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# Estimation of the surface potential of clay mineral taking Na<sup>+</sup>/K<sup>+</sup>-specific ion effects into account

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Surface potential is a key electrochemical property of colloids in the study of particle interactions. However, the specific ion effects are not involved in the existing measuring methods. In this study, approaches for the estimation of the surface potential of montmorillonite with or without consideration of the specific ion effects were explored through the montmorillonite particle aggregation in the presence of Li<sup>+</sup>, Na<sup>+</sup>, and K<sup>+</sup> ions. The montmorillonite aggregation process exhibited remarkable specific ion effects, and the critical coagulation concentration (CCC) values show the following: Li<sup>+</sup> (271.8 mm) > Na<sup>+</sup> (130.8 mm) > K<sup>+</sup> (85.04 mm). Based on the mathematic relationship between electrostatic repulsion and the van der Waals attractive interaction at the CCC, the fluctuation coefficient  $\beta$  was obtained. The value of  $\beta$  could quantify the strength of the specific ion effects of different cations. Then, the fluctuation coefficient  $\beta$  was introduced into the classical method for calculating the surface potential, considering the specific ion effects. The quantificational sequence of the ionic specificity of K<sup>+</sup> and Na<sup>+</sup> was as follows:  $\beta_K = 1.433 > \beta_{Na} = 1.187$ . Simultaneously, the surface potential considering specific ion effects can be obtained by introducing this coefficient. Our findings provide ideas for getting reliable surface potentials of charged particles in different electrolyte environments.

## KEYWORDS

surface potential, Hamaker constant, specific ion effect, critical coagulation concentration, potential curve

## Introduction

Surface potential is an important parameter for the description of surface properties of charged colloid particles, which has significant effects on chemical, physical, and biological properties and processes, especially in environmental science and technology. Although this is an important property and a basic parameter in evaluating colloidal particle interactions, no reliable method for its determination is available yet (Li et al., 2004). The interaction of clay mineral colloids is a significant

process in soil and water environments, significantly affecting the fate and transport of nanoparticles along with ions and contaminants (Gao et al., 2019). The acquisition of accurate and reliable surface potential is of great significance for the accurate assessment of particle-to-particle interactions.

Specific ion effects or Hofmeister effects ubiquitously exist in colloidal and biological systems (López-León et al., 2008; Kunz, 2010; Nostro and Ninham, 2012). These effects present in an interfacial reaction will bring colloidal stability and coagulation (Tian et al., 2014; Badizad et al., 2020; Katana et al., 2020) and different exchange selectivity (Liu et al., 2012) and enzyme activities (Pinna et al., 2005; Bauduin et al., 2006). It was found that under high electrolyte concentrations, ionic hydration and the ionic dispersion forces resulted in the specific ion effects (Boström et al., 2001; Moreira et al., 2006). Therefore, the specific ion effects should disappear at very low electrolyte concentrations, for the hydration and dispersion forces decreased as the ionic concentration decreased. Conversely, Liu (2013) and Kim et al. (2001) found that, with the decrease in the electrolyte concentration, the specific ion effects sharply increased. Thus, some researchers have proposed that a strong electric field exists near the charged particle surface, which is as strong as  $10^8$  V/m, and increases at a low ion concentration in the bulk solution (Li et al., 2011). The strong polarization effects, resulting from coupling between the quantum fluctuation of ionic outer shell electrons and the surface electric field, strongly change the electron cloud configuration of adsorbed ions on the charged surface, which is the origin of such specific ion effects (Xu et al., 2015).

Due to the difficulty in obtaining the surface potential, zeta potential, that is, the potential on the shear plane, is often used instead of the surface potential (Somasundaran et al., 1997; Li et al., 2020). However, it turns out that the shear plane is far away from the Stern plane but close to the Gouy plane, and the surface potential may be several times higher than the zeta potential (Missanal and Adell, 2000; Li et al., 2003, 2009; Liu et al., 2015). The surface potential of colloidal particles is dependent not only on the surface properties but also on the composition and concentration of the ambient electrolyte solutions. The classical theoretical calculation of surface potential was due to the ionic valence and ion concentration only (Li et al., 2004); however, various influences from ion species with identical valence are always neglected. Previous studies have showed that monovalent cations such as  $\text{Li}^+$ ,  $\text{Na}^+$ , and  $\text{K}^+$  demonstrate strong specific ion effects on the kinetic stability of proteins (Broering and Bommarius, 2005), in ion exchange (Liu et al., 2013), under the influence of active energy in particle interaction (Li et al., 2015). In addition, a principle of surface potential determination of the charged particles in mixed electrolyte solutions was established considering the dielectric saturation (Zou et al., 2020). According to the aforementioned analysis, we believe that it is necessary to consider the specific ion effects

in the calculation of surface potential when the particles are in  $\text{Li}^+$ ,  $\text{Na}^+$ , and  $\text{K}^+$  solutions.

In this study, we use dynamic light scattering experiments to obtain the critical coagulation concentration (CCC) and then determine the Hamaker constant by the potential curve stepwise approaching method in  $\text{LiNO}_3$ . After that, we get the fluctuation coefficient  $\beta_{\text{Na}}$  and  $\beta_{\text{K}}$  by calculating the surface potential at CCC<sub>Na</sub> and CCC<sub>K</sub>. It was found that the Hamaker constant was  $10.75 \times 10^{-20}$  J and  $\beta_{\text{K}} = 1.433 > \beta_{\text{Na}} = 1.187$ , which were introduced to the classic theory equations so that a more reliable surface potential was estimated. In this article, a new approach for the determination of the surface potential of charged particles through the modified DLVO theory taking  $\text{Na}^+$  and  $\text{K}^+$ -specific ion effects into account using the DLS measurement was developed.

## Theory

### The calculation of the Hamaker constant

In the light of DLVO theory (Visser and Israelashvily, 1985), the van der Waals (vdW) force makes particles attract together and the electrical double layer (EDL) repulsive force makes particles repel each other. As the repulsive force is stronger than the attractive force, the particles will disperse in the medium and form a stable suspension. For this case, only external pressure was applied on the particle, and the particle's distance became closer. We considered the applied external pressure is  $P_{\text{ext}}$  (atm), which equals to the net repulsive pressure at equilibrium. Therefore, assuming the corresponding average distance between two adjacent particle surfaces is  $\lambda$  (dm) at this applied pressure, we obtain the following:

$$P_{\text{ext}}(\lambda) = P_{\text{EDL}}(\lambda) - P_{\text{vdW}}(\lambda), \quad (1)$$

where  $P_{\text{EDL}}$  (atm) is the pressure from the electric repulsive force and  $P_{\text{vdW}}$  (atm) is the pressure from the van der Waals force. Eq. 1 is applicable when the distance between surfaces of two particles is larger than 1.5 nm because the hydration force was observed at a distance shorter than 1.5 nm between surfaces of two particles (Ducker et al., 1992), when the hydration force cannot be neglected.

$P_{\text{EDL}}(\lambda)$  can be calculated using the Langmuir equation (Verwey et al., 1948; Hou et al., 2009) for a 1:1 type electrolyte, and it can be written as follows:

$$P_{\text{EDL}}(\lambda) = \frac{2}{101} RTc_0 \left\{ \cosh \left[ \frac{ZF\varphi(\lambda/2)}{RT} \right] - 1 \right\}, \quad (2)$$

where  $Z$  is the valence of the ion producing positive adsorption on the particle surfaces,  $\varphi(\lambda/2)$  (V) is the potential at the overlapping position of two EDLs for two adjacent particles,  $c_0$  (mol/L) is the concentration of the electrolyte in a bulk

solution,  $R$  (8.314 J/molK) is the gas constant,  $T$ (K) is the absolute temperature, and  $F$  (96,487 C/mol) is Faraday's constant.

Hou et al. (2009) obtained an equation to calculate the value of  $\varphi(\lambda/2)$  from the value of the surface potential  $\varphi_0$ ; later, a more accurate equation was also obtained for calculating  $\varphi(\lambda/2)$  for a 1:1 type of electrolyte, and it can be expressed as follows:

$$\frac{\pi}{2} \left[ 1 + \left(\frac{1}{2}\right)^2 e^{\frac{2ZF\varphi(\lambda/2)}{RT}} + \left(\frac{1.3}{2.4}\right)^2 e^{\frac{4ZF\varphi(\lambda/2)}{RT}} \right] - \arcsin e^{\frac{ZF\varphi_0 - ZF\varphi(\lambda/2)}{2RT}} = \frac{1}{4} \lambda \kappa e^{-\frac{ZF\varphi(\lambda/2)}{2RT}} \tag{3}$$

The van der Waals attractive force  $P_{vdW}$  was expressed as a function of the Hamaker constant, with the following relationship (Li et al., 2009):

$$P_{vdW}(\lambda) = \frac{A_{eff}}{0.6\pi} (10\lambda)^{-3}, \tag{4}$$

where  $A_{eff}$ (J) is the effective Hamaker constant.

Next, to discuss how to get  $P_{ext}$ , it is known that particles in the suspension have released mean kinetic energies at given temperatures because of Brownian motion. The mean kinetic energy means that the overwhelming majority of particles in the suspension have this kinetic energy. Therefore, the fast aggregation process can occur when the potential barrier (the activation energy) is lower than the particle's mean kinetic energy. Therefore,  $e$  is simply the repulsive pressure when the potential barrier is equal to the mean kinetic energy.

According to the Einstein equation (Uhlenbeck and Ornstein, 1930), we have the following:

$$\bar{v} = \frac{\sqrt{\langle [\Delta x(t)]^2 \rangle}}{t} = \frac{\sqrt{2D}}{\sqrt{t}}, \tag{5}$$

where  $\langle [\Delta x(t)]^2 \rangle$  is the mean square displacement in one dimension of a free Brownian particle at time  $t$  and  $D$  is the diffusion constant. The diffusion constant can be calculated using  $D = kT/\gamma$ , where  $k$  (J/K) is Boltzmann's constant and  $\gamma$  is the Stokes friction coefficient. Obviously,  $\rightarrow \infty$  at  $t \rightarrow 0$ , which means that  $\bar{v}$  does not represent the real velocity of the particle. Eq. 7 is valid only when  $t \gg \tau$ ; here,  $\tau = m/\gamma$  is the momentum relaxation time of a particle with mass  $m$ . However, at very short time scales of  $t \ll \tau$ , according to the Langevin equation,

$$\bar{v} = \frac{\sqrt{\langle [\Delta x(t)]^2 \rangle}}{t} \xrightarrow{t < \tau} \frac{\Delta x(t)}{t} = v = \sqrt{\frac{kT}{m}}. \tag{6}$$

Therefore, the real velocity of a particle in the suspension is  $v_2 = kT/m$ , which means the kinetic energy of the particle is 0.5 kT. This Brownian particle kinetic energy has been experimentally verified by Li et al. (2010), who found that the energy conservation theorem is still correct for a Brownian particle. However, because of viscosity resistance ( $\gamma$ ), the actual kinetic energy of particles at the moment of collision

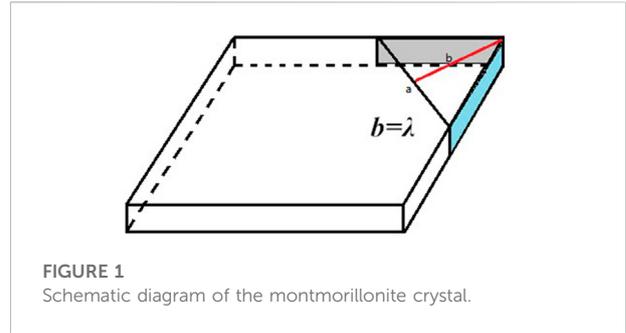


FIGURE 1 Schematic diagram of the montmorillonite crystal.

would be less than 0.5 kT. Therefore, 0.5 kT and 0 kT are the maximum and minimum kinetic energies of the extreme cases, respectively. Then, the DLVO potential curve stepwise approaching method was used to determine the two corresponding Hamaker constants in both extreme cases. The average value of these two constants was considered the average effective Hamaker constant of the complex system.

Regarding  $\tau = m/\gamma$ , the lowest  $\gamma$  value corresponds to the highest  $\tau$  value, so the most likely way for a montmorillonite plate to get close to another montmorillonite plate in the aggregation process is if the tip of one plate approaches the surface of another plate, which ensures that the  $\gamma$  value is as low as possible.

Suppose the width of the potential barrier is  $\lambda$  nm at  $c_0 = CCC$  and the area of the montmorillonite plate side face is  $S$  nm<sup>2</sup> (as shown in the shaded region of the graph in Figure 1), the approximate thickness of the hydrated montmorillonite plate is 10–8 dm; we have the function of  $P_{ext}$  as follows:

$$P_{ext}(\lambda) = \frac{E}{\lambda \cdot S} = \frac{E \times 1.38 \times 10^{-23} \times 10^7 T (\text{dyn} \cdot \text{cm})}{\lambda \times 2\sqrt{2} \lambda \times 10^{-21} (\text{cm}^3)} = 16.114E/\lambda S \text{ atm}. \tag{7}$$

In summary,  $P_{EDL}(\lambda) - P_{vdW}(\lambda) = 16.114E/\lambda S$  when  $c_0 = CCC$ . According to the formula  $P_{EDL}(\lambda) - P_{vdW}(\lambda) - 16.114E/\lambda S = 0$  at  $c_0 = CCC$ , we could obtain the Hamaker constant and  $\lambda$  through the stepwise approaching method.

### The classical method for calculating the surface potential

Since charges on the montmorillonite surface can be taken as a permanent charge, the surface potential for a symmetric electrolyte system (for the 1:1 type of electrolyte) can be calculated through the following equation (Li et al., 2004):

$$\varphi_0 = -\frac{2RT}{ZF} \ln\left(\frac{1-a}{1+a}\right), \tag{8}$$

where  $Z$  is the valence of the ion producing positive adsorption on the surface of the solid particles.

$$\frac{\bar{c}}{c_0} = 1 + \frac{4}{1+a} - \frac{4}{1+e^{-1}a}. \quad (9)$$

Considering a flat double layer, when adsorption equilibrium is reached, the average concentration of the ion in the diffuse double layer can be defined as follows:

$$\bar{c} = \frac{N_{\infty}}{V} = \frac{\text{CEC}}{S \cdot 1/k} = \frac{\kappa \cdot \text{CEC}}{S}, \quad (10)$$

where  $\kappa$ (1/dm) is the Debye–Hückel parameter and

$$\kappa = \sqrt{\frac{8\pi Z^2 F^2 a_0}{\epsilon RT}}, \quad (11)$$

where  $\epsilon$  is the dielectric constant; here, it equals  $8.9 \times 10^{-10} \text{ C}^2/\text{Jdm}$  for water;  $a_0$  is the activity of ions in the bulk solution.  $a_0$  could be obtained through the following equations:

$$\lg a_0 = -0.5102Z^2 \left( \frac{\sqrt{I}}{1 + \sqrt{I}} - 0.3I \right), \quad (12)$$

where  $I$  is the ionic strength and

$$I = 0.5 \sum Z_i^2 c_i^0. \quad (13)$$

The values of the cation exchange capacity (CEC) = 84.8 cmol<sub>c</sub>/kg and specific surface area (S) = 716 m<sup>2</sup>/g have been determined by using the combined determination method proposed by Li et al. (2011). The values were introduced into upper Eqs 8–11; the corresponding surface potential  $\phi_0$  at certain electrolyte concentrations can be calculated. Obviously, this classical method did not consider the specific ion effects in the calculation process.

## Correct calculation method of the surface potential—Fluctuation coefficient $\beta$ calculation

According to the theoretical calculations in 2.1, the Hamaker constant of montmorillonite considering specific ion effects and the distance between particles  $\lambda$  could be obtained. We could calculate  $P_{vdW}$  and then obtain  $P_{EDL}$  through  $P_{EDL}(\lambda) - P_{vdW}(\lambda) - 16.114E/\lambda S = 0$  at CCCNa and CCCK. Then, the true values of  $\phi_{true}(\lambda/2)$  and  $\phi_{true0}$  at CCC considering the specific ion effects were obtained through Eqs.12, 13.

$$P_{EDL}(\lambda) = \frac{2}{101} RTc_0 \left\{ \cosh \left[ \frac{ZF\phi_{true}(\lambda/2)}{RT} \right] - 1 \right\}, \quad (14)$$

$$\begin{aligned} & \frac{\pi}{2} \left[ 1 + \left( \frac{1}{2} \right)^2 e^{\frac{2ZF\phi_{true}(\lambda/2)}{RT}} + \left( \frac{1.3}{2.4} \right)^2 e^{\frac{4ZF\phi_{true}(\lambda/2)}{RT}} \right] \\ & - \arcsin e^{\frac{ZF\phi_{true0} - ZF\phi_{true}(\lambda/2)}{2RT}} \\ & = \frac{1}{4} \lambda \kappa e^{\frac{-ZF\phi_{true}(\lambda/2)}{2RT}}. \end{aligned} \quad (15)$$

Since the ion radius of Li<sup>+</sup> is only 0.9Å with the electron shell structure 1s<sup>2</sup>, these two negative electrons were attracted by the three positive electrons from the center nucleus, and as a result, Li<sup>+</sup> was considered as a no quantum fluctuation ion. Given the presence of specific ion effects of Na<sup>+</sup> and K<sup>+</sup> for their quantum fluctuation, we introduce the fluctuation coefficient  $\beta$  to the formula of the surface potential in order to obtain accurate results. Furthermore,  $\beta$  is a quantitative characterization of the strength of specific ion effects. Then, we replace  $Z$  with  $\beta Z$  in Eqs. 8–11. After being corrected, related equation changes are as follows:

$$\kappa = \sqrt{\frac{8\pi(\beta Z)^2 F^2 c_0}{\epsilon RT}} = \beta \sqrt{\frac{8\pi Z^2 F^2 c_0}{\epsilon RT}}. \quad (16)$$

Since  $\kappa$  was corrected to  $\beta\kappa$ , the equation of calculating  $a$  was changed into the following:

$$\frac{\beta\bar{c}}{c_0} = 1 + \frac{4}{1+a} - \frac{4}{1+e^{-1}a}. \quad (17)$$

The classical calculation theory of surface potential becomes the following equation after correction:

$$\phi_{true0} = -\frac{2RT}{\beta ZF} \ln \left( \frac{1-a}{1+a} \right). \quad (18)$$

It will give a function between surface potential  $\phi_{true0}$  and  $\beta$  at CCCs through Eqs 16–18 and then introduce  $\phi_{true0}$  at CCCs into this function to get the fluctuation coefficient  $\beta$ . The coefficients  $\beta_{Na}$  and  $\beta_{K}$  were used to regulate classical formulas, and then, the surface potential at any electrolyte concentrations can be calculated.

## Materials and methods

### Material preparation

The clay K<sup>+</sup>-montmorillonite used in this study is a nanoscale material composed of two tetrahedral Si-O layers sandwiching an octahedral Al-O layer (Ray and Okamoto, 2003). They were bought from Wu Hua Tian Bao Mineral Resources Co., Ltd. (Chifeng, China). Isomorphic substitution within the layers generates permanent negative charges on the surface of the montmorillonite colloid. The cation exchange capacity is 84.8 cmol<sub>c</sub>/kg, and the specific surface area amounts to 716 m<sup>2</sup>/g (Li et al., 2011). The montmorillonite particles were prepared according to the following procedure. First, 50.0 g montmorillonite and 10 ml of 0.1 mol/L KOH solution were successively added to a 500-ml beaker and then diluted with ultrapure water, making it up to 500 ml. After 15-min intensive sonication (SCIENTZ-IIID, Ningbo, China, with 350-W output, equipped with a 10-mm diameter titanium probe), the suspension was further diluted to 5 L by ultrapure water. The

montmorillonite particles with the effective hydrodynamic diameter  $< 200$  nm were extracted and collected using the static sedimentation method (Xiong et al., 1985), estimated by the oven drying method to be approximately 1.892 g/L. As measured by the flame photometer, the concentration of  $K^+$  in the bulk suspension was less than 0.01 mmol/L and, therefore, can be neglected. Then, this suspension was diluted 10 times, and the pH value was approximately 8.0.

## Dynamic light scattering measurements

A BI-200SM multi-angle laser light scattering instrument (Brookhaven Instruments Corporation, New York, United States) with an autocorrelator of BI-9000AT (Brookhaven Instruments Corporation) was used. The power of the laser device equals 200 mW and is vertically polarized with a wavelength of 532 nm. The dynamic light scattering (DLS) measurements were performed for measuring the effective hydrodynamic diameters of particles or aggregates. It can also record the changes of the hydrodynamic diameters with time at different concentrations of the electrolyte. All the measurements were at a  $90^\circ$  scattering angle.

Experimentally, the suspensions containing the montmorillonite particles were subjected to a 2-min period of sonication (KQ-300VDE, Shanghai, China, with 300 W output operating at 28 kHz) and then pipetted into a clean borosilicate vial. The  $LiNO_3$ ,  $NaNO_3$ , and  $KNO_3$  solutions of different concentrations and different amounts of ultrapure water were added to ensure that the total volume was 10 ml. The electrolyte concentrations that have been uniformly mixed with the montmorillonite particles were equal to 10, 30, 50, 70, 100, 150, 200, 300, and 400 mmol/L for  $LiNO_3$  and  $NaNO_3$  and 10, 20, 30, 40, 50, 70, 100, 150, and 200 mmol/L for  $KNO_3$ . The particle density of montmorillonite in these electrolyte solutions was determined to be 0.09458 g/L. Data regarding the average effective hydrodynamic diameters and the size distributions of the montmorillonite particles were recorded every 30 s. The DLS experiments were carried out at a normal temperature of  $298 \pm 0.5$  K.

## Results and discussions

### The CCC values of $LiNO_3$ , $NaNO_3$ , and $KNO_3$ in montmorillonite aggregation

We used the method developed by Jia et al. (2013) to estimate the CCC from calculations of the total average aggregation (TAA) rates at different electrolyte concentrations by DLS measurements in suspensions of polydisperse non-spherical colloids. First, the TAA rate was

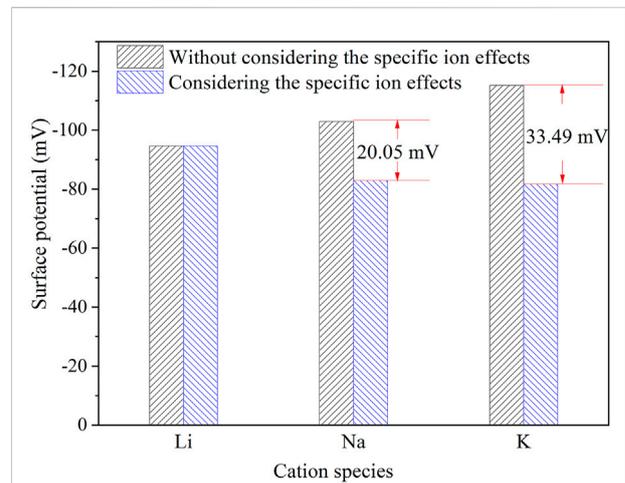
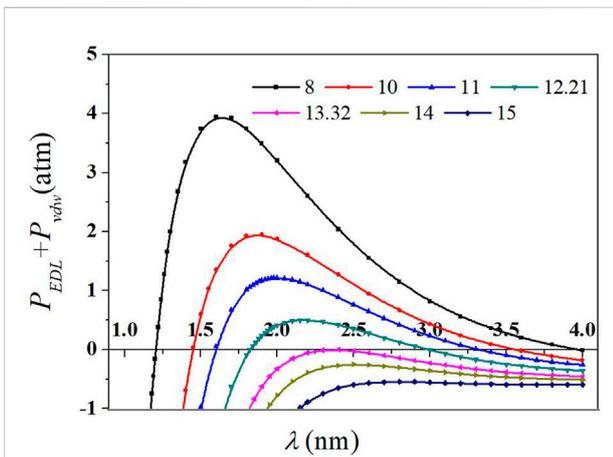
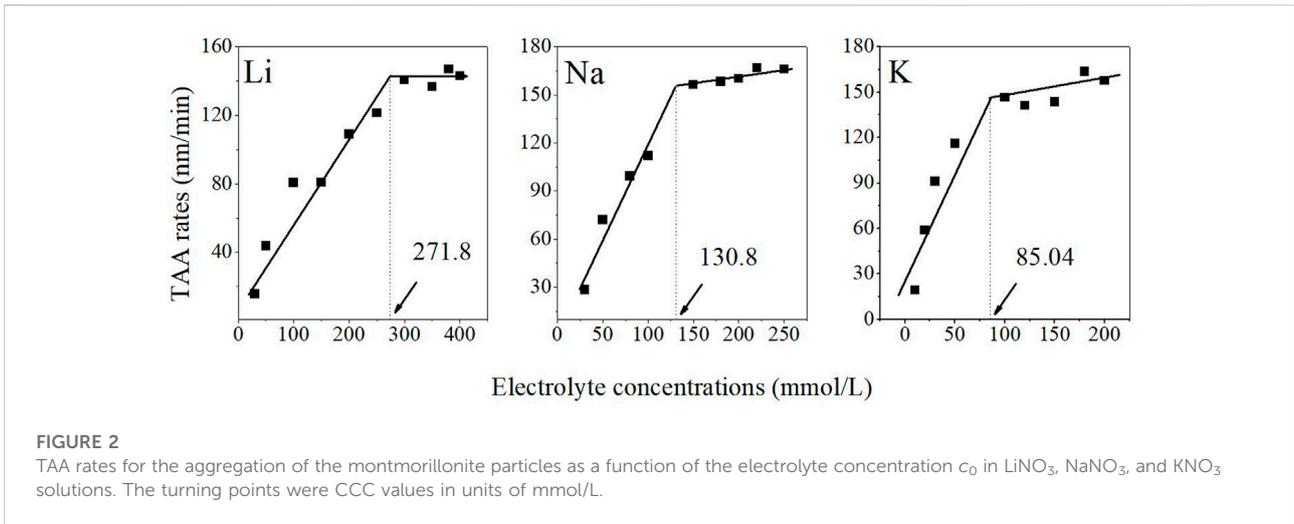
calculated; the TAA rate will increase linearly with the increase in the electrolyte concentration until this concentration reaches the CCC value, and the TAA rate will remain constant or slightly increase as the electrolyte concentration increases. Therefore, the electrolyte concentration at the turning point will be the CCC value (Figure 2). The CCC values for  $LiNO_3$ ,  $NaNO_3$ , and  $KNO_3$  were 271.8, 130.8, and 85.04 mmol/L, respectively. The CCC value for  $Li^+$  is 2.078 and 3.196 times that for  $Na^+$  and  $K^+$ . The different CCC values of these three ions reflected that the cations  $Li^+$ ,  $Na^+$ , and  $K^+$  had strong specific ion effects (Parsons et al., 2011) on colloid particle interactions. The CCC is an important parameter for characterization of the aggregation process, and the coagulation capability decreased in the order  $K^+ > Na^+ > Li^+$ .

### The Hamaker constant of montmorillonite measured in $LiNO_3$

By assuming  $Li^+$  ions of quantum fluctuations approaching zero, the results of the electrostatic properties of  $Li^+$ -system could be correctly described by the classical electric double layer and DLVO theory. Accordingly, the Hamaker constant obtained from the  $Li^+$  system rather than the others should be accurate for characterizing the interaction between colloidal particles of montmorillonite under van der Waals forces.

At  $c_0 = c$  (CCCLi) = 271.8 mmol/L, first, many different Hamaker constants (values between  $10^{-14} \times 10^{-20}$  in Figure 3) and a series values of  $\lambda$  are assumed, for example, 1, 1.1, 1.2, 1.3, 1.4, 1.5, 1.6, 1.7, 1.8, 1.9, 2, 2.1, 2.2, 2.3, 2.4, 2.5, 2.6, 2.7, 2.8, 2.9, 3, 3.1, 3.2, 3.3, 3.4, 3.5, 3.6, 3.7, 3.8, 3.9, and 4 nm. After that, the value of  $P_{EDL}(\lambda) + P_{vdW}(\lambda) - P_{ext}(\lambda)$  became a function of  $\lambda$ . The curves of the sum force ( $P_{EDL}(\lambda) + P_{vdW}(\lambda) - 16.114E/\lambda S$ ) at each assumed Hamaker constant and  $\lambda$  were obtained through the aforementioned equations. It is shown in Figure 3 that for  $Li^+$ , one curve with a peak value exactly zero was selected using the stepwise approaching method. The corresponding value of the Hamaker constant was  $13.32 \times 10^{-20}$  J; then, several  $P_{ext}(\lambda) \sim \lambda$  curves were calculated from a series of Hamaker constants, and the average kinetic energy was obtained by integrating the area of the exclusion barrier. The corresponding Hamaker constant was  $12.21 \times 10^{-20}$  J at the point of  $E = 0.5$  kT. In other words, the Hamaker constant for montmorillonite is  $A_{eff} = (12.21 \times 10^{-20} + 13.32 \times 10^{-20})/2 = 12.77 \times 10^{-20}$  J, corresponding to  $\lambda = 0.84$  nm.

Figure 3 shows that in the area near the particle surface, the total DLVO forces between particles are negative, indicating that the net force was the attractive force; with the increasing distance between two adjacent particles, van der Waals attraction tended to negative infinity in the form of  $\lambda^{-3}$  (Li et al., 2009), while the electrostatic repulsion tended to a finite positive. There may be a net positive force during this process.

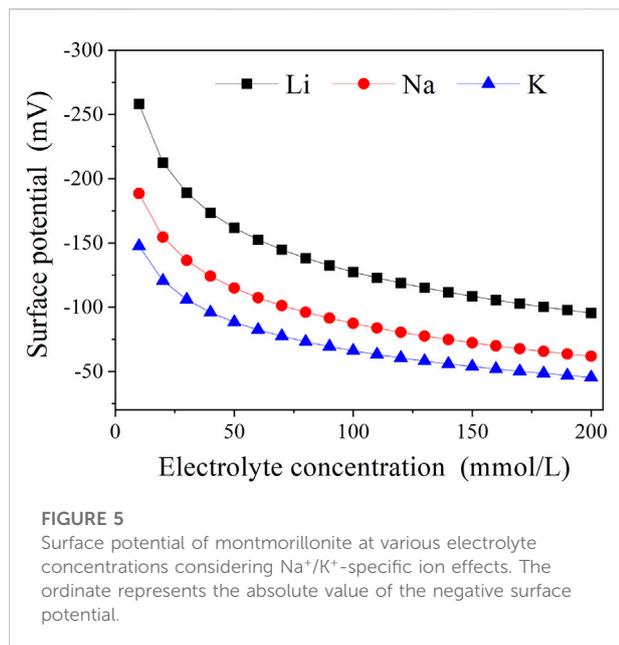


### Calculation of the surface potential

The difference of the extranuclear electron structure leads to the various quantum fluctuations of  $\text{K}^+$  and  $\text{Na}^+$ , which is the origin of such specific ion effects. The calculation of surface potential through Eq. 8 discriminates the difference of the cation valence without considering the specific ion effects from the cations in the same valence, so it is essential to consider these effects in calculating the surface potential.

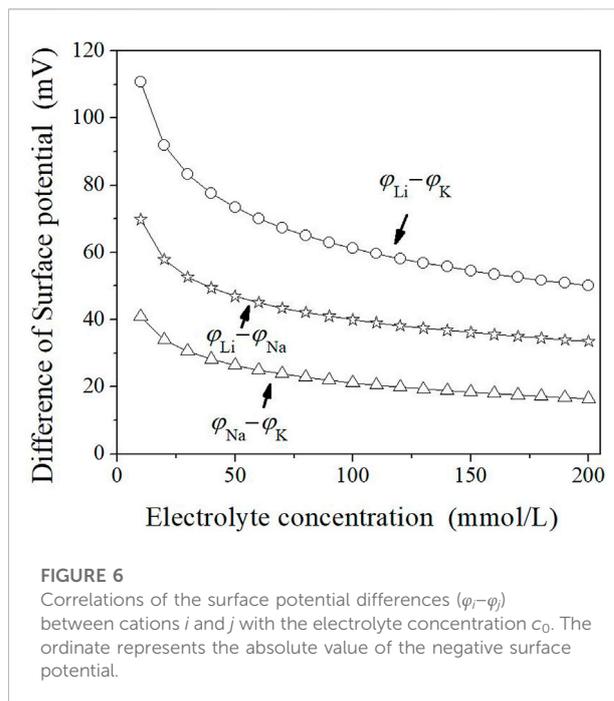
The CCC values of  $\text{Li}^+$ ,  $\text{Na}^+$ , and  $\text{K}^+$  are obviously different since the specific ion effects. Using the Hamaker constant of montmorillonite and  $\lambda$  given in Figure 3,  $P_{vdW}(\lambda)$  and  $P_{ext}$

being in adjacent particles are calculated through Eqs. 4–7. They are  $P_{vdW} = -5.508$  atm and  $P_{ext} = 0.03962$  atm. According to the formula  $P_{EDL} - P_{vdW} = P_{ext}$  at  $c_0 = \text{CCC}$ , we could obtain  $P_{EDL} = 5.546$  atm either for  $\text{Na}^+$  or  $\text{K}^+$ . By introducing  $P_{EDL} = 5.546$  atm into Eq. 12,  $\phi_{true}(\lambda/2)$  was found to be  $-35.62$  mV and  $-42.18$  mV for  $\text{Na}^+$  and  $\text{K}^+$ , respectively.  $\phi_{true}(\lambda/2)$  values were brought into Eq. 13 to get  $\phi_{true0}$  values of  $-82.91$  mV and  $-81.72$  mV for  $\text{Na}^+$  and  $\text{K}^+$  at CCCs, respectively. Then, the fluctuation coefficient  $\beta_{Na} = 1.187$  and  $\beta_K = 1.433$  were obtained in accordance with the theory of correct calculation of surface potential. It implies that the fluctuation ability of  $\text{K}^+$  was 1.207 and 1.433 times as



strong as that for Na<sup>+</sup> and Li<sup>+</sup>. This coefficient could be used as a quantitative characterization of specific ion effects. The larger the coefficient  $\beta$  is, the stronger the fluctuation of the electron cloud does, and this further results in a larger polarization effect, for example,  $\beta_{\text{Na}} = 1.187$  and  $\beta_{\text{K}} = 1.433$ . It implies that K<sup>+</sup> rather than Na<sup>+</sup> has a higher probability to appear in the proximity of the particle surface, neutralizing more surface negative charges, which leads to a lower surface potential under the same concentration.

The surface potential of montmorillonite in NaNO<sub>3</sub> and KNO<sub>3</sub> solutions at their CCC were  $-102.96$  mV and  $-115.21$  mV through the classical theory equations without considering the specific ion effects, while the  $\phi_{\text{true}0}$  values considering the specific ion effects were  $-82.91$  mV and  $-81.72$  mV for Na<sup>+</sup> and K<sup>+</sup>. It was found that the surface potential was reduced after considering the specific ion effects. As shown in Figure 4, the difference of surface potential between considering and without considering the specific ion effects was 20.05 mV and 33.49 mV in Na<sup>+</sup> and K<sup>+</sup> solutions, further evidencing that specific ion effects influence the particle surface potential significantly. The surface potential differences between considering and without considering the specific ion effects in KNO<sub>3</sub> were bigger than those in NaNO<sub>3</sub>, implying the stronger quantum fluctuation of K<sup>+</sup> than Na<sup>+</sup>. The differences between considering and without considering the specific ion effects in NaNO<sub>3</sub> were bigger than those in LiNO<sub>3</sub>, implying the stronger quantum fluctuation of Na<sup>+</sup> than Li<sup>+</sup>. In general, regarding the specific ion effects, K<sup>+</sup> has the strongest ionic quantum fluctuation capability in the three, resulting in the strongest polarization and strongest electric field screening,



followed by Na<sup>+</sup> and Li<sup>+</sup>. Thus, it obviously shows the influence of specific ion effects on surface potential.

Accordingly, the surface potentials of montmorillonite at any NaNO<sub>3</sub> and KNO<sub>3</sub> concentration could be calculated (shown in Figure 5).

The surface potentials of montmorillonite particles within Li<sup>+</sup>, Na<sup>+</sup>, and K<sup>+</sup> solutions at the same concentration were all the same value, according to the classical theory calculation. However, Li<sup>+</sup>, Na<sup>+</sup>, and K<sup>+</sup> have different quantum fluctuation properties, resulting in different effects on surface potential. So it is essential to consider the specific ion effects on the calculation of surface potential in Na/K solutions. As can be seen from figure 5, Li<sup>+</sup> has the biggest surface potential, followed by Na<sup>+</sup> and the lowest K<sup>+</sup> at any given electrolyte concentration. For example, when the electrolyte concentration equals to 50 mmol/L, the surface potential values of montmorillonite particles are calculated to be  $-161.8$  mV,  $-114.8$  mV, and  $-88.39$  mV for Li<sup>+</sup>, Na<sup>+</sup>, and K<sup>+</sup>, respectively. It can be seen that, at this concentration, the surface potential for Li<sup>+</sup> is 1.409 and 1.831 times as much as those for Na<sup>+</sup> and K<sup>+</sup>, which indicates the strongest quantum fluctuation and the strongest charge neutralization of K<sup>+</sup>, followed by Na<sup>+</sup>, and shows good agreement with the aforementioned result of specific ion effects on the CCC value.

Figure 6 shows that for Li<sup>+</sup> and Na<sup>+</sup> or Li<sup>+</sup> and K<sup>+</sup>, their surface potential differences for the aggregation of montmorillonite particles increase with the decrease in ion concentrations. In other words, the decrease in ion concentrations leads to an obvious increase in specific ion

effects for the cation species. This originates from the strong polarization effects, resulting from coupling between the quantum fluctuation of ionic outer shell electrons and the surface electric field, which is the origin of  $\text{Na}^+$  and  $\text{K}^+$  specific ion effects (Liu et al., 2013; Tian et al., 2014).

Generally, the surface potential is much higher than the Stern potential. The surface potential is about seven times as high as the Stern potential considering specific ion effects. The surface potential and Stern potential increase with decreasing polarization of ions (Liu et al., 2015). Therefore, the classical theory calculation neglecting the specific ion effects or taking Stern potential as the surface potential cannot obtain the correct result comparison with the experimental data, especially at low ion concentrations.

## Conclusion

The surface potential of mineral montmorillonite was strongly affected by the specific ion effects. At any given electrolyte concentration, the effects of these three ions on surface potential from strong to weak followed the order  $\text{K}^+ > \text{Na}^+ > \text{Li}^+$ .

A fluctuation coefficient  $\beta_{\text{Na}} = 1.187$  and  $\beta_{\text{K}} = 1.433$ , which could either quantitatively characterize the strength of specific ion effects or were introduced into the calculation of surface potential in order to obtain more accurate surface potential considering specific ion effects. In addition, the potential curve stepwise approaching method, as a convenient method, can be used to measure the Hamaker constant of polydisperse colloidal particles. The effective Hamaker constant of montmorillonite was  $A_{\text{eff}} = 10.75 \times 10^{-20}$ .

## Data availability statement

The original contributions presented in the study are included in the article/Supplementary Material; further inquiries can be directed to the corresponding author.

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XG: funding acquisition, sample analysis, data curation, and writing—original draft. ZZ: sample analysis and format modification. JZ: data curation and format modification. JW: supervision and writing—review and editing. YX: funding acquisition, data curation, and writing—review and editing.

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## Conflict of interest

The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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