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# Constrained model assumptions using recent data of $\alpha$ -particle reactions on <sup>144</sup>Sm

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Analysis of the latest high-precision cross sections of  $(\alpha, \gamma)$  and  $(\alpha, n)$  reactions on <sup>144</sup>Sm below the Coulomb barrier is carried out using a consistent parameter set of the statistical model. This prevents the need to use empirical rescaling factors of either  $\gamma$  or neutron widths. Particular attention is paid to uncertainties of the calculated cross sections which are related to the accuracy of the primary data that were used to set up the consistent input parameters. The calculated cross sections are found in good agreement with the new experimental data for the <sup>144</sup>Sm $(\alpha, n)^{147}$ Gd reaction; however, the same is not true for the excitation function of <sup>144</sup>Sm $(\alpha, \gamma)^{148}$ Gd which decreases faster at incident energies below ~12 MeV. An increase of the  $\alpha$ -particle direct collective inelastic scattering at lower energies is found responsible for this decrease of the  $(\alpha, \gamma)$  reaction cross sections. The consequent lower nuclear effects may correspond to the Coulomb excitation effect assumed, although in a different manner, within the so-called " $\alpha$ -potential mystery" for the same optical-potential account of  $\alpha$ -particle absorption and emission as well.

#### KEYWORDS

nuclear reactions, cross sections, nuclear models, optical potential, nuclear level density, model calculation uncertainty bands

## **1** Introduction

Recent high-precision measurements of angular distributions of  $\alpha$ -particle elastic scattering [1] and cross sections of  $(\alpha, \gamma)$  and  $(\alpha, n)$  reactions [2, 3] on <sup>144</sup>Sm make possible an extended analysis of the related  $\alpha$ -particle optical model potential (OMP). It concerns the agreement between the experimental and statistical-model (SM) calculated cross sections for the <sup>144</sup>Sm $(\alpha, n)^{147}$ Gd reaction below the Coulomb barrier (*B*), with two recent potentials [4, 5], while the <sup>144</sup>Sm $(\alpha, \gamma)^{148}$ Gd reaction data cannot be reproduced with the same accuracy [3]. However, the latter reaction has been most important for the validation of the  $\alpha$ -particle OMP since its first measurement with a singular energy precision [6]. Thus, it was the first one concerned regarding the ' $\alpha$ -potential mystery' of an OMP that accounts for  $\alpha$ -particle both absorption and emission [7]. A key issue in this respect has been the Coulomb excitation (CE) within the former process. Specific studies on <sup>144</sup>Sm have also evaluated the sensitivity of SM results to various input parameters for these reactions [8, 9] as well as their significance [1–3].

Nevertheless, the knowledge of the  $\alpha$ -particle OMP has greatly impacted nuclear astrophysics and fusion technology (e.g., [10, 11]). Thus, it motivated the analysis of the new data in addition to the earlier ones involved to obtain the OMP parameter set [4]. This potential was established and verified using no empirical rescaling factors of either  $\gamma$  or neutron widths within reaction data analysis but SM consistent parameters [11–17] found by

analysis of other independent data [18]. Nevertheless, the uncertainties of these primary data may have effects on the calculated reaction cross sections that could be better assessed within the increased accuracy of the recently measured cross sections [2, 3].

# 2 Models and methods

# 2.1 Consistent setting up and confirmation of $\alpha$ -particle OMP

Several steps were needed to set up the  $\alpha$ -particle OMP of Ref. [4]. First, only the  $\alpha$ -particle elastic scattering on nuclei with the mass number  $A \sim 100$ , at energies E < 35 MeV, was analyzed above B [19]. Question marks related to the rest of SM parameters needed to calculate cross sections of reactions with either incident or emitted *a*-particles were thus avoided. Moreover, a double-folding model (DFM), with an explicit treatment of the exchange component, was initially used in a semi-microscopic approach. A dispersive correction to the microscopic DFM real potential was also considered, along with a phenomenological imaginary part that was energy-dependent. A full phenomenological analysis then focused on the same angular distributions, without changing the already determined imaginary part, provided the local OMP parameter sets corresponding to each data set. Lastly, a regional OMP with energy-dependent average mass and charge parameters was derived for further use in SM calculations.

Additional semi-microscopic and phenomenological analyses were carried out for the target nuclei with *A* between 50 and 120 and  $\alpha$ -particle energies of 13–50 MeV [20]. However, an SM assessment of the cross sections of  $\alpha$ -induced reactions below *B*, available for the same *A* range and energies below 12 MeV, was included. Similar consideration for the heavy nuclei (*A* between 121 and 197) also resulted in different results for the energy-dependence eventual change below *B* of the surface imaginary potential depth  $W_D$  and the volume imaginary potential depth  $W_V$  [21]. Thus, there were no issues in the extrapolation to lower energies of  $W_V$  from analysis of the  $\alpha$ -particle elastic scattering above *B*, while  $W_D$  presents a distinct case.

The  $\alpha$ -particle elastic scattering analysis, above *B*, provides a decrease of  $W_D(E)$  with the energy increase. However, its extrapolation below B would contradict the strong increase in the number of open reaction channels of the compound-nucleus (CN). The related trend was well described by a minimum constant value until an energy limit  $E_1$ , followed by a linear increase of  $W_D(E)$  up to a second energy limit  $E_2$  corresponding to  $0.9^*B$  [20]. Only then, a decrease in  $W_D$  with increasing energy is in order, until its cancellation at a few tens of MeV [21], along with the  $W_V$ continuum increase. Both are considered by the parameters of the OMP, especially the more inelastic channels which are opened by the incident energy increase. These channels are open due to  $\alpha$ -particle interactions with the target nucleus on the surface region, firstly, and then within its whole volume. Thus, the data analysis of the  $\alpha$ -induced reactions determines the increasing side of  $W_D$  while the elastic-scattering data constrain its decrease at higher energies.

Finally, the updated parameter set [4] for  $A\approx 45-209$  took advantage of the new measured data, including their enlarged accuracy, as well as of an improvement for the well-deformed nuclei (152<A<190). This OMP has described successfully, without further parameter changes, most of the recently published ( $\alpha$ ,x) data [11, 13–17] and elastic–scattering angular distributions [22–24]. Moreover, a similar data account has finally been proven for  $\alpha$ -emission from excited nuclei in nucleon-induced reactions on nuclei with  $A\sim 60$  [16, 17] and  $A\sim 90$  [11], provided that (i) consistent parameter sets are used, (ii) additional consideration is given to the ( $n,\alpha$ ) pickup direct reactions to the low–lying states of the residual nuclei, and (iii) all competitive reaction channels and eventually isotopic chains of neighboring elements have been considered.

The above review of the OMP [4] setting up is twofold. The energy limits  $E_1 = 13.896$  MeV and  $E_2 = 16.863$  MeV for <sup>144</sup>Sm are are within the incident–energy range ~10–20 MeV of the recent measurements [1–3]. However, all energies of the ( $\alpha$ , $\gamma$ ) data are just below  $E_1$ , whereas the ( $\alpha$ ,n) data are mainly above it as well as centered on  $E_2$ . Therefore, the former data set constrains the parameters of the OMP [4] triggered by the reaction–data analysis, and the latter is equally related to the setting of the OMP based on the two types of data analysis.

It is noteworthy that, at the time, the former <sup>144</sup>Sm( $\alpha, \gamma$ )<sup>148</sup>Gd data set [6] was the only one available below  $E_1$  for target nuclei with  $A \ge 130$ . Based on this analysis, the constant  $W_D$  of 4 MeV at energies  $\le E_1$ , for A < 130 nuclei [20], was replaced with (2.5 ±1) MeV and a footnote states " $W_D = 3.5$  for A < 130 while  $W_D = 1.5$  fits better the data for A > 130" [21]. However, new ( $\alpha, \gamma$ ) data on <sup>120</sup>Te and <sup>141</sup>Pr, even fully below  $E_1$ , were driven back to  $W_D = 4$  (+0.5/-2.5) MeV [4]. Therefore, an uncertainty band related only to  $W_D$  limits at lower energies has covered both ( $\alpha, \gamma$ ) data sets [2, 6]. Nevertheless, a parallel assay of the uncertainties of calculated cross sections for the reactions on <sup>144</sup>Sm below and near B, particularly related to the uncertainty of the primary data used to obtain the consistent parameters, remains of interest.

#### 2.2 Parameters of the statistical model

The SM analysis and the assessment of direct–interaction (DI) collective inelastic–scattering cross sections were recently carried out by using the same models and codes [25, 26] within a local approach [4, 27] and excitation energy grid with an equidistant binning  $\geq 0.2$  MeV. Therefore, only different or additional aspects are discussed hereafter.

Similar parameters of (i) back-shifted Fermi gas (BSFG) [28], (ii) OMP parameter sets [4, 29], and (iii) radiative strength functions (RSF) [30, 31] were used to account for the nuclear level density (NLD) and particle and  $\gamma$ -ray transmission coefficients, respectively. Particularly, the NLD and RSF consistent parameters were established or validated in advance with distinct data analysis.

The number and maximum excitation energy of the low-lying discrete levels [32] and level density parameters are given in Table 1 for the main SM reaction channels. They are followed by the data used for setting up the corresponding NLD parameters, such as the low-lying levels fitted along with, if known, the *s*-wave nucleon–resonance spacings  $D_0^{exp}$  [33] in  $\Delta E$  energy range [34]

TABLE 1 Low-lying levels number  $N_d$  up to excitation energy  $E_d^*$  [32] used in SM calculations,  $N_d$  and s-wave nucleon-resonance spacings<sup>a</sup>  $D_0^{exp}$  (with uncertainties given in units of the last digit in parentheses) in the energy range  $\Delta E$  above the separation energy S, for target-nucleus g.s. spin  $I_{0r}$ , fitted to obtain BSFG leveldensity parameter a and g.s. shift  $\Delta$  (for a spin cutoff factor corresponding to a variable moment of inertia [48] between half and 75% of the rigid-body value, from g.s. to S, and reduced radius  $r_0 = 1.25$  fm).

Nucleus	N <sub>d</sub>	Eð	Fitted level and resonance data					а	Δ
			N <sub>d</sub>	E <i>ă</i>	$S + \frac{\Delta E}{2}$	I <sub>o</sub>	$D_0^{\exp}$		
		(MeV)		(MeV)	(MeV)		(keV)	(MeV <sup>-1</sup> )	(MeV)
<sup>143</sup> Sm	17	1.990	11	1.748				14.0	0.36
<sup>144</sup> Sm	15	2.729	21(2)	2.883				15.5(4)	1.40(1)
<sup>145</sup> Sm	25	2.050	25	2.050	6.757	0	0.770(45)	14.35(4)	0.34(3)
<sup>147</sup> Eu	18	1.244	18	1.244				17.30	-0.03
<sup>147</sup> Gd	15	1.702	18(2)	1.797				17.3(6)	0.52(1)
<sup>148</sup> Gd	23	2.700	20(2)	2.633				17.0(6)	1.30(2)

<sup>a</sup>RIPL-3 [33] if not otherwise mentioned.



FIGURE 1

Comparison of measured RSFs of <sup>148,149,150,151,152,153,154</sup>Sm and <sup>152,154</sup>Gd nuclei [36] and calculated sum of *M*1-radiation SLO model (short dotted) and either *E*1-radiation SLO (dash-dot-dotted), GLO (dash-dotted) models, or the sum of upbend *M*1 component and EGLO (solid) models, with the resonance parameters for <sup>150</sup>Sm nucleus ([31], Table III) for <sup>148</sup>Gd nucleus. The corresponding average *s*-wave radiation widths  $\Gamma_y$  (in meV), deduced from systematics [33] as well as calculated with the above models, are also shown.

above the separation energy *S*, for the ground state (g.s.) spin  $I_0$  of the target nucleus. The level-density parameter *a* and g.s. shift  $\Delta$  thus obtained were then involved within SM calculations at excitation energies above the low-lying discrete levels.

The smooth-curve method has been used for nuclei without resonance data [35]. Thus, an average of the fitted *a*-values for nearby nuclei [4] was employed to obtain only the  $\Delta$  value by

fitting the low-lying levels. Table 1 also shows the cumulative uncertainty of the NLD parameters corresponding to the incertitude of the above-mentioned data involved within their setting up. Larger uncertainties of the averaged *a*-values are due to the spreading of the results of  $D_0^{exp}$  fit. The NLD effects on the calculated cross sections are assessed in Section 3 using these uncertainties.

The transmission coefficients were obtained using the global OMPs of either Koning and Delaroche [29], for nucleons, or [4] for  $\alpha$ -particles. Moreover, the same parameters provided the DI collective inelastic–scattering cross sections through the distorted-wave Born approximation (DWBA) method and the DWUCK4 code [26]. A more detailed discussion follows in Section 2.3.

The y-ray transmission coefficients were provided by the recently available widespread RSFs systematics [31, 36]. However, there is no related RSF analysis for the neutron-poor Gd isotopes similar to those in the rare-earth region for the <sup>148,149,151,153</sup>Sm isotopes [30, 37]. The comparative survey of the RSF data [36] of lighter Sm and Gd isotopes shown in Figure 1 suggested an apparent mass-and charge-dependency. It may support a prediction for the compound nucleus 148Gd based on measured RSF data for <sup>148,149</sup>Sm nuclei. Therefore, we employed the giant dipole resonance (GDR) parameters of Kawano et al. for <sup>150</sup>Gd [31] within the former Lorentzian (SLO) [38], generalized Lorentzian (GLO) [39], and enhanced generalized Lorentzian (EGLO) [40] models for the electric-dipole RSF. Moreover, the SLO model and the additional M1 upbend parameters that were recently found to describe the RSF data for 151,153Sm nuclei [37] were used. A nuclear-temperature EGLO parameter  $T_f$ =0.4 MeV, which is between the values found for Sm and Gd isotopes (Table I of Ref. [4]), was considered appropriate.

We obtained a suitable EGLO account of the RSF measured data of <sup>148,149</sup>Sm nuclei [30, 36] as well as the averaged *s*-wave radiation widths  $\Gamma_{\gamma}$  [33]. The dependency of the  $\Gamma_{\gamma}(S)$ , for the even-even nuclei [33], also provided an estimation of this width and its uncertainty for <sup>148</sup>Gd nucleus as (88 ± 20) meV. Figure 1 shows an RSF uncertainty band corresponding to these  $\Gamma_{\gamma}$  estimated limits to match almost all data measured either above or below *S*. The effect of this uncertainty on the calculated reaction cross sections is also concerned hereinafter. Nevertheless, the SLO and GLO models resulted in different RSF energy dependencies below *S*, as well as larger  $\Gamma_{\gamma}$ -values well beyond the systematic uncertainty (Figure 1).

#### 2.3 Direct collective inelastic scattering

The  $\alpha$ -particle OMP [4] was employed to get the DI collective inelastic scattering with the DWUCK4 code [26] using the corresponding deformation parameters of the first 2<sup>+</sup> and 3<sup>-</sup> collective states [41, 42]. The DI cross-section was then subtracted from the  $\sigma_R$  to obtain the CN cross-section for further SM calculations.

A note should be added concerning the CE discussion given in Sec. II of Refs. [4, 13, 15]. Because the inelastic–scattering cross section could be strongly affected by the Coulomb component of the interaction between the projectile and target nucleus, we used a value COUEX = 1.0 in the DWUCK4 calculations [26]. Actually, a previous DWBA analysis pointed out the issue of the collective form factors corresponding to (i) either CE or nuclear excitation (NE) alone, as well as their coherent interference (NE+CE) (e.g., [43]), and (ii) integration radii  $R_{max}$  of either 15 or 30 fm, which are typical to the short–range nuclear interactions [26] and the long-range Coulomb field, respectively [44]. The largest contributor to the CE cross sections were partial waves larger than those contributing

to the optical model total–reaction cross section  $\sigma_R$ . Simultaneously, the assessment of  $\alpha$ -particle DI inelastic scattering should include the effects of the CE+NE interference corresponding to an integration radius that is typical of the short–range nuclear interactions (~15 fm).

We obtained  $\alpha$ -particle DI inelastic–scattering cross sections up to ~9% of  $\sigma_R$  for incident energies of ~14 MeV. Above 20 MeV, these cross sections slightly decreased to 2% of  $\sigma_R$ . The corresponding decrease of  $\sigma_R$  was then considered within the SM analysis of various reaction channels.

## 3 Results and discussion

#### 3.1 The $(\alpha, \gamma)$ reaction

Figure 2 provides an initial comparison of the measured cross sections of the reactions ( $\alpha$ , $\gamma$ ) [2, 6] and ( $\alpha$ ,n) [3] on <sup>144</sup>Sm, and calculated results obtained with the  $\alpha$ -particle OMP [4] and the above–mentioned model parameters and assumptions. It includes the calculated  $\alpha$ -particle  $\sigma_R$ , to highlight the weight of each reaction channel at various energies.

The recent  $(\alpha, \gamma)$  measured data [2], which had higher accuracy than previous ones [6], are described within so small error bars only at incident energies above 12 MeV. Otherwise, there is an overestimation which increases with the energy lowering, until a factor of ~2 around 10.5 MeV. This trend, at incident energies where the  $(\alpha, \gamma)$  cross section equals  $\sigma_R$ , can be explained neither by the RSF option (Figure 2A) nor the incertitude of the NDL parameters given in Table 1 for the compound nucleus <sup>148</sup>Gd (Figure 2C).

On the other hand, at energies where the  $\alpha$ -capture becomes a minor reaction channel, the uncertainty band of the calculated cross section corresponding to the systematic  $\Gamma_{\gamma}$  [33] incertitude is similar to the error bar of the highest–energy measured data (Figure 2A). Moreover, a replacement of the EGLO strength function with the GLO and then SLO forms leads each time to additional overestimation of the same size.

A similar uncertainty band is related, at the same energies, to the incertitude of the NLD parameters for the compound nucleus <sup>148</sup>Gd (Figure 2C). Another uncertainty band corresponds to NLD of the residual nucleus <sup>147</sup>Gd at incident energies well above the ( $\alpha$ , n) reaction threshold for the continuum population of this nucleus (Figure 2D). Altogether, below the incident energy of ~12 MeV, no RSF and NLD effects may correspond to the increasing overestimation of the ( $\alpha$ , $\gamma$ ) data.

#### 3.2 The $(\alpha, n)$ reaction

The accurate most recently measured ( $\alpha$ , *n*) cross sections [3] are well described within their small error bars (Figures 2B, D). Only the two lowest-energy points, at 13–14 MeV incident energies, are accounted for at the lowest limit of the experimental errors. However, an interplay of the ( $\alpha$ , $\gamma$ ) and ( $\alpha$ ,*n*) cross sections for various RSF occurs solely at these energies. Thus, while the EGLO model provides lower cross sections for the former reaction, the reverse occurs with the usual SLO model. On the other hand, the uncertainty band of only ~10% for ( $\alpha$ , *n*) calculated cross sections at



#### FIGURE 2

Comparison of measured [1–3, 6] and calculated ( $\alpha$ ,  $\gamma$ ) and ( $\alpha$ , n) reaction (solid curves) as well as  $\alpha$ -particle total-reaction cross sections (dotted curves), for the target nucleus <sup>144</sup>Sm and  $\alpha$ -particle OMP [4], vs. either  $\alpha$ -particle laboratory energy (bottom) or ratio of center-of-mass energy to Coulomb barrier *B* [49] (top). The excitation functions calculated by using *E*1-radiative strength functions of the SLO (dash-dott-dotted), GLO (dash-dotted), and EGLO (solid curves) models are shown at once with the corresponding average *s*-wave radiation widths  $\Gamma_{\gamma}$  (in meV). The displayed uncertainty bands correspond to (**A**, **B**) the  $\Gamma_{\gamma}$  error bar deduced from systematics [33], and (**C**, **D**) the error bars of the level–density parameter *a* (Table 1) of the CN <sup>148</sup>Gd (light–gray), and residual nucleus <sup>147</sup>Gd (gray).

these energies, related to the systematic  $\Gamma_{\gamma}$  incertitude, is hardly visible in Figure 2B. Meanwhile, the results of the GLO and SLO models decrease by ~17% and 36%, respectively.

This case provides a sound motivation for further study of the RSF modeling and competition between the capture and particle emission. At incident energies near 13 MeV, even lower RSF values would provide a better data account for both the  $(\alpha, \gamma)$  and  $(\alpha, n)$  calculated cross sections. However, a further decrease of the RSF for the compound nucleus <sup>148</sup>Gd is less probably on the basis of the RSF data available for neighboring nuclei (Figure 1).

The comparison of the  $\sigma_R$  values which were deduced through the elastic–scattering analysis at incident energies between 16 and 20 MeV [1] and the calculated results using the OMP [4] shows an agreement at the highest–energy point but a significant underestimation at the lower energies (Figure 2B). A previous note [1] on this measured and calculated  $\sigma_R$  difference concerned the fact that the setting up of the OMP [4] included the fit of a similar angular distribution measured at the same energy of 20 MeV. Nevertheless, the present suitable account of the more accurate ( $\alpha$ , n) cross sections at these incident energies, which amount to 97%–90% $\sigma_R$ , supports additionally the  $\alpha$ -particle OMP [4]. Moreover, a suitable account of elastic–scattering angular distribution by the same OMP was proven for another semi–magic nucleus <sup>140</sup>Ce at a comparable lower energy of 15 MeV [Figure 8(d) of Ref. [4]].

# 3.3 Increased Coulomb effects on DI inelastic scattering

The faster decrease of the  $(\alpha, \gamma)$  cross sections below ~12 MeV could be associated only with the above–mentioned weighting of the



 $\alpha$ -particle collective inelastic–scattering cross sections. Their maximum around 9% of  $\sigma_R$  at incident energies near 14 MeV, followed by a decrease to 2% above 20 MeV, is in line with the agreement of the measured and calculated ( $\alpha$ , $\gamma$ ) and ( $\alpha$ ,n) cross sections at these energies. However, following the dependency of the DWBA outcome on the integration radius  $R_{\text{max}}$ , we found that the newly measured ( $\alpha$ , $\gamma$ ) cross sections, at the incident energies

newly measured  $(\alpha, \gamma)$  cross sections, at the incident energies decreasing from 12 to 10.5 MeV, correspond to DI inelastic-scattering cross sections increased by the use of  $R_{\text{max}}$ values rising from 15.5 to 17 fm. Taking into account the agreement already provided by the use of the value  $R_{\text{max}} = 15$  fm at the energies >13 MeV it results that a simple

the value  $R_{\text{max}}=15$  fm at the energies  $\geq 13$  MeV, it results that a simple linear dependency of the form  $R_{\text{max}}(\text{fm})=25.4-0.8E$  is leading to suitable collective DI inelastic–scattering and  $(\alpha, \gamma)$  reaction cross sections also at the incident energies between 10.5 and 13 MeV (Figure 3). Thus, the excitation function of the  $(\alpha, \gamma)$  reaction which formerly overlapped  $\sigma_R$  below ~12 MeV (Figures 2A, C), has now a distinct trend. However, while  $R_{\text{max}}=17$  fm has currently been used down from the energy of 10.5 MeV, its form below the energy range of the new  $(\alpha, \gamma)$  reaction data [3] should be clarified by further analysis.

The increase of the integration radius beyond the typical 15 fm value to the short-range nuclear interactions, with the decrease of the  $\alpha$ -particle energy, may correspond to nuclear effects decreasing [43]. Therefore, it could be a Coulomb excitation effect, as was assumed although in a different manner [7]. Nevertheless, the above  $R_{\max}(E)$  dependency is a form used to describe only the recently measured ( $\alpha$ , $\gamma$ ) data at  $\alpha$ -particle energies above 10.5 MeV [2].

#### 4 Conclusions and outlook

An analysis of the latest high–precision measured cross sections of  $(\alpha, \gamma)$  and  $(\alpha, n)$  reactions on <sup>144</sup>Sm [2, 3], below the Coulomb barrier, is carried out using a consistent parameter set of the statistical model. Therefore, empirical rescaling factors of either  $\gamma$  or neutron widths are no longer involved. Moreover, in addition to previous studies on SM sensitivities [1–3, 8, 9], particular attention was paid to the uncertainties of the calculated cross sections that correspond to the accuracy of the primary data used to set up the consistent input parameters. The experimental and calculated cross sections of <sup>144</sup>Sm $(\alpha, n)$ <sup>148</sup>Gd reactions agreed only at energies above 12 MeV. This leaves open the question of suitable parameter or model assumptions.

First, we considered that the calculated cross–section accuracy cannot exceed that of the model parameters and, consequently, of the data used for their setting. However, we found minor nuclear–level density effects within SM analysis, with respect to the uncertainty of either the average level–density parameter *a* values, based on both the spreading and the error bars of the fitted  $D_0^{exp}$  for nuclei with known resonance data, or the fitted low–lying discrete levels.

A similar case was that of the RSF impact. The RSF data as well as the average *s*-wave radiation widths  $\Gamma_{\gamma}$  deduced from systematics [33] were considered in the absence of the corresponding data for the compound nucleus <sup>148</sup>Gd. An interplay of the calculated cross sections of ( $\alpha$ , $\gamma$ ) and ( $\alpha$ ,n) reaction was found near the threshold of the ( $\alpha$ ,n) reaction. Thus, while the EGLO model provided lower cross sections for the ( $\alpha$ , $\gamma$ ) reaction, the reverse corresponds to the usual SLO model. This case is significant owing to the scarce attention paid to the RSF assessment within  $(\alpha, \gamma)$  reaction studies, leading to a distinct conclusion on the other important SM parameter which is the  $\alpha$ -particle optical potential. For the sake of completeness, one may note the claimed need for OMPs correction factors [45, 46], at once with no proof of the accompanying RSF. It thus fully explains the disagreement with the previous conclusions for the same reactions [4, 13–15, 20, 47], which followed a former RSF detailed analysis.

Because we found no RSF and NLD effects at the origin of the  $(\alpha, \gamma)$  data overestimation, which is increasing below the incident energy of ~12 MeV, further consideration was given to the DWBA analysis of the  $\alpha$ -particle direct inelastic scattering. The faster decrease of the  $(\alpha, \gamma)$  reaction cross sections below ~12 MeV is described by means of an increase of the corresponding integration radius at lower  $\alpha$ -particle energies, from the typical value of 15 fm (corresponding to the short-range nuclear interactions) at the incident energy of 13 MeV, to 17 fm at 10.5 MeV. This increase of the integration radius with the decrease of the  $\alpha$ -particle energy may correspond to nuclear effects decreasing. Therefore, it could be a Coulomb excitation effect, as was assumed although in a different manner [7], within the so-called " $\alpha$ -potential mystery" for the same optical-potential account of  $\alpha$ -particle absorption and emission as well. However, the integration-radius form below the energy range of the measured cross sections of the  $(\alpha, \gamma)$  reaction [3] should be clarified by further analysis. This is important for both nuclear astrophysics and fusion technology.

#### Data availability statement

The raw data supporting the conclusion of this article will be made available by the authors, without undue reservation.

# Author contributions

All authors listed have made a substantial, direct, and intellectual contribution to the work and approved it for publication.

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## Conflict of interest

The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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