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Ultrathin high-temperature ferromagnetic rare-earth films: GdScGe and GdScSi monolayers

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Two-dimensional (2D) ferromagnetism with robust room-temperature ferromagnetism has sparked intense interest for future miniature information storage devices. However, most 2D ferromagnetic materials have a low Curie temperature. Here, by using density functional theory, two rare-earth monolayers, the GdScSi monolayer and the GdScGe monolayer, were predicted, in which these two monolayers exhibit ferromagnetic orders with large magnetic moments of approximately $7\mu_B/\text{Gd}$. Monte Carlo simulations predict Curie temperatures of approximately 470 K and 495 K for the 2D GdScSi monolayer and the GdScGe monolayer, respectively. The spin band calculations show that they are metal. In addition, these two monolayers exhibit dynamical, mechanical, and thermal stabilities. The combination of these novel magnetic properties makes these 2D ferromagnetic crystals promising candidates for high-efficiency spintronic applications.

KEYWORDS

high-temperature ferromagnetic materials, rare-earth films, two-dimensional material, density functional theory, large magnetic moments

1 Introduction

Since the successful synthesis of graphene, two-dimensional (2D) materials have attracted a great deal of attention [1–11]. First, the ‘star material’ graphene possesses excellent mechanical and electronic properties, but it has zero band gap. Then, a MoS₂ monolayer was successfully prepared, but it has relatively low electron and hole mobilities. In 2014, black phosphorus with a direct band gap and high carrier mobility was confirmed in an experiment, but it has poor stability when exposed to air. In addition, most synthesized 2D materials are non-magnetic, which has prevented their application in advanced spintronics. Although many efforts have been made in designing 2D ferromagnetism by introducing defects [12,13], strains [11,14–17], doping [18–22], and surface functionalization [19,23–26], it is still very challenging to obtain robust magnetism.

In 2017, an ultrathin ferromagnetic CrI₃ monolayer and a CrGeTe₃ bilayer were discovered [7,8], which disturb the limitation to the Mermin–Wagner (M–W) theorem [27]. The Mermin–Wagner theorem shows that the magnetic order is prohibited in the 2D isotropic Heisenberg model at finite temperatures. Recent studies have shown that magnetic anisotropy is the fundamental cause of 2D long-range magnetism [28–36]. Almost all synthetic and predicted 2D ferromagnetic materials have relatively low Curie temperatures (T_C) and small magnetic anisotropy energies (MAEs), for example, 45 K for the CrI₃ monolayer [8], 30 K for the CrGeTe₃ bilayer [7], 146 K for the CrSBr monolayer [37], 185 K for the ScCl monolayer [22], and 24 K for the GdI₂ monolayer [38]. Therefore, it is highly desirable to search for new

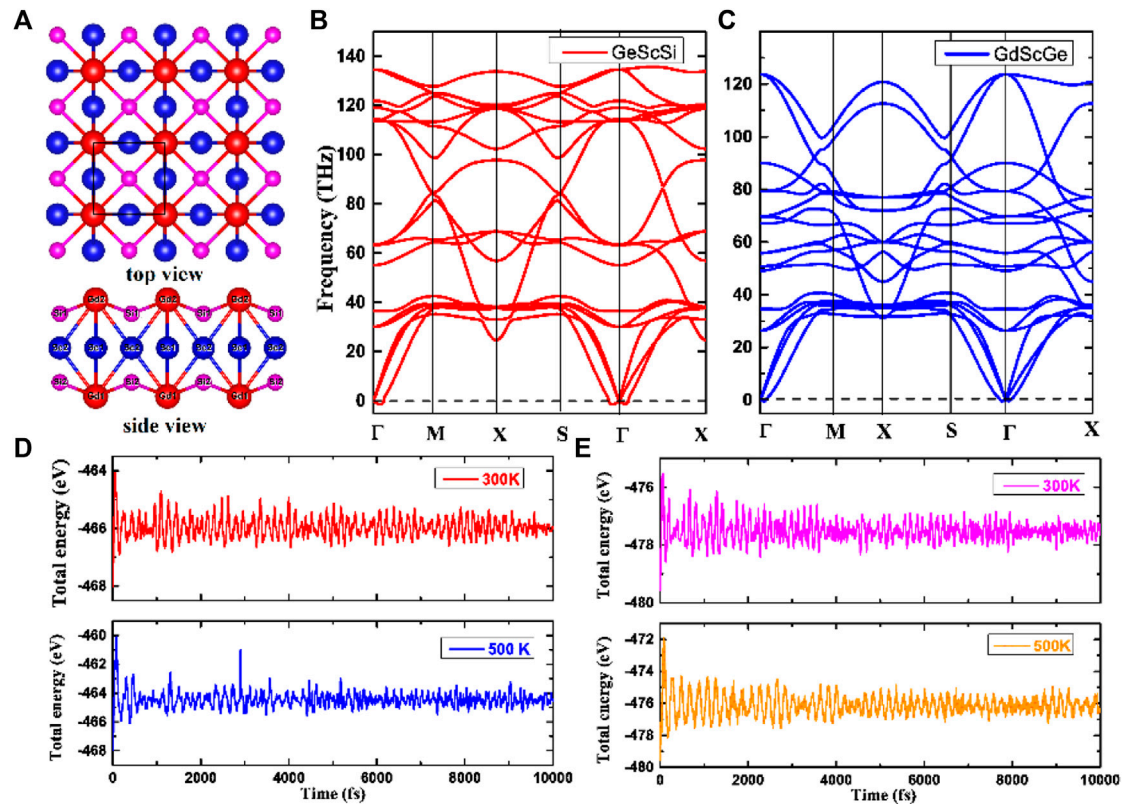


FIGURE 1

(A) Structures of GdScX ($X = \text{Si}, \text{Ge}$) monolayers. The Gd atom is located at $2g$ (0, 0, 0.3633), Sc at $2e$ (1/2, 0, 1/2), and Si at $2h$ (1/2, 1/2, 0.5971) for the GdScSi monolayer. The Gd atom is located at $2g$ (0, 0, 0.3628), Sc at $2e$ (1/2, 0, 1/2), and Ge at $2h$ (1/2, 1/2, 0.5988) for the GdScGe monolayer. (B, C) Phonon dispersion spectra of the GdScX ($X = \text{Si}, \text{Ge}$) monolayers. (D, E) Evolution of the total energy from the 10 ps AIMD simulations at 300 K and 500 K.

intrinsically 2D ferromagnetic materials with high T_C . Rare-earth elements usually have large magnetic moments and high T_C . With the increasing demand for device miniaturization, 2D rare-earth magnetic materials will be highly sought after for future spintronics. Gd-based compounds usually possess a long-range ferromagnetic order with a high T_C . We predicted the 2D GdI₂ monolayer to be a ferromagnetic semiconductor with a high T_C of 241 K and a large magnetization [38]. GdX₂ ($X = \text{Cl}, \text{Br}, \text{and I}$) monolayers were also ferromagnetic semiconductors and underwent spontaneous valley polarization [39,40]. GdGe₂ was predicted to be a ferromagnetic half-semiconductor with a large magnetic moment and an indirect band gap [41]. Gd₂C was predicted to be a time-reversal-symmetry-breaking Weyl semimetal phase [42]. The CeI₂ monolayer was predicted to be an intrinsic room-temperature ferrovalley semiconductor [43]. Dong et al., introduced the importance of 4f and 5d orbitals in 2D Gd halides [44,45]. Topological, nodal-line semimetals were also predicted in ferromagnetic rare-earth-metal monohalides [46]. As a result, 2D Gd-based compounds exhibit excellent ferromagnetism.

In this work, two rare-earth compounds of GdScX ($X = \text{Si}$ and Ge) monolayers were predicted by using first-principles calculation. The result shows that they both are ferromagnetic with a large magnetization ($7 \mu_B/\text{Gd}$). Monte Carlo simulations show that they possess a high T_C : 470 K for the GdScSi monolayer and 495 K for the GdScGe monolayer. Analysis of electronic band properties shows that they both are metals. In addition, their thermal, dynamical, and

mechanical stabilities were confirmed by *ab initio* molecular dynamics, phonon dispersions, and elastic constants, respectively. Our results certainly boost the study of 2D Gd-based magnetism.

2 Computational methods

The optimized structures were simulated by density functional theory (DFT), as implemented in the Vienna *ab initio* simulation package (VASP) [47]. The ion–electron interaction was described by using the projector-augmented plane wave (PAW) approach [48], and the exchange and correlation interactions of the electrons were calculated using the Perdew–Burke–Ernzerhof (PBE) functional within the generalized gradient approximation (GGA) [49]. In addition, to consider the Coulomb and exchange interactions of f electrons, the GGA + U method was adopted with $U = 6.6 \text{ eV}$, according to previous studies [50], and 500 eV was used as the energy cutoff of the plane wave. The convergence criteria for the energy and ionic force were set to 10^{-8} eV and $0.01 \text{ eV}/\text{\AA}$, respectively. To avoid interaction between the layers, the vacuum length was set to 20 \AA along the z -axis.

Density functional perturbation theory was used to calculate the phonon dispersions, as embedded in phonopy software [51]. The *ab initio* molecular dynamics (AIMD) simulations were carried out to evaluate the thermal stabilities of GdScX ($X = \text{Si}, \text{Ge}$) monolayers. At 300 K and 500 K, AIMD simulations were performed in the NVT

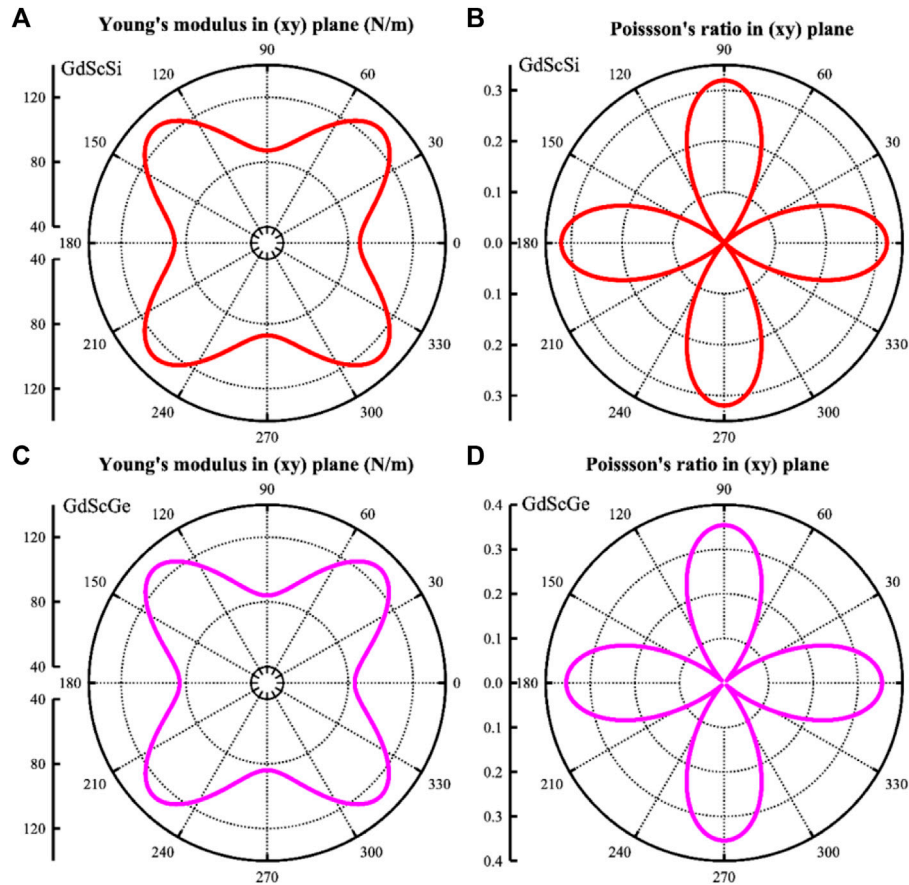


FIGURE 2 Calculated orientation-dependent (A) Poisson's ratios and (B) Young's moduli of the GdScSi monolayer (A, B) and the GdScGe (C, D) monolayer.

ensemble. The temperature was controlled by using the Nosé–Hoover method [52], and the simulation lasted for 10 ps with a time step of 1 fs at 300 K and 500 K. The orientation-dependent Young's modulus $E(\alpha)$ and Poisson's ratio $\nu(\alpha)$ were calculated as follows [30,33,53]:

$$E(\alpha) = \frac{C_{11}C_{22} - C_{12}^2}{C_{11}s^4 + C_{22}c^4 + \left(\frac{C_{11}C_{22} - C_{12}^2}{C_{44}} - 2C_{12}\right)c^2s^2}, \quad (1)$$

$$\nu(\alpha) = \frac{\left(C_{11} + C_{22} - \frac{C_{11}C_{12} - C_{12}^2}{C_{44}}\right)c^2s^2 - C_{12}(c^4 + s^4)}{C_{11}s^4 + C_{22}c^4 + \left(\frac{C_{11}C_{22} - C_{12}^2}{C_{44}} - 2C_{12}\right)c^2s^2}, \quad (2)$$

where $c = \cos\alpha$ and $s = \sin\alpha$.

3 Results and discussion

3.1 Structures and stabilities of GdScX monolayers

The structures present the P4/MMM group (No. 123) with a tetrahedron structure. The optimized lattice constants are $a = 4.08 \text{ \AA}$ and $b = 4.12 \text{ \AA}$ for GdScX ($X = \text{Si}$ and Ge) monolayers as shown in Figure 1A; Figures 1B, C show the calculated phonon dispersion spectra of the GdScSi monolayer and the GdScGe monolayer,

respectively. Notably, the absence of imaginary modes along the entire Brillouin zone indicates their dynamical stability. The corresponding fluctuations of the total potential energy for GdScX ($X = \text{Si}$ and Ge) monolayers at 300 K and 500 K are shown in Figures 1D, E, respectively, which last for 10 ps in the *ab initio* molecular dynamics. The result shows that the average values of the total potential energy oscillate with a very narrow range, confirming their thermal stabilities. As a result, the GdScX ($X = \text{Si}$, Ge) monolayers are both dynamically and thermally stable at high-temperatures.

Mechanical stability is also necessary for materials. The elastic constants are $C_{11} = C_{22} = 97 \text{ N/m}$, $C_{12} = 31 \text{ N/m}$, and $C_{66} = 65 \text{ N/m}$ for the GdScSi monolayer, and $C_{11} = C_{22} = 96 \text{ N/m}$, $C_{12} = 34 \text{ N/m}$, and $C_{66} = 64 \text{ N/m}$ for the GdScGe monolayer. Their elastic constants meet the Born criteria for a tetrahedron 2D system ($C_{11} > 0$; $C_{44} > 0$; $C_{11} > |C_{12}|$; $C_{11} + 2C_{12} > 0$), indicating their good mechanical stabilities. According to Eqs 1, 2, Young's moduli and Poisson's ratios, as functions of the arbitrary direction α in the 2D polar representation curve, were also calculated (Figures 2, 3), where α is the angle relative to the positive x -direction in these monolayers. Figures 2A, C show that the Young's moduli for GdScX monolayers first increase to a maximum value of approximately 125 N/m at $\alpha = 45^\circ$ from $\alpha = 0^\circ$ (x -direction) and decrease to a minimum value of approximately 100 N/m at $\alpha = 90^\circ$ (y -direction). The maximum value (125 N/m) is comparable to that of a MoS₂ monolayer

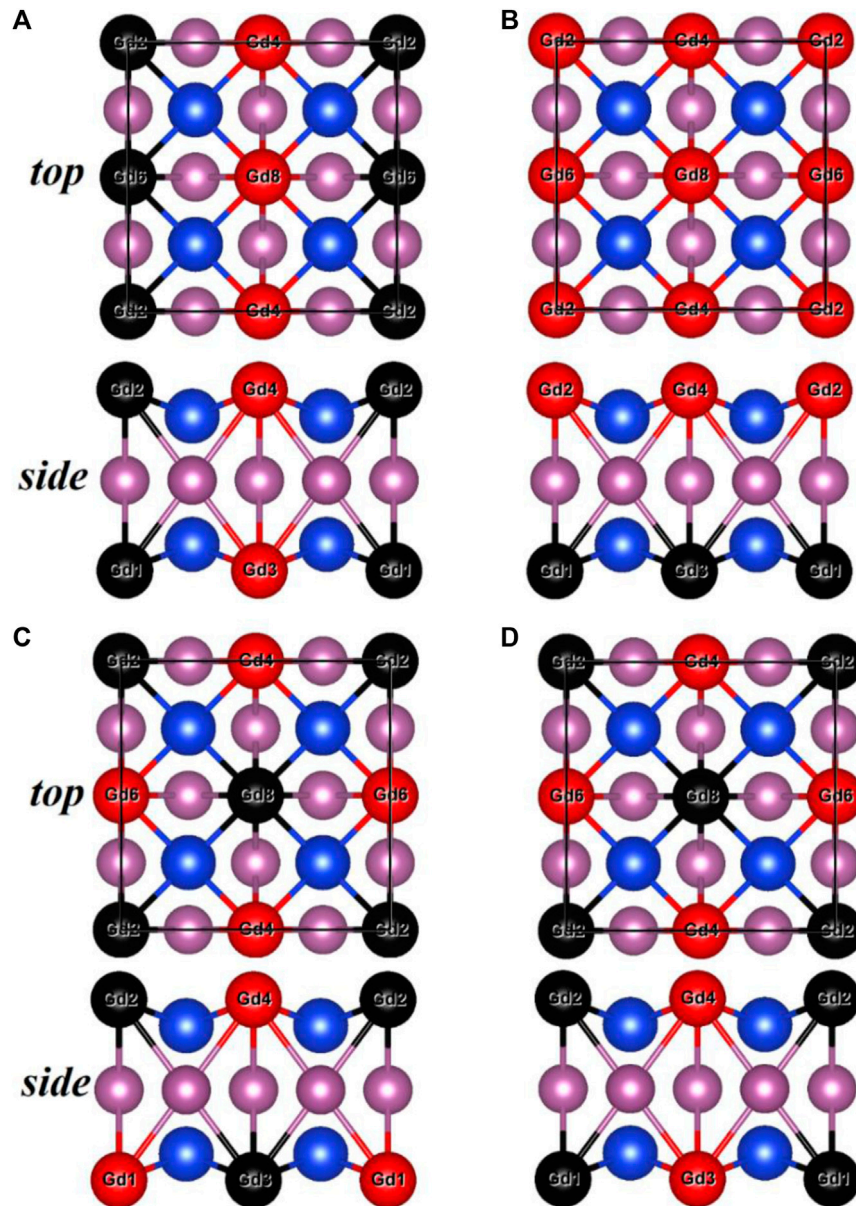


FIGURE 3
Top and side views of four AFM structures [(A), AFM1; (B), AFM2; (C), AFM3; (D), AFM4] for the GdScSi and GdScGe monolayers.

(123 N/m) [54]. Figures 2B, D show that the Poisson's ratios also strongly depend on the direction α . This shows their anisotropic mechanical properties.

3.2 Electronic band structures of GdScX monolayers

After confirming the stabilities of the GdScX monolayers, their magnetic ground states were investigated. One ferromagnetic (FM) state and four antiferromagnetic (AFM) states were considered, and the FM configuration is energetically lower than all the AFM orders (Figure 4), indicating that GdScX monolayers prefer FM coupling. Their spin band structures were also calculated by using the PBE + U

method, which are shown in Figures 4A, C. The result shows that these two monolayers are metal, in which the spin up and spin down bands cross the Fermi level. Because of the relatively heavy element Gd, the spin-orbit coupling (SOC) interactions were also considered for the electronic band structures of GdScX monolayers (Figures 4C, D). The figures show that SOC has a negligible influence on the band structure.

3.3 MAEs of GdScX monolayers

Due to the M-W theorem, [27] no long-range FM state exists if a 2D material lacks magnetic anisotropy. Therefore, magnetic anisotropy, which can be scaled by MAE, is an important property in 2D ferromagnetic systems [55]. In addition, MAE is of importance

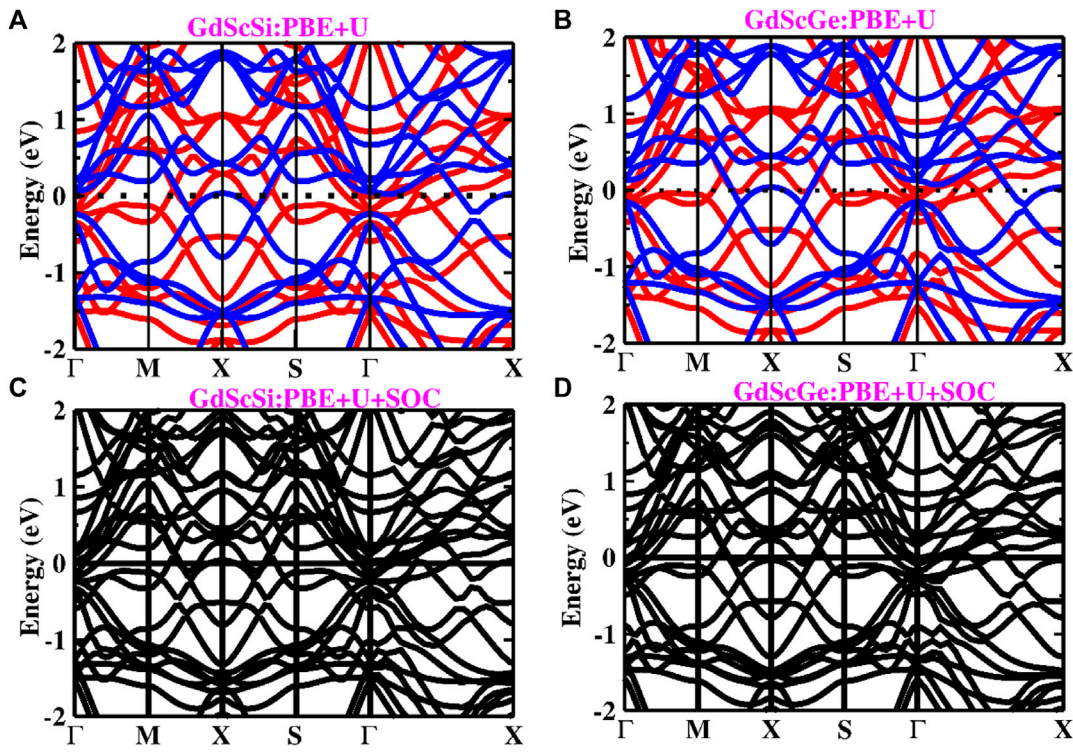


FIGURE 4 Band structures of the GdScSi monolayer (A, B) and GdScGe (C, D) monolayer determined using PBE + U and PBE + U + SOC methods.

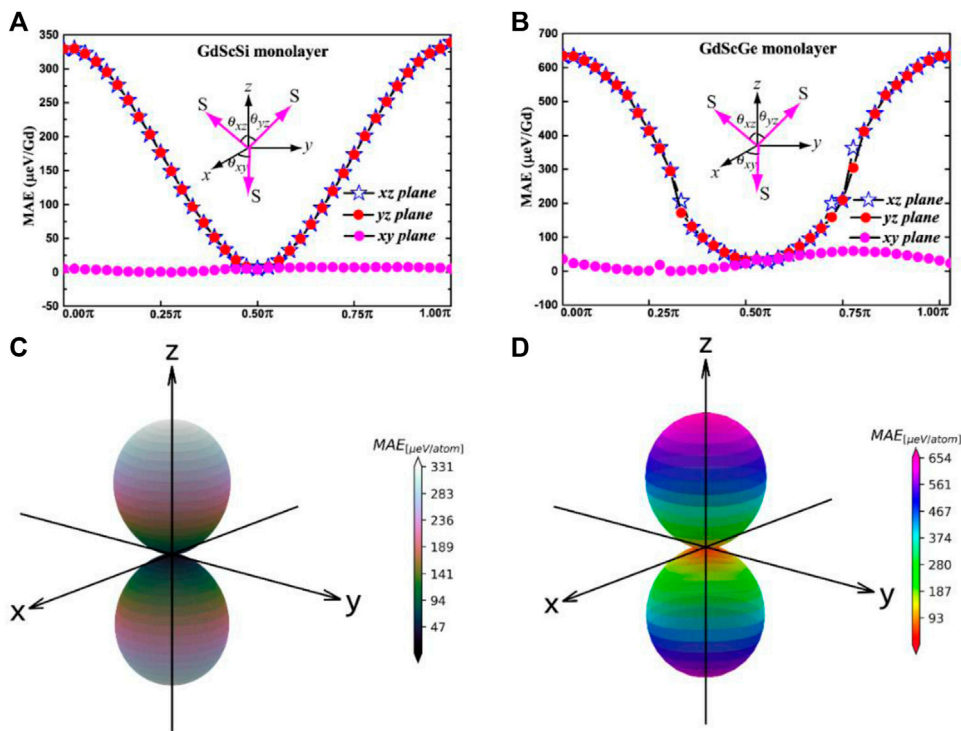


FIGURE 5 Angular dependence of the magnetic anisotropic energy (MAE) with the direction of magnetization lying on three different planes and the whole space for the GdScSi monolayer (A, B) and the GdScGe (C, D) monolayer.

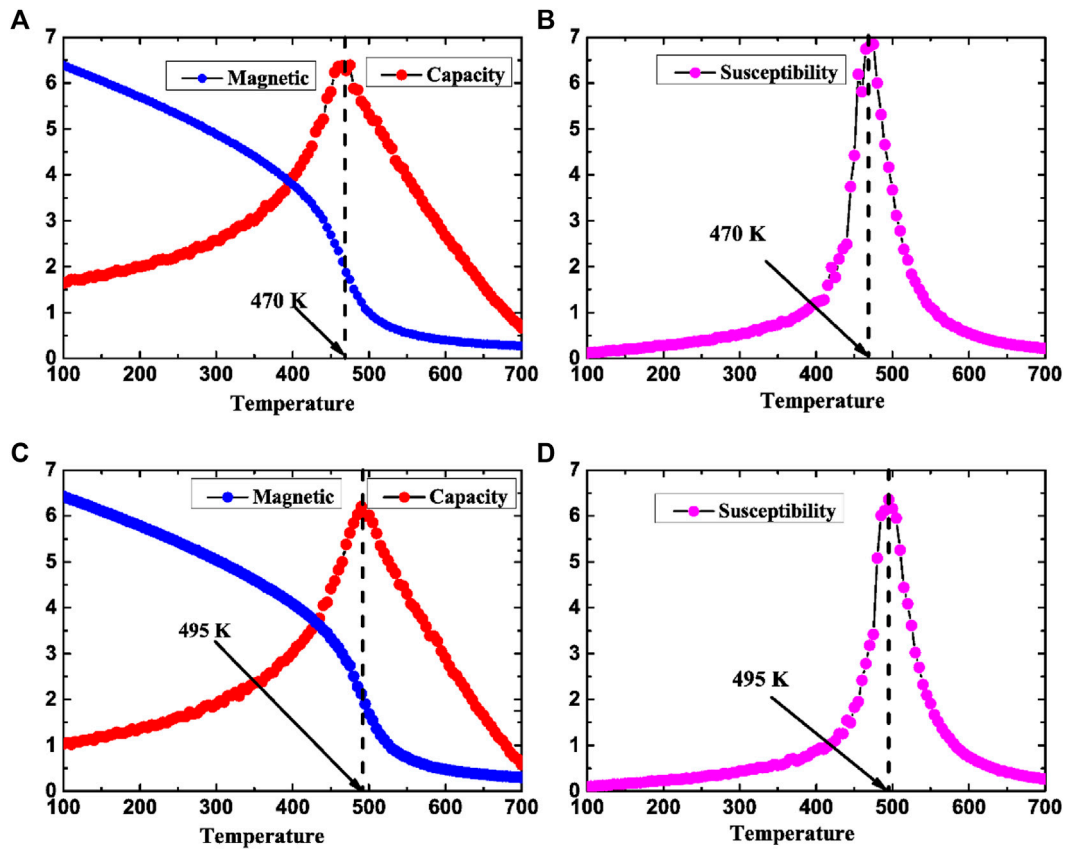


FIGURE 6

Magnetic moment (blue line), capacity (red), and magnetic susceptibility (magenta) as functions of temperature for the GdScSi monolayer (A, B) and the GdScGe (C, D) monolayer.

for the thermal stability of magnetic storage. SOC calculations were performed on the GdScX monolayers to obtain the values of MAE. Figures 5A, B show the MAEs of *xy*, *yz*, and *xz* planes for the GdScSi monolayer and the GdScGe monolayer, respectively. These figures clearly show that the MAE is almost a straight line in the *xy* plane, and that it strongly depends on the angular dependence of magnetization. In addition, the MAE of the *xy* plane is lower than that of the *xz* and *yz* planes, which indicates that these two monolayers belong to the family of 2D XY magnets. In other words, they possess an easy magnetization plane. The corresponding MAE through the whole space is also plotted in Figures 5C, D, which confirms again the strong magnetic anisotropy in these monolayers.

3.4 Curie temperatures of GdScX monolayers

T_c is an important parameter for ferromagnetic materials. To get an accurate estimate of the T_c for GdScX monolayers, Monte Carlo simulations based on the Heisenberg model were used. The Hamiltonian is defined as follows:

$$H = -\sum_{ij} J_1 S_i S_j - \sum_{ik} J_2 S_i S_k - \sum_{ik} J_3 S_i S_k - AS_i^z S_i^z,$$

where J_1 , J_2 , and J_3 are the first, second, and third nearest-neighboring exchange parameters, respectively. Using the

energy differences of the FM and AFM orders, the exchange parameters J_1 , J_2 , and J_3 are calculated to be 4.82 meV (4.81 meV), -0.106 meV (-0.038 meV), and 0.163 meV (0.102 meV) for the GdScSi monolayer and the GdScGe monolayer, respectively. The magnetic moments, capacities, and susceptibilities of the GdScX monolayers with respect to temperature (Figure 6) show that the T_c of the GdScSi monolayer and the GdScGe monolayer are approximately 470 K and 495 K, respectively, which are significantly higher than room temperature.

4 Conclusion

In summary, two 2D intrinsic ferromagnetic rare-earth monolayers, the GdScSi monolayer and the GdScGe monolayer, were predicted using first-principles calculation. Interestingly, these 2D GdScX ($X = \text{Si, Ge}$) monolayers exhibit high T_c (470 K for the GdScSi monolayer and 495 K for the GdScGe monolayer), which are above room temperature. In addition, they possess excellent dynamical, thermal, and mechanical stabilities. Our findings on the intrinsic room-temperature ferromagnetic rare-earth material GdScX ($X = \text{Si, Ge}$) monolayers open up new possibilities for spintronic applications at the nanoscale.

Data availability statement

The original contributions presented in the study are included in the article/supplementary material; further inquiries can be directed to the corresponding authors.

Author contributions

RW: data curation, investigation, validation, and writing—original draft; PS: data curation, investigation, and validation; LH: data curation, investigation, and validation; QC: validation, writing—review and editing, and supervision; YZ: writing—review and editing, supervision, and funding acquisition.

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Conflict of interest

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