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# Triblock copolymer micelle model of spherical paraspeckles

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Paraspeckles are nuclear bodies scaffolded by RNP complexes of NEAT1\_2 RNA transcripts and multiple RNA-binding proteins. The assembly of paraspeckles is coupled with the transcription of NEAT1\_2. Paraspeckles form the core-shell structure, where the two terminal regions of NEAT1\_2 RNP complexes compose the shell of the paraspeckle and the middle regions of these complexes compose the core. We here construct a theoretical model of paraspeckles by taking into account the transcription of NEAT1\_2 in an extension of the theory of block copolymer micelles. This theory predicts that the core-shell structure of a paraspeckle is assembled by the association of the middle region of NEAT1\_2 RNP complexes due to the multivalent interactions between RBPs bound to these regions and by the relative affinity of the terminal regions of the complexes to the nucleoplasm. The latter affinity results in the effective repulsive interactions between terminal regions of the RNA complexes and limits the number of complexes composing the paraspeckle. In the wild type, the repulsive interaction between the middle and terminal block dominates the thermal fluctuation. However, the thermal fluctuation can be significant in a mutant, where a part of the terminal regions of NEAT1\_2 is deleted, and distributes the shortened terminal regions randomly between the shell and the core, consistent with our recent experiments. With the upregulated transcription, the shortened terminal regions of NEAT1\_2 in a deletion mutant is localized to the core to decrease the repulsive interaction between the terminal regions, while the structure does not change with the upregulation in the wild type. The robustness of the structure of paraspeckles in the wild type results from the polymeric nature of NEAT1\_2 complexes.

## KEYWORDS

paraspeckle, NEAT1\_2, architectural RNA, micellization, transcription

## Introduction

A cell nucleus is not a uniform solution of DNA and proteins, but there are a number of nuclear bodies in the interchromatin space (Chujo et al., 2016; Nakagawa et al., 2018; Palikyaras and Papantonis 2019; Banani et al., 2017; Berry et al., 2015; Van Treeck and Parker 2018). Some nuclear bodies are scaffolded by RNAs that make ribonucleoprotein (RNP) complexes with RNA-binding proteins (RBPs). A class of RNAs that are essential in assembling nuclear bodies are called architectural RNAs (arcRNAs) (Chujo et al., 2016). Growing number of evidences suggest that nuclear bodies are condensates assembled by liquid-liquid phase separation (LLPS) because of the multivalent interactions between the intrinsically disordered regions of RBPs that are bound to arcRNAs (Chujo et al., 2016; Nakagawa et al., 2018; Palikyaras and Papantonis 2019; Banani et al., 2017; Berry et al., 2015; Van Treeck and Parker 2018). Condensates produced by LLPS are thought to act as reaction crucibles of specific biochemical reactions, molecular sponges that sequester specific proteins and RNAs from the nucleoplasm, and hubs to organize the 3D structure of genome (Shin and Brangwynne 2017). It is of interest to study the assembly mechanism of nuclear bodies due to the possible relationship with their physiological functions.

Paraspeckles are nuclear bodies that are scaffolded by NEAT1\_2 arcRNA (Sunwoo et al., 2008; Clemson et al., 2009; Sasaki et al., 2009). Paraspeckles act as molecular sponges that sequester some types of RNA transcripts and proteins (Chen and Carmichael 2009; Hirose et al., 2014; Imamura et al., 2014; Hu et al., 2015; West et al., 2016; Nakagawa et al., 2018; Wang et al., 2018; Yap et al., 2022) and interact with chromatin regions, enriched in active promoters and enhancers (West et al., 2014; Li et al., 2017; Sridhar et al., 2017; Fang et al., 2019; Bonetti et al., 2020; Cai et al., 2020). *De novo* assembled paraspeckles are often observed at the proximity to the transcription site of NEAT1\_2 and are disassembled when the transcription of arcRNA is suppressed (Clemson et al., 2009; Sasaki et al., 2009; Mao et al., 2011). The number of paraspeckles increases when transcription of NEAT1\_2 is upregulated (Clemson et al., 2009; Hirose et al., 2014). These results imply that the assembly of paraspeckles is coupled with the transcription of NEAT1\_2. RNA-binding proteins can be bound to nascent NEAT1\_2 transcripts, which are still connected to the transcription site *via* RNA polymerase II (Pol II). The array of nascent NEAT1\_2 RNAs produced during a transcription burst probably act as a nucleation site of paraspeckles (Chujo and Hirose 2017; Yamazaki et al., 2020).

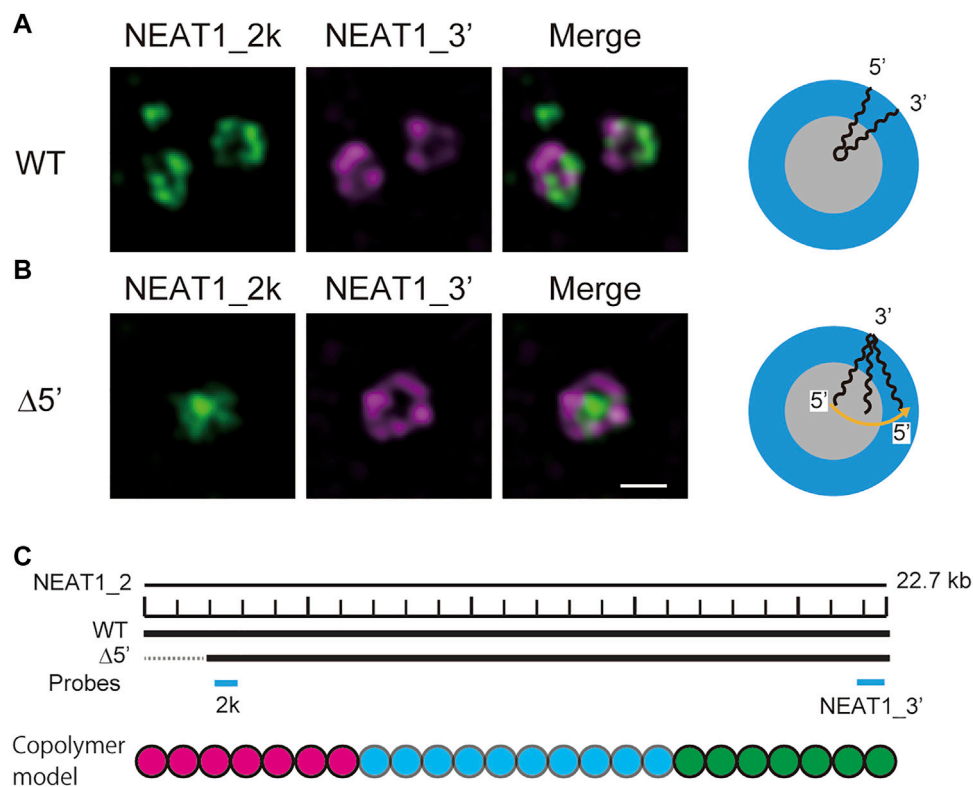
We have recently extended the Flory-Huggins theory, which is the standard theory of phase separation of polymers in a solution (Doi 1996), to predict the phase separation driven by the production of arcRNAs due to transcription (Yamamoto et al., 2020). The condensates assembled by this mechanism are disordered liquids of complexes of arcRNAs and RBPs. However, paraspeckles are not condensates of disordered liquid,

but form a characteristic core-shell structure (Souquere et al., 2010; West et al., 2016): the two terminal regions and the middle region of NEAT1\_2 form the shell and the core of paraspeckles, respectively. The structure of paraspeckles is analogous to micelles of ABC triblock copolymers in a selective solvent, where two polymer chains (A and C blocks) composed of hydrophilic units are chemically bonded to the two ends of a chain (B block) composed of hydrophobic units (Monzen et al., 2000; Mai and Eisenberg 2012; Moughton et al., 2012). The ordered structure and the transcription driven formation of paraspeckles are two features that distinguish paraspeckles from condensates assembled by the classical phase separation, such as LLPS, in the thermodynamic equilibrium.

In our recent experiments, we have constructed mutant NEAT1\_2 cell lines, in which the terminal regions of NEAT1\_2 were partly deleted by CRISPR/Cas9 and have observed paraspeckles in such cell lines with the super-resolution optical microscope and the electron microscope (Yamazaki et al., 2018, 2021). Our experiments have shown that the terminal regions of NEAT1\_2 RNAs were localized in the shells of paraspeckles in the wild type (WT) (Figure 1A), whereas the terminal regions were distributed both to the core and the shell in the mutant cells (Figure 1B) (the schematics of NEAT1\_2 for each case is shown in Figure 1C). Motivated by this result, we here construct a model of paraspeckles by taking into account the transcription dynamics of NEAT1\_2 in an extension of the theory of micelles of ABC triblock copolymers. The A and C blocks correspond to the terminal regions of NEAT1\_2 RNP complexes and the B block corresponds to their middle region. The B blocks are associative due to the multivalent interactions between RBPs, such as NONO and FUS, that specifically bind to this B block region due to its sequence (Yamazaki et al., 2018).

In many cases, paraspeckles are approximately spherical, whereas cylindrical paraspeckles are also observed, for example, when NEAT1\_2 transcription is upregulated (Hirose et al., 2014). The analysis of cylindrical paraspeckles greatly complicates the theory, while the essence of the biophysical mechanism of the assembly of paraspeckles is already in the theory of spherical paraspeckles. Not to hide the essence behind the complexity of analysis, in this paper, we limit our discussion to spherical paraspeckles.

Our theory predicts the distribution of terminal blocks (A blocks) and the size of paraspeckles in wild type and mutant with deleted terminal blocks and also the effect of the upregulation of NEAT1\_2 transcription. Our prediction is consistent with our recent experiments (Yamazaki et al., 2018, 2021), implying that the assembly of paraspeckles can be understood as micellization. Our theory provides biophysical insight into the assembly of WT and mutant paraspeckles. The sequences of arcRNAs determine the arrangements of RBPs along these arcRNAs and thus play a role in the blueprints of nuclear bodies, while their assembly is fine-tuned by the transcription dynamics of arcRNAs. Our theory can be extended to understand the mechanism of the



**FIGURE 1**

Super-resolution microscopic images of paraspeckles in HAP1 NEAT1 wild type (A) and D5' mutant cells lacking their NEAT1 0–1.8 kb regions (B) detected by NEAT1\_2k FISH probes against 5' terminal region of NEAT1 (green) and NEAT1\_3' FISH probes (magenta) in the presence of MG132 (5 mM for 6 h). Scale bar, 500 nm. (C) The schematics of WT NEAT1\_2 and mutants with deletions in the 5' terminal regions. The positions of NEAT1 probes (NEAT1\_2k and NEAT1\_3') are shown by the blue bars. See Yamazaki et al. 2021 for experimental details. Copolymer model is schematic and the borders of A, B, and C blocks remain to be experimentally characterized.

assembly of other nuclear bodies once the arrangements of RBPs along arcRNAs are determined by experiments.

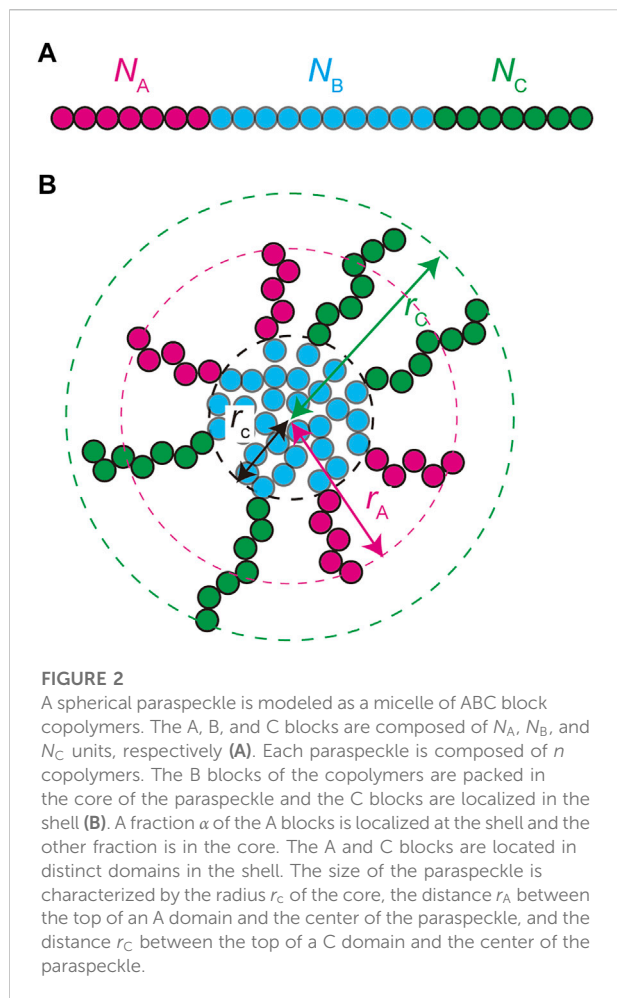
## Materials and methods

### Model

We treat the NEAT1\_2 RNP complexes as ABC triblock copolymers (Figure 2A). Different RBPs are bound to A, B, and C blocks and this makes the magnitudes of interactions between units in the same blocks different from the magnitudes of the interactions between different blocks. Treating a complex as one polymer, instead of treating arcRNA and RBPs separately, is effective for the case in which the binding affinity of RNA-binding proteins to these blocks is relatively large (Yamamoto et al., 2020). The A, B, and C blocks are composed of  $N_A$ ,  $N_B$ , and  $N_C$  (Kuhn) units, respectively, (Figure 2A). The core of a paraspeckle is assembled by the association of the B blocks because of the attractive interactions between the

RBPs bound to these blocks (Figure 2B). The A and C blocks form the shell because the RBPs bound to these terminal blocks have affinity to the solution (nucleoplasm), rather than the RBPs bound to B blocks. The analysis of the cylindrical paraspeckles greatly complicates the theory because of the massive form of the free energy, an extra geometrical parameter that should be determined by minimizing the free energy, and the lack of steady state. In this paper, we focus on spherical paraspeckles.

In the thermodynamic equilibrium, the most stable state is the one at the minimum of the free energy of the system. The free energy of a micelle of block copolymers is composed of 1) the stretching free energy of the blocks in the core, 2) the surface free energy at the interface between the core and the shell, and 3) the free energy of the blocks in the shell (Halperin and Alexander 1989; Semenov et al., 1995; Zhulina et al., 2005). The growth of polymer micelles decreases the surface free energy and increases the stretching free energy of blocks in the core and the free energy due to the excluded volume interactions between



blocks in the shell (Halperin and Alexander 1989; Semenov et al., 1995; Zhulina et al., 2005). The stable size of spherical micelles is determined by the balance of these free energy contributions. Most theories predict the distribution of the size of polymer micelles that are assembled uniformly in a block copolymer solution at the thermodynamic equilibrium (Anniansson and Wall 1974; Safran 2003; Hadjiivanova et al., 2011; Mysona et al., 2019). We extend the theory of polymer micelles by taking into account the fact that paraspeckles are assembled locally at the transcription site of NEAT1\_2 and their assembly is coupled with the transcription of NEAT1\_2.

## Free energy

The free energy quantifies the stability of the system at the thermodynamic equilibrium. We here derive the free energy of a paraspeckle by taking into account the fact that the terminal blocks of NEAT1\_2 are distributed both to the shell and the core

in an extension of the free energy of a polymer micelle (Halperin and Alexander 1989; Semenov et al., 1995; Zhulina et al., 2005). The free energy of a paraspeckle composed of  $n$  triblock copolymers has the form

$$F_n = F_{\text{cor}} + F_{\text{sur}} + F_{\text{shl}} + F_{\text{mix}}, \quad (1)$$

where  $F_{\text{cor}}$  is the free energy of the core,  $F_{\text{sur}}$  is the surface free energy at the interface between the core and the shell,  $F_{\text{shl}}$  is the free energy of the shell, and  $F_{\text{mix}}$  is the mixing free energy (Figure 3).

The free energy of the core has the form

$$\frac{F_{\text{cor}}}{k_B T} = \frac{3}{2} \lambda_s \frac{r_c^5}{N_B^2 b^5} 4\alpha + \frac{3}{2} \lambda_s \frac{r_c^5}{(N_A + N_B) b^5} (1 - \alpha) + \chi_{AB} \phi_A \phi_B \frac{V_c}{b^3}. \quad (2)$$

The first and second terms are the stretching free energy of the B blocks in the core and are derived in the spirit of Semenov 1985, see Supplementary Section S1. The third term is the free energy due to the interactions between the A and B units in the core. For cases in which the number  $N_A$  of the A blocks is relatively large, these blocks may aggregate to minimize the repulsive interactions between A and B units. However, to keep the simplicity of the theory, we derived the third term of Eqn. 2 by assuming that the fraction  $1 - \alpha$  of the A blocks are distributed uniformly in the core, independent of the number  $N_A$  of units in A blocks. With the assumption with which the core is packed with A and B blocks, the volume  $V_c$  has the form

$$V_c = \frac{4\pi}{3} r_c^3 = n b^3 (N_B + (1 - \alpha) N_A) \quad (3)$$

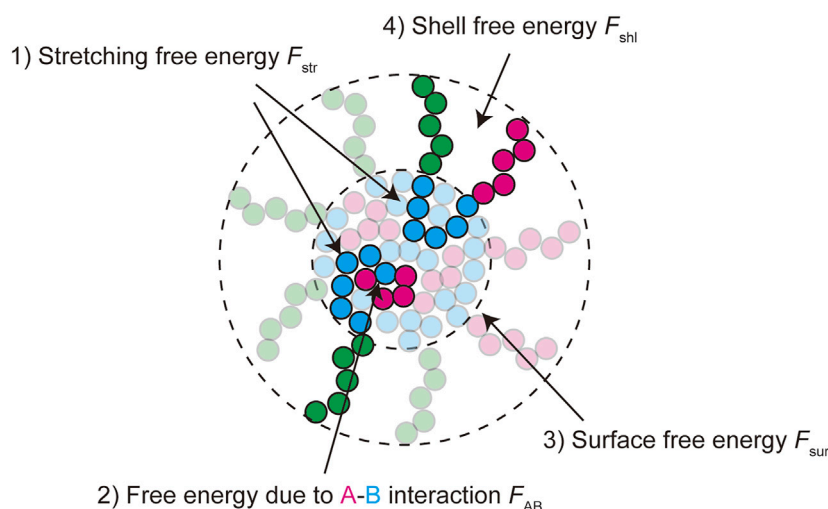
where  $r_c$  is the radius of the core.  $\lambda_s (= \pi^3/30)$  is the geometrical factor (Semenov 1985). The interaction parameter  $\chi_{AB}$  accounts for the excluded volume interactions between the A blocks and the B blocks.  $\phi_A (= b^3 (1 - \alpha) N_A n / V_c)$  and  $\phi_B (= b^3 N_B n / V_c)$  are the volume fractions of the A blocks and the B blocks in the core, respectively. The core is occupied by the A and B blocks,  $\phi_A + \phi_B = 1$ .

The surface free energy has the form

$$F_{\text{sur}} = 4\pi \chi_B \frac{r_c^2}{b^2}. \quad (4)$$

The interaction parameter  $\chi_B$  accounts for the (free) energetic penalty due to the fact that the B units at the surface have less number of interacting partners than in the interior of the core. Without changing the physics, we treat cases in which the A and C units are dilute both in the core and the shell. In such cases, the interactions between the B units at the core surface and the A units in the shell as well as the interactions between the A units at the core surface and the solution are both negligible.

Theories of block copolymer micelles treat blocks in the shell as a polymer brush on a curved surface (Halperin and Alexander 1989; Semenov et al., 1995; Zhulina et al., 2005). There are elaborate approaches to treat polymer



**FIGURE 3**

The free energy of a paraspeckle is composed of five terms: 1) the stretching free energy of blocks in the core  $F_{str}$ , 2) the free energy due to the repulsive interactions between A and B units in the core  $F_{AB}$  ( $\approx \chi_{AB} N_A n$ ), 3) the surface free energy  $F_{sur}$  ( $\approx N_B^{-1/3} n^{5/3}$ ), 4) the free energy of the shell  $F_{shl}$  ( $\approx N_A N_B^{-5/9} n^{23/18}$ ), and 5) the mixing free energy  $F_{mix}$ . The free energy contributions  $F_{AB}$  and  $F_{sur}$  represent the (free) energetic penalty because B units at the vicinity of A units in the core and at the surface have a lesser number of partners of multivalent interactions.

brushes on planer (Netz and Schick 1998) and curved surfaces (Zhulina et al., 2006), however, for simplicity, we here use the scaling theory of polymer brush (Alexander 1977; de Gennes 1980). With this approach, the free energy of the shell has the form

$$F_{shl} = F_A + F_C \tag{5}$$

with

$$\frac{F_A}{k_B T} = \frac{3}{5} \frac{(n\alpha)^{\frac{3}{2}}}{(4\pi f_A)^{\frac{1}{2}}} C_s \log\left(1 + \frac{5}{3} \frac{h_A}{r_c}\right) \tag{6}$$

$$\frac{F_C}{k_B T} = \frac{3}{5} \frac{n^{\frac{3}{2}}}{(4\pi(1-f_A))^{\frac{1}{2}}} C_s \log\left(1 + \frac{5}{3} \frac{h_C}{r_c}\right). \tag{7}$$

Eqn. 6 includes the stretching free energy of the A blocks in the shell and the free energy due to the excluded volume interactions between A units in the shell. Eqn. 7 is the corresponding free energy for the C blocks. We neglected the excluded volume interaction between the A and C units because the 3' and 5' terminal regions are segregated in separate domains in the shell of wild type paraspeckles (West et al., 2016). Eqs. 6, 7 are derived by using so-called Daoud-Cotton scaling theory (Daoud and Cotton 1982), assuming that the solution is a good solvent to both A and C blocks, following the usual treatment of block copolymer micelles (Halperin and Alexander 1989; Semenov et al., 1995; Zhulina et al., 2005), see also in Supplementary Section S2.1  $f_A$  is the fraction of the core surface occupied by A blocks and has the form

$$f_A = \frac{\alpha}{1 + \alpha}. \tag{8}$$

Eqn. 8 is derived by using the fact that the osmotic pressure in the domains of A blocks is equal to the osmotic pressure in the domains of C blocks, see Supplementary Section S2.1.  $h_A$  and  $h_C$  are the heights of A and C blocks in the limit of planer brush,  $r_c \rightarrow \infty$ , respectively. These heights have the forms (Alexander 1977; de Gennes 1980)

$$h_A = N_A b \left( v_A \frac{n\alpha}{4\pi f_A r_c^2 b} \right)^{\frac{1}{3}} \tag{9}$$

$$h_C = N_C b \left( v_C \frac{n}{4\pi(1-f_A)r_c^2 b} \right)^{\frac{1}{3}}. \tag{10}$$

$v_A$  and  $v_C$  are the excluded volumes that account for the excluded volume interactions between the A units and those between the C units, respectively.  $C_s$  is a numerical constant of order unity and is determined as  $C_s \approx 1.38$  by curvefitting the experiments on the micelles of polystyrene-polyisoprene copolymers with the scaling theory (Zhulina et al., 2005).

The mixing free energy represents the entropic contribution that distributes the A blocks randomly to the shell and the core and has the form

$$\frac{F_{mix}}{k_B T} = n(\alpha \log \alpha + (1 - \alpha) \log(1 - \alpha)). \tag{11}$$

The free energy  $F_n(\alpha)$  is a function of the number  $n$  of triblock copolymers comprising the paraspeckle and the fraction

$\alpha$  of A blocks in the shell. We determine the fraction  $\alpha$  by the minimization of the free energy  $F_n(\alpha)$ . This corresponds to cases in which the time scale of the redistribution of A blocks is smaller than the time scale of the production of transcripts.

## Association and dissociation dynamics of NEAT1\_2

Most theories of polymer micelles predict the most stable size and the distribution of the size of polymer micelles that are assembled uniformly in a block copolymer solution at the thermodynamic equilibrium (Annianson and Wall 1974; Safran 2003; Hadgiivanova et al., 2011; Mysona et al., 2019). In contrast, the assembly of paraspeckles is coupled with the transcription of NEAT1\_2 (Mao et al., 2011). RBPs can bind to nascent NEAT1\_2 transcripts, which are still connected to the transcription site via Pol II, and an array of complexes of nascent NEAT1\_2 transcripts and RBPs during a transcription burst act as a nucleation site of paraspeckles. Once a paraspeckle is nucleated, nascent NEAT1\_2 transcripts are added to the paraspeckle one by one as nascent transcripts are produced by Pol II. This situation may be somewhat analogous to the assembly of micelles due to the association of side chains that are attached to a main chain, except for the fact that these side chains are not produced and released dynamically. The side chains assemble micelles without translational entropy cost, in contrast to the micellization of polymer chains freely diffusing in the solution (Borisov and Halperin 1995). We thus derive the time evolution equation of a paraspeckle at the transcription site by taking into account the facts that 1) nascent NEAT1\_2 transcripts are associated with the paraspeckle without the translational entropy cost and 2) paraspeckles are assembled locally at the transcription site. Because of these features, paraspeckles are different from block copolymer micelles assembled in the thermodynamic equilibrium (Annianson and Wall 1974; Safran 2003; Hadgiivanova et al., 2011; Mysona et al., 2019).

We treat the probability  $q_n(t)$  that the paraspeckle assembled at the transcription site of NEAT1\_2 is composed of  $n$  transcripts at time  $t$ . The time evolution of the probability  $q_n(t)$  has the form

$$\frac{d}{dt}q_1(t) = -J_1(t) \quad (12)$$

$$\frac{d}{dt}q_n(t) = -J_n(t) + J_{n-1}(t). \quad (13)$$

The flux  $J_n(t)$  has the form

$$J_n(t) = k_0\phi_p q_n(t) - k_0 e^{-(F_n+F_1-F_{n+1})/(k_B T)} (n+1)q_{n+1}(t) + k_{tx}q_n(t). \quad (14)$$

The first term of Eqn. 14 is the rate with which transcripts diffusing in the solution are spontaneously associated with the paraspeckle.

The second term is the rate with which a transcript is spontaneously dissociated from the paraspeckle. The third term is the rate with which a nascent transcript during production is added to the paraspeckle through transcription.  $k_0$  is the rate constant that accounts for the association of transcripts diffusing in the solution with the paraspeckle.  $\phi_p$  is the volume fraction of transcripts that are not associated to paraspeckles.  $F_n$  is the free energy which is already minimized with respect to the fraction  $\alpha$ , see Eqn. 1.  $k_{tx}$  is the rate with which a nascent transcript is added to the paraspeckle. The form of the third term of Eqn. 14 represents the fact that nascent transcripts can be associated with the paraspeckle without the translational entropy cost. We note that the probability  $q_n(t)$  is the local quantity of the paraspeckle assembled at the transcription site, in contrast to the usual treatment of micelles that predict the global distribution function of the size of micelles in a solution (Annianson and Wall 1974; Safran 2003; Hadgiivanova et al., 2011; Mysona et al., 2019).

For cases in which the transcription is suppressed,  $k_{tx} \rightarrow 0$ , the probability  $q_n^{eq}$  in the equilibrium has the form

$$q_n^{eq} \propto \frac{\phi_p^{n-1}}{(n-1)!} e^{-\frac{F_n - nF_1}{k_B T}}. \quad (15)$$

Substituting Eqn. 15 into Eqn. 14 leads to  $J_n = 0$  for  $k_{tx} \rightarrow 0$  that ensure the detailed balance at the thermodynamic equilibrium.

In the steady state,  $\frac{dq(t)}{dt} = 0$ , the solution of Eqs. 12, 13 has the form

$$q_n^{st} = \frac{1}{Z_{st}} e^{-\frac{\mathcal{F}_n^{st}}{k_B T}}. \quad (16)$$

The effective free energy  $\mathcal{F}_n^{st}$  has the form

$$\mathcal{F}_n^{st} = F_n - nF_1 - k_B T (n-1) \log(\phi_p + \zeta) + k_B T \log(n!) \quad (17)$$

where  $\zeta (= k_{tx}/k_0)$  is the ratio of the association rates.  $Z_{st}$  is the effective partition function

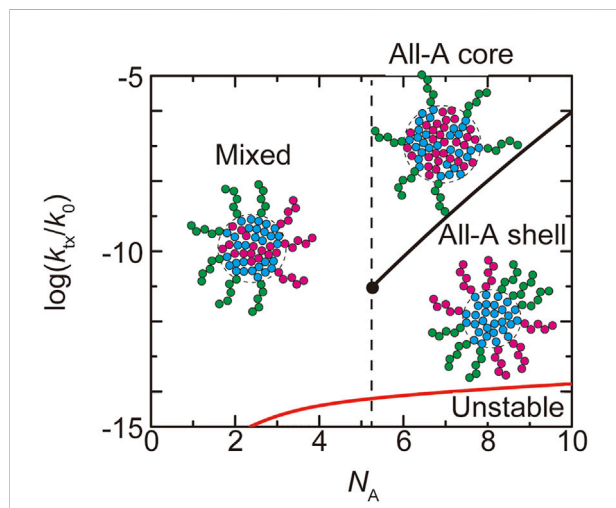
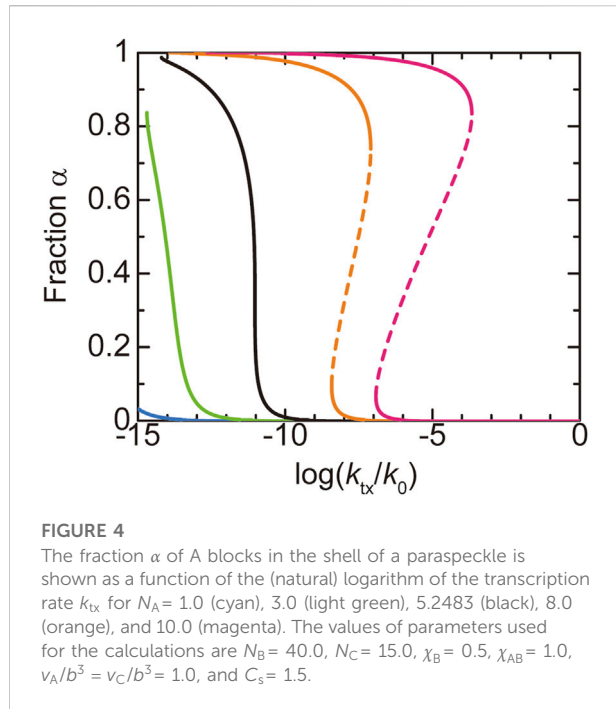
$$Z_{st} = \sum_{n=1}^{\infty} e^{-\mathcal{F}_n^{st}/(k_B T)}. \quad (18)$$

The number of transcripts composing a paraspeckle with the maximum probability in the steady state is derived by minimizing the effective free energy  $\mathcal{F}_n^{st}$  with respect to  $n$ . In this paper, we treat cases in which NEAT1\_2 transcripts are exclusively localized in paraspeckles,  $\phi_p \rightarrow 0$  (Sasaki et al., 2009; Yamazaki et al., 2021).

## Results

### Transcription dynamics regulates the structure of paraspeckles

We first discuss the dependence of the fraction  $\alpha$  of A blocks in the shell on the production rate  $k_{tx}$  of NEAT1\_2 transcripts. The number  $n$  of transcripts in a paraspeckle is derived as a



function of  $k_{tx}$  by minimizing the effective free energy  $\mathcal{F}_n^{st}$ , see Eqn. 17, and the fraction  $\alpha$  of A blocks in the shell is derived by minimizing the free energy  $F_n$  for this number  $n$ , see Eqn. 1. When the number  $N_A$  of units in the A blocks is smaller than a critical value  $N_{Ac}$ , the fraction  $\alpha$  decreases continuously with

increasing the production rate  $k_{tx}$  (the cyan and light green lines in Figure 4). When the number  $N_A$  of units in the A blocks is larger than the critical value  $N_{Ac}$ , the paraspeckles are the ‘all-A shell’ state, in which all the A blocks are in the shell,  $\alpha \approx 1$ , for low transcription rate and the ‘all-A core’ state, in which all the A blocks are in the core,  $\alpha \approx 0$ , for high transcription rate (the orange and magenta lines in Figure 4). There is a discontinuous transition between the all-A shell and all-A core states at a threshold value of production rate. This result is summarized in the phase diagram (Figure 5). The ‘mixed’ state for  $N_A < N_{Ac}$ , where A blocks are distributed between the core and the shell, results from the thermal fluctuation, which is quantified by the mixing free energy  $F_{mix}$ . For  $N_A > N_{Ac}$ , the interaction free energy,  $F_{shl}$  and  $F_{AB}$ , where both scale proportional to  $N_A$ , dominates the mixing free energy  $F_{mix}$ , which is independent of  $N_A$  and thus only the all-A shell and all-A core states are possible (see a quantitative argument below). It is analogous to the Flory-Huggins theory that predicts that the interaction free energy dominates the mixing free energy in polymer systems (Doi 1996). The fraction  $\alpha$  of A blocks in the shell is sensitive to the upregulation of the transcription of NEAT1\_2 transcripts when  $N_A < N_{Ac}$ , whereas the fraction  $\alpha$  does not change significantly by the moderate upregulation of the transcription when  $N_A > N_{Ac}$  (Figure 4). It is because for  $N_A > N_{Ac}$ , the interaction free energy dominates the mixing free energy and thus the changes of the fraction  $\alpha$  is suppressed.

In the WT, most of the terminal regions of NEAT1\_2 are localized at the shell (Souquere et al., 2010; West et al., 2016; Yamazaki et al., 2018, 2021). This implies that paraspeckles in the WT are in the ‘all-A shell’ state, which happens for  $N_A > N_{Ac}$  and relatively low transcription rate. In deletion mutants, a fraction of the terminal blocks, which were partially deleted, is localized at the core, implying that paraspeckles in the deletion mutants correspond to the case of  $N_A < N_{Ac}$ . Our recent experiments have shown that in deletion mutants, the fraction  $\alpha$  of the terminal regions, which were partially deleted, localized at the shell decreases by the upregulation of the transcription of NEAT1\_2, whereas in the WT, the fraction does not change with the upregulation of transcription (Yamazaki et al., 2021). These predictions are consistent with the prediction of our theory. However, we note that in the WT, the fraction of cylindrical paraspeckles increases by the upregulation (Hirose et al., 2014) and the morphological transition to cylinder may also be involved in the insensitivity.

Our theory predicts the biophysical mechanism of the assembly of paraspeckles. The fact that all the terminal blocks are localized at the shell in the WT paraspeckles results from the strong repulsive interaction between A and B blocks, where its influence to the structures of paraspeckles is quantified by the free energy  $F_{AB}$  ( $\approx \chi_{AB} N_A n$ ). Indeed, the free energy  $F_{shl}$  ( $\approx N_A N_B^{-5/9} n^{23/18}$ ) of A and C blocks in the shell and the free energy  $F_{str}$  ( $\approx N_B^{-1/3} n^{5/3}$ ) due to the stretching of B blocks in the core both decrease as the fraction  $\alpha$  of A blocks in the shell

decreases. However, the free energy  $F_{AB}$  dominates probably because the magnitude  $\chi_{AB}$  of the interaction between A and B blocks and the number  $N_B$  of units in each B block is large enough in WT NEAT1\_2. The influence of the thermal fluctuation that randomly distributes A blocks between the core and the shell to the structure is quantified by the mixing free energy  $F_{mix}$  and it is independent of the number  $N_A$  of units in A blocks. In contrast, the free energy  $F_{AB}$  due to the interactions between A and B blocks in the core increases as the number  $N_A$  of units in each A block increases. For  $N_A > N_{Ac}$ , the interaction free energy  $F_{AB}$  dominates the mixing free energy  $F_{mix}$  and thus the ‘all-A shell’ state becomes stable. In contrast, for  $N_A < N_{Ac}$ , the mixing free energy is still significant and thus A blocks are distributed between the shell and the core. This explains the difference of the structures of paraspeckles between WT and deletion mutants (Figure 1 and Yamazaki et al., 2018, 2021).

The number  $n$  of transcripts in the paraspeckle increases with increasing the transcription rate. For a relatively small transcription rate, all-A shell state becomes stable because the free energy  $F_{AB}$  due to the repulsive interactions between A and B blocks in the core (see Eqn. 2 for  $N_B > N_A$ ) dominates the free energy  $F_{shl}$  due to the excluded volume interactions between A units in the shell and the stretching free energy  $F_{str}$  of blocks in the core (see Eqn. 2 for  $N_B > N_A$ ). The free energy  $F_{shl}$  of the blocks in the shell and the stretching free energy  $F_{str}$  of blocks in the core increase faster than the free energy  $F_{AB}$  due to the repulsive interactions between A and B blocks in the core as the number  $n$  of transcripts in the paraspeckle increases. This results in the decrease of the fraction  $\alpha$  of the A blocks in the shell with increasing the transcription rate (see the Supplementary Discussion for the relative significance of the free energy contributions  $F_{shl}$  and  $F_{str}$ ). For very small production rate, stable paraspeckles are not assembled, see the region delineated by the red line in Figure 5.

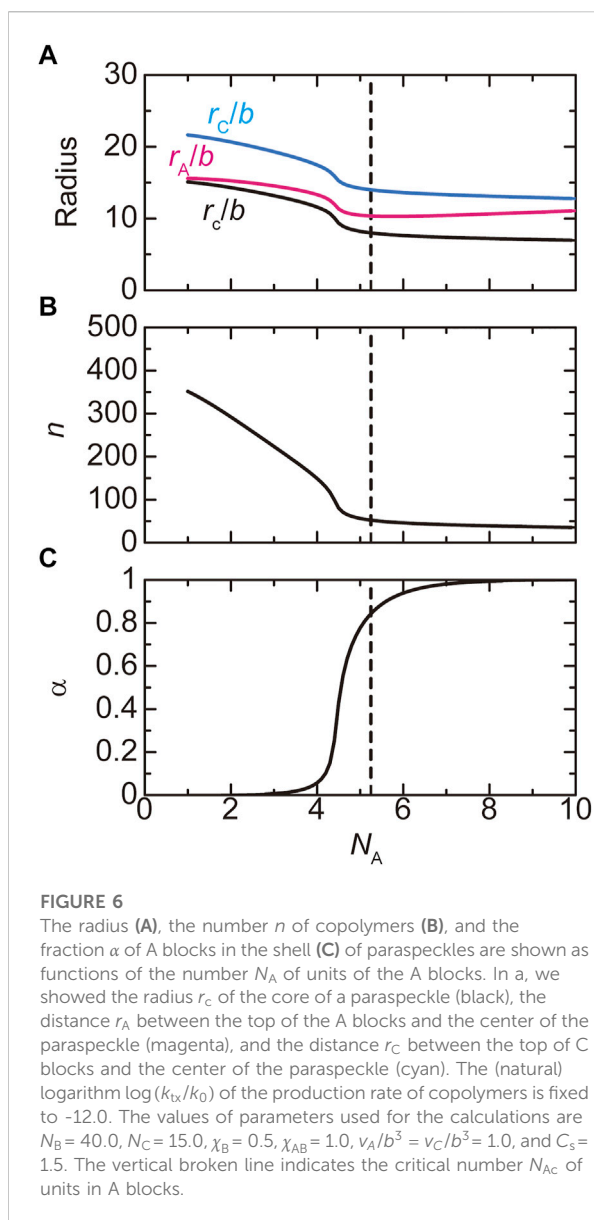
## Repulsive interactions of terminal blocks and entropic elasticity of middle blocks limit the number of transcripts in paraspeckles

The size of paraspeckles in the WT and deletion mutants is experimentally accessible. The radius  $r_c$  of the core is derived by using Eqn. 3. The radii,  $r_A$  and  $r_C$ , are derived by using the forms

$$r_A = r_c \left( 1 + \frac{5}{3} \frac{h_A}{r_c} \right)^{\frac{3}{5}} \quad (19)$$

$$r_C = r_c \left( 1 + \frac{5}{3} \frac{h_C}{r_c} \right)^{\frac{3}{5}}, \quad (20)$$

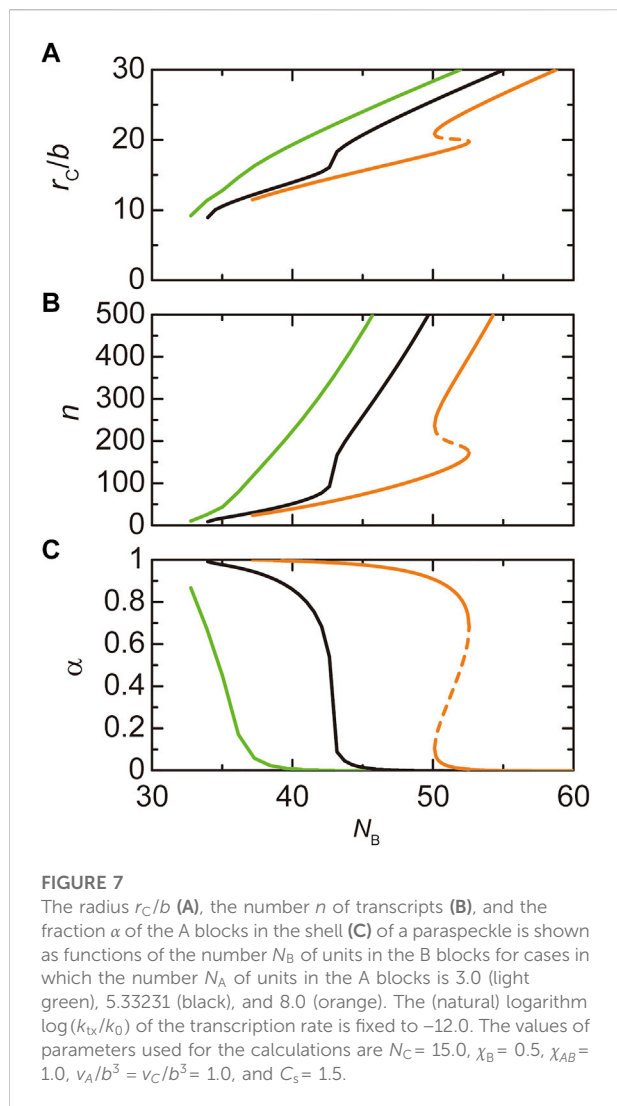
where the heights,  $h_A$  and  $h_C$ , are given in Eqs. 9, 10. The derivation of Eqs. 19, 20 are shown in Supplementary Section S2.1. These radii



are functions of the number  $n$  of transcripts in a paraspeckle and the fraction  $\alpha$  of blocks in the shell, where the latter parameters are derived similarly to Figure 4. At a first glance, one may think that the radius of the paraspeckle decreases as the number  $N_A$  of units in A blocks decreases. However, our theory predicts that the radius of paraspeckles (defined by the distance between the top of the A or C blocks and the center of the paraspeckle) increases with decreasing the number  $N_A$  of units in A blocks, see Figure 6A. It is because the number  $n$  of transcripts in the paraspeckle increases with decreasing the number  $N_A$  of units in A blocks, see Figure 6B. This prediction is consistent with our recent experiments (Yamazaki et al., 2021).

The number of transcripts in a paraspeckle is limited by the free energy  $F_{shl}$  of blocks in the shell and the stretching free energy  $F_{str}$  of blocks in the core, analogous to micelles of

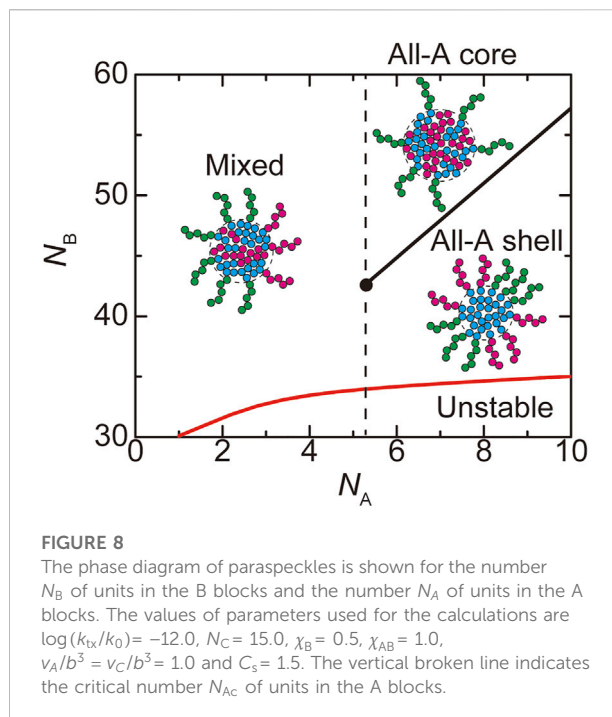




diblock copolymers. These free energy contributions decreases as the fraction  $\alpha$  of A blocks in the shell decreases. Indeed, the fraction  $\alpha$  of A blocks in the shell decreases with decreasing the number  $N_A$  of units in the A blocks, see [Figure 6C](#). More transcripts can therefore associate with paraspeckles as the number  $N_A$  of units in A the blocks decreases. These predictions are consistent with our recent experiments, see [Discussion and Yamazaki et al., 2021](#).

## Paraspeckles are assembled by the association of the middle regions

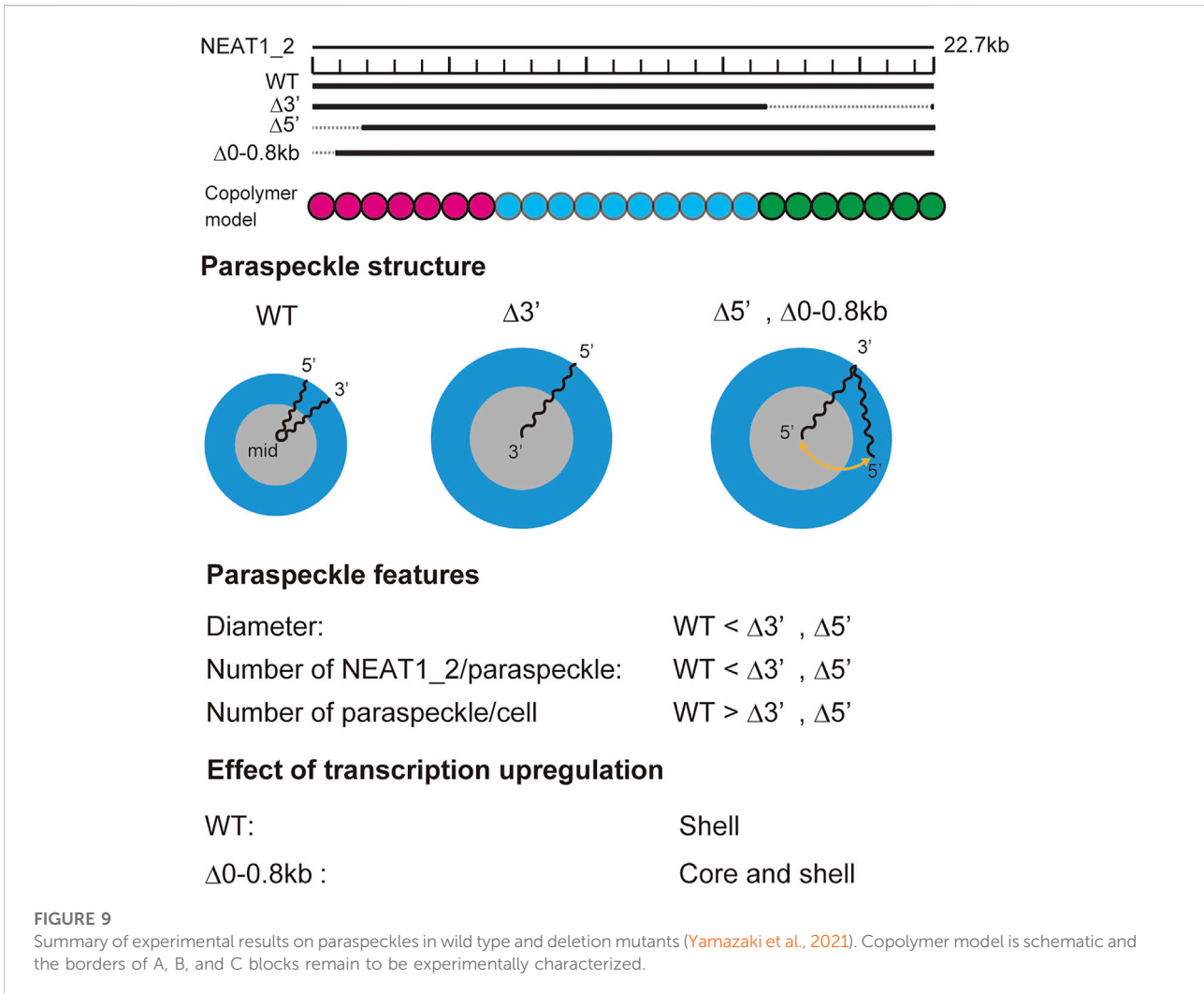
Paraspeckles are assembled by the attractive interactions between the B blocks of NEAT1\_2 RNP complexes. As expected, the radius  $r_c$  of paraspeckles decreases as the number  $N_B$  of units in the B blocks decreases, see [Figure 7A](#). With a fixed



transcription rate, the number  $n$  of transcripts in the paraspeckle decreases with decreasing the number  $N_B$  of units in the B blocks. It is because decreasing the number  $N_B$  of units in the B blocks increases the density of A and C blocks in the shell and thus increases the free energy  $F_{shl}$  of A and C blocks in the shell, see [Figure 7B](#). It also increases the extent of the stretching of B blocks in the core and thus increases the stretching free energy  $F_{str}$  of the B blocks in the core. The fraction  $\alpha$  of A blocks in the shell increases as the number  $N_B$  of units in B blocks decreases because A blocks in the core suppress the attractive interactions between the B blocks, see [Figure 7C](#). The formation of paraspeckles is suppressed for cases in which the number  $N_B$  of units in the B blocks is too small, see [Figure 8](#). These predictions are consistent with our experiments that show that paraspeckles of mutant cells, in which a part of the middle region of NEAT1\_2 is deleted, are small and dispersed, compared with the WT, see also the [Discussion and Yamazaki et al., 2018](#).

## Discussion

We have constructed a theory of paraspeckle assembly by taking into account the transcription dynamics of NEAT1\_2 in an extension of the theory of ABC triblock copolymer micelles. This model captures two features of paraspeckles: paraspeckles form the characteristic core-shell structure and the assembly of paraspeckles is coupled with the transcription of NEAT1\_2. Our theory provides a biophysical insight into the assembly of paraspeckles. Paraspeckles are assembled by multivalent interactions between



the middle blocks of the NEAT1\_2 RNP complexes (Yamazaki et al., 2018). The repulsive interactions between A and B blocks, quantified by the interaction free energy  $F_{AB}$ , expels A blocks from the core, while the thermal fluctuations, quantified by the mixing free energy  $F_{mix}$ , distribute A blocks randomly between the core and the shell. All the A blocks are localized in the shell for the WT, where the number  $N_A$  of units in A block is large enough, because the interaction free energy  $F_{AB}$  dominates the mixing free energy  $F_{mix}$ . This reflects the connectivity of RBPs via the terminal regions of NEAT1\_2 and is a well-known feature of polymeric molecules (Doi 1996). This also accounts for the fact that the all-A shell structure of WT paraspeckles is not sensitive to the upregulation of transcription, even for spherical paraspeckles.

Our recent experiments have revealed that (I) the 5' terminal regions of NEAT1\_2 transcripts were distributed randomly between the shell and the core in paraspeckles of  $\Delta 5'$  deletion mutants, where the 5' terminal region of NEAT1\_2 was deleted by  $\approx 2$  kb, (II) the 3' terminal region of most NEAT1\_2 transcripts was localized in the core of paraspeckles

of  $\Delta 3'$  deletion mutants, where the 3' terminal region of NEAT1\_2 was deleted by 6 kb, (III) the sizes of paraspeckles in  $\Delta 5'$  and  $\Delta 3'$  deletion mutants were larger than the size of wild type paraspeckles, (IV) paraspeckles of deletion mutant, where the middle region of NEAT1\_2 was deleted by 8.6 kb, were smaller and more dispersed than the wild type paraspeckles, (V) in deletion mutants, the fraction of the terminal blocks localized in the shell decreased when the transcription of NEAT1\_2 was upregulated (Yamazaki et al., 2018, 2021). The core-shell structure of paraspeckles is disorganized in  $\Delta 5'$ -  $\Delta 3'$  double deletion mutants (Yamazaki et al., 2018, 2021). The assembly of such disordered paraspeckles has been studied theoretically in our recent research (Yamamoto et al., 2020). The summary of these results is shown in Figure 9. The predictions of our theory are consistent with these experimental results. The assembly of paraspeckles can be therefore viewed as the micellization of NEAT1\_2 RNP complexes, at least in the first approximation. More quantitative comparison requires the characterization of the

interaction parameters between each pair of units by, for example, osmotic pressure measurements (Mangenot et al., 2002) and scattering techniques (Oohashi et al., 2014).

Our theory provides a biophysical insight into our experimental results: In the WT, all the A blocks are localized in the shell because the free energy  $F_{AB}$  due to the repulsive interaction between A and B blocks dominates the mixing free energy  $F_{mix}$ , see the first paragraph of this Discussion. However, the mixing free energy  $F_{mix}$  becomes significant as the number  $N_A$  of units in A blocks decreases. Moreover, the excluded volume interactions between A blocks and those between C blocks, quantified by the free energy  $F_{shl}$ , as well as the stretching of B blocks in the core, quantified by the free energy  $F_{str}$ , drive the relocation of A blocks from the shell to the core. This explains our experimental results (I) and (II), see Figure 9. Because these free energy contributions,  $F_{shl}$  and  $F_{str}$ , limit the number of NEAT1\_2 transcripts that form paraspeckles, the paraspeckles of deletion mutant can accommodate more NEAT1\_2 transcripts. The size of paraspeckles can increase with decreasing the length of the terminal regions of NEAT1\_2 because the number of NEAT1\_2 transcripts in a paraspeckle increases, see Figure 9. In contrast, the number of NEAT 1\_2 transcripts decreases with decreasing the length of the B blocks because the free energy decreases due to the attractive interactions between B blocks by the association of NEAT1\_2 RNP complexes becomes less significant than the free energy increase due to the repulsive interactions between A blocks and those between C blocks. The radius of paraspeckles thus decreases as the number  $N_B$  of units in B blocks decreases, see Figure 9. The number  $n$  of NEAT1\_2 in a paraspeckle increases with the upregulation of the transcription of NEAT1\_2. The free energy contributions,  $F_{shl}$  and  $F_{str}$ , increase relative to the free energy with increasing the number of NEAT1\_2 in a paraspeckle  $F_{AB}$ . This drives the relocation of A blocks from the shell to the core with the upregulation of NEAT1\_2 transcription in the deletion mutant. The all-A shell configuration of a WT paraspeckle does not change with the upregulation of NEAT1\_2 transcription, see the first paragraph of this Discussion.

In our approach, we take into account only the essential features to understand the mechanism of the assembly of paraspeckles, instead of doing computer simulations by including all known things. It is indeed the strategy of theoretical physics. Our theory is certainly an important first step, but there are a couple of remaining mysteries. First, we focused on the analysis of spherical paraspeckles, not to hide the essence of the assembly of paraspeckles behind the complexity in treating cylindrical paraspeckles. We thus did not explain the sphere-cylinder morphological transition of paraspeckles. The fact that the fraction of cylindrical paraspeckles increases with the upregulation of NEAT1\_2 transcription is indeed consistent with our conclusion that paraspeckles are assembled by micellization. Second, in the WT, 3' and 5' terminal regions are not randomly mixed, but are separated in microdomains

(West et al., 2016). Our present theory takes into account this feature in the free energy  $F_{shl}$  of the shell by neglecting the interaction between A and C blocks, but did not explain it theoretically. Identifying the RBPs bound to A and C blocks will greatly help to understand the mechanism of the assembly of the microdomains. One possible explanation of the assembly of microdomains is that RBPs bound to A and C are different and the interactions between different blocks are more repulsive than the interactions between the same blocks. However, the microdomains are probably assembled by the microphase separation, judging from the fact that multiple microdomains at the shell of a paraspeckle do not show fusion, and the A-C interaction alone is not enough to explain the assembly of the microdomains. The super-resolution microscope experiments suggest that multiple NEAT1\_2 RNPs form a bundle (West et al., 2016). This bundling probably plays an important role in the assembly of the microdomains of A and C blocks. Third, we used the steady state approximation to derive the distribution of the number  $n$  of NEAT1\_2 transcripts in a paraspeckle. However, the number of NEAT1\_2 transcripts that can be incorporated in a paraspeckle should be limited by the number of NEAT1\_2 transcripts produced in one transcription burst. The experiments that study the relationship between the transcription dynamics and the number of NEAT1\_2 transcripts per paraspeckles would greatly help our understanding of the assembly mechanism of paraspeckles.

## Conclusion

By the combination of theory and experiments, we have shown that paraspeckles are assembled by micellization, not liquid-liquid phase separation. One important feature of micelles is that their size is regulated by the balance between the surface free energy  $F_{sur}$  (that drives the growth of micelles) and the free energy  $F_{shl}$  due to the repulsive interactions between blocks in the shell (that limits the growth of micelles). The free energy  $F_{str}$  due to the entropic elasticity of blocks in the core also limits the growth of micelles. The number of paraspeckles per cell is usually larger than the number of the transcription sites of NEAT1, implying that paraspeckles can diffuse far away from the transcription sites. Paraspeckles may take advantage of this size control mechanism to gain the mobility toward target sites through the meshwork of chromatin in a nucleus.

Our theory and experiments provide insight into the general principle of the assembly of nuclear bodies: The pattern of RBPs binding to arcRNAs is tailored into their RNA sequences and the RNP complexes behave as copolymers that direct the ordering in the internal structures of nuclear bodies. Our theory can be therefore

extended to understand the mechanism of the assembly of other nuclear bodies by using the experimentally determined arrangement of RBPs along arcRNAs. The assembly of nuclear bodies is facilitated by the transcription of arcRNAs. The number of arcRNAs per nuclear body is controlled by both the interactions and connectivity of RBPs bound to the arcRNAs and the transcription dynamics. Chemical engineers control the stability and size of liquid condensates by using surfactants. Life takes the same strategy by using RNA.

## Data availability statement

The datasets presented in this study can be found in online repositories. The names of the repository/repositories and accession number(s) can be found below: <https://doi.org/10.6084/m9.figshare.20209202>.

## Author contributions

All authors designed the research and wrote the manuscript. TeY constructed the model and performed the calculations.

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## Conflict of interest

The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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## Supplementary material

The Supplementary Material for this article can be found online at: <https://www.frontiersin.org/articles/10.3389/fmolb.2022.925058/full#supplementary-material>

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