



## A New Architecture of Morphing Wing Based on Hyperelastic Materials and Metastructures With Tunable Stiffness

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Morphing wings with the ability of shape changing may enlarge the flight envelop of air vehicles. This is particularly important for small-scale aircrafts demanding maneuverability and adaptability in dynamic environments. However, to design a shape-changing mechanism suitable for small drones is very challenging due to extreme requirements raised by dimensional constraint, actuating limits, and weight restriction in Micro Air Vehicles (MAVs). A novel design method of morphing wings is proposed for smallscale aircrafts in this paper. The morphing wing is composed of a heterogeneous architecture, including three components: a longitudinal spar with pneumatic actuators, chordwise stiffening ribs with cable-driven metastructures, and a compliant skin. Through employing both pneumatic networks with hyperelastic behavior and modified pantographic metastructures with tunable stiffness, structural deformation along both spanwise and chordwise. Mechanical behaviors of this morphing wing were investigated thoroughly by theorical analysis, numerical verification, and experimental validation. Theorical predictions agree well with the results of 3D Finite Element Method (FEM). With optimal design determined through design of experiment (DOE) and FEM, prototyped morphing wings were fabricated accordingly. The aerodynamic performance was examined by a wind tunnel test with a Particle Image Velocimetry (PIV) instrument. Results demonstrate the efficiency and capacity of this morphing wing to adjust aerodynamic layout of aircraft in a low-speed airflow environment. This proposed design provides a promising solution applicable to small-scale aircrafts with morphing wings.

Keywords: micro air vehicles (MAVs), morphing wing, pneumatic networks, hyperelastic materials, metastructures with tunable stiffness

#### **1 INTRODUCTION**

Micro Air Vehicles (MAVs) have advantages of good maneuverability, high portability, and outstanding invisibility compared with regular size aircrafts (Ward et al., 2017). As a class of miniature Unmanned Aerial Vehicles (UAVs), MAVs are more suitable for complex environments and prospectively applied in both civil (Ettinger et al., 2003) and military missions (Davis et al., 1996). Since the concept of MAVs emerged, many scholars have investigated this area (Ifju et al., 2002; Pérez-Arancibia et al., 2011; Graule et al., 2016). However, pursuit of miniaturization and light weight may cause aircrafts to be susceptible to gusts and unstable airflow (Galiński and Żbikowski,

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2007; Lian, 2009). Triumphing over these shortcomings, morphing wings to dynamically adjust shape is an effective way to improve flight performance during different flight phases (Shyy et al., 2008; Ahmed et al., 2011).

Originally, conventional actuation of deformable airfoils is based on mechanical transmission devices such as gears, motors, and hinges. These conventional mechanisms may cause weight penalties and discontinuities to the aerodynamic structure. The disjointed skins may lead to abrupt changes in pressure, producing negative impacts on aerodynamic performance of aircrafts (Barbarino et al., 2011). However, a wing morphing with smooth and continuous change requires a deformable and integrated structure to replace conventional mechanism. It is highly demanded to adjust aerodynamic layout of aircrafts without compromising flight performance (Joo et al., 2015). This concept is also widely accepted to be a promising solution to design of small-sized engines, robotics, or drones (Zhao et al., 2018; Chen et al., 2019).

Extensive research focusing on morphing wing design has been conducted. A deformable wing was developed by employing PBP (post-buckled precompressed) actuators (Vos et al., 2007). This actuator was piezoelectric and distributed along wing span to achieve rolling control for UAVs. A novel flexible-rib system was designed to improve flight performance of small UAVs (Meguid et al., 2017). This mechanism was actuated by a servomotor and used to adjust the camber with accurate deformability. Another morphing wing composed of artificial feathers with folded and deployed configurations was introduced (Di Luca et al., 2017). Their works showed that this design may extend the flight envelope of small drones and asymmetric folding of wings may be used for rolling control of aircrafts. Bilgen et al. (2007) designed a morphing wing adopted for MAVs using macro fiber composites. Compared with traditional control surface, macrofiber-composite actuators were more efficient and produced less drag in controlling the roll and pitch maneuvers of MAVs. A compliant polymorphing wing driven by stepper motors was designed for small UAVs to achieve both chord and camber morphing (Muhammed, 2020). With a pre-tensioning skin, the wrinkling instability of wing was suppressed. Obviously, compliant mechanism with potential advantages of light weight and continuous deformable surface is suitable for small-scale morphing structures.

Made of elastomeric materials, soft pneumatic actuators (SPAs) are well adopted for applications demanding high compliance and light weight (Sun et al., 2013). Inspired by mollusca and biological tissue, SPAs are generally constructed as an integral structure (Polygerinos et al., 2015). Owing to smooth and bionic motion, this actuator has been developed for swimming robot (Suzumori et al., 2007), soft glove for hand rehabilitation (Polygerinos et al., 2013), and multi-gait soft robot (Shepherd et al., 2011). Diversified configuration of embedded chambers may give rise to multiple modes of motions, such as bending, twisting, and extending/contracting (Polygerinos et al., 2015). For example, a related design called pneumatic networks (PneuNets) was investigated by Whitesides group (Ilievski et al., 2011; Mosadegh et al., 2014). This structure contains a series of parallel chambers and its bending motion is realized through the

different extent of material stretching. When inflated, the uneven distribution of materials causes the thinner or softer part to be stretched more easily and bends a thick or hard one. Employing PneuNets fabricated with low-modulus elastomers, the actuator can be actuated at relatively low pressure.

In addition, metamaterial or metastructure is a class of synthetic materials and its macroscopic properties can be artificially controlled to obtain a new type of material or structure with exotic properties, such as mechanical metamaterial, acoustic metamaterial, and thermal metamaterial (Harne et al., 2016). The special properties of metamaterial or metastructure are achieved by engineering its cellular architecture and chemical composition (Cui et al., 2010). Among them, pantographic structure presents considerable freedom to tune the multiaxial stiffness (Dell'Isola et al., 2016). This structure is composed of orthogonal beams interconnected to each other by cylinders called pivots (Seppecher et al., 2019). Its stiffness is tailorable by sizing the dimensions of beams or pivots. A morphing structure achieved via a configuration of pantographs was proposed (Saeed and Kwan, 2014).

In this paper, a novel architecture of morphing wings for MAVs is represented. The proposed design adopted soft actuators with hyperelastic PneuNets and pantographic metastructures to achieve seamless and continuous deformation in both spanwise and chordwise directions. The wing contains a longitudinal pneumatic spar, chordwise stiffening ribs, and a compliant skin covering on top of both spar and ribs. The spar filled with PneuNets may bend in spanwise actuated pneumatically. A set of ribs composed of modified pantographic metastructures may deflect the trailing-edge actuated by cables. The actuating control along both spanwise and chordwise directions are decoupled and accurately parametrized. Through a set of optimizations with design of experiment (DOE), the maximum morphing capacities can be achieved at  $\pm 12^{\circ}$  angular deflection in spanwise and ±35° angular deflection in chordwise. A wind tunnel test with a Particle Image Velocimetry (PIV) instrument was finally conducted to examine the aerodynamic performance of such a morphing wing in a low-velocity flow field.

The paper is divided into six sections. In Section 2, conceptual design and fabrication of morphing wing are described. In Section 3, analytical derivations of two morphing mechanisms based on the energy principles are presented. Then, the verification of analytical models of both SPAs and modified pantographic metastructures are addressed using Finite Element Method (FEM). In Section 4, sensitivity analysis of structural dimensions on morphing performance are investigated through DOE and an optimal configuration of such a morphing wing is obtained based on FEM. In Section 5, experiments to examine actuation behaviors, load bearing capacities, and aerodynamic responses are provided. Finally, conclusions about this work are outlined in Section 6.

# 2 CONCEPTUAL DESIGN AND PROTOTYPE FABRICATION

#### 2.1 Architecture of Morphing Wing

In this section, both design logic and prototype manufacturing including material properties of this morphing wing are



introduced. NACA 0012 with a symmetrical configuration is chosen as the airfoil of morphing wings for the consideration of bidirectional control. NACA airfoils are airfoil shapes developed by the National Advisory Committee for Aeronautics (NACA). The shape of the airfoil is described by four digits following the word "NACA." For NACA 0012, "00" means this airfoil has no camber and "12" indicates that its maximum thickness is equal to 12% of chord length. As shown in Figure 1A, the morphing wing proposed in this paper contains two critical components: a pneumatic spar realizing spanwise bending and cable-driven metastructure realizing chordwise bending. A bidirectional SPAs with PneuNets is used to design the spar with the capability of switching from dihedral to anhedral. The spar length is 50% of chord size. This structure is a combination of two symmetrical actuators sharing a middle layer to yield bidirectional deflection.

The trailing-edge is built by three modified pantographic ribs seamlessly covered by a layer of soft skin with the same material as the spar. The ribs are jointed with the pneumatic spar by adhesives. Legacy configuration of pantographic metamaterial is asymmetric, and out-of-plane distortion occurs when a side force is applied. Thus, a new pantographic structure is proposed in this work by adding a mirroring portion, as shown in **Figure 1B**. As a mechanical metastructure, this pantographic structure possesses anisotropic stiffness property (Dell' Isola et al., 2019). It is flexible chordwise but stiffer spanwise. This property may meet the requirements of both stiffness to morph chordwisely and strength to bear aerodynamic loads. Overall, both continuous and smooth deformation are obtained along spanwise and chordwise directions.

## 2.2 Material Behaviors and Fabrication

In this paper, a platinum cured silicone, Dragon Skin 30 (produced by Smooth-On; http://www.smooth-on.com), was adopted for preparing SPAs and flexible skin of the morphing wing. Its fracture strain is up to 364%. As a silicone rubber, its mechanical behavior is typically hyperelastic, which is nonlinear in tension and nearly incompressible in compression. The constitutive model of hyperelastic material can be derived through a strain energy density function:

$$\boldsymbol{W} = \boldsymbol{W}(\mathbf{I}_1, \mathbf{I}_2, \mathbf{I}_3) \tag{1}$$

**TABLE 1** | Material properties of modified pantographic ribs.

Hardness	79 D
Tension yield strength	35 Mpa
Fracture elongation	6–9%
Elastic Modulus	2,370–2,640 Mpa

where  $I_1$ ,  $I_2$ , and  $I_3$  are strain invariants of the right Cauchy-Green deformation tensor (Arruda and Boyce, 1993), which are functions of the principal stretches:

$$\begin{cases} \mathbf{I}_{1} = \operatorname{tr}(\mathbf{B}) = \lambda_{1}^{2} + \lambda_{2}^{2} + \lambda_{3}^{2} \\ \mathbf{I}_{2} = \frac{1}{2} \left[ (\operatorname{tr} \mathbf{B}) - \operatorname{tr}(\mathbf{B}^{2}) \right] = \lambda_{1}^{2} \lambda_{2}^{2} + \lambda_{2}^{2} \lambda_{3}^{2} + \lambda_{3}^{2} \lambda_{1}^{2} \\ \mathbf{I}_{3} = \operatorname{det}(\mathbf{B}) = \mathbf{J}^{2} = \lambda_{1}^{2} \lambda_{2}^{2} \lambda_{3}^{2} \end{cases}$$
(2)

In this expression, **B** is left Cauchy-Green deformation tensor and  $\lambda_i$  (i = 1,2,3) is principal extension ratio. For an incompressible material,  $\lambda_1\lambda_2\lambda_3 = 1$ . There are various forms of constitutive models of hyperelastic material. Here, a second order reduced polynomial model, Yeoh model, was chosen to describe stress-strain relationship of the elastomer in this paper. The advantages of this model are due to its simplicity and wide range of application for elastomers. It often provides an accurate fit over a large strain range based on uniaxial test data (Ali et al., 2010). The constitutive model form is expressed as:

$$W = C_{10} \left( \mathbf{I}_{1} - 3 \right) + C_{20} \left( \mathbf{I}_{1} - 3 \right)^{2}$$
(3)

where  $C_{10}$ ,  $C_{20}$  are constants relative to material and determined by uniaxial tests.

The Cauchy stress for the Yeoh model is given as:

$$\boldsymbol{\sigma} = -p\boldsymbol{I} + 2\frac{\partial \boldsymbol{W}}{\partial \mathbf{I}_1}\boldsymbol{B}$$
(4)

For uniaxial elongation, there are:  $\lambda_2^2 = \lambda_3^2 = 1/\lambda_1$  and  $\sigma_{22} = \sigma_{33} = 0$ , then the following equation is obtained:

$$\boldsymbol{\sigma}_{11} = 2\left(\lambda_1^2 - \frac{1}{\lambda_1}\right) \frac{\partial \boldsymbol{W}}{\partial \mathbf{I}_1}$$
(5)

By submitting **Eq. 3** into **Eq. 5**, the function of stresselongation can be derived. Uniaxial tensile tests were performed using dumbbell coupons at a rate of 500 mm/min. And test data were fitted to Yeoh model numerically. Finally,  $C_{10}$ and  $C_{20}$  were calculated as 0.117 and -0.0006865 respectively.

The large deformation of modified pantographic metastructure comes from the accumulation of small elastic deformation out of each structural member. Thus, a resin material with high strength and toughness was used to fabricate pantographic ribs. Properties of the material are given in **Table 1**.

Lost-Wax casting is a general method for duplicating metal products. This casting idea can be used as a fabrication process to manufacture fluidic elastomer actuators (Marchese et al., 2015). In this work, molds for casting elastomeric components of the morphing wing are divided into two types, including both resin and wax molds. Resin molds are used for molding exterior shape of the morphing wing and can be prepared by 3D printer. Wax molds, made of paraffin wax with low melting point, can change phases from solid to liquid at around 70°C. It is used to fabricate wax products forming inner channels of SPAs. After the elastomer is cured, the whole part is put into the oven. The wax is melted into fluid and flowed out through the molded channels. This process realizes an integrated manufacturing with good airtightness and produces good quality of wing surfaces.

The manufacturing process of pneumatic spar and skin is depicted in **Figure 2A**. Firstly, Part A and Part B of silicones are taken 1:1 by weight and mixed thoroughly for 3 min in a mix container. Secondly, the liquid mixture is poured into resin molds and vacuum degassing is adopted to eliminate the trapped air in the mixture. After 15 min of vacuum, the wax mold is inserted into liquid rubber slowly. Resin molds are designed with grooves to position the wax mold. Then the whole molds are placed in a thermostatic container. The whole part is cured fully at 30°C for 16 h at first. Then bake at 100°C for 30 min to let the wax melt.

Three modified pantographic ribs were manufactured by 3D printer. They are inserted into the trailing edge section and glued onto the skin and spar with adhesives. A fabricated prototype of the morphing wing is shown in **Figure 2B**.

#### **3 ANALYTICAL MODELS**

#### 3.1 Spar With Hyperelastic PneuNets

To simplify analytical modeling, it's assumed that the change of height along chordwise is small and negligible. Then the actuator can be treated as a cuboid structure. The 3D model and crosssection view of the pneumatic actuator are shown in **Figure 3**. Taking nonlinearity and incompressibility into consideration, relationship among structural parameters, air pressure, and deflecting angle of elastomeric actuator is derived based on the energy principle.

The bending of the actuator is caused by different stretching extent of walls in the unit cell, and it's assumed that the actuator bends curvedly by pressurizing upper chambers and unpressurizing lower chambers, and vice versa. The bottom wall is assumed to be bended and its length remains unchanged. Strain energy of a loaded bidirectional spar with PneuNets can be decomposed as:

$$U_{tot} = U_t^s + U_m^s + U_{s1}^s + U_{s2}^s + U_b^b$$
(6)

In this expression,  $U_t^s$  and  $U_m^s$  represent strain energies of top walls and the middle layer induced by inflation.  $U_{s1}^s$  represents the stretching energy about side walls separating chambers and its thickness is set as  $l_{s1}$  in **Figure 3**.  $U_{s2}^s$  represents the stretching energy of side walls paralleling to *y*-*z* plane and its thickness is denoted by  $w_{s2}$ .  $U_b^b$  is the bending energy of bottom wall in unpressurized chambers.

Other geometric dimensions of a unit cell of the actuator are illustrated in **Figure 3**. Length and width of cavity are denoted by  $l_c$  and  $w_c$ . Height of top wall, cavity, and middle layer are denoted by  $h_t$ ,  $h_c$  and  $h_m$  respectively. It should be noted that stretch ratio of the side wall paralleling to *y*-*z* plane varies linearly with height h and an average value is adopted here for analytical modeling. According to geometry depicted in **Figure 3**, there is:



FIGURE 2 | (A) Molding process of spar and skin; (B) A fabricated prototype of the morphing wing.

$$\begin{cases} \frac{\lambda_t l}{\vartheta_1} = \frac{l}{\vartheta_1} + 2h \\ \lambda_m = \overline{\lambda_{s2}} = \frac{\lambda_t + 1}{2} \end{cases}$$
(7)

where  $h = h_t + h_c + h_m/2$ ,  $l = l_c + l_{s1}$ .  $\lambda_t$  and  $\lambda_m$  are the stretch ratios of top walls and middle layer.  $\overline{\lambda_{s2}}$  is the averaged stretch ratio of the side wall paralleling to *y*-*z* plane.

According to the force equilibrium for longitudinal and transverse sections (presented by yellow dash line in B-B section in **Figure 3**), there is:

$$\begin{cases} Ph_c w_c = \sigma_t h_t w + \sigma_m h_m w_c + 2\overline{\sigma_{s2}} (2h - h_t) w_{s2} \\ Pl_c w_c = \sigma_{s1} l_{s1} w_c \end{cases}$$
(8.1)

Small deformation assumption is adopted here to linearize the nonlinearity of hyperelastic material. Combining two equations in **Eq. 8.1**, relationship between stress of the side wall separating chambers and top wall is calculated as:

$$\frac{\sigma_{s1}}{\sigma_t} = \frac{l_c \left[ h_t w + 0.5 h_m w_c + (2h - h_t) w_{s2} \right]}{l_{s1} h_c w_c}$$
(8.2)



Then according to **Eq. 8.2**, relation between stretch ratio of the side wall separating chambers and top wall is given as:

$$\lambda_{s1} = K^* (\lambda_t - 1) + 1 \tag{8.3}$$

where  $K^* = \frac{l_c [h_t w + 0.5 h_m w_c + (2h - h_t) w_{s2}]}{l_{s1} h_c w_c}$ .

Combining Eq. 7 and Eq. 8.3 into Eq. 6, each term of strain energy is represented as:

$$\begin{cases} U_{t}^{s} = V_{t}C_{10}\left(\lambda_{t}^{2} + \frac{1}{\lambda_{t}^{2}} - 2\right) + C_{20}\left(\lambda_{t}^{2} + \frac{1}{\lambda_{t}^{2}} - 2\right)^{2} \\ U_{s1}^{s} = V_{s1}C_{10}\left(\lambda_{s1}^{2} + \frac{1}{\lambda_{s1}^{2}} - 2\right) + C_{20}\left(\lambda_{s1}^{2} + \frac{1}{\lambda_{s1}^{2}} - 2\right)^{2} \\ U_{s2}^{s} = V_{s2}C_{10}\left(\overline{\lambda_{s2}}^{2} + \frac{1}{\overline{\lambda_{s2}}^{2}} - 2\right) + C_{20}\left(\overline{\lambda_{s2}}^{2} + \frac{1}{\overline{\lambda_{s2}}^{2}} - 2\right)^{2} \\ U_{m}^{s} = V_{m}C_{10}\left(\lambda_{m}^{2} + \frac{1}{\lambda_{m}^{2}} - 2\right) + C_{20}\left(\lambda_{m}^{2} + \frac{1}{\lambda_{m}^{2}} - 2\right)^{2} \\ U_{b}^{b} = \frac{E\kappa^{2}h_{t}^{3}lw}{24(1 - \gamma^{2})} \end{cases}$$
(9)

In this expression,  $\kappa$  is curvature and *E* is equivalent modulus obtained from fitting of the experimental data.

Due to incompressibility, the volume of hyperelastic material remains unchanged during deformation. Thus, volume of pressurized cavity can be approximated by:

$$V_c = V - V_e = \frac{(\lambda_t + \lambda_m)lhw}{2} - (lhw - l_ch_cw_c)$$
(10)

where V is the total volume of exterior envelope of the pressurized unit cell.  $V_e$  is the material volume of elastomer.

According to the principle of virtual work:

$$P\delta V_c = V_t \delta U_t^s + V_{s1} \delta U_{s1}^s + V_{s2} \delta U_{s2}^s + V_m \delta U_m^s + V_b \delta U_b^b \quad (11)$$

Analytical relation between applied pressure *P* and bending angle  $\vartheta_1$  can be obtained by taking the derivative of **Eq. 11** with respect to  $\vartheta_1$ .

The cumulative bending angle of actuators with N unit cells in series along the span direction is calculated as:

$$\phi_1 = N\vartheta_1 \tag{12}$$

The above equations can be used to calculate air pressure P required to achieve bending angle  $\phi_1$  at a certain configuration. This formula is applicable in a condition that  $l_c$  is smaller than  $h_c$ . Otherwise, top wall of chambers more likely undergoes a ballooning deformation instead of uniaxial stretching.

## 3.2 Rib With Modified Pantographic Metastructures

The modified pantographic structure is created by an array of repeated unit cells. As shown in **Figure 4A**, each unit is composed



of three staggered rectangular shafts (grey) connected by cylindrical shafts (blue and black). When a torque M is applied to the cantilevered end, the whole structure bends. This deflection is caused by the accumulation of small deformation in each structural member of unit cell, including rotation of blue shafts and bending of grey shafts. Black shafts connecting midpoints of three staggered rectangular shafts strengthen the structural stability and lateral stiffness. Obviously, geometric dimensions of rectangular and cylindrical shafts are primary factors determining the stiffness of the modified pantographic metastructure.

Firstly, in order to model its deformation theoretically, three assumptions are made as follows:

- (1) Only torsion and pure bending occur in structural members under the action of external torque *M*;
- (2) Simple stress states are assumed in structural members. Blue cylindrical shafts are torsional bars. Grey rectangular shafts and black cylindrical shafts are treated as beams under pure bending;
- (3) Deformation of torsional shafts is consistent in each unit cell.

Under these assumptions, the loading-deflection behavior of pantographic rib is derived as follows. Considering the left end of the overall structure is fixed, there is no torsion of blue shafts in the first unit. The ends of black shafts are located at the midpoint of two adjacent grey shafts. Thus, black shafts deflect when projections of the midpoints on *y*-*z* plane are eccentric. It should be noted that shifts of the midpoints are induced by bending of grey shafts or torsion of blue shafts, as shown in **Figure 4B**. In the first unit, deflection  $w_{ms}^1$  of black shafts is only induced by bending of grey shafts and calculated as:

$$w_{ms}^{1} = 2w_{rs}sin\frac{\alpha}{2} = \frac{\theta_{rs}l_{rs}}{4}sin\frac{\alpha}{2}$$
(13.1)

where  $w_{rs}$ ,  $l_{rs}$ , and  $\theta_{rs}$  are the deflection, length, and angular deflection of rectangular shaft.  $\alpha$  is the angle of two intersecting rectangular shafts.

As for  $i_{th}$  unit (i > 1), angular rotation of blue shafts leads to the rigid body rotation of grey shafts and its influence on midpoints shifting is greater than the one induced by grey shafts bending. Therefore, to consider rigid body rotation of grey shafts only, deflection  $w_{ms}^i$  (for i > 1) of black shafts can be derived as:

$$w_{ms}^{i} = \varphi l_{rs} sin \frac{\alpha}{2}$$
(13.2)

where  $\varphi$  is torsion angle of torsional shafts.

On account of structural configuration, torque acting on middle rectangular shaft is twice of the one acting on two side rectangular shafts. Assumed as pure bending beams, deflection angle of grey rectangular shafts can be calculated as follows:

$$\theta_{rs} = \frac{\overline{M_r} l_{rs}}{E I_{rs}} = \frac{3\varphi G I_{cs} l_{rs}}{2E l_{cs} I_{rs}}$$
(14)

In this expression,  $\overline{M_r}$  is equivalent torque acting on each rectangular shaft and  $l_{cs}$  is the length of circular shaft. *G* is shear modulus and *E* is elastic modulus.  $GI_{cs}$  is torsional rigidity of blue cylindrical shaft and  $EI_{rs}$  is flexural rigidity of grey rectangular shaft.

The minimum theory of potential energy is used to derive governing equations. The advantage is that energy approach disregards the deformation history and is only related to the deformed state. For a tortional bar, strain energy  $U_{\varepsilon_{-}t}$  is:

$$U_{\varepsilon_{-t}} = \frac{GI_p}{2l}\varphi^2 \tag{15.1}$$



 $D \rightarrow D^{4}$ 

where  $\varphi$  is torsional angle and  $I_p = \frac{\pi D^4}{32}$  is moment of inertia of circular section.

For purely bending beam with a centering angle  $\theta$ , the strain energy function  $U_{\varepsilon_b}$  is expressed as:

$$U_{\varepsilon_{-b}} = \frac{EI}{2l}\theta^2 \tag{15.2}$$

where  $I = \frac{bh^3}{12}$  is inertia moment of rectangular section.

Combining Eqs 13.1, 13.2, 14, 15.1, 15.2, total strain energy of a cell unit including two torsional bars (except for the first unit cell), four bending shafts can be obtained. The potential energy  $\Pi$  is the subtraction of strain energy U and work done by external torque W. For the entire metastructure under the action of an external torque M, the total work is expressed as  $W = M\vartheta_2$ . There is:

$$\mathbf{\Pi} = U - W = U_{tot} - M\vartheta_2 \tag{16}$$

where  $\vartheta_2$  is bending angle of unit cell. It should be noted that for the first unit,  $\vartheta_2$  equals deflection angle  $\theta_{rs}$ . According to the minimum theory of potential energy  $\frac{\partial \Pi}{\partial \theta} = 0$ , bending angle of the first unit cell can be calculated as:

$$\vartheta_2 = M / \left( \frac{3EI_{rs}}{l_{rs}} + \frac{9EI_{rs}l_{rs}^2 \sin^2 \alpha/2}{32l_{cs}^3} \right)$$
(17.1)

As for  $i_{th}$  unit (i > 1),  $\vartheta_2$  is mainly determined by torsional angle  $\varphi$ :

$$\vartheta_{2} = M \left( 1 + \frac{3GI_{cs}l_{rs}}{2El_{cs}I_{rs}} \right)^{2} / \left[ \frac{4GI_{cs}}{l_{cs}} + \frac{27G^{2}I_{cs}^{2}l_{rs}}{4EI_{rs}l_{cs}^{2}} + \frac{9EI_{rs}l_{rs}^{2}sin^{2}\frac{\alpha}{2}}{2l_{cs}^{3}} \right]$$
(17.2)

Bending angle of a modified pantographic metamaterial with *n* unit cells is:

$$\phi_2 = \sum_{i=1}^{n} \vartheta_{2(i)}$$
(18)

#### 3.3 Analytical Solution Validation by FEM

In this paper, FEM is used to verify the validity of analytical model and predict the actuating performance of morphing wings. Hyperelastic behaviors of compliant skin and the pneumatic spar are characterized by Yeoh model. The pneumatic spar, stiffening ribs, and skin are discretized by solid elements. In this section, both ends of pneumatic spar and modified pantographic metastructure are fixed as cantilevered beams. The pressure and moment loading are applied respectively. These two parts are modeled individually for the purpose of model verification. The skin is not considered here, but in **Section 5.1**.

The 3D FEM of pneumatic spar and a modified pantographic metastructure were built with a set of parameters respectively to verify the accuracy of derived functions. The models are shown in **Figure 5A**. Pressure is applied on all internal faces of pressurized



deflection of ribs corresponding to different applied cable forces.

chambers to simulate inflation of SPAs. Torque loading is applied to the cantilevered end of the modified pantographic metastructure. Firstly, for SPAs, the dimensional parameters were chosen as  $l_c = 2.8 \text{ mm}$ ,  $l_s = 2.2 \text{ mm}$ ,  $h_t = 1 \text{ mm}$ ,  $h_c = 6 \text{ mm}$  and  $h_m = 2.8 \text{ mm}$ ,  $w_{s2} = 1.2 \text{ mm}$ ,  $w_c = 40 \text{ mm}$ , N = 20, respectively. Both analytical and FEM results are plotted together in **Figure 5B-1**. The dashed line represents the analytical results and hollow blue circles denote the numerical results. Both analytical and FEM results agree well with each other.

Secondly, for modified pantographic metastructure, the dimensional parameters were chosen as  $l_{rs} = 6.5 \text{ mm}$ ,  $T_{rs} = 1.2 \text{ mm}$ ,  $D_{cs} = 1.5 \text{ mm}$ ,  $l_{cs} = 5.4 \text{ mm}$ ,  $\alpha = 90^{\circ}$  and n = 6, respectively. Curve of analytical results and FEM data is depicted in **Figure 5B–2**. It's shown that the bending angle of the structure varies with external torque in a linear relation. The theorical function of both pneumatic spar and modified pantographic structure is more accurate for small deformation.

#### **4 DESIGN OPTIMIZATION**

In Section 3, relations between structural parameters and actuating loads are established. There are a dozen parameters associated with the analytical model. Therefore, orthogonal experiment of DOE is adopted in this paper to identify critical parameters among multiple factors (Xia et al., 2016).

For compliant spar with PneuNets, wall thicknesses, dimensions of chambers, and thickness of middle layer may impact actuating performance. The overall height of the actuator and chamber height are limited by airfoil dimensions

TABLE 2	Orthogonal	experiment	t of structural	parameters in a	pneumatic spar.
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Test case	Test parameters				
	I <sub>s1</sub> (mm)	l <sub>c</sub> (mm)	h <sub>t</sub> (mm)	Bending angle $\phi_1$ (°)	
1	2.0	2.0	1.0	15.13	
2	2.0	2.4	1.2	13.64	
3	2.0	2.8	1.4	12.26	
4	2.2	2.0	1.2	14.78	
5	2.2	2.4	1.4	13.41	
6	2.2	2.8	1.0	17.07	
7	2.4	2.0	1.4	14.32	
8	2.4	2.4	1.0	18.22	
9	2.4	2.8	1.2	16.39	
$\overline{T_1}$	13.68	14.74	16.81		
$\overline{T_2}$	15.09	15.09	14.94		
$\overline{T_3}$	16.31	15.24	13.33		
R	2.63	0.5	3.48		

and their effects are first disregarded. Thus, length of cavity  $l_c$ , length of side wall  $l_{s1}$ , and thickness of top wall  $h_t$  are chosen for analysis. Orthogonal experiment about the pneumatic spar is shown in **Table 2**. The applied pressure is set as 20 kPa.

 $\overline{T_i}$  is the averaged output corresponding to the  $i_{th}$  level of each factor. *R* is the range of outputs corresponding to various factors x ( $R = x_{max} - x_{min}$ ) and it's an index to reflect the degree of the effect of various factors on outputs (Wang et al., 2019). The results show that the effect of top wall thickness  $h_t$  on bending angle is the largest and the best combination of structural parameters is  $l_{s1} = 2.4 mm$ ,  $l_c = 2.4 mm$ ,  $h_t = 1.0 mm$  within these groups of factors.

TABLE 3 | Orthogonal experiment of structural parameters in a pantographic rib.

Test case	Test parameters				
	α	T <sub>rs</sub> / I <sub>cs</sub>	D <sub>cs</sub> / I <sub>rs</sub>	Bending angle $\phi_2$ (°)	
1	80	1/5	1.5/8.5	49.749	
2	80	1.5/5	1.5/6.5	30.592	
3	80	2/5	1.5/4.5	25.165	
4	90	1/5	1.5/6.5	43.842	
5	90	1.5/5	1.5/4.5	28.933	
6	90	2/5	1.5/8.5	19.408	
7	100	1/5	1.5/4.5	38.640	
8	100	1.5/5	1.5/8.5	25.350	
9	100	2/5	1.5/6.5	19.490	
$\overline{T_1}$	35.169	44.077	31.502		
$\overline{T_2}$	30.728	28.292	31.308		
$\overline{T_3}$	27.83	24.354	30.912		
R	7.339	19.723	0.59		

As for modified pantographic ribs, dimensions of shafts and angle between staggered rectangular shafts have effects on actuating performance. Similarly, orthogonal experiment was designed to study the sensitivity of these parameters on the behavior of ribs. According to analytical model, five structural parameters including  $l_{rs}$ ,  $T_{rs}$ ,  $D_{cs}$ ,  $l_{cs}$ , and  $\alpha$  are chosen to study their effects on bending of modified pantographic metastructure. However, 16 experiments need to be conducted to fulfill an orthogonal experiment with five factors and three levels. For simplifying, two dimensionless ratios of  $T_{rs} / l_{cs}$  and  $D_{cs} / l_{rs}$  are defined to reduce the number of studies. The orthogonal experiment of structural parameters in a pantographic rib is shown in **Table 3**.

The results show that effects of  $\alpha$  and  $T_{rs} / l_{cs}$  on bending angle are larger than the effect of  $D_{cs} / l_{rs}$  and the best combination of structural parameters is  $\alpha = 80$ °,  $T_{rs}/l_{cs} = 1/5$ , and  $D_{cs}/l_{rs} = 1.5/8.5$ .

Orthogonal experiments investigate the effect intendency of structural parameters on morphing mechanism and provide guidance for further optimization. Parametric studies with FEM were also conducted as a validation purpose and for structural optimization. The simulation results are shown in **Figure 6**. Loading condition similar with the model used for theorical validation was applied to pneumatic spar. While the



force; (B-1) Comparison of spanwise deflection between FEM and experimental results under pressure control in a pneumatic spar; (B-2) Comparison of chordwise deflection between FEM and experimental results under force control in a pantographic rib (Red dots: experimental data, black dashed curves: FEM results).



pantographic rib is actuated by cables in practice, an equivalent force loading to torque was used to plot the curves in **Figure 6B** for experimental correlation.

As can be seen from **Figure 6A**,  $l_{s1}$  and  $l_c$  nearly have little effect on bending performance of the pneumatic spar. The effect of top wall thickness  $h_t$  is quite prominent. The bending angle

increases as  $h_t$  reduces. However, it should be noted that a small value of top wall thickness  $h_t$  results in ballooning locally, which should be avoided in final design. As shown in **Figure 6B**,  $\alpha$  and  $T_{rs}/l_{cs}$  have greater influences than  $D_{cs}/l_{rs}$  to the pantographic rib. The bending behavior is nonlinear and the bending angle changes dramatically as  $T_{rs}/l_{cs}$  decreases.

### **5 EXPERIMENTS**

#### 5.1 Morphing Control

The prototype was fabricated based on the referenced parameters from design optimization. The pneumatic spar contained 18 unit cells. The upper chamber and lower chamber were separated by a middle layer with thickness of 1.5 mm. Each cavity was 5 mm in length and about 6 mm in height. The thickness of top wall  $h_t$ , side wall  $l_s$  and  $w_{s2}$  were all set as 2.0 mm. And stiffening ribs were composed of three modified pantographic metastructures with structural parameters of  $l_{rs} = 4.0 \text{ mm}$ ,  $T_{rs} = 1.0 \text{ mm}$ ,  $D_{cs} = 1.5 \text{ mm}$ ,  $l_{cs} = 6.0 \text{ mm}$ , and  $\alpha = 70^{\circ}$ .

The experimental setup to verify actuating performance of manufactured prototype is shown in **Figures 7A-1,A-2**. The morphing wing was clamped on one end and air pressure was supplied through a hand pump. The inner pressure is monitored and measured by a digital differential pressure gauge. Besides, tail end of each modified pantographic rib is tied with a fishing wire. The other end of three fishing lines is attached to a force gauge for calibration. A protractor is utilized to measure bending angles of morphing wings along spanwise and chordwise.

As shown in **Figures 7B–1,B-2**, both bending angle  $\phi_1$  and  $\phi_2$  were compared against FEM results. In this numerical model, the whole wing was modeled with the existence of hyperelastic skin. The comparison shows the prototype is actually more flexible and exhibits a larger bending angle along spanwise when air pressure is applied beyond 25 kPa. The differences may be attributed to manufacturing precision. The dimensions of wax mold forming PneuNets are not as accurate as a 3D printed product and error raised by mold assembly exists, causing some variances in geometrical parameters of PneuNets. On the other hand, the experimental results of trailing-edge deflection agree well with numerical results, even with the elastomeric skin considered in FEM. It is probably due to the thinness of the skin, which is 1 mm in design. Results show that the maximum morphing capacities can be achieved at  $\pm 12^{\circ}$  angular deflection in spanwise and ±35° angular deflection in chordwise.

#### 5.2 Wind Tunnel Test

At last, a wind tunnel test with a Particle Image Velocimetry (PIV) instrument was conducted to examine load bearing capacity and dynamic response of the morphing wing in air-flow field. PIV is an optical method to visualize flow field. It can map the flow field and provide physical insight into flow behaviour (Atkins, 2016). The morphing wing may deflect in two directions. Spanwise morphing may improve lateral stability and maneuverability of the aircraft (Abdulrahim and Lind, 2004;

Geva et al., 2019). Therefore, it was not considered in this test. As shown in **Figure 8A**, a test setup was built to focus on the evaluation of trailing-edge bending on aerodynamic layout through tunnel tests.

Firstly, maximum load bearing capacity of the morphing wing was tested. It's observed that obvious torsional instability of morphing wing happened when wind speed was beyond 13 m/s. To inflate internal cavities may increase the stiffness in elastomeric membranes. After being pressurized in pneumatic spar above 10 kPa, the maximum wind velocity that morphing wing can bear increased from 13 to 16 m/s.

As shown in **Figure 8B**, airflow velocity contours near morphing wing at different air-flow speeds and specific chordwise angles are demonstrated. It can be qualitatively observed that flow velocity field above the wing accelerated with deflection angle of trailing-edge increasing.

When the velocity of wind reaches 12 m/s, the morphing wing is still effective, but the aeroelastic fluttering of soft skin occurs. It may induce the local turbulence effect, which is a common issue in the compliant-skin design. It may be improved by the pre-tensioned technique (Muhammed, 2020).

## **6 CONCLUSION**

This work developed a novel design of morphing wing to produce smooth and continuous deformation during shape changing. A new compliant structural architecture composed of pneumatic spar, cable driven ribs, and soft skins was described. Pneumatic spar based on PneuNets is used to achieve bending along wing span and modified pantographic ribs are used to control trailing-edge morphing. Large deflection of both longitudinal spar and chordwise ribs are realized through the microscopic design with metastructural type of unit cells. Analytical models of two basic units were derived and verified through FEM. Sensitivities of structural parameters on actuating performance were investigated by DOE methodology. With optimal combination of parameters, a prototype was manufactured through Lost-Wax casting. A series of experiments including a wind tunnel test were conducted. The results show that this morphing wing can achieve  $\pm 12^{\circ}$ deflection along spanwise and  $\pm 35^{\circ}$  deflection of trailing-edge. The reliable deformability of the wing was verified by wind tunnel test and it's shown that this morphing wing can tune aerodynamic performance qualitatively. With advantages of lightweight, tunable stiffness and large morphing range, the novel design concept provides a feasible solution for smallscale aircraft with morphing wings.

#### DATA AVAILABILITY STATEMENT

The raw data supporting the conclusion of this article will be made available by the authors, without undue reservation.

#### **AUTHOR CONTRIBUTIONS**

LX: Investigation, Methodology, Validation, Software, Visualization, Writing—original draft; HZ: Conceptualization, Project administration, Methodology, Resources,

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