

[A New Estimation Method for Rotor](https://www.frontiersin.org/articles/10.3389/fphy.2022.865240/full) [Size of UAV Based on Peak Time-Shift](https://www.frontiersin.org/articles/10.3389/fphy.2022.865240/full) [Effect in Micro-Doppler Lidar](https://www.frontiersin.org/articles/10.3389/fphy.2022.865240/full)

Yong Zhang^{1,2}, Dongmei Li^{1,2}, Yi Han³, Zhen Yang^{1,2}*, Xin Dai^{1,2}, Xinmin Guo^{1,2} and Jianlong Zhang^{1,2}

1 National Key Laboratory of Science and Technology on Tunable Laser, Harbin Institute of Technology, Harbin, China, 2 Department of Optoelectronic Information Science and Technology, School of Astronautics, Harbin Institute of Technology, Harbin, China, ³School of Instrument Science and Engineering, Institute of Functional Materials and Acoustooptic Instruments, Harbin Institute of Technology, Harbin, China

The aim of this study was to solve the problem that the existing identification parameters of rotor unmanned aerial vehicles (UAVs) are few and limited by the detection mode, and an identification method for estimating the rotor blade width based on the peak time-shift effect is proposed for the first time. Taking the width of the rotor blade as the parameter to identify the rotor of UAVs, the time-shift effect and its relationship with rotor blade width are verified by theoretical analysis and simulation. The proposed time-shift method has the characteristics of high-precision extraction of rotor width, and its effectiveness is verified by simulation and experiments. The aspect ratio of the rotor is accurately extracted based on the proposed time-shift method under the condition of an unknown pitch angle. Simulation results show that the estimation accuracy of the width and aspect ratio is up to 98 and 98.4%, respectively. The experimental results show that the relative errors of the width and aspect ratio are less than 7 and 4%, respectively. This study provides the theoretical basis and technical support for the high-accuracy identification of rotorcraft UAVs.

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Qun Hao, Beijing Institute of Technology, China

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*Correspondence:

Zhen Yang sailoryz@hit.edu.cn

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INTRODUCTION

The rotor blade is the main power component of the rotorcraft, and its rotating motion modulates the Doppler echo generated by the UAV fuselage motion to form micro-Doppler signals $[1-3]$ $[1-3]$ $[1-3]$ $[1-3]$; therefore, the echo signal contains the size information of the rotor [\[4](#page-8-2)–[6](#page-8-3)]. Different types of rotorcraft UAVs have different blade parameter information [[7](#page-8-4)], mainly including blade width and aspect ratio of a rotor blade, which are crucial reference indexes for identifying rotorcraft UAVs [[8](#page-8-5)–[10](#page-8-6)].

At present, there are only three parameters available for rotor UAV identification: rotor blade length [[11](#page-8-7)–[13\]](#page-8-8), number of blades [\[14](#page-8-9)–[16](#page-8-10)], and number of rotors [\[17\]](#page-8-11). The different models of rotor blades reflect different information and can extract different parameters. In a certain establishing model, the whole rotor blade is equivalent to a point target and used to simulate the rotation of the rotor [[18](#page-8-12)–[20\]](#page-8-13). This model can vividly reflect the motion trajectory of rotor blades. Unfortunately, this model is too rough and has a big difference from the actual echo signal. Chen et al. [[21\]](#page-8-14) equated rotor blades to linear scatterers. Based on this modeling, the length of the rotor blade, number of blades, and number of the rotor can be extracted. On the contrary, this kind of modeling lacks lot of detailed information [[22,](#page-8-15) [23](#page-8-16)]. Chen et al. [\[24\]](#page-8-17) discretized the rotor blade

into scattering panel elements with uniform scattering coefficients and equally spaced distribution. The echo of a rotor blade is superimposed by the echo, which is formed by countless scattering surface elements. Jiang et al. [\[25\]](#page-8-18) verified through this model that the envelope shape in the time–frequency diagram formed by different blade width and blade tip sweep angle is different. Wang et al. [\[26\]](#page-8-19) confirmed that the greater the rotor blade width, the greater the sub-frequency band. However, the peak phenomenon in the time–frequency diagram was not introduced in detail, ignoring the contribution of rotor blade width to peak timeshift. In addition, the contribution of rotor blade thickness to echo could not be verified, either. Based on the aforementioned research results, it is necessary to establish a new model to verify the influence of various parameters of rotor blades on laser micro-Doppler echo. Based on this model, a new identification parameter of the rotor UAV is extracted. The width and aspect ratio of the rotor blade are urgently required to establish a high-precision identification method that can accurately identify the width and aspect ratio parameters of the UAV blade.

As the parameters of rotorcraft UAV identification based on the laser micro-Doppler effect are few and cannot be accurately identified [\[27,](#page-8-20) [28\]](#page-8-21), this study proposed the UAV parameter high-precision identification avenue based on the time-shift method for the first time. By using the high spatial resolution lidar [\[29](#page-9-0)–[31](#page-9-1)] and establishing a cuboid geometric model with multiple scattering points, it ensures that the echo signal contains a lot of details of the rotor [\[32](#page-9-2)–[34](#page-9-3)]. Based on the proposed time-shift method, the influence of blade width on the micro-Doppler echo signal is studied with the proven correctness by simulation and experiment. The results show that the proposed method can achieve a high recognition rate extraction of rotor width and aspect ratio. The UAV width recognition rate is 98% and its aspect ratio is 98.4% in simulation,

while they are 93 and 96% in theoretical verification, which provides the technical support for further recognition of UAVs.

THEORETICAL MODELING AND ANALYSIS OF THE SINGLE-BLADE ROTOR

Multipoint Scattering Rotor Echo Modeling

As shown in the small diagram in [Figure 1](#page-1-0), the light emitted by the lidar shines on the rotating rotor blade target of rotorcraft UAVs and scatters, and the rotating motion of the rotor blade modulates the echo signal and forms the micro-Doppler echo signal. The micro-Doppler echo signal contains geometric structure information such as the length, width, and length–width ratio of the rotor blade target. The rotor blade targets are identified by extracting the information from the micro-Doppler. Assuming that the rotation center of the rotor blade is located at the coordinate origin O , α is azimuth which is zero here, along with β which is the pitching angle. The distance between the lidar and rotor center is R_0 , where z_0 is the height of the rotor blade, the distance between the scattering point on the blade and the rotor center is l_M ($l_M < R_0$), and the scattering point rotates around the *z*-axis at constant angular velocity ω . Supposing that the initial phase of point M on the rotor blade is ϕ_0 , the rotor blade passes through time t from point M to point M' . Based on single-point modeling, the baseband signal returned by the scattering point at distance R is [\[2](#page-8-22), [3\]](#page-8-1).

$$
s_R(t) = \exp\left\{ \begin{array}{l} -j2\pi f_0 t - j\frac{4\pi}{\lambda}R_0 - j\frac{4\pi}{\lambda}z_0\sin\beta \\ -j\frac{2\pi}{\lambda}l_M\cos\beta(\cos\phi_0\cos\omega t - \sin\phi_0\sin\omega t) \end{array} \right\}.
$$
\n(1)

The rotor blade is equivalent to a cuboid with a certain thickness, and it has meshed. The points on the meshing are

named scattering points to replace the central points of the scattering surface element of the rotor blade. Let the coordinates of scattering points be (x_i, y_i, x_i) , where i, j, and k are integers; the distance between the rotor center O and each scattering point is $l_M(x, y, z) = (x^2 + y^2 + z^2)^{1/2}$. Then, the scattering echo signal is modified as follows:

$$
s_{R}(t) = \sigma \sum_{i=-\frac{5}{2}}^{\frac{x}{2}} \sum_{j=0}^{y} \sum_{k=-\frac{5}{2}}^{\frac{5}{2}} \exp \left\{ \begin{array}{l} -j2\pi f_{0}t - j\frac{4\pi}{\lambda}\left(R_{0}^{'} + z_{0}\sin\beta\right) \\ -j\frac{2\pi}{\lambda}I_{M}\left(x_{i}, y_{j}, z_{k}\right)\left[\cos\beta\left(\cos\phi_{0}\cos\omega t - \sin\phi_{0}\sin\omega t\right)\right] \\ 2\end{array}\right\},
$$
\n(2)

where $R'_0 = R'_0 + l_M(x, y, z)$ σ is the scattering coefficient

Contribution of Rotor Width to Echo

The relative position of the rotor and lidar is shown in [Figure 1](#page-1-0). The distance between the lidar and target rotor is much larger than the length of the rotor L , and the visible laser is a parallel ray (parallel line with an arrow on the right of the [Figure 1](#page-1-0)). To simplify the calculation, the lidar is equivalent to point Q, and the line QO is parallel to the lidar line of sight. The distance between lidar Q and the rotation center O of the rotor blade is R_0 , and the distance between Q and point M on the top of the rotor blade is R_M . θ is the rotation angle of the line between point M and the rotation center O of the rotor blade around the *x*-axis, and its magnitude is complementary to the included angle between the linear velocity direction and radial velocity direction of point M. From the references of [\[13](#page-8-8), [30\]](#page-9-4), it can be known that

$$
f_M = \frac{2}{\lambda} \omega L \sin \theta \cos \beta.
$$
 (3)

According to [Eq. 3](#page-2-0), the micro-Doppler frequency-shift generated by scattering points on rotor blades is related to ω and θ . When $\theta = \pm n\pi$, the micro-Doppler shift reaches the minimum value zero. So, the time–frequency diagram is periodic.

As shown in the upper right corner of [Figure 1](#page-1-0), points A and B are the two vertices of the blade, and the width of the rotor blade is AB. The rotor rotates at the same angular velocity. When $\theta = \pm (2n + 1)\frac{\pi}{2}$, the maximum micro-Doppler frequency-shift

is generated due to the influence of the length of the rotor blade, and its magnitude is

$$
f_{L-\max} = \frac{2\omega L}{\lambda} \cos \beta.
$$
 (4)

However, when the connection between rotor apex A and rotor blade rotating center O is perpendicular to the radar line of sight (OA is perpendicular to the radar line of sight), the micro-Doppler frequency-shift generated by vertex B does not reach the maximum value. When *OA* rotates $\Delta \phi$ angle, the linear velocity direction of vertex B is parallel to the radar line of sight direction and the micro-Doppler frequency-shift reaches the maximum value. According to [Eq. 4](#page-2-1), the maximum frequency-shift of the micro-Doppler is related to L. The distance between vertex A and B and rotor blade center O is the greatest. Therefore, in this process, the micro-Doppler frequency-shift gradually decreases from the maximum frequency-shift at point A to the minimum value at the center point AB and then increases gradually to the maximum value at point B, that is, two peak values appear, and the time taken to generate the two peak values is the time taken for the angle change $\Delta \phi$, which is called the peak time-shift Δt in this study, and

$$
\Delta t = \frac{\Delta \varphi}{\omega}.\tag{5}
$$

SIMULATION ANALYSIS OF THE ECHO SIGNAL FOR THE ROTOR BLADE

As shown in the small diagram in [Figure 1](#page-1-0), the larger the width of the rotor blade is the bigger the phase $\Delta \phi$ of the corresponding

rotation center o is. Combining with [Eq. 5](#page-2-2), it can be found that under the condition of the same rotation frequency of the rotor, the larger the $\Delta\phi$ is the longer the rotor rotates around the whole width. To verify that the simultaneous peak effect of the rotor blade width contributes to the micro-Doppler echo is more intuitive, the rotor blade width was simulated with equal columns of the 0.06-m interval based on the fixed rotor blade length. The numerical values are 0.18 m, 0.12 m, 0.06 m, and 0.01 m. The peak can be clearly seen in [Figure 2A](#page-2-3). There is a large distance between the two peaks. The peak of [Figure 2B](#page-2-3) decreases relative to the peak in [Figure 2A](#page-2-3). Similarly, the peaks of [Figures](#page-2-3) [2C,D](#page-2-3) gradually decrease relative to the previous simulation time–frequency map. The width relative to the length of the rotor blade can be considered a line when the width ratio of the rotor blade is 40:1:1. The same results, as in [[18](#page-8-12)–[20\]](#page-8-13) linear modeling, correct the results of this study. [Table 1](#page-2-4) shows the parameters used in the simulation, in which the results are shown in [Figure 2](#page-2-3).

The laser micro-Doppler echo signal formed by the rotor blade rotation is a time-varying nonstationary signal. Then, the original time–frequency diagram can be obtained. However, the data span ambassador in the original time–frequency map has a large dynamic range using the log compression dynamic range. Meanwhile, the points in the time–frequency map are discrete, and Gaussian smoothing is taken and filtered.

[Figure 2](#page-2-3) shows that the simulation time–frequency diagram changes periodically and the time spectrum is a visually twisted rope, completing four cycles within a second, which expressed the rotation of the rotor as 4 HZ. As can be seen from [Figure 2A](#page-2-3), there are two peaks at the peak location in one cycle. In [Figure 2A](#page-2-3), the physical quantity of abscissa is time, the physical quantity of ordinate is micro-Doppler frequency, and the maximum micro-Doppler frequency shift generated at the peak is 11 MHz. The interval between the two peak values is the time-shift. When the aspect ratio decreases in equal proportion, the time-shift decreases with the decrease of rotor width. As shown in the simulation time–frequency diagram, according to the proportional relation of the aspect ratio, the width of the rotor blade in [Figure 2A](#page-2-3) is the largest, and the corresponding timeshift is larger. When the rotation frequency is the same, the longer it takes for the vertex at one end of the width to reach the peak formed by the other vertex the larger the interval between the two peaks and the bigger the time-shift. The aforementioned simulation verification and analysis show that the time-shift effect does exist and the time-shift method can be used to estimate the width of the rotor blade.

ROTOR SIZE ESTIMATION BASED ON THE PEAK TIME-SHIFT METHOD

It can be seen from the aforementioned section that the echo signal time–frequency diagram will show a peak time-shift due to the influence of rotor width. In this section, the time-shift method will be used for parameter estimation and error analysis of the rotor width and aspect ratio.

Rotor Width Estimation

Assuming that the pitch angle of the rotor is 30° , the rotation frequency $f_0 = 4 Hz$, and the maximum micro-Doppler frequency-shift corresponding to the length of the rotor is f_{L-max} , the length of the rotor can be obtained from [Eq. 4](#page-2-1) as follows:

$$
L = \frac{f_{L-\text{max}}\lambda}{2\omega \cos \beta}.
$$
 (6)

The ratio of length to width of the selected rotors in this study is not less than 3:1, in which the width can be approximated as $W = 2L\sin(\frac{\Delta\varphi}{2})$. Combining **[Eqs 5](#page-2-2), [6](#page-3-0),** the width can be obtained as follows: follows:

$$
W = 2L\sin\left(\frac{\Delta\varphi}{2}\right) = \sin\left(\frac{\omega \cdot \Delta t}{2}\right) \frac{\lambda f_{L-\text{max}}}{\omega \cos \beta}.
$$
 (7)

The simulation results show that the thickness of the rotor blade has no contribution to the maximum micro-Doppler frequency-shift, rotation frequency, and waveform envelope in the time–frequency diagram after processing. Therefore, this article does not study the correlation effect of rotor blade thickness. In the simulation calculation of the contribution of the rotor blade size to echo signal, the width is changed by adjusting the aspect ratio, and the thickness of the rotor is set as 1/ 40 of the length. According to [Eq. 7](#page-3-1), the width of the rotor blade determines the peak (Δt) in the time–frequency diagram. According to the characteristics of the time–frequency diagram, the rotor blade rotation frequency ω and the maximum micro-Doppler frequency-shift f_{L-max} can be extracted as shown in [Figure 3A](#page-4-0).

The laser micro-Doppler echo signal formed by the rotating rotor blade is transformed into the original time–frequency diagram by a short-time Fourier transform. The original time–frequency map has some disadvantages, such as less lowfrequency details reserved, low contrast between time–frequency features and background, unsmooth edge leading to time–frequency spectrum repetition period, and the unclear edge of the outer envelope. Logarithmic transformation and Gaussian filtering are used to smooth the edge noise of the original time–frequency graph in order to compress the dynamic range of the data while increasing the low-frequency details, and the time-spectrum envelope is clearer.

The outer envelope function of the time–frequency diagram is extracted, and its derivative is used to calculate the maximum value of the function. The outer envelope function takes time as a variable, and the maximum value of the function is the maximum frequency-shift of micro-Doppler. According to the maximum value of the envelope function, the corresponding occurrence time is calculated. The two nearest adjacent maximum values and the corresponding time interval are the peak value of the micro-Doppler frequency-shift and its corresponding time-shift, respectively.

Substituting the laser wavelength $\lambda = 1064$ nm, $\omega = 8\pi$ rad/s, sampling rate 10,000, and pitch angle $\beta = 30^{\circ}$ into [Eq. 7](#page-3-1), the results are shown in Table 2. The length of the simulation results are shown in [Table 2](#page-4-1). The length of the simulation setting is 0.24 m. According to the equivalent length–width

FIGURE 3 | Rotor size estimation based on the peak time-shift method. (A) Flow chart of the blade width extractional algorithm. (B) Relationship between estimated width and actual width. (C) Width estimation error.

TABLE 2 | Width estimation results.

TABLE 3 | Estimation results of the aspect ratio.

ratio of the real rotor blade between 4:1 and 16:1, the width value of the rotor blade is set to be between 0.08 and 0.015 m. Based on this, this study extracted the width of the rotor blade in turn based on the peak method and the equal difference decreasing law of the width of the rotor blade. The average value of the peak value (f_{L-max}) and time-shift (Δt) in each cycle of the time–frequency diagram of each group of experiments was calculated and recorded. The extraction results are shown in [Table 2](#page-4-1).

The relationship between the estimated width and the actual rotor width can be obtained according to [Table 2](#page-4-1), as shown in [Figure 3B](#page-4-0). The line is the linear fitting result of the estimated width. The slope of the line is 1.016 and the sum of squares of residuals is 5.37×10^{-7} , which is extremely linear, indicating that the estimated result is consistent with the real width value.

The width estimation error obtained from [Table 2](#page-4-1) is shown in [Figure 3C](#page-4-0). The red dotted line and black dotted line are cubic spline interpolation curves of the width estimation error of the rotor blade. When the length is constant, the vibration amplitude increases with the increase of the width from 0.015 to 0.045 m and decreases with the increase of the width from 0.045 to 0.080 m. Similarly, the extraction result of the width of the rotor blade is related to the length–width ratio of the rotor blade. The higher the length–width ratio of the rotor blade, the smaller the time-shift of the time–frequency diagram formed. Due to the influence of time resolution, the larger the extracted time-shift (Δt) error is the larger the estimated error of the rotor blade is. The amplitude of the error vibration decreases slowly. In other words, when the actual width is large, the absolute error is enormous too, but not more than 1 mm. The relative error fluctuates around 1.09%, and the maximum relative error is less than 2%. In conclusion, the time-shift method proposed in this study can estimate the rotor width accurately, and the estimation results have high credibility.

The main error sources of width estimation in this study are as follows:

1) Discrete error: In the process of modeling, the model is gridded; in a word, the model is dispersed. The degree of model dispersion will have a certain influence on estimation accuracy. The more the grid dividing the higher the estimation accuracy is recognized and the smaller the error will be. The discrete error is inevitable, so this study minimizes the error as far as possible within a reasonable range.

- 2) Maximum frequency-shift extraction error: Because there is no absolute edge in the time–frequency graph and the frequency resolution in this study is 0.01 MHz, there is an error in the extraction of the maximum frequency-shift of the micro-Doppler, which leads to the error of width estimation.
- 3) Time-shift extraction error: Because the peak time-shift generated by the smaller rotor width is relatively small, the time resolution in this study is 0.1 ms, and it is difficult to accurately extract the time difference between the two peak values, so the error is generated.

Estimation of the Rotor Aspect Ratio

According to [Eq. 7](#page-3-1), the estimated width is related to the pitch angle. However, the real situation is the generally unknown pitching angle, so it is hard to estimate the width directly. Combined with [Eqs 6](#page-3-0), [7](#page-3-1), we can get

$$
\frac{L}{W} = \frac{1}{2\sin(\frac{1}{2}\omega \cdot \Delta t)}.
$$
 (8)

As shown in [Eq. 8](#page-5-0), the expression of the aspect ratio of the rotor only includes the rotation speed ω and the time-shift Δt , which has nothing to do with the pitch angle parameter. In other words, the aspect ratio of the rotor can also be solved by the unknown pitch angle. The simulation calculation is carried out according to the following process, and the estimated results of the time-shift rotor aspect ratio are shown in [Table 3](#page-5-1).

The flow chart of the rotor aspect ratio estimation algorithm based on the time-shift method is shown in [Figure 4A](#page-6-0) The relationship between the estimated aspect ratio and actual aspect ratio is drawn according to [Table 3](#page-5-1), as shown in [Figure 4B](#page-6-0). The red dot is the estimated aspect ratio of simulation, and the black line is the linear fitting result of the real ratio and estimated ratio. The straight slope is 1.007, and the sum of squares of residual errors is 0.029. The results show that the simulated aspect ratio is close to the set aspect ratio. The absolute and relative errors of the estimated aspect ratio are shown in [Figure 4C](#page-6-0). The red curve and green curve are the cubic spline interpolation results of the absolute and relative errors, respectively. It shows that the

absolute error of the estimated aspect ratio fluctuates between 0 and 0.2, while the absolute error shows a rising trend with the increase of the aspect ratio. Similarly, the relative error increases with the increase of the aspect ratio, and the actual maximum relative error is only 1.6%. Similar to the width estimation, the estimation error of the aspect ratio mainly comes from the discrete error introduced by model meshing and the extraction error of time-shift, while the extraction result of frequency-shift

Eigen light incident acousto-optic modulator with a frequencyshift of 70 MHz. The outgoing light passes through the fiber attenuator and enters the fiber buncher. The two beams are mixed in the fiber combination and transmitted to the balance detector to form heterodyne interference and retain the difference frequency part. The optical signal is converted into an electrical signal collected by the acquisition card. Finally, the time–frequency diagram is obtained by computer processing.

In this experiment, the pulsed lidar at 70 GHz was used. The distance between the laser and target is 80 m, and the spot diameter of the laser beam is about 3 cm. The number of revolutions of the motor is 500 r/min, and the target rotating the power supply voltage is 6 V . [Figure 6](#page-7-0) shows the

does not affect the estimation of the aspect ratio. Therefore, the relative error of the estimation result of the aspect ratio is smaller than that of the width estimation result. It can be seen from the aforementioned analysis that the time-shift method proposed in this study has a good effect and high credibility in the estimation of the rotor aspect ratio parameters.

EXPERIMENTAL VERIFICATION OF UAV PARAMETER ESTIMATION

Different types of rotor UAVs have different rotor blade size information, but the same type of rotor UAVs has the same size information. The micro-Doppler echo signal formed by rotor blade rotation of the same UAVs carries the same information. Based on this, a single rotor blade contains the micro-Doppler echo information formed by all the rotor blades. The rotor UAVs can be recognized by extracting the information of a single rotor blade. The equivalent width and aspect ratio of rotor blades are important parameters to identify UAVs with different signals. In this study, the equivalent width and length–width ratio of the rotor are extracted by the following experimental devices, and the correctness of the simulation experiment is verified.

[Figure 5](#page-6-1) is a schematic diagram of a UAV rotor blade parameter estimation experimental device. The laser beam from the 100-mW seed laser is divided into signal light and intrinsic light using a fiber beam splitter. The signal light with 90% of the total power is reflected after irradiating to the target of the rotor blade through the transmitting optical system. The reflected micro-Doppler echo signal is transmitted to the optical fiber buncher through the receiving optical system, that is, the

time–frequency diagram obtained using experimental measurements when the equivalent length–width ratio of rotor blades is 3:1. The length and width of a single blade of the rotor are 9 and 3 mm, respectively, and its rotation frequency is 1.59 Hz. The time–frequency diagram after data processing mainly comprises two parts: the main part with the envelope of the micro-Doppler echo signal formed by the rotation of the rotor blade and the irregular burr edge part formed by noise. In the time–frequency diagram, the two vertical lines are the peaks formed by the two tip points of the rotor width, and the optimal envelope function in the time–frequency diagram is extracted, and the maximum frequency-shift of the rotor and the corresponding t are calculated through several iterations. The five groups of data were averaged for each group, and the time when the peak occurred and the corresponding maximum frequency-shift were recorded. The experimental and simulation results are as follows:

As the accuracy of the simulation is higher than that of the experiment, it can be concluded from [Table 4](#page-7-1) that the maximum relative error of rotor width recognition is 3.33%, and the maximum relative error of the aspect ratio is 4.52%. The aforementioned comparison results prove the feasibility of the UAV parameter estimation method proposed in this study, which can accurately extract the rotor width and aspect ratio.

CONCLUSION

Aiming at the problems of low spatial resolution and few parameters of the rotor UAVs identified by the microwave radar, this study proposes a method for identifying the rotor

UAV blade parameters based on the peak time-shift method and high spatial resolution lidar. To solve the problem of the lack of rotor geometric structure information in single-point scattering modeling of rotorcraft UAV identified by the microwave radar, a rectangular multipoint scattering geometric model is established in this study. This method can identify two crucial parameters of rotorcraft UAV, rotor width, and aspect ratio with high accuracy.

Based on the established multipoint scattering rotor echo model, the contribution of rotor width to the micro-Doppler echo signal is studied theoretically, and the existence of the timeshift effect is verified using theoretical analysis and simulation. Based on the relationship between the contribution of rotor width to the echo and the time-shift effect, the UAV parameter estimation method based on the time-shift effect is proposed. The estimation accuracy of the rotor width is 98 and 93%. The aspect ratio of the UAV rotor is extracted using the time-shift method. The results show that the relative errors of the aspect ratio of the UAV rotor identified by the simulation and experiment are less than 1.6 and 4%, respectively. This study

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proposes a new parameter estimation method for laser micro-Doppler identification of rotorcraft UAVs and provides a theoretical and technical basis for further identification of details and structural parameters of rotorcraft UAVs.

DATA AVAILABILITY STATEMENT

The original contributions presented in the study are included in the article/Supplementary Material, further inquiries can be directed to the corresponding authors.

AUTHOR CONTRIBUTIONS

DL: provided innovation and wrote the manuscript; XD and YH: helped with the experiment; YZ: theoretical and experimental guidance; ZY, XG, and JZ: guidance in the writing of the manuscript.

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