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# Influence of diverse timescales on the evolution of cooperation in a double-layer lattice

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This paper studies the influence of diverse strategy-updating timescales on the evolution of cooperation, defection, and extortion strategies in a double-layer lattice. Individuals can adjust the frequencies with which they updating their strategies adaptively according to their fitness and interlayer information. On the basis of Fermi dynamics, we find that information sharing between the two lattice layers can effectively promote cooperative behavior in a double-layer lattice. In each lattice layer, cooperation–extortion alliances can be formed to defend against invasion by defection. We find that there exists an optimal value of the extortion factor to promote the evolution of cooperation and that the frequency of cooperation in a double-layer lattice is higher than that in a single-layer one.

#### KEYWORDS

double-layer network, cooperation, timescale variation, extortion strategy, evolutionary game theory

### **1** Introduction

The emergence of cooperation is a scientific problem widely studied in both natural and social contexts. The prisoner's dilemma (PD) game model provides a uniform framework in which this phenomenon can be studied [1]. In the PD game model, a cooperator pays a certain cost (*c*) to provide benefits (*b*) to an opponent, while a defector pays nothing, and the corresponding Nash equilibrium is mutual defection. In the traditional PD game model, the payoff of both sides depends on the strategy of the opponent, and the zero-determinant (ZD) strategy ensures that the payoff of both sides is linear [2]. One important subset of the ZD strategy is called the extortion strategy, in which it is unilaterally guaranteed that a player's own payoff is  $\chi > 1$  times that of its opponent. When the extortion strategy meets the defection strategy, both of players gain zero, and the relationship between them is neutral drifting. Hence, defection can invade an extortion population, which means that the evolution of the extortion strategy is unstable within a well-mixed population [3]. Studies have suggested that the extortion strategy can act as a catalyst to promote the emergence of cooperation in small well-mixed populations [4–7]. Therefore, the evolution of cooperation in populations based on the extortion strategy deserves further study [8–11].

Network reciprocity provides a useful mechanism for escaping the dilemma of mutual defection [12–14]. In networked games, each individual is located on a node of the underlying interactive network and competes with those neighbors that are directly connected. In the PD game, in regular spatial networks, cooperators can form tight clusters for defense from invasion by defectors [15–24]. In heterogeneous scale-free networks, cooperators can easily occupy the

hubs and establish positive feedback with their cooperative neighbors, thereby ensuring the evolution of cooperation [25–30]. In multilayer networks, the reciprocity between different layers greatly facilitates the emergence of cooperation [31–41].

There are many other mechanisms to facilitate the evolution of cooperation, such as those based on memory [42, 43] and timescales [44, 45]. The process of an evolutionary game usually involves two timescales: an interaction timescale, which describes how many times individuals play the game, and a strategy-updating timescale, which represents the frequency with which strategies are updated [46]. Most previous studies have assumed that these two timescales are identical, with individuals updating strategies immediately after playing a round of games. However, some investigations have considered cases in which the two timescales differ, which leads to a nontrivial evolutionary path of cooperation [8, 10, 47–52].

This paper studies the evolution of cooperation in a double-layer network where interactions occur on a shorter timescale than that on which strategies are updated, i.e., individuals are allowed to hold on to their current strategies and interact in several rounds of the PD game before updating these strategies. In particular, we assume that the strategy-updating timescale of an individual is dependent on both its fitness and its current strategy. In this paper, the strategy-updating timescale of each individual is associated with the performance of its current strategy in the other layer of the network in such a way that the higher the fitness of its strategy in the other layer, the longer is the time interval in which the individual is able to retain its current strategy. Under the reciprocity between the different layers of the network, the individual is reluctant to change its current strategy even if a neighbor with another strategy has a higher fitness. We study a networked evolutionary PD game in a double-layer lattice with the aim of revealing the interaction mechanism in the case of heterogeneous timescales. We first introduce our model and then present our numerical and analytical results in detail. Finally, we present the conclusions of our work.

### 2 Methods

Т

We consider the PD game staged in a double-layer lattice where each layer is a 100 × 100 square lattice with periodic boundary conditions. The two lattices are not physically connected, while their interdependence is one-to-one, and will be introduced as part of the strategy updating described below. In each layer of the lattice, individuals choose one of three strategies: unconditional cooperation (*C*), unconditional defection (*D*), or extortion ( $E_{\chi}$ ) and interact with their k = 4 von Neumann neighbors. The long-term payoff matrix of the three strategies can be obtained as follows [5]:

Here,  $\chi > 1$  is the extortion factor: the larger the value of  $\chi$ , the more

extortioners exploit their partners. In contrast to the neutral drifting relationship between extortion and defection, a cooperator can obtain a small but positive benefit from its extortionate neighbor and form a snowdrift-like relationship, i.e., the best response to the extortionate neighbor is to choose cooperation. The parameter *b* determines the benefit factor: the larger the value of *b*, the more difficult it is for cooperation to emerge. By setting b - c = 1, there are only these two parameters in the payoff matrix.

We assume that strategy updating can only be carried out between neighbors in the same layer of the lattice, rather than between networks in different layers. That is, at each step t, the individual i in the upper layer of the lattice updates its strategy according to the probability

$$p_i(t) = \frac{1}{1 + \eta_i \max(0, f_i)}.$$
(2)

Here  $f_i$  represents the fitness of individual *i*, which is calculated according to the payoff matrix. If individual *i* decides to update its strategy, it will randomly select a neighbor *j* from the four neighbors in the upper layer of the lattice and learns *j*'s strategy with probability

$$W(S_i \leftarrow S_j) = \frac{1}{1 + \exp[(f_i - f_j)/\kappa]}.$$
(3)

Here,  $S_i$  ( $S_j$ ) is the current strategy of *i* (*j*), and  $\kappa$  represents the rationality of the individual, and generally is set as  $\kappa = 0.1$  [47]. Individual *i'* in the lower layer of the lattice performs the same strategy-updating step.  $\eta_i$  is the strategy-updating timescale factor of the individual *i* and is calculated by

$$\eta_i = 1 + \max\left(0, \frac{f_i + \sum_{m \in \Gamma_i, S_m = S_i} f_m}{1 + \sum_{m \in \Gamma_i, S_m = S_i} 1}\right).$$
(4)

Here,  $\Gamma_{i'}$  is the set consisting of individual i' and its neighbors in the other layer of the lattice corresponding to *i*. It can be seen that the strategy-updating timescale factor  $\eta$  of the individual is closely related to the current strategy of that individual, and it is related to the fitness of the individual and the fitness of the current strategy in the other layer of the lattice. If the current strategy of the individual can obtain a higher fitness in the other layer of the lattice, feedback of interlayer information will make the individual tend to maintain its current strategy and delay the updating of this strategy.

Initially, each individual has an equal chance to choose one behavior from the strategies *C*, *D*, and  $E_{\chi}$ . In this paper, we perform 20 independent runs in the double-layer lattice to eliminate randomness in the process of updating strategies. Each time, we obtain the frequencies of different strategies for each layer lattice through averaging over the last 10 000 generations after the transient state of 90 000 generations. Below, we presents results and an analysis to reveal how cooperation evolves in the presence of defection and extortion strategies in the double-layer lattice.

### **3** Results

First, we study the influence of the interlayer information sharing mechanism on the evolution of the three strategies in the double-layer lattice when the extortion factor is relatively small ( $\chi$  =



#### FIGURE 1

Frequencies of cooperation, defection, and extortion strategies as functions of benefit factor *b* for an extortion factor  $\chi = 1.5$ . (A) No interlayer information sharing mechanism. (B) Information sharing between the two layers of the lattice.



1.5). Figure 1 shows the influence of the interlayer information sharing mechanism on the frequencies of the cooperation, defection, and extortion strategies. The trends of the strategy frequencies are the same in both layers, and so here we only present the results for one of them. As can be seen in Figure 1A, in the case of  $\eta = 1$ , i.e., when there is no information sharing between the two layers of the lattice, the strategy-updating timescale factor is only related to

the fitness of the individuals. With increasing benefit factor b, the frequency of cooperation rapidly drops to zero, and the frequency of defection rapidly rises to one, while the frequency of the extortion strategy is always zero, and an extortion strategy cannot exist in the network. Interestingly, when the interlayer information sharing mechanism is introduced, the frequency of cooperation is greatly promoted, as is shown in Figure 1B. As b increases, an extortion



strategy can emerge in the network. When b is large (b = 2), the cooperation and extortion strategies vanish, and defection dominates the network.

We then analyze the evolution of the average fitness  $\langle f \rangle$  and strategy frequency F over time without and with an interlayer information sharing mechanism. At first, the three strategies are randomly distributed in the network. Because the values of *b* and  $\chi$  are both small (*b* = 1.1 and  $\chi$  = 1.5), cooperators have the highest fitness, as shown in Figure 2A. In the absence of an interlayer information sharing mechanism, an individual only adjusts the strategy-updating timescale according to its own fitness. The frequency of cooperation reaches its peak quickly at around t = 20, as shown in Figure 2B. At the same time, the average fitness of cooperators in the network reaches its maximum. Since the value of  $\chi$  is relatively small at this time, extortioners tend to share payoff with cooperators, and the neighbors who encounter extortion and defection get nothing. Cooperators get a small but positive payoff from extortioners and a positive payoff from their cooperative neighbors. Hence, cooperators can invade extortionate clusters, and the extortion strategy will gradually diminish and eventually die out. When the extortion strategy dies out and cooperation faces defection alone, the average fitness of the cooperators in the network drops sharply to a negative value. Finally, cooperation dies out in the network, while defection takes over the whole network.

When the interlayer information sharing mechanism is introduced, the fitness of the current strategy in the other layer of the lattice needs to be taken into account when an individual updates its strategy. With the evolution of the time step, as is shown in Figure 2C, the average fitness of cooperators in the network becomes higher than those of extortioners and defectors. It can be seen from Figure 2D that the frequency of cooperation first increases and then decreases, the frequency of defection first fluctuates slightly and then increases, and the frequency of the extortion strategy gradually decreases. At about t = 800, cooperation and defection wane and wax, and the extortion strategy is less prominent in the network. Since the average fitness of extortion strategies in the network is positive, it can be inferred that the few extortioners that survive are primarily close to cooperators. Finally, cooperation, defection, and extortion strategies coexist in the network.

Next, we observe the evolution of strategies without interlayer information sharing through a set of strategy distribution patterns at different time intervals. Figure 3 describes the distribution of the cooperation, defection, and extortion strategies in the network when t = 1, 20, 100, and 10000. Blue, red, and green represent the cooperation, defection, and extortion strategies, respectively. Initially, as shown in Figure 3A, the three strategies are randomly mixed in the network. Cooperators with high fitness can persist and spread their cooperative behaviors to their neighbors under regulation of the strategy-updating timescale. As shown in Figure 3B, cooperation has spread to the positions originally belonging to the extortion strategy. Since cooperative pairs in the network are randomly established at this time, and their mutual support is very fragile, cooperation cannot be maintained in the absence of large cooperative clusters. Under the influence of the fast Fermi updating rules and the rationality  $\kappa$  of the individual, cooperation is gradually reduced, as shown in Figure 3C. In the absence of the extortion strategy, it is difficult for cooperation to defend against defection. In the final state, defectors occupy the whole network, as shown in Figure 3D.



represent the cooperation, defection, and extortion strategies, respectively. The time steps are (A) t = 1, (B) t = 100, (C) t = 200, and (D) t = 100, 000.



In the same way, we analyze the distribution of strategies that introduce interlayer information sharing mechanism between layers by using the spot map. At the initial time (t = 1), cooperation, defection, and extortion strategies are randomly distributed in the network, as shown in Figure 4A. Because the fitness of cooperation is high, under adjustment of the strategy-updating timescale, cooperators can persist and spread their cooperative behaviors. When t = 100 and t = 200, cooperation gradually invades the extortion strategy, as shown in Figures 4B, C. Owing to the regulation of the information sharing mechanism between layers, a few extortioners can be connected with the cooperators to survive. However, after cooperators with high fitness form an alliance with extortioners, they can effectively resist invasion by defectors. Finally, the three strategies coexist in the network, as shown in Figure 4D.

We have analyzed and compared the evolution of strategies without and with an interlayer information sharing mechanism in the case of a relatively small extortion factor. Now, we change it to  $\chi = 5.0$  to further study the influence of the extortion strategy on cooperation under adjustment of the interlayer information sharing mechanism. As shown in Figure 5A, in the absence of an information sharing mechanism, a relatively high extortion factor can greatly promote the



evolution of cooperation strategies. With increasing benefit factor b, the frequency of cooperation first decreases, then increases, and then decreases, the frequency of extortion strategy keeps increasing, and the frequency of defection first increases and then decreases sharply to zero. When  $b \ge 1.2$ , defection vanishes, and cooperation and extortion strategies coexist in the network. Comparison with Figure 1A shows that when the extortion factor is increased, extortion strategies can emerge in the network and help cooperation evolve. Reference [10] have found that in a single-layer lattice, when individuals adjust the strategy-updating timescale according to fitness under a high extortion factor, a variable strategy-updating timescale can help cooperation reduce the speed of strategy updating after a high fitness has been obtained, thus promoting the formation of a cooperation-extortion strategy alliance in the network. In this way, the frequency of cooperation can be increased. Henceforth in this paper, we will no longer consider evolution without information sharing between layers, but will focus on interlayer information feedback.

When the interlayer information sharing mechanism is introduced, with increasing benefit factor b, the frequency of cooperation first increases slightly and then decreases, the frequency of the extortion strategy increases continuously, while the frequency of defection decreases to zero, as shown in Figure 5B. When  $b \ge 1.2$ , cooperation and extortion strategies coexist in the network. As can be seen from comparison with Figure 5A, when the interlayer information sharing mechanism is introduced, the frequency of cooperation increases, while

the threshold for extinction of defection stays the same. Comparison with Figure 1B shows that with the increased extortion factor, extortion strategies can emerge in the network, and the frequency of cooperation is greatly increased, while defection cannot exist in the network when  $b \ge 1.2$ .

Next we analyze the evolution of the strategies and their pairs with time. The three strategies of cooperation, defection, and extortion can form six different pairs in the network, namely, cooperation-cooperation (C-C), cooperation-defection (C-D), cooperation-extortion  $(C-E_{\gamma})$ , defection–defection (D-D) pair, defection-extortion  $(D-E_y)$ , and extortion–extortion  $(E_y - E_y)$  pairs. Figures 6A, B show the evolution of the upper layer of the lattice, and Figures 6C, D show the evolution of the lower layer. It can be seen that the frequencies of the strategies and strategy pairs evolve similarly over time in the upper and lower layers of the network. At first, the three strategies are distributed randomly and occupy one-third of the network, as shown in Figures 6A, C. Meanwhile, as shown in Figures 6B, D, C-C, D-D, and  $E_{\chi}$ - $E_{\chi}$  pairs each account for one-ninth, and the remaining three strategy pairs C-D,  $D-E_{\nu}$  and  $D-E_{\nu}$  each account for two-ninths. Since the values b = 1.3and  $\chi = 5.0$  are both large, cooperation is invaded by the defection and extortion strategies, and therefore the frequency of cooperation decreases, while the frequencies of defection and extortion strategies increase, and those of C–C, C–D and C– $E_x$  pairs decrease. At around t =10, the rate of decline of C-C and  $C-E_{\chi}$  pairs slows down to give a stable



FIGURE 7

Strategy distribution patterns at different times in a double-layer lattice for b = 1.3 and  $\chi = 5.0$ . (A–D) Results in the upper layer of the lattice. (E–H) Results in the lower layer. The time steps are (A,E) t = 1, (B,F) t = 20, (C,G) t = 100, and (D,H) t = 10 000.



period, while the proportion of C-D pairs is still decreasing, which indicates that some individuals adopting an extortion strategy form a stable cooperation–extortion strategy alliance structure with the remaining cooperators in the network. As time passes, the cooperation–extortion strategy alliance gradually comes to occupy

part of the network and begin to spread, and hence the frequency of cooperation begins to rise, while the frequency of defection begins to decline, and the frequencies of C-C and  $C-E_{\chi}$  pairs gradually increase. Finally, cooperation and extortion strategies coexist in the lattice, while defection vanishes.

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Although the trends of the frequencies of strategies and pairs in the two lattice layers are similar, we find that the strategy distribution in the upper and lower layers of the network is asymmetrical. Figure 7 shows the strategy distribution patterns of the upper and lower layers at different time steps. Figures 7A-D show the results for the upper layer and Figures 7E-H those for the lower layer. Initially, the strategies are randomly distributed in the network, as shown in Figures 7A, E. It can be seen from the payoff matrix (1) that in the beginning, the defection and extortion strategies gain more from cooperation, and cooperation is invaded by the defection and extortion strategies. As shown in Figures 7B, F, at around t = 20, the surviving cooperators are mainly associated with extortioners. Once the fitness of a cooperator becomes high, the cooperator slows down its rate of strategy renewal and forms an alliance with an extortioner to spread across the network. At around t = 100, in the cooperation-extortion strategy alliance, the extortion strategy protects cooperation from being invaded by defection, and hence defection cannot get in touch with cooperation and gain benefit from it, while the extortion strategy on the border can resist invasion by defection, because it can gain greater benefit from internal cooperation, as shown in Figures 7C, G. Finally, as shown in Figures 7D, H, extortion and cooperation strategies coexist in the network, while defection can no longer survive in the network.

We finally study the effects of the extortion factor  $\chi$  on the frequencies of cooperation ( $F_C$ ), defection ( $F_D$ ), and extortion ( $F_{E_{\chi}}$ ) strategies for different values of the benefit factor *b*. With increasing  $\chi$ , as shown in Figure 8A,  $F_C$  changes nonmonotonically, first rising and then decreasing, and there is an optimal extortion factor to promote the evolution of cooperation. In the cases b = 1.1 and 1.3,  $F_D$  gradually decreases to zero, as shown in Figure 8B, while  $F_{E_{\chi}}$  gradually increases, as shown in Figure 8C. When b = 1.5,  $F_{E_{\chi}}$  first increases and then decreases with increasing  $\chi$ , and defection can re-emerge in the network at larger values of  $\chi$ . The choice of appropriate values for the extortion factor can promote the growth of cooperation in the double-layer lattice.

The dashed lines in Figure 8 show the results for a single-layer lattice. We find that no matter whether a lattice is single-layer or double-layer, there exists an optimal extortion factor  $\chi$  for which cooperation have the highest frequency. However, for the same value of the benefit factor *b*, the optimal value of  $\chi$  in a single-layer lattice is higher than that in a double-layer lattice, which means that in a single-layer lattice, a greedy extortion strategy is needed to resist invasion by defection. Meanwhile, we find that when the value of  $\chi$  is small, in contrast to the defection-dominant network that arises in a single-layer lattice, cooperation, defection, and extortion strategies can coexist in a double-layer lattice. At each value of  $\chi$ , the frequency of cooperation in a double-layer lattice is higher than that in a single-layer lattice. Therefore, under adjustment of the strategy-updating timescale, a double-layer lattice is more conducive to the emergence of cooperation than a single-layer lattice.

## 4 Discussion

In this paper, we have studied the effects of extortion strategies on the evolution of cooperation in a double-layer lattice. Individuals can adjust the strategy-updating timescale according to their fitness and the current performance of their strategy in the other layer of the network. Strategy updating occurs only in the same layer lattice, and interlayer information sharing will affect the speed of strategy updating. Our results show that when the extortion factors in the two layers of the lattice are the same, the trend of strategy evolution in the upper and lower layers is similar. When the extortion factors in a double-layer lattice are small, the diversity in the strategyupdating timescale, that is, enabled by the double-layer network structure greatly promotes the level of cooperation compared with what can be achieved in the absence of an interlayer information sharing mechanism. Finally, we find that the extortion factor has a nonmonotonic effect on the emergence of cooperation in the network. An appropriate value for the extortion factor can promote the evolution of cooperation in the network, and a double-layer lattice is more conducive to the evolution of cooperation than a single-layer network.

### Data availability statement

The original contributions presented in the study are included in the article/Supplementary Material, further inquiries can be directed to the corresponding author.

### Author contributions

YM: Data curation, Formal Analysis, Methodology, Writing–original draft. ZR: Data curation, Methodology, Writing–original draft. XX: Writing–original draft. ZH: Writing–original draft.

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### Conflict of interest

Author XX was employed by the company Tencent.

The remaining authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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