a thicker neutron skin is expected [20–23]. There are some Δr_{np} measurements in neutron-rich unstable nuclei using the low-lying dipole resonance [24] and electric dipole polarizability [25–27]. Compared to the above experimental methods, the total reaction (σ_R), interaction (σ_I), and charge-changing cross sections (σ_{CC}), which will be focused in this paper are powerful tools for determining the size properties and $\Delta r_{\rm np}$ of neutron-rich unstable nuclei far from the stability line. The $\sigma_{\rm R}$ and $\sigma_{\rm I}$ are sensitive to the matter radius $(r_{\rm m})$, which is the RMS radius of the nucleon density distribution, $\rho_{\rm m}(r)$. Therefore, if $r_{\rm m}$ is precisely obtained via $\sigma_{\rm R}$ or $\sigma_{\rm I}$, one can determine $\Delta r_{\rm np}$ by combining with $r_{\rm p}$ from another method, such as isotope shift measurements [28, 29], using Equation 1 together with the relation of $Ar_{\rm m}^2 = Zr_{\rm p}^2 + Nr_{\rm n}^2$, where A, Z, and N are the mass, atomic, and neutron numbers of the nucleus of interest.

Furthermore, recent developments using $\sigma_{\rm R}$ and/or $\sigma_{\rm CC}$, mentioned in Section 5, offer new ways to determine $\Delta r_{\rm np}$ solely from these total cross sections. Compared to other major nuclear reaction measurement techniques using RI beams [30], these total cross sections can be measured even with extremely low radioactiveisotope (RI) beam intensities of, e.g., around 0.1 particles/sec, making it possible to extract $\Delta r_{\rm np}$ of very neutron-rich nuclei. In this paper, we briefly review recent studies regarding these total cross sections, with a particular focus on advances related to the neutron skin.

2 Overview of experimental techniques

The $\sigma_{\rm R}$ and $\sigma_{\rm I}$ are defined as the total cross sections for all inelastic reactions and all reactions that change the nuclides, respectively. At energies above approximately 200 MeV/nucleon, $\sigma_{\rm I} \approx \sigma_{\rm R}$ is generally assumed in Glauber-model analyses (Section 3) because the inelastic scattering where the projectile nucleus remains in the ground state hardly occurs. Theoretical studies have indicated that the ratio of this inelastic scattering cross section $(\sigma_{\rm inel})$ to $\sigma_{\rm R}$, $\sigma_{\rm inel}/\sigma_{\rm R}$, is typically 2%–3% at energies above 200 MeV/nucleon, increasing to around 5% as energy decreases to several tens MeV/nucleon [31, 32]. The $\sigma_{\rm inel}/\sigma_{\rm R}$ values for Mg isotopes on ¹²C at 240 MeV/nucleon were experimentally estimated to be around 2% [33].

The $\sigma_{R(I)}$ is often measured using the transmission method [34] represented by

$$\sigma_{\rm R(I)} = -\frac{1}{N_t} \ln\left(\frac{\gamma}{\gamma_0}\right),\tag{2}$$

where N_t is the number of target nuclei per unit area, γ and γ_0 are the nonreaction rates for measurements with and without the target. The γ and γ_0 in Equation 2 are obtained by counting the number of incident particles and that of outgoing nonreaction ones, respectively. This method has lower experimental uncertainty compared to the associate- γ method [35], which assumes that all inelastic scatterings necessarily emit γ rays.

At energies above 200 MeV/nucleon, $\sigma_{\rm I}$ is often measured instead of $\sigma_{\rm R}$. This is because the "nonreaction particle" for $\sigma_{\rm I}$ represents the particle that has not changed nuclide species, which is easier to identify experimentally. Conversely, at energies below around 100 MeV/nucleon, where $\sigma_{\rm inel}$ cannot be ignored, $\sigma_{\rm R}$ are often measured. The definition of "nonreaction particle" of $\sigma_{\rm R}$ includes the "elastically scattered particle." Therefore, in addition to the identification of nuclide species, energy or momentum measurements are required downstream of the target. The $\sigma_{\rm inel}$ are practically estimated from the tail of the energy or momentum distribution [33, 36], while that peculiarly from the inelastic excitations to bound states is sometimes estimated from counting de-exciting *y* rays [37, 38].

The charge-changing cross section, $\sigma_{\rm CC}$, mentioned in Section 5.2, is also measured by the transmission method. This is the total cross section of atomic-number-changing reactions of the projectile nucleus, so that particles with the same Z number as the projectile ones downstream of the target are counted as "nonreaction particles." Note that some studies treated products with a larger Z than projectile nuclei as nonreaction particles because an increase in Z is not considered to result from the fragmentation reaction [39–41]. For example, in C isotopes [39, 42], that contribution was comparable or less to the experimental uncertainty of $\sigma_{\rm CC}$ (around 1%).

3 Glauber model

There are several approaches to theoretically describe the relationship between $\sigma_{\rm R}$ (or $\sigma_{\rm I}$) and the RMS radii of colliding nuclei, such as the black sphere model [31, 43–45] and the folding model with optical potentials [46–55]. Among these, the Glauber theory [56] has frequently been used. In the Glauber formalism, $\sigma_{\rm R}$ is expressed as

$$\sigma_{\rm R} = \int d\boldsymbol{b} \left(1 - \left| e^{i\chi(\boldsymbol{b})} \right|^2 \right),\tag{3}$$

where **b** is the impact parameter vector, $\chi(\mathbf{b})$ is the phase-shift function for the elastic scattering between the projectile and target nuclei. The $\chi(\mathbf{b})$ in Equation 3 is given by the ground-state wave functions of the projectile and target nuclei, $\Psi_0^{\rm P}$ and $\Psi_0^{\rm T}$, respectively:

$$e^{i\chi(\boldsymbol{b})} = \left\langle \Psi_{0}^{\mathrm{P}}\Psi_{0}^{\mathrm{T}} \middle| \prod_{i\in\mathrm{p},\mathrm{n}} \prod_{j\in\mathrm{p},\mathrm{n}} \prod_{k\in\mathrm{P}} \prod_{l\in\mathrm{T}} \left[1 - \Gamma_{ij} \left(E, \boldsymbol{s}_{k}^{\mathrm{P}} - \boldsymbol{s}_{l}^{\mathrm{T}} + \boldsymbol{b} \right) \right] \middle| \Psi_{0}^{\mathrm{P}}\Psi_{0}^{\mathrm{T}} \right\rangle,$$
(4)

where the subscripts "*i*" and "*j*" denote the isospin of nucleons of the projectile and target nuclei, the superscripts "P" and "T" the projectile and target nuclei, respectively, *E* is the incident energy per nucleon, and s_k^p (s_l^T) are the two-dimensional vectors of the *k*(*l*)th nucleon's cordinates (*r*) in the plane perpendicular to the beam axis. The nucleon-nucleon profile function Γ_{ij} , obtained by a Fourier transform of the nucleon-nucleon scattering amplitude, is typically parameterized as [57].

$$\Gamma_{ij}(E, \boldsymbol{b}) = \frac{1 - i\alpha_{ij}(E)}{4\pi\beta_{ij}(E)}\sigma_{ij}(E)\exp\left(-\frac{\boldsymbol{b}^2}{2\beta_{ij}(E)}\right),\tag{5}$$

where σ_{ij} is the nucleon-nucleon total cross section [58] (Figure 1A), α_{ij} the ratio of the real to the imaginary part of the nucleon-nucleon scattering amplitude, and β_{ij} the slope parameter of the nucleonnucleon elastic differential cross section representing the range of nucleon-nucleon interaction.

To calculate $\chi(b)$ in Equation 4, multiple integrals of the wave functions of the projectile and target nuclei are required, which can be performed using the Monte Carlo integration technique [59, 60]. However, approximations are generally applied to avoid the complexity of the calculations. One of



FIGURE 1

Properties regarding total-reaction cross sections σ_{R} or interaction cross sections σ_{I} (A) Energy dependence of proton-proton and proton-neutron (or neutron-proton) total cross sections, σ_{pp} (closed circles) and $\sigma_{pn(np)}$ (open circles), which are fundamental inputs of the Glauber-model calculations. The experimental values are taken from Ref. [58]. (B) Energy dependence of reaction cross section $\sigma_{R}(E)$. Crosses [78], closed circles [64], and closed triangles [72] show experimental data, and the dotted black, dashed blue, and solid red lines represent the Glauber-model calculations under the zero-range OLA, NTG [63], and MOL [64] formalisms. (C) Comparison between experimental data [70] and theoretical calculations of σ_{I} for Ca isotopes on ¹²C at 280 MeV/nucleon. Open blue squares connected by a dotted line represent the Glauber-model calculation under the NTG approximation with density distributions of Ca isotopes obtained from the Hartree–Fock calculation using the SLy4 interaction [71], dot-dashed green lines with the shaded band the Glauber-model calculations using 31 different interactions [69], respectively. For comparison, the double-folding-model calculation with the Gogny-D1S HFB with the angular momentum projection (GHFB + AMP) is also shown by open red triangles connected by a dashed line [50].

the simplest and most frequently used approximations is the optical-limit approximation (OLA):

$$e^{i\chi_{\text{OLA}}(\boldsymbol{b})} = \prod_{i \in \text{p}, n \ j \in \text{p}, n} \prod_{j \in \text{p}, n} \exp\left[-\iint d\boldsymbol{r}^{\text{P}} d\boldsymbol{r}^{\text{T}} \rho_{i}^{\text{P}}(\boldsymbol{r}^{\text{P}}) \rho_{j}^{\text{T}}(\boldsymbol{r}^{\text{T}}) \Gamma_{ij}(\boldsymbol{E}, \boldsymbol{s}^{\text{P}} - \boldsymbol{s}^{\text{T}} + \boldsymbol{b})\right],$$
(6)

Here, ρ^{P} (ρ^{T}) represents the density distribution of the projectile (target) nucleus. Using the OLA, σ_{R} can be calculated given the density distributions of projectile and target nuclei and Γ_{ij} . However, this approximation does not account for various possible multiple-scattering effects. To incorporate them effectively, Γ_{ij} is extended to the nucleon-target profile function, Γ_{NT} [61, 62], which is called the "nucleon-target formalism in the Glauber model" (NTG) [63] or "modified OLA" (MOL) [64]:

$$e^{i\chi_{\text{NTG}}(b)} = \exp\left[-\int d\boldsymbol{r}^{\text{P}}\rho^{\text{P}}\left(\boldsymbol{r}^{\text{P}}\right) \times \left\{1 - \exp\left[-\int d\boldsymbol{r}^{\text{T}}\rho^{\text{T}}\left(\boldsymbol{r}^{\text{T}}\right)\Gamma\left(\boldsymbol{E},\boldsymbol{s}^{\text{P}}-\boldsymbol{s}^{\text{T}}+\boldsymbol{b}\right)\right]\right\}\right].$$
(7)

Here, although Equation 7 also incorporate the isospin dependence *i* and *j* similar to those in Equation 6, these isospin notations are omitted for the sake of simplicity. Note that a modified version of this equation that satisfies symmetry regarding the exchange between projectile and target components is usually used [61, 62]. Other various effects have been also considered: the energy dependendent parameters of α_{ij} and β_{ij} in Γ_{ij} [63, 65–68], Fermi-motion effect [64], and Pauli blocking [69]. Although these frameworks have minor differences, each is constructed to effectively reproduce the

benchmark dataset (e.g., the energy dependence of $\sigma_{\rm R}$ for ¹²C on ¹²C shown in Figure 1B). Then, measured $\sigma_{\rm R(I)}$ results are analyzed based on these evaluated theoretical framework. As an example, Figure 1C shows $\sigma_{\rm I}$ for Ca isotopes on ¹²C at 280 MeV/nucleon [70] together with the calculations using the Glauber model [69, 71] as well as the double-folding model [50] employing theoretical density distributions. To improve the Glauber formalism much more, there are recent experimental contributions, such as high-precision $\sigma_{\rm I}$ data for ¹²C on ¹²C at energies of 400–1,000 MeV/nucleon [72] and $\sigma_{\rm R(I)}$ for ¹⁷F and ¹⁷Ne on a solid hydrogen target [73] at energies of 50–450 MeV/nucleon [74, 75].

4 Progress of total-reaction and interaction cross section studies

4.1 Progress in recent 20 years

After the pioneering work of $\sigma_{\rm I}$ measurements by Tanihata *et al.* [76, 77], $\sigma_{\rm R}$ and $\sigma_{\rm I}$ have been extensively measured at the RI-beam facilities. Here, the progress of studies related to $\sigma_{\rm R}$ and $\sigma_{\rm I}$ achieved after the 2001 review paper [78] is outlined.

Regarding nuclei near the neutron dripline, ²²C [38, 79] and ²⁹F [80] were newly identified as halo nuclei through $\sigma_{R(I)}$ measurements, and the structure of these nuclei and neighboring ³¹F were also investigated theoretically [60, 81–84]. The σ_{I}

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measurements for ^{22,23}O found that the structure of ²³O can be understood within the model consisting of a ²²O core and a $2s_{1/2}$ valence neutron [85]. Systematic $\sigma_{I(R)}$ measurements for F [86], Ne [87], Na [88], and Mg [33] isotopes at RIBF, which accessed more neutron-rich ones compared to previous measurements at GSI [89, 90], have significantly contributed to revealing the area consisting of islands of inversion around N = 20 and 28. Additionally, these systematic data showed that ^{29,31}Ne and ³⁷Mg were found to have the halo structure induced by the strong deformation [91, 92]. The mechanisms of these phenomena were further investigated by various theoretical studies [46–48, 93–95]. The $\sigma_{\rm R}$ measurements, especially below 100 MeV/nucleon, have been extensively conducted to probe the details of density profiles near the nuclear surface [74, 96–109] because $\sigma_{\rm R}$ at lower energy than 200 MeV/nucleon are more sensitive to the dilute density of nuclei due to the large σ_{ii} values [36, 110-113] (Figure 1A).

In the heavier region, other halo nuclei and islands of inversion have been predicted theoretically [114–116]. Regarding experimental progress in this region, $\sigma_{\rm I}$ measurements for Cl and Ar [37], Ca [70], and Kr isotopes [117] have been conducted mainly to discuss the evolution of neutron (proton) skins, which are reviewed separately below.

4.2 Studies on neutron skins

After revealing thick neutron skins in ^{6,8}He from σ_{I} and neutronremoval cross sections [118], the first direct observation of neutronskin growth along a long chain including unstable nuclei was conducted in Na isotopes by combining σ_{I} results [119] with the r_{p} from the isotope-shift measurements [120]. The deduced Δr_{np} of Na isotopes, as well as those of Cl and Ar isotopes [37], show a monotonic dependence on the difference between one-neutron and one-proton separation energies, $S_{n} - S_{p}$ [119]. In contrast to these isotopes, the trend of Δr_{np} in Kr isotopes was different, implying that only the valence nucleons are responsible for the trend [117].

Recent $\sigma_{\rm I}$ measurements revealed a substantial growth of neutron skin in Ca isotopes across the neutron magic number N =28 [70], which is different from the isotopes mentioned above. It has been known that the trend of $r_{\rm p}$ (charge radii) shows a sudden slope change against *N* globally at the neutron magic numbers, which is called a "kink" [28, 29]. The experimental $r_{\rm m}$ values determined from $\sigma_{\rm I}$ for ^{42–51}Ca [70] (Figure 1C) also show a kink structure at N = 28 similar to that of $r_{\rm p}$ [121]. Interestingly, the magnitude of the kink in $r_{\rm m}$ is much larger than that in $r_{\rm p}$, resulting in the emergence of the kink also in the $\Delta r_{\rm np}$ evolution. Various mechanisms have been proposed for the possible origins behind the kink structure in $r_{\rm p}$ (e.g., see Ref. [122]).

The evolution of neutron skin in Ca isotopes provides new insight also into the bulk properties of nuclear matter. The Hartree–Fock calculations have pointed out that the kink structure occurs depending on the properties of the occupying valence single-neutron states to minimize the energy loss resulting from the saturation of the densities in the internal region of the nucleus [71, 116]. Evaluating the contribution of Δr_{np} caused by the surface difference between $\rho_n(r)$ and $\rho_p(r)$ is also important for determining the EOS parameter *L*. Decomposing Δr_{np} into the bulk part (Δr_{np}^{bulk}), which is sensitive to *L*, and the surface part ($\Delta r_{np}^{surface}$) within the

incompressible droplet model has clarified that the neutron-skin kink appears when the trend of $\Delta r_{np}^{surface}$ changes [23, 123–126]. Thus, while the neutron skin is sensitive to the parameter *L* as mentioned in the introduction, the neutron-skin kink itself plays a different role in identifying the effect of $\Delta r_{np}^{surface}$ on determining *L*.

In addition to the approach with the total collision cross sections described above and below, methods only using nucleon removal cross sections have been proposed [127].

5 Extraction of neutron skin thickness solely from collision cross sections

Recently, two novel methods have been developed to derive Δr_{np} solely from nuclear collision cross sections. One method utilizes the energy and target dependence of σ_R (Section 5.1), and the other combines σ_{CC} and σ_R (Section 5.2) [128–131].

5.1 Total reaction cross sections utilizing its energy and isospin dependence

This method [126, 132] utilizes the isospin and energy dependence of nucleon-nucleon total cross sections, $\sigma_{ij}(E)$ [58]. As shown in Equation 5, the $\sigma_{ij}(E)$ shown in Figure 1A is a fundamental input for Glauber model calculations, leading to the energy dependence of $\sigma_{\rm R}$. The ratio of the proton-neutron ($\sigma_{\rm pn}$) to proton-proton (or neutron-neutron) total cross sections ($\sigma_{\rm pp(nn)}$) is $\sigma_{\rm pn}/\sigma_{\rm pp} \sim 3$ at $E \leq \sim 100$ MeV/nucleon, and $\sigma_{\rm pn}/\sigma_{\rm pp}$ decreases as the energy increases, then reaches unity at around 600 MeV/nucleon. At higher incident energies, although $\sigma_{\rm pp}$ becomes slightly larger than $\sigma_{\rm pn}$, $\sigma_{\rm pn}/\sigma_{\rm pp}$ remains around unity. Therefore, proton targets and nuclear targets such as ¹²C, which contain equal numbers of protons and neutrons, are expected to have a different sensitivity to $\Delta r_{\rm np}$.

Horiuchi et al. analyzed the correlation between $\sigma_{\rm R}(E)$ and $\Delta r_{\rm np}$ through the Glauber-model calculation using the density distributions obtained from Skyrme-Hartree-Fock (SHF) theory [126]. In this analysis, the "reaction radius" $a_{\rm R}$ was introduced in regard to $\sigma_{\rm R}$, namely, $a_{\rm R}(N, Z, E, T) \equiv \sqrt{\sigma_{\rm R}(N, Z, E, T)/\pi}$, where N and Z are the neutron and atomic numbers of the projectile nucleus, Eis the reaction energy, and T is the label of the target species. The correlation between Δr_{np} and the difference in a_R obtained from $\sigma_{\rm R}$ at different energies, $\Delta a_{\rm R}(E,E') = a_{\rm R}(N,Z,E',T) - a_{\rm R}(N,Z,E,T)$, shows global consistency over all isotopes of O, Ne, Mg, Si, S, Ca, and Ni isotopes examined here. For carbon targets, $\Delta a_{\rm R}(E,E')$ is almost independent of Δr_{np} , whereas for proton targets, the plot of $\Delta r_{\rm np}$ versus $\Delta a_{\rm R}(E, E')$ shows a clear non-zero slope. Especially, the $\Delta a_{\rm R}(E,E')$ trends including 100 MeV/nucleon data have a higher sensitivity to $\Delta r_{\rm np}$. To further investigate the effectiveness of $\sigma_{\rm R}(E)$ on Δr_{np} , a_{R} was parameterized as the empirical formula of

 $a_{\mathrm{R}}(N, Z, E, T) \equiv \alpha(E, T) r_{\mathrm{m}}(N, Z) + \beta(E, T) \Delta r_{\mathrm{np}}(N, Z) + \gamma(E, T),$

where $\alpha(E, T)$, $\beta(E, T)$, and $\gamma(E, T)$ are energy- and target-dependent parameters. The parameter $\beta(E, T)$, representing the effect of Δr_{np} , shows prominent energy and target (isospin) dependence: $\beta(E, T)$ is independent of energy for carbon targets, whereas strongly



FIGURE 2

(A)Energy dependence of σ_{CC} for ²⁸Si on a carbon target [135]. The dashed and dotted lines represent the ZROLA calculations of $\tilde{\sigma}_{CC}$ (Equation 8) and σ_{R} , respectively. The solid line shows the ZROLA calculation of σ_{CC} with the empirical correction factor $\epsilon(E)$. (B) A dependence of σ_{CC} for Ca isotopes on a carbon target at around 280 MeV/nucleon (bottom figure), and the corresponding P_{evap} values (top figure). The black solid and green dashed lines represent $\tilde{\sigma}_{CC}$ calculations using Equation 8 with and without the empirical correction factor $\epsilon(E)$, respectively. The thin-dashed lines, red-solid lines with shaded bands, and dotted lines show σ_{CC} calculations from Equation 9 with different E_{max} values of 20, 45 ± 8, and 70 MeV, respectively. Figures in (A, B) were reprinted from Ref. [144], respectively.

dependent for proton targets. Therefore, it is possible to extract $\Delta r_{\rm np}$ by measuring $\sigma_{\rm R}$ at multiple energies and/or targets having different $\beta(E, T)$. Furthermore, to enhance sensitivity to $\Delta r_{\rm np}$, it is desirable to use a combination of proton and neutron targets that are completely isospin asymmetric pair. The use of deuteron targets has been proposed as an alternative to a neutron target [133].

The sensitivity of $\sigma_{\rm R}(E)$ for separating density distributions of proton and neutron, $\rho_{\rm p}(r)$ and $\rho_{\rm n}(r)$, using these properties was demonstrated experimentally in halo nuclei. The experimental $\sigma_{\rm R}$ values for ¹¹Be and ⁸B on proton targets at 50–120 MeV/nucleon were consistent only with calculations assuming neutron and proton tails, respectively [134]. The $\rho_{\rm p}(r)$ and $\rho_{\rm n}(r)$ of ¹¹Li were determined solely from the energy dependence of the experimental $\sigma_{\rm R}$ values on proton and carbon targets [103].

5.2 Charge-changing cross sections

The $\sigma_{\rm CC}$ measurements aiming to derive $r_{\rm p}$ have been conducted for isotopes up to Fe, particularly since 2010 [39, 40, 65, 135–147]. By analogy with the relationship between $\sigma_{\rm R}$ and $r_{\rm m}$, $\sigma_{\rm CC}$ is expected to be sensitive to $r_{\rm p}$. The relationship between $\sigma_{\rm CC}$ and $r_{\rm p}$ is usually treated in the following Glauber-model-like formalism [65, 135, 136]:

$$\tilde{\sigma}_{\rm CC} = \int \left[1 - \left| e^{i\chi_{\rm p}(\boldsymbol{b})} \right|^2 \right] d\boldsymbol{b},\tag{8}$$

where $\chi_{p}(b)$ is obtained from Equation 6 by omitting $\rho_{n}(r)$ of the projectile nucleus, that is, only *i* = p is adopted for Equation 6

[148]. In the case of $\sigma_{\rm CC}$, the situation appears to be less straightforward than that of $\sigma_{R(I)}$ due to the potential influence of neutrons in the incident nucleus. Here, for the sake of subsequent expressions, the calculated value from this equation is denoted as $\tilde{\sigma}_{CC}$. There are several treatments to depict σ_{CC} based on Equation 8. First, Yamaguchi et al. introduced an energy-dependent phenomenological correction factor $\varepsilon(E)$ into Equation 8 with the zero-range optical-limit approximation (ZROLA) to reproduce σ_{CC} data for ²⁸Si on ¹²C at energies of 100-600 MeV/nucleon [135], as shown in Figure 2A. It has been shown that this calculation with $\varepsilon(E)$ explains the experimental values for Be to O isotopes on ¹²C at 300 MeV/nucleon with 3% standard deviation [136]. Second, the experimental σ_{CC} of stable B, C, N, and O isotopes on ¹²C at around 900 MeV/nucleon were well reproduced by the finite-range opticallimit approximation (FROLA) calculations without $\varepsilon(E)$ [39–41, 141]. For ^{10,11}B, the ratio of the experimental values to the calculated ones is 1.01(2) [141]. Third, Tran et al. determined profile-function parameters with the FROLA calculation common to reproduce both $\sigma_{\rm R}(E)$ and $\sigma_{\rm CC}(E)$ for ¹²C on ¹²C over the range of 10–2,100 MeV/nucleon [65]. However, this calculation still underestimates at around 300 MeV/nucleon. Thus, although the consistency over respective treatments is not necessarily guaranteed, the reliability is ensured by locally normalizing with well-known σ_{CC} data.

Contrary to the description by Equation 8, it has been suggested that considering the contribution of $\rho_n(r)$ of the projectile nucleus is crucial to describe σ_{CC} [148–151]. Tanaka *et al.* demonstrated that the trend of the experimental σ_{CC} data can be explained by explicitly incorporating the contribution of $\rho_n(r)$ of the projectile nucleus [144] based on the abrasion-ablation model [152, 153]. In

this framework, the contribution of the cross section σ_{evap} , which accounts for the charge-changing process of the projectile nucleus caused by the evaporation of charged particles following neutron removal reactions, was introduced in addition to the ZROLA calculation of Equation 8:

$$\sigma_{\rm CC} = \tilde{\sigma}_{\rm CC} + \sigma_{\rm evap}.$$
 (9)

The $\sigma_{\rm evap}$ is calculated using the contribution probability of the neutron-removal reaction to $\sigma_{\rm CC}$, $P_{\rm evap}$. The $P_{\rm evap}$ depends on the applied value of the parameter E_{max} , which represents the maximum excitation energy of the prefragment produced after a one-nucleon removal reaction (Figure 2B). Using $E_{\text{max}} = 45$ MeV, this calculation consistently explains existing $\sigma_{\rm CC}$ data on $^{12}{\rm C}$ at around 300 MeV/nucleon over a wide mass region from C to Fe isotopes, with 1.6% standard deviation [144]. Figure 2B represents measured σ_{CC} results for Ca isotopes on ¹²C together with several caluculated cross sections explained in this subsection (see caption). This framework also reproduces new experimental results for C, N, and O isotopes on ¹²C at 300 MeV/nucleon [146] as well as one of two datasets of $\sigma_{\rm CC}$ for N isotopes on $^{12}{\rm C}$ at around 900 MeV/nucleon [40]. The framework of Equation 9; Figure 2B indicates that the majority of $\sigma_{\rm CC}$ provides information on $\rho_{\rm p}(r)$ of the projectile nucleus and the contribution of σ_{evap} decreases as N of the projectile nucleus increases. Thus, in very neutron-rich region, the assumption of Equation 8 works well. The sensitivity of $\sigma_{\rm CC}$ to $r_{\rm p}$ becomes much larger.

A proton target has been adopted in $\sigma_{\rm CC}$ measurements, as in the cases of 30 Ne, 32,33 Na [139], and ${}^{34-36}$ Ar [142]. Suzuki *et al.* emphasized the necessity of considering the contribution of $\rho_n(r)$ of the projectile nucleus peculiarly in $\sigma_{\rm CC}$ on a proton target [154]. The FROLA calculation of Equation 8 underestimates the experimental $\sigma_{\rm CC}$ values by 10%–20% for C isotopes on a proton target at around 900 MeV/nucleon. They found that this discrepancy can be explained by introducing the "p-n exchange" effect, in which a part of the proton flux of the target is converted to the neutron flux by neutrons of the projectile, contributing to $\sigma_{\rm CC}$.

To derive the EOS parameter *L*, the difference in the charge radii of mirror nuclei, Δr_p^{mirr} , has been used [155–160]. Similarly, the relationship between *L* and the difference in σ_{CC} of mirror nuclei, $\Delta \sigma_{\text{CC}}^{\text{mirr}}$, was demonstrated to show a good linear correlation [161]. The degree of this linear correlation is equivalent to the ones between *L* and Δr_{np} or Δr_p^{mirr} .

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6 Summary

This paper has reviewed recent advancements in the total reaction ($\sigma_{\rm R}$), interaction ($\sigma_{\rm I}$), and charge-changing cross sections ($\sigma_{\rm CC}$), with a special emphasis on the neutron skin and corresponding nuclear radii. The framework describing the relationship between these cross sections and the size properties of atomic nuclei has been well investigated, providing the advantage to probe nuclear sizes of neutron-rich unstable nuclei, where a thick neutron skin is expected. The review has also highlighted two novel methods for extracting $\Delta r_{\rm np}$ from the total collision cross sections: one utilizing the energy and isospin dependence of $\sigma_{\rm R}$, and the other combining $\sigma_{\rm CC}$ with $\sigma_{\rm R}$. These advancements lead to more accurate constraining the slope parameter (L) in the symmetry energy term of the EoS of nuclear matter through $\Delta r_{\rm np}$ of unstable nuclei in very neutron-rich region.

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