



On the Possibility of Experimental Detection of the Discreteness of Time

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The Bose-Marletto-Vedral (BMV) experiment tests a quantum gravitational effect predicted by low energy perturbative quantum gravity. It has received attention because it may soon be within observational reach in the lab. We point out that: (i) in relativistic language, the experiment tests an interference effect between proper-time intervals; (ii) the feasibility study by Bose et al. suggests that current technology could allow to probe differences of such proper-time intervals of the order of 10^{-38} seconds, about twenty orders of magnitude beyond the current resolution of the best atomic clocks; (iii) the difference of proper times approaches Planck time (10^{-44} s) if the masses of the particles in the experiment approach the Planck mass (\sim micrograms). This implies that the experiment might open a window on the structure of time at the Planck scale. We show that if time differences are discrete at the Planck scale—as research in quantum gravity may suggest—the Planckian discreteness of time would appear as quantum levels of an in principle measurable entanglement entropy.

Keywords: quantum gravity, time discreteness, entanglement, non perturbative effects, quantum gravity phenomenology

1. INTRODUCTION

Bose et al. [1] and Marletto and Vedral [2, 3] have proposed an ingenious idea to amplify and observe minuscule quantum gravitational effects in a table-top experiment. The idea has received considerable attention [4–14]. In the version proposed in Bose et al. [1] the observable signal is given by Bell-like correlations among the spins of two particles. The correlations are produced by a gravitational interaction. If we assume the identification of gravity with spacetime geometry which is at the basis of general relativity, the observation of these correlations implies that spacetime geometry can be in a quantum superposition (in a non-semiclassical state), and therefore can be taken as evidence for quantum behavior of the geometry [10].

The Bose-Marletto-Vedral (BMV) effect is predicted by low energy perturbative quantum gravity, and hence by any approach to quantum gravity consistent with this low energy expansion, including string theory and loop quantum gravity. It is therefore plausibly real. If detected, it would provide indirect empirical evidence that spacetime geometry does obey quantum mechanics.

On the other hand, the BMV effect is insensitive to the limit $c \rightarrow \infty$, hence the gravitational interaction involved can be described in a non-relativistic language. For this reason, it does not test the full relativistic quantum gravitational regime. In fact, the effect can be accounted for purely in terms of the scalar non-radiative modes of the gravitational field, hence it does not test the quantum *dynamics* of gravity. If we do not fold in the relativistic information provided by classical

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general relativity, the effect can be interpreted in terms of Newton's action at a distance, leading to objections on the relevance of the effect for the quantum properties of spacetime [4].

Here, we point out that a refinement of the BMV effect *could* open a window on a quantum gravitational effect that would definitely not be accounted for by non-relativistic quantum physics: time discreteness. The reason this is possible is that from the point of view of general relativity the BMV set up is a delicate interference apparatus that picks up a tiny difference $\delta\tau$ in proper time between two quantum branches, due to gravitationally-induced time dilatation. As derived below, the phase difference $\delta\phi$ responsible for the gravity-mediated entanglement, and giving rise to the effect, can be written in a particularly simple form

$$\delta\phi = \frac{m}{m_{Pl}} \frac{\delta\tau}{t_{Pl}}, \quad (1)$$

where the experiment is performed with particles of mass m , m_{Pl} is the Planck mass and t_{Pl} the Planck time. This expression shows that the time scales probed are extremely small. With current technology, the BMV effect might be detected in the lab by probing relevant entanglement (generated when $\delta\phi \sim 1$) using mesoscopic particles, with masses of the order of a millionth of a Planck mass ($m \sim 10^{-6}m_P \sim 10^{-14}kg$) [1]. The corresponding time dilation is of the order of a million Planck times, $\delta\tau \sim 10^6 t_P \sim 10^{-38}s$. This is about twenty orders of magnitude above current capabilities of direct time measurements with atomic clocks [15].

Now, it is often pointed out in quantum gravity research that the Planck time t_{Pl} could be a minimal observable time; this follows from relativity plus the fact that many approaches to quantum gravity predict a minimal length [16]. In loop quantum gravity for instance, there is indirect evidence of discretization of time coming from loop quantum cosmology [17, 18] and other arguments [19, 20]. The simplest possibility is to assume that a measurement of a time lapse can only yield multiples of the Planck time. If this holds for the time difference $\delta\tau$, namely if $\delta\tau = n t_{Pl}$, with integer n , then

$$\delta\phi = n \frac{m}{m_{Pl}}. \quad (2)$$

That is, a discontinuity in $\delta\tau$ could be detected as a discontinuity in $\delta\phi$. As discussed below, such a discretization of the phase could be detected by the Bell-like correlations among the particles' spins, which would acquire a characteristic quantum band structure.

The extremely small time intervals probed by the current proposal to implement the BMV experiment are still too large to see time discreteness. But if the experiment can be pushed to work with more massive particles, further approaching the Planck mass, $\delta\tau$ will approach the Planck time [see (1)]. While the Planck time t_P is at the—so far—deeply inaccessible scale $t_P \sim 10^{-44}s$, the Planck mass is an easily accessible scale (\sim micrograms). Thus, by directly manipulating quantum superpositions of Planck mass particles, interference as a result of

gravitational attraction we can indirectly probe time at the Planck scale. This is the key theoretical observation of this paper.

The analysis that follows is rough and the effect might be questioned by a more detailed investigation. It may turn out that the BMV apparatus does not measure eigenvalues but rather expectation values, or, that the scale of discreteness for differences in duration is actually smaller than Planckian. Nevertheless, a prospect of experimental access to the scale of the Planck time is so interesting to deserve full attention.

2. THE BMV EXPERIMENT

Let us start by describing the version of the BMV experiment of Bose et al. [1] in relativistic language, as in Christodoulou et al. [10]. Two mesoscopic particles (a and b) of mass m and embedded [21] spin $\frac{1}{2}$ are quantum split (say with a Stern-Gerlach-like apparatus) and each is set in a superposition of two distinct states, say with spins $+$ and $-$ in some basis, with different positions in space. This gives rise to four different branches, which we denote $|++\rangle, |+-\rangle, |-+\rangle,$ and $|--\rangle$ and a tensor state

$$\begin{aligned} |\psi\rangle &= \frac{|+\rangle_a + |-\rangle_a}{\sqrt{2}} \otimes \frac{|+\rangle_b + |-\rangle_b}{\sqrt{2}} \\ &= \frac{|++\rangle + |+-\rangle + |-+\rangle + |--\rangle}{2}. \end{aligned} \quad (3)$$

After a time t the two components of each particle are recombined. The relative positions of the particles differ in the distinct branches during the time t , giving rise to different gravitational fields, namely different spacetime geometries. Therefore, during the interval t the quantum state of the geometry is in a superposition of four (semiclassical) spacetimes, each corresponding to a classical metric. In particular, the proper time τ along the worldline of one particle is affected by the presence of the other by relativistic time dilation. This effect is obviously very small, but, as we shall see, it may be picked up by interference.

For simplicity, consider the case in which the two particles are kept at a small distance d only in a single branch, say $|--\rangle$, while in the other three branches the time dilation is negligible. According to general relativity, the gravitational time dilation is [10]

$$\delta\tau = \frac{Gm}{dc^2} t. \quad (4)$$

where G is the Newton constant and c the speed of light. The phase of the quantum state of a particle of mass m evolves in time as $e^{i\phi} = e^{imc^2\tau/\hbar}$. Therefore, after a (laboratory frame) time t the $|--\rangle$ branch picks up a phase difference

$$\delta\phi = \frac{mc^2}{\hbar} \delta\tau \quad (5)$$

with respect to the other branches. This equation is equivalent to Equation (1).

After the time t the state of the two particles has become

$$|\psi\rangle = \frac{|++\rangle + |+-\rangle + |-+\rangle + e^{i\delta\phi} |--\rangle}{2}. \tag{6}$$

This is an entangled state. The amount of entanglement is measured by the entanglement entropy

$$I = \text{Tr}[\rho \ln \rho] \tag{7}$$

where

$$\rho = \text{Tr}_b |\psi\rangle \langle\psi| \tag{8}$$

the trace being on the spin states of one of the two particles. A quick calculation gives

$$\begin{aligned} \rho = & \frac{1}{2} \left(|+\rangle \langle +| + |-\rangle \langle -| \right) \\ & + \frac{e^{-i\delta\phi} + 1}{4} |+\rangle \langle -| + \frac{e^{i\delta\phi} + 1}{4} |-\rangle \langle +|. \end{aligned} \tag{9}$$

This is correctly a hermitian matrix of unit trace. To compute the entropy we need to diagonalize ρ . A straightforward calculation gives the eigenvalues

$$\rho_{\pm} = \frac{1}{2} \pm \frac{\sqrt{1 + \cos \delta\phi}}{2\sqrt{2}} \tag{10}$$

When $\delta\phi = 0$, the eigenvalues are $\rho_+ = 1$ and $\rho_- = 0$, thus giving vanishing entanglement entropy, i.e., there is no interference in the output. When $\delta\phi = \pi$, we have $\rho_+ = 1/2$ and $\rho_- = 1/2$; the state is maximally entangled and $I = \log 2$, i.e., we observe the BMV effect. For a general $\delta\phi$, the entanglement entropy is

$$\begin{aligned} I = & -\rho_+ \ln \rho_+ - \rho_- \ln \rho_- \\ = & -\left(\frac{1}{2} + \frac{\sqrt{1 + \cos \delta\phi}}{2\sqrt{2}}\right) \ln \left(\frac{1}{2} + \frac{\sqrt{1 + \cos \delta\phi}}{2\sqrt{2}}\right) \\ & -\left(\frac{1}{2} - \frac{\sqrt{1 + \cos \delta\phi}}{2\sqrt{2}}\right) \ln \left(\frac{1}{2} - \frac{\sqrt{1 + \cos \delta\phi}}{2\sqrt{2}}\right). \end{aligned} \tag{11}$$

See **Figure 1**. In the lab, for a given mass m and distance d , $\delta\phi$ can be controlled by modulating t via

$$\delta\phi = \frac{Gm^2}{d\hbar} t. \tag{12}$$

that follows from (4) and (5). The entanglement entropy can be measured by repeated spin measurements on the recombined particles. A specific method would be the following: for a given t , and thus for a given $\delta\phi$ through (12), one of the particles is discarded and state tomography is performed on the second particle. This would give a density matrix ρ' of the form of Equation (9), where the cross terms would be some real numbers. Diagonalizing this matrix, an entanglement entropy I' can be computed. Assuming all noise has been accounted for, I' can be

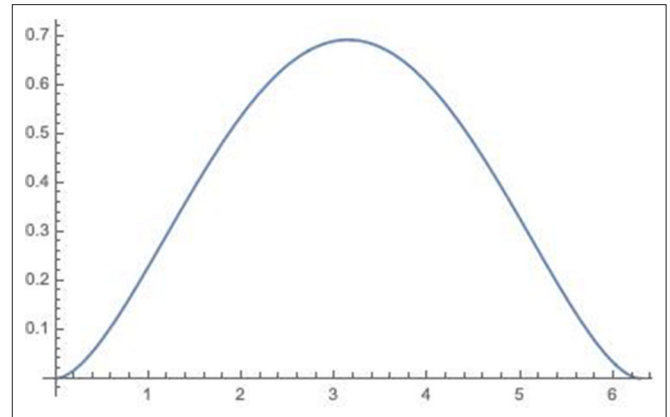


FIGURE 1 | The entanglement entropy for $\delta\phi \in \{0, 2\pi\}$.

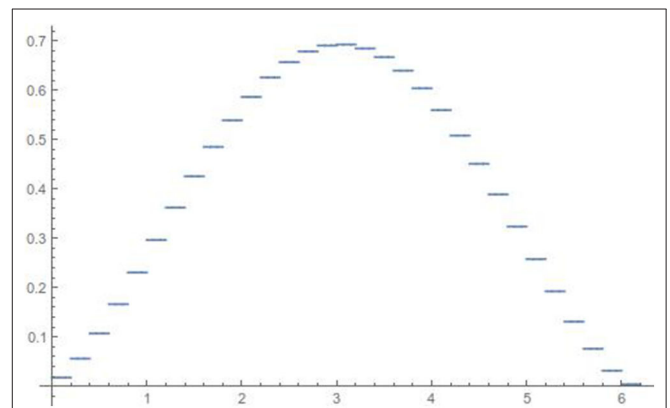


FIGURE 2 | The entanglement entropy for $\delta\phi \in \{0, 2\pi\}$ under the assumption that $\delta t/t_P \in \mathbb{N}^+$, for particles with mass one fifth of the Planck mass.

plotted against $\delta\phi(t)$ and compared with I as given by (11) and (12). Any deviation of I' from I could be a signal of a quantum gravity effect, and in particular the presence of plateaus in I' would be a signal of time discreteness.

Consider now the hypothesis that time is discrete at the Planck scale. We consider here the simplest possible ansatz: that

$$\delta\tau = n t_P \tag{13}$$

with a non negative integer n . Writing $m = \alpha m_P$ with α a dimensionless positive real parameter, we have that the only values of ϕ that are actually realized are

$$\delta\phi = \alpha n, \tag{14}$$

that is, the phase ends up taking only discrete quantized values, when t is varied continuously. It follows that the entropy is not anymore given by a continuous curve as in **Figure 1**, but has characteristic quantum steps. As long as $\alpha \ll 1$ the steps are too fine to be resolved, but if α approaches unit the steps become visible, as in **Figure 2**, where $\alpha = .2$.

For particles with masses larger than the Planck mass interference is likely to disappear altogether, as is common in interference experiments when the wave frequency is much higher than the relevant scale of the apparatus. In this case wave theory goes to the Eikonal approximation. Wave mechanics goes to classical mechanics. The Compton frequency

$$\nu_c = \frac{mc^2}{\hbar} = \frac{m}{m_{Pl}} \frac{\nu_P}{2\pi} \quad (15)$$

of objects with mass larger than the Planck mass is formally larger than the Planck frequency $\nu_{Pl} = \frac{2\pi}{t_{Pl}}$ and probably meaningless.

Notice that in this case an apparatus capable of detecting $\delta\phi \sim 1$ is going to be affected by genuine dynamical effects since we can also write

$$\delta\phi = \frac{m^2}{m_{Pl}^2} \frac{ct}{d} \quad (16)$$

and if the left hand side and the first fraction are of order unit, so must be the second, with the consequence that the duration t of the interaction must be of the same order than the light travel time d/c between the particles. This would take us outside the static approximation used in the analysis (see also [22]).

3. DISCUSSION

The current hope is to realize the BMV experiment in the lab with masses $m \sim 10^{-6}m_P$ in the next few years [1]. Our key observation is that with masses at this scale, the BMV experiment is testing time differences of the order of $\delta\tau \sim 10^{-38}s \sim 10^6 t_{Pl}$. This is already an extraordinarily small time. For comparison, the most accurate direct measurements of time at our disposal make use of the frequencies corresponding to energy differences in atomic states, atomic clocks, with an accuracy corresponding at best to a period of the order $\sim 10^{-19}s$ [15]. It is this extraordinary sensitivity to small time intervals in the BMV interference that makes this experiment so interesting.

A relativistic language is not needed to derive the correlations that the BMV experiment is expected to detect. In the non-relativistic language no small time intervals are in play: instead of $\delta\phi = mc^2\delta\tau/\hbar$, the phase reads $\delta\phi = t\delta E/\hbar$, and the c^2 makes all the difference, where the relevant time t at play is that of the laboratory frame.

But, if time discreteness is detected, the non-relativistic language becomes insufficient to describe the relevant physics. Time discreteness, according to current tentative theories, is a genuine relativistic effect arising from quantum gravity. On the other hand, this study does not go beyond the observation that the scales probed are possibly close to the relevant scale for such (naïve) models. Here we do not justify or discuss in depth a possible discretization of time and its implications. The effect discussed here however is a relativistic effect, and we do not

think it could be relevant for systems in Newtonian gravity. In contrast for instance to Muller et al. [23], here the relativistic interpretation is used to discuss signatures of possible new physics associated with the discretization of time at the Planck-scale. These effects, if real, require the relativistic interpretation to be described. For completeness, although we are not aware of any such indication, let it be noted that as this is a yet unexplored time regime, there remains the logical possibility that there is time discreteness in this regime independently from quantum gravity.

As mentioned in the introduction, the analysis given here assumes the discreteness of $\delta\tau$ in Planck time multiples. It is possible, but it is not certain that this is implied by quantum gravity. Two reasons that could question this assumption are the following. First, the spectrum of τ could be less trivial and, as a consequence, *differences* of proper time could be much smaller. For instance, if the spacing between eigenvalues decreases when the eigenvalues are large, their differences may become small. Second, a more careful analysis might show that the interference depends on averages, or expectation values of time durations, and these may be continuous even if direct duration measurements are quantized. This issue in particular requires a more detailed quantum treatment of the phenomenon that will be developed elsewhere.

Even with these caveats, the possibility that quantum interference effects could depend on time differences of the order of Planck time, a scale so far considered totally out of reach, definitely deserves attention.

DATA AVAILABILITY STATEMENT

All datasets generated for this study are included in the article/supplementary material.

AUTHOR CONTRIBUTIONS

All authors listed have made a substantial, direct and intellectual contribution to the work, and approved it for publication.

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