



A Comprehensive Review of Fluorescence Correlation Spectroscopy

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Fluorescence correlation spectroscopy (FCS) is a powerful technique for quantification of molecular dynamics, and it has been widely applied in diverse fields, e.g., biomedicine, biophysics, and chemistry. By time-correlation of the fluorescence fluctuations induced by molecules diffusing through a focused light, FCS can quantitatively evaluate the concentration, diffusion coefficient, and interaction of the molecules *in vitro* or *in vivo*. In this review, the basic principle and implementation of FCS are introduced. Then, the advances of FCS variants are reviewed, covering dual-color FCCS, multi-focus FCS, pair correlation function (pCF), scanning FCS, focus-reduced FCS, SPIM-FCS, and inverse-FCS. Besides, the applications of FCS are demonstrated with the measurement of local concentration, hydrodynamic radius, diffusion coefficient, and the interaction of different molecules. Lastly, a discussion is given by summarizing the pros and cons of different FCS techniques, as well as the outlooks and perspectives of FCS.

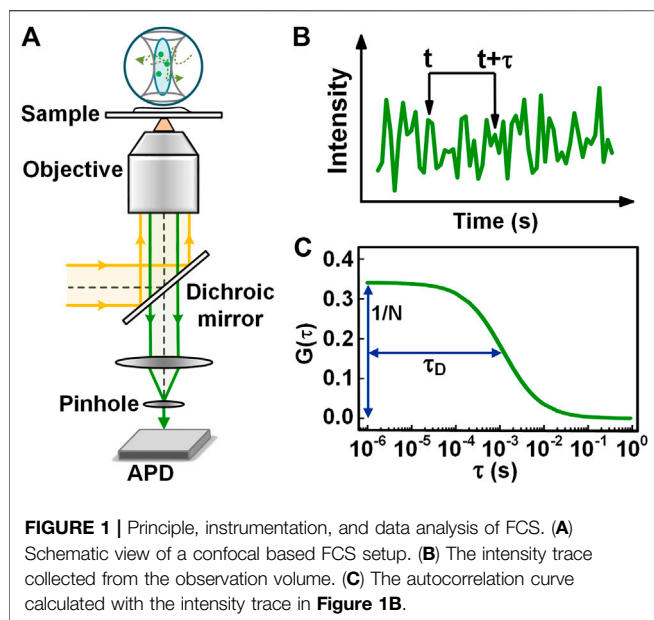
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INTRODUCTION

Molecular dynamics in biological systems are the foundation of life events. Fluorescence correlation spectroscopy (FCS) is a powerful tool for detecting molecular dynamics through analyzing the intensity fluctuation emitted by biomolecules diffusing in and out of a focused light [1–3]. The local concentration, hydrodynamic radius, diffusion coefficient, and the interaction of different proteins, etc. [4–7] can be accurately measured with FCS. Compared with other dynamics orientated approaches, FCS has a broader measurable time range spanning from ~ns to ~s, and a higher sensitivity that can be up to a single-molecule level.

FCS was first proposed by Magde *et al.* in 1972, which was designed for the measurement of the binding of the fluorescent dye EtBr and DNA [8]. It has become a practical tool for the investigation of molecular dynamics since the 1990s when FCS was firstly implemented with confocal microscopy. Confocal microscopy provides a much-confined observation volume ~0.5 fl, which enhances the signal-to-noise ratio (SNR) of FCS significantly [9].

When investigating diverse dynamic processes in live biological systems, FCS is inevitably complicated with many factors, such as the movement of cells, the photobleaching of fluorophores, and anomalous dynamics in sub-diffraction regions, etc. To overcome these difficulties, many advances have been initiated to extend the capability of FCS during the past two decades. To name a few, dual-color FCCS [10] was proposed to measure the interaction of different molecules. Space-multiplexing techniques allow FCS to probe dynamics at different locations [11]. Pair correlation function (pCF) based FCS provides information on the



directional motion of molecules along a certain direction, *i.e.*, between a pair of points [12]. Parallel/perpendicular line-scanning FCS [13] overcomes the photo-bleaching caused by slow diffusion of molecules on the membranes by swiftly scanning the focus on the membrane or perpendicular to the membrane. Moreover, the perpendicular line-scanning FCS overcomes the artificial fluorescence signal fluctuation caused by membrane movements. The combination of stimulated emission depletion (STED) and FCS [14] reduces the detection volume and consequently enables us to detect anomalous diffusion in the nanoscale regions. Single plane illumination microscopy based FCS (SPIM-FCS) [15] combines light-sheet illumination with FCS to acquire molecular information from thousands of pixels simultaneously and reduce the observation volume along the z -axis effectively. Inverse-FCS [16] measures the particle volume independent of diffusion dynamics by analyzing the fluctuation of unlabeled particles in the context of a densely labeled surrounding medium. Moreover, the extensions arise in data analysis, such as photon counting histogram (PCH) [17] and fluorescence intensity distribution analysis (FIDA) [18], which are capable of obtaining the molecular brightness that not available in FCS. These above advances extend the capability of conventional FCS in different aspects and make it suitable for measuring the biomolecular dynamics and interactions in complex biological environments.

In this review, the basic principle, the implementation schemes, and data analysis of FCS are elaborated at first. Secondly, the advances in FCS, including dual-color FCCS, multi-focus FCS, pair correlation function (pCF) based FCS, scanning FCS, focus-reducing FCS, inverse-FCS, and PCH are elaborated in both conception or implementation. Thirdly, the applications of FCS in chemistry and biology are outlined. Eventually, the comparison among the different FCS approaches, as well as the outlooks and perspectives of FCS, are discussed.

PRINCIPLE OF FLUORESCENCE CORRELATION SPECTROSCOPY

Experimental Setup

FCS is based on the analysis of time correlations in fluorescence fluctuation emitted when fluorescently labeled molecules are diffusing in and out of a tiny observation volume [2]. In the implementation, FCS is often performed in a confocal system, as illustrated in **Figure 1A**. The fluorescence emitted from the fluorescently-labeled molecules in the observation volume is collected by the same objective, and propagate along the opposite direction to that of the excitation/depletion light. After passing through a long-pass dichroic mirror, the fluorescence is focused through a pinhole onto an avalanche photodiode (APD). The fluorescence emitted in the out-of-focus region is rejected by the pinhole, and therefore, it does not reach the detector. Consequently, the pinhole reduces the axial extension of the observation volume. Such confined observation volume enhances the signal-to-noise ratio significantly and also reduces the measurement time needed to obtain a decent correlation curve. Despite a continuous-wave (CW) laser is available for FCS, the usage of pulsed lasers for excitation and time-correlated single-photon counting (TCSPC) for detection is preferable for the rejection of environmental background and also allows performing dual-color FCCS in a pulsed interleaved excitation scheme [19].

Data Analysis

To perform dynamics measurement with FCS, a sample of the fluorescently-labeled molecules is placed in the focal plane of the confocal microscope. Due to the free diffusion of molecules by nature, an intensity fluctuation $F(t)$ will be induced when the molecules are diffusing in and out of the observation volume. Then, the autocorrelation of $F(t)$ is calculated with:

$$G(\tau) = \frac{\langle F(t)F(t+\tau) \rangle}{\langle F(t) \rangle^2} - 1 \quad (1)$$

$\langle \rangle$ represents the temporal average, τ is the lag time. $G(\tau)$ is a measure of the self-similarity of a signal in time, *i.e.*, the overlap of a signal with itself at various lag time τ . With the approximation, the observation volume has a 3D Gaussian profile, $G(\tau)$ can be fitted with a 3D diffusion model:

$$G(\tau) = \frac{1}{N} \left(1 + \frac{\tau}{\tau_D} \right)^{-1} \left(1 + \frac{\tau}{\tau_D} \cdot \frac{r_0^2}{z_0^2} \right)^{-1/2} \quad (2)$$

N is the average molecule number in detection volume, τ_D is the average time of molecules diffusing through the detection volume. r_0 and z_0 are the lateral and axial radial distances over which the intensity decay by $1/e^2$ in the lateral and axial directions, respectively. For 2D diffusions, such as the molecule diffusion on membranes, **Eq. 2** still holds after the substitution of $r_0/z_0 = 0$. Apparently, the amplitude of the correlation curve $G(0)$ is inversely proportional to the average number of fluorescent molecules N in the observation volume, *i.e.*, $G(0) \sim 1/N$. Furthermore, the width of the correlation curve $\tau_D = r_0^2/(4D)$ represents the average time a molecule diffuses

through the waist of the focus laterally. Here D indicates the diffusion coefficient of the molecules. For quantitative analysis, N and τ_D can be obtained by fitting $G(\tau)$ with the model in Eq. 2. Then, the diffusion coefficient $D = r_0^2 / (4\tau_D)$ can be obtained once r_0 is pre-calibrated. Furthermore, a more meaningful parameter, namely, the hydrodynamic radius R_H , can be obtained from the relationship $R_H = K_B T / 6\pi\eta D$. Here, K_B is the Boltzmann constant, T is absolute temperature, and η is solution viscosity which is known for a specific solvent at a certain temperature T .

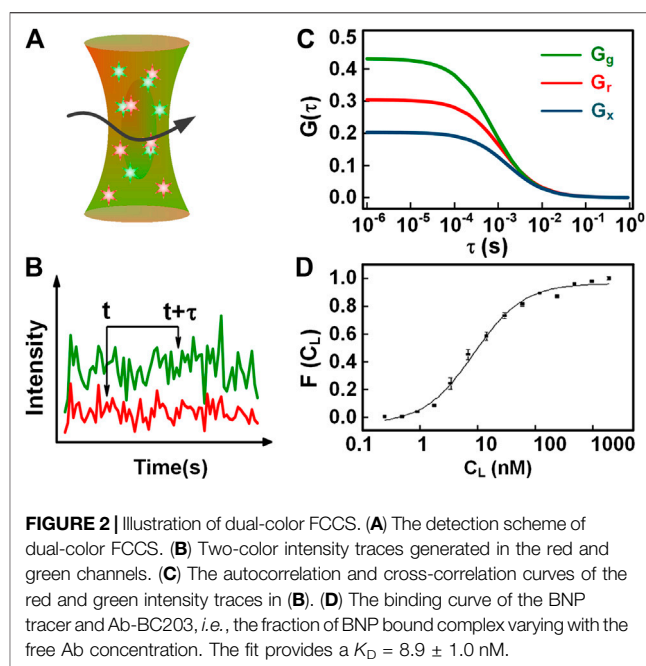
The correlation in Eq. 1 can be calculated with a computer-based software or hardware correlator [20–23]. With the software correlator, photon counts and arrival times are imported into the computer and then correlated with relevant programs. The hardware correlators correlate on board the incoming photon arrival times electronically and feed the correlated data [5]. Both of the two approaches employ the multi-tau algorithm, but there are still some differences [5, 24]. Firstly, the hardware correlator works out in real-time mode, allowing adjusting the experimental setting in time, while the software correlator performs the calculation after experiments. Secondly, the speed of the hardware correlator is much faster than that of the software correlator. Thirdly, the hardware correlator can not reserve the raw data and is not capable of handling the issues of photobleaching, clusters, or other disturbances. By contrast, the software correlator can dispose or compensate for the above-mentioned disturbances and enables us to make other analyses such as pulsed interleaved excitation (PIE) to remove the spectrum-crosstalk and time-gated detection to suppress the background once using pulsed excitation. In short, hardware and software correlator both have their own advantages and disadvantages. The choice of each method is determined by the desired property in experiments. Compared with imaging-based dynamic determination approaches, the temporal resolution of FCS can reach the ns range, so it allows detecting molecular diffusion both *in vitro* and *in vivo* [25–27].

ADVANCES IN FLUORESCENCE CORRELATION SPECTROSCOPY

In this section, we will introduce the recent advances on FCS that aim at endowing FCS with new capabilities by concept or adapting FCS for specific applications.

Dual-Color FCCS for Molecular Interaction Investigation

To measure the molecular binding, conventional FCS is only available when the binding lead to a resolvable change in diffusion time, compared to individual molecules. This application will be handicapped when uninteresting molecules are bound to the fluorescently labeled molecules. Compared to conventional FCS, dual-color FCCS is a preferable technique to detect molecular binding without these limitations [4, 10, 28–30]. The concept of dual-color FCCS was first proposed by Eigen and Rigler [30], and was implemented experimentally by Schwille *et al.* [31] In dual-color



FCCS, two species of interest are labeled with two different types of spectrally distinct fluorophores, indicated with the subscript r (red) and g (green) for simplicity. Upon the excitation of the red and green lights (as shown in Figure 2A), the fluorescence from the two-color fluorophores is separated and counted into two detection channels, respectively (Figure 2B shows two intensity traces). The autocorrelations of the intensity traces $F_g(t)$ and $F_r(t)$ from the two-color channels are calculated with Eq. 1, yielding G_g and G_r for the two channels (as shown in Figure 2C). The complexes introduce synchronized intensity fluctuation in the two channels when diffusing into and out of the observation volume. Accordingly, the presence of the complexes can be analyzed with the cross-correlation of the two-color intensity traces:

$$G(\tau) = \frac{\langle F_g(t)F_r(t+\tau) \rangle}{\langle F_g(t)F_r(t) \rangle} - 1 \quad (3)$$

$F_g(t)$ and $F_r(t+\tau)$ are the intensity traces from the two-color channels and have a lag time τ . The proportion of the complex versus the green molecules can be estimated with $G_X(0)/G_r(0)$, where $G_X(0)$ and $G_r(0)$ are the amplitude of the cross-correlation curve and the autocorrelation curve of the red channel. Moreover, a binding affinity K_D is often used to quantify the binding tendency of two kinds of molecules, which can be calculated with $K_D = C_R C_L / C_{RL}$ [32], where C_R , C_L , and C_{RL} refer to the concentration of free receptors, ligands, and the complex, respectively. These three quantities can be obtained with FCS measurement. However, this method determines K_D with a single ligand concentration C_L , and the result can be easily wrong due to the existence of a variety of disturbances in the measurement. As an improvement, a binding curve [33], which represents the fractions of the complex to the total receptors versus different

free-ligand concentrations, is often employed to acquire a more precise K_D . In practice, to calculate the binding curve, dual-color FCCS experiments are performed for a series of C_L spanning in a broad range, yielding $G_r(0)$, $G_g(0)$, and $G_X(0)$ for each C_L . Then, the fractional occupancy $F(C_L) = A_{\text{eff}}/A_g \cdot G_X(0)/G_g(0)$ is calculated for each C_L , as shown in **Figure 2D**. Here A_g is the observation area for the green species, and A_{eff} is the effective observation area. Eventually, the value of K_D is determined by fitting the $F(C_L)$ data with the following model:

$$F(C_L) = \beta \cdot (1 + K_D/C_L)^{-1} \quad (4)$$

Compared with the method of determining K_D with $K_D = C_R C_L / C_{RL}$, this approach is more robust since there are much more statistics, which are obtained in a systematic and organized way (at different C_L). In addition to the dissociation constants K_D , the fit can also extract the ratio β between receptors carrying a functional fluorescent domain and all (exogenous or endogenous) receptors capable of specific binding.

Dual-color FCCS labels two species of interest with spectrally distinct fluorophores, and the binding of the two species is analyzed with the cross-correlation. Therefore, compared with the single species, dual-color FCCS is neither limited by the relative size change of the complex compared with single species nor susceptible to binding with other species. Hence, it has been widely used to investigate molecular interactions in cells, small organelles, and many other issues [34–37].

However, there are still some factors affecting the accuracy of the dual-color FCCS. Firstly, spectral crosstalk, *i.e.*, the signal of the green species falling in the red channel, often produces a “false-positive” cross-correlation amplitude. There have been some mathematical approaches to correct the cross-talk mathematically. For instance, a simple and reliable correction approach was proposed to compensate for the cross-talk with the bleed-through ratio, the brightness ratio, and the number ratio [10, 38]. Pulsed interleaved excitation (PIE) [19], which excites and detects interleaved two-color fluorescence in separate time windows, provides a solution for this problem (**Supplementary Material**). Similarly, fluorescence lifetime correlation spectroscopy (FLCS) can also be used to distinguish the fluorescence from two different species that have different fluorescence lifetimes and therefore to remove crosstalk [39].

The second is the imperfect focus-overlap of two excitation lights, which often reduces the cross-correlation amplitude falsely. Fortunately, this artifact reduces the cross-correlation amplitude by a constant ratio. This ratio can be determined by performing dual-color FCCS on one kind of fluorophores with a broad absorption spectrum, and calculating the ratio of the obtained cross-correlation amplitude and the autocorrelation amplitudes. Then, the influence of the imperfect focus-overlap can be compensated by dividing the cross-correlation by this ratio, when measuring the binding of two species. Alternatively, two-photon excitation, which uses one laser to excite two kinds of fluorophores employing respectively single-photon excitation and two-photon excitation regimes, is available to avoid this artifact [40, 41].

The third is the uncorrelated background from the auto-fluorescence of cells, extracellular environment, or stray lights. This uncorrelated background will affect both the

autocorrelations and cross-correlation curves. In the general case, the background in the red and green channel, denoted with B_r and B_g respectively, reduces the amplitude of the auto- and cross-correlation curves by [42]:

$$C_{\text{rg}}^{\text{meas}} = C_{\text{rg}}^{\text{true}} \frac{F_r}{F_r + B_r} \frac{F_g}{F_g + B_g} \quad (5)$$

F_g and F_r are the means of the green and red fluorescence intensities, excluding the background.

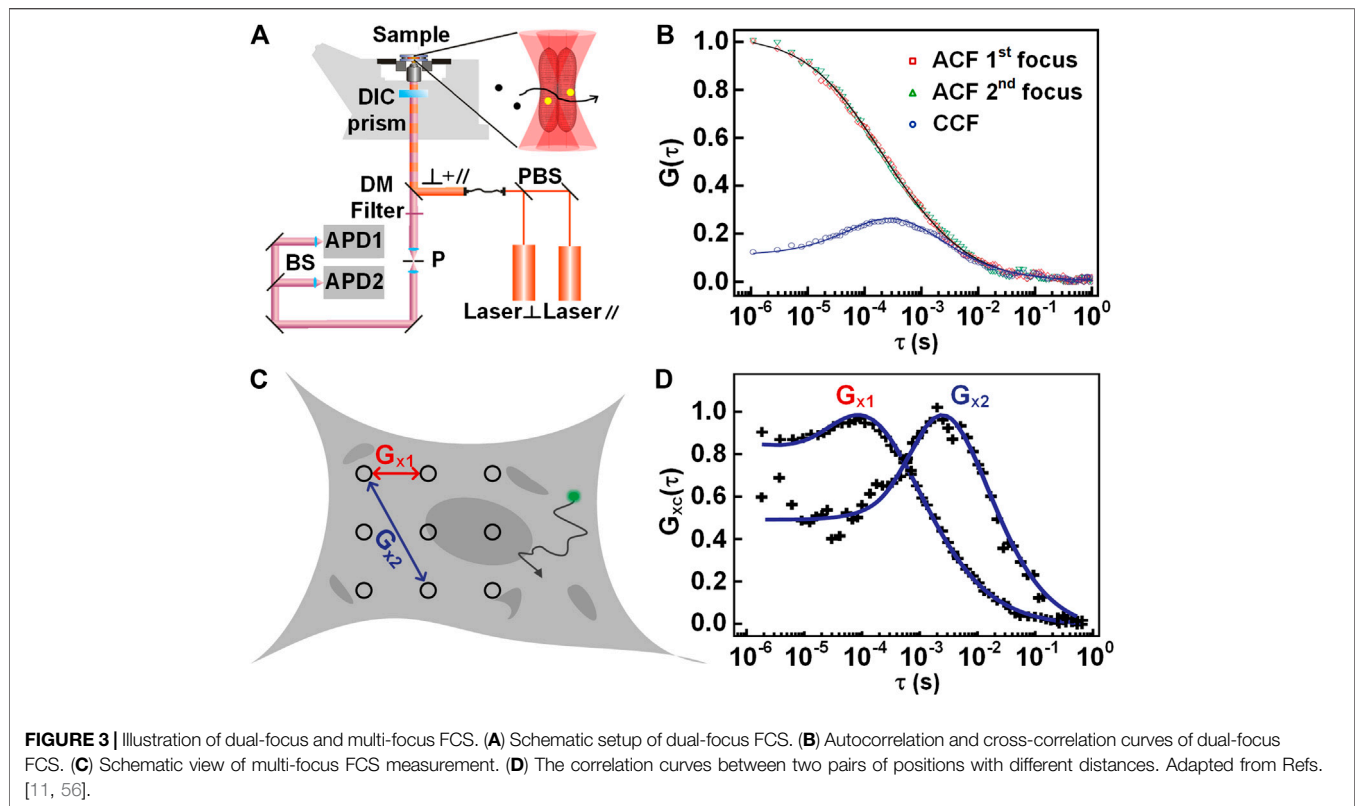
$C_{\text{rg}}^{\text{meas}}$ and $C_{\text{rg}}^{\text{true}}$ are the amplitudes of the cross-correlation calculated from the measurement and the cross-correlations in reality, respectively. With **Eq. 5**, the auto-fluorescent background and detector dark counts can be corrected.

The fourth factor is photobleaching. The continual loss of fluorophores in the focus area with time will falsely distort the autocorrelation curves by providing apparently smaller molecule numbers N_r and N_g , and shorter correlation time τ_{Dr} and τ_{Dg} . Interestingly, it was found recently that the amplitude of the cross-correlation is barely influenced by the bleaching of either red or green species [43]. Furthermore, the molecule numbers can be corrected by multiplying N_r and N_g with the coefficients γ_r and γ_g , which is quantified with the raw red and green intensity traces, considering the fluorescence intensity is linear to the molecule number [43]. Nevertheless, it is always preferable to avoid bleaching in both channels, since the lateral shift of the correlation curves induced by the bleaching can never be restored yet.

Dual/Multi-Focus Fluorescence Correlation Spectroscopy and Imaging Fluorescence Correlation Spectroscopy to Acquire Space-Multiplexing Dynamics

Conventional FCS could only detect the dynamics of a single spot. Dual-focus FCS (and multifocal FCS) was developed with their major merit of probing dynamics simultaneously at two separated positions. Meanwhile, in single-focus FCS, the pre-calibration for focus size r_0 is needed for the quantitative analysis of the FCS data [44]. Dual-focus FCS can avoid this pre-calibration procedure when the inter-focal distance is prior-known [45, 46].

In dual-focus FCS, a DIC prism splits two orthogonal linear-polarized pulsed lasers into two laterally shifted foci, as shown in **Figure 3A**. The fluorescence alternatively excited by the two foci is separated by using a time-correlated single-photon counting (TCSPC) module. By applying a global fit to all correlation curves, including the ACF from each focus, and the CCF between both foci, one can extract the absolute values of the diffusion coefficient D and the focus size r_0 when the inter-focal distance is pre-known [45]. Therefore, it is promising for dual-focus FCS to obtain a more accurate diffusion coefficient in experiments [47]. With the dual-focus FCS, Kerstin *et al.* investigated protein diffusion in black lipid membranes, yielding highly accurate diffusion coefficients [48]. In addition, it is also worthy of mentioning that the inter-focal distance was also influenced by specific experimental settings, such as the thickness of the cover-slip and index mismatch. So a pre-calibration is necessary for most of measurements.

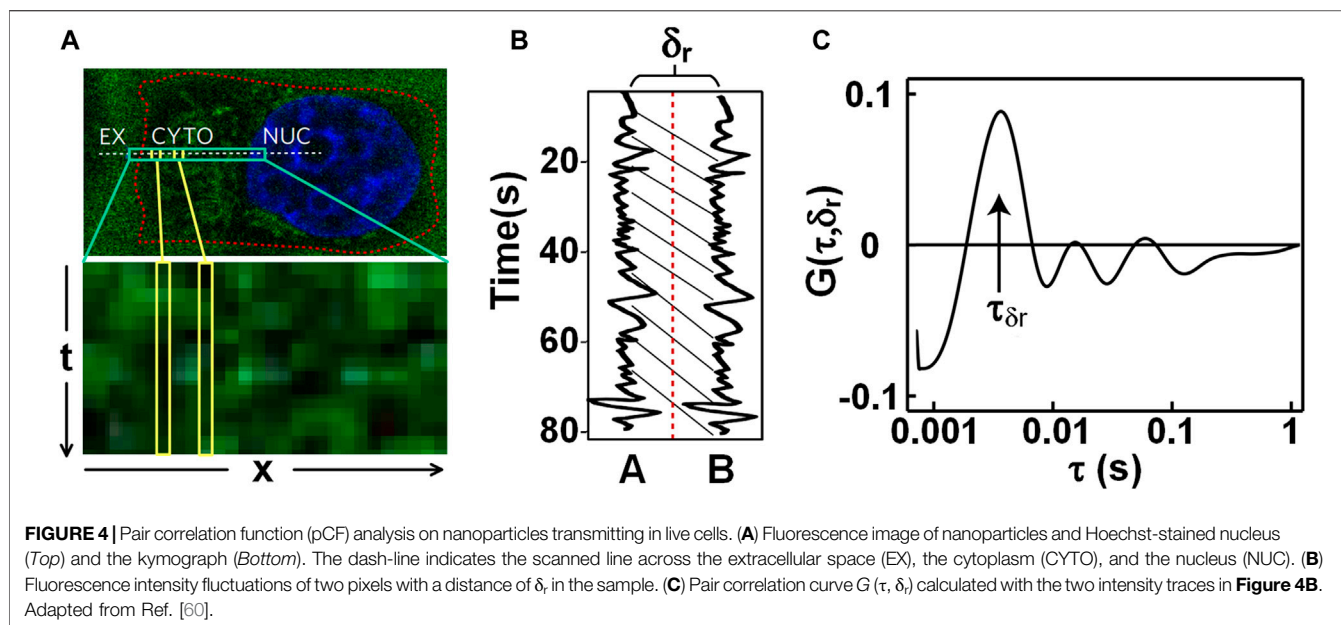


Besides the dual-focus FCS, there exist similar techniques, such as imaging FCS [49], multi-scale FCS [11], and multi-focus FCS [50, 51]. In imaging FCS, a series of images are taken on a certain area of the sample, and then the intensities associated with each pixel are correlated with time. When fitted with a suitable diffusional model, the dynamics at thousands of points can be measured simultaneously [15, 52]. Except for auto- and cross-correlation analysis, spatiotemporal image correlation spectroscopy (STICS) [53, 54] and k-space image correlation spectroscopy (kICS) [55] have been proposed to analyze the dynamics at different locations. STICS allows measurement of diffusion coefficients and velocity vectors of particles by using temporal and spatial correlation on measured image stacks. kICS can quantify molecular dynamics by performing correlation in reciprocal space even in the presence of fluorophore photobleaching and blinking. kICS does not rely on nonlinear curve fitting, or the knowledge of the beam radius of the exciting laser. With the advent of fast and sensitive EMCCD cameras, the potential of the imaging FCS will be further exploited for wide applications in biomedical and chemical sciences. Similarly, multi-scale and multi-focus FCS both detect the signals from multi-points in an extended area, as shown in **Figure 3C**. Then, the spatial information of molecular motion can be analyzed by the autocorrelation or the cross-correlation curves between the different pairs of points (**Figure 3D**). Multi-focus FCS was implemented recently by using a spinning-disk [51] or beam-splitter array [50]. Multi-scale FCS was proposed by Baum *et al.* [11] to characterize the intracellular architecture by employing a line for illumination. As the common disadvantages of imaging

FCS, multi-scale FCS, and multi-focus FCS, their temporal resolution is low (in the millisecond range) due to the usage of 2D imaging sensors; meanwhile, these three techniques have a larger observation volume than the confocal based FCS due to the lack of pinhole filtering. In addition, by scanning a wide area across the sample and performing a correlation analysis of relevant subregions within the acquired image, the dynamics can be probed by the analysis of raster image correlation spectroscopy (RICS) [57]. Despite the dynamics can be obtained by scanning one frame, RICS often scans a few frames to compensate for the immobile component in the image. In RICS, the correlation data is calculated with a dozen of pixels that are connected with each other along the line scan. Therefore, the spatial resolution of RICS (a few micrometers) is much lower than the above-mentioned techniques.

Pair Correlation Function Analysis for Directional Diffusion

The conventional FCS detects dynamics at one point or two, and lacks the ability to detect path-related anisotropic diffusion. To acquire directional diffusions or to detect obstacles to molecular diffusion, Digman *et al.* incorporated pair correlation function (pCF) into FCS [12]. pCF was performed by repeatedly scanning a line in a cell (indicated with the white-dash line in **Figure 4A**), and then assembling the acquired lines into a kymography (**Figure 4A-bottom**). In the kymography, when the intensities of a specific pixel assembled are correlated with time, an autocorrelation $G(\tau)$ is generated, the local concentration and



the diffusion coefficient of targeted biomolecules at this pixel can be obtained by fitting $G(\tau)$ with the diffusion model in Eq. 2. Furthermore, when the cross-correlation of a pair of pixels (see **Figure 4B**) separated by δ_r is calculated, the lag time of the cross-correlation peak characterizes the transmit time a molecule diffusing from point A to point B, as shown in **Figure 4C**. The longer the transit time is, the more the mobility between the two pixels is hindered. Therefore, according to the pCF analysis, the obstacles which hinder the molecular diffusion can be detected from the abnormal migrating time [12, 58]. Recently, Bianchini *et al.* [59] utilized STED-based pCF to investigate local diffusion barriers in living Chinese Hamster Ovary cells. This method provides directional spatial motion information, which is not obtainable with conventional FCS.

There is a certain similarity between pCF and dual-focus FCS [46]. However, dual-focus FCS can only detect dynamics on a fixed pair of points. pCF can obtain information about any pair of points in the detection area or scanned line, which greatly increases the amount of spatial information. In all, pCF is more practical and convenient for biological researchers.

Recently, two-dimensional pair correlation function (2D pCF) was developed as an extension of pCF analysis. 2D pCF probes the anisotropic paths at different spatial locations and maps the intercellular environment [61]. Compared with one-dimension pCF, 2D pCF can provide more information of the intercellular environment. Specifically, correlating the intensity series of each image pixels with its neighboring pixels at a certain distance yields a set of pair correlation functions. Plotting the results of pCFs as a function of time delay and angle, a sub-image for each pixel can be obtained, and then a polar plot for each pixel can be generated. If the molecules move isotropically, the correlation function will be equal in all directions. However, if there are barriers in some directions, a deformed polar plot can be obtained and analyzed by moment analysis [62]. Therefore, the 2D pCF is a fingerprinting tool for the investigation of anisotropic motions and intracellular structures in

living cells. Compared with 1D pCF, 2D pCF using a 2D image sensor for the detection trades its temporal resolution for spatial information.

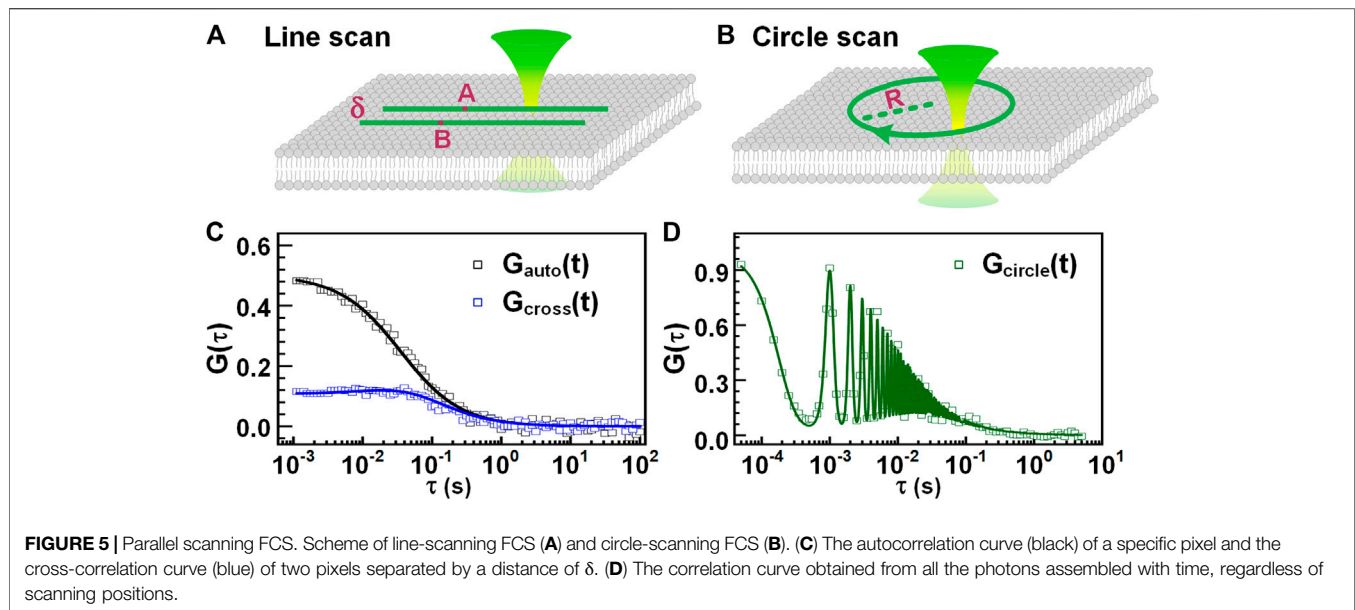
Except for analyzing the fluorescence fluctuation, some researchers applied pCF analysis to sense other parameters such as molecular brightness. For instance, Hinde *et al.* [63] utilized pCF to quantify molecular brightness (pCOMB) and tracked the mobility of different oligomeric species within living cell nuclear architecture.

Scanning Fluorescence Correlation Spectroscopy Targeting Dynamics on Membranes

For static FCS, the observation volume is kept fixed at a specific location in the sample, and therefore, it is not applicable for the studies of rather slow diffusional dynamics in bio-membranes. The reason lies in that the infrequent appearance of fluorophores in the focal spot poses sampling problems, and meanwhile, their long retention in the focus volume enhances the likelihood of photo-destruction. Scanning FCS was proposed to overcome this difficulty by sweeping the focus rapidly across a sample, calculating the autocorrelation of the assembled intensity trace associated with one or multiple positions, and then obtaining the dynamics after applying a fit model [64, 65]. Sorted by the scanning direction with respect to the membrane position, scanning FCS can be classified into two categories: parallel scanning FCS and perpendicular scanning FCS.

Parallel Scanning Fluorescence Correlation Spectroscopy

Parallel scanning FCS scans a focused light along one line [66], two lines (as shown in **Figure 5A**), or a circle [67, 68], (as shown in **Figure 5B**) in the plane of a membrane, acquiring and assembling the photons with pixels and time. After that, the intensities of each pixel from the scanned line or circle are extracted and binned into an



intensity trace, the autocorrelation of the intensity trace can provide the concentration and diffusion coefficient of the targeted biomolecules. Furthermore, similar to dual-foci FCS, the intensity of two pixels from the two scanned lines or from the scanned circle, which has a known distance, can be auto-correlated and cross-correlated. A global fit on the obtained autocorrelations and the cross-correlation can provide, the focus size, concentration, and diffusion coefficient of measured biomolecules, as shown in **Figure 5C**. This method avoids additional procedures for detection volume calibration. Alternatively, in circle-scanning FCS, the photons collected during the whole scanning process are globally assembled with time, yielding a global intensity trace (regardless of the scanning position). The concentration and diffusion coefficient of biomolecules can be obtained from the calculated autocorrelation curve (see **Figure 5D**) with a suitable fit model [67, 69, 70].

In general, parallel scanning FCS alleviates the photobleaching of fluorophore by splitting the light exposure among a set of pixels. Equivalently, the time each fluorophore spends in the focus during measurement is reduced. Scanning FCS has been widely used in the study of biomolecular dynamics on membranes. For instance, Ries *et al.* [66] used line-scanning FCS to measure the diffusion coefficients of lipids accurately, interpreting the diffusion behavior in three phase-separating bilayers and the temperature dependence in several model membranes.

Perpendicular Lateral/Axial Line-Scanning Fluorescence Correlation Spectroscopy

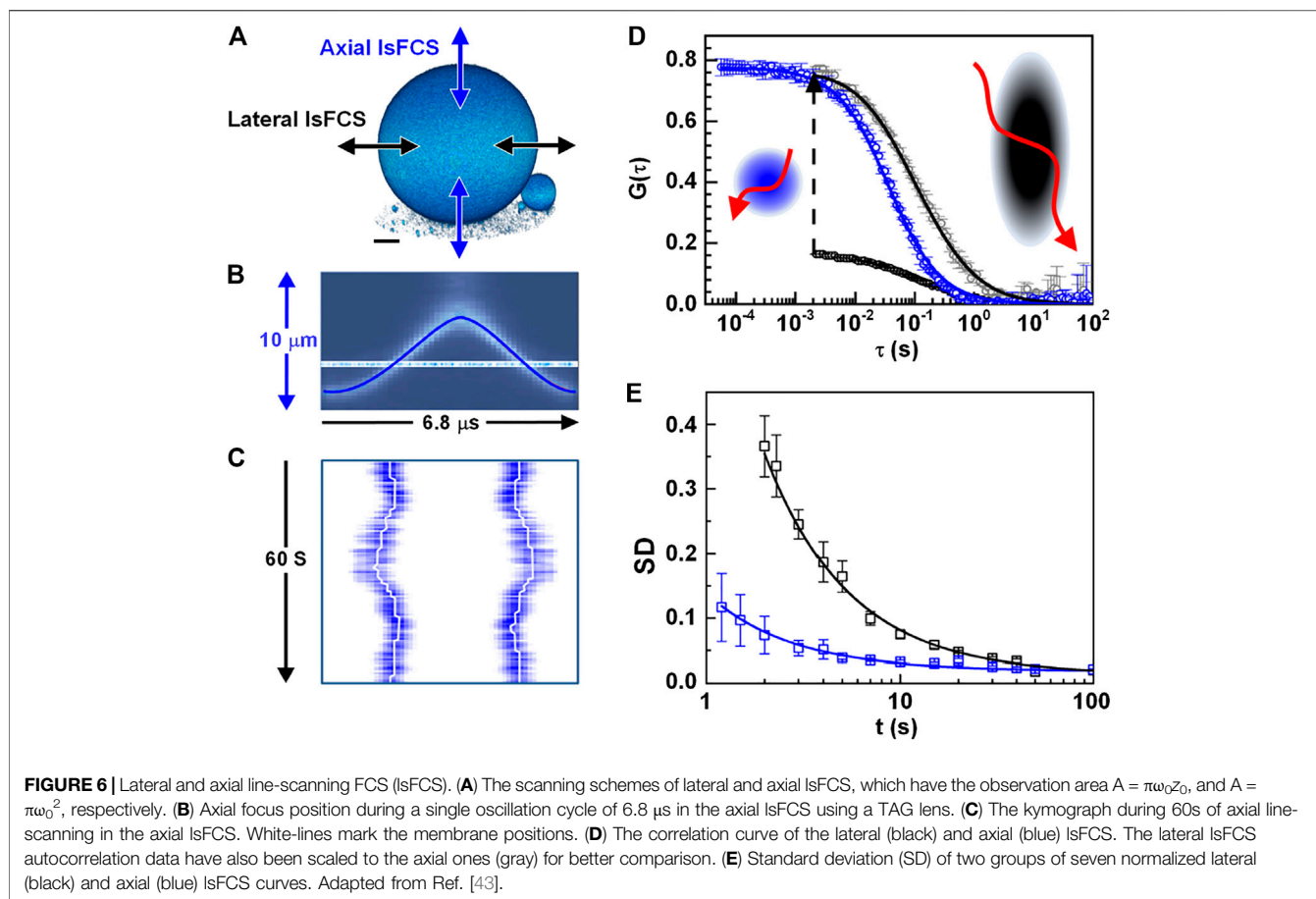
When FCS is used to investigate dynamics on membranes, the movement of the membranes with respect to the observation volume gives rise to strong intensity fluctuations, obscuring those resulting from molecular diffusion in the plane of the membrane. Z-scan FCS tried to solve this problem by measuring a stack of correlation curves at discrete axial positions (“z-scan”) and selecting the correlation curve corresponding to the shortest diffusion time and the minimal number of particles [71, 72]. Alternatively, lateral/axial

line-scanning FCS (lsFCS) solves this problem by quickly scanning the observation volume perpendicularly through the membrane or GUV [43, 73], as shown in **Figure 6A**. For both lateral and axial lsFCS, the fluorescence collected along the direction is binned into a 2D pseudo image (see **Figure 6C**). For data analysis, the photons from the membrane, which is identified with the highest photon counts, are selected and binned into an intensity trace. Then, the intensity trace is correlated and analyzed with 2D diffusional model, yielding useful information, including biomolecular concentration, diffusion coefficient, *etc.* These methods are ideally suited to study dynamics in the membrane [42, 73]. Furthermore, they can be extended to dual-color lateral/axial lsFCS to study the interaction between different molecules, such as ligands and receptors, when tagged with different fluorophores [32].

For comparison, lateral lsFCS is often performed with a galvo-scanner, which limits the time resolution to \sim ms [32]. Nevertheless, the recently reported axial lsFCS performed a resonant axial-scan (see **Figure 6B**) by using a tunable acoustic gradient index of refraction lens (TAG lens), providing a time resolution of 0.05 ms, 40 times faster than that the time resolution (2 ms) of lateral lsFCS, as shown in **Figure 6D** [43]. Furthermore, the axial lsFCS has a smaller and more symmetric focal area, and therefore, it can achieve comparable data quality with a remarkably reduced data acquisition time. The reduced measurement time will, in turn, reduces the photobleaching caused. Moreover, compared to the elliptical cross-section in lateral lsFCS, the circular cross-section in the axial lsFCS makes the fit more robust [43].

Reduction of Observation Volume to Probe Nanoscale Dynamics

As we all know, molecules in cells are usually hindered and differ from locations [74]. Also, the anomalous diffusion usually occurs on a small spatial scale with nanoscales [75]. In conventional FCS,



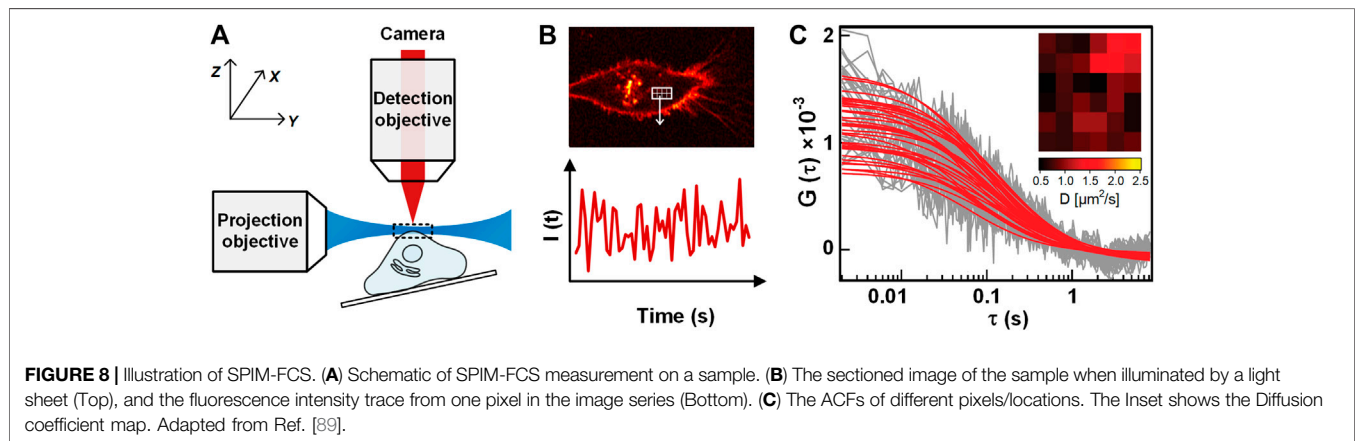
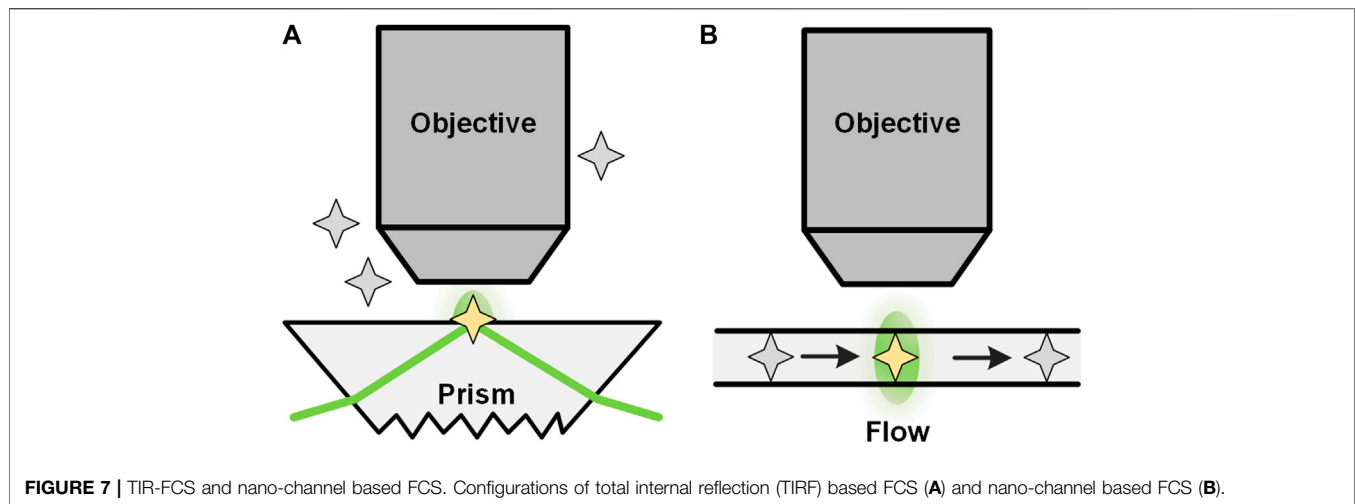
due to the limitation of the optical diffraction, the observation volume is limited to $\sim 0.5 \text{ fl}$ [76]. Despite being tiny already, this observation volume can also average out the heterogeneous dynamics happening in the diffraction-limited observation volume. Meanwhile, the diffraction-limited observation volume limits the measurable concentration, not exceeding $\sim 100 \text{ nM}$ [77]. Otherwise, the fluctuations will be averaged out. However, the concentration of many biomolecules in living cells, especially when induced by an external transfection, is often quite high, usually in the micro-to the millimolar range. Therefore, it is crucial to reduce the detection volume of FCS to measure biomolecular dynamics with much higher concentration or the dynamics happening in the sub-diffraction areas. This section will introduce three techniques that reduce the detection volume, namely, total internal reflection FCS (TIR-FCS), nanofluidic channel-based FCS, SPIM-FCS, and STED-FCS.

Total Internal Reflection-Fluorescence Correlation Spectroscopy and Nanofluidic Channel Based Fluorescence Correlation Spectroscopy

Total internal reflection FCS (TIR-FCS) is a method that can significantly reduce the observation area in the axial direction by utilizing total internal reflection (TIR). TIR-FCS was first proposed by Thompson *et al.* in the 1980s [78]. In TIR-FCS (see **Figure 7A**), a laser beam is totally and internally reflected at

the surface-solution interface at an angle greater than the critical angle, forming an evanescent wave in a very thin layer with a thickness typically from tens of nm up to a few hundreds of nm. [79, 80] The excited fluorescence is collected by a microscopic objective and used for correlation analysis, from which the quantitative dynamic parameters of the sample can be obtained [81]. In addition to the setup in **Figure 7A**, TIR-FCS can also be realized by epi-illumination. [82] Through total internal reflection, the excitation of fluorophores, which are far away from the surface, is avoided. Therefore, compared with confocal based FCS, TIR-FCS has a much smaller focus volume that contributes to measuring high-concentration molecules and reducing the measurement time. On the other side, molecular diffusion investigated with TIR-FCS is handicapped by the binding of the molecules to the solid surface. Another difficulty in using TIR-FCS is the lack of a valid analysis model. Recently, many researchers have studied mathematical models to enhance TIR-FCS [83–85], taking into account the decay of evanescent waves and many other related problems. TIR-FCS has been widely applied to measuring receptor-concentration near membrane surfaces and the ligand-receptor binding occurring on the membrane [86].

Another way to reduce the observation volume is to use nanofluidic channels in FCS (**Figure 7B**). Foquet *et al.* [87] used nanofabricated channels with dimensions smaller than



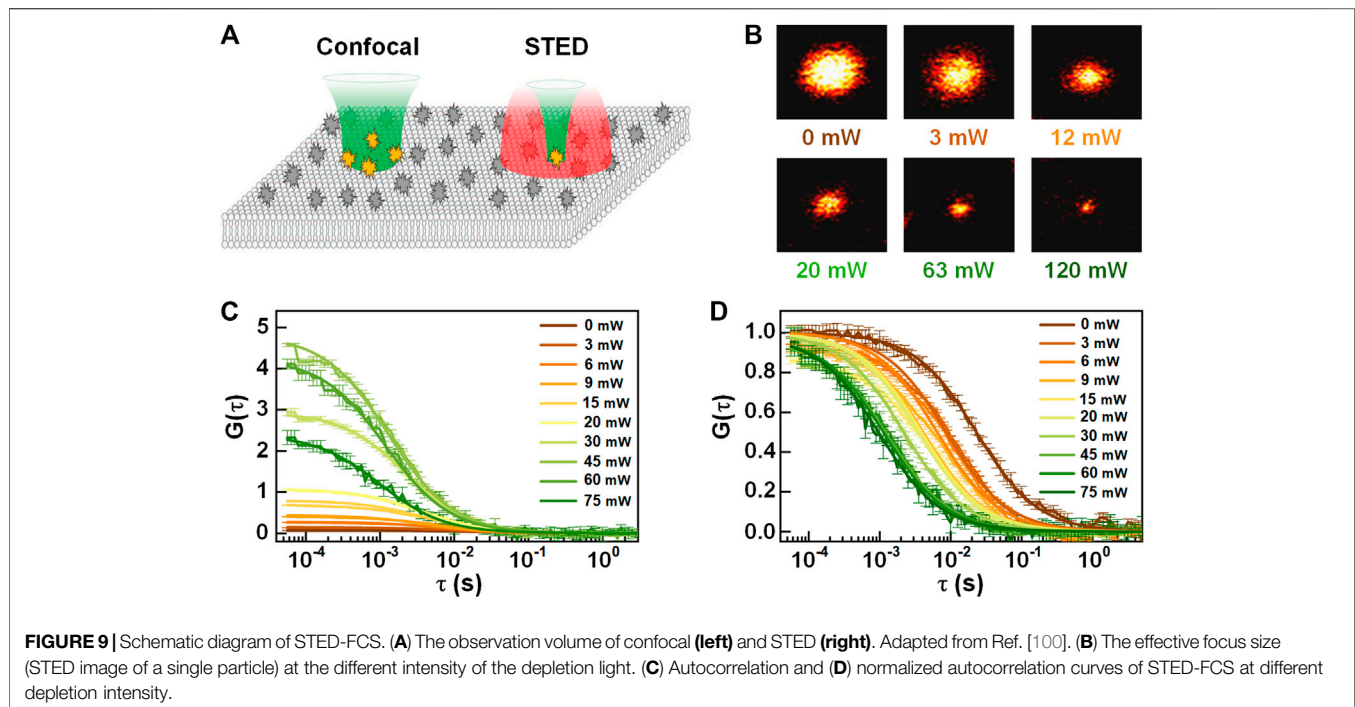
the diffraction-limit as the container of molecules during FCS studies. With such a nano-channel, an effective detection volume of tens of attoliters was achieved. In addition, non-linear or higher harmonics techniques, 4π -like excitation, near-field techniques, and surface plasmon can also be used to generate an effective focus volume smaller than the diffraction limit [77]. It should be noted that the detection volume of these methods is inherently adjacent to a surface, and consequently, free diffusion is restricted in at least one direction [77]. Another limitation of FCS in microfluidics is the lack of suitable interpretive models under different conditions, especially when measurements are performed in microchannels in which boundary effects cannot be neglected [24].

Single Plane Illumination Microscopy-Based FCS

Single plane illumination microscopy-FCS (SPIM-FCS) is a multiplexed technology that allows simultaneous FCS measurements on thousands of adjacent observation volumes to provide spatial maps of the diffusion coefficient and concentration [15]. In SPIM, a thin light sheet with a typical thickness of $1 \sim 1.5 \mu\text{m}$ is generated by using a projection objective and a conjugated cylindrical lens, and the emitting fluorescence signal is detected in

perpendicular (as illustrated in **Figure 8A**) by a high-speed camera [88]. After that, a series of images are recorded, and the fluorescence intensity trace of each pixel is generated by assembling the intensities of each pixel in the image series (**Figure 8B**). With ACF of the pixelated intensity traces, the quantitative diffusion coefficient and concentration maps are obtained (**Figure 8C**).

Comparing to confocal-based FCS, SPIM-FCS avoids the out-of-focus excitation and hence provides a well-confined observation volume. Moreover, SPIM-FCS can also detect the dynamics of multiple locations simultaneously, providing a diffusion-coefficient map and concentration map [15]. Besides, SPIM-FCS has high flexibility during data analysis. For instance, the observation volume can be controlled during data analysis artificially in SPIM-FCS, which is convenient to adjust the analysis area according to the specific samples. Compared to RICS, which obtains the diffusion coefficient with multiple pixels along the scanning direction, SPIM-FCS excels in the spatial resolution [49]. However, the temporal resolution of SPIM-FCS/FCCS is limited by the performances of cameras. A camera with sufficient quantum efficiency and high speed is needed for SPIM-FCS to measure fast molecular motions with good statistics. There are some available cameras such as SPAD, sCMOS, EMCCD,



where EMCCD provides the highest quantum efficiency of more than 90% and the relatively low frame rates of 1000 s^{-1} , which is the most suitable detector with a comprehensive consideration yet [49, 90]. In summary, device advances help to further improve the performance of SPIM-FCS.

SPIM-FCS has played an important role in the detection of molecular diffusion within cells and organizations [89, 91]. Besides dynamics measurement, Krieger *et al.* [92] proposed two-color SPIM-FCS that allows measuring spatially varying molecular interactions. In two-color SPIM-FCS, two light sheets of different wavelengths are used as the excitation, and an image splitter was used to split the detected fluorescence into two separate color channels. Agata *et al.* [93] utilized this method to study the interactions of the molecules Fos and c-Jun in HeLa cells.

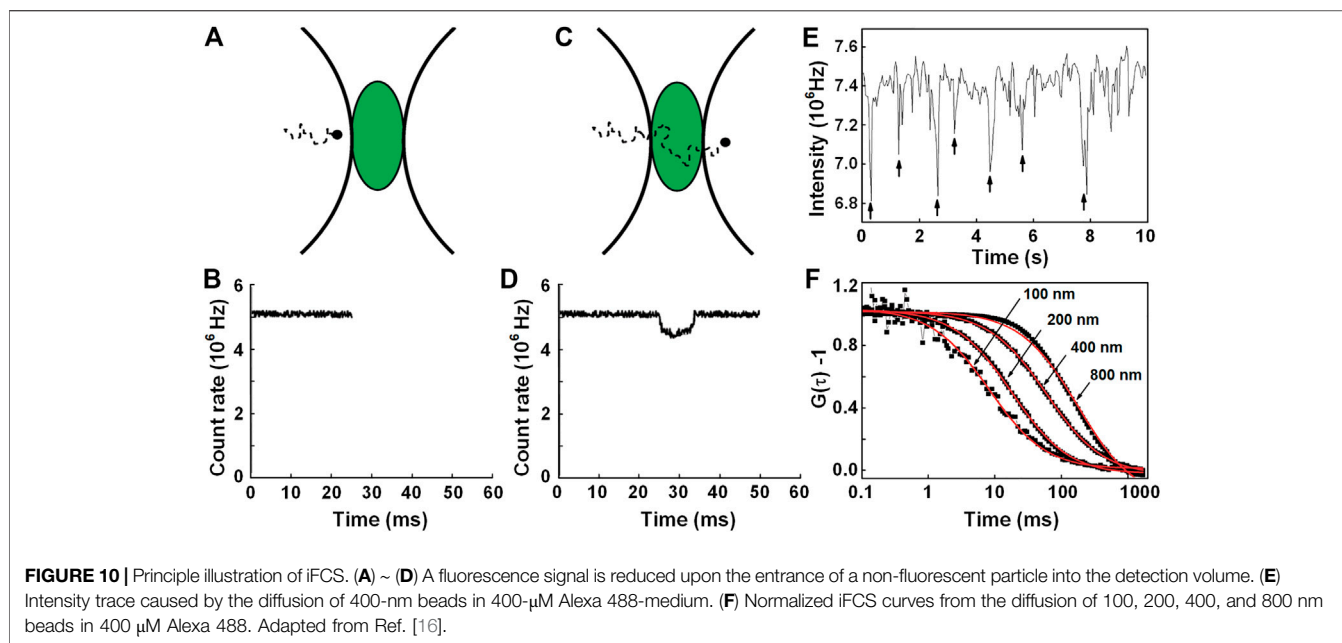
Stimulated Emission Depletion-Fluorescence Correlation Spectroscopy

To study the anomalous dynamics of molecules, in 2005, Kastrop *et al.* reduced the FCS detection volume to one-fifth of the conventional confocal volume by using stimulated emission depletion (STED) [14]. In the so-called STED-FCS, a red-shifted doughnut-like depletion light depletes the excited fluorescence in the periphery of the excitation focus, yielding an effective focus much smaller than the diffraction limit (see **Figure 9**) [94]. In principle, the effective focus size of STED-FCS can become infinitely small by increasing the intensity of depletion light, but in actual situations, it is limited by photobleaching of fluorophores and reduction of signal to background ratio. Also, the background fluorescence from the out-of-focus region will directly influence the determination of both the concentration and diffusion coefficient. Recently, stimulated emission double-depletion (STEDD) based FCS (STEDD-FCS) [95] was proposed, which determines the effective fluorescence

and background by temporally modulating the effective fluorescence “on” and “off” by applying an additional depletion light and later subtracts the background from the signal in total. Alternatively, time-gated detection was proposed on continuous-wave stimulated emission depletion (CW-STED) to reduce background [96]. As an enhanced approach, Lanza *et al.* [97] separates the effective signal and background photons by lifetime tuning (SPLIT-FCS) for reducing anti-stokes fluorescence emission background in STED-FCS. Compared with the gating method, SPLIT-FCS does not need complex fitting procedures such as fluorescence intensity distribution analysis (FIDA). Compared with STED-FCS in solution or cytosol, STED-FCS is more promising to probe membrane-related dynamics. This is due to the fact that the membrane intrinsically provides perfect axial confinement of the focus, no longer suffering from the out-of-focus fluorescence. In 2009, Eggeling *et al.* [98] applied STED-FCS to the study of living cell membranes, and proved that STED-FCS is capable of detecting the anomalous or heterogeneous diffusion in the membrane [75, 99]. Also, STED-FCS, which has excellent spatial resolution, can be combined with other techniques to obtain better consequents and facilitates solving more complex biological problems. For instance, Maraschini *et al.* [69] demonstrated the ability of circle scanning STED-FCS in quantifying spatiotemporal heterogeneities of lipid diffusion in cell membranes.

Inverse Fluorescence Correlation Spectroscopy

Wennmalm *et al.* [16] proposed inverse FCS (iFCS), which analyzes the fluctuation of unlabeled particles in the context of a densely labeled surrounding medium. As illustrated by **Figures 10A–D**, when a nonfluorescent particle transits



through the detection volume, a fraction of the fluorescent medium molecules will be replaced by the particle, resulting in a reduction of the fluorescence signal. Therefore, the generated intensity trace $F(t)$ features multiple negative spikes, as shown in **Figure 10E**. To quantify the molecular density and dynamics of the molecule, the autocorrelation of the intensity trace can be calculated and fitted to the following 3D diffusion model (see **Figure 10F**) [16]:

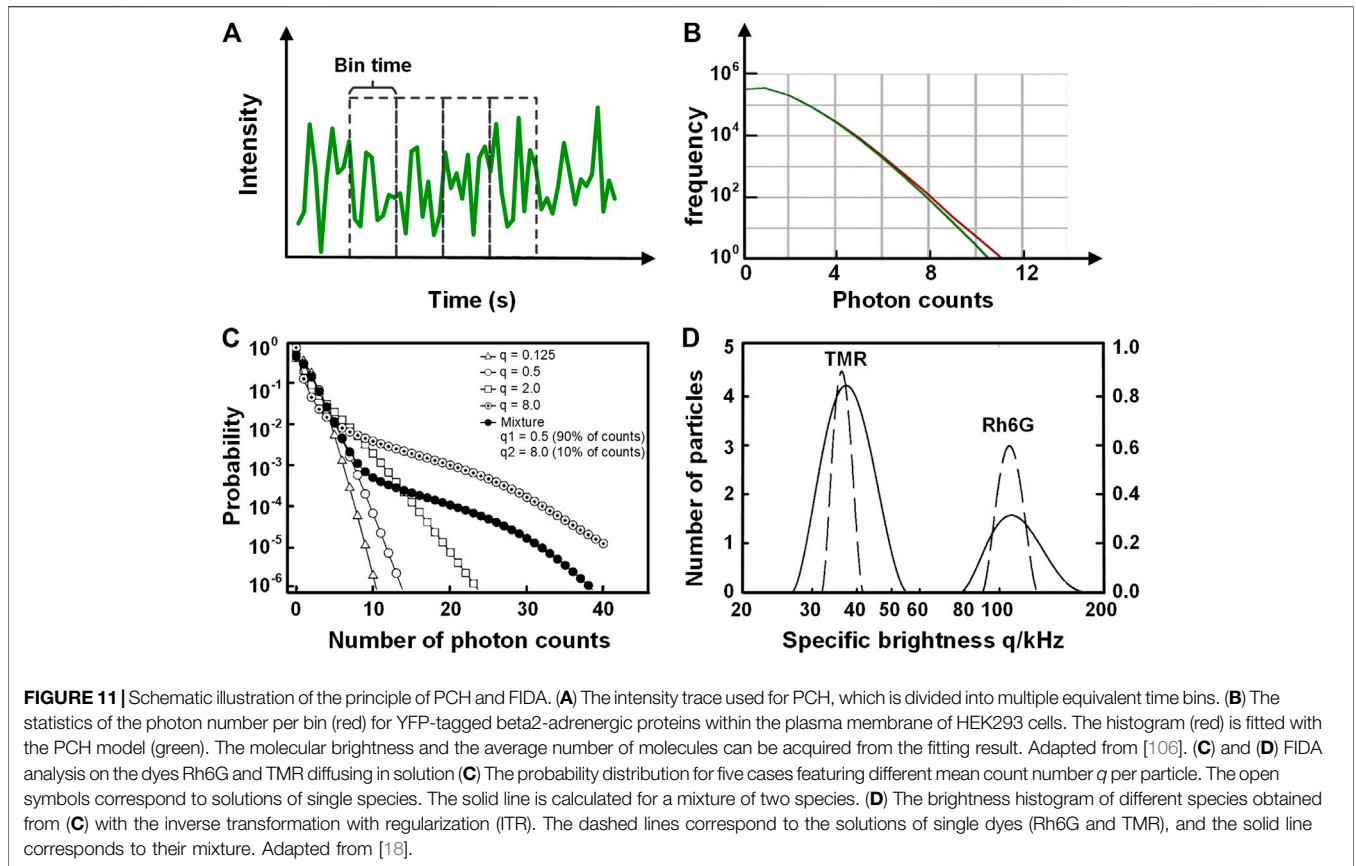
$$G(\tau) = \frac{N}{(1/V_q - N)^2} \cdot \left(1 + \frac{\tau}{\tau_D}\right)^{-1} \cdot \left(1 + \frac{\tau}{\tau_D} \cdot \frac{r_0^2}{z_0^2}\right)^{-1/2} \quad (6)$$

where N is the average number of molecules in the detection volume. $V_q = V_{\text{particle}}/V_{\text{detection}}$ with V_{particle} being the particle volume and $V_{\text{detection}}$ the detection volume. The fitting model in **Eq. 6** is the same as that in standard FCS, but with the only difference that $1/N$ is replaced by $N/(1/V_q - N)^2$. In iFCS, the average non-labeled molecule number N in the observation volume can be calculated with $1/\sqrt{N} = -\langle(\delta F(t))^3\rangle/\langle(\delta F(t))^2\rangle^{3/2}$, where $\delta F(t)$ is the fluorescence fluctuation ($\delta F(t) = F(t) - \langle F \rangle$), considering the skewness of the fluorescence intensity distribution [101]. Then, the ratio V_q can be determined with N and $G(0)$ solely, irrelevant to the diffusion term. Eventually, the concentration and the volume of the non-labeled particles can be determined after the detection volume $V_{\text{detection}}$ is obtained with standard FCS. Jiang *et al.* [101] used this method to observe the growth of phase domains and study the stages of phase separation in model lipid bilayer membranes. Interestingly, Jiang demonstrated that iFCS could uniquely provide accurate and consistent size of nanodomains while conventional FCS approaches can not. Besides the moment analysis, iFCS can examine the particle volume directly by providing the ratio of the particle to detection volume [102]. Bergstrand *et al.* [103]

estimated that the diameter of NPs with iFCS, and provided results that the NPs with a specified diameter of 250 nm was 257 ± 12 nm, and the NPs of 40 nm was 62 ± 26 nm with iFCS.

iFCS has some advantages above FCS. At first, iFCS provides particle sizes directly from $G(\tau = 0)$ without resort to the interpretation of the 3D diffusion model. The diffusion is often influenced by the temperature and viscosity of the medium, and therefore, the obtained diffusion coefficient and particle size are not accurate in a complex environment. Second, in iFCS experiments, the high molecular brightness is not very important, but the total fluorescence signal should be high to improve the signal-to-noise ratio. Thus, the concentration of medium dyes should be high and gives a negligible contribution to ACF. Usually, the concentration of medium used in the experiment is about 10 μ M or higher [104].

However, iFCS is limited to the analysis of rather large-volume particles. For instance, Wennmalm's experiments reveal that the lower limit for the particle size that can be analyzed is ~ 100 nm diameter with a detection volume of 0.3 fl [16]; in Jiang's work, the domain which size is five times smaller than the detection area can be detected [101]. To measure the smaller particle, it is necessary for iFCS to perform on the smaller detection volume, such as STED and nanostructured surfaces. The smaller detection volume provides a possibility for iFCS to detect smaller particles. Sandén *et al.* [105] combined iFCS with subwavelength apertures in plasmonic metal layers, which confines the detection volume to 1.2×10^{-4} fl, by which they directly examine the volume of a protein molecules allophycocyanin (APC) as $2.5 \pm 0.6 \times 10^{-7}$ fl in solution. Till yet, iFCS has not been applied in the plasma membranes of living cells [104]. This is mainly because the intercellular environment is very complicated, and different non-labeled cellular organelle are mixed.



Photon Counting Histogram and Fluorescence Intensity Distribution Analysis

In addition to FCS which analyzes the fluorescence fluctuation based on the temporal domain, photon counting histogram (PCH) [17] and fluorescence intensity distribution analysis (FIDA) [18] can extract the molecular brightness (photon counts per second per molecule) and the average number of molecules within the observation volume by analyzing the distribution of fluorescence fluctuation amplitude. In PCH, the fluorescence intensity trace is divided into multiple pieces with equivalent time bins, and the photon counts in each piece (**Figure 11A**) are integrated, yielding a photon-counting histogram (red curve in **Figure 11B**). The photon distribution arisen from molecular diffusion in observation volume exhibits a super-Poissonian distribution. The molecular brightness and the average number of molecules can be uniquely extracted by fitting the data with a suitable PCH model, for which Chen *et al.* derived a model [17]:

$$\Pi(k; \bar{N}_{PSF}, \varepsilon) = \sum_{N=0}^{\infty} p^{(N)}(k; V_0, \varepsilon) p_{\#}(N) \quad (7)$$

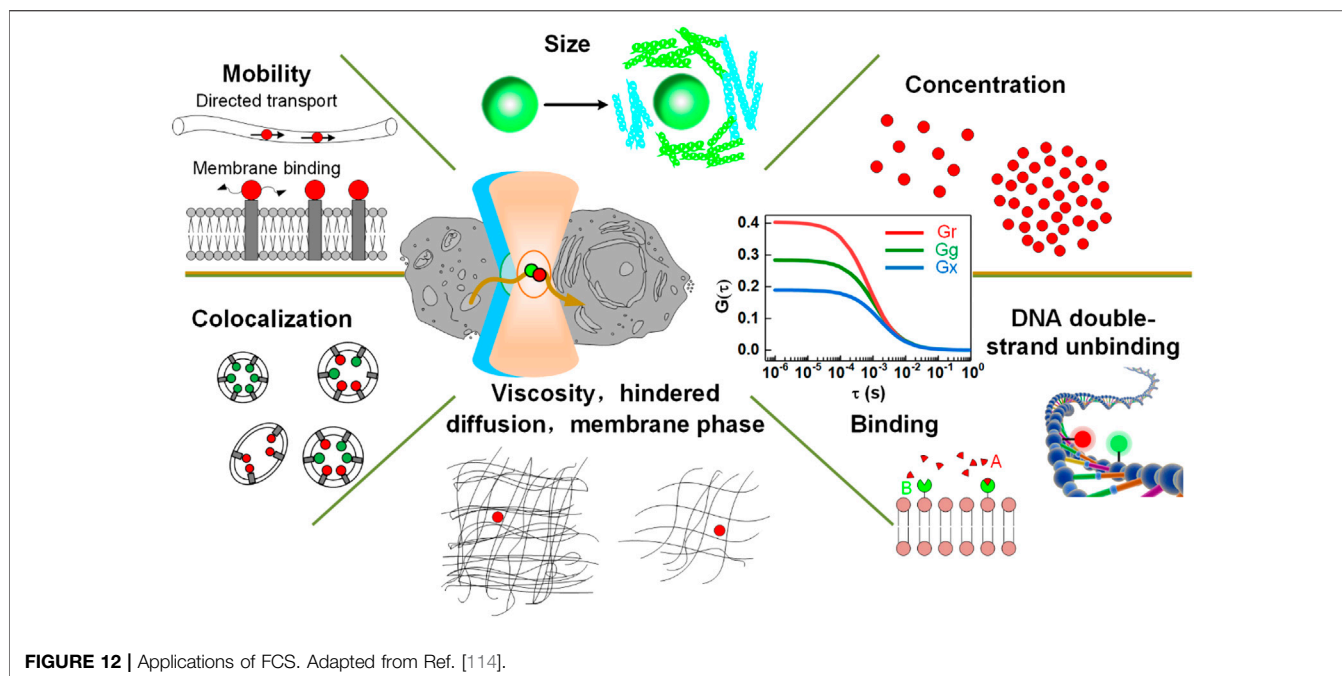
Eq. 7 describes the probability of observing k photon counts in an open system for a particle solution with a concentration of $c = \bar{N}/(V_0 N_A) p^{(N)}$ is the probability of observing N particles in the observation volume V_0 , which is obtained by N -times convolution of single-particle PCH. $p_{\#}(N)$ is the Poissonian

probability of observing N particles. Moreover, the PCH for multiple molecular species is generated by successively convoluting the photon distribution of each species with the others. As shown in **Figure 11B**, the green curve is the experimental data, and the red curve is the fitting curve with the PCH model in **Eq. 7**. Finally, the brightness and the average number of molecules can be obtained from the PCH fit [106, 107]. Katharine *et al.* [106] used PCH to study the receptor-receptor interactions in HEK293 cells. The result indicates an average molecular brightness of 17,857 counts per second per molecule. Through comparing the molecular brightness to that of monomer, they found the beta2-adrenergic receptors have a dimeric structure.

Besides PCH, fluorescence intensity distribution analysis (FIDA), firstly proposed by Kask *et al.* [18], is also a useful tool that determines the molecular brightness and the concentration by analyzing the distribution of photon counts. In the FIDA analysis, the observation volume is divided into a great number of spatial sections and calculated the distribution of the photon counts in each spatial section:

$$P_i(n) = \sum_{m=0}^{\infty} \frac{(cdV_i)^m}{m!} e^{-cdV_i} \frac{(mqB_i T)^n}{n!} e^{-mqB_i T} \quad (8)$$

$P_i(n)$ is a double Poissonian distribution, indicating the distribution of the number of molecules with the mean value cdV_i and the photon counts with the mean value $mqB_i T$, provided



that there are m molecules inside the confocal volume, respectively. The overall distribution $P(n)$ can be obtained by spatial integrals of $P_i(n)$ over the whole observation volume. The measured $P(n)$ is shown in **Figure 11C**, and the brightness and the concentration of the sample (**Figure 11D**) can be acquired by analyzing the data with the FIDA model. The result would be a single δ -peak for the single species and two δ -peaks for the mixture of two species, which offers us an efficient way to distinguish the different species in the sample directly. As shown in **Figure 11D**, the TMR or Rh6G shows one peak in the result (dash lines on the left or right sides); the mixture of two species contains two peaks (solid line). So the different species in solutions can be easily distinguished.

Both PCH and FIDA analyze the molecular brightness and the average number of molecules within the observation volume. They have both similarities and differences. PCH begins with the calculation of the probability associated with fluctuations for a single particle in a reference volume and then convolutes the histogram of a single particle with n times to generate the histogram for n particles; FIDA begins with the calculation of the histogram for all particle numbers in a small volume and then convolutes it over the whole space, which generates the overall photon counts distribution. However, the theoretical formulations of the two in mathematical have been proved to be equivalence [108]. Meng *et al.* demonstrated that the numerical efficiency of PCH is faster than FIDA under the condition of power series expansion being used for the PSFs calculation [108].

FCS, PCH, and FIDA are all the methods for analyzing the fluorescence fluctuation within the observation volume. Compared with PCH and FIDA, FCS can acquire information on dynamics such as diffusion coefficients, and it can distinguish two species with different diffusion coefficients. Nevertheless,

PCH and FIDA can analyze heterogeneous samples containing multiple species having different molecular brightness.

APPLICATIONS OF FLUORESCENCE CORRELATION SPECTROSCOPY IN BIOLOGY

Since its invention, FCS has been extensively demonstrated for various applications in chemistry and life science [4–6], as shown in **Figure 12**, of which a few representative applications are listed below.

Diffusion Coefficient

The first important application of FCS is to measure the diffusion coefficient of biomolecules, which is directly related to the molecular size in a certain surrounding medium. For instance, Priest *et al.* [109] used FCS to measure the size of an inert fluorescent tracer inside the nucleus of a living cell. Shang *et al.* [110] utilized FCS to measure the hydrodynamic radius increase of the nanoparticles (NPs) due to protein adsorption. Klapper *et al.* [111] used FCS to quantify the hydrodynamic radius increase of the lipid-coated quantum dots (QDs) when being adsorbed with blood plasma proteins. Negwer *et al.* [112] utilized NIR excitation and emission based NIR-FCS to directly monitor the size and the loading efficiency of drug nanocarriers in human blood. Fu *et al.* [113] implemented multi-photon FCS and detected the dynamics of nanoparticles occurring within the vasculature in the brain of a live mouse. Recently, Struntz *et al.* [91] utilized SPIM-FCS to derive the diffusion maps of peripheral membrane protein PLC1 δ 1 in the embryo's cytoplasm and on the plasma membrane, and the result shows the spatially varying diffusion coefficients of PLC1 δ 1 across the embryo. Moreover, FCS can be used to quantify shape-related

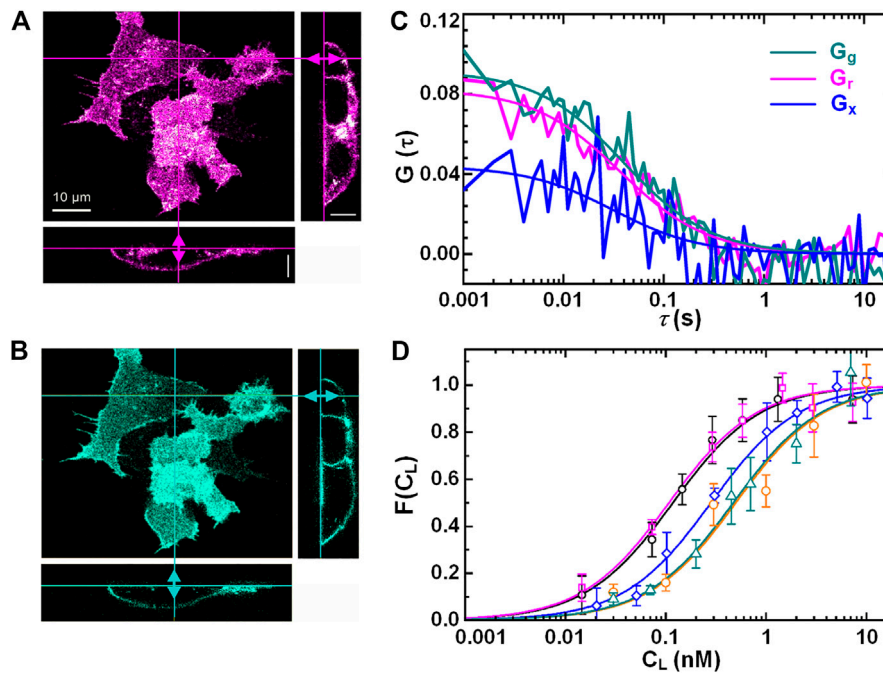


FIGURE 13 | Axial line-scanning FCS measurement on the interactions of ligand (DKK1-eGFP) and receptor (LRP6-mCherry) on cell membranes. Dual-color confocal images of live HEK293 T cells in the red channel (A) and the green channel (B). (C) The autocorrelation curves (G_g and G_r) and cross-correlation curve (G_x) on live NCI-H1703 cells. (D) Five binding curves (Fractional occupancies of the receptors) of five different cell-lines with different receptor densities. Adapted from Ref. [43].

diffusional dynamics. In this regard, Hinde *et al.* [60] used FCS to quantify the dynamics of four kinds of polymeric nanoparticles with identical surface chemistries but different shapes. The results turned out that these nanoparticles with different shapes behave differently in diffusional rates when moving across various cellular barriers. This finding is potentially useful for defining the site of drug release and optimizing the shape of drugs for effective release.

Rotational Diffusion

Except for the detection of translational diffusions, FCS can also detect rotational diffusion in the nanosecond to the microsecond time range. For the analysis, an exponential term is added to the FCS autocorrelation function considering the contribution of rotational diffusion [115–118]. Then, the rotational diffusion can be quantified from the fitting result. Jerker *et al.* [118] identified with this method the rotational diffusion of the GFP molecules in the nanosecond time range. Tsay *et al.* [117] studied the translational and rotational diffusion of peptide-coated semiconductor nanorods (pc-NRs) of various sizes and aspect ratios of the nanorods. The result from polarization-dependent FCS reveals that the pc-NRs with the square length of 12 nm have the translational diffusion constant of $40 \pm 10 \mu\text{m}^2\text{s}^{-1}$ and the rotational diffusion constant of $(1.5 \pm 0.5) \times 10^5 \text{s}^{-1}$.

Biomolecular Concentration

FCS can also be used to accurately measure the biomolecular concentration *in vitro* or *in vivo* by analyzing the amplitude of the correlation curve with a known observation volume. In this pursuit, FCS is often used to determine the concentration of

dye solutions after being diluted from a stock solution. Ries *et al.* [42] used dual-color FCCS to determine the concentration of free ligand Fgf8, free receptors (Fgfr1 and Fgfr4), and the ligand-receptor complexes in the cell membrane of living zebrafish embryos.

Viscosity

Moreover, FCS is capable of quantifying the viscosity of a solution, which can be determined from the diffusion coefficient by using the Stokes-Einstein relation. For example, the viscosity of poly (acrylic acid) grafted onto poly (ethylene terephthalate) films was determined by FCS [119].

Binding of Biomolecules

In addition, dual-color FCCS can be used to monitor the binding or unbinding of two kinds of biomolecules labeled with spectrum-distinct fluorophores. For example, Wenger *et al.* [120] used dual-color FCCS to study the kinetics of enzymatic cleavage reaction at 2- μM DNA oligonucleotide concentration. Veneri *et al.* [121] used FCS to detect impairment of Oct4-chromatin interactions and measured the dynamics changes in transcription factors Oct4 and Sox2 after differentiation was induced. The results are valuable to the studies of embryo development. Chelladurai *et al.* [122] used STED-FCS to provide novel insight on the physics/mechanism nanoparticles show enhanced binding tendency on two-component lipid bilayers compared to single-component membranes. This study also revealed how the binding and the diffusion of nanoparticles are linked to sub-diffraction dynamics and structures. Zhang *et al.* [123] measured by using

FCS the degree of the association and dissociation of mRNAs in the different buffer, such as full human serum and human ascitic fluid. Eckert *et al.* [43] measured the binding of the ligand DKK1 and the receptor LRP6 on cell membranes by utilizing axial lsFCS. In this experiment, the receptor proteins LRP6 were tagged with fluorescent protein mCherry, and the ligand DKK1 with eGFP. **Figures 13A, 3B** show 3D dual-color images of HEK293T cells with the receptor LRP6-mCherry and the ligand Dkk1 bound on the membrane. Dual-color axial lsFCS were performed at different ligand concentrations spanning from 0.05 to 100 nM. One group of correlation curves are shown in **Figure 13C**. Using the obtained FCS data, a binding curve can be calculated with **Eq. 4**, yielding $K_D = 0.22 \pm 0.02$ nM for the transiently transfected NCI-H1703 cells expressing LRP6-mCherry. Then, the binding of DKK1-eGFP and LRP6-mCherry on cell membranes were measured for five different cell lines that have different receptor densities. The results in **Figure 13D** implies that the binding affinity has a strong dependency on the receptor density.

Intercellular Obstacles

FCS is also capable of probing the diffusion paths of different directions and mapping the intercellular obstacles. Malacrida *et al.* [61] applied 2D-pCF to measure EGFP diffusing in MB231 cells. From the connectivity maps (**Figures 14A, 4C**), they found obstacles inside the nucleus (**Figures 14B, 4D**). In 2019, Hidde *et al.* used 2D-pCF to map the environment in cellular synapses perceived by natural killer (NK) cell receptors [62].

Developing Trend in Fluorescence Correlation Spectroscopy Applications

To determine more comprehensive dynamic information, multiple analysis on biomolecular diffusion have been used recently. For instance, Rienzo *et al.* [124] combined 2D pCF with iMSD to generate a fluorescence-fluctuation-based diffusion tensor that contains information on the speed and directionality of the local dynamical processes. Thus, the results provided a fresh insight into the GFP diffusion in the cytoplasm of *E. coli* and the dynamics of a protein diffusing on the plasma membrane of eukaryotic cells. Besides, Scipioni *et al.* [125] combined spot-variation FCS, 2D pCF, and iMSD to provide a comprehensive analysis of free GFP diffusing in live cells at different subcellular compartments.

In recent years, Malengo *et al.* [126] used FCS and PCH to estimate the diffusion coefficient and oligomerization state of GPI-anchored proteins. They showed that the mobile fractions of the two proteins uPAR-G and D2D3-G have comparable diffusion coefficients despite they are constituted by monomers and dimers, respectively. James *et al.* [127] implemented PCH and FCS in a confocal system for single-molecule detection. They found that the detection of single α -synuclein amyloid fibrils with this method has improved sensitivity of more than 10^5 -fold over bulk measurements. Scale *et al.* [128] proposed correlated PCH (cPCH), which reflects the probability to detect both a particular number of photons at the current time and another number at a later time. cPCH unifies FCS and PCH to resolve different fluorescent species using the information of their brightness and diffusion.

They demonstrated that two species differing in both their diffusion and brightness can be better resolved with cPCH than with either FCS or PCH.

SUMMARY

Being a powerful tool for detecting molecular concentration, hydrodynamic radius, diffusional dynamics, and the interaction of different biomolecules, FCS has been widely applied to different fields. Except for the applications in biology, FCS also has been applied in other fields [129–131]. For instance, FCS has been applied in physics for the study of dynamics/structure of liquid crystal molecules on silicon wafers [131], as well as anomalous diffusion inside soft colloidal suspensions [130]. We believe that, with further developments of lasers and sensors, FCS will become a more and more powerful tool for the study of molecular dynamics in different fields.

FCS has the advantages of high spatial and temporal resolution, short analysis time, and high sensitivity. Recently, novel techniques have been developed as extensions of FCS. Dual-color FCCS was proposed to quantify molecular interactions without the limitation of molecular size but need to correct incomplete overlap of two-color detection volume. Multi-focus FCS can provide spatial information at several points but is limited in time resolution. pCF is performed by calculating the correlation between a pair of points and thus provides spatial

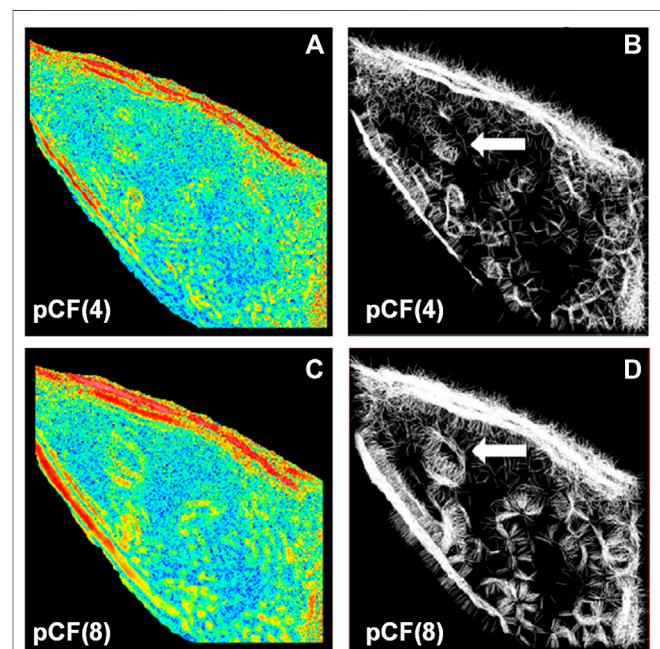


FIGURE 14 | 2D-pCF analysis of EGFP diffusing in MB231 cells. **(A)** and **(C)** The eccentricity of the diffusion calculated by using a pair of locations having a distance of 4 and 8 pixels. **(B)** and **(D)** The connectivity map is calculated by using a pair of locations having a distance of 4 and 8 pixels. The white arrows in **(B)** and **(D)** indicate an obstacle that forces the molecules to go around. Adapted from Ref. [61].

TABLE 1 | Overview of different FCS techniques.

Technique/Methods	Features/Capabilities	References
Traditional FCS	<ul style="list-style-type: none"> ✓ time resolution of sub-μs, enabling fast mobilities to be detected (D up to $300 \mu\text{m}^2\text{s}^{-1}$) ✓ need pre-calibration of focus size ✓ measurable concentration range: $1 \text{ pM} \sim 100 \text{ nM}$ ✓ data collection time, typically $10 \sim 120 \text{ s}$ ✓ lack of spatial information 	[3, 132]
Dual-color FCCS	<ul style="list-style-type: none"> ✓ susceptible to photo-bleaching, background noise ✓ target the interactions of different molecules ✓ more sensitive to the binding of two-color molecules due to the usage of cross-correlation ✓ susceptible to spectral crosstalk, focus overlap, photo-bleaching, background noise 	[10, 114]
Imaging FCS Multi-focus/scale FCS	<ul style="list-style-type: none"> ✓ capable of probing dynamics at different locations ✓ no need to characterize the focus size ✓ time resolution is limited by imaging sensor, typically tens of ms 	[11, 45]
Pair correlation function (pCF)	<ul style="list-style-type: none"> ✓ the correlation of any pairs of spots can be analyzed ✓ enables to detect a barrier along a certain path ✓ typical time resolution: 1 ms 	[12, 60]
Scanning FCS	<ul style="list-style-type: none"> ✓ reduced photobleaching ✓ limited time resolution, typically, 1 ms ✓ parallel scanning FCS is capable of obtaining location-dependent dynamics ✓ perpendicular scanning FCS compensates for membrane movements 	[64, 68]
TIR-FCS	<ul style="list-style-type: none"> ✓ axial resolution $\leq 100 \text{ nm}$ ✓ only applicable to the molecules diffusing at surfaces ✓ capable of measuring samples of higher concentration ✓ diffusion is inevitably influenced by the bottom surface 	[81]
SPIM-FCS	<ul style="list-style-type: none"> ✓ enable to detect dynamics at any position in a volumetric sample ✓ less phototoxicity and photobleaching ✓ axial extension of the observation volume is reduced by a light sheet ✓ time resolution is limited by the imaging sensor 	[15]
STED-FCS	<ul style="list-style-type: none"> ✓ lateral resolution \sim tens of nm ✓ capable of detecting heterogeneous dynamics ✓ capable of measuring higher concentration samples ✓ susceptible to photobleaching 	[75, 97]
Inverse FCS	<ul style="list-style-type: none"> ✓ measure unlabeled particles in fluorescent surrounding medium ✓ requires high-concentration surrounding medium, $\geq 10 \mu\text{M}$ ✓ only applicable to relatively large particles to detection volume 	[16, 104]
PCH/FIDA	<ul style="list-style-type: none"> ✓ capable of acquiring the concentration and brightness of molecules ✓ capable of analyzing multiple particle species with different brightness ✓ incapable of determining diffusion coefficient 	[17, 18]

information. Scanning FCS is suitable for measuring membrane-associated dynamics since it avoids photobleaching and the artifact induced by membrane movement. Of note, the recent axial line-scanning FCS has a significantly enhanced time resolution ($\sim 50 \mu\text{s}$), targeting the dynamics on time-varying membranes. TIR-FCS measures molecular motion that occurs in the sample surface specifically. SPIM-FCS detects dynamic information from thousands of points simultaneously and avoids the noise from out-of-focus regions. STED-FCS reduces detection volume and allows measuring biomolecular dynamics in nanoscale or with a much higher concentration. Inverse-FCS measures unlabeled particles in a dense fluorescent medium, then provides particle size and concentration independent of the diffusional dynamic. While, this method is only applicable to relatively large particles (preferably with particle radius $\geq 40 \text{ nm}$). While, if being combined with STED, iFCS can detect particles with even smaller diameters. PCH and FIDA, being parallel techniques to FCS, can determine the molecular brightness and is capable of measuring heterogeneous samples with multiple species. The features and capabilities of different FCS technique have been summarized in **Table 1**.

It is worthy to point out that FCS also has some drawbacks. The results of FCS are easily handicapped by many factors in the experimental system or sample preparation. First, The observation volume changes with specific experimental settings, such as the cover-slide thickness variation and index mismatch [44]. Second, the focus volumes of two-color excitation pulses are different in dual-color FCCS, which may decrease the amplitude of cross-correlation. So we must correct it during data processing. Third, FCS is not suited for samples with a tendency to aggregate. When FCS is used to measure aggregating samples, the correlation curves become ill-shaped and poorly reproducible because a few very bright aggregates can distort the entire data set [133]. Therefore, a careful selection of an intensity trace is necessary in this case. Fourth, the photobleaching of fluorophores at high excitation powers is usually unavoidable during the measurements. The photobleaching reduces the fluorescence intensity over time and results in a reduction of the concentration and increase of the diffusion coefficient. So the compensation for the effect of photobleaching on both the intensity trace and the measured amplitude of the correlation curves is important [43]. Fifth, the measurable concentration range is limited to $1 \text{ pM} \sim 100 \text{ nM}$ with FCS. The lower limit is set to guarantee the fluorescence fluctuation is larger than the noise,

and the upper limit is set to guarantee the fluctuation is sufficient (more molecules in focus will have a lower fluctuation). Sixth, FCS is, in essence, a statistical method, and the result obtained with FCS presents the average behavior of a large number of molecules. By contrast, single molecular tracking (SMT) enables to provide dynamics for specific molecules by taking image series, leading to insensitivity to single-molecule heterogeneity.

Being driven by the above-mentioned drawbacks of FCS and the existence of essentially complex problems in biology, there is still a need to further improve FCS in the future. First, the experimental setups of FCS can be further improved, *e.g.*, to further enhance the temporal and spatial resolution. Second, the optimization of FCS mathematical models is expected to fit better specific experimental settings. Third, the extension of dual-color FCCS to multi-color FCS is needed to support this scenario where the interactions among multiple species are involved in reality. Fourth, the combination of FCS with other technologies is still in need to fit a complex biological application, considering different methods feature different advantages and limitations.

AUTHOR CONTRIBUTIONS

PG conceived the manuscript. LY and YL wrote the draft of the manuscript; YM, ML, JZ, and DD organized the manuscript; all the authors edited the article.

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SUPPLEMENTARY MATERIAL

The **Supplementary Material** for this article can be found online at: <https://www.frontiersin.org/articles/10.3389/fphy.2021.644450/full#supplementary-material>.

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Conflict of Interest: The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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