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# [Research on the design of](https://www.frontiersin.org/articles/10.3389/fphy.2024.1481543/full) [progressive addition multifocal](https://www.frontiersin.org/articles/10.3389/fphy.2024.1481543/full) [defocused freeform lenses](https://www.frontiersin.org/articles/10.3389/fphy.2024.1481543/full)

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In this study, we developed a new method for designing progressive additionmultifocus defocused freeform lenses. We used two independent meridians and achieved a smooth gradient transition of additional optical power from the center to the peripheral area of the lens, along with an asymmetric distribution of additional optical power on the nasal-temporal side of the lens. To improve the optical performance of the lenses, we developed three different designs based on the distribution of the additional optical power on the meridians. We conducted simulations and processing on the three different designs. The lenses designed using improved logistic regression and sine functions for meridian optical power distribution exhibited stable optical performance in the central focus area. They also met the design requirements for additional optical power. However, significant distortion was still observed in the peripheral region, which required further optimization. Lenses designed using piecewise linear functions for meridian optical power distribution exhibited relatively poor optical performance with significant optimization potential. Thus, combining the optical power distribution and surface-type factors for optimization is necessary. The proposed method enabled designing of defocus-free curved mirror lenses that satisfy the optical performance requirements. Thus, this method provides a new approach for the design of progressive addition lenses.

#### KEYWORDS

freeform surface, defocus lens, optical power, astigmatism, optimization

# 1 Introduction

Myopia is a common refractive error characterized by an elongated eyeball axis or excessive corneal curvature, resulting in blurred vision caused by the focusing of parallel light in front of the retina [[1](#page-9-0)]. Myopia not only disrupts daily lives and learning of the affected but can also lead to ophthalmic complications, such as macular holes, retinal detachment, retinal degenerative diseases, retinal hemorrhage, and even blindness [\[2\]](#page-9-1). Thus, it is a major public health issue worldwide. According to the "World Vision Report" released by World Health Organization in 2020, the total prevalence of myopia in highincome countries in the Asia-Pacific region is as high as 50%. With the rapid development of modern technology and an increase in the human development index, the global population was estimated to reach 3.36 billion by 2023. The incidence of myopia in

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Chinese teenagers exceeds 80%, with nearly 20% of teenagers being highly myopic [\[3\]](#page-9-2). The main methods for treating myopia in teenagers are wearing frame-style glasses for correction and surgery for normalizing the refractive ability of the eye [\[4\]](#page-9-3).

In recent years, an increasing number of young people have chosen to use eyeglasses that control peripheral defocus (such as multifocal contact lenses and peripheral defocus myopia-control lenses) to manage the progression of myopia [\[5\]](#page-9-4). Long-term exposure to hyperopic defocus can accelerate the development of myopia, whereas exposure to myopic defocus can delay its progression [[6](#page-9-5)]. Few theoretical studies support this view from two perspectives. According to the experiments conducted by Smith [\[7\]](#page-9-6) and Lin [[8\]](#page-9-7) on rhesus monkeys and population, respectively, peripheral hyperopic defocus on the retina induces axial elongation and increases myopia. In addition, according to many researchers, including [[9\]](#page-9-8), the accommodative sensitivity of myopic children is significantly lower than that of emmetropic children. Compared to contact lenses, eyeglasses with peripheral defocus frames are convenient, noninvasive, and have wider adaptability and fewer adverse reactions. This makes them suitable for young people who cannot adapt to contact lenses or have low myopia or flat corneal curvature [\[10](#page-9-9)]. Currently, many types of peripheral defocus lenses are available in the market, such as defocus incorporated multiple segments (DIMS) lenses and concentric ring bifocal micro-prism defocus lenses [[11\]](#page-9-10). DIMS lenses [\[12](#page-9-11)] have a 9 mm central focus area surrounded by multiple small lenses that induce myopic defocus, providing good adaptability. The concentric ring bifocal microprism defocus lenses [\[13](#page-9-12)] manage myopia through the structure of microprism lenses, which creates high-order aberrations to inhibit axial elongation and delay myopia progression.

According to Laura [[14\]](#page-9-13), the population at the greatest risk of myopia progression has asymmetric retinas, that is, the optical characteristics and morphology of the nasal and temporal areas of the retina are different [[15\]](#page-9-14). Therefore, research on the asymmetric design of defocusing lenses is important. Starting with the design method of progressive addition freeform surfaces [[16](#page-9-15)–[19](#page-9-16)], in this study, we optimized a new defocus freeform surface. To obtain a meridian line, we divided the surface into the nasal and temporal zones and connected the central focus area of the two zones to the central point of the myopic defocus area. The optical power change law at each point on the meridian line was determined separately, and the focal light distribution of the entire surface was directly generated by specifying the curve intersecting the meridian line. Next, optical power optimization was performed on the entire surface for smoothness. Finally, the surface shape was calculated. This method can achieve an asymmetric distribution of the light focal length on freeform surfaces while ensuring a smooth transition of the light focal length from the central focus to peripheral defocus area of the lens. It provides excellent optical performance and ensures the comfort of the wearer. In the second section, the design principles of the peripheral defocus freeform surface are explained, and in the third section, simulation processing examples are presented to validate the design.

# 2 Principle of optimal design method

## <span id="page-1-0"></span>2.1 Design of the optical power of the defocus freeform surface lenses

Progressive multifocal freeform surfaces are widely used in the design of progressive addition lenses (PALs) that provide variable optical power for different viewing zones [[16](#page-9-15)]. As shown in [Figure 1A](#page-2-0), 7PALs are primarily divided into four zones: distance, near, intermediate, and blending [\[17\]](#page-9-17). The optical power gradually and smoothly increased along the meridian line of the lens; the gradient of increase started from the distance-vision area at the top of the lens and reached the maximum addition power (ADD) at the near-vision area at the bottom of the lens. In the figure, MM' represents the meridian line, while points D and N represent the distance and near reference points. In the design concept of progressive multifocal lenses [[18\]](#page-9-18), the design of optical power along the meridian line determines the optical power distribution on the entire lens surface. Therefore, a smooth transition function was used along the meridian line to achieve a change in the optical power from the distance to near zone. In addition to designing the optical power along the meridian line, progressive lens designers use a set of contour lines intersecting the meridian line to diffuse the optical power change along the meridian line to the entire surface [[20](#page-9-19)]. The optical power on the contour lines was consistent with that at the contour–meridian line intersection points, as shown in [Figure 1B.](#page-2-0) After obtaining the optical power distribution on the entire surface, calculations, simulations, and manufacturing processes for the lens shape were conducted, and a finished progressive lens was obtained. The design process is illustrated in [Figure 2.](#page-2-1)

Unlike progressive multifocal freeform surfaces, defocused freeform surfaces consist of central focusing and peripheral defocused areas. The central focusing area provides a constant negative diopter, whereas the peripheral defocused area provides additional power relative to the central focusing area (defocus amount). However, this design fundamentally involves the transition of power from one focus area to another, which can be controlled using meridians. To achieve an asymmetric power distribution between the nasal and temporal sides of the defocused freeform surface, we used two meridians and controlled the power variations on each side, as shown in [Figure 3.](#page-3-0) ON and OT represent the nasal and temporal meridians, respectively, which control the power changes on the nasal and temporal sides of the freeform surface. Viewing each area as a separate gradient power freeform surface and taking the temporal side as an example, the central focusing area on the temporal side has a constant negative diopter but with zero additional power. The additional power smoothly increased along the meridian OT until it reached the maximum additional power, and then stabilized. Subsequently, the power variations on the meridian diffused to the temporal side of the surface through a cluster of contour lines intersecting the temporal meridian. Here,  $OT = ON = R$ , where R represents the radius of the freeform surface, and L is the length of the section where the additional power gradually increases along the meridian.



<span id="page-2-0"></span>

<span id="page-2-2"></span><span id="page-2-1"></span>To achieve the variation in light focus on the meridian ([Figure 3](#page-3-0)), we used a relatively simple linear segmented function ([Equation 1\)](#page-2-2) and a sine function [\(Equation 2](#page-2-3)).

$$
Add = \begin{cases} m & d < R_1 \\ (Add \max - m)^*(d - R_1)/L & R_1 \le d \le R_1 + L, \\ Add \max & R_1 + L < d \le R \end{cases}
$$
 (1)

<span id="page-2-3"></span>
$$
Add = \begin{cases} m & d < R_1 \\ (Add\max - m)^* \sin (\pi^* (d - R_1) / L & R_1 \le d \le R_1 + L \\ Add\max & R_1 + L < d \le R \end{cases}
$$
 (2)

where d represents the distance from a point to origin O of the meridian line; Add is the additional optical power at a distance d from the origin; m is the additional optical power in the central focusing area, usually set to 0; and Add max represents the maximum additional optical power value. While the two functions above can achieve a gradual change in the additional optical power, the nondifferentiable parts existing in the functions may affect the smooth change in the additional optical power.

Among commonly employed functions, the logistic regression function ([Equation 3\)](#page-2-4) exhibits smoothness, continuity, and highorder differentiability within its domain. Notably, its rates of change are gradual at both extremes. This characteristic renders it particularly advantageous for the design of meridians, facilitating enhanced stability of the central focusing area of the free-form surface. Therefore, we developed an improved logistic regression function ([Equation 4](#page-2-5)) to fit the change in additional optical power on the meridian line.

$$
f(x) = 1/(1 + e^x) \tag{3}
$$

$$
Add = (Add \max - m) / (1 + e^{(A^*d - b)}), \qquad (4)
$$

<span id="page-2-5"></span><span id="page-2-4"></span>where A is the curve control coefficient, and b is the curve translation coefficient. Three types of meridian light-focusing functions were obtained, with the parameters set as nasal Add  $max = 1.5D$ , temporal Add  $max = 2.0D$  (commonly used values of additional optical power), central focusing zone additional light



<span id="page-3-0"></span>

<span id="page-3-1"></span>focus m = 0, R = 30 mm, R1 = 6 mm, L = 18 mm, A = 0.7, and b = 10. This resulted in specific changes in light focusing for the nasal and temporal meridians, as shown in [Figures 4A, B,](#page-3-1) respectively, with specific contour line settings, as shown in [Figure 4C.](#page-3-1)

### 2.2 Calculated surface shape

<span id="page-3-2"></span>After obtaining the additional optical power distribution on the two meridians and the contour line distribution of the surface, the additional optical power distribution  $Add(x, y)$  for the entire surface was derived. Then, the optical power distribution  $F(x, y)$ over the entire surface was determined as [Equation 5:](#page-3-2)

$$
F(x, y) = M + Add(x, y),
$$
 (5)

where M is the optical power of the central fixed-focus zone, which is a constant. As the freeform surface was independently designed for the nasal and temporal sides and the contour line density was limited, the optical power variation across the entire freeform surface was still not sufficiently smooth. Therefore, the interpolation of the optical power distribution across the entire freeform surface is necessary. The interpolated optical power distribution is denoted as  $FF(x, y)$ . The optical power distributions of the surface before and after the interpolation are shown in [Figure 5](#page-4-0).

<span id="page-3-3"></span>After obtaining the interpolated optical power distribution  $FF(x, y)$  of the surface, the expected mean curvature distribution  $P(x, y)$  of the surface was derived as [Equation 6:](#page-3-3)

$$
P(x, y) = \frac{FF(x, y)}{1000^{*}(n - 1)},
$$
\n(6)

where n is the refractive index of the lens that depends on the material used to manufacture the free-form lens.

Before calculating the surface shape, it is essential to recognize that there are two key parameters associated with the surface shape  $z(x, y)$ : mean curvature and astigmatism, are only related to the



<span id="page-4-1"></span><span id="page-4-0"></span>sum and the difference of the two principal curvatures, respectively. Suppose  $k_1$  and  $k_2$  are the two local principal curvatures of the surface  $z(x, y)$ , then, the mean curvature is defined as [Equation 7:](#page-4-1)

Mean curvature = 
$$
\frac{k_1 + k_2}{2}
$$
 (7)

<span id="page-4-2"></span>And the astigmatism is defined as [Equation 8:](#page-4-2)

$$
Astigmatism = (n-1)\frac{k_1 - k_2}{2}
$$
 (8)

Next, we determined an optimal surface shape solution that maximized the closeness of the mean curvature distribution of the surface to the expected mean curvature distribution and minimized unnecessary astigmatism on the surface to the greatest extent possible. We constructed a loss function to obtain the optimal solution for the surface shape by minimizing the loss function as [Equation 9](#page-4-3)

<span id="page-4-3"></span>
$$
I(z) = \int_{\Omega} \left[ \alpha(x, y) \left( \frac{k_1 - k_2}{2} \right)^2 + \beta(x, y) \left( \frac{k_1 + k_2}{2} - P(x, y) \right)^2 \right] dxdy,
$$
\n(9)

where  $\Omega \in R$  represents the integral domain of the surface. The weighting functions  $\alpha(x, y)$  and  $\beta(x, y)$  control the distribution of astigmatism of the lens and the distribution of optical power of the lens, respectively. In this study, weighting functions  $\beta(x, y)$  had a high weight across the entire surface, while weighting function  $\alpha(x, y)$  had a high weight in the central fixed-focus zone and a low weight in other areas.

<span id="page-4-4"></span>To obtain the surface shape  $z(x, y)$ , we employed the method of minimizing least squares and determined the matrix of surface heights  $z(x, y)$ . First, the surface was discretized into a matrix consisting of  $N \times N$  points. For computational convenience, the progressive lens surface was assumed to be composed of a specified reference surface  $\omega(x, y)$  and another small perturbation surface  $v(x, y)$  relative to the chosen reference surface  $\omega(x, y)$ ([Equation \(10\)](#page-4-4).

<span id="page-4-5"></span>
$$
z(x, y) = \omega(x, y) + \nu(x, y), (x, y) \in \Omega, \tag{10}
$$

$$
\omega(x, y) = \sqrt{R^2 - x^2 - y^2}, (x, y) \in \Omega,
$$
 (11)

$$
R = \frac{(n-1)}{M+B} \times 1000, \ (x, y) \in \Omega \tag{12}
$$

<span id="page-4-6"></span>The perturbation surface takes the form of an aspheric freeform surface controlled by weighting functions and the desired mean curvature. The reference surface is typically a standard spherical surface; its shape is defined by [Equation 11,](#page-4-5) where R is the curvature radius of the given spherical surface and its value is determined by [Equation 12.](#page-4-6) In [Equation 12,](#page-4-6) B represents the front surface power of the designed lens. Next, we specified three boundary conditions forthe surface as [Equation 13:](#page-4-7)

$$
\begin{cases} \text{Min } I(\omega; \nu) = \int_{\Omega} f(\nu_{i,j}) \\ \nu_{1,1} = \nu_{1,N} = \nu_{N,1} = 0 \end{cases}
$$
 (13)

<span id="page-4-8"></span><span id="page-4-7"></span>The process of solving the freeform surface height matrix using least squares is given by the [Equation 14:](#page-4-8)

$$
\frac{\partial I(v)}{\partial v_{ij}} = 0, i \in [1, 2, \dots, N], j \in [1, 2, \dots, N]
$$
 (14)

The optical power M of the central fixed-focus zone, front surface power of the lens, and matrix size N were assumed as -2D, 3.43D, and 60, respectively. The thus-obtained base surface  $\omega(x, y)$  is shown in [Figure 6A](#page-5-0). The perturbation surface  $\nu(x, y)$ obtained from the solution is shown in [Figure 6B](#page-5-0).

# 3 Results and discussion

### 3.1 Optical simulation

For the linear segmented function [\(Section 2.1](#page-1-0)) to design the meridian optical power, the solved freeform surface was used for the lens design (Lens 1 in this design instance). The design parameters of Lens 1 are listed in [Table 1.](#page-5-1)



#### <span id="page-5-1"></span><span id="page-5-0"></span>TABLE 1 Design parameters of Lens 1.



(SPH: Central Fixed-Focus Optical Power; NADD: nasal Add; TADD:temporal AddIndex: refractive index; BC: Base Curve).



<span id="page-5-2"></span>The optical power and astigmatism of Lens 1 were simulated, as shown in [Figure 7](#page-5-2).

According to the simulation results of the optical power and astigmatism, the astigmatism in the central fixed-focus zone of Lens 1 was slightly higher. In addition, the additional optical powers on the nasal and temporal sides differed significantly from the expected values. This indicated a room for optimization when using linear segmented functions to design meridian optical powers.

For the method ([Section 2.1](#page-1-0)), which uses sine functions to design meridian optical powers, the solved freeform surface was used for the designing Lens 2. The design parameters for Lens 2 are listed in [Table 2](#page-6-0).

The optical power and astigmatism of Lens 2 were simulated, as shown in [Figure 8](#page-6-1).

Based on the simulation results, Lens 2 (designed using sine functions for meridian optical powers) showed a relative reduction

#### <span id="page-6-0"></span>TABLE 2 Design parameters of Lens 2.



#### <span id="page-6-2"></span>TABLE 3 Design parameters of Lens 3.





<span id="page-6-1"></span>in astigmatism in the central fixed-focus zone and surrounding areas. The optical power in the central fixed-focus zone satisfied the requirements of the Chinese National Standard [\[21\]](#page-9-20) GB 10810.1–2005″Ophthalmic Optics - Spectacle Lenses Part 1: Single Vision and Multifocal Lenses." The additional optical power on the nasal and temporal sides met the expected requirements. Therefore, it can be considered as a relatively good design. However, owing to the nondifferentiable points in the original meridian function, a significant gradient was observed in the additional optical power from the center to the sides of the lens.

For the method [\(Section 2.1\)](#page-1-0), which uses logistic regression functions to design meridian optical powers, the solved freeform surface was used for the designing Lens 3. The design parameters for Lens 3 are listed in [Table 3.](#page-6-2)

The optical power and astigmatism of Lens 3 were simulated, as shown in [Figure 9](#page-7-0).

From the simulation results, Lens 3 (designed using an improved logistic regression function for meridian optical powers) exhibited ideal optical power and astigmatism in the central fixed-focus zone. The additional optical power around the central fixed-focus zone exhibited a smoother and more gradual variation. The additional optical power on the nasal and temporal sides also satisfied the design requirements. However, Lenses 3 and 2 exhibited excessive peripheral astigmatism.

### 3.2 Processing and analysis

To verify the optical performance of the designed freeform surfaces, the three sets of freeform lenses (Lenses 1–3) were processed and tested. Initially, various processes, such as turning, milling, grinding, and polishing, were conducted on the freeform lenses using the freeform machining equipment Satisloh VFT-orbit provided by Mingyue Optical Co., Ltd. The lenses were measured using a VM2000 freeform measurement instrument to obtain their optical power and astigmatism distributions, as shown in [Figures 10](#page-7-1), [11.](#page-7-2)

Simultaneously, using a focimeter, following parameters of the physical lenses were measured [\(Table 4](#page-8-0)): the actual center optical power (Center SPH), center astigmatism (Center CYL), actual maximum additional optical power on the nasal side (Actual NADD), and actual maximum additional optical power on the temporal side (Actual TADD).

According to the comprehensive data in [Table 4](#page-8-0) and [Figures 10,](#page-7-1) [11](#page-7-2), all three lenses exhibited relatively good optical performance. The center optical power error in the center focus area of the three lenses did not exceed 0.25D, and astigmatism was also within 0.25D. Astigmatism was predominantly concentrated in the four corners of the lens periphery. Lens 1, designed with meridian optical powers using a linear segmented function, showed sparse astigmatism



<span id="page-7-0"></span>

<span id="page-7-2"></span><span id="page-7-1"></span>

Lens	Center SPH/D	Center CYL/D	<b>Actual NADDD</b>	Actual TADD/D
$1.$ Lens $1$	$-1.86$	$-0.13$	0.76	1.34
2. Lens 2	$-1.95$	$-0.05$	1.44	2.01
3. Lens 3	$-1.96$	$-0.05$	1.45	1.96

<span id="page-8-0"></span>TABLE 4 Actual measurement results of three sets of lenses.

<span id="page-8-1"></span>TABLE 5 Comparison of the advantages and disadvantages of three sets of lenses.

Lens	Advantages	<b>Disadvantages</b>
1. Lens 1	low peripheral astigmatism	central area instability and high Add error
2. Lens 2	Slightly higher peripheral astigmatism	low Add error
3. Lens 3	Slightly higher peripheral astigmatism	better optical performance in the central area and low Add error

gradients on the defocused freeform surface. However, the center power deviated from the expected design by 0.14D, and the astigmatism in the center focus area exceeded 0.12D, potentially affecting comfort. The reason for this phenomenon may be that the meridian function of Lens 1 is not smooth at the edges of the center focus area, which leads to significant errors in the astigmatism and optical power of the lens in the center focus area during subsequent calculations. Moreover, the additional optical power in the peripheral areas of the lens exhibited errors of ˃0.5D, indicating significant room for optimization for this design method. Lens 2, designed using sine functions for meridian optical powers, exhibited a center optical power deviation of 0.05D from the expected values, with astigmatism values at −0.05D. The maximum additional optical power errors on the nasal and temporal sides were <±0.06D, complying with the requirements of the national standard (GB10810.1–2005). However, this design showed localized areas of excessive astigmatism in the lens periphery. Lens 3, designed using an improved logistic regression function for meridian optical powers, showed a center optical power deviation of 0.04D from the expected values, with astigmatism values at −0.05D. The maximum additional optical power errors on the nasal and temporal sides were −0.05D and −0.04D, respectively. It also satisfied the requirements of the national standard (GB10810.1–2005). Compared to the second design method, this approach exhibited smaller astigmatism in adjacent areas around the center and a sparser gradient of astigmatism in the center area, potentially offering better comfort. However, similar to other designs, the localized areas of excessive astigmatism in the periphery indicated the need for further optimization. Through the discussion of the fabrication results of the three lenses and the introduction of the three design methods in the previous sections, we can derive [Table 5,](#page-8-1) which clearly illustrates the advantages and disadvantages of the lenses obtained from the three design approaches. The table shows that although the design method of Lens 1 has lower peripheral astigmatism, it has a larger Add error and unstable optical performance in the central region. In contrast, the design methods of Lens 2 and Lens 3 have larger peripheral astigmatism but exhibit smaller Add errors. Furthermore, compared to the design method of Lens 2, Lens 3 has better optical

performance in the central region. Therefore, in the actual design process, we are more inclined to choose the design method of Lens 3.

# 4 Conclusion

This study was based on the design approach of progressive multifocal freeform lenses. We established a new concept for designing asymmetric defocus freeform lenses. Initially, the desired distribution of the mean curvature of the freeform surface was determined. This distribution was incorporated into a loss function related to the average principal curvatures and their difference on the freeform surface, which was minimized to obtain the surface heights of the freeform lens. In this study, we designed two meridians with different levels of optical power variation on the nasal and temporal sides of the freeform surface to achieve an asymmetric distribution of additional optical power. Furthermore, to achieve a smooth transition of additional optical power between the central fixed-focus zone and peripheral defocused zones of the freeform surface, along with basic linear segmented and sine functions, we introduced an improved logistic regression function in the design of the meridian optical power variation. Finally, lenses designed using these three functions were analyzed using optical simulation software, and they were manufactured and quality-tested using freeform machining equipment to validate experimental results. Based on the study findings, in subsequent lens design efforts, to address the issue of significant astigmatism observed in lens 2 and 3, one approach involves superimposing an additional surface with a negative Add onto the existing surface, aiming to counteract a portion of the unwanted astigmatism in the peripheral regions. Alternatively, the lens surface profile could be refined through re-interpolation techniques to reduce peripheral astigmatism, thereby enhancing the optical performance of lens 2 and 3. Then, future research should also focus on further optimizing the design methods for meridian optical powers and investigate more effective mathematical functions or technical methods to enhance the optical performance of freeform lenses and achieve a superior design.

# Data availability statement

The original contributions presented in the study are included in the article/supplementary material, further inquiries can be directed to the corresponding author.

# Author contributions

HX: Conceptualization, Data curation, Investigation, Methodology, Software, Validation, Writing–original draft, Writing–review and editing. LM: Data curation, Investigation, Methodology, Software, Writing–original draft. XZ: Supervision, Validation, Writing–review and editing. HC: Supervision, Validation, Writing–review and editing. ZZ: Supervision, Validation, Writing–review and editing. JC: Supervision, Validation, Writing–review and editing. CW: Software, Supervision, Validation, Writing–review and editing. DZ: Supervision, Validation, Writing–review and editing. SZ: Supervision, Validation, Writing–review and editing.

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# Conflict of interest

The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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