



Soliton Generation in Negative Thermal Expansion Materials

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Strain solitons have been observed statically in several 2D materials and dynamically in substrate materials using ultrafast laser pulses. The latter case relies on lattice relaxation in response to ultrafast heating in a light-absorbing transducer material, a process which is sensitive to the thermal expansion coefficient. Here we consider an unusual case where the sign of the thermal expansion coefficient is negative, a scenario which is experimentally feasible in light of rapid and recent advances in the discovery of negative thermal expansion materials. We present numerical solutions to a nonlinear differential equation which has been repeatedly demonstrated to quantitatively model experimental data and discuss the salient results using realistic parameters for material linear and nonlinear elasticity. The solitons that emerge from the initial value problem with negative and positive thermal expansion are qualitatively different in several ways. The new case of negative thermal expansion gives rise to a nearly-periodic soliton train with chirped profile and free of an isolated shock front. We suggest this unanticipated result may be realized experimentally and assess the potential for certain applications of this generic effect.

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1 INTRODUCTION

The propagation of strain waves through materials originating from an initial disturbance is of high interest to a variety of theoretical, experimental, and technological efforts. A practical method of realizing this context involves use of a laser light pulse incident on an opaque material surface. The resultant energy absorption, heating, and subsequent thermal expansion can generate a dynamic strain profile capable of propagating over macroscopic distances. Early ultrafast laser experiments at low laser fluence (energy density) generated and subsequently detected acoustic strain pulses and related this observed sound propagation to the linear elastic properties of the propagation medium (Thomsen et al., 1984; Eesley et al., 1987; Wright, 1992). As experimentation with ultrafast lasers advanced, experiments were developed which are sensitive to the nonlinear elastic properties as well (Hao and Maris, 2001; Muskens, 2004). In particular, strongly pumped materials are observed to generate solitary solutions called solitons which move at supersonic speeds and do not disperse in contrast to the weakly-pumped experimental regime. To our knowledge, all such experiments have been performed on materials with positive thermal expansion (PTE).

For many years, mention of negative thermal expansion (NTE), a materials tendency to shrink when heated, evoked discussion of liquid water ice expansion responsible for icebergs and the 4 K temperature window above the ice water phase boundary where phase fluctuations occur. However, since the late 1990s, many materials have been identified and discovered which have strong NTE

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(Sleight, 1998; Goodwin et al., 2008; Miller et al., 2009; Azuma et al., 2011; Lind, 2012; Takenaka, 2012; Dove and Fang, 2016; Qu et al., 2017; Attfield, 2018; Takenaka et al., 2019) over a large range of temperatures and material compositions. NTE materials hold promising application potential in stabilizing fiber Bragg gratings for high-speed telecommunication (Fleming et al., 1997; Kowach and Ramirez, 2002), substrates for devices which benefit from controllable stresses, and rigid composite materials with engineered thermal characteristics through combinations of PTE and NTE components (Balch and Dunand, 2004; De Buysser et al., 2004; Lommens et al., 2005; Sullivan and Lukehart, 2005; Lind et al., 2011). Here we explore the potential use of NTE materials as strain pulse transducers.

2 STRAIN PULSE PRODUCTION AND DETECTION IN SOLIDS

Figure 1 shows a typical scheme capable of demonstrating the development of strain solitons. An ultrafast laser pulse (~10-200 fs) delivers energy Q over an area A of a lightabsorbing transducer film (reflectivity R, volumetric specific heat C) deposited on a substrate. The deposited energy per unit area (1-R)Q/A is absorbed by the transducer film, first heating electrons which thermalize with the lattice degrees of freedom within a few picoseconds. Immediately following electron-lattice thermalization, heat distributed within the optical absorption depth ζ drives a depth-dependent temperature profile $\Delta T(z)$, where z is the direction of propagation into the sample (Matsuda et al., 2015). The resultant ultrafast heating introduces a sudden thermal stress within the illuminated volume $\sigma_T = -3B\alpha_L \Delta T$ where *B* is the bulk modulus and α_L is the linear coefficient of thermal expansion (CTE) (Hao and Maris, 2001; Matsuda et al., 2015). This thermal stress induces a thermal strain $\eta_0 = \frac{3B\alpha_L(1-R)Q}{AC\zeta\rho_0^2}$, which depends on the equilibrium mass density ρ and the sound speed c_0 in the direction normal to the surface, but is also proportional to the linear CTE α_L in a direction perpendicular to the plane of the film.

Here, we consider only transducer films of cubic crystal symmetry. As observed in many experiments (Hao and Maris, 2001; Wright et al., 2001; Muskens et al., 2004; Péronne and Perrin, 2006; Schmidt et al., 2008; Wang et al., 2010; Péronne et al., 2017), this initial strain profile enters the underlying substrate and evolves as a propagating strain wave which can be detected after propagation over macroscopic mm-lengths scales typical of sample dimensions.

For small amplitude of the initial strain η_0 , evolution of the propagating strain pulse $\eta(z, t)$ moves at the speed of sound with subtle shape changes which can be described by the dispersion $\omega_{LA}(\vec{k})$ of the longitudinal acoustic wave appropriate in the regime of linear (Hooke's law) elasticity. For larger amplitude of the initial strain pulse, where nonlinear elastic properties of the substrate material govern strain evolution, solitons can be observed after propagation through the substrate. These phenomena are sensitive to the nonlinear elasticity, sound wave dispersion, and density and can be described quantitatively in this context using a one-dimensional Korteweg-deVries equation (Korteweg and de Vries, 1895; Gardner et al., 1974; Whitham, 1999; Debnath, 2007):

$$\frac{\partial \eta}{\partial t} + \frac{C_3}{2c_0\rho} \eta \frac{\partial \eta}{\partial y} + \gamma \frac{\partial^3 \eta}{\partial y^3} = 0$$
(1)

Here, C_3 is the appropriate nonlinear elastic parameter, γ quantifies the curvature of the acoustic dispersion $\omega_{LA}(\vec{k}) = c_0 k - \gamma k^3 + \dots$, and y is a co-moving spatial coordinate which moves at the sound speed c_0 : $y = z - c_0 t$. A key feature of the solutions of Eq. 1 is the emergence of solitons, which are local regions of high density which move at supersonic speeds and propagate without distortion. Below we present numerical solutions (Landau and Pez, 2018) of profiles Equation 1 using various initial strain corresponding to a transducer with conventional positive (PTE) or negative (NTE) thermal expansion and substrate parameters corresponding to sapphire with strain wave propagation along the 100 direction, a specific case where much experimental work has been done (Hao and Maris, 2001; Wright et al., 2001; Muskens et al., 2004; Péronne et al., 2017). For the case of conventional CTE in the transducer film, the initial pulse front is compressive but the detailed shape depends upon a number of factors. Naively, the exponentially extinguished profile of the incident laser light pulse sets up an exponential temperature profile and therefore an exponential strain profile. However, known effects of electronic diffusion affect the electron-lattice thermalization (Tas and Maris, 1994; Wright, 1994) on a similar time scale to the light absorption in typical laser systems. A recent direct measurement using ultrafast Sagnac interferometry and a propagation analysis accounting for acoustic dispersion has been observed to have a Gaussian-derivative profile (Péronne et al., 2017):

$$\eta(y,t=0) = -\eta_0 \frac{y}{\sigma} e^{-\frac{y^2}{2\sigma^2}}.$$
 (2)



We use this initial strain profile in the simulations presented here. In real experiments, the transducer film is typically aluminum, gold, palladium alloys, or other opaque materials with conventional thermal expansion $\alpha_L > 0$ (Wang et al., 2010). The primary consequence of a transducer with positive thermal expansion is a compressive front and $\eta_0 > 0$, corresponding to negative strain followed by a dilatational trailing edge. After discussing these PTE results, we will compare the evolution for the NTE case with $\eta_0 < 0$. Numerical solutions to **Equation 1** with the initial strain profile in **Eq. 2** were performed using a finite difference scheme following (Landau and Pez, 2018). Here, the first-time step is solved using a forward difference scheme while the remaining time steps use a central difference scheme, following other analyses of experimental data (Muskens, 2004; Mogunov et al., 2020).

The material dependent dispersion and nonlinear parameters used in the numerical calculation were those for a *z*-cut (1,000) sapphire (Al₂O₃) substrate. In all calculations we used the known parameters (Hao and Maris, 2001) $C_3 = -18.3 \times 10^{11} \text{ g/(mm s}^2)$, $c_0 = 11.23 \times 10^6 \text{ mm/s}$, $\rho = 3.98 \times 10^{-3} \text{ g/mm}^3$, and $\gamma = 3.50 \times 10^{-8} \text{ mm}^3$ /s.

Figure 2A shows that with $\eta_0 = +3.0 \times 10^{-4}$ the initial profile shown for 0 ns evolves dynamically according to **Equation 1** into a linear-sloped shock front near y = 0. In addition, several well-separated compressive solitons emerge on the supersonic side of the shock front y > 0. The leading solitons are strongest and the strength decreases linearly with soliton number as the shock front is approached around y = 100 nm. Under these conditions, numerical solution of **Eq. 1** comports with experiments and

describes well the evolution of an initial strain pulse into a shock front and a set of supersonic solitons followed by a dispersive tail - an oscillatory strain profile traveling at subsonic speeds. These phenomena are labeled in **Figure 1** and have been demonstrated in a host of materials (e.g. MgO (Hao and Maris, 2001), Sapphire (Hao and Maris, 2001; Muskens, 2004), GaAs (Péronne et al., 2017)).

Figure 2B shows that increasing the initial strain amplitude to $\eta_0 = 5.75 \times 10^{-4}$ increases the number of solitons produced, steepens the shock front, and extends the dispersive tail. The increase in the number of solitons is expected from theoretical grounds where the number of solitons can be related to the number of bound states of a Schrodinger equation whose potential shape is set by the initial strain profile (Gardner et al., 1974; Debnath, 2007). Since increasing the initial strain profile effectively deepens the potential, more bound states and therefore solitons are expected. The initial strain profiles considered here are shown as the t = 0 ns traces in **Figures 2A,B, 3A,B**.

3 RESULTS: STRAIN WAVES PRODUCED IN MATERIALS WITH NEGATIVE THERMAL EXPANSION

Recent discoveries in synthesis of materials with low and negative thermal expansion in a wide variety of material contexts has motivated



us to explore how the production of solitons would be impacted by the case $\alpha_L < 0$. There is much interest in systems which exhibit this remarkable material behavior, particularly because strong NTE has been observed in the vicinity of low-temperature phase transitions. For example, insulating perovskite ScF₃ appears to have an incipient structural instability (Handunkanda et al., 2015; Wendt et al., 2019; Bird et al., 2020) while semiconducting Sm_{1-x}Y_xS (Takenaka et al., 2019; Mazzone et al., 2020) shows an unusual magnetic transition at low temperature. Experiments of the type proposed here are nondestructive and sensitive to other lattice-related materials properties and may benefit NTE research in certain contexts.

Specific candidates of opaque NTE films include metallic perovskite ReO₃ (Chatterji et al., 2009a; Chatterji et al., 2009b; Rodriguez et al., 2009), semiconducting Sm_{0.8}Y_{0.2}S (Takenaka et al., 2019; Mazzone et al., 2020), and insulating Si (Shah and Straumanis, 1972) or CdTe (Greenough and Palmer, 1973; Jovanovic et al., 2014) at low temperature at pump photon energies exceeding their band gap (1 and 1.51 eV at 300 K respectively (Bludau et al., 1974; Jovanovic et al., 2014)). Given recent advances in high-harmonic generation of laser sources, any NTE material could be considered if the photon energy exceeds the candidate material band gap. For the sake of exploring the physics of soliton evolution from NTE transducers, we assume the substrate would again be sapphire oriented along the 100 direction and we repeat the calculations of **Figure 2** with $\eta_0 < 0$ describing the initial strain pulse. Physically

this means the initial pulse has a dilatational/low density front and compressive/high density tail.

Figure 3 shows results of KdV evolution of a strain pulses produced from a NTE transducer with the same magnitudes as in Figure 2. Both PTE and NTE cases produce a similar extended dispersive tail for y < -300 nm and clearly produce solitons. An exact correspondence is expected between the number of solitons in the NTE and PTE cases because the number of Schrodinger bound states of the initial strain profiles, which are related by a simple mirror reflection around y = 0, are exactly the same. However, strong differences in both the form of the shock front and distribution of solitons are apparent. For example, the soliton train in the PTE case emerges from the leading edge of the shock front discontinuity while for the NTE case solitons emerge from the back of the shock front. As for the case of a PTE transducer, several isolated supersonic solitons are produced within a few 10 s of ns. However, unlike the PTE case, they appear to merge continuously with the oscillatory tail and appear without a clearly isolated shock front.

4 SECTION: FITTING SOLITONS FOR PTE AND NTE CASES

The KdV equation permits analytic expressions describing isolated solitons and in this section we apply these to our





numerical solutions to determine and compare the distribution of solitons produced by NTE and PTE transducer films.

The KdV Eq. 1 has as solutions

$$\eta(y,t) = \eta_{s} \operatorname{sech}^{2} \left(\frac{\sqrt{\eta_{s}} (y - y_{s})}{w} \right)$$
(3)

where η_s is a measure of the strength of the soliton, y_s is the co-moving coordinate position where the soliton peaks, and $w = \sqrt{24\rho c_0 \gamma/C_3}$ is a material-dependent length which quantifies the soliton width. Specifically, the half-width-half maximum of the free soliton Eq. in 3 is $\delta = warccosh\sqrt{2}/\sqrt{\eta_s} \simeq 0.881 w/\sqrt{\eta_s}$. We model the shock front as a linear background with slope s which terminates at a critical value of the co-moving coordinate y_c . We sum each soliton contribution and the shock front in a nonlinear fit at late times and in the y range where solitons appear. Each soliton is parametrized by its strain η_s and the global material-dependent w =0.143 nm was fixed in both fits. The shock slope and intercept y_c was allowed to adjust between the NTE and PTE cases.

Figure 4 shows the result of the fitting procedure and particularly **Figure 4C** compares the strain parameter η_s versus soliton number as labelled in **Figures 4A,B**. Interestingly, the leading soliton (labelled 1) has similar strength in the PTE and NTE cases, but for the PTE case, the strength linearly decreases to zero as a function of soliton number, a phenomenon pointed out long ago (Zabusky and Kruskal, 1965). In contrast, the NTE transducer case shows that η_s is more uniform and so the soliton speed $U = c_0 + C_3\eta_s/6\rho c_0$ is also more uniform within the experimentally-accessible range considered here. This reveals a potential advantage of NTE transducers in retaining a periodic strain texture capable of propagating over long distances in functional acousto-optic devices.

5 DISCUSSION

Our simulations reveal qualitative differences in soliton trains generated from NTE and PTE transducer films. The phenomena are expected to be found for any NTE film on any substrate or within a single crystal of NTE material. Here we address possibilities for applications.

The ability to create well-defined propagating strain textures on nanometer length scales and nanosecond time scales portends functionality in novel electronic and acoustic device construction. Recent work analyzing the transient spectral response of excitons in GaAs to incident solitons (Scherbakov et al., 2007) has shown definitively an electronic-soliton coupling is present in this common device material. Recent investigations in 2D materials (Alden et al., 2013; Edelberg et al., 2020) have shown that static strain solitons form under certain conditions related to twisted van der Waals stacking patterns. These static solitons could be used to confine electronic states and one can consider dynamic soliton trains and the interaction between static and dynamic solitons may be sufficient to manipulate the charge states in novel device schemes.

Another clear feature of NTE-generated pulse trains is that they are more periodic than their PTE-generated counterparts. Figure 5 compares the spatial Fourier transforms of the pulse trains at different times and reveals that at early times, the NTE-generated pulse train is comprised of spatial frequencies much higher than in the PTE case, with significant spectral weight at Fourier wavevectors as large as $k \approx 0.4$ nm⁻¹, corresponding to fine periodic textures with space of order $2\pi/k \approx 15$ nm. This length scale corresponds to industry-leading features in integrated circuits and may present an inroad to novel devices. Furthermore, one may consider use of the fine periodic strain texture in potential applications related to transient diffraction gratings appropriate to photons in the vacuum ultraviolet and soft X-ray regimes. Currently, static diffraction gratings are constructed from conventional photolithography or novel contact-mode lithography methods (Gleason et al., 2017). If an appropriately conditioned periodic train of strain solitons can be produced simultaneously with arrival of an X-ray pulse, one may be able to produce a transient grating with configurable characteristics from an atomically smooth surface.

Importantly, the evolution of strain is related to the linear and nonlinear elasticity of the propagation medium. Here we have presented results for an opaque transducer film and compare the results of propagation through sapphire. However, similar considerations could model the case of an opaque single crystal specimen with unusual NTE. In the



pursuit of mechanistic descriptions of NTE capable of leading materials discovery efforts, anomalous behavior of such elastic parameters is of interest. In cases such as ScF₃ and Hg₂I₂, the lowtemperature behavior has been difficult to study due to proximity of a ferroelastic instability and a competing structural phase. Some methods of studying elasticity such as resonant ultrasound spectroscopy may be too invasive to be effective and the relatively weak perturbations of ultrasonic pulses are promising at addressing this experimental challenge.

6 SUMMARY AND CONCLUSION

In summary, we have provided the first assessment of the use of NTE materials as acousto-optic transducers for strain wave generation. In the case of strong, nonlinear acoustic response, unconventional strain textures are anticipated when the strain is generated from a NTE transducer film in comparison to the conventional PTE type where many experiments have been performed. In particular, while both the NTE and PTE cases ultimately produce the same number of solitons as anticipated, the NTE case delivers a soliton train with more uniform distribution of strain over the solitons present and significantly higher spatial frequencies at early times. Furthermore, while nonlinear strain profiles generated from conventional PTE transducer films have always been observed with clear separation of the shock front and solitons, in the NTE case the shock front and soliton train interacts strongly over the entire experimentally accessible time scale for the case we

have considered. We have suggested several technologically relevant applications for the effects observed. However, while we have considered a prevalent case of a thin transducer film on a z-cut sapphire substrate, solitons have been observed in many other applicable materials, suggesting more diverse phenomena beyond the scope of this work. Future efforts are needed to experimentally observe NTE solitons as well as understand their interactions and variability across materials classes.

DATA AVAILABILITY STATEMENT

The raw data supporting the conclusions of this article will be made available by the authors, without undue reservation.

AUTHOR CONTRIBUTIONS

All authors listed have made a substantial, direct, and intellectual contribution to the work and approved it for publication.

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