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A circularly polarized folded reflectarray antenna using a polarization-sensitive linear-to-circular polarization converter

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This work proposes a low-profile circularly polarized folded reflectarray antenna (CPFRA). Compared to traditional CPFRA that comprise the main reflectarray, a polarization grid (PG), and a linear-to-circular polarization (LP-CP) converter, the proposed CPFRA utilizes a polarization-sensitive LP-CP converter that plays the roles of both PG and LP-CP converter to minimize the CPFRA profile. One period of the polarization-sensitive LP-CP converter consists of an LP and a CP patch on the bottom and top layer of the substrates, respectively, which are connected by a metalized via. Due to its frequency-selective characteristic, the polarizationsensitive LP-CP surface can simultaneously reflect the x-polarized waves and transfer the received y-polarized waves into the CP state. A 1-bit unit cell at the bottom layer is adopted for polarization conversion and phase shift. A planar patch antenna is integrated as the primary feeding source. A high-gain circularly polarized folded reflectarray antenna at the X-band is designed, fabricated, and measured. Both simulated and measured results demonstrate the advantages of high gain and a lower profile of the proposed CPFRA compared to those in its traditional counterparts.

KEYWORDS

polarization-sensitive, linear-to-circular polarization (LP-CP) converter, circular polarization, folded reflectarray antenna (FRA), low-profile

Introduction

Printed reflectarrays (RAs) consist of numerous planar elements for phase compensation and a feeding source assembled over the planar elements at some distance. RA development has attracted increased attention in recent years due to the high gain, planar structure, and cost-effectiveness of RAs compared to traditional reflector antennas [1-6]. However, the common RA design has a high profile, including a bulky feeding horn and a distance between the feeding source and array that depends on the focal-length-to-diameter (F/D). The use of a low-profile antenna as the feeding source can reduce the overall profile [7, 8]. A folded reflectarray (FRA) was proposed to reduce the RA profile [9-14]. The FRA consists of a main reflectarray and a polarizer grid (PG) where the incident wave is reflected in one polarization and transmitted in the other polarization. The main reflectarray provides a phase shift to the suitable phase in the farfield zone and twists the polarization by 90°. Compared to that of traditional RAs, the profile of FRAs is reduced by one-half focal length (F). Based on this low-profile feature, various FRAs have been designed. The wideband polarization rotating metasurface (PRM) was used to design the wideband FRA [14-16]. Moreover, a sub-wavelength element was also used to improve RFA bandwidth [17]. A dual-band FRA was proposed for the downlink and uplink of VSAT links [18]. For beam-scanning applications, FRAs have been developed with reconfigurable beams [10, 19]. An FRA with a high-gain filtering function was recently reported [20], in which a polarization-sensitive frequencyselective surface (FSS) was used to replace the polarization grid of the transitional RFA.

Satellite communications demand high-performance antennas with high gain that are also circularly polarized (CP) and with a low profile [21]. CP RAs with high profiles were proposed in earlier works [22, 23]. FRAs can easily realize the high-gain and CP performance. Unfortunately, CPFRA is hard to realize as the polarization-selective polarization grid (PG) is on the top layer of FRAs. Metasurfaces can powerfully manipulate electromagnetic waves, including those of polarization, with easy fabrication and low costs [24–28]. Therefore, there is a simple method to design the CP antenna by locating the LP-CP converter or metasurface on the LP antenna [29–31]. Recently, CPFRA was achieved by locating the LP-CP converter on the top layer, with a suitable distance to the PG [32, 33], which increased both the FRA profile and assembly complexity.

The present work describes a polarization-sensitive LP-CP converter with a dual function to replace the PG and traditional LP-CP [32, 33]. The planar antenna is integrated as a primary source. Compared to traditional FRAs, it showed satisfactory performance with a lower profile.

Antenna design

Design concept

As shown in Figure 1A, the traditional CPFRA is composed of the polarization-insensitive LP-CP converter

on the top layer to covert the LP plane wave to the CP wave. The main reflectarray can twist the x-polarized wave to y-polarization. The phase compensation is also provided by the main reflectarray for the focusing director, transforming the spherical wave into a plane wave. The distance between the PG and the LP-CP converter should be carefully selected for optimal performance. Nevertheless, the profile is inevitably increased as a consequence. To reduce the profile, the dual functions of LP-CP and PG can be integrated by a polarization-sensitive LP-CP converter, as shown in Figure 1B.

Design of the polarization-sensitive LP-CP converter

The unit cell of the LP-CP converter is shown in Figure 2. It consisted of an LP and a CP patch that are connected to a metalized via-hole. Both patches and the ground layer are printed on surfaces of two substrates (Rogers 4003C) with a height of 1.524 mm, a relative permittivity of 3.5, and a loss tangent of 0.0027. The prepreg RO4450F with a relative permittivity of 3.7 and a thickness of 0.1 mm is adopted between the two dielectric substrates for integrated design. The top-layer metallic structure is shown in Figure 2B. Two corners of the patch are truncated, and one slot is embedded to separate two degenerate modes for CP radiation. As shown in Figure 2C, a circular clearance is used to void the metalized via-hole connecting to the ground. An LP patch with two slots is etched on the bottom layer for receiving LP waves, as shown in Figure 2D. The LP and CP patches and their interconnection work in an antenna-filter-antenna topology. It can receive the LP wave from the main reflectarray on the bottom layer and then transmit it to the CP patch on the top layer.

The CST-WMS with periodic boundary conditions was used to study the properties of the unit cell. Figure 3 shows the reflection coefficients of the polarization-sensitive LP-CP converter under different oblique incidences with x-polarization. The reflection coefficients (Rxx) were larger than -0.5 dB under different incident angles in the X-band. Therefore, the polarization-sensitive LP-CP converter can fully replace the PG, reflecting most of the incident waves with x-polarization. Figure 4 shows the reflection coefficients and axial ratios (ARs) under normal incidence waves with y-polarization, demonstrating a reflection coefficient better than -10 dB at 9.3-10.5 GHz. Figure 5A shows the transmission coefficients of the unit cells under the incidence wave with y-polarization. The magnitudes of Txy and Tyy were -3.3 dB, with a phase difference of 90° at 10.1 GHz; thus, a circular polarization wave was obtained with the y-polarization incident wave at



Topology of traditional and proposed CPFRAs. (A) Traditional CPFRA. (B) Proposed CPFRA.





FIGURE 3

Simulated reflect coefficients of the polarization-sensitive LP-CP converter excited by x-polarized wave at different incidence angles.



approximately 10.1 GHz. As shown in Figure 5B, the polarization efficiency of y-polarization to left-handed circular polarization (LHCP) was >0.94 at 9.8–10.3 GHz. Therefore, the polarization-sensitive LP-CP converter effectively performed the functions of the PG and the polarization-insensitive LP-CP converter. The physical properties of the LP-CP converter can be

described by the ellipticity and azimuth rotation angle, as defined by [34]:

$$\theta = \frac{1}{2} \left(\arg(T_{++}) - \arg(T_{--}) \right)$$
(1)

$$\eta = \arctan \frac{|T_{++}| - |T_{--}|}{|T_{++}| + |T_{--}|}$$
(2)

where T++, T-- are the transmission coefficients for RHCP and LHCP waves, respectively. The ellipticity and azimuth rotation angle of the proposed LP-CP converter under the normal incident wave are plotted in Figure 6. The ellipticity and azimuth rotation angle are 45<u>o</u> and 180<u>o</u> at 10.1GHz, respectively, which represent a pure CP radiating wave. This result is inconsistent with that shown in Figure 5B.

1-Bit phase shift unit cell with 90-degree polarization twisting

An easily designed 1-bit unit cell is used in the main reflectarray to provide phase compensation and polarization twisting. The geometry of the 1-bit phase shift unit cell for the main reflectarray is shown in Figures 7A,B. The two states of unit cells were designed based on the Rogers 4003, with a thickness of 1.524 mm and a relative permittivity of 3.55. The 0°state unit cell consisted of a circular patch with a stub, rotating 45°anticlockwise. The 180°-state unit cell was obtained by rotating the 0°-state unit cell clockwise by 90°. According to the theory in [35], a 180° phase difference exists between the two states. The simulated S-parameters of the two-state unit cells are plotted in Figure 7C. The reflection coefficients of the two unit cells under the normal incidence wave with x-polarization (Rxx) are better than -10 dB and the transmission coefficients of x-to y-polarization (Ryx) are approximately -0.25 dB in the range of 9.5-10.42 GHz. The simulated phase of the two-unit cells is shown in Figure 7D, with a phase difference of 180°. To analyze the angle stability, the reflection and transmission coefficients of unit cells were simulated under an oblique incident wave at 30° (Figure 7E,F). Figures 7E,F shows that the reflection coefficients are also better than -10 dB, while the phase difference of the two units maintains the stability of 180° at the operating frequency band.

Design of the circularly polarized folded reflectarray antenna

As shown in Figures 8A, a low-profile and wideband microstrip antenna coupled with parasitic patches was designed as the primary source [36] and could be easily integrated into the bottom layer of the main reflectarray.



200 40 - 00 Azimuth rotation angle 100 20 Ellipticity 0 0 -20 -40 -200 10.00 10.50 9.75 10.25 9.50 Frequency (GHz) FIGURE 6 Ellipticity and azimuth rotation angle of the LP-CP converter.

The total size of the feeding source, replacing the area of 3×2 unit cells of the main reflectarray, was $42 \text{ mm} \times 28 \text{ mm}$. A coaxial probe was used to excite the microstrip antenna. The layout and dimensions of the microstrip antenna are also shown in Figure 8A. Simulated |S11| is shown in Figure 8B, while the normalized radiation pattern at 10.1 GHz is shown in Figure 8C. The microstrip antenna was well matched from 9 to 10.5 GHz, with an |S11| below -10 dB.

The main reflect array consists of 19×20 elements and a total size of 266 mm \times 280 mm. The focal-length-todiameter (F/D) was set to 0.96, with the distance between the main reflectarray at the bottom layer and the LP-CP converter at the top layer set to half of the focal length. The total height of the antenna was $139.78 \text{ mm} (4.7\lambda@10\text{ GHz})$, while the distance between the main reflectarray at the bottom layer and the LP-CP converter at the top layer was 135 mm. As shown in Figure 8D, the direction of the CPFRA radiation beam xwas along the z-axis. The phase distributions of the main reflectarray are shown in Figure 8D. To implement the phase shown in Figure 8D by using the 1-bit unit cell, it is discretized by using the two-phase states of 0° and 180°. The discretized phase distribution is illustrated in Figure 8E.

Fabrication and measurements

Figure 9A shows the CPFRA prototype. Four plastic columns are used to support the main reflectarray at the bottom layer and the polarization-sensitive LP-CP converter. The feeding source of the microstrip antenna is located at the center of the main reflectarray with the phase implemented, as shown in Figure 9B. The top and bottom sides of the LP-CP converter are shown in Figures 9C and D, respectively. As shown in Figure 10A, the simulated and measured $|S_{11}|$ are better than -10 dB. Due to the fabrication tolerance, a tiny frequency shift of reflection zero is observed between these two results. The measured gain was approximately 21 dBic, which is close to the simulated result with a modest gain loss (Figure 10B). The measured and simulated ARs are also plotted in Figure 10B. A frequency shift was observed between the measured and simulated results. The simulated -3 dB AR bandwidth was 9.8-10.3 GHz. The simulated and measured normalized radiation patterns of the CPFRA at 10 GHz in xzand yz-plane are plotted in Figure 11. The simulated



and measured LHCP radiation patterns were consistent with each other in these planes. Finally, the normalized radiation gain of the RHCP (cross-polarization) was less than -15 dB.

The results of performance comparisons between other CP reflectarrays (CP-RA) and the CPFRA are shown in Table 1. Compared to the CPFRA in [32], the device described in the present work reduced the number of





Prototype of the proposed CPFRA. (A) Perspective view. (B) Top view of the bottom layer. (C) Top view of the LP-CP converter. (D) Bottom view of the LP-CP converter.





TABLE 1 Performance comparisons of other similar antennas.

	Туре	Gain (dBiC)	AR bandwidth (AR<3 dB)	Number of layers	Heigh/diameter
[22]	Circularly Polarized RA	25.8	9.2-10 GHz	1	1
[23]	Circularly Polarized RA	24.8	8–12 GHz	1	0.87
[32]	CPFRA	22.8	5.22–5.46 GHz	3	0.85
This work	CPFRA	21	9.8–10.3 GHz	2	0.47

layers from three to two. Moreover, the height over the diameter was 0.47 in the present study, which was smaller than that of 0.87 in [32]. Compared to the CP-RA in [22, 23], the profile was effectively reduced. Therefore, the results of this study demonstrated the successful development of a low profile.

Conclusion

This work proposed a low-profile CPFRA using a polarization-sensitive LP-CP converter to replace PG and polarization-insensitive LP-CP converters. This highly integrated design reduced the profile with a simple design process. The CP and LP patch antenna elements were connected by a metallic via at the two surfaces to provide the functions of LP-CP transformation. As the LP antenna elements can only transmit waves of specified polarization, the converter was polarization-sensitive. The main reflectarray consisted of 1bit unit cells that provided 90-degree polarization twisting and 0 and 180-degree phase shifting. Both simulated and measured results demonstrated the effectiveness of the proposed CPFRA. This design concept can be used to develop high-performance CPFRA with wideband high-gain and low profile by using a wideband polarization-insensitive LP-CP converter.

Data availability statement

The original contributions presented in the study are included in the article/supplementary material. Further inquiries can be directed to the corresponding author.

Author contributions

SL is responsible for the entire study. YL contributed to the data curation, study methodology, and results validation. S-WW, XZ, and SW contributed to the study methodology and results validation. LF and QG mainly contributed to the data curation.

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Conflict of interest

The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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