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# Assessing the liquefaction potential of seabed soils based on ocean ambient noise in the Yellow River Delta

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Seabed soils can undergo liquefaction under cyclic loading, resulting in a rapid decrease in strength and stiffness, which may lead to the destruction of offshore structures. Therefore, the assessment of seabed soil liquefaction will become an important factor in disaster prevention and risk analysis in coastal and offshore engineering construction. In this study, the ocean ambient noise with low-frequency, long-wavelength, and wide-band characteristics was used to conduct and analysis noise based on the horizontal-to-vertical spectral ratio method. The shear wave velocity of the seabed soil was obtained by inverting the ocean ambient noise dataset. Then, we proposed a shear wave velocity threshold that can be used for liquefaction assessment of Holocene unconsolidated fine-grained soils by statistical analysis, and the liquefaction potential of the soils was evaluated according to 1-D shear wave velocity structures and 2-D shear wave velocity profiles. The results showed that the distribution of the shear wave velocity obtained by inverting ocean ambient noise was generally consistent with the measured shear wave velocity in the field, indicating that the inversion results have a certain degree of accuracy. A shear wave velocity threshold of 200 m/s was proposed for liquefaction assessment, determining that the soils within 0-10 m depth in the coastal area of Yellow River Delta have liquefaction potential. This result is in accordance with the assessment based on the critical shear wave velocity, indicating that this threshold is applicable to the assessment of seabed soil liquefaction in the Yellow River Delta. The *in-situ* observations of ocean ambient noise provide a more convenient, economical, and environmentally friendly method, which can help to investigate marine geology disasters and serve marine engineering construction.

## KEYWORDS

ocean ambient noise, in-situ observations, shear wave velocity, inversion, liquefaction assessment

## 1 Introduction

Soil liquefaction is one of the significant factors affecting soil stability, among them, seabed soil liquefaction is a harmful marine geological disaster, which has attracted widespread attention from domestic and foreign geotechnical engineering and coastal engineering communities. Under the continuous erosion and scouring of waves, fine particles on the surface soil of the seabed migrate out and escape along the pores of the coarse particles, thereby forming larger pores in the soil (Dassanayake et al., 2022). This can destroy the structural integrity of the soil, and weaken the hydraulic properties (Jia et al., 2014) and engineering characteristics (Liu et al., 2013) of the soil, which may induce soil liquefaction under cyclic loading (Bachrach et al., 2001), causing damage to offshore structures such as submarine pipelines (Sumer et al., 1999; Zhou et al., 2013), offshore platforms (Sumer, 2014; Zhang et al., 2017), and breakwaters (Jeng, 2001; Zhao and Jeng, 2015). The Yellow River Delta is a typical rapidly deposited delta, and also the place with the densest offshore structures on the south coast of the Bohai Bay. The fine-grained soils such as silt and silty sand are widely developed in the Yellow River Delta, with weaker permeability and poorer water stability, which makes them more prone to unstable failure of soil such as liquefaction (Ren et al., 2020; Wang et al., 2022; Liu et al., 2023; Zhang et al., 2023). For this reason, accurately assessing the seabed liquefaction has become an essential part of disaster prevention and mitigation in the construction of the Yellow River Delta.

At present, there are three primary methods for assessing soil liquefaction: *in-situ* tests (Fergany and Omar, 2017), laboratory tests (Kumar et al., 2020), and numerical simulation (Ye et al., 2016; Zhao et al., 2018). These methods have been maturely applied in the study of liquefaction in sandy soils due to their safety and reliability (Amini and Qi, 2000; Dobry and Abdoun, 2017; Ye et al., 2018). However, for seabed soil, sampling measurements and laboratory tests can only obtain the physical and mechanical properties of shallow soil layers (Meng et al., 2018), and cannot guarantee the natural structure and stress state of seabed soil, resulting in failure to reflect the real dynamic response of soil. Numerical simulation can provide guidance for experimental research and theoretical analysis, but the simplification of boundary conditions and material properties in the numerical simulation process with a certain degree of randomness can lead to affect the reliability of the results. Furthermore, invasive *in-situ* tests such as standard penetration test (SPT) (Seed et al., 1983) and cone penetration test (CPT) (Boumpoulis et al., 2021; Geyin and Maurer, 2021) are complex and expensive, making them unsuitable for large-scale seabed measurements. Submarine acoustic exploration technology uses the acoustic properties of the compression waves (P-waves) and the shear waves (S-waves) to investigate the engineering properties of seabed soils. This method can effectively avoid measuring errors caused by disturbances, which is becoming a prominent means for studying the properties of seabed soils (Gorgas et al., 2002; Hou et al., 2018). Compared with the results of SPT and CPT testing, shear wave velocity ( $V_s$ ) is closely related to liquefaction resistance, and is influenced by factors such as porosity ratio, stress state, relative density, and soil type (Hardin and Drnevich, 1972;

Tokimatsu and Uchida, 1990; Xu et al., 2015). Moreover,  $V_s$  is one of the fundamental mechanical properties of soils, which can characterize the shear stiffness under small strain conditions and soil-structure interaction, and has potential application prospects in assessing soil liquefaction (Qin et al., 2020; Lin et al., 2021). Nevertheless, traditional shear wave velocity testing requires placing shear wave sensors in surface or underground boreholes, making it difficult to conduct measurements in the seabed. Moreover, the harsh seafloor environment and complex sediment structure seriously affect the measurement accuracy, and the high cost and limited measurement range restrict the development of submarine acoustic exploration technology.

There exist weak and low-amplitude vibration in the natural environment, known as ambient noise, which are commonly considered as an interference signal in geophysics. Over the past few decades, researchers have gradually discovered that ambient noise can be used to prospect subsurface structures (Aki, 1957; Toksoz, 1964). The composition of different body and surface waves in ambient noise is highly complex (Bonnetfoy-Claudet et al., 2006). Nakamura (Nakamura, 1989; Nakamura, 2008; Nakamura, 2009) proposed the horizontal to vertical spectral ratio method (HVSR), which normalizes the amplification effects of the horizontal and vertical components of ambient noise, calculates the Fourier spectrum ratio of the horizontal and vertical components of noise, and evaluates the ground response characteristics of soft sediment caused by multiple reflections of shear waves (Nakamura, 2000; Nakamura, 2019). The HVSR curve is closely related to the properties of the soil (Field et al., 1990; Field and Jacob, 1993) and is considered as a “transfer function” of the vertically incident shear wave in the strata (Nakamura, 1989; Nakamura, 2008). Kawase et al. (2011) proved that the horizontal-to-vertical spectral ratios match the ratios estimated from 1D shear wave velocity model using the simple theory of diffuse field. Therefore, based on the fundamental resonant frequency and spectral amplitude on the HVSR curve, the shear wave velocity can be estimated using an inversion algorithm (forward modeling routine and Monte Carlo method) and an empirical relationship between shear wave velocity and depth, such as the quarter-wavelength theory (Joyner et al., 1981; Boore, 2003; Edwards et al., 2011). The ambient noise on land is mainly caused by industrial machinery, vehicles, and other human activities, which is predominantly composed of high-frequency and short-wavelength noise (Bonnetfoy-Claudet et al., 2006). In contrast, ocean ambient noise is mainly caused by the action of waves on the seabed (Hasselmann, 1963; Bromirski et al., 2005), and it is a broad-band vibration with low-frequency and long-wavelength characteristics, which ensures that ocean ambient noise exploration has a greater detection depth and sufficient resolution.

The structure of this study is as follows: Firstly, we introduce the feasibility analysis for assessing the liquefaction potential of seabed soils based on shear wave velocities obtained by inverting ocean ambient noise. Secondly, we present the geological overview of the study area (the coastal zone of the Yellow River Delta). Third, we describe the inversion method and strategy of ocean ambient noise. Fourth, we discuss the characteristics of ocean ambient noise and the accuracy of inversion results, respectively. In addition, we propose and validate the shear wave velocity threshold that can

be used for fine-grained soil liquefaction assessment based on statistical analysis. Finally, we conclude this study by discussing and concluding the effectiveness, limitations and potential for assessing the liquefaction of seabed soils by the shear wave velocity obtained by the inversion of ocean ambient noise.

## 2 Geological overview

The Yellow River Delta is located on the southern coast of Bohai, and the Yellow River Delta Plain is a fluvial plain formed by the long-term siltation and continuous sea reclamation of high-concentration sediment carried by the Yellow River. We selected the northern coastal zone of the Yellow River Delta as our study area (Figure 1), which has an overall flat topography and gentle slope. The thickness of the Quaternary strata is about 26 m, with a horizontal distribution. Due to the special deposition pattern, silty soils are commonly developed in the surface sediments, with predominantly silt, fine sand and small amounts of clay (Zhao et al., 2013), showing the engineering characteristics of a high water content, poor grading, low bearing capacity, and high compressibility. In addition, thin-layered soft soil layers are widely developed in the stratum, with a thickness of about 1-5 m, which are interspersed with the sedimentary layers in a finger-like way. The engineering geological environment of the Yellow River Delta region is controlled by the sedimentary dynamic environment, which is mainly determined by the muddy and sandy nature of the Yellow River and its frequent siltation and migration. Owing to the migration of the Yellow River Estuary, the

sediment supply has been interrupted. In the northern coastal zone, under the action of long-term differential hydrodynamic forces, the structural integrity of the surface soil of the tidal flats are destroyed, leading to a decrease in strength and gradual erosion, which has formed a drop of nearly 1 m between the tidal flats and the embankment. Thus, the study of the engineering characteristics of seabed soil under dynamic action would be helpful to maintain the safety of marine buildings.

## 3 Inversion method

In this paper, the OpenHVSR-inversion program (Bignardi et al., 2018) is used to invert the HVSR curves of ocean ambient noise and obtain the shear wave velocity. This program can be used to model and invert HVSR dataset simultaneously, obtaining the distribution of shear wave velocity in different depth layers to construct 2-D or 3-D subsurface models. The forward modeling is based on the method proposed by Tsai and Housner (1970), which calculates the theoretical transfer function of the layered subsurface model. The inversion strategy is based on the Monte Carlo method, where a randomly perturbed version of the best fitting model is generated in each iteration, and used to compute a set of simulated curves for comparison with experimental curves. The generation of many trial models allows exploring the parameters space while searching for a new and better fitting model.

Several *in-situ* ambient noise recordings were carried out in the Yellow River Delta, and the observed distribution of fundamental frequency is shown in Figure 2, which is mainly concentrated in the range of 0.8-9.8 Hz (Meng et al., 2023). As a result, we set the frequency band for inversion from 0.6 to 10 Hz. The inversion was divided into three stages. In the first stage, the inversion was started with a simple 4-layer subsurface model (Table 1), limiting the frequency band to 0.6-4 Hz. Successively, when the best-fit model was found, the result was saved as a new project and the subsurface

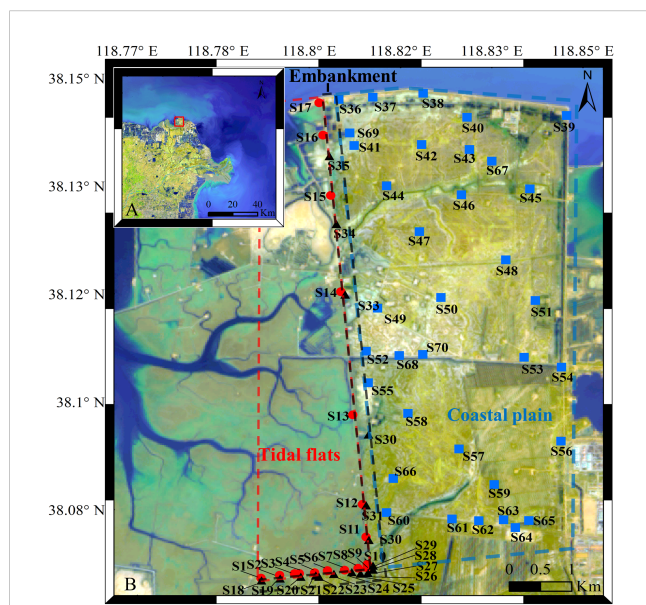


FIGURE 1

Map of the northern coastal areas of the Yellow River Delta. (A) The map of the study area (red rectangle). (B) The distribution of measurement stations within the study area. The red dashed line represents the tidal flats with the stations in red circles; the black dashed line represents the embankment with the stations in black triangles; the blue dashed line represents the coastal plain with the stations in blue square.

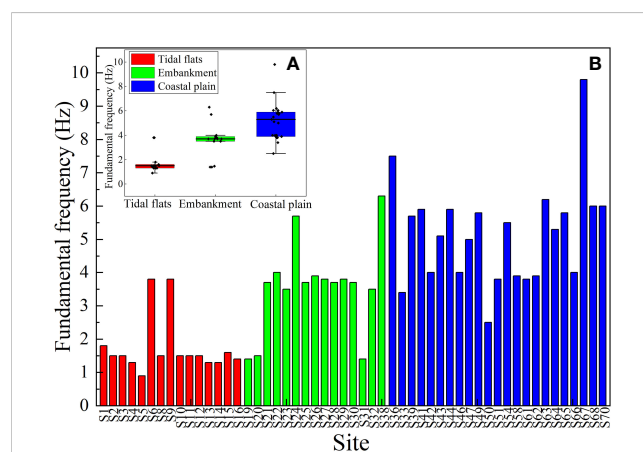


FIGURE 2

Statistics of fundamental frequency in the coastal zone of the Yellow River Delta (modified from Meng et al., 2023). (A) The distribution of fundamental frequency for stations in different study areas, where the red represents the tidal flats, the green represents the embankment, and the blue represents the coastal plain. (B) The fundamental frequency for all stations.

TABLE 1 Initial subsurface parametric model.

Compressive waves velocity/ $V_p$ (m/s)	Shear waves velocity/ $V_s$ (m/s)	Density $\rho$ ( $Kg/m^3$ )	Thickness $h$ (m)	P-waves damping $/Q_p$	S-waves damping $/Q_s$
386	192	1.7	30	15	5
620	310	1.8	30	25	10
792	390	1.8	40	30	15
1000	500	1.8	999	999	999

model was edited, dividing the deeper layer in three sublayers, while the total thickness of the layer remains unchanged. Then, set the frequency band for the second stage to 0.6-8 Hz and continue with the next, with the shallower layer dividing in four sublayers, and so on. The frequency band for the third stage was set at 0.6-10 Hz, with a total of 10 layers.

In each stage of the inversion, firstly, the longitudinal wave velocity, shear wave velocity, and thickness were allowed a 5% perturbation for 3000 iterations of global inversion. Secondly, the best-fitting model of the HVSR curve for each station was locally optimized, allowing a 15% perturbation of the parameters for 5000 iterations. Finally, 10000 iterations were performed with 20% lateral constraint perturbations. In order to provide a more intuitive description of the inversion results, an example of the inversion of the ocean ambient noise in the Yellow River Delta is given in Figure 3. Figure 3A illustrates the HVSR curve of the measured noise (black), the standard deviation (gray), the best-fitting curve obtained by Monte Carlo inversion (red), and the fitting curve generated by the last iteration of Monte Carlo inversion (blue). It can be seen that peaks are observed in the HVSR curve at both 1.9 Hz and 10 Hz in Figure 3A. According to the method for identifying the fundamental frequency proposed by Meng et al. (2023), the fundamental frequency of the soil at this station is 1.9 Hz, not 10 Hz, and the peak at 10 Hz was caused by the fundamental Rayleigh waves (Nakamura, 2008). The Figure 3A also shown the good consistency among the best-fit curve and the fitted curve generated by the last iteration with the HVSR curve. Figure 3B represents the

shear wave velocity structure of the observation station obtained by inversion of the ocean ambient noise.

To evaluate the accuracy of the inversion, we used two concepts: global misfit and local misfit. Local misfit refers to the normalized misfit between the simulated and experimental curve at each station. For the global misfit, we introduced the objective function (Biguardi et al., 2018):

$$E(m) = aM(m) + bS(m) + \sum_{j=1}^5 \alpha_j R_j(m)$$

Where  $M(m)$  represents the misfit between the simulated and experimental curves;  $S(m)$  represents the fitting degree of the simulated and experimental curves at the peaks; and  $R_j(m)$  represents the regularization term. The constants  $a$  and  $b$  in above Equation are used to balance the relative weight of the  $M(m)$  and  $S(m)$  terms. Based on the objective function, we define the global misfit as  $aM(m) + bS(m)$ .

Figure 4A shows the global misfit of the inversion results. As can be seen from the figure that the global misfit between the inversion results and experimental data is 0.1, and the fitting degree at the peak of the experimental curve and simulated curve is around 0.9. The normalized misfit between the experimental data and simulated data at each station is shown in Figure 4B, and it can be seen that there are 52 stations with a local misfit of less than 0.1; 6 stations with a local misfit between 0.1 to 0.2; and only 6 stations have a local misfit exceeding 0.2.

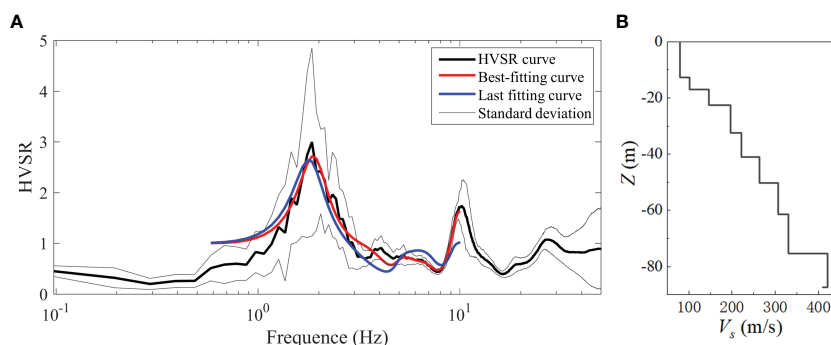


FIGURE 3 Example of inversion of marine ambient noise recording. (A) Best-fit model. (B) The structure of shear wave velocity corresponding to the best-fit model.

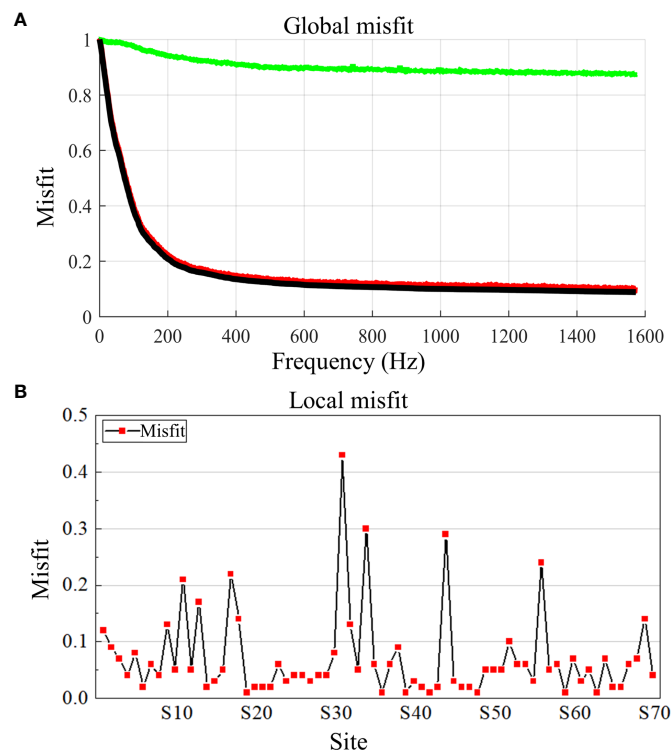


FIGURE 4

Value of the normalized misfit. (A) Global misfit, where the black curve represents the misfit of the inversion results (the  $aM(m)+bS(m)$  in Equation); the red curve is the misfit of the experimental and simulated curves (the  $aM(m)$  in Equation); and the green curve is the fitting degree at the peak of the experimental and simulated curves (the  $bS(m)$  in Equation). (B) Normalized misfit for each station at the end of the inversion.

## 4 Results and discussion

### 4.1 Characteristics of ocean ambient noise

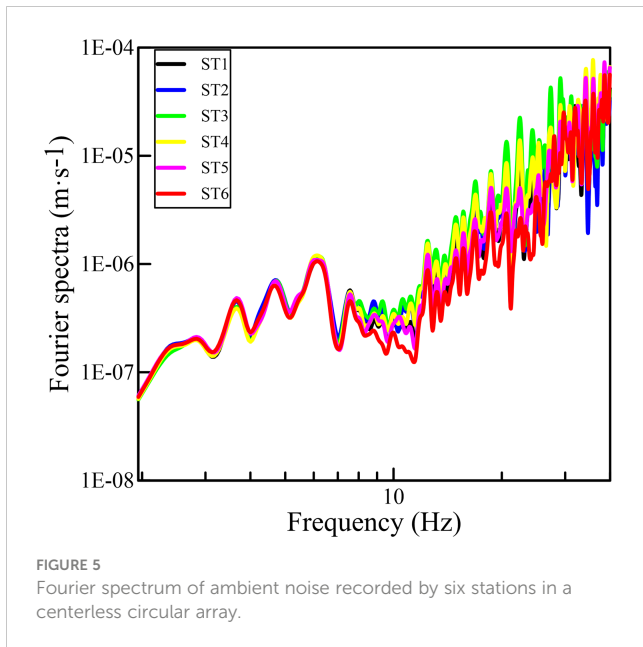
Ocean ambient noise is a persistent acoustic field in the ocean, and different sources produce noise of different frequencies (Bonnefoy-Claudet et al., 2006). The movement of the Earth's crust is the primary source of ultra-low frequency noise in the ocean, with quasi-periodicity of 1-7 Hz; nonlinear interaction of back-propagating sea surface waves produces random noise with frequencies between 5-10 Hz; sound waves emitted by atmospheric sources (such as lightning) can couple into the underwater sound field, with frequencies also below 10 Hz; ship navigation produces sound waves with frequencies ranging from 5-500 Hz; and deep-sea currents, internal solitary waves, and turbulence caused by fragmentation create a wider frequency range. In the coastal and nearshore noise fields, waves, as the primary source of noise, waves striking along the coasts are the main source of low-frequency noise with a range of 0.5-1.2 Hz (Gutenberg, 1958), and the strong interaction between waves with the seabed can generate noise up to 10 Hz (Olofsson, 2010). In this paper, we concern the ambient noise with frequency below 10 Hz.

We conducted ocean ambient noise recordings using the single-station array and the centerless circular array with a radius of 1 m on the tidal flats in the Yellow River Delta. Figure 5 shows the Fourier spectrum of ocean ambient noise recorded by six stations in

the centerless circular array. There is a certain energy of ambient noise in each station from low to high frequencies. The Fourier spectrum shows good amplitude consistency in the low-frequency band (1.9-7.7 Hz) and differentiation in the high-frequency band. Thus, it could be considered that the ocean ambient noise propagates in all directions with almost the same energy in each direction within this band. According to the analysis of the characteristics, the ocean ambient noise recorded on the tidal flats in the Yellow River Delta shows a good consistency in the low-frequency band and relative dispersion in the high-frequency band. We analyze that the factors such as waves, tides, and wind are the main sources of noise on the tidal flats, so the recorded noise mainly presents low-frequency and long-wavelength characteristics, and of course, it also contains some high-frequency and short-wavelength noise generated by the navigation. Compared with land ambient noise, ocean ambient noise dominates in the low-frequency band, which can be used to obtain deeper seabed soil information.

### 4.2 Inversion results of shear wave velocity

After obtaining the inversion results, the distribution of shear wave velocity within the depth range of 0-100 m was statistically analyzed. The confidence intervals of the shear wave velocity at the confidence levels of 95% and 75% were also calculated, as shown in Table 2. The accuracy and applicability of the inverted shear wave



velocity were tested by comparing them with the field measurements (Liu et al., 2015).

From Table 2, it can be found that the average, minimum and maximum values of shear wave velocity obtained by inversion are basically consistent with the field measurements at depths of 10-90 m depth. However, the ranges of shear wave velocities obtained from the inversion are underestimated in the depth of 0-10 m. Among them, the shear wave velocity obtained from the inversion respectively are 83-102 m/s and 87-98 m/s at 90% and 75% confidence intervals, which deviate from the field results of 108-183 m/s and 123-167 m/s. The inversion results are lower compared with the measured results, -which is speculated to be related to the groundwater table. The field measurements of shear wave velocity

were carried out at locations far from the sea, while the study area is located in the coastal zone with extremely shallow groundwater table and high soil moisture content, resulting in a lower shear wave velocity. Within the range of 10-90 m, the distribution of the inverted shear wave velocity in the stratum satisfies the results of the field measurements at the 95% and 75% confidence intervals. Nevertheless, in the depth range below 30 m, the maximum value of the shear wave velocity and the lower limit of the 95% confidence interval are both higher than the measured data. Moreover, there exist an abnormally high value for the inverted shear wave velocity at the bottom layer.

Liu et al. (2007) conducted shear wave velocity tests on the northern coastal zone in the Yellow River Delta and obtained measured shear wave velocities of 91-137 m/s within the depth range of 0-10 m (Table 3). Yang et al. (2022) carried out field measurements using the single-hole method on tidal flats in the Yellow River Delta, and the measured shear wave velocities were mainly distributed in a range of 100-250 m/s within the depth range of 0-20 m. The inverted results are in good agreement with the field measurements, which further proves the accuracy of the inversion shear wave velocities.

### 4.3 Shear wave velocity threshold

Andrus and Stokoe (Andrus and Stokoe, 1999; Andrus and Stokoe, 2000; Andrus et al., 2004) proposed a simplified method for soil liquefaction assessment using shear wave velocity ( $V_s$ ) and stress-corrected shear wave velocity ( $V_{s,t}$ ) based on a large amount of investigations of earthquake liquefaction occurring in fine-grained soils, such as fine sand, gravel, and silty clay. For Holocene unconsolidated fine-grained soil, Youd and Idriss (2001) established the relationship between  $V_s$  and cyclic stress ratio (CSR) for liquefaction and non-liquefaction areas according to

TABLE 2 Distribution of shear wave velocity obtained by HVSR curves inversion and measured field data from Liu et al. (2015).

Depth (m)	Average value (m/s)		Minimum value (m/s)		Maximum value (m/s)		Standard deviation (m/s)		Confidence interval (m/s)			
									Confidence 95%		Confidence 75%	
	A	B	A	B	A	B	A	B	A	B	A	B
1-10	145	93	100	80	233	134	19.1	19.4	108-183	83-102	123-167	87-98
11-20	191	206	130	117	318	297	27.6	43.6	137-245	185-227	159-223	196-218
21-30	245	259	152	166	369	373	31.7	66.5	183-307	227-291	208-281	241-277
31-40	264	266	179	146	377	486	34.4	87.1	196-331	224-308	224-303	242-290
41-50	301	318	202	214	397	423	33.1	53.1	236-366	293-344	263-339	304-333
51-60	328	321	231	222	431	425	31.3	67.0	267-390	288-353	292-364	302-339
61-70	349	359	255	285	446	510	29.3	61.3	291-407	330-389	315-383	342-376
70-80	369	381	260	230	479	490	33.3	83.3	303-434	340-421	330-407	358-403
81-90	390	411	291	286	491	499	32.8	57.4	326-455	384-439	352-428	396-427
91-100	414	443	309	296	501	856	32.4	121.9	350-477	384-501	376-451	410-476

The A stands for inversion results and the B stands for field test data.

TABLE 3 Field measured shear wave velocity and calculated critical shear wave velocity in the Yellow River Delta (modified from Liu et al., 2007).

Depth (m)	shear wave velocity (m/s)	stress-corrected shear wave velocity (m/s)
1	91	136.98
2	115.6	141.47
3	127.4	151.37
4	155.9	150.39
5	150.3	152.59
10	137.7	160.43

a probabilistic statistical method and proposed the upper limit of  $V_s$  (180 m/s) as a threshold for liquefaction assessment in engineering practice (Yulianur et al., 2020). However, statistical analysis of the relationship between stress-corrected shear wave velocity and CSR revealed certain limitations of this threshold. To illustrate this viewpoint, we collected the investigation data from over 50 different locations. The liquefaction areas were determined by the observation of liquefaction phenomena and *in-situ* tests (SPT and CPT). The relationship between the cyclic stress ratio (CSR) and shear wave velocity or stress-corrected shear wave velocity is established based on probabilistic statistics of the distribution of shear wave velocity.

Figure 6A shows the relationship between CSR and the measured average  $V_s$  in liquefaction and non-liquefaction fields, and Figure 6B presents the relationship between CSR and  $V_{s1}$ . The measured  $V_s$  of soils in liquefaction area ranged from 79 to 210 m/s, generally lower than 180 m/s, with only four data exceeding this threshold for an

error of about 4%. Differently, the distribution of  $V_{s1}$  ranged from 104 to 271 m/s, with 15% of the data exceeding 180 m/s. As a result, it may be risky to use the shear wave velocity of 180 m/s as the threshold for soil liquefaction assessment in practical engineering applications. The confidence interval of  $V_{s1}$  in 95% confidence is 149.10-160.47 m/s, with 95% of the data below 200 m/s. Accordingly, it is considered that 200 m/s as the threshold for liquefaction assessment of fine-grained soils will be of practical application.

### 4.4 Soil liquefaction assessment

According to the statistics of the field investigation data for soil liquefaction, wave-induced soil liquefaction generally occurs in shallow surface seabed within a few meters (Hirst and Richards, 1977; Sassa et al., 2006), and depth of the seismic liquefaction may occur up to 20 m below the surface in the gravel, and the depth in silt and silty sand is commonly less than 20 m (Holzer et al., 1999; Bray et al., 2004). Liu et al. (2005) considered that the silt soils in the Yellow River Delta have liquefaction potential under dynamic loads based on the pore-pressure model. As shown in Tables 2, the inverted shear wave velocity is in general agreement with the field measured results within 30 m depth. Consequently, it can be used to evaluate problems such as seabed soil liquefaction.

Figure 7 shows the shear wave velocity structures of three areas on the coastal zone. The red dashed line and solid line represent the dividing lines of shear wave velocity of 180 m/s and 200 m/s, respectively. It can be seen that the vertical distribution of shear wave velocity corresponds roughly to the boundaries of soil indicated by the borehole Yang et al. (2022). Moreover, the shear wave velocity of the soil within a depth of 10 m is generally less than

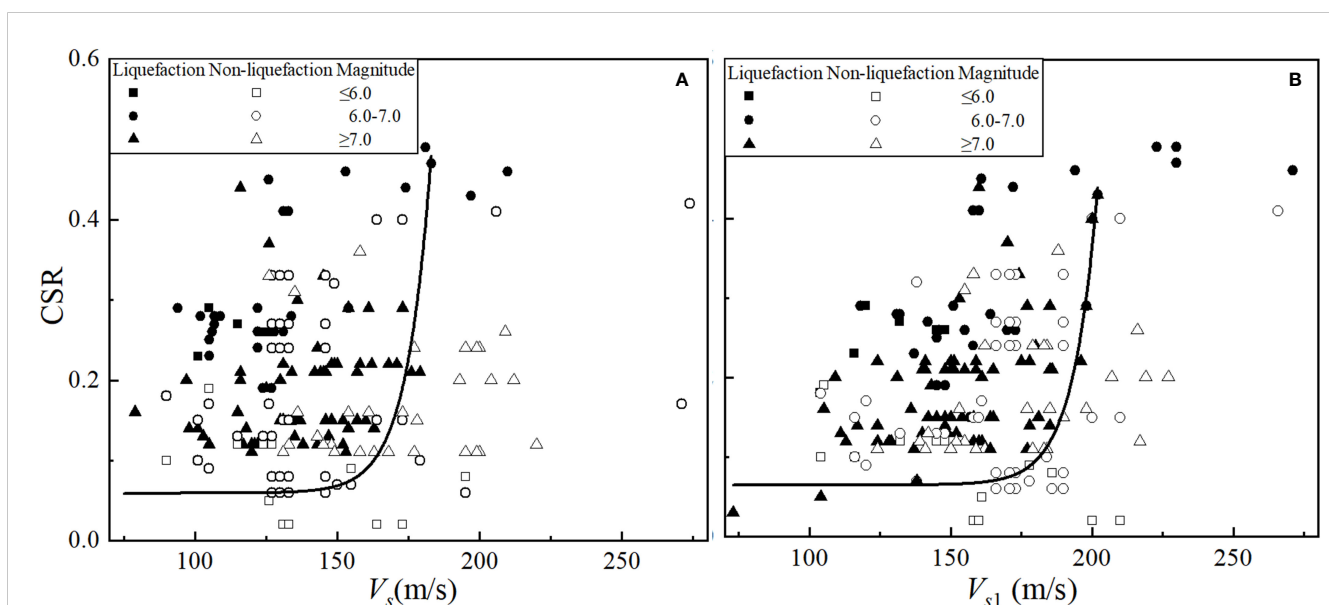
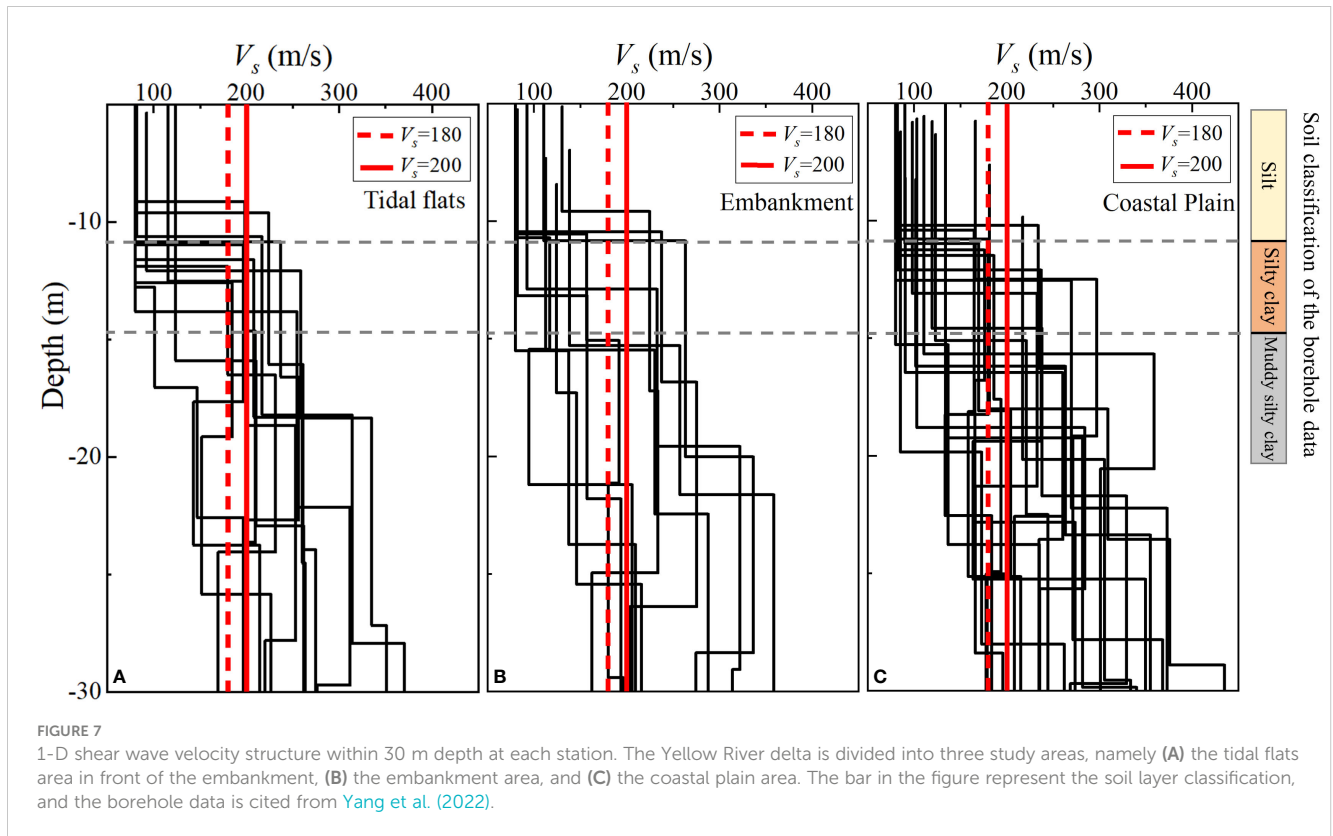


FIGURE 6  $V_s$ -based liquefaction and non-liquefaction for Holocene unconsolidated fine-grained soils. (A) The relationship between the measured  $V_s$  and cyclic stress ratio (CSR). (B) The relationship between  $V_{s1}$  and CSR. In the figures, the square, circle and triangle represent respectively shear wave velocities of soils with earthquake magnitudes  $\leq 6.0$ , 6.0-7.0,  $\geq 7.0$ ; the solid and hollow figures correspond to shear wave velocities liquefaction and non-liquefaction areas respectively.



200 m/s, indicating that the fine-grained soil at this depth has a certain potential for liquefaction. Liu et al. (2007) calculated the critical shear wave velocity within the range of 0-10 m based on the empirical relationship between shear wave velocity and the number of blows of standard penetration, which is found to be from 136 to 160 m/s (Table 3). The inverted shear wave velocity within the depth range of 0-10 m is determined to be between 80-133.87 m/s, which is lower than the critical shear wave velocity for each layer. Therefore, it is determined that the soil within the range of 0-10 m on the tidal flat was judged to be liquefiable. The results of the soil liquefaction assessment based on the shear wave velocity threshold and the critical shear wave velocity were consistent within the depth range of 0-10 m. Meanwhile, it can be observed that there were multiple low-velocity anomalies in the vertical shear wave velocity structure of the strata, and there were significant differences in the shear wave velocity of the soil at the same depth range in the lateral direction. As shown in Figure 7, from the coastal plain to the tidal flat in front of the embankment, the shear wave velocity of the soil follows the trend of gradually decreasing from land to sea. According to geological data in the region, the high-concentration sediment continuously accumulates during the transportation process of the river due to oscillation and diversion of the Yellow River estuary, sea level changes, and the combined effects of waves, tides, and storm surges. The fluvial deposits and coastal deposits in different periods have been superimposed and deposited, forming a sedimentary structure that appears as a finger-like interlocking in the horizontal direction, and the gradually advancing from land to sea in the vertical direction. In different depth ranges, there are

marine deposits with high water content and high saturation, as well as soft soil layers with high water content, high porosity ratio, and low shear strength, which are unevenly distributed in the tidal flat. This results in the common presence of low-velocity abnormal segments in the shear wave velocity structure.

A measuring line was set up along the east-west direction on the tidal flat in front of the embankment in the Yellow River Delta. Figure 8 shows the inversion results of seven observation stations on the tidal flat. Figure 8A shows the shear wave velocity profile within a depth range of 30 m. For comparison, we first converted the frequency to “pseudo-depth” using the quarter-wavelength formula ( $h=V_s/4f$ ) to obtain the HVSR curve with depth, then, we plotted the HVSR profiles in Figure 8B with interpolation method based on all curves. The figure shows that the shear wave velocity of the geological layer exhibits a layered distribution, which is consistent with the sedimentary characteristics of the region. Geological layers with a shear wave velocity less than 200 m/s are distributed within a depth range of 10 m, and some stations can reach 20 m. The distribution of the HVSR shows a negative correlation with the magnitude of the shear wave velocity (Figure 8B). The level of the horizontal and vertical spectral ratio of ambient noise reflects the amplification effect of the soil on seismic motion. The looser the soil, the more significant the amplification effect of the seismic wave amplitude is, while the noise spectral ratio is larger. At the same time, soft soil has a lower degree of compaction and a lower shear wave velocity. It can be understood that the shear wave velocity of the surface soil of the tidal flats is low and its engineering properties are poor. Soft surface soil will amplify the amplitude and energy of



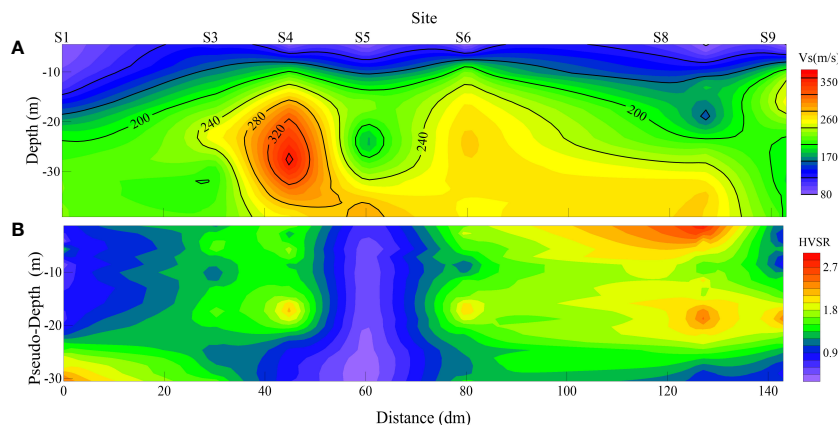


FIGURE 8

Inversion results along the east-west lateral line of 7 observation stations on the tidal flat in the Yellow River Delta. (A) 2-D Shear wave velocity profile of the tidal flat. (B) For comparison, the HVSR profile is formed by the HVSR curves, and the frequency axis is converted to “pseudo-depth” by the assumption that  $V_s=350$  m/s for soft layers.

seismic waves. If seismic waves in a certain frequency band coincide with the resonance frequency of the overlying soil, the resonance effect will be induced, which will cause unpredictable damage to the overlying buildings.

## 5 Conclusion

The purpose of this paper is to obtain the shear wave velocity of seabed soils by inversion of ocean ambient noise for rapid assessment of seabed soil liquefaction. *In-situ* noise recording and analysis were performed in the northern coast of the Yellow River Delta using the HVSR method to obtain the shear wave velocity of the seabed soil. Based on statistical analysis of liquefaction investigation data, a shear wave velocity threshold was proposed for assessing the liquefaction potential, and the location of liquefiable soil was identified in the light of 1-D shear wave velocity structure and 2-D shear wave velocity profile. In summary, the following results were obtained:

1. Ocean ambient noise has the characteristics of low-frequency, long-wavelength, and wide bandwidth. Therefore, *in-situ* observations of ocean ambient noise can not only obtain the physical and mechanical properties of the seabed soil in a deeper range depending on the propagation characteristics of noise in the seabed sediment, but also monitor the deformation and stability of the seabed soil, provide the necessary support for the design and construction of marine engineering, and are of great significance for risk assessment and the early warning of marine geology disasters.

2. Shear wave velocities of seabed soils were obtained by inverting the HVSR dataset of oceanic ambient noise. The stratigraphic distribution of the shear wave velocity obtained by inversion is broadly consistent with existing research results, which indicates that the results have a certain degree of accuracy and that the method for inverting ocean ambient noise is quite feasible.

3. The application of a shear wave velocity threshold of 200 m/s in assessing the liquefaction potential of fine-grained soils in the Yellow River Delta yielded consistent results with traditional methods. The assessment showed the liquefaction potential of soil in depths of 0-10 m, and indicated that this threshold is reasonable for liquefaction assessment of seabed soil in the Yellow River Delta. Accordingly, the stability problems of the soil in the tidal flat area should be taken into sufficient consideration during engineering construction. It is necessary to adopt measures such as replacement methods and dynamic consolidation for foundation treatment to ensure the safety of engineering construction and use.

4. The HVSR-based ocean ambient noise prospecting method has the advantages of being convenient, economical, environment-independent, and deeper detection depth. It can provide services for disaster prevention and mitigation of marine engineering construction, and has good practical application. In addition, in the actual application process, combining this method with other geotechnical tests (such as drilling, *in-situ* tests, or laboratory tests, etc.) can more accurately determine the engineering characteristics of soil, and further classify the liquefaction hazard of soil, which is crucial for coastal protection and marine engineering construction.

## Data availability statement

The raw data supporting the conclusions of this article will be made available by the authors, without undue reservation.

## Author contributions

Conceptualization & methodology, YL, QM and SW. Formal analysis, YL and WW. Data curation, YL and YC. Writing—original draft preparation, YL. Writing—review & editing, YL and QM. Visualization, YC and SW. Project administration, YL and WW.

Funding acquisition, QM. All authors contributed to the article and approved the submitted version.

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## Conflict of interest

The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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