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# Effects of indium segregation and strain on near-infrared optical absorption in InGaN/GaN quantum wells

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In this study, we present a novel numerical model that incorporates the effects of spontaneous and piezoelectric polarization-induced electric fields, along with multiple intersubband transitions, to investigate the optical absorption characteristics of InGaN/GaN strained single and double quantum well's structures. Focusing on the role of Indium surface segregation (ISS) in polar QW structures, we examine its influence on intersubband transition-related optical absorption and the resulting spectral behavior. Specific structural configurations are designed to achieve four-energy-level with single and double quantum wells, optimized for three-color absorption within the near-infrared range. Our findings reveal that the combined impact of ISS and strain induces a notable red shift in the absorption spectra, with shifts varying significantly across different intersubband transitions. These findings underscore the potential of strained InGaN-based semiconductor compounds for developing advanced multi-color photonic devices, including near-infrared photodetectors and lasers, by harnessing their tunable optical properties.

## KEYWORDS

ingan, double quantum wells, strained quantum well, segregation, thin film, multilayers

## 1 Introduction

Due to a wide range of current and potential applications in the military, industrial, and scientific fields, infrared (IR) photodetectors are an intriguing subject. Aside from standard silicon material, innovative materials such as (In,Ga) N ternary could be a viable choice for further reimbursements, notwithstanding that manufacturing technology remains a complex and expensive solution.  $In_xGa_{1-x}N$  alloys have recently emerged as attractive materials due to their controllable band gap energies, physical and chemical stabilities, and superior photovoltaic properties (Walukiewicz et al., 2006; Lin et al., 2012; Matioli et al., 2011; Farrell et al., 2011; Wu et al., 2003; Selmi and Belghouthi, 2017; Polyakov et al., 2013; Laxmi et al., 2019; Lourassi and Soudini, 2016). Also, because of the large conduction band offset at  $In_xGa_{1-x}N/GaN$  hetero-interfaces, the large electron effective mass and the

significant longitudinal optic-phonon energy, in GaN, intersubband transitions (ISBTs) in  $In_xGa_{1-x}N/GaN$  quantum wells (QWs) are advantageous over other III-V semiconductor ones. Furthermore, ISBTs in semiconductor quantum wells and their related optical absorption have piqued the interest of researchers in recent years due to their potential applications in ultrafast optoelectronic components such as all-optical switches for optical networking systems, near-infrared photodetectors, and quantum cascade lasers (Gmachl et al., 2001; Mayrock et al., 2000; Tchernycheva et al., 2006; Zhou et al., 2003; Kumtornkittikul et al., 2007; Nevou et al., 2006). The influence of Indium surface segregation (ISS) on the optical characteristics has been intensively studied according to the substrate temperature and ratio of III/V components fluxes, which strongly impacts the segregation lengths. Nevertheless, to our knowledge, there is a noteworthy deficiency in information about how the ISS can affect optical characteristics such as absorption and refractive index. Choubani et al. (Choubani et al., 2022) studied the indium segregation and In/Ga combining effects in lens-shaped  $In_xGa_{1-x}As/GaAs$  quantum dots related to their wetting layer theoretically based on Muraki's theory. On the other hand, the radial and vertical indium distributions caused by the In/Ga intermixing effect in the quantum dot were considered, assuming a three-dimensional Gaussian distribution. Souaf et al. (2015) theoretically examined the effect of In-Ga inter-diffusion on QW emission energy for various indium segregation coefficients. They discovered that raising the segregation coefficient reduced the emission energy shift in single strained asymmetric  $In_xGa_{1-x}As/GaAs$  QWs. Moreover, Senichev et al. (2018) report the effects of growth parameters on indium segregation in metal-polar (In, Al)N alloys formed by plasma-assisted molecular beam epitaxy (PAMBE) with the technologically relevant indium mole fraction of 0.17, which is lattice-matched to GaN. Also, Rossow et al. (2017) use *in situ* reflection measurements to investigate the integration of Indium into group-III nitride layers under pulsed and continuous growth circumstances. The results reveal that segregated Indium on the surface and in the environment also contribute to the indium incorporation process, likely also via the adlayer. Furthermore, Wang et al. (2023) report the study of the migration process of Indium atoms and its impact on the QW luminescence properties. It is revealed that the material and optical quality of high-in-content InGaN QWs can be improved by improving the Indium migration capacity via low-pressure growth. Also, when the growth process is in the surface-reaction-controlled mode, the experimental results indicate that the Indium incorporation into InGaN QWs drops while the luminescence property increases as the growth pressure decreases. In addition, the growth conditions impact on indium segregation in metal-polar  $In_{0.17}Al_{0.83}N$  lattice-matched to GaN grown by plasma-assisted molecular beam epitaxy over a wide range of temperatures and active nitrogen fluxes been investigated recently by Senichev et al. (2018). The authors reported that studied growth conditions, including those cited in the literature as conducive to homogeneous InAlN, are not single-handedly enough to eliminate the 'honeycomb' indium segregation in InAlN. Their samples' 'honeycomb' structure is associated with delayed indium adlayer formation.

Despite the extensive research on intersubband transitions (ISBTs) in InGaN/GaN quantum wells, a significant research gap

remains in understanding how Indium Surface Segregation (ISS) impacts the optical characteristics, such as absorption and refractive index, especially within the near-infrared (NIR) spectrum. Most studies have focused on the influence of ISS in terms of material growth parameters or structural properties. Yet, there is limited information on how ISS interacts with strain-induced effects and the built-in electric fields (spontaneous and piezoelectric polarizations) to shape ISBT-related absorption spectra. Addressing this gap, our work investigates the effects of Indium surface segregation on NIR optical absorption in InGaN/GaN single quantum wells (SQWs) and double quantum wells (DQWs), incorporating the combined contributions of built-in electric fields and all low-lying ISBTs. The remainder of this paper is structured as follows: the first section provides the theoretical background, a discussion of our findings in the second section, and a summary in the final section.

## 2 Theoretical background

### 2.1 Electron low-lying states

The absorption coefficient considering all low-lying states in  $GaN/In_xGa_{1-x}N/GaN$  QW and DQWs can be given *versus* the incident photon angular frequency (Lei et al., 2008):

$$\alpha(\omega) = \frac{\omega}{L} \frac{\sqrt{\mu_0}}{\sqrt{\epsilon_0 \epsilon^*}} \sum_{i < j} \frac{|M_{ij}|^2 (N_i - N_j) \hbar \Gamma_{ij}}{(E_j - E_i - \hbar\omega)^2 + (\hbar \Gamma_{ij})^2}$$

Where  $L$  is the total QW width,  $\mu_0$  is the vacuum's permeability,  $\epsilon_0$  is the vacuum permittivity,  $\epsilon^*$  is the relative dielectric constant,  $N_k$  is the 2D electron gas density in the  $k^{th}$  subband,  $E_k$  is the energy level of the  $k^{th}$  subband,  $\hbar$  is the reduced Planck constant,  $\Gamma_{ij}$  ( $= 1/\tau_{ij}$ ) is the damping parameter related to the transition from initial to final states and  $M_{ij}$  ( $= \langle \Psi_i | e z | \Psi_j \rangle$ ) is the dipole matrix element. The energy level ( $E_k$ ) and corresponding wave function ( $\Psi_k$ ) are obtained by solving numerically the Schrödinger equation given as follows:

$$-\frac{\hbar^2}{2} \frac{d}{dz} \left[ \frac{1}{m(z)} \frac{d}{dz} \right] \Psi(z) + [V(z) - eFz] \Psi(z) = E \Psi(z)$$

Where  $V(z)$  is the potential barrier given as the sum of the unstrained and strained contributions,  $e$  is the elementary charge, and  $F$  is the built-in electric field due to spontaneous and piezoelectric polarizations (For more details, see: (El Ghazi and Jorio, 2013; En-Nadir et al., 2021a; El Ghazi and John-Peter, 2015; El Ghazi and Jorio, 2014; En-nadir et al., 2022; En-nadir et al., 2021b)). III-nitride semiconductors are usually built in the Wurtzite crystallographic structure. Both the positive and negative gravity centers of the dipoles are distinct due to the poor symmetry of the crystal. Thus, a spontaneous polarization field is observed along the  $\langle 0001 \rangle$  axis. Superimposed on the spontaneous compound, a piezoelectric polarization is current in InGaN/GaN heterostructures that are linearly dependent on the strain field within the material.

As we mentioned above, our calculations have been performed using Finite Element Method (FEM). To precisely calculate the energy levels and associated wave functions, boundary conditions are imposed to maintain the continuity of current density across material interfaces considering spontaneous and piezoelectric

polarizations. These conditions ensure that both the wave function and its derivative are continuous at the interfaces between distinct regions, thus preserving physical integrity within the quantum well structure. This is represented by the following expression:

$$\left[ \vec{\nabla} \cdot \vec{\nabla} \left( \frac{\psi(z)}{m_{\text{GaN}}^{*(e)}} \right) \right]_{\text{barrier}} = \left[ \vec{\nabla} \cdot \vec{\nabla} \left( \frac{\psi(z)}{m_{\text{InGaN}}^{*(e)}} \right) \right]_{\text{well}}$$

As we mentioned above, the system under study uses a mesh grid of  $3N + 1$  points for single QW, while we used  $5N + 1$  for double QW structure, with each layer discretized by distinct step sizes. For the barriers, the step size is defined as  $h_{\text{GaN}} = L/N$ , while for the well region, it is given by  $h_{\text{InGaN}} = l/N$ . Here,  $L$  and  $l$  represent the thicknesses of the barriers (i.e., GaN) and wells (i.e., InGaN), respectively. The first and second derivatives of the wave functions at each node are calculated as follows:

$$\left( \frac{\partial^2 \psi(z)}{\partial z^2} \right)_{z_n} = \frac{\psi_{n+1} - 2\psi_n + \psi_{n-1}}{(z_{n+1} - z_n)^2}$$

$$\left( \frac{\partial \psi(z)}{\partial z} \right)_{z_n} = \frac{\psi_{n+1} - \psi_n}{z_{n+1} - z_n}$$

We suppose that,  $h_{\text{GaN}} = z_{n+1} - z_n$ , then we will have the following expression:

$$\left( \frac{-\hbar^2}{2m_e^*} \right) \left[ \frac{\psi_{n-1} - 2\psi_n + \psi_{n+1}}{(h_{\text{GaN}})^2} \right] + V(z) \psi_n = E \psi_n$$

Solving these analytical equations produces a matrix representation of the problem. We utilized Python with libraries such as NumPy, SciPy, Math, Matplotlib, and other supportive packages to compute numerical solutions for these matrices. Through these methods, combined with the indium distribution model outlined below, this study accurately captures the effects of indium segregation on the optical properties of quantum well structures, providing valuable insights into the roles of strain and polarization in optoelectronic applications.

## 2.2 Indium distribution

The molecular beam hetero-epitaxy (MBE) technique of  $\text{In}_x\text{Ga}_{1-x}\text{N}$  material on the GaN layer is characterized by excessive indium segregation along the growth direction (001). The high indium mobility in the floating layer causes this. Furthermore, due to the miscibility difference between GaN and InGaN, the Indium (In) atoms segregate (float) onto the upper monolayer during the capping process. According to the literature, the GaN layer is not pure, and indium segregation results in complicated Indium content profiles that have received little attention. Muraki et al. (1992) developed a phenomenological framework based on PL and Secondary Ion Mass Spectroscopy (SIMS) data in 1992 to characterize this phenomenon. During the formation of  $\text{In}_x\text{Ga}_{1-x}\text{N}$  on GaN, In atoms on the top of the last epitaxial monolayer separate to the surface of the next layer with a coefficient  $R$  known as the segregation coefficient. As a result, the indium content of each monolayer (ML) of  $\text{In}_x\text{Ga}_{1-x}\text{N}$  grows until it achieves the nominal value provided by In and Ga cells. This nominal value is obtained after several MLs of  $\text{In}_x\text{Ga}_{1-x}\text{N}$  are

deposited on top of a GaN layer. When the active layer is no longer growing and the capping layer (GaN) is deposited, the leftover proportion  $(1-R)$  of Indium atoms is integrated into the bulk material to produce an  $\text{In}_x\text{Ga}_{1-x}\text{N}$  alloy, the In content diminishes until pure GaN is grown. So, according to Muraki's model, Muraki et al. (1992), gives the In concentration in the  $n$ th ML as follows:

$$x(\text{In}) = \begin{cases} 0 & \text{for GaN} \\ x_0(1 - R^n) & \text{for } 1 \leq n \leq N \\ x_0(1 - R^n)R^{n-N} & \text{for } n > N \end{cases}$$

Where  $R$  is a typical value for the growth conditions of such nanostructures.

Modeling and parameterizing the indium profile in the structure with surface segregation impacts can be accomplished in various ways. Several researchers use the Gaussian distribution to calculate the potential profile approximation for QWs with impacts on surface segregation. In this case, the width of the Gaussian function is a fitting parameter that can be determined using experimental data or theory treatment. This approach yields a symmetrical indium distribution function. Nevertheless, TEM observations of QW structures demonstrate that surface segregation makes the indium distribution profile asymmetrical. As a result, a more exacerbated and accurate description of surface segregation that uses kinetic equations (Stanley et al., 2003) is required. Recently, Khazanova et al. (2024) investigated the effects of strain and compositional distribution on the optical characteristics of GaAs/InGaAlAs/GaAs double asymmetric tunnel-coupled quantum wells. Their comprehensive approach combines structural, optical, and theoretical analyses, revealing that the technique reduces the deviation between experimental and simulated photoluminescence (PL) spectra to 10%. The study highlights the sensitivity of PL peaks to quantum well profiles and shows that elastic strain and compositional segregation can shift PL peak energies by approximately 50 meV. The strong agreement between the theoretical model and experimental data supports the validity of their findings in evaluating the optical performance of quantum well structures. Maidaniuk et al. (2021) introduce a nondestructive method for investigating indium segregation in ultra-thin In(Ga) As/GaAs nanostructures using photoluminescence (PL) spectroscopy and effective bandgap simulations. They find a strong correlation between this method's indium segregation coefficient and scanning transmission electron microscopy (STEM) results. Karpov (2017) introduces a unified semi-empirical model that effectively captures the radiative and Auger recombination constants in bulk InGaN, integrating the impact of hole localization resulting from composition fluctuations, and successfully aligns with experimental data on the dependence of these constants on emission wavelength, thereby validating its applicability to InGaN behavior. Moreover, Auf der Maur et al. (2016) investigate the efficiency of III-nitride InGaN/GaN quantum well-based white light emitting diodes (LEDs). Their study employs atomistic simulations to demonstrate that a significant portion of the "green gap"—a systematic drop in efficiency within the green-yellow spectrum—can be attributed to a reduction in the radiative recombination coefficient as indium content increases, driven by random fluctuations in indium concentration present in InGaN

alloys. O'Donovan et al. (2024) investigate efficiency limitations in (In,Ga)N-based light emitting diodes (LEDs) due to uneven hole distribution in the (In,Ga) N/GaN multiquantum well stack. The study reveals that random alloy fluctuations significantly impact carrier distribution by employing an atomistic tight-binding model combined with a quantum corrected drift-diffusion model. Their findings indicate that while the electron blocking layer is less critical, incorporating quantum corrections and random fluctuations is essential for accurately representing experimentally observed light emission patterns, challenging the conventional virtual-crystal approximation. Hence, the solution of the coupled kinetic equations leads us to parameterize the indium distribution profile in the structure. In this trend, to quantify the influence of the ISS on optical absorption, the error function is adopted as follows [(Stanley et al., 2003; Khazanova et al., 2024)]:

$$x(z) = \begin{cases} 0 & \text{for } 0 < z \leq L \\ x_0 \operatorname{erf}\left(\frac{z-L}{L_1}\right) & \text{for } L < z \leq L+l \\ x_0 \operatorname{erf}\left(\frac{l}{L_1}\right) \left[1 - \operatorname{erf}\left(\frac{z-L-l}{L_2}\right)\right] & \text{for } L+l < z \leq l+2L \end{cases}$$

Where  $z$  is the growth-axis coordinate,  $x_0$  is the nominal Indium content in the QW,  $L$ , and  $l$  are the first and the second layer thicknesses, respectively,  $L_1$  and  $L_2$  the segregation lengths correspond to the first and second InGaN/GaN interfaces. Such asymmetric Indium distribution leads to better conformity results when compared to a symmetric one (Gaussian profile). Notice that generally,  $L_1$  and  $L_2$  are not the same. Based on the kinetic theory of MBE growth, Stanley et al. (2003) show that segregation lengths depend strongly on the substrate temperature and III/V component fluxes. In particular, they reported that the segregation lengths are Indium flux-independent for high substrate temperatures. Henceforward, we restrict ourselves to this case and consider them equals for both interfaces. Compared to Muraki and FukatsuIto (1992). Dussainge et al. (2003), this formula approximates the indium distribution with high accuracy. With two adjusting parameters instead of one for the Gaussian profile, more freedom to provide accurate fitting is done. In the  $\text{In}_x\text{Ga}_{1-x}\text{N}/\text{GaN}$  heterostructures, the Indium spreading control potential profiles of the band edges. A substantial indium quantity leads to a massive mismatch of the lattice constants in semiconductor layers. Piezoelectric effects originate from severe strain caused by lattice mismatch. This paper uses nonlinear relations for ternary alloys found in El Ghazi and Jorio (2013). to calculate the piezoelectric polarization. As a result of doping, the space charge of the depletion layers and spontaneous and piezoelectric charges merge to form the internal electrostatic field that results in the quantum well.

### 3 Results and discussions

Through this paper, the proposed structure under investigation considers nitride single quantum well (SQW) and double QW (DQWs) with layers made of GaN and InGaN. Except for the band gap energy and spontaneous polarization obtained by the second-order interpolation formula with the bowing parameter, all

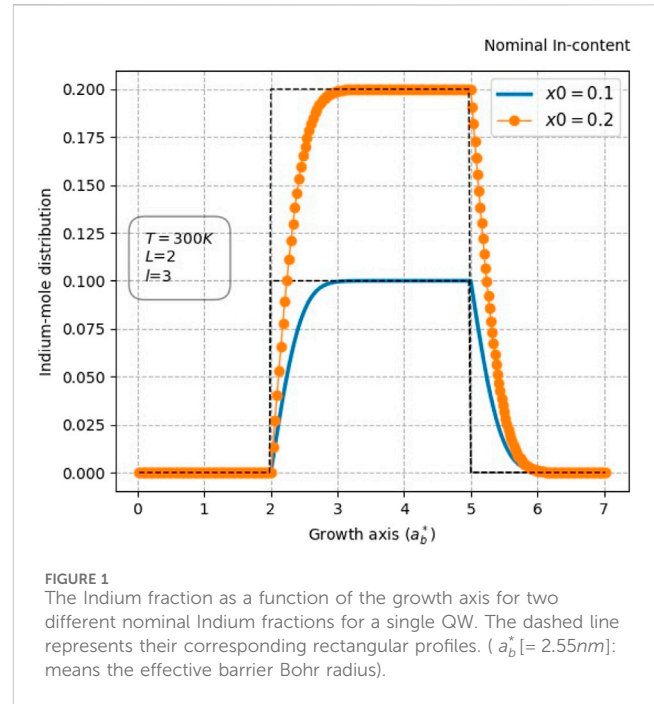


FIGURE 1 The Indium fraction as a function of the growth axis for two different nominal Indium fractions for a single QW. The dashed line represents their corresponding rectangular profiles. ( $a_b^0$  [= 2.55nm]: means the effective barrier Bohr radius).

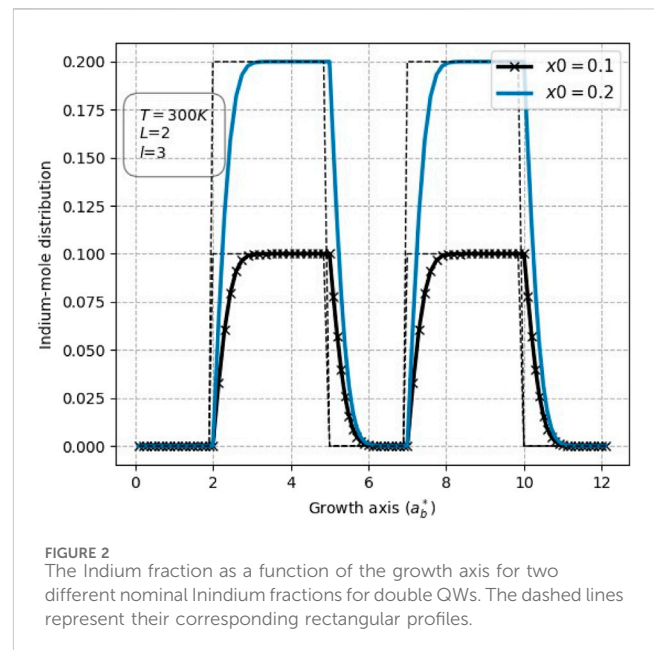
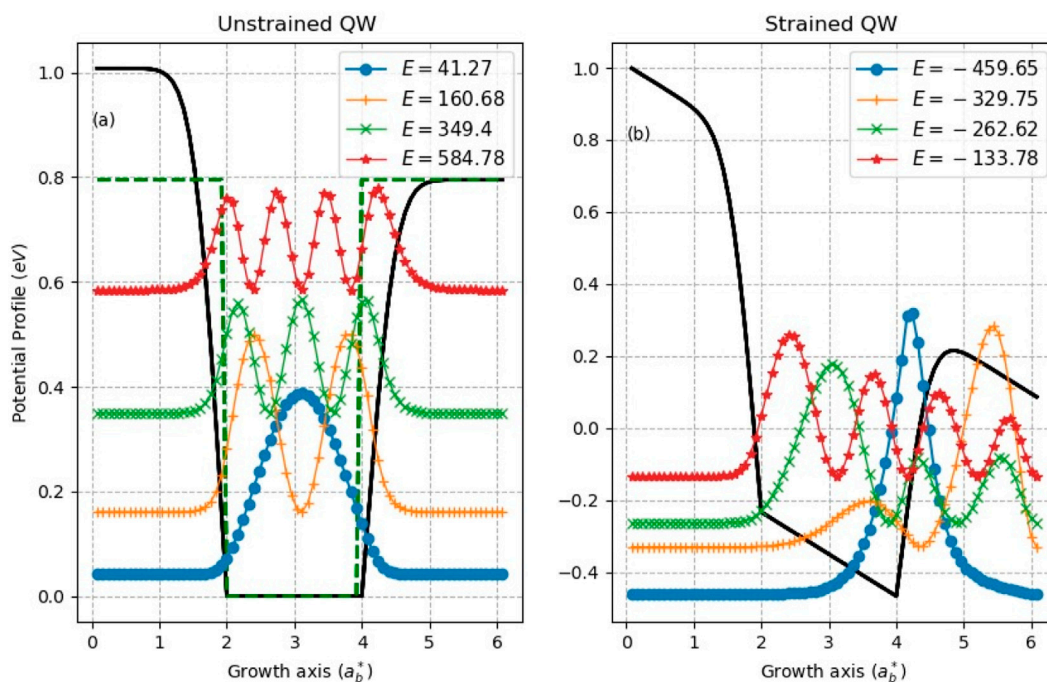


FIGURE 2 The Indium fraction as a function of the growth axis for two different nominal Indium fractions for double QWs. The dashed lines represent their corresponding rectangular profiles.

ternary parameters materials were given via linear interpolation formulas. Strong internal electric fields caused by spontaneous and piezoelectric polarization influences are a well-known feature of the wurtzite crystal heterostructure. We have utilized the same parameters as in Refs for relevant binary materials. (El Ghazi and Jorio, 2013; En-Nadir et al., 2021a; El Ghazi and John-Peter, 2015; El Ghazi and Jorio, 2014; En-nadir et al., 2022; En-nadir et al., 2021b). The segregation of distinct atomic types on the surface throughout growth is a particularly noticeable result. It is widely acknowledged that Indium atoms segregate on the surface during the growth of InGaN on GaN, resulting in their prolonged inclusion in the crystal.

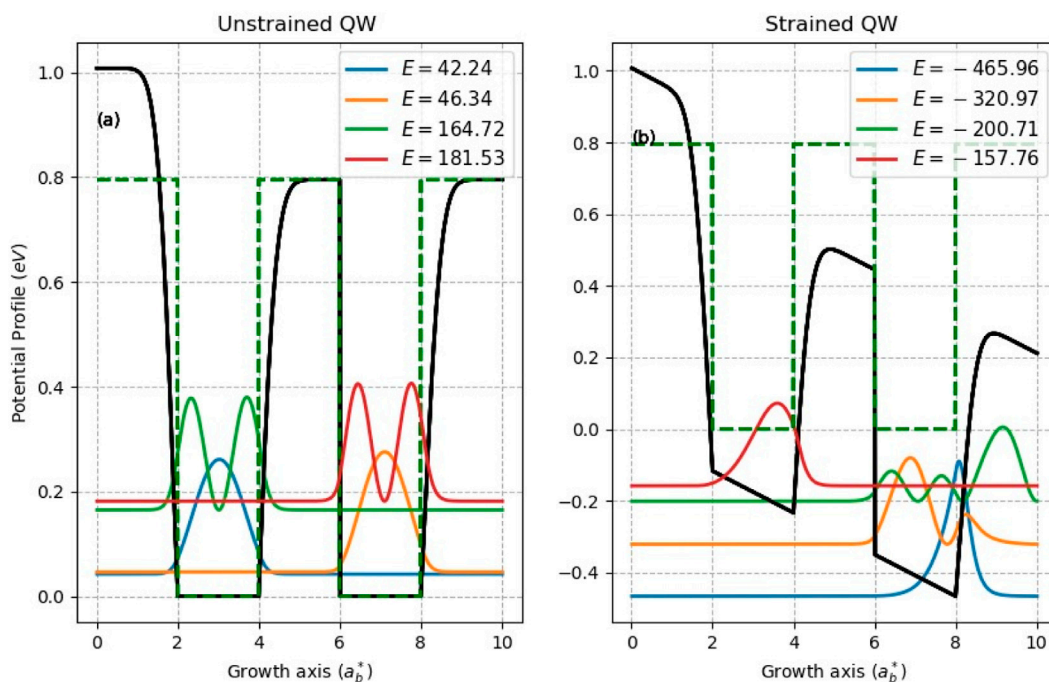


**FIGURE 3** The band structure of strained and unstrained QW, probability densities, and their corresponding eigenvalues for four low-lying states under the effects of ISS for nominal In-content of 20% and  $L = l = 2$  at room temperature. Energy levels and corresponding eigenvectors (density of states) for the quantum well system, with energy given in meV. Each color indicates a specific energy level: the ground state is shown in blue, the first excited state is in yellow, the second excited state is in green, and the fourth excited state is in brown. (A) Show the probability densities of unstrained QW while. (B) Show the probability densities of strained QW.

As a result, their composition profile increases gradually at the InGa<sub>N</sub> on the Ga<sub>N</sub> interface. Because the inclusion of segregating Indium atoms remained on the surface during cap layer growth is postponed owing to the surplus In atoms on the growth surface, the chemical profile is also graded at the Ga<sub>N</sub> on InGa<sub>N</sub> interface. Figures 1, 2 illustrate the results of the asymmetrical Indium distribution according to the growth axis for two nominal In-fractions. Single and double QW structures with different nominal in-contents are reported, showing that the ISS impact on the band structure is more pronounced for high values than for small ones.

Figure 3 elucidates the alteration of the conduction band profile under the influence of ISS in both strained and unstrained quantum wells, with a nominal indium content of 20% and a well width of  $L = l = 2a_b^*$  at room temperature. The reference dashed line illustrates a rectangular conduction band profile without the contributions from strain or ISS. In Panel (a), the analysis of the unstrained QW reveals that the incorporation of ISS impacts the structural profile significantly. The ISS modifies the potential relief of the band edges, leading to an asymmetric configuration within the QW. This asymmetry is particularly critical as it alters the confinement potentials experienced by charge carriers, which can subsequently affect their dynamic behavior and transport properties. The probability density distributions of the eigenstates demonstrate distinct characteristics: for the unstrained QW, the subband electron probability densities are predominantly localized within the quantum well, which is indicative of strong quantum confinement.

Conversely, in Panel (b), the behavior of the strained QW under ISS shows a noteworthy shift in the electron probability densities, particularly for the 1S and 2S subbands, where resonance tunneling facilitates the migration of electron densities towards the right barrier. This shift can be interpreted as a consequence of altered energy landscapes resulting from strain, which can enhance tunneling phenomena and affect carrier lifetimes and relaxation dynamics. The observed energy level modifications underscore the profound influence of strain on electronic transitions. Specifically, the 1S-2S intersubband transition (ISBT) energy experiences a notable increase from 120.5 meV to 145.8 meV, signifying a blue shift of approximately 25.3 meV. This blue shift can be attributed to enhanced confinement effects in the strained QW, which make higher energy states more accessible, thereby improving the efficiency of devices such as quantum cascade lasers and detectors. In stark contrast, the 2P-3S ISBT demonstrates a red shift of about 108.6 meV, suggesting that higher subband states in strained QWs may become less energetically favorable for transitions due to strain-induced modifications in the band structure. The findings on the effects of Intersubband Indium Segregation (ISS) and strain in quantum wells (QWs) demonstrate that tailored strain engineering can significantly modify semiconductor materials' electronic properties and transition dynamics. The observed blue-shifts in intersubband transition energies under strain indicate enhanced quantum confinement, which may improve efficiency in optoelectronic devices such as quantum cascade lasers and photodetectors. Conversely, the red shifts of higher energy transitions suggest the

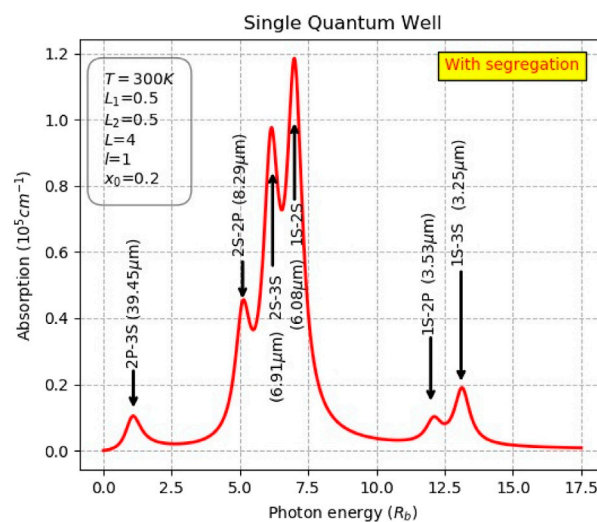


**FIGURE 4** The band structure of strained and unstrained double QWs, probability densities, and their corresponding eigenvalues for four low-lying states under the effects of ISS for nominal In-content of 20% and  $L = l = 2$  at room temperature. Energy levels and corresponding eigenvectors (density of states) for the quantum well system, with energy given in meV. Each color indicates a specific energy level: the ground state is shown in blue, the first excited state in yellow, the second excited state in green, and the fourth excited state in brown. (A) Show the probability densities of unstrained QW while. (B) Show the probability densities of strained QW.

potential for selective control over electronic states, paving the way for developing advanced materials that exploit strain-induced effects to optimize performance in high-speed electronic and photonic applications.

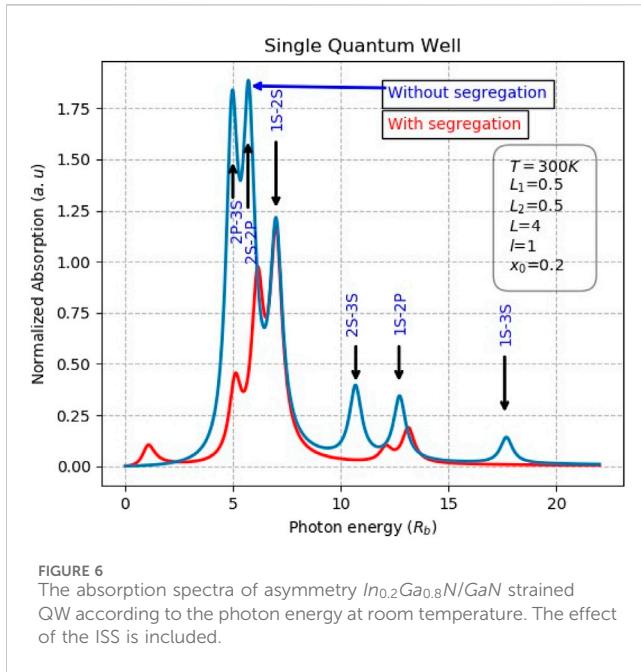
For nominal In-content of 20% and  $L = l = 2$  at room temperature, Figure 4 shows the alterations of the schematic conduction band configuration under the influence of ISS for strained and unstrained QW. It is unambiguous that the ISS effects on the configuration shapes influence the alleviation of band edges, yielding an asymmetric structure for double QWs. Also, it is evident that for strained DQWs, the three first states are moved to the right QW while the last state is displaced to the left one, considering the ISS impact. Furthermore, it is noted that when strained QW is compared to unstrained QW, all energy levels decrease, showing significant redshifts.

Based on equation, the ISBT-related absorption coefficient of  $In_xGa_{1-x}N/GaN$  single and double QWs is governed principally by three parameters. The first is the electron density residing in the initial state, while the second is the energy difference between the initial and final states. The third one is the dipole matrix element representing the overlap of the wave functions between the initial and final states. Figure 5 illustrates the variation of the absorption spectrum according to the photon energy for asymmetric.  $In_{0.2}Ga_{0.8}N/GaN$  strained QW at room temperature. The oscillation pattern observed in Figure 5 is due to different low-lying ISBTs implied in the studied structure. The main obtained results corresponding to different resonant ISBT wavelengths are in the figure. For instance, the wavelengths of 1S-2S and 2S-3S ISBT are



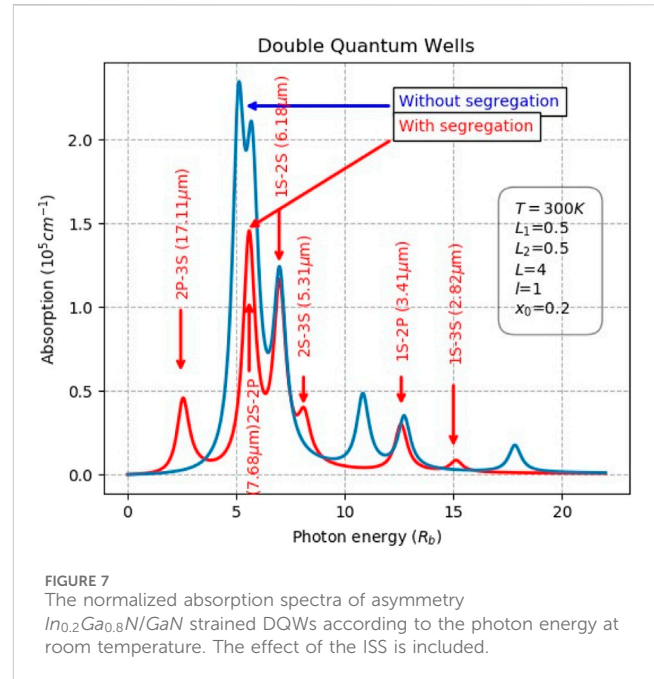
**FIGURE 5** The absorption spectra of asymmetry polar  $In_{0.2}Ga_{0.8}N/GaN$  strained SQW according to the photon energy at room temperature considering the ISS effects. ( $R_b = 29.13 meV$ ) Means the effective Rydberg energy).

located respectively at  $6.08\mu m$   $6.9\mu m$ . Since the absorption coefficients of these ISBTs are approximately comparable, the three energy levels  $In_{0.2}Ga_{0.8}N/GaN$  QW are obtained, which help construct two-color optoelectronic devices. To get more



shine on such a phenomenon, we report in Figure 6 the absorption spectra of  $In_{0.2}Ga_{0.8}N/GaN$  strained QW with and without ISS. According to Figures 5, 6, it is apparent that the ISS effects strongly influence the absorption spectra. Our results show that the absorption spectra are strongly red shifted under the ISS influences. For instance, 1S-3S ISBT is displaced to higher wavelengths from  $2.41\mu m$  to  $3.25\mu m$ , showing a red shifted of about 35%. This latter is around of 5.6%, 0.9%, 72%, 11% and 357% for 1S-2P, 1S-2S, 2S-3S, 2S-2P and 2P-3S ISBT respectively. It is noticeable that 1S-2S redshift is the smallest while 2P-3S is the greatest. This can be explained by the fact that 1S and 2S states are less sensitive to band edge deformation due to ISS effects compared to 2P and 3S ones, as shown in Figure 1. It is interesting to notice that without ISS impact, the ISBT-related absorption coefficients of 1S-2S, 2S-2P, and 2P-3S are comparable and then the four-energy-levels  $In_{0.2}Ga_{0.8}N/GaN$  QW can be obtained. These results illustrate the significant impact of the ISS on the absorption spectra of quantum wells, revealing a pronounced redshift in the intersubband transition (ISBT) energies. Specifically, the redshift of the 1S-3S ISBT from  $2.41\mu m$  to  $3.25\mu m$ , alongside substantial shifts for other transitions, indicates that ISS profoundly modifies the material's optical characteristics. The varying sensitivity of different subband states to band edge deformation due to ISS underscores the necessity for careful consideration in device design. The observed reduction in ISBT energies, particularly for transitions involving higher-energy states (2P and 3S), suggests that ISS could be utilized to tailor the optical response of optoelectronic devices, potentially enhancing performance in applications such as infrared detection and laser technologies. This research emphasizes the importance of ISS in the engineering of quantum well structures for optimized device functionality, paving the way for advancements in high-efficiency optoelectronic applications.

The variations of the absorption coefficient as a function of photon energy in asymmetric  $In_{0.2}Ga_{0.8}N/GaN$  strained quantum wells (QWs) are depicted in Figure 6, highlighting the significant



influence of nominal indium content on the optical properties of the material. As indicated, the absorption spectra are markedly dependent on the increasing nominal indium content, resulting in a pronounced amplitude drop for intersubband transitions (ISBTs). This observation suggests that higher indium concentrations lead to a more complex band structure, which alters the density of states and affects the transitions between different energy levels.

Notably, as the nominal indium content varies from 10% to 30%, the 1S-2S and 2S-2P ISBTs become undetectable as their amplitudes drop to two orders of magnitude smaller than those of other transitions. This disappearance of certain transitions under increased indium content indicates a critical threshold where the balance of potential barriers and electronic states is disrupted, leading to diminished absorption characteristics for these specific transitions. Such behavior can significantly influence optoelectronic devices' overall efficiency and performance based on these materials, as the loss of specific ISBTs could affect the spectral response of devices like photodetectors and lasers. The differential response of each ISBT to changes in nominal indium content further illustrates the complexity of the underlying physics. For instance, the energy of the 2P-3S ISBT shows a blue shift from  $4.42 Rb_{bb}$  to  $5.34 Rb_{bb}$ , representing a shift of approximately 26.8 meV (20.8%).

In contrast, the 1S-3S, 1S-2P, and 2S-3S ISBTs experience red shifts of 28%, 44.5%, and 24.6%, respectively. This contrasting behavior can be attributed to the interplay of ISS and the built-in electric field within the QW, which modifies the energy levels by altering the potential relief at the band edges. The ISS effect tends to favor stabilizing certain energy states while destabilizing others, leading to complex absorption spectra reflecting these interactions.

Further insights into the absorption spectra of double quantum wells (DQWs) are provided in Figure 7, which clearly demonstrates that the ISS phenomenon substantially impacts the ISBT-related absorption characteristics. The consistent red shifts observed for all ISBTs when accounting for ISS effects underscore the importance of

TABLE 1 The redshift of all implied ISBTs under ISS effects for SQW and DQWs.

ISBT		2P-3S	2S-2P	1S-2S	2S-3S	1S-2P	1S-3S
Redshift ( $\mu\text{m}$ )	SQW	30.39	0.76	0.02	2.94	0.16	0.84
	DQWs	8.73	0.14	0.03	1.37	0.05	0.42

including such phenomena in the analysis of quantum well systems. To elucidate the significance of these shifts, a comparative analysis with single quantum wells (SQWs) is presented in Table 1, offering a quantitative measure of manner in which Intersubband Indium Segregation (ISS) alters the spectral responses between these two structures. The findings regarding the absorption spectra of asymmetric InGaN/GaN strained quantum wells with 20% of indium compositions highlight the crucial role of nominal indium content and ISS in determining the optical characteristics of semiconductor materials. The observed amplitude drop and the shifting of ISBT energies suggest that careful engineering of indium concentration can tailor the optical response of quantum well structures, optimizing their performance in various optoelectronic applications. The implications of these results underscore the potential for designing advanced devices that leverage strain and ISS effects to achieve desired spectral properties, ultimately leading to enhanced efficiency in applications such as infrared detectors and high-performance lasers.

The results underscore the critical role of the ISS in achieving more accurate simulation data, particularly for devices that involve high-energy states. The findings suggest that incorporating ISS effects into the modeling of optoelectronic devices is essential for capturing the complexities associated with these high-level states. This is particularly relevant for quantum well structures where precise energy levels and transition probabilities significantly influence device performance. In contrast, neglecting ISS can provide a reasonable approximation for low-energy states, such as the fundamental 1S and 2S states. This discrepancy arises because the deeper states are less sensitive to the deformation of band edges caused by ISS, as illustrated in Figure 1. Moreover, the results presented in Table 1 reveal a notable distinction between single quantum wells (SQWs) and double quantum wells (DQWs) concerning the redshift of ISBT energies under ISS influences. Specifically, the ISBT redshift is more pronounced in SQWs, where the absorption spectra are shifted to lower energies compared to those observed in DQWs. This indicates that the unique confinement and structural characteristics of DQWs mitigate the extent of ISS-induced energy shifts, thereby maintaining more stable transition energies. Interestingly, despite the variations in the spectral displacement due to ISS, the ISBT-related absorption coefficients for the transitions 1S-2S, 2S-2P, and 2P-3S are found to be of comparable magnitude. This characteristic allows for the realization of four-energy-level structures in InGaN/GaN DQWs, emphasizing the potential for these systems to support complex transitions while benefiting from ISS's mitigating effects. The overall findings corroborate existing literature, although some discrepancies highlight areas for further model exploration and refinement. These insights are particularly promising for designing and optimizing future optoelectronic devices, especially those targeting multiple-color operations within the optical communication wavelength range. The implications of this research point to the potential for tailoring quantum well

structures to achieve desired optical characteristics, ultimately contributing to the advancement of high-performance devices suitable for diverse applications in telecommunications and photonics. The findings regarding the significance of the ISS in quantum wells emphasize its necessity in accurately simulating and understanding the optical properties of semiconductor devices. By recognizing the differential impact of ISS on high-energy *versus* low-energy states, researchers can better design quantum well structures that optimize performance across various applications. The pronounced redshift in ISBTs for SQWs compared to DQWs further suggests that careful structural engineering can enhance the efficacy of optoelectronic devices, particularly for multiple-color applications in optical communication. These results advocate for integrating ISS effects into future design frameworks, ultimately leading to innovations that enhance the functionality and efficiency of next-generation photonic devices. This study presents several limitations that must be acknowledged to understand the findings comprehensively. First, the analysis relies on simplified model assumptions regarding the material properties and behavior of the quantum wells, potentially overlooking complex interactions inherent in real materials. Additionally, the research was conducted at room temperature, limiting insights into how temperature variations could impact the behavior of the ISS and optical absorption.

Furthermore, focusing on a narrow range of indium concentrations (10%–30%) restricts the generalizability of the results; exploring a broader range could yield more comprehensive insights into the effects of indium content. The lack of experimental validation also poses a significant limitation, as real-world data are crucial for corroborating theoretical findings. Lastly, the study does not account for the influence of other phenomena, such as carrier scattering and external electric fields, which could further affect the optical properties. Addressing these limitations in future research will enhance the reliability and applicability of the findings, ultimately leading to improved design and optimization of optoelectronic devices based on nitride materials.

This study employs a one-dimensional (1D) model to investigate the optical transitions in InGaN/GaN quantum wells. While this approach provides key insights into the effects of indium segregation and strain on the intersubband transitions, it is inherently limited in capturing in-plane compositional fluctuations within the quantum wells. These fluctuations can significantly influence carrier energies and localization, affecting wavefunction overlap and optical properties. By accounting for these complexities, we acknowledge that a three-dimensional (3D) model would provide a more comprehensive representation of the material behavior. Implementing a 3D model would refine our understanding of the system and yield results that more closely align with experimental data. Such advancements in modeling could pave the way for improved designs of optoelectronic devices, as it would facilitate a deeper understanding of how varying indium distributions and strain conditions affect device performance.



## 4 Conclusion

This study analyzes the impact of Indium surface segregation (ISS) on optical absorption related to intersubband transitions (ISBT) in strained InGaN/GaN single quantum well (SQW) and double quantum well (DQW) structures at room temperature for  $L = 4l = 4a_b^*$  with 20% of indium concentration. The key findings are: (i) ISS significantly affects the optical absorption spectra of both SQW and DQW structures, with its interplay with strain and polarization altering absorption characteristics. (ii) Deep-related ISBTs, such as the 1S-2S transition, show lower sensitivity to ISS than higher-energy transitions like 2P-3S, indicating that band edge deformations influence lower-energy states less. (iii) The main effect of ISS is a redshift across all absorption spectra, with the 1S-2S ISBT being the least affected and the 2P-3S ISBT experiencing the most significant shift. This red-shifting has important implications for the design of optoelectronic devices. (iv) The findings suggest applications for developing three- or four-color devices in the near-infrared range. This research contributes to understanding ISS impacts on nitride materials' optical properties and is expected to inspire further investigations into enhancing solar cell tandem configurations and laser systems. This study underscores the importance of considering ISS in the modeling and design of optoelectronic devices, facilitating innovations in nitride semiconductors.

## Data availability statement

The original contributions presented in the study are included in the article/supplementary material, further inquiries can be directed to the corresponding authors.

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HE: Investigation, Software, Validation, Writing–original draft, Writing–review and editing. RE-n: Formal Analysis, Investigation, Methodology, Visualization, Writing–review and editing. MB-M: Conceptualization, Investigation, Validation, Visualization, Writing–review and editing. JI: Data curation, Investigation, Validation, Visualization, Writing–review and editing. AS: Conceptualization, Data curation, Formal Analysis, Resources, Validation, Writing–review and editing.

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## Conflict of interest

The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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