



# Dual-Band Bandpass Filter With Controllable Stopband Bandwidth

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A novel dual-band bandpass filter (BPF) is proposed with independently controllable transmission zeros (TZs) which can realize widely tunable stopband bandwidth (BW). The planar microstrip filter consists of a three-degree L-C ladder lowpass filter loaded with two unsymmetrical shorted stubs which are used to produce different TZs. By tuning the parameters of the two unsymmetrical shorted stubs, the TZs can be independently controlled. Therefore, the BPF has independent controllable center frequencies (CFs), passband bandwidths, and stopband bandwidths between adjacent passbands. All the L-C values in the equivalent circuit of the proposed filter are optimized to fulfill the design specifications. For demonstration, a dual-band BPF is designed. The measured results show good agreement with the simulated ones.

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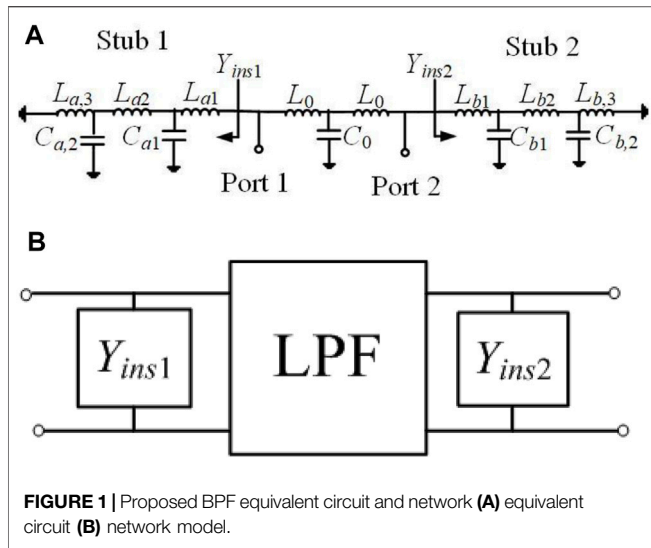
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## INTRODUCTION

Modern wireless communication systems need high performance filters which have controllable CFs, passband bandwidths, stopband bandwidths, and sharp rejection. Different designing structures and methods have been greatly studied [1–17]. Generally, the dual-band bandpass filter (BPF) adjusts the CFs by changing transmission poles (TPs) [1, 2]. To suppress the harmonic responses, the multiple resonant modes excited by a stepped impedance stub-loaded resonator are used to design dual-band BPFs with a wide upper stopband [3]. However, there is only one transmission zero (TZ) in the stopband. Therefore, the stopband bandwidth is narrow. By introducing more TZs in the stopband, the performances of selectivity and stopband bandwidth can be enhanced. Signal-interference principles [4–6] are applied to design single- or dual-band BPFs with broad stopband bandwidths by creating multiple TZs. To design high performance filters with multiple passbands, the method of multiple mono-frequency resonators coupling to a non-resonating node is proposed in [7]. To have more TZs, couplings between the non-resonating nodes are introduced in [8], or couplings and more open/shorted-substubs [9, 10] are applied in the configurations. However, it is difficult to realize the coupling for application when the number of passband increases. Moreover, TZs introduced by the coupling matrix need to change all the coupling coefficients, so it is also difficult to independently adjust the position of TZs [11].

This study presents a novel BPF loaded with two unsymmetrical shorted stubs to introduce two different TZs in the stopband to realize the controllable stopband bandwidth. Following our early work [12], the theoretical analysis of the TZs and TPs is shown in this study, which can demonstrate that the design method has advantages of simplicity and effectiveness. A three-degree lowpass filter



prototype is chosen for simplicity; the in-band performance will be improved when choosing more degrees of the lowpass filter prototype. A dual-band BPF has been designed and fabricated to verify the proposed concept.

### ANALYSIS

The equivalent circuit and network of the proposed prototype are shown in **Figure 1**. The network can be divided into three subnetworks, as shown in **Figure 1B**, which are the lowpass filter (LPF) section in the middle and two unsymmetrical shunt admittance sections at the sides. The LPF section is also a symmetric network and has chosen a three order L-C ladder prototype for simplicity, as shown in **Figure 1A**.

From our early analysis in [12], the shorted stub with two equivalent capacitors will introduce two TZs. As shown in **Figure 1**, the configuration has two unsymmetrical shorted stubs; the shunt admittances of Stub1 and Stub 2 have different LC values, which will produce four different TZs.

The ABCD matrix of the transmission network in **Figure 1B** is expressed as follows, where  $M_{Y1}$  and  $M_{Y2}$  are the ABCD matrices of the Stub 1 and Stub 2, respectively.  $M_{LPF}$  is the ABCD matrix of the middle LPF section. According to the relationship of scattering parameters with the ABCD matrix, the TZs and the reflection zeros (TPs) are the roots of polynomials  $P(s)$  and  $F(s)$ , respectively, where the impedance of the source/load is normalized to be 1. When the root of  $F(s)$  is an imaginary number, the reflection zero related to the root represents a TP.

$$M_{Y1} = \begin{bmatrix} 1 & 0 \\ Y_{ins1} & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ \frac{D_1(s)}{N_1(s)} & 1 \end{bmatrix} \tag{1a}$$

$$= \frac{1}{N_1(s)} \begin{bmatrix} N_1(s) & 0 \\ D_1(s) & N_1(s) \end{bmatrix},$$

$$N_1(s) = C_{a1}C_{a2}L_{a1}L_{a2}L_{a3}s^5 + [C_{a1}L_{a1}(L_{a2} + L_{a3}) + C_{a2}L_{a3}(L_{a1} + L_{a2})]s^3 + (L_{a1} + L_{a2} + L_{a3})s, \tag{1b}$$

$$D_1(s) = C_{a1}C_{a2}L_{a2}L_{a3}s^4 + (C_{a1}L_{a2} + C_{a1}L_{a3} + C_{a2}L_{a3})s^2 + 1, \tag{1c}$$

$$M_{Y2} = \begin{bmatrix} 1 & 0 \\ Y_{ins2} & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ \frac{D_2(s)}{N_2(s)} & 1 \end{bmatrix} \tag{2a}$$

$$= \frac{1}{N_2(s)} \begin{bmatrix} N_2(s) & 0 \\ D_2(s) & N_2(s) \end{bmatrix},$$

$$N_2(s) = C_{b1}C_{b2}L_{b1}L_{b2}L_{b3}s^5 + [C_{b1}L_{b1}(L_{b2} + L_{b3}) + C_{b2}L_{b3}(L_{b1} + L_{b2})]s^3 + (L_{b1} + L_{b2} + L_{b3})s, \tag{2b}$$

$$D_2(s) = C_{b1}C_{b2}L_{b2}L_{b3}s^4 + (C_{b1}L_{b2} + C_{b1}L_{b3} + C_{b2}L_{b3})s^2 + 1, \tag{2c}$$

$$M_{LPF} = \begin{bmatrix} L_0C_0s^2 + 1 & L_0^2C_0s^3 + 2L_0s \\ C_0s & L_0C_0s^2 + 1 \end{bmatrix} \tag{3}$$

$$= \begin{bmatrix} a(s) & b(s) \\ c(s) & d(s) \end{bmatrix},$$

$$\begin{bmatrix} A & B \\ C & D \end{bmatrix} = M_{Y1} \times M_{LPF} \times M_{Y2} \tag{4a}$$

$$= \frac{1}{N_1(s)N_2(s)} \begin{bmatrix} A'(s) & B'(s) \\ C'(s) & D'(s) \end{bmatrix}$$

$$= \frac{1}{P(s)} \begin{bmatrix} A'(s) & B'(s) \\ C'(s) & D'(s) \end{bmatrix}, \tag{4b}$$

$$P(s) = N_1(s)N_2(s),$$

$$F(s) = A'(s) + B'(s) - C'(s) - D'(s) \tag{5}$$

$$= N_1(s)N_2(s)[b(s) - c(s)]$$

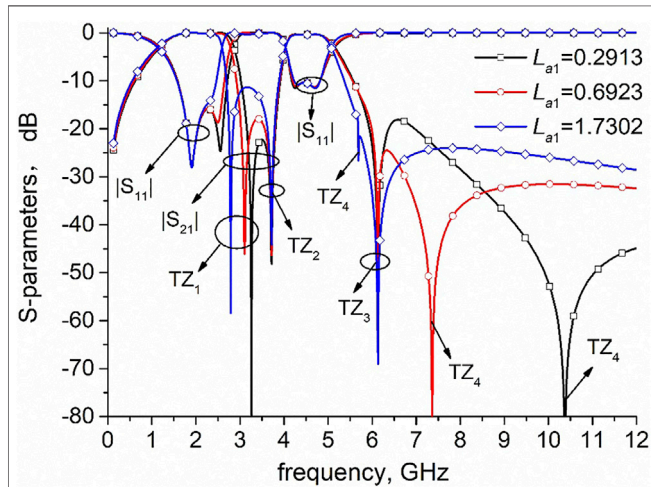
$$- [N_1(s)D_2(s) + D_1(s)N_2(s)]a(s) - D_1(s)D_2(s)b(s).$$

From **(Eq. 4b)**, polynomial  $P(s)$  has  $4n+2$  roots ( $n = 2$ ), of which 2 roots are at the origin and others are conjugate and symmetrical on the imaginary axis. Therefore, each shorted stub produces  $n$  TZs and the two unsymmetrical shorted stubs produce  $2n$  different TZs on the imaginary axis. From **(Eq. 5)**, the degree of polynomial  $F(s)$  is  $4n+5$ .  $N_1(s)$ ,  $N_2(s)$ ,  $b(s)$ , and  $c(s)$  have odd terms only, while  $D_1(s)$ ,  $D_2(s)$ , and  $a(s)$  have constant terms. Therefore, polynomial  $F(s)$  has one root at the origin; two real roots and the remaining  $4n+2$  roots are conjugate and symmetrical on the imaginary axis or in four quadrants. The optimization algorithm is used to obtain the required lumped element values for independently controlling the TZs and the return losses, such as genetic algorithm and so on.

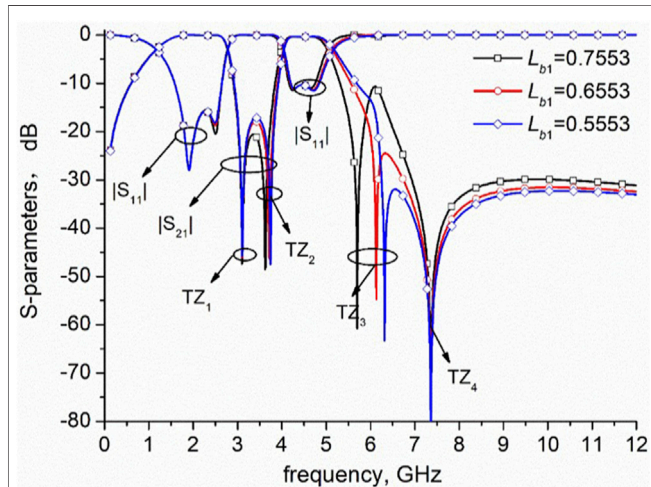
Since one of the two shorted stubs can tune two TZs, a dual-band BPF is presented for demonstration. The optimized L-C values are shown in **Table 1**. The S-parameters of the circuit with different parameters of the shorted stub are shown in **Figures 2, 3**. The parameter  $L_{a1}$  of the shorted stub 1 can tune TZ<sub>1</sub> and TZ<sub>4</sub>, which means the first passband CF and stopband bandwidth can

**TABLE 1** | Optimized L-C values for a dual-band BPF ( $L$  unit in nH,  $C$  unit in pF).

$L_{a1}$	$L_{a2}$	$L_{a3}$	$L_{b1}$	$L_{b2}$	$L_{b3}$
0.6923	2.1267	2.2803	0.6053	2.6080	2.0501
$C_{a1}$	$C_{a2}$	$C_{b1}$	$C_{b2}$	$C_0$	$L_0$
0.9256	2.0160	1.4576	1.3815	0.9321	1.7690

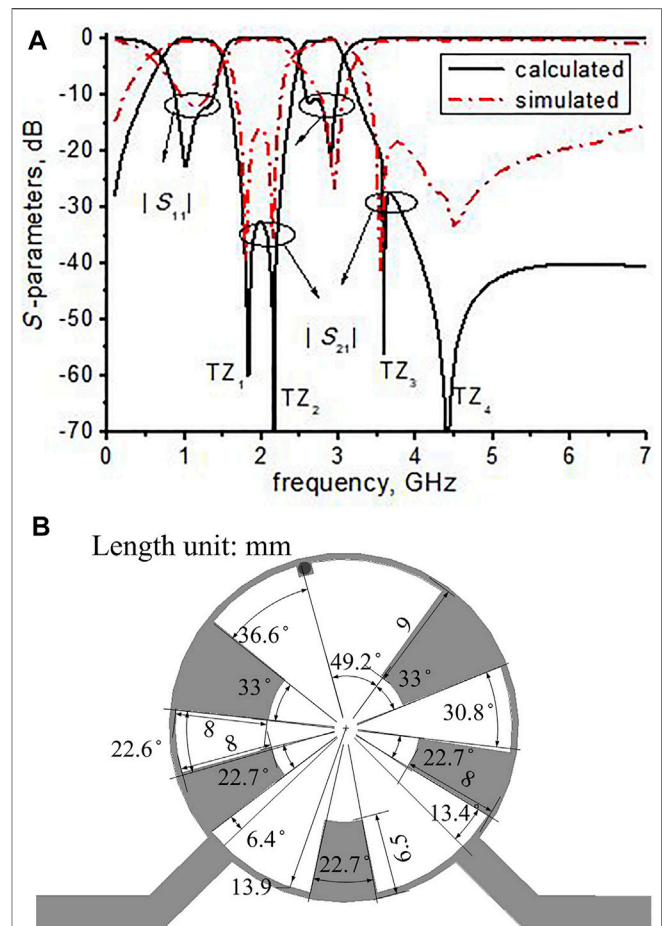


**FIGURE 2** | Tunable  $TZ_1$  and  $TZ_4$  versus different  $L_{a1}$ .

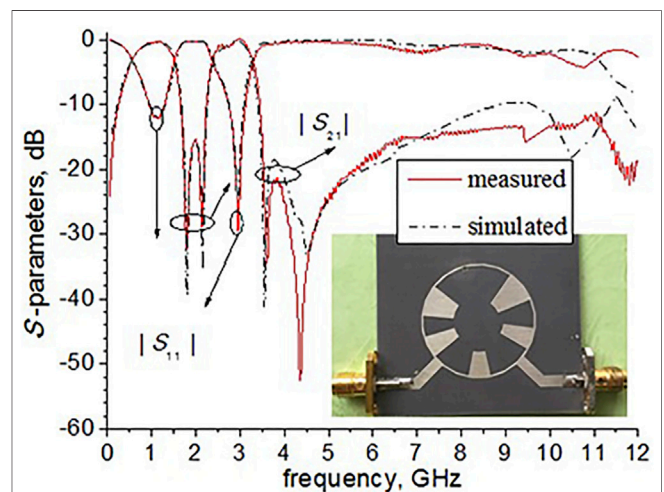


**FIGURE 3** | Tunable  $TZ_2$  and  $TZ_3$  versus different  $L_{b1}$ .

be tuned independently, while the second passband width,  $TZ_2$  and  $TZ_3$  keep unchanged. The larger the value of  $L_{a1}$ , the smaller will be the frequencies of  $TZ_1$  and  $TZ_4$ . Meanwhile, when the parameter  $L_{b1}$  of the shorted stub 2 changes, the frequencies of  $TZ_2$  and  $TZ_3$  vary simultaneously. As shown in **Figure 3**, the value of  $L_{b1}$  gets large and the frequencies of  $TZ_2$  and  $TZ_3$  decrease, which move at the same direction as that of  $TZ_1$  and  $TZ_4$ . Therefore, the bandwidth of the second passband can be



**FIGURE 4** | Calculated and measured S-parameters and optimized structure (A) calculated and simulated S-parameters (B) optimized BPF structure.



**FIGURE 5** | Simulated and measured S-parameters with photograph inset.

**TABLE 2** | Comparison of the proposed filter with previous designs.

Ref.	CF (GHz)/FBW (%)	IL (dB)	OBS	Controllable TZs	Size ( $\lambda_g \times \lambda_g$ )
[3]	1.5/12.7, 2.41/9.1	1.1, 0.9	2.4 $f_{02}$ , >20 dB	--	0.12 $\times$ 0.09
Prototype 2 in [4]	0.68/94.9, 2.33/26.4	0.09, 0.83	--	3	0.5 $\times$ 0.75
[7]	0.72/16.7, 1/13	0.55, 0.6	--	3	0.27 $\times$ 0.39
[8]	0.7/--, 0.8/--	--	1.3 $f_{02}$ , >20 dB	2	--
[12]	1.08/103.2, 3.05/48.5	0.2, 0.6	2.7 $f_{02}$ , >15 dB	2	0.2 $\times$ 0.19
This work	1.03/91.3, 2.8/31	0.5, 0.8	4.3 $f_{02}$ , >10 dB	4	0.15 $\times$ 0.15

tuned independently. Since the position of the last TP is near that of TZ<sub>3</sub>, the upper stopband performance is effected by the move of TZ<sub>3</sub>.

## RESULTS

A dual-band BPF is designed and fabricated to demonstrate the design method. The CFs of dual passbands are 1 and 2.8 GHz, respectively. The stopbands are 1.75–2.2 GHz (<25 dB) and >3.55 GHz (<25 dB), respectively. Therefore, the TPs are preset as 1.8, 2.15, 3.6, and 4.4 GHz. The optimized L-C values are  $L_{a1} = 0.5922$ ,  $L_{a2} = 2.5267$ ,  $L_{a3} = 3.3803$ ,  $L_0 = 3.0691$ ,  $L_{b1} = 1.1153$ ,  $L_{b2} = 2.4080$ ,  $L_{b3} = 3.9501$  (unit in nH),  $C_{a1} = 2.8256$ ,  $C_{a2} = 3.2161$ ,  $C_0 = 1.4321$ ,  $C_{b1} = 2.8576$ , and  $C_{b2} = 3.6815$  (unit in pF). The S-parameters calculated by the optimized L-C values are shown in **Figure 4A**. The roots of  $P(s)$  are 0, 0,  $\pm 1.83j$ ,  $\pm 2.16j$ ,  $\pm 3.59j$ , and  $\pm 4.41j$ , which are calculated in unit GHz for facility. The positive imaginary roots of  $P(s)$  represent the TZs. The L-C values of shunt admittance  $Y_{ins1}$  control TZ<sub>2</sub> and TZ<sub>4</sub>, while the L-C values of shunt admittance  $Y_{ins2}$  control TZ<sub>1</sub> and TZ<sub>3</sub>. The roots of  $F(s)$  are 0,  $-0.05 \pm 1.01j$ ,  $0.1 \pm 1.37j$ ,  $-0.07 \pm 2.59j$ ,  $0.04 \pm 2.9j$ ,  $0.03 \pm 3.58j$ ,  $-8.94$ , and 15.15. Since the roots  $0.03 \pm 3.58j$  of  $F(s)$  are close to the roots  $\pm 3.59j$  of  $P(s)$ , the second passband has two TPs not three TPs [7].

The BPF is simulated and fabricated on a substrate with  $\epsilon_r = 2.65$ ,  $\tan\delta = 0.003$ , and  $h = 1$  mm. Here, we choose the 117.8  $\Omega$  high-impedance line, which has the line-width of 0.5 mm. As shown in **Figure 4B**, the line width of the open stub which acts as the capacitor is tapered. The characteristic impedance is calculated by the waist width of the taper. Due to the discontinuity of the microstrip line and the minor coupling between the open stubs, the final dimension parameters are optimized by the full-wave electromagnetic simulation software HFSS. The optimized values of parameters are given in **Figure 4B**. The circuit size is about  $0.15 \lambda_g \times 0.15 \lambda_g$ , where  $\lambda_g$  is the guided wavelength at  $f_{01}$ . The simulated S-parameters agree well with the calculated ones,

as shown in **Figure 4A**. **Figure 5** shows the simulated and measured S-parameters with the photograph inset. The measured results are in good agreement with the simulated ones. The discrepancies between the simulated results and the measured results may be due to the ignorance of transmission line discontinuity and fabrication tolerances. The measured CFs, fractional bandwidths (FBWs), insertion losses (ILs) at the CF, out-band suppressions (OBSs), the number of controllable TZs, and the size are listed in **Table 2**. As shown in **Table 2**, the proposed dual-band BPF with simple circuit topology has advantages such as relative low IL, wide FBW, wide upper stopband, and more controllable TZs.

## CONCLUSION

A dual-band BPF with a controllable stopband bandwidth between the passbands is designed by the method of independently controlling TZs. By tuning the parameters of the two unsymmetrical shorted stubs, the introduced two TZs between adjacent passbands can be independently controlled. After optimizing the equivalent circuit lumped element values, the CFs, passband bandwidths, and stopband bandwidths can be tuned in a certain range. With a simple filter structure and good performance, the proposed method is attractive for application in high-selectivity filter designs.

## DATA AVAILABILITY STATEMENT

The original contributions presented in the study are included in the article/Supplementary Material; further inquiries can be directed to the corresponding author.

## AUTHOR CONTRIBUTIONS

All authors listed have made a substantial, direct, and intellectual contribution to the work and approved it for publication.

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