Developments and Recent Progresses in Microwave Impedance Microscope

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Microwave impedance microscope (MIM) is a near-field microwave technology which has low emission energy and can detect samples without any damages. It has numerous advantages, which can appreciably suppress the common-mode signal as the sensing probe separates from the excitation electrode, and it is an effective device to represent electrical properties with high spatial resolution. This article reviews the major theories of MIM in detail which involve basic principles and instrument configuration. Besides, this paper summarizes the improvement of MIM properties, and its cutting-edge applications in quantitative measurements of nanoscale permittivity and conductivity, capacitance variation, and electronic inhomogeneity. The relevant implementations in recent literature and prospects of MIM based on the current requirements are discussed. Limitations and advantages of MIM are also highlighted and surveyed to raise awareness for more research into the existing near-field microwave microscopy. This review on the ongoing progress and future perspectives of MIM technology aims to provide a reference for the electronic and microwave measurement community.

Keywords: microwave impedance microscope, near-field measurement, microwave probes, electrical properties, microwave measurement technique

INTRODUCTION

The past decade has witnessed efforts in the field of microwave to develop a near-field scanning microwave microscope (NSMM) as a scientifically powerful instrument with rapid development [1–9]. Early implementations of the microscope either used a small aperture at microwave cavities [2, 4] or a needle-shape probe coupled to a microwave resonator [5, 8–11]. Due to the hardship in tip-sample distance control, these approaches are intrinsically susceptible to tip damage and difficult in nanoscale quantitative measurement applications [9, 12]. The microwave impedance microscope (MIM) can control tight distance perfectly and solve the crucial probe-sample gap control issue in the nanometer range NSMM. Moreover, it shows great advantages in reducing the loss in doped silicon traces while ensuring large power gain and high sensitivity because it employs metal lines for the electrodes and cancels background signal before amplification. In addition, the MIM can significantly suppress the common-mode signal since the inductive probe is separated from the excitation electrode. Compared to atomic force microscopy (AFM) and scanning tunneling microscopy (STM), the long-range electrostatic force involved in scanning MIM reduces the stringent requirements for proximal probes, enabling high-speed, non-contact, and non-destructive measurements [13–16]. Due to the aforementioned advantages, the MIM achieves near-field measurements at nanoscale and has great potential in future application of high-resolution microwave images generation.

FIGURE 1 | Schematic diagram of MIM. Reproduced with permission from Rev. Sci. Instrum. 79, 6 (2008). Copyright 2008 American Institute of Physics.

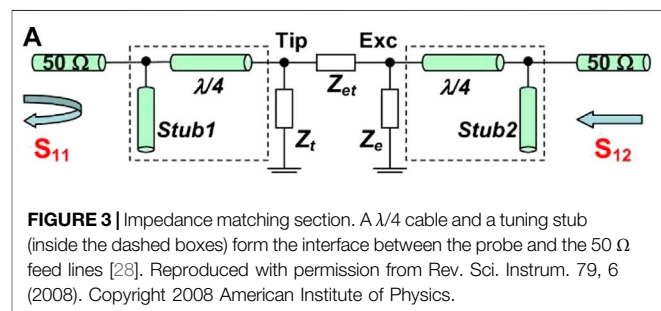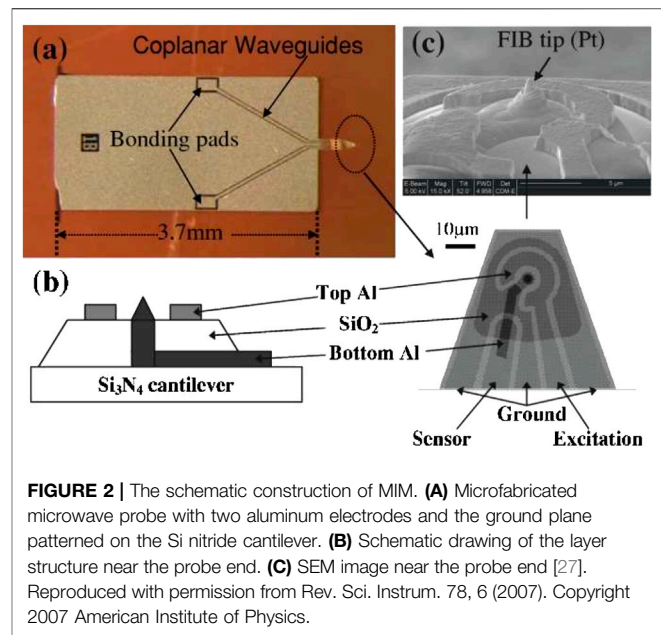In this review, we present a comprehensive study of development and recent progress in MIM. This review focuses on technique improvements and applications and covers MIM limitations and advantages, as well as the opportunities for further research into the subject of near-field measurement. The rest of this paper is organized as follows. *Basic Design and Improvement of Scanning Microwave Impedance Microscopy* gives a brief history and an overview of the structure of MIM and discusses the fabrication process and improvement of MIM. *Cutting-Edge Application of Microwave Impedance Microscope* treats various cutting-edge applications. *Conclusion* presents the conclusions and discussion.

BASIC DESIGN AND IMPROVEMENT OF SCANNING MICROWAVE IMPEDANCE MICROSCOPY
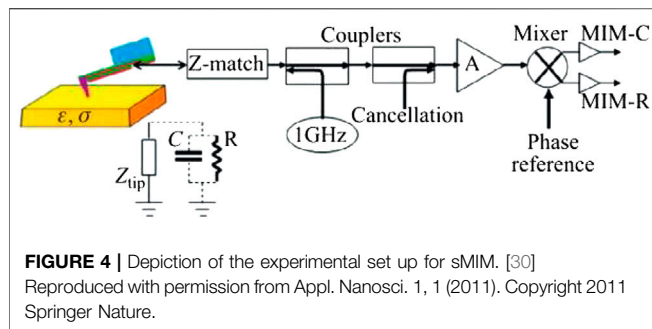
History and Design of Scanning Microwave Impedance Microscopy

The employment of microwave frequency band has many advantages, such as strong penetration, the ability to detect the internal information of the sample, and the common polarization of short relaxation time by the frequency influence. The near-field microwave microscope works in the same principle in several generations. The resonator resonates in the $\lambda/4$ coaxial resonator through the coupling loop, then the resonant signal acts on the sample after the needlepoint conduction. The microwave reflection of the sample absorbed by the resonator will interact with the microwave resonance. It causes resonance frequency change. The reflected microwave decays quickly and is much smaller than the microwave output signal, so the perturbation equation can be used to analyze it [17–19]. Scanning microwave microscopy (SMM) is a powerful tool for the investigation of various properties, including conductivity, permittivity, and impedance at the nanoscale. Different kinds of resonant SMMs with excessive sensitivity and spatial resolution have been demonstrated [5–9]. Despite the great progress in SMMs, various barriers exist in current designs [14, 20]. A case in point is the large common-mode signal, which results in loud noise. Slow

FIGURE 2 | The schematic construction of MIM. **(A)** Microfabricated microwave probe with two aluminum electrodes and the ground plane patterned on the Si nitride cantilever. **(B)** Schematic drawing of the layer structure near the probe end. **(C)** SEM image near the probe end [27]. Reproduced with permission from Rev. Sci. Instrum. 78, 6 (2007). Copyright 2007 American Institute of Physics.

FIGURE 3 | Impedance matching section. A $\lambda/4$ cable and a tuning stub (inside the dashed boxes) form the interface between the probe and the 50 Ω feed lines [28]. Reproduced with permission from Rev. Sci. Instrum. 79, 6 (2008). Copyright 2008 American Institute of Physics.

operation and low bandwidth dampen the special effect of long-range force involved in a microwave microscope. Scanning microwave impedance microscopy (MIM) is a species of SMM [21–26]. MIM solves this problem successfully. Unlike traditional SMMs, MIM determines the electrical properties through the analysis of the phase and amplitude of the reflected wave instead of through frequency drift and quality factor change. The preponderance of this technique is that it shields the external signal and reduces the common-mode signal. MIM detects dielectric responses at a much wider frequency range (GHz). MIM demonstrates the capacity to acquire high-resolution microwave images of buried structures, as well as nanoparticles, nanowires, and biological samples.

In Ref. 27, a handy and clear explanation of MIM system characteristics was introduced. As shown in **Figure 1**, system characterization involved tip-sample interaction, impedance matching, and microwave circuitry. The outstanding point of MIM is that the sensor probe is separated from the excitation electrode while maintaining high sensitivity and spatial resolution. The schematic construction of MIM was shown in **Figure 2**, in which the traditional tip is replaced with a standard AFM tip assembly and two transmission lines are included, one

FIGURE 4 | Depiction of the experimental set up for sMIM. [30] Reproduced with permission from Appl. Nanosci. 1, 1 (2011). Copyright 2011 Springer Nature.

FIGURE 5 | S_{11} image with four different probes indicates a minimum sensitivity. [40] **(A)** Scan results for the Ti/Al NW probe over DUT showing the change in the amplitude of the microwave reflection coefficient S11. All micro-capacitors are present in the image, indicating sensitivity to at least 0.7 fF. **(B)** S11 image with a bare NW probe indicates a minimum sensitivity of 3 fF. **(C)** S11 image with Si probe indicates a minimum sensitivity of 6 fF. **(D)** S11 image with Pt probe indicates a minimum sensitivity of 0.7 fF. All scans are plotted with different Z-axis color scales for clarity. All micro-capacitors are present in the image, indicating sensitivity to at least 0.7 fF [40]. Reproduced with permission from Appl. Phys. Lett. 104, 2 (2014). Copyright 2014 American Institute of Physics.

for excitation and the other for sensing. A two-layer implementation like this improves the system's common-mode rejection ratio and reduces the noise level significantly. With appropriate design, the detector can be "orthogonal". Then the signal is minimized without a sample. A high throughput near-field scanning microwave microscope can be implemented. Besides the sharp sensing electrode, a second electrode surrounding the tip is also present on the cantilever to significantly suppress the common-mode signal.

In Ref. 28, the lumped element circuit description is related to the representative probe, with three impedances Ze, Zt, and Zet as illustrated in **Figure 3**. Since there is a large mismatch between Zt (Ze) and the transmission line impedance Z_0(50 Ω), the microwave power cannot be transmitted to the probe, and detecting a small microwave impedance variation is infeasible if the microwave power is directly connected to the feeder. In order to improve the transmission of microwave power, it is important to achieve impedance matching. The tip of the MIM is first connected to a portion at the end of a λ/4 section of a transmission line to form a resonator. As shown in **Figure 3**, the resonator is then critically coupled to the feed line by a parallel open-end tuning stub. An almost perfect match is easily obtained with this adjustable stub [29].

In Ref. 30, the microwave is conducted into the tip through a directional coupler. Then it gets into the directional coupler after the surface reflection, and a cancellation signal is inputted to suppress the background reflected signal at the same time. Reflection microwave signals and cancellation signals are amplified and demodulated to the quadrature mixer. Finally, the reflected signal is composed of in-phase and out-of-phase components [28, 29]. It contains data about the local permittivity (capacitance) and conductivity (resistance) of the sample. But there are still some problems. The tip electrode is the most sensitive to local electrical performance, while the ring electrodes to topography. Therefore, combining the signals from the two electrodes may eliminate the convolution of electrical and topographical information.

Improvement of Scanning Microwave Impedance Microscopy

In recent years, MIM has been developed to characterize the electrical properties of samples such as permittivity and conductivity. Accordingly, the need for MIM is increased.
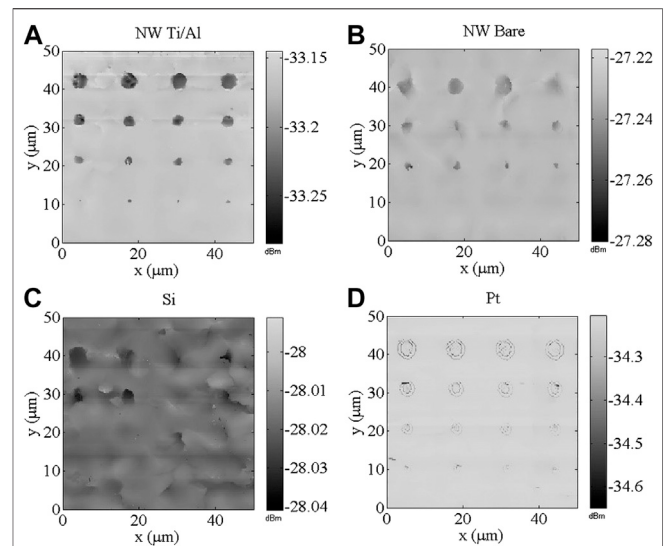
Many recent articles discuss the improvement of MIM in sensitivity, resolution and wideband. Meanwhile, tip wearing and sample dragging have become an increasingly serious issue in near-field microwave measurement. Many researchers have been able to make probes on a large scale by improving the manufacturing process [31]. **Table 1** compares and summarizes different techniques and methodologies for the improvement of MIM.

In Ref. 32, a compact mode microwave impedance imaging based on an atomic force microscope platform was proposed. Tap mode microwave imaging was also superior to contact mode because thermal drift and other electron drift observed in contact mode can be completely eliminated and absolute measurements of dielectric properties can be made. Because the actual tip-sample interaction is modulated at the tapping frequency, slowly varying temperatures and other electronic drifts that occur over a longer time frame do not contaminate the microwave image [33–35]. Since the cantilever probe oscillates at its resonant frequency, it only intermittently contacts the surface of the sample. Tip wear and sample drag are greatly reduced. It was also shown that the tap mode MIM can be executed on the actual Nanodevices.

In Ref. 36, the authors reported the design and fabrication of a piezoresistive cantilever with a low-impedance conduction line to our electrically-shielded tip. Their new design exhibits a vertical displacement resolution of 3.5 nm in a measurement bandwidth from 1 Hz to 10 kHz. The probes provide topography feedback

TABLE 1 | Summarization of different techniques for the improvement of MIM.

Indicator	Different techniques	Result
Sensitivity	Fabrication in a GaN nanowire probe [40]	Improve sensitivity and alleviate the need to re-calibrate the system frequently
	a fully integrated CMOS-MEMS SMM [59]	Improve the signal to noise ratio and maximize the sensitivity
Resolution	a silicon donor nanostructure design for STM [55]	Quantify the resolution limit of sMIM
Wideband	a piezoresistive cantilever with a low-impedance conduction line to electrically-shielded tip [36]	Resolution of 3.5 nm in a measurement bandwidth from 1 HZ to 10 kHz
Measurement conditions	a compact mode microwave impedance imaging [32]	Tip wear and sample drag are greatly reduced
	a novel batch-processed low impedance, well-shielded and sharp tips piezoresistive cantilever probes [46]	MIM capability at both room and cryogenic temperatures
	SMM integrated into a scanning electron microscope and a focused ion beam (SEM/FIB) instrument [53]	The automated operation of nanoobjects goes a step further

FIGURE 6 | Block diagram of the SMM system.
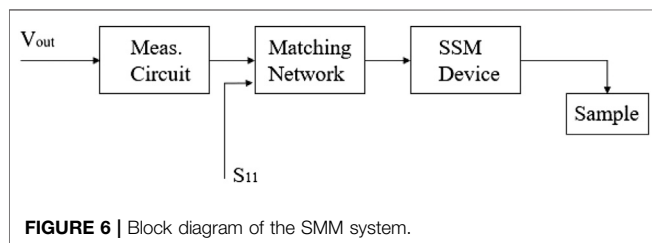
with nanometer vertical resolution for samples or setups where laser detection is not feasible or desirable. Furthermore, the low parasitic impedance of the tip enables MIM measurements. Although the capacitance and resistance of the tip are not as low as previously reported probes, the measured impedance suggests MIM measurements can be obtained in a self-sensing mode, though with decreased MIM sensitivity and thus contrast [37–39]. The self-sensing cantilever allows topography feedback where the laser beam bounce technique is not available or hard to implement. This probe will enable coupled topography scans with MIM images.

In Ref. 40, a novel fabrication in a GaN nanowire probe for near-field scanning microwave microscopy was suggested and investigated, with improved sensitivity and reduced uncertainty achieved which can measure capacitance values down to as small as 0.7 fF while simultaneously recording 10 nm height changes. The changes of the Mean measurement parameter (S_{11}) sensitivity that the nanowire probe is coated a Ti/Al layer and across the device under test (DUT) micro capacitors were much greater than a commercial Pt NSMM probe [41–45]. The measurement uncertainty was significantly reduced. It is important to improve wear resistance during contact-mode scanning. The high-intensive of the defect-free nanowire improved measurement repeatability and alleviated the need to re-calibrate the system frequently because it keeps the tip radius constant between the scans.

In Ref. 46, the authors reported a new type batch-processed low impedance, well-shielded and sharp tips piezoresistive cantilever probes for simultaneously topographical and electrical scanning probe microscopy. The integration of a piezo resistor on MIM probes is a challenging task [47–49]. The small resistance and capacitance, as well as the shielded

structure, ensure great electrical performance. High quality piezo resistive topography and MIM images are simultaneously obtained with the fabricated probes [50–52]. These novel piezoresistive probes remarkably broaden MIM applications in scientific and engineering research of new materials and electronic devices by operating photosensitive samples with an integrated feedback mechanism at low temperatures. The probes show good piezoresistive topographic and MIM capability at both room and cryogenic temperatures.

In Ref. 53, the main idea was to integrate a scanning microwave microscope into a scanning electron microscope and a focused ion beam (SEM/FIB) instrument for nanoscale imaging, characterization, and manipulation. Scanning electronics and microwave microscopy operated in an open-source automation software environment [54]. The automated operation of nanoobjects goes a step further with the development of hybrid open-source microscope tools. This scanning microwave microscope can image the terrain, measure electromagnetic performance at microwave frequencies, and manipulate the "sample under test."

In Ref. 55, a simple and novel silicon donor nanostructure design for scanning tunneling microscopy (STM) mode was introduced to quantify the resolution limit of sMIM. The doping pattern is buried under a protective silicon cap by a 10 nm highly conductive silicon line and imaged with sMIM, which is an ideal test for the resolution and sensitivity of sMIM technology because it is made in nm resolution and can reduce the complexity caused by terrain convolution [56–58]. sMIM has been identified as an excellent platform for studying buried donor structures, opening up a field of research with further advantages of this technology, such as monotonic signal response. Looking ahead, sMIM is an ideal technique for identifying buried-pattern devices and may allow for quantified post-processing characterization of donor structures, which may be an important tool for studying atomic-level transistors and the latest quantum computing solutions.

In Ref. 59, the format and overall performance of a fully integrated CMOS-MEMS SMM were described particularly. A measuring unit has been developed, constructed, and applied to enhance the signal to noise ratio and maximize the sensitivity of
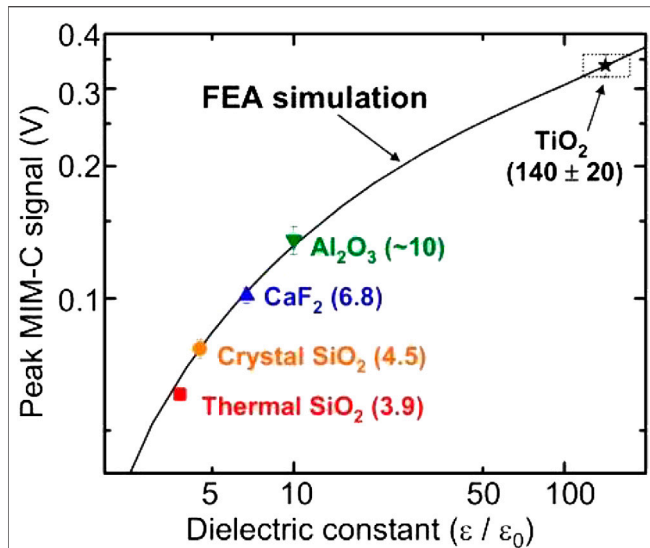
FIGURE 7 | Peak MIM-C signal in tip-sample approaching as a function of the relative dielectric constant [61]. Reproduced with permission from Appl. Phys. Lett. 93, 12 (2008). Copyright 2008 American Institute of Physics.
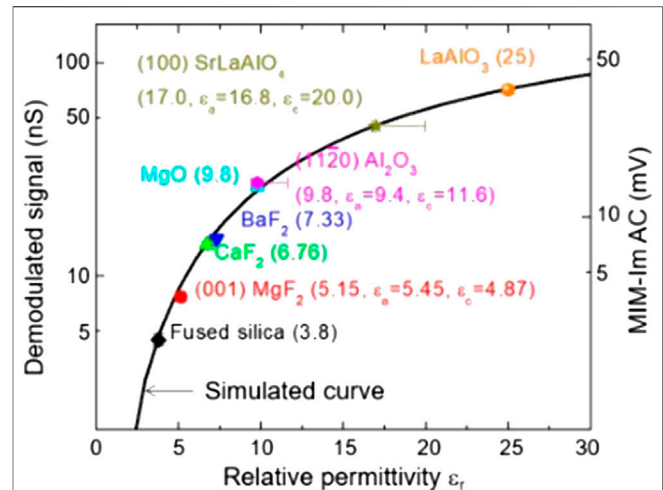

FIGURE 8 | Demodulated tip-sample admittance and the corresponding MIM-Im AC signals as a function of the relative permittivity [69]. Reproduced with permission from Rev. Sci. Instrum. 89, 4 (2018). Copyright 2018 American Institute of Physics.

the CMOS-MEMS SMM system. The block diagram of the complete SMM system includes the tip of the sample being tested, the SMM device fabricated using CMOS-MEMS technology, the matching network, and the measurement circuit [60]. In this situation, an increase in sensitivity means that for a given tip-sample impedance change, the change in system output (V_{out} or S_{11} in **Figure 6**) will be maximized. These experiments confirmed the workable of SMM to reveal characteristics not detected using AFM. These analyses are carried out on the new CMOS-MEMS SMM system described in this paper to assist designers to enhance the sensitivity of traditional SMM systems. The analysis presented in this article applies not only to CMOS-MEMS SMMs but to any kind of SMM.

Cutting-Edge Application of Microwave Impedance Microscope

sMIM is a quantitative near-field tool [27, 28] that operates at a high-frequency ~ GHz range [28]. It can detect the electrical properties of various samples and implement microwave detection technology at a macro/nano scale, showing broad application prospects. MIM has made rapid progress. With the passing of the years, many people have participated in the research of MIM application, and push the frontiers of MIM further. MIM technology does not have limitations on the dimensions of the sample as well as on its properties. It can be widely used in semiconductors, insulators, metals, magnetic materials, chemical molecules, and biological cells. In terms of property measurement, it can measure the basic electrical properties such as dielectric constant, conductance, capacitance variation, and electronic inhomogeneity. Recent applications of SMM are summarized in this section.

Quantitative Measurements of Nanoscale Permittivity and Conductivity

In Ref. 61, the dielectric constant of materials including high-k insulators can be quantitatively measured and the author measured the approximate curve of an oscillating tip toward bulk dielectric samples using the MIM. Unlike coplanar probes with poor shielding capabilities, which sense a sample distance of tens of microns, the shielding of the wire eliminates spurious signals from the cantilever body and enables quantitative analysis of tip-sample interactions. The approximation curve of the MIM-C channel output can be accurately described by lumped element FEA simulation using standard locking techniques. The peak signal near the curve is a measure of the dielectric constant of the sample and can be used to explore unknown bulk materials [61]. permit by using a large number of dielectrics and permittivity of unknown materials.

In Ref. 62, the authors presented a rigorous modeling of nanosized SMM probes and their electrodynamic interaction with material samples at microwave frequencies [62]. They concluded that the SMM had the potential for use as a broadband dielectric spectroscopy operating at higher frequencies up to THz [63, 64]. The numerical simulation is carried out by the finite element method (FEM). They pointed out that the quasi-static model was accurate in calculating the tip sampling capacitance., and with the increase of frequency, the accuracy of loss calculation decreased [65, 66]. Their simulations show that the SMMs operating at higher frequency provides greater sensitivity on the evaluation of dielectric loss.

In Ref. 67, the authors demonstrated the MIM experiments on a static random-access memory (SRAM) sample to resolve the local conductivity distribution. They showed the microwave imaging on the staircase and SRAM samples in the linear impedance. While the conventional SCM images match the nominal device structure, the MIM images display certain unexpected features of the nominal
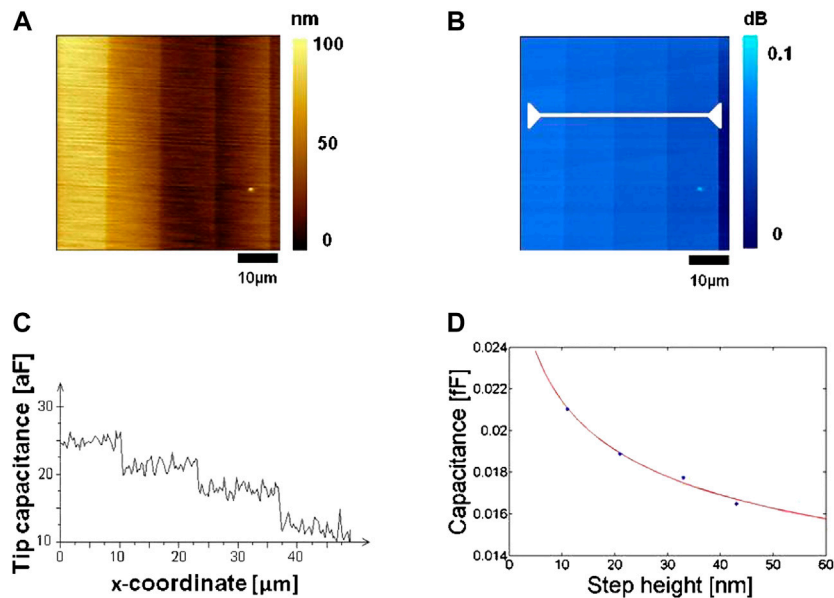
FIGURE 9 | AFM-tip/sample capacitance and effective tip radius. [70] **(A)** Topographical image of the bare 10 nm stepped dielectric staircase structure. **(B)** Corresponding PNA amplitude image with the different steps resolved (0 dB corresponds to the bare silicon surface, as seen at the far-right edge of the image). **(C)** The PNA amplitudes were converted to capacitances and plotted concerning the x-coordinate of the white line in **(B)**. **(D)** For each dielectric step, the capacitance was determined using an area analysis and subsequent averaging of the PNA amplitude [70]. Reproduced with permission from Rev. Sci. Instrum. 81, 11 (2010). Copyright 2010 American Institute of Physics.
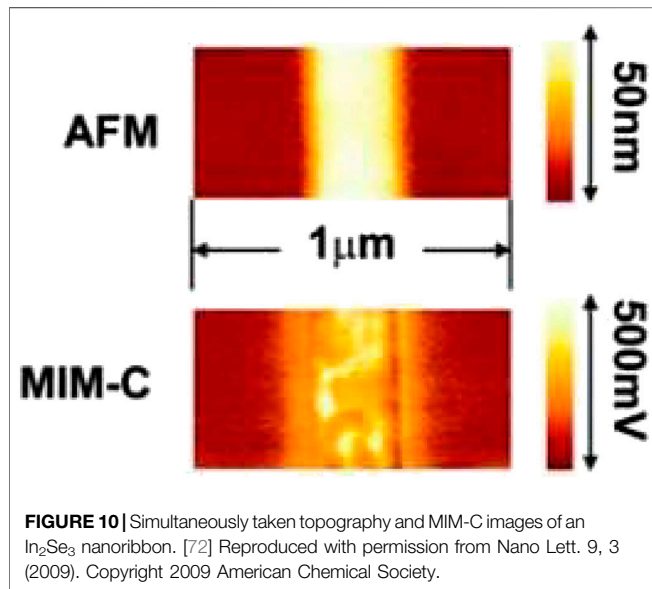

FIGURE 10 | Simultaneously taken topography and MIM-C images of an In_2Se_3 nanoribbon. [72] Reproduced with permission from Nano Lett. 9, 3 (2009). Copyright 2009 American Chemical Society.

doping maps, which originate from a thin layer of the dopant ions that go through protective layers during the ion-implantation processes. Real-space mapping of doping concentration in semiconductor devices is of great importance for the microelectronic industry. Their technique can measure the surface impedance by MIM and carry types by SCM. With these capabilities, our technique clearly shows great potentials for applications in the semiconductor industry.

In Ref. 68, the authors created a quantification scheme extracting sample conductivity and permittivity from admittance with only the use of the capacitive calibration die provided by the instrument using simulations and MIM measurements. The prediction was verified with a sample of polytetrafluoroethylene (PTFE). They have provided with finite element simulations the full tip-sample behavior as a function of both permittivity and conductivity. They furthermore demonstrated a method for extracting values of permittivity from the contrast map under certain constraints for the conductivity. Here they supply the full behavior for multiple values of both parameters. MIM is a valuable technique that can image admittance contrast with minimal sample preparation.

In Ref. 69, the authors reported a method for the quantitative measurement of nanoscale dielectric constant and conductivity using a tuning-fork (TF) based MIM. A tuning fork (TF) based MIM with an etched metal tip provides an excellent solution to tip degradation problems. They further developed TF-MIM by using drive amplitude modulation (DAM) mode, which provides satisfactory stability for samples with rough surfaces. The demodulated MIM AC signal was simulated by combining the finite element analysis (FEA) of the leading sample admittance with the Fourier transform of the real-time signal. The simulation results agree well with the experimental data on bulk media and working nanometer devices. This work shows that TF-MIM is an effective tool for quantitative nanoscale imaging of electrical properties in functional materials. Their work provides a method to perform quantitative near-field microwave imaging, where absolute signal levels can be easily construed as local permittivity and conductivity [69].

Capacitance Variation

In Ref. 70, this paper proposes a calibration method that can be widely applied to SMM based on the study of the quantitative dimension of dielectric constants of thin films using SMM. And calibration procedures for nanoscale capacitance measurements permit quantitative evaluation of material and device overall performance in SMM measurements. Customized standard samples, coupled with end-to-end interaction modeling and thorough PNA data processing, make it possible to calibrate SMM parameters, including calibration capacitance and effective probe size. This quantitative information is important to understand the response and conduct of nanoscale systems, in particular when equipment performance must be evaluated over its expected operating frequency range. In order to determine the absolute capacitance value by the PNA reflection amplitude, a calibration pattern of quite a number sizes of conductive gold pads on the SiO_2 step shape used to be used.

In Ref. 71, the authors proposed a general method for calculating the change in capacitance of a tip-sample in a near-field scanning microwave microscope. This method can accurately calculate the change in capacitance due to uneven perturbations in insulated or conductive samples, which has been verified by finite element analysis of commercial software and experimental data from MIM. Furthermore, the method presented in this paper also provides a rigorous framework to solve the inverse problem, with great potential to increase the resolution by deconvolution. This method can be applied directly to scanning microscopes and saves a lot of time and memory. The frame is suitable for a wide range of models. Regardless of tip shape, sample type, and disturbing material, the results are very accurate and can be applied to any tip shape, thick film, and variations due to uneven disturbances.

Electronic Inhomogeneity

In Ref. 72, the authors reported the observation of electronic inhomogeneity in indium selenide (In_2Se_3) nanoribbons by near-field scanning MIM. Microwave probes compatible with atomic force microscopy enable quantitative sub-surface electronics research in a non-invasive manner. The large signal with opposite signs recorded by the MIM most vividly displays the phase change memory function of the In_2Se_3 devices. It is possible to further implement the MIM as a spatially-resolved readout instrument for memories with great resistivity changes [72]. MIM cannot detect small topographic changes with phases changes, but can directly measure local electronic properties and is more sensitive to operations [73–76]. The author demonstrates that the MIM can provide spatially resolved information when In_2Se_3 nano-devices are phase-switched by voltage pulses [72].

CONCLUSION

Near-field microscopy at microwave frequencies has attracted many research interests in the past decades. MIM expands the scope of local electrical characteristics testing. The MIM based on

microwave detection mainly uses microwave as the detection source and obtains the information of the tiny electrical parameters in the sample microregion in combination with probe technology. The MIM probe is microfabricated on a silicon nitride cantilever with a shielded metal trace and a Pt tip deposited by a focused ion beam (FIB). Microwave electronics can get the local information of these materials by detecting the real and imaginary parts of the effective tip-sample impedance, and microwave electronics output as MIM-R and MIM-C signals [72]. Therefore, we believe that MIM can provide a powerful and versatile tool to study nanoscale dielectric inhomogeneities in a non-invasive manner [72]. This paper reviews developments and recent progress in MIM and discusses both MIM limitations and advantages, as well as the opportunities for further research into the subject of near-field measurement. This paper also seeks to raise awareness regarding the need for more research into the existing near-field microwave microscopy in order to address the limitations of MIM.

The MIM has been successfully used to obtain calibrated values of relevant physical quantities, such as capacitance, complex impedance and resistance, and surface localized physical sample properties (electric permittivity, dopant density, and resistivity) with nanoscale spatial resolution. In a hot research field, MIM plays important roles in the detection of various electrical properties of samples. In addition, the MIM can also work at room temperature, low temperature, vacuum, and magnetic field, which greatly improves the measurement range and the feasibility of operating in multiple environments.

However, the geometry of the tip is limited to a few specific types. The finished nib is almost impossible to have a strictly regular shape in practice. For near-field microscope in the microwave state, few theoretical works focus on specific designs presented. As with any artifact, due to the disturbance caused by the probe, the measurement component of the microwave signal and the image deconvolution has not been attracted much attention. With the development of microwave near-field microscopy, these voids will be filled in time [14]. At the same time, the preparation of the scale and the durability of the probe are long-term topics.

AUTHOR CONTRIBUTIONS

XC and XQ conducted the review and guide on the content. ZZ wrote the manuscript. HH and FN contributed in discussion and helped searching the literature. LS and YY conceived the design and layout of the paper.

FUNDING

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