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# Fluid-structure interaction of flexible collectors affects particle capture efficiency at ecologically relevant collector Reynolds numbers

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**Introduction:** The capture of suspended particles, which is an important process in many aquatic and terrestrial ecosystems, has been modeled using stationary rigid collectors and, more recently those that move in response to flow-induced vibrations. These models do not, however, account for collector flexibility, despite the fact that many biological collectors, especially aquatic collectors, exhibit flexibility.

**Methods:** This study examined the effect of collector flexibility (indicated by the Young's Modulus, *E*; range =  $10^{-3}-10^2$  GPa) on particle capture efficiency ( $\eta$ ; flux of captured particles: flux of particles) at different collector Reynolds numbers (*Re<sub>c</sub>* where the collector diameter [*d<sub>c</sub>*] is the length scale; range = 30-508) in a recirculating flow chamber.

**Results:** Patterns in  $\eta$  were generally similar for flexible and rigid collectors until moderate  $Re_c$  (~374) when higher  $\eta$  were observed on the most flexible collectors. This threshold corresponded to periods of vortex induced motions in which the oscillation frequency of the collector transverse to the flow direction was >4 Hz and the maximum amplitude of the oscillation relative to  $d_c$  was >60% in the transverse and >100% in the longitudinal direction.

**Discussion:** Given the range in *E* examined in this study, it is likely that particle capture on flexible natural collectors has been underestimated using the standard model of a rigid stationary or oscillating collector. The role of collector flexibility should be considered in models and studies of particle capture in natural systems.

#### KEYWORDS

particle capture efficiency, elasticity, collector, collector Reynolds number, flexibility, Cauchy number

# 1 Introduction

The capture of suspended particles is an important process in many aquatic and terrestrial ecosystem processes including suspension feeding, sexual reproduction and the fate and transport of contaminants (reviews in Niklas, 1985; Shimeta and Jumars, 1991; Ackerman, 2000; Ackerman, 2006; Armitage et al., 2008). For example, aquatic plants capture suspended particles and in doing so retain nutrients in bottom sediments, which affects their production and that of aquatic ecosystems (e.g., Jordan et al., 1986; Leonard

et al., 1995). Essentially, the physical process of particle capture includes the encounter, capture and retention of particles suspended within a fluid medium (Vogel, 1994). Five principal mechanisms of particle capture have been characterized (Rubenstein and Koehl, 1977; Spielman, 1977): (1) direct interception in which a particle flowing within a streamline comes into direct contact (i.e., within a particles radius) of the collector and is intercepted; (2) inertial impaction in which denser particles deviate from fluid streamlines moving around the collector, because of their inertia, and thus impact on the collector; (3) diffusional deposition in which Brownian-like motion causes particles of small diameters  $(<10^{-6} \text{ m})$ to deviate from streamlines and be intercepted by the collector; (4) gravitational deposition in which particles with excess density settle onto the collector; and (5) electrostatic attraction in which particle and the collector are of opposite electrical charge inducing an attraction that leads to capture by the collector. Typically, larger diameter particles are captured via direct interception and inertial impaction whereas smaller diameter particles are captured through diffusional deposition and electrostatic attraction (Rubenstein and Koehl, 1977).

Axisymmetric cylindrical collectors have been used in particle capture experiments and modeling (Rubenstein and Koehl, 1977; Shimeta and Jumars, 1991; Spielman, 1977; Palmer et al., 2004; Haugen and Kragset, 2010; Gosselin, 2019; Espinosa-Gayosso et al., 2021). The cylindrical shape is analogous to many biological collectors including the siphons and cilia of suspension feeding organisms as well as the stems of aquatic plants (macrophytes; e.g., Shimeta and Jumars, 1991). This shape is also amenable to fluid dynamic characterization using the collector Reynolds number ( $Re_c$ ) given by

$$Re_c = \frac{d_c U}{v} \tag{1}$$

where  $d_c$  is the diameter of the collector, U is the velocity and v is the kinematic viscosity.  $Re_c$  provides an indication of the ratio of inertial to viscous forces acting on the scale of the collector in addition to the pattern in the flow field in the immediate vicinity of the collector (e.g., Sumer and Fredsøe, 2006). Considerable literature on the mechanics of particle capture by single cylinders exists for creeping flow (i.e.,  $Re_c \ll 1$ ) and for potential flow (i.e.,  $Re_c > 1,000$ ) (e.g., Rubenstein and Koehl, 1977; Spielman, 1977; Shimeta and Jumars, 1991), however, analytical solutions do not exist for 1 <  $Re_c < 1,000$ , which are of interest to ecological systems (Palmer et al., 2004; Espinosa-Gayosso et al., 2013; Espinosa-Gayosso et al., 2021; Boudina et al., 2021). Characteristics of the particle capture process are also provided by the particle Stokes number (*Stk*) given by

$$Stk = 1/9 \, Re_c R^2 s \tag{2}$$

where *R* is the relative particle diameter (ratio of particle diameter to cylinder diameter; i.e.,  $d_p/d_c$ ) and *s* is the specific gravity (ratio of particle density to the density of the fluid; i.e.,  $\rho_p/\rho_f$ ). *Stk* describes the ratio of the particle stopping distance to that of the collector radius. When *Stk* < 1 particles are integrated into the streamlines (Raju and Meiburg, 1995), whereas when *Stk* > 1 particles are likely to deviate from the flow, although the magnitude of *s* may modulate this relationship (Espinosa-Gayosso et al., 2015). Particle capture efficiency ( $\eta$ ) is used to determine the effectiveness of the particle

capture process and to compare among studies.  $\eta$  is based on the number of particles captured per unit area and time divided by the particle flux that would move through an equivalent rectangular cross-sectional area of the collector in the absence of the collector.

The effects of collector motion on  $\eta$  have been examined using physical modeling and an examination of wind pollination in timothy grass (McCombe and Ackerman, 2018) and numerical modeling of soft coral feeding (Boudina et al., 2021). These studies were motivated by the fact that vortex induced oscillations occur in nature as a result of the shear forces between the fluid and the organisms (de Langre, 2008; de Langre, 2019; Gosselin, 2019) in which vibrations are caused when vortices are shed alternatively downstream, inducing a pressure gradient along the surface of the fluid causing motion of the collector in the transverse direction (e.g., Vandiver and Jong, 1987; Bourguet et al., 2011). McCombe and Ackerman (2018) demonstrated that the effects of oscillatory motion on the  $\eta$  of a rigid collector was substantial (>400 predicted by stationary collectors), varied spatially on the collector, and also varied with Rec. The effect was greatest for collectors moving transversely to the flow direction at large magnitude, which encountered more particles with higher relative momentum with respect to the moving collector. Those results confirmed earlier computational fluid dynamic models (Espinosa- Gayosso et al., 2012; Espinosa- Gayosso et al., 2013; Krick and Ackerman, 2015), as well as the influence of the direction of the motion on  $\eta$ . During transverse oscillations, the momentum of low Stk particles relative to the approaching moving collector is sufficient for the particle to penetrate the boundary layer and be captured by the collector. The effect of collectors moving longitudinally to the flow on  $\eta$  is lower because the increase in relative momentum in the approaching phase of the collector oscillation is lost in the retreating phase of the collector motion (Krick and Ackerman, 2015). Nonetheless, a sixth mechanism of particle capture, entitled collector chasing, was identified for moving collectors in which particle capture occurs when a moving particle is intercepted by a collector in its retreating phase (Krick and Ackerman, 2015).

The influence of flexibility of the motion of the collector and the concomitant effects on  $\eta$  remain unknown empirically despite the large range in mechanical properties of biological materials (Table 1). The purpose of this study is, therefore, to examine the effects of flexibility of the collector on particle capture efficiency,  $\eta$ . We do so by measuring  $\eta$  empirically on polymers of different flexibility indicated by their Young's moduli in a recirculating flow chamber under differing  $Re_c$  and comparing them to a stationary rigid collector (standard model).

# 2 Materials and methods

Experiments were conducted in a 14.5-L recirculating flow chamber (test section: 170 cm long × 17 cm wide × 4.5 cm water depth; see vanden Byllaardt and Ackerman, 2014) equipped with three flow straighteners (collimators) placed in the 13-cm long expansion section of the inlet to rectify the flow and one 10 cm upstream of the channel outlet to prevent circulation (Figure 1). The chamber was operated at an average velocity (U) of 2 cm s<sup>-1</sup>, 10 cm s<sup>-1</sup>, 20 cm s<sup>-1</sup>, 25 cm s<sup>-1</sup> and 34 cm s<sup>-1</sup>, which provided turbulent

Young's modulus (E; GPa)	Material (physical and biological within range, and associated <i>E</i> )	References	
180–200	Stainless Steel (180–200 GPa)	Engineering Toolbox (2003)	
130–180	Silicon (130–185 GPa)	Engineering Toolbox (2003)	
100-130	Titanium Alloy (105–120 GPa)	Engineering Toolbox (2003)	
5-100	Glass (50–90 GPa) Jewel box clam shell- <i>Chama</i> (82 GPa) Snail shell- <i>Conus</i> (68 GPa) Coral skeleton- <i>Acropora palmata</i> (21.5 GPa) Wood (birch)- <i>Betula lutea</i> (14.5 GPa) Soft coral skeleton- <i>Ellisella barbadensis</i> (9 GPa)	Engineering Toolbox (2003) Wainwright et al. (1982) Wainwright et al. (1982) Chamberlain (1978) Niklas (1992) Jeyasuria and Lewis (1987)	
2-5	Polymethylmethacrylate (PMMA; 2.4–3.4 GPa) Wood (willow)– <i>Salix nigra</i> (5.0 GPa) Lobster claw– <i>Homarus</i> (4.2 GPa) Soft coral skeleton– <i>Plexaura kuna</i> (4.1 GPa)	Engineering Toolbox (2003) Niklas (1992) Wainwright et al. (1982) Boller et al. (2002)	
1.5-2	Polypropylene (1.5–2 GPa) Soft coral skeleton- <i>Pterogorgia citrina</i> (1.5 GPa)	Ellis and Smith (2000) Jeyasuria and Lewis (1987)	
0.01–1.5	Polyethylene (high density; HDPE; 1 GPa) Polyethylene (low density; LDPE; (0.45 GPa) Polytetrafluoroethylene (PTFE; 0.4 GPa) Black coral axis- <i>Cirripathes</i> (0.3 GPa) Aquatic plant stem- <i>Myriophyllum alteniflorum</i> (0.019 GPa) Potato tuber- <i>Solanum tuberosum</i> (0.01 GPa) BUNA rubber (0.01 GPa)	Engineering Toolbox (2003) Ellis and Smith (2000) Engineering Toolbox (2003) Wainwright et al. (1982) Miler et al. (2012) Ackerman and Nishizaki (1999) Ellis and Smith (2000)	
0.002–0.01	NBR rubber (0.002–0.006 GPa) Silicon Rubber (0.001–0.05 GPa)	Ellis and Smith (2000) Ellis and Smith (2000)	
0.001-0.002	VITON = Viton fluoroelastimer (0.001 GPa) Elastin-ligament (0.001 GPa)	Ellis and Smith (2000) Vogel (1988)	

TABLE 1 Comparison of Young's modulus (E) of biological collectors and physical materials.

conditions based on flow chamber Reynolds number ( $Re_{dh}$ ) using the hydraulic diameter as the length scale (Table 2). Velocity profiles were taken in the area where the collector was placed (i.e., at x =143 cm downstream from the last collimator near the inlet) using a 3D side-looking Acoustic Doppler Velocimeter (ADV; Nortek Vectrino+; sampling frequency = 20 Hz, maximum velocity range = 50 cm s<sup>-1</sup>) to generate velocity profiles at heights of 2.5, 3.5 and 4.0 cm above the bottom, which includes the observation region of the collector used to assess particle capture efficiency. The velocity measurements were generally consistent with theoretical predictions of the 1/7 power law for turbulent flat-plate flow especially at the higher velocities (Supplementary Figure S1). The assessment also indicated that the boundary layer thickness ( $\delta$ ) was greater than the height of the observation region in all cases, and  $\delta >$  $l_{\rm c}$  (length of the collector) for the three lowest velocities (Figure 1 and Supplementary Figure S1). In other words, the observation region of the collectors was contained within the turbulent boundary layer flow of the chamber.

Five materials were used to obtain a range of flexibility in the collectors ( $d_c = 1.5$  mm diameter and  $l_c = 3.75$  cm long) indicated by the Young's Modulus (*E*) that spanned the range found in nature (i.e.,  $10^{-3}$  and  $10^2$  GPa; Table 1). These included: (1) rigid Stainless Steel encased in a  $3M^{TM}$  black heat-shrink tubing (final  $d_c = 1.5$  mm) used as a stationary collector or no-movement control (Young's modulus, nominal E = 200 GPa and density,  $\rho = 7.85 \times 10^3$  kg m<sup>-3</sup>; TW Metals, Hamilton, ON); High Density Polyethylene (HDPE; E = 1.0 GPa and  $\rho = 0.97 \times 10^3$  kg m<sup>-3</sup>; eplastics, San Diego, CA); Low

Density Polyethylene (LDPE; E = 0.45 GPa and  $\rho = 0.94 \times 10^3$  kg m<sup>-3</sup>; eplastics, San Diego, CA); BUNA rubber (BUNA;  $E = 10^{-2}$  GPa and  $\rho = 1.35 \times 10^3$  kg m<sup>-3</sup>; BRP Manufacturing, Lima, OH); and Viton fluoroelastimer (VITON;  $E = 10^{-3}$  GPa and  $\rho = 1.80 \times 10^3$  kg m<sup>-3</sup>; BRP Manufacturing, Lima, OH). The natural frequency for mode 1 of these collectors in water was 710.3 Hz for stainless steel, 95.2 Hz for HDPE, 67.9 Hz for LDPE, 9.7 Hz for BUNA and 2.8 Hz for VITON based on the closed form solution

$$f_n = \frac{3.52}{2\pi} \sqrt{\frac{EI}{ql_c^4}} \tag{3}$$

where *I* is the area moment of inertia, *q* is the total mass per unit length, which includes both the mass of the collector  $(m_c = \rho_c \pi \frac{d_c^2}{4}, \text{where } \rho_c \text{ is the density of the collector})$  and the water added mass  $(m_a = \rho_f \pi \frac{d_c^2}{4}, \text{where } \rho_f \text{ is the density of the fluid})$  (Tongue, 2002). A non-dimensional bending stiffness (*k*') was also determined using the dynamic pressure for each flow chamber velocity given by

$$k' = \frac{EI}{\frac{1}{2}\rho U^2 l_c^3} \tag{4}$$

where  $\rho$  is the density (Shukla et al., 2013). Silver-coated, hollow glass spheres (CONDUCT-O-FIL; Potters Industries Inc., Carlstandt, NJ, USA) were used as particles based on their small size (mean diameter ~13 µm) and density (1.6 g cm<sup>-3</sup>) and reflective properties that facilitated counting. The experimental parameters given by the



Schematic diagram of the experimental system: (A) side view of the open channel flow chamber with the collector located at x = 143 cm downstream of the last collimator (flow is from left; chamber is 17 cm wide); (B) enlarged image of the collector (length  $l_c = 3.75$  cm) with the observation region identified in dark grey (the collector was held on a plexiglass base tacked adhered onto the bottom of the chamber); (C) the relationship between the flow chamber velocity and the thickness of the boundary layer ( $\delta$ ) at x = 143 cm.

TABLE 2 Hydrodynamic conditions in the flow chamber, expected around the collector, and for the particles indicated by the chamber Reynolds number (length scale = hydraulic diameter,  $d_{hi}$ ;  $d_{h}$  = 0.12 m) and flow regime, the collector Reynolds number (length scale = collector diameter) and flow regimes downstream including the vortex shedding frequency indicated by the predicted Strouhal number, and the particle Stokes number.

Flow chamber			Collector			Particle
Velocity (m s <sup>-1</sup> )	Reynolds number ( <i>Re<sub>dh</sub></i> )	Flow regime	Reynolds number ( <i>Re<sub>c</sub></i> )	Flow regime downstream	Strouhal number ( <i>St</i> )	Stokes number ( <i>Stk</i> )
0.02	2,344	Turbulent	30	Attached pair of vortices	0.035	$4.01 \times 10^{-4}$
0.10	11,722	Turbulent	149	Vortices shed in laminar street	0.194	$2.00 \times 10^{-3}$
0.20	23,445	Turbulent	299	Transition to turbulent	0.211	$4.01 \times 10^{-3}$
0.25	29,306	Turbulent	374	Turbulent	0.213	$5.01 \times 10^{-3}$
0.34	39,856	Turbulent	508	Turbulent	0.215	$6.81 \times 10^{-3}$

relative particle diameter, *R* (ratio of particle diameter to cylinder diameter;  $d_p/d_c = 8.67 \times 10^{-3}$ ) and the specific gravity, *s* (ratio of particle density to the density of the fluid,  $\rho_f$ ;  $\rho_p/\rho_f = 1.6$ ), were held constant. Conversely, *Stk* varied from  $4.01 \times 10^{-4}$  to  $6.81 \times 10^{-3}$  as a function of  $Re_c$  based on the flow chamber velocities (Table 2). This range of  $Re_c$  represents flow regimes ranging from attached vortices to fully turbulent conditions characterized by flow instabilities, random fluid motion and the presence of a turbulent wake downstream of the collector; this is reflected in the predicted Strouhal number (*St* =  $fd_c/U$ , where *f* is the vortex shedding frequency) for a

circular cylinder (data digitized from figure 5.2 in White, 2011; also see Sumer and Fredsøe, 2006; Table 2). They also span the range of ecologically relevant  $Re_o$  which are intermediate between creeping and potential flow (Palmer et al., 2004; Krick and Ackerman, 2015).

Observations of collector motion were made using an iPhone 6 camera (8 megapixels, Apple Inc.) placed on the plexiglass plate supported by the side walls of the flow chamber directly above the collector (240 frames per second). Data from the video recordings, displayed on a computer monitor (30 cm  $\times$  45 cm), were digitized manually to characterize collector

motion at each  $Re_c$ . Specifically, these included: (1) the maximum amplitude in the transverse direction relative to  $d_c$  (%); (2) the maximum deflection in the longitudinal direction relative to  $d_c$ (%); and (3) the oscillation frequency (f) in the transverse direction (Hz) to determine the observed Strouhal number for the moving collector. Additional 60 s video recordings were made through the side wall of the flow chamber to determine the longitudinal motion of the collector from an orthogonal perspective.

Degassed tap water was carefully added to the recirculating flow chamber before the collector, which was coated with <0.1 mm of silicon grease to retain particles, was placed in the flow chamber at the test location, i.e., at x = 143 cm downstream. A ~ 15 mL solution of distilled water and 0.5 g of CONDUCT-O-FIL particles was carefully poured into the outlet of the test chamber and time, t =0 was dictated when the particles reached the collector. Once the experiment concluded (t = 300 s) the model was enclosed in a watertight plexiglass casing to facilitate removal and photography of its front, back and side portions of the observation region (Figure 1) using a digital camera (Nikon 1 J1; Nikon, Tokyo, Japan) attached to a stereomicroscope (Nikon SMZ-2T). The flow chamber was thoroughly cleaned after each trial to ensure that no residual particles remained in system. A randomized design was used to choose materials and  $Re_c$ ; 5 replicates were obtained.

Images were uploaded into Adobe Photoshop Creative Cloud version 14.0 and overlaid with a transparent counting grid. The number of particles was counted manually, and particles that fell on the dividing lines of the grid were counted in the segment to the right. The particle counts (N) were normalized by the area of the grid ( $A_c$ ) given by

$$A_c = \frac{1}{2} H d_c \pi \tag{5}$$

where H is the height of the grid cell;  $A_c$  was used to determine the particle count per unit area ( $N_c$ )

$$N_c = \frac{N}{A_c} \tag{6}$$

The settlement of particles through the 300 s trial was measured directly by determining the particle concentration (via a hemocytometer) in ~5 mL water samples taken from a depth of ~1.5 cm at the test location (x = 143 cm downstream) at t = 0, 60, 120, 180, 240 and 300 s for each  $Re_c$ . Particle settling rates were determined from the slope of the particle concentration vs. time curves at each  $Re_c$ , which were linear ( $R^2 = 0.91 \pm 0.02$  [mean  $\pm$  SE]), ranged between 3 – 4 × 10<sup>8</sup> particles m<sup>-3</sup> s<sup>-1</sup> and did not differ among  $Re_c$  (Analysis of Variance [ANOVA] of particle concentration at t = 300:  $F_{4, 10} = 0.55$ , p = 0.740). Consequently, the measured value of the particle concentration at t = 150 s ( $C = (1.26 \pm 0.08) \times 10^{11}$  particles m<sup>-3</sup>; n = 5) was used to determine the particle flux.

Control experiments were conducted to determine whether particle capture varied among collectors, which was necessary because it was not possible to obtain a single material with the range of nominal flexibility used in this research. Experiments were conducted using a 7-cm collector length to facilitate the restriction of its movement using a bulldog clip (1.5 cm wide). The clip was clamped at the top of the collector (above the water surface) and tension was applied (upward) to prevent oscillations from occurring. The data were obtained in the same manner as described above.

#### 2.1 Statistical analysis

Three separate fixed effect Analysis of Covariance (ANCOVA) models were used to examine the effect of collector flexibility (independent variable) on relative amplitude in the transverse direction, the relative deflection in the longitudinal direction, and the oscillation frequency in the transverse direction, respectively (response variable), and using  $Re_c$  as a covariate. The particle capture data were analyzed using a mixed model ANCOVA to determine the effect of collector flexibility (independent variable) on particle capture efficiency (response variable) using Rec as a covariate. The response variable (particle capture efficiency) was  $log_{10}$  (x<sup>2</sup>) transformed to meet the assumptions of normality and homogeneity of variance. ANOVA was used to analyze the effect of collector material on particle capture efficiency separately for the control experiments conducted at  $Re_c = 149$  and  $Re_c = 508$ . Tukey's Honest Significant Difference test was used to examine pairwise differences when significant factors were found. All statistical tests were completed using a probability of error rate,  $\alpha = 0.05$  in SAS (version 9.4).

# **3** Results

#### 3.1 Collector motion

The flexible collectors moved in response to the flow and this motion generally increased with increasing collector Reynolds number ( $Re_c$ ), in contrast to the stationary collector (Stainless steel), which did not exhibit motion (Figures 2, 3). Motion in the longitudinal plane was characterized as a deflection in which the collectors bent downstream under steady state conditions (constant velocity and pressure) and curvature was noted in the most flexible collectors at the higher  $Re_c$  (Supplementary Figure S2). Motion in the transverse plane was oscillatory in nature and could be characterized by the amplitude and frequency of the motion.

The total deflection of the collector in the longitudinal direction ranged from 0% to >135% relative to the collector diameter ( $d_c$ ) as measured above the collector (Figure 2 and Supplementary Figure S2). The magnitude of the deflection was more pronounced as the flexibility (i.e., lower E) of the collector increased and at higher  $Re_c$ ; i.e., VITON > BUNA > LKPE > HDPE for  $Re_c \ge 149$ , and VITON deflected by 135.3%  $\pm$  0.6% at  $Re_c = 508$  (Figure 2A). The pattern in the magnitude of the deflection measured from the side of the collectors was consistent with this description (compare hollow vs. solid symbols in Figure 2A) as was the angle of the deflection with respect to the vertical (Figure 2B). Statistically significant differences were detected among collectors for flexibility (ANCOVA  $F_{4, 19} =$ 5.19, p = 0.005) and the collector Reynolds number (covariate; F<sub>1</sub>,  $_{19} = 14.94$ , p = 0.001). In this case, significant pairwise differences were detected between VITON and HDPE (p = 0.008) and between VITON and the stationary collector (p = 0.007).



Characteristics of the longitudinal motion of elastic collectors vs. collector Reynolds numbers ( $Re_c$ ): (A) Maximum deflection in the longitudinal direction relative to  $d_c$  measured from above the collector (solid symbols; mean  $\pm$  SE, n = 5) and from the side (hollow symbols); and (B) Maximum angle of deflection from the vertical measured from the side. Legend: Stationary collector = stainless steel rod encased in heat-shrink tubing (E = 200 GPa;  $\rho = 7.85 \times 10^3$  kg m<sup>-3</sup>); HDPE = High Density Polyethylene (E = 1.0 GPa;  $\rho = 0.97 \times 10^3$  kg m<sup>-3</sup>); LDPE = Low Density Polyethylene ( $E = 10^{-2}$  GPa;  $\rho = 1.35 \times 10^3$  kg m<sup>-3</sup>); BUNA = BUNA rubber ( $E = 10^{-2}$  GPa;  $\rho = 1.35 \times 10^3$  kg m<sup>-3</sup>); and VITON = Viton fluoroelastimer ( $E = 10^{-3}$  GPa;  $\rho = 1.80 \times 10^3$  kg m<sup>-3</sup>).

The amplitude of the collector deflection in the transverse direction ranged from 0% to >70% relative to  $d_c$  (Figure 3A). In general, the magnitude of the amplitude of the collectors increased with flexibility (i.e., lower E) and as  $Re_c$  increased (i.e., VITON > BUNA > LDPE > HDPE for  $Re_c \ge 299$ ). Statistically significant differences were detected among collectors ( $F_{4, 19} = 7.15, p = 0.001$ ) and the covariate was also significant ( $F_{1, 19} = 40.04$ , P = <0.001). Significant pairwise differences were detected between each of the flexible collectors and the stationary collector (p < 0.027). The frequency of oscillation of the flexible collectors expressed as Strouhal number (St) followed a similar pattern to what is reported above in terms of magnitude of the response and relationship with increasing Reo however the ranking changed with BUNA > VITON > LDPE > HDPE for  $Re_c$  > 299 (Figure 3B) perhaps due to the greater deflection in VITON. Statistically significant differences were detected among collectors (F<sub>4, 19</sub> = 9.11, p = 0.003) and the covariate (Re<sub>c</sub>) was significant (F<sub>1, 19</sub> = 32.05, p = 0.001). Significant pairwise differences were detected in the response between VITON, BUNA and LDPE and the stationary collector (p < 0.009) and between BUNA and HDPE (p = 0.035).

#### 3.2 Collector capture efficiency

The particle capture efficiency  $(\eta)$  declined by an order of magnitude across the range of Rec examined for all types of collectors (i.e., 0.3%–0.6% at  $Re_c = 30$  vs. 0.03%–0.06% at  $Re_c =$ 508; Figure 4A). Whereas the pattern was similar among collectors, HDPE and LDPE had consistently lower  $\eta$  compared to the more flexible collectors (BUNA and VITON) and the stationary collector. Only at the highest  $Re_c$  did  $\eta$  of BUNA appear to exceed that of the stationary collector. Statistically significant differences among collectors were detected ( $F_{4, 119} = 2.46$ , p = 0.049), and  $Re_c$  was a significant covariate ( $F_{1, 119} = 168, p = 0.001$ ). In this case, significant pairwise differences (p < 0.001) were detected between collectors in the higher  $\eta$  group (BUNA, VITON, and stationary collector) and collectors in the lower  $\eta$  group (HDPE and LDPE). Distinction among the collector types was evident when  $\eta$  was plotted vs. the non-dimensional stiffness (k') (Figure 4B). In this case, the curves for each collector type were somewhat parallel with clear separation and ranking matching the Young's modulus of the collector. Two important distinctions were, however, evident: (1) there was overlap among collector curves at given k' values (e.g., HPDE, LDPE and



Characteristics of the transverse motion of elastic collectors vs. collector Reynolds numbers ( $Re_c$ ): (A) Maximum amplitude in the transverse direction relative to collector diameter ( $d_c$ ); and (B) observed Strouhal number of the collector oscillation frequency in the transverse direction (mean  $\pm$  SE, n = 5).

BUNA at  $k' \sim 10^{-1}$ ); and (2) collector efficiency ( $\eta$ ) for BUNA and VITON were greater than those for the stationary collector when  $Re_c > 299$ -the left-most point in each curve.

The spatial pattern of capture (Eqs 5, 6) can provide insight into the mechanism of particle capture. Particles were captured circumferentially around collectors at the lowest  $Re_c = 30$  with moderately higher capture at 90° and 270°, i.e., 90° from the stagnation point (=0°), for both the stationary collector and VITON, the most flexible collector (Figure 5). The average particle captured increased by ~50% at the highest  $Re_c = 508$  for both collectors (47% ± 7% and 52% ± 8% for stationary collector and VITON, respectively) but the pattern differed. The increase in particle capture on the stationary collector was larger restricted to the upstream and to a lesser extent on the downstream sides, whereas particle capture on VITON also increased at 90° on either side of the stagnation point (i.e., 90° and 270°; Figure 5). Similarity on these patterns were observed on the other collectors depending somewhat on their flexibility (data not provided).

No-movement control experiments, in which collectors were held rigid within the flow chamber, were used to determine if the differences among the two groups of collectors identified above were due to material properties of the collectors that may have affected particle capture or particle identification in images. Particle capture efficiency was not uniform among the collectors at  $Re_c = 149$  even though they were stationary in orientation (Figure 6). Rather  $\eta$  were higher and more similar on VITON, BUNA and the stationary collector than on the two polyethylene collectors (Figure 6A). Significant differences in  $\eta$  were found among collectors (ANOVA  $F_{2, 12} = 7.92$ , p = 0.006) and pairwise differences were found between the stationary collector and the HDPE and LDPE collectors (p = 0.023 and p = 0.008, respectively). Similar results in which  $\eta$  was lower on HDPE and LDPE were obtained at  $Re_c = 508$ , but in this case the comparison involved the two polyethylene and stationary collector (Figure 6B). Statistically significant differences in  $\eta$  were detected among collectors (F<sub>2, 11</sub> = 0.0166, *p* < 0.001) and pairwise differences were found between the stationary collector and HDPE and LDPE (p = 0.001, p = 0.003, respectively). On average the HDPE collector captured particles 13.9% ± 0.8% less efficiently relative to the stationary collector and the LDPE collector captured particles  $17.4\% \pm 0.5\%$  less efficiently. These correction factors were used when calculating the relative capture efficiencies between flexible and stationary collectors.



Particle capture efficiency (%) of stationary and flexible collectors measured in a flow chamber versus (A) collector Reynolds number ( $Re_c$ ) and (B) non-dimensional stiffness (k) (mean  $\pm$  SE; n = 5).

#### 4 Discussion

The results of this study demonstrate that the flexibility of a collector (indicated by the Young's modulus, *E*) affects the capture efficiency ( $\eta$ ) of suspended particles from a fluid medium at ecologically relevant Reynolds numbers (Eq. 1), i.e., 30 <  $Re_c$  < 500. Specifically,  $\eta$  appears to be related to the dimensionless stiffness (k'; Eq. 4), which is somewhat comparable to the reciprocal of the Cauchy number (*Ca*, ratio of inertial forces: compressible [elastic] forces; de Langre, 2008). Capture efficiency declined from  $Re_c = 30$  to 299 but remained somewhat higher for the

stiffer collector (Figure 4B), which was more perpendicular to the flow (Figure 2A; longitudinal deflection  $\alpha$  1/*k*'). At higher  $Re_c$ (i.e., >299), however, the flexible collectors had  $\eta$  that were up to 23% higher (BUNA at  $Re_c > 508$ ) than the rigid stationary collector because flexible collectors experienced larger transverse amplitudes (Figure 3A; transverse amplitude  $\alpha$  1/*k*') that resulted in additional particles captured on the sides perpendicular to the flow (Figure 5). These higher  $Re_c$  corresponded to periods when the most flexible collectors had large transverse oscillation frequencies (>4 Hz), and a large relative amplitude (>60% in the transverse direction and >100% in the longitudinal). It is relevant to note that 4 Hz



exceeds the natural frequency ( $f_n$ ; Eq. 3) of the most flexible collector in water. Given these observations, it is likely that the capture efficiency of flexible collectors has been underestimated at ecologically relevant  $Re_c$  using the standard model of a rigid stationary collector.

The material properties of the collector also affect  $\eta$  as was determined in the control experiments. It is likely that part of this difference was due to the difficulty of visualizing bright particles on the polyethylene surfaces, which were white in color relative to the darker grey/black and brown colors of the BUNA, VITON, and stationary collectors, respectively. It is relevant to note that the  $\eta$  measured on the stationary collector were similar to those reported elsewhere (Figure 7). Overall,  $\eta$  of the rigid collector in this study ranged from 0.57% to 0.046% across the Re<sub>c</sub> and these values fall within the range reported in other empirical and computational studies (Figure 7). In general,  $\eta$  increases with the relative particle diameter, R, at these  $Re_c$  (Palmer et al., 2004). The correspondence between our values for rigid stationary collectors (R = 0.087) and consistent observations using Rvalues similar to ours are indicated by grey colored symbols in Figure 7. Our observations appear to be reasonable within this range, although the value for  $Re_c = 30$  is at the higher end of the range than has been reported elsewhere.

To the best of our knowledge, this is the first empirical examination of the effects of flexible moving collectors on particle capture (Figure 8). Capture efficiency declined rapidly with  $Re_c$  in the laminar regime, but the rate of decline decreased for rigid and flexible collectors that experienced motion at higher and turbulent  $Re_c$  relative to stationary rigid collectors. Specifically, the movement of the collector through higher frequency oscillations

lead to increased  $\eta$  in the case of mechanical actuation of rigid collectors (McCombe and Ackerman, 2018) or in terms of both static drag reconfiguration and flow-induced vibration of flexible collectors examined empirically in the present study and modeled previously for a soft coral (Boudina et al., 2021). An estimate of the static drag contribution to deflection was made through the calculation of the drag force on the collector from the quadratic drag equation and using this is determine the deflection of a uniformly loaded cantilever beam. This technique could only be applied to the LDPE collector because it was the only linearlyelastic material with a response. In this case, the maximum observed deflection (%  $d_c$ ) increased from 23%, 33% and 47% at 20, 25 and 34 cm/s, respectively vs. 6%, 9% and 15% increases for the calculated static drag. In other words, an average of  $28\% \pm 2\%$ of the deflection observed on LDPE between 20 and 34 cm/s was estimated to be due to static drag reconfiguration. These empirical studies build on the insight obtained through direct numerical simulations (DNS; Espinosa-Gayossa, 2012; Espinosa-Gayossa, 2013; Espinosa-Gayossa, 2015) and computational fluid dynamic models (CFD; Krick and Ackerman, 2015), respectively. Those models investigated the effects of vortex induced vibrations on particle capture efficiency, however they did not include Young's modulus of the collector (i.e., flexibility) as an experimental parameter. The present study demonstrates that flexibility affects the motion of a collector at each  $Re_{c}$ , which is especially important as the flow region downstream of the collector becomes turbulent ( $Re_c > 299$ ) when vortex induced vibrations are more likely to occur.

The difference in  $\eta$  across *E* may also be understood through the particle Stokes number (*Stk*; Eq. 2). When *Stk* was low (i.e., 10<sup>-4</sup>) the



particles did not have enough momentum to penetrate the collector boundary layer to be captured. At intermediate  $Re_c$  ( $Re_c = 149$  and 299) the *Stk* increased to  $10^{-3}$  and the relative difference in  $\eta$  between the most flexible and less flexible collector decreased. This was likely due to increased relative momentum of the particles with respect to the collector and subsequent penetration of the collector boundary layer caused by collector motion. Flow-induced collector motion leading to oscillations in the transverse direction adds additional momentum to the system making capture more likely at higher Rec. When the system becomes turbulent ( $Re_c = 374$  and  $Re_c = 508$ ), the oscillation frequency of the BUNA collector exceeded 5 Hz and most particles were captured on the upstream surface of the collector. In the case of the VITON, the oscillation frequency was ~4 Hz and the relative amplitude exceeded >60% in the transverse direction and >100% in the longitudinal, leading to more particle capture on the side surfaces of the collector. These results are consistent with those of McCombe and Ackerman (2018) who found that transversely oscillating collectors capture more particles on the downstream and sides of the collector. These results are also supported by the CFD model by Krick and Ackerman (2015), who identified the 'collector chasing' capture mechanism in which a moving collector overtakes a particle. This mechanism is likely responsible for capture on the sides and downstream portion of the collector in this study. Moreover, particles caught in vortices leeward of the collector have high residence times and, therefore, have a higher probability of being captured (i.e., on the downstream side; Shimeta and Jumars, 1991). Higher turbulence (high  $Re_c$ ) and Stokes number (i.e.,  $Stk > 10^{-1}$ ) may lead to higher  $\eta$  through increased encounter rates, but increased relative momentum of such particles would not be relevant because they already have sufficient inertia to penetrate collector boundary layers (Krick and Ackerman, 2015).

There are limitations of this study that may affect the interpretation of the results. Most notable among these is the short length of the collectors used because of the size limitations of the flow chamber. Specifically, the chamber was designed to provide suitable conditions for benthic mass transport studies (e.g., low volume, flow conditioning and entrance length for boundary layer development and fully developed flow, large width to depth ratio to minimize secondary flows [i.e., >3.5], and minimal flow obstruction of channel by the subject of interest; Nowell and Jumars, 1987; Ackerman, 1999).



Comparison of particle capture efficiency ( $\eta$ ) measured on rigid collectors at different collector Reynolds numbers ( $Re_c$ ) in empirical (Palmer et al., 2004; McCombe and Ackerman, 2018) and computational studies (Espinosa-Gayosso et al., 2013; Krick and Ackerman, 2015). Capture efficiency,  $\eta$ , generally increases with the relative particle diameter, R, which is indicated in the legend. Observations using R similar to the present study are indicated by grey colored symbols.



#### FIGURE 8

Comparison of particle capture efficiency ( $\eta$ ) measured on moving collectors at different collector Reynolds numbers ( $Re_c$ ) including flexible ones examined in this study and rigid ones measured (McCombe and Ackerman, 2018) or modeled previously (Espinosa-Gayosso et al., 2012; Krick and Ackerman, 2015). Note that increasing the movement of the collector through higher frequency oscillations leads to increased  $\eta$  in the case of mechanical actuation of rigid collectors or in terms of flow induced vibration of flexible collectors. Consequently, a collector length of 3.75 cm ( $l_c = 0.0375$  m) was used. This limited the  $f_n$  of the collectors to relatively large values, which decline non-linearly with increases in  $l_c$  (i.e.,  $l_c^{-2}$ ); the  $f_n$  of longer collectors would occur at higher frequency and thus have relatively more motion under these hydrodynamic conditions. In addition,  $l_c$  likely limited the movement of the collector to more rigid-like oscillations and deflections without any large flow induced bends or curvature observed in longer collectors in nature (de Langre, 2008). The effect of such large flow induced morphological changes in flexible collectors on particle capture efficiency,  $\eta$ , is unknown, but would likely be relevant to  $\eta$  because they represent large-scale motions, which have been shown to increase  $\eta$ . Certainly, there is considerable opportunity for future studies involving particle capture.

# **5** Conclusion

The results of this study indicate that the flexibility of a collector affects its ability to capture suspended particles once the flow regime around the collector leads to larger-scale hydromechanical responses. Specifically, enhanced particle capture efficiency,  $\eta$ , occurs once turbulent flow leads to a collector oscillation frequency transverse to the flow direction >4 Hz along with a relative amplitude >60% of the collector diameter in the transverse and >100% in the longitudinal direction. A variety of mechanisms are responsible for particle capture in nature including direct interception, inertial impaction as well as capture on lateral surfaces and collector chasing due to flow induced vibrations. These results should provide a better understanding of how freely moving flexible collectors capture particles due to vortex induced vibrations at ecologically relevant collector Reynolds numbers. Ultimately it should be possible to better understand the complexity of biological collectors and hence particle capture processes in aquatic and terrestrial environments.

### Data availability statement

The original contributions presented in the study are included in the article/Supplementary Material, further inquiries can be directed to the corresponding authors.

# Author contributions

KS: Data Analysis, curation. Formal Investigation. Methodology, Visualization, Writing-original draft, Writing-review and editing. MH: Methodology, Validation, Writing-review and editing. JDA: Conceptualization, Formal Analysis, Funding acquisition, Methodology, Project

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# Conflict of interest

The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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# Supplementary material

The Supplementary Material for this article can be found online at: https://www.frontiersin.org/articles/10.3389/fmech.2024.1411361/ full#supplementary-material

#### SUPPLEMENTARY FIGURE S1

Characteristics of the hydrodynamic conditions in the flow chamber at the location at which the collector was placed. Flow profiles are based on the 1/ 7th power law solution for a turbulent flat plate boundary layer. Symbols represent measured values obtained at heights of 2.5, 3.5 and 4 cm above the bottom at 5, 10 and 25 cm s<sup>-1</sup> (data were not obtained at the other chamber velocities).

#### SUPPLEMENTARY FIGURE S2

Drawing of the maximum longitudinal deflection of collectors at different collector Reynolds numbers as viewed from the side of the flow chamber (flow is from left to right). The neutral position of the collector is indicated by dashed lines. Collectors are 0.15 cm in diameter ( $d_c = 1.5$  mm).

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