



## A Comprehensive Comparison and Analysis of Several Intensity Modulations Based on the Underwater Photon-Counting Communication System

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Han X, Li P, Chang C, Gao D, Zhang D, Liao P, Wang W and Xie X (2022) A Comprehensive Comparison and Analysis of Several Intensity Modulations Based on the Underwater Photon-Counting Communication System. Front. Phys. 9:815343. doi: 10.3389/fphy.2021.815343 Underwater wireless optical communication is facing absorption, scattering problems, which, in principle, can be greatly resolved by underwater photon-counting communication (UPCC) technology that exhibits high-sensitivity communication characteristics in long-range underwater wireless optical communication. Recent studies on UPCC are mainly focused on a single intensity modulation such as on-off keying (OOK) and pulse position modulation (PPM) technologies, and the comprehensive analysis of communication performance combing OOK modulation and digital pulse modulations remains a lack. To this, by using a UPCC system based on a singlephoton avalanche diode, we reveal the communication performances of OOK, PPM, differential pulse interval modulation (DPIM), differential pulse position modulation (DPPM), and dual-header pulse interval modulation, and find that (1) the PPM has the longest transmission distance at the same bit error ratio when M > 2, but the lowest communication rate under identical modulation bandwidth and average transmit power; and (2) the DPPM and DPIM perform the optimum communication performance at the fixed communication rate when M = 8. We thus conclude that the DPPM and DPIM have advantages of low modulation bandwidth and long time slot time compared with PPM, indicating the significance of reducing the difficulty of signal synchronization and the complexity of the underwater photon-counting system accordingly.

Keywords: underwater wireless optical communication (UWOC), intensity modulation (IM), direct detection (DD), digital pulse modulation, photon counting, channel model

## INTRODUCTION

Lasers, since their invention, have been widely used in the fields of sensing [1], communication [2], and measurement [3] because of their special characteristics such as high directionality, high brightness, monochromaticity, and good coherence. Especially in recent years, with the increase in comprehensive ocean observations in scientific, industrial, and military activities, building efficient, flexible, and reliable marine environmental sensing networks is becoming urgent and important [4].

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In fact, any sensors need to be linked to each other in some way of communication, so there is great interest around how to communicate between marine mobile sensing devices in a high-speed and reliable way [5]. For underwater wireless communication, the existing communication methods mainly include hydroacoustic communication. microwave communication, optical communication, and so on [6]. Underwater wireless optical communication (UWOC) is a technology that uses the blue/green light in the visible spectrum as the information carrier for signal transmission in water [7] and has the advantages of high data transmission rate, low latency, high bandwidth, low power consumption, and so on, compared with the hydroacoustic communication and microwave communication [8]. However, achieving long-range, high-speed underwater wireless optical transmission still faces challenges due to the existence of severe water attenuation and the bandwidth limitations of blue-green wavelength devices [9]. This makes high-speed signal modulation and demodulation techniques and high-sensitivity reception techniques an important research topic in the field of UWOC. Currently, the main modulation methods include intensity modulation (IM) [10], nonlinear frequency conversion [11], subcarrier modulation [12], higherorder modulation, signal multiplexing [13], and so on. The nonlinear frequency conversion technique can generate highspeed blue-green light signals with the help of mature 1,064nm high-power devices, but the coherence of the optical signal is demanded in the frequency doubling process that high-energy consumption is needed because of the low electro-optical conversion efficiency. Although subcarrier modulation, higherorder modulation, and signal multiplexing techniques can significantly increase the data transmission rate of the system, they require high water quality and system stability and are applicable only to the laboratory technology research stage; the adaptability of these modulation techniques to the underwater channel needs further verification. In practical engineering applications, the IM techniques represented by on-off keying (OOK) are still the preferred choice. However, the high requirements for transmitting optical power for long-range underwater communications make OOK modulation unsuitable for applications on energy-limited underwater platforms. Thus, it is necessary to study the channel suitability of IM techniques with high-power utilization efficiency for underwater channels.

High-energy utilization modulation technologies represented by pulse position modulation (PPM) and high-sensitivity reception technology represented by photon-counting have become hot topics to improve power efficiency and achieve long-distance transmission. Theoretically, Hiskett et al. [14] first proposed to apply the photon-counting reception technology into underwater communication. Mao et al. [15] formulated the output characteristics of the single-photon avalanche diode (SPAD) as an ideal Poisson model and investigated the communication performance of long-range underwater photon-counting communication (UPCC) system applied with OOK modulation. Wang [16] established a longdistance underwater visible light communication system with a two-term exponential channel model and a SPAD receiver, and the arrived link distance in pure seawater can be extended to 500 m by proposing the SPAD detection algorithm. Sarbazi et al. [17] investigated the bit error performance of the receiver based on SPAD array with OOK modulation in various array sizes, dead time, and background count rate. Experimentally, Rao et al. [18] demonstrated a multirate UPCC system at data rates up to 10.416 Mbps over a 9.1-m tap water channel. Hu et al. [19] achieved a PMT-based UPCC system using a 256-PPM; the length of channel and communication sensitivity are 120 m and 3.32 bits/photon in Jerlov II water. Chen et al. [20] used a 520-nm laser diode modulation to generate the OOK signal, whereas a high-sensitivity silicon photomultiplier was used at the receiver side to achieve an attenuation length of more than 14 at a communication rate of 20 Mbps.

By and large, in the reported research articles about UPCC systems, the research and analysis are based on a single IM such as OOK or PPM. It is well known that the OOK is one of the simplest IM techniques with high bandwidth utilization, but low power utilization makes the signal transmission distance limited. For PPM, the high-power utilization makes the signal transmission distance much higher, but low bandwidth utilization leads to a short bit duration, making it difficult for signal synchronization. Furthermore, digital pulse modulation techniques including differential pulse position modulation (DPPM), differential pulse interval modulation (DPIM), and dual-header pulse interval modulation (DH-PIM), combining both bandwidth utilization and power utilization, are expected to be a good alternative modulation technique for UPCC system in some application scenarios. Therefore, a comparative analysis of the communication performance of OOK modulation and various digital pulse modulations is not only important for optimizing the performance of the UPCC system, but also an important guide for the design of communication systems. Of course, as far as modulations are concerned, similar comparisons have been made by numerous researchers, but mostly based on positive-intrinsic-negative (PIN) and avalanche photodiode (APD) receivers. However, single-photon detector-based receivers differ from conventional PIN and APD-based receivers in terms of the statistical model of the signal output [21]. Therefore, it is significant to compare the performance of multiple IM schemes based on the photon counting receiver model.

In this article, an underwater photon counting system is built based on IM and direct detection (IM/DD) photon counting reception technique. First, this article introduces the bit-symbol mapping principles of OOK, PPM, DPPM, DPIM, and DH-PIM; the seawater channel model; the statistical model of the output of the SPAD under the influence of dead time; and the minimum error judgment criterion to obtain the expressions for the bit error ratio (BER) calculation. Second, the performance parameters of a commonly used UWOC system and a commercially available SPAD detector are selected to analyze and compare the communication performance of different IM methods in a pure seawater channel. For one thing, the article compares the variation of BER with a transmission distance of communication system for different modulation schemes when modulation bandwidth is fixed. For another thing, the same analysis is done under a fixed communication rate. Finally, the simulation results are shown and discussed.



## UPCC SYSTEM MODELING

The system architecture of UPCC, as shown in Figure 1, is composed of two parts: IM and DD photon-counting receiver. As demonstrated in Figure 1, the source bit is encoded and modulated into the optical carrier; the optical signal is transmitted through the underwater channel and degraded by the absorption, scattering, and turbulence effects of the medium. At the receiver, the photon-counting receiver that uses a SPAD working in counting mode is used to receive and process singlephoton signals. When the receiver works, the SPAD detects the weak photon signal to generate a single electrical pulse signal, and a large number of noise pulses are introduced due to SPAD dark counts and background noise. For these reasons, a screener is used to extract useful information by rejecting noisy count pulses regarding the synchronous clock. Finally, the count module counts the signal pulses within a certain period, and counted signal pulses are used to restore the initial code stream signal by comparing it with the threshold value. In addition, to increase the reliability of data transmission, communication systems often use channel coding and equalization, and so on. It should be noted that it is assumed that the UPCC system has been clock synchronized at both the transceiver side in this study.

# The Modulation Schemes for OOK and Digital Pulse Modulations

In the UPCC system with IM/DD, OOK and PPM are the commonly used IM schemes. Compared with OOK modulation, PPM has higher power utilization efficiency but

lower bandwidth utilization [22], which is often used in photon-counting communication systems to improve sensitivity. To optimize the bandwidth utilization of PPM, many digital pulse modulation schemes have been developed, such as DPPM, DPIM, DPIM, and DH-PIM. OOK modulation uses one optical pulse to represent a 1-bit signal, whereas digital pulse modulations decompose a signal symbol into multiple time slots; the position of the optical pulse within a symbol is used to represent multiple bits, with the remaining slots being empty. DPPM removes the redundant time slots that exist in PPM. For DPIM, each symbol begins with a slot-duration pulse, followed by a series of empty data slots, the number of which depends on the decimal value of the encoded M-bit data stream. To mitigate intersymbol interference degradation of the signal, a guard slot consisting of one or more empty slots is added after the pulse. Compared with PPM, DPPM, and DPIM, DH-PIM not only removes the redundant time slots that follow the pulse in the PPM and but also reduces the average symbol length compared with DPIM. The time-domain waveforms of OOK and several digital pulse modulation schemes are shown in Figure 2 [23]. As shown in the figure, to have the same data throughout as OOK, the slot duration time  $T_s$  of digital pulse modulation is shorter than the OOK bit duration time  $T_b$ .

For IMs, the digital signal is loaded into the carrier wave by modulating the intensity and position of a light wave. The biggest difference between these modulations is the number of slots in a single symbol, which influences directly the transmit optical power per ON slot. The more slots, the higher transmit optical power per ON slot when the average optical transmit power keeps fixed; the relation between the mean transmit power



**FIGURE 2** Time waveforms for OOK, DPIM, PPM, DPIM, DPPM, DH\_PIM ( $\alpha$  = 2). NRZ non-return-to-zero, RZ return-to-zero, IS information slots, RS redundant slots, GS guard slots; the time-domain waveform reflects the bit mapping relationships for the several intensity modulations. The presence or absence of an optical pulse is used to represent 1 bit of data in OOK modulation, and the duration time of the optical pulse is equal to 1-bit duration, whereas the duration of the optical pulse of OOK-RZ modulation is less than the duration of a single bit. When the duty ratio is 0.5, the light pulse duration of OOK-RZ modulation is half of the single bit duration. For PPM, The slot position of the optical pulse, corresponding to the decimal value of the M-bit input data, represents the information bit. DPIM and DPIM remove the redundant time slot after the optical pulse compared with PPM, whereas DH-PIM not only removes the redundant time slot after the PPM optical pulse but also reduces the number of time slots within a single symbol compared with DPIM.

<b>TABLE 1</b>   The modulation orders and the communication rates for different	
modulation schemes under a given $B$ and $M$ [23].	

Modulation schemes	Modulation order ( <i>L</i> or $\overline{L}$ )	Rates ( <i>R<sub>b</sub></i> )
PPM	2 <sup>M</sup>	MB/2 <sup>M</sup>
DPIM(1GUARD)	$(2^M + 3)/2$	$2MB/(2^{M}+3)$
DPPM	$(2^{M} + 1)/2$	$2MB/(2^{M}+1)$
DH-PIM	$(2^{M-1}+2\alpha+1)/2$	$2MB/(2^{M-1}+2\alpha+1)$

per symbol and optical power per ON slot can be expressed as  $P_{\rm ON} = LP_{\rm average}$ , where  $P_{\rm average}$  is the average optical of a symbol, and L is the length of a single symbol or usually named the modulation order. For OOK\_NRZ and OOK\_RZ, L is equal to 2 and 4, respectively. For the PPM,  $L = 2^M$  [24]. For DPPM, DPIM, and DH-PIM, different symbols have different numbers of time slots, so the symbol length is represented by the average symbol length, and the average symbol length  $\bar{L}$  can be found in [23]. The modulation orders and the communication rates for different modulation schemes under a given modulation bandwidth  $(B = 1/T_s)$  are listed in **Table 1**.

#### **Underwater Channel Model**

The absorption and scattering of the light by the seawater will cause the attenuation of the energy of the optical signal, especially when the turbidity of seawater is high; the signal quality will also deteriorate. The extinction coefficient  $c(\lambda)$  of seawater on light, which is determined by the absorption coefficient  $a(\lambda)$  and scattering coefficient  $b(\lambda)$  of seawater, can be expressed by the formula [25]:

$$c(\lambda) = a(\lambda) + b(\lambda) \tag{1}$$

In the formula, the units of the three parameters are  $m^{-1}$ . The energy loss factor  $L(\lambda, z)$ , decided by the light beam transmission distance z (m) and the wavelength  $\lambda$  (nm) of light, can be given by the following equation [26].

$$L(\lambda, z) = e^{c(\lambda)z}$$
(2)

The coefficients  $a(\lambda)$ ,  $b(\lambda)$ , and  $c(\lambda)$  for Petzold seawater types are presented in **Table 2** at the wavelength of 532 nm, which are taken from [27].

Many channel models of UWOC can be obtained from [25, 28–31]. When an optical beam is transmitting in the pure seawater and clear seawater, the temporal spread of the optical pulse can be neglected. Geometric Beer's Law (GBL) can be applied to these two water types to calculate the geometric attenuation since the beam spreading and alignment error [32]. In this article, we consider the line-of-sight communication link model. In this scenario, the light beam is directed from a transmitter into a receiver; both telescope gain and loss are taken into account, the optical signal reaching the receiver is obtained by [25]:

TABLE 2 | Absorption, scattering, and extinction coefficient for the Pure seawater and three Petzold water types.

Water type	Pure seawater	Clear seawater	Coastal seawater	Harbor seater
a (m <sup>-1</sup> )	0.0405	0.114	0.179	0.266
b (m <sup>-1</sup> )	0.0025	0.037	0.219	1.824
c (m <sup>-1</sup> )	0.043	0.151	0.298	2.190

$$P_{R} = \begin{cases} P_{ON}\eta_{T}\eta_{R}L\left(\lambda,\frac{d}{\cos\theta}\right)\frac{A_{Rec}\cos\theta}{2\pi d^{2}(1-\cos\theta_{0})} & \theta_{0} \\ P_{ON}\eta_{T}\eta_{R}L\left(\lambda,\frac{d}{\cos\theta}\right)\frac{A_{Rec}\cos\theta}{\pi(d\tan\theta_{0})^{2}} & \theta_{0} <<\pi/20 \end{cases}$$
(3)

where  $P_{ON}$  is the transmitted-light power per slot,  $\eta_T$  is the optical efficiency of the transmitter,  $\eta_R$  is the efficiency of the receiver, *d* is the perpendicular distance between the transmitter and receiver plane, and  $\theta$  is the angle between the perpendicular to the receiver plane and the transmitter-receiver trajectory, also known as the angle of inclination between transmitter and receiver.  $A_{\text{Rec}}$  is the receiver aperture area, and  $\theta_0$  is the optical beam divergence angle (half-angle transmit beam width) [25].

#### Underwater Turbulence Model

In the practical application of UWOC, considering aperture average effect, received optical power under the influence of underwater optical turbulence can be represented by log-normal distribution from weak to strong turbulence condition, which has been validated by a large number of field experiments. The probability density function (PDF) f(I) for the underwater channel can be expressed by the log-normal function [33]:

$$f(I) = \frac{1}{P\sigma\sqrt{2\pi}} \exp\left(-\frac{\left(\ln\left(I/I_0\right) + \sigma^2/2\right)^2}{2\sigma^2}\right)$$
(4)

where  $I_0$  is the mean received light energy in the time interval  $[0, T_s]$ . For plane-wave, the scintillation index (S.I),  $\sigma$ , can be expressed as [34]:

$$\sigma^{2} = \exp\left(\frac{0.49\sigma_{\rm r}^{2}}{\left(1+1.11\sigma_{\rm r}^{12/5}\right)^{7/6}} + \frac{0.51\sigma_{\rm r}^{2}}{\left(1+0.69\sigma_{\rm r}^{12/5}\right)^{5/6}}\right) - 1 \quad (5)$$

where  $\sigma_r^2$  is the Rytov variance; the classical Kolmogorov spectrum model can be given [35]:

$$\sigma_{\rm r}^2 = 44.76\epsilon^{2/3} \overline{\left(\frac{\partial T}{\partial z}\right)^2} \left(\frac{2\pi}{\lambda_{\rm light}}\right)^{7/6} z^{11/6} N^{-1} \tag{6}$$

where  $\varepsilon$  is the turbulence kinetic energy dissipation rate,  $\partial T/\partial z$  is the temperature gradient,  $\lambda_{light}$  is the optical wavelength, z is the transmitting distance of the light beam, and N represents the buoyancy frequency.

#### SPAD Photon-Counting Receiver Model

When the UWOC works, assume the average signal photon rate reaching the front end of the detector is the constant  $\lambda_s$ , the average background photon-counting rate is the constant  $\lambda_b$ , and the dark count rate of SPAD is the constant  $\lambda_d$ . Of course, the

other parameters including afterpulsing and timing-jitter, crosstalk, and fill-factor should also be considered, but in this article, we neglect these influences. Thus, the SPAD's photoelectron count model can be given:

$$\lambda = \begin{cases} \eta \lambda_{s} + \eta \lambda_{b} + \lambda_{d} & \text{signal} \\ \eta \lambda_{b} + \lambda_{d} & \text{no-signal} \end{cases}$$
(7)

where  $\eta$  is the photon detection efficiency of SPAD, the average photon arrival rate  $\lambda_s$ , and  $\lambda_b$  is related to the received optical power  $P_R$  of signal and background  $P_b$ ; the relational expression is given as:

$$\lambda_{\rm s} = \frac{\eta P_{\rm R}}{h\nu} \tag{8}$$

$$\lambda_{\rm b} = \frac{\eta P_{\rm b}}{h\nu} \tag{9}$$

where *h* is the Planck constant, and  $\nu$  is the frequency of the single photon.

We assume the sampling rate of SPAD is very high compared with the dead time so that the counting losses due to finite sampling rate can be negligible. If the dead time of SPAD is the constant  $\tau$ , the maximum number of photons recorded by SPAD during the slot interval time  $[0, T_s]$  can be expressed as  $k_{\text{max}} = [T_s/\tau] + 1$ , where [x] is the maximum that is smaller than *x*. The PDF of counting *k* photons in a timing period  $[0, T_s]$  is given [36]:

$$p(k, \lambda, T_{s}) = \begin{cases} \sum_{i=0}^{k} \frac{\lambda^{i} (T_{s} - (k+1)\tau)^{i}}{i!} \exp(-\lambda(T_{s} - (k+1)\tau)) \\ -\sum_{i=0}^{k} \frac{\lambda^{i} (T_{s} - k\tau)^{i}}{i!} \exp(-\lambda(T_{s} - k\tau)), \\ 0, & k \ge k_{max} \end{cases}$$
(10)

#### **Bit Error Ratio Calculation**

For OOK modulation, based on the principle of threshold test, the bit error ratio (BER) can be given as [37]:

$$P_{OOK} = \frac{1}{2} - \frac{1}{2} \sum_{k=0}^{k_{th}} \left[ \int_{0}^{\infty} p(k, \lambda_{sn}, T_s) f(I) dI - p(k, \lambda_n, T_s) \right]$$
(11)

where  $k_{th}$  is the optimum decision threshold of the number of photons in the interval time  $[0, T_s]$ , which can be obtained by the following decision principle of the threshold.

For PPM, DPIM, DMMP, and DH-PIM symbol, the symbol error ratio (SER) for a continuous output *L*-order digital pulse modulation signal is [38] :

$$P_{SER} = 1 - \left[ 1 - \frac{1}{L} \sum_{k=0}^{k_{th}} \int_{0}^{\infty} p(m, \lambda_{sn}, T_{s}) f(I) dI - \frac{L-1}{L} \sum_{k=k_{th}}^{\infty} p(k, \lambda_{n}, T_{s}) \right]^{L}$$
(12)

The SER can be converted into BER by:

$$P_{BER} = \frac{LP_{SER}}{2(L-1)}$$

Based on the principle of minimum error probability [39], by solving the following **Eq. 13**, we can get the optimum threshold  $k_{th}$ .

$$\frac{\int_{0}^{\infty} p(k, \lambda_{sn}, T_{s}) f(I) dI}{p(k, \lambda_{n}, T_{s})} = \frac{P(0)}{P(1)}$$
(13)

where P(0) and P(1) are a prior probability of time slot detection.

#### NUMERICAL RESULTS AND DISCUSSION

In this research, with the assumption of negligible delay spread, based on the GBL model and SPAD photon-counting receiver model, we establish the relationship between the BER and attenuation length on the underwater wireless UPCC system in the pure seawater. The effect of M on various IM schemes is also investigated. The parameters of the UWOC system are listed in Table 3. In the following discussion, the specifications of the SPCM20A from Thorlabs [40] have been applied to this simulation. The values of other parameters characterize the classical channel of the UWOC system. According to [41], the attenuation length, which is defined as the multiple of the transmission distance and attenuation coefficient, is used to represent the link transmission distance to remove the ambiguity of distance and various water conditions. In addition, with the assumption of negligible slot time delay spread, the degradation of signal bandwidth and the intersymbol caused by channel transmission can be ignored. Therefore, the mathematical relationship between data rate and modulation bandwidth in Table 1 [23] can be used in this article.

On the one hand, BERs for OOK, PPM, DPIM, DPPM, and DH-PIM as the function of attenuation length when  $T_s = 15\tau$  (modulation bandwidth B = 1.9 Mbps) are given in **Figure 3**. The forward-error-correction (FEC) limit of  $3.8 \times 10^{-3}$ , a commonly used BER at some of the reported UWOC systems [42–44], and some FEC codes providing reliable communication with an overhead of approximately 7% [45], is regarded as a criterion for evaluation in this article. As shown in **Figure 3**, BERs of all modulation schemes rise with the increment of attenuation length. At the FEC limit, the OOK system can arrive the maximum attenuation length for M = 2, and the attenuation length that the DH\_PIM system can achieve its minimum. For the fixed modulation bandwidth and average transmit power, to achieve the same BER, the UPCC system for all digital pulse modulation schemes transmits over a shorter distance than the

TABLE 3 | Parameters of UPCC system.

Parameter	Symbol	Value
The wavelength of lighter (nm)	λ	532
Extinction coefficient $(m^{-1})$	С	0.045
Divergence angle (rad)	$\lambda_0$	0.1745
Average transmit power (W)	PT	1.0
Transmitter inclination angle (rad)	θ	0
Photon efficiency of the transmitter	$\eta_{T}$	0.9
The optical efficiency of the receiver	$\eta_{\rm B}$	0.9
Receiver aperture (mm)	D	350
Photon detection effeciency@532 nm	η	35%
Deadtime (ns)	τ	35
Dark count rate (counts/sec)	$\lambda_d$	60
Background photon count (counts/slot)	$\lambda_b$	0.01
Average turbulence kinetic energy ( $m^2 s^{-3}$ )	ε	$3 \times 10^{-10}$
temperature gradient (°C m <sup>-1</sup> )	∂T/∂z	7.94 × 10 <sup>-6</sup>
Average buoyancy frequency(s <sup>-1</sup> )	<n></n>	$2.9 \times 10^{-4}$

OOK\_RZ modulation system when M = 2. The longer the transmission distance, the higher the power utilization is. Thus, the DPIM with a guard slot has higher power utilization than DPPM, and the power utilization of PPM is the highest. As bit resolution improves, when M = 4, 6, 8, the power utilizations of DH-PIM ( $\alpha \le 4$ ), DPPM, DPIM (1GUARD), and PPM have higher power utilization than OOK modulation, and the power utilization of DPPM and DPIM(1GUARD) tends to keep consistent. When the modulation bandwidth and average transmit power are certain, it should be noted that the communication distance that can be achieved by OOK modulation at a given BER does not change with M.

DH-PIM is one of the digital pulse modulations. Compared with PPM and PIM, DH\_PIM not only removes the redundant time slots that follow the pulse in the PPM but also reduces the average symbol length compared with PIM [46]. In DH-PIM, the nth symbol starts with a header duration and follows with a sequence of  $d_n$  empty slots, the header duration consists of a header pulse  $H_n$  and a guard band  $G_n$ , and the value of  $d_n$  is the decimal value of modulated binary codeword within a symbol. If the value of  $d_n \in \{0, 1, \dots, 2^{M-1}\}$ ,  $H_1$  will be as header pulse; otherwise, the header pulse will be  $H_1$ . The duration time of the header  $H_1$  and  $H_2$  is  $0.5\alpha T_s$  and  $\alpha T_s$ , respectively; each header pulse is followed by a guard band  $G_n \in \{(0.5\alpha + 1)T_s, T_s\}$ ; the number of empty slots is equal to the decimal value of modulated binary codeword and the decimal value of complement of the modulated binary word. In this modulation, the header pulse plays dual roles of symbol initial and time reference for preceding and succeeding symbol. For the value,  $\alpha$ , which is an adjustment factor, the average symbol length  $\overline{L}$  of DH\_PIM will be changed by adjusting  $\alpha$  When  $\alpha$  is reduced, the reduction of average symbol length improves transmission throughput. By analysis, we can conclude that with increasing the  $\alpha$ , the BER becomes bigger gradually when the system transmits the same attenuation length, or when BER is a constant, the smaller the adjustment factor  $\alpha$ , the bigger the attenuation length.

As the results of the above analysis, increasing the value of the M for the same modulation bandwidth significantly improves the power utilization of the digital pulse





modulation so that the attenuation length of the system increases. However, M is related to the bandwidth utilization, which decides the transmission rate of a communication system. The higher transmission rate means the higher bandwidth utilization for the same M.

We limit the BER simulation results to below the FEC limit; the transmission rates and attenuation lengths of a system for DH-PIM, PPM, DPPM, and DPIM under the different M are shown in Figure 4. This figure clearly shows the trade-off between transmission rate and attenuation length. For PPM, DPIM, and DPPM systems, the attenuation length increases with M, but the transmission rate decreases accordingly. This is because for digital pulse modulation schemes, when the modulation bandwidth is fixed, the power utilization is proportional to the value of M, and the bandwidth utilization is inversely proportional to M. For DPIM with a guard slot, the transmission rate and attenuation length of the system are almost the same for M = 6 and M = 8. Comparing the performance of DPIM with a guard slot and PPM, the system for the PPM scheme can achieve a longer transmission length, but the transmission rate is lower than the DPIM system at a certain value of M. For DH-PIM, the bandwidth utilization efficiency is the highest of all digital pulse modulations, and it is evident that there is the highest point of transmission rate for DH-PIM when M = 4.

On the other hand, to do a fair comparison between the different IM schemes, the communication performance of the UPCC system under the various IM schemes is compared when the data rate and average transmit optical power are fixed. As shown in **Figure 5**, setting the bit rate to 50 Kbps, the value of *M* is 2, 4, 6, 8 in sequence. When M = 2 and BER is the



FEC limit, the minimum attenuation length that DH-PIM ( $\alpha$  = 4) can transmit is approximately 15.74 and the maximum attenuation length that OOK-RZ can transmit is approximately 16.90. Similarly, when M = 4, the attenuation lengths of DH-PIM ( $\alpha = 4$ ) and OOK-RZ are 16.38 and 16.90, respectively. When M is 6 and 8 separately, the attenuation lengths of DH-PIM ( $\alpha = 4$ ) and OOK (OOK-NRZ and OOK-RZ) can arrive at 16.73 and 16.90, and 16.99 and 16.90. We can conclude that the performance of the OOK keeps constant, but the other system performances do not improve much with the increase in M. For digital pulse modulation schemes, the power utilization is proportional to the value of M, and the bandwidth utilization is inversely proportional to M. The power utilization is improved, and the bandwidth utilization is decreased with the increase in M. When the transmission rate keeps fixed, an increasing Maffects both the bandwidth utilization and the power utilization of the system, which makes the performance of the system with digital pulse modulations not improve much. But, for OOK, the power utilization and the bandwidth utilization keep constant with the increase in M; the performances of the OOK as M increases have no changes. Compared with digital pulse modulation schemes, OOK has poor power utilization efficiency, but good bandwidth utilization efficiency compensates for this disadvantage. Therefore, when M = 2, the performance of the UPCC system with OOK is much better than the other systems in

the overall comparison. As M increases, digital pulse modulations can transmit a longer attenuation length than OOK modulation. Except for DH-PIM, the digital pulse modulations can transmit a longer attenuation length than OOK modulation for M > 2. Various modulation schemes, including DPIM (1GUARD), DPPM, and PPM, tend to transmit the same distance at the same rate when M = 4and M = 6. However, with the increase in the value of M, the DPPM and DPIM (1GUARD) display a more excellent communication performance compared with DH-PIM and PPM schemes when M = 8.

## CONCLUSION

In this article, a UPCC system model based on IM and DD photon counting reception techniques is built. The article compares the variation of BER with a transmission distance of communication system for OOK, PPM, DPIM, DPPM, and DH-PIM under the same modulation bandwidth. From our analysis, we conclude that the PPM has the longest transmission distance at the same BER when M > 2, but the lowest communication rate. Transmission distance gets farther, and the communication rate gets lower as *M* increases. In addition, the same analysis is done under a fixed communication rate. It is concluded that the DPPM and DPIM have the optimum communication performance at

the same communication rate when M = 8. As the modulation bandwidth is lower and the time slot time is longer for DPPM and DPIM than PPM when the communication rate is the same, long slot time will help reduce the difficulty of signal synchronization and hence the complexity of the underwater photon counting system. The simulation and analysis in this article are based on published theoretical models, and the results concluded can be referenced for real transmission communication.

## DATA AVAILABILITY STATEMENT

The original contributions presented in the study are included in the article/supplementary material, further inquiries can be directed to the corresponding authors.

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### **AUTHOR CONTRIBUTIONS**

XX, WW, and XH conceived the idea of the study; XH and PL analyzed the data, interpreted the results, and wrote the article; all authors discussed the results and revised the manuscript.

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