



Multivariate Adaptive Step Fruit Fly Optimization Algorithm Optimized Generalized Regression Neural Network for Short-Term Power Load Forecasting

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Short-term load forecasting plays a significant role in the management of power plants. In this paper, we propose a multivariate adaptive step fruit fly optimization algorithm (MAFOA) to optimize the smoothing parameter of the generalized regression neural network (GRNN) in the short-term power load forecasting. In addition, due to the substantial impact of some external factors including temperature, weather types, and date types on the short-term power load, we take these factors into account and propose an efficient interval partition technique to handle the unstructured data. To verify the performance of MAFOA-GRNN, the power load data are used for empirical analysis in Wuhan City, China. The empirical results demonstrate that the forecasting accuracy of the MAFOA applied to the GRNN outperforms the benchmark methods.

Keywords: power load, multivariate adaptive step, fruit fly optimization algorithm, generalized regression neural network, forecasting

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INTRODUCTION

It is well known that the role of short-term power load forecasting is increasingly crucial in the management of power plants. Short-term power load forecasting mainly refers to electric load forecasting in the next few hours, 1 day to several days. Accurate short-term power load forecasting can reasonably arrange the operation of units, ensure the safety of operation of the power grids, and improve the economic benefits of power enterprises (Friedrich and Afshari, 2015; Dudek, 2016). On the contrary, inaccurate forecasts will produce unnecessary electricity and result in considerable electrical power system losses (Yang et al., 2017). Hobbs et al. (1999) pointed that the reduction of 1% in load forecasting error of 10,000 MW utility can save up to \$1.6 million annually. So, it is of vital importance to achieve high accuracy for short-term power load forecasting nowadays.

With the development of computer technology, the theory of artificial neural networks (ANNs) has been applied in a wide range of fields such as power market, system engineering, and control system (Jiang et al., 2014; Liu et al., 2018; Du et al., 2019; Yang et al., 2022). The forecast of power load considers not only the load but also the factors that affect the load, so the use of ANNs has been highly concerned by researchers. For example, Xuan et al. (2021) combined the convolutional neural network (CNN) and bidirectional gated recurrent unit (Bi-GRU) to forecast the short-term load. In the meantime, the random forest was used to select features. The final result showed that this hybrid method had a higher accuracy. Wang et al. (2020) applied an extreme learning machine model to electricity price forecasting, as well as considering the influence of outliers. The Elman neural

network (ENN) model was also used to forecast the electrical power system (Zhen Wang et al., 2018). Abedinia and Amjady (2016) presented a new stochastic search algorithm to find the optimum number of neurons for the hidden layer, and they used the proposed method to predict the power load. They compared the obtained results with those of several other recently published methods, and it confirmed the validity of the developed approach. Lu et al. (2016) used the weighted fuzzy C-means clustering algorithm based on principal component analysis to determine the basis function centers, and they used the gradient descent algorithm to train the output layer weights. The proposed model was implemented on real smart meter data, and simulation results showed that the proposed method had good forecasting accuracy. Ding et al. (2016) applied variable selection and model selection to power load forecast to ensure an optimal generalization capacity of the neural network model, and the results showed that the neural network-based models outperform the time series models.

The generalized regression neural network (GRNN) is a type of ANNs based on mathematical statistics, proposed by Specht (1991). Instead of listing the equations in advance, the network uses a probability density function to predict the output. Therefore, the GRNN has strong non-linear mapping capability and quick learning speed, which is better than the radial basis function neural network. In addition, even if the number of input training samples is small, its output can converge to the optimal value, which is very suitable for solving the problem of non-linearity (Jiang and Chen, 2016; Zhu et al., 2018). It has been applied in a wide range of fields such as prediction of wind speed (Kumar and Malik, 2016), two-dimensional spectral images (Jianzhou Wang et al., 2018), automated emotion detection systems (Talele et al., 2016), short-term load forecasting (Hu et al., 2017), mineral resource estimation (Das Goswami et al., 2017), and the estimation of peak outflow (Sammen et al., 2017). The optimization of smoothing parameter is a crucial step in the application of GRNN. There are a few ways to estimate its value. For example, Agarkar et al. (2016) applied particle swarm optimization (PSO) to the smoothing parameter of GRNN, which reduced the time complexity and produced more accurate results than random selection of spread factor. Gao and Chen (2015) presented an improved GRNN algorithm, using phase space reconstruction to strike GRNN training samples, applying adaptive PSO algorithm to optimize the smoothing parameter. Zhao et al. (2020) applied PSO-GRNN for risk prediction of urban logistics and found that the model can handle the high-frequency influencing factors well. The result showed that PSO-GRNN can better improve the accuracy of prediction than others.

Recently, Pan (2012) proposed a fruit fly optimization algorithm (FOA) to optimize the financial distress model, which was based on the foraging behavior of fruit flies. This algorithm has been effectively applied in a few fields including the dual-resource constrained flexible job-shop scheduling problem (Zheng and Wang, 2016), monthly electricity consumption forecasting (Jiang et al., 2020), multidimensional knapsack problem (Meng and Pan, 2017), seasonal electricity consumption forecasting (Cao and Wu, 2016), joint replenishment problems (Wang et al., 2015),

steelmaking casting problem (Li et al., 2018), and optimization of support vector regression (Samadianfard et al., 2019; Zhang and Hong, 2019; Sattari et al., 2021). With the extensive applications of FOA, more and more scholars studied the optimization of this algorithm. Hu et al. (2017) changed the step length of the fruit fly from a constant to a decrement sequence to improve the optimization abilities of FOA, and the empirical results showed that the performance of the proposed algorithm was improved. Pan et al. (2014) introduced a new control parameter that adaptively adjusted the range of search space around the location of the cluster, and the accuracy and convergence speed were improved.

In this paper, we propose a multivariate adaptive step fruit fly optimization algorithm (MAFOA) to optimize the smoothing parameter of GRNN for short-term load forecasting. We make three contributions as follows. Firstly, we consider factors that affect the power load as much as possible, such as temperature, weather type, and date type. Secondly, we propose an efficient interval partition technique to handle the structured and unstructured data. Finally, we improve the selection of step size, which has a multivariate adaptive step and can achieve high adaptability.

The remainder of this paper is organized as follows. FOA and its improvement are presented in *The Improvement of Fruit Fly Optimization Algorithm*. *Improvement of Generalized Regression Neural Network* shows the MAFOA-optimized GRNN for short-term load forecasting. We carry out the empirical analysis and compare the proposed model with other models in *Empirical Analysis*. Finally, the summary of this study is drawn in *Conclusion*.

THE IMPROVEMENT OF FRUIT FLY OPTIMIZATION ALGORITHM

Considering the problems of local optimum in the ordinary FOA, we propose the MAFOA to optimize the smoothing parameter of GRNN. In this section, we first briefly introduce the ordinary FOA in *Fruit Fly Optimization Algorithm*, and then we propose the MAFOA in *Multivariate Adaptive Step Fruit Fly Algorithm*.

Fruit Fly Optimization Algorithm

Fruit fly is a kind of flying insect, which is very sensitive to the external environment because of its superior olfactory and vision. Firstly, the olfactory organ is used to obtain the odor floating in the air. Then, it will distinguish the general direction of the food source and fly to the source of food. Finally, the fruit fly can discover the position of food by its keen vision, and then fly to the position. The process of searching food for the fruit flies can be simulated as follows (Mitić et al., 2015):

- 1) Randomly initialize the population size, maximal number of iterations, and position coordinates (x, y) of the group in a set interval.
- 2) Choose the search radius of the fruit fly. Then, determine the new position coordinates (x_i, y_i) of individual fruit fly by using

$$\begin{cases} x_i = x + L_0 \times \text{rands}(-1, 1), \\ y_i = y + L_0 \times \text{rands}(-1, 1), \end{cases} \quad (1)$$

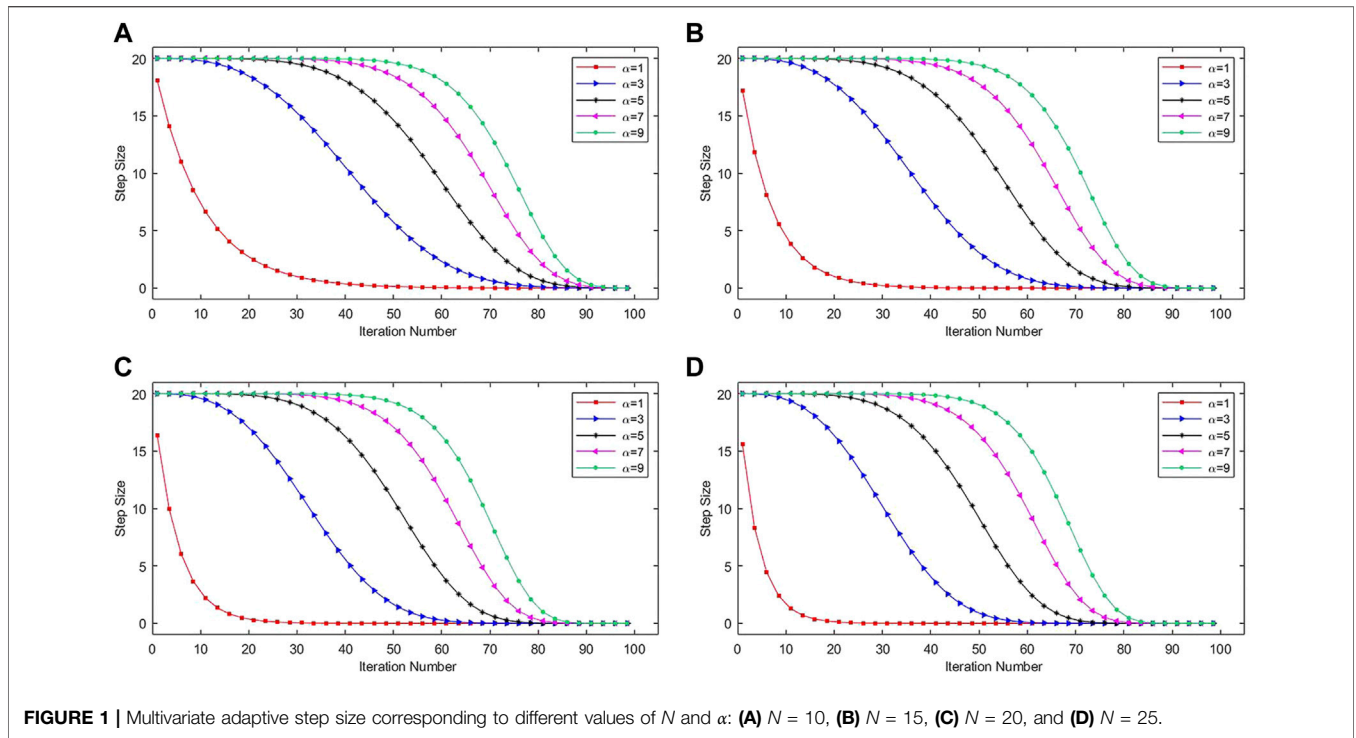


FIGURE 1 | Multivariate adaptive step size corresponding to different values of N and α : **(A)** $N = 10$, **(B)** $N = 15$, **(C)** $N = 20$, and **(D)** $N = 25$.

where L_0 is a fixed step size and $rands(-1, 1)$ is a sample of uniform distribution on $(-1, 1)$.

- 3) Estimate the distance (d_i) between the individual fruit fly and the coordinate origin and then calculate the judgment value (S_i) of smell concentration:

$$d_i = \sqrt{x_i^2 + y_i^2}, \tag{2}$$

$$S_i = 1/d_i. \tag{3}$$

- 4) Calculate the smell concentration ($smell_i$) by substituting S_i into the fitness function (f) of the taste concentration:

$$smell_i = f(S_i). \tag{4}$$

- 5) Find out the best smell concentration ($smell_i$) among the fruit fly swarm:

$$[bestsmell \quad bestindex] = best(smell_i), \tag{5}$$

where $bestsmell$ is the extreme value of $smell_i$ and $bestindex$ is the position coordinate of the individual fruit fly with best smell concentration.

- 6) Determine whether the smell concentration is better than the previous one. If yes, implement step 7; otherwise, repeat the process from step 2 to step 6.
- 7) Retain the best smell concentration value ($Smellbest$) and the position coordinate of the individual fruit fly with the best smell concentration (x_{best}, y_{best}):

$$Smellbest = bestsmell, \tag{6}$$

$$\begin{cases} x_{best} = x(Smellbest), \\ y_{best} = y(Smellbest). \end{cases} \tag{7}$$

- 8) Determine whether the end condition is reached. If yes, find out the location of the best smell concentration value; otherwise, return to step 2.

Multivariate Adaptive Step Fruit Fly Algorithm

In the ordinary FOA, the individual fruit fly seeks the food source with the pre-set step size. Obviously, if the step size is too small, the search space will be limited, and it will cause the problem of local optimum. On the contrary, if the step size is too large, its local search ability will become weaker, and the convergence rate will slow down. To deal with these issues, the setting of step size should adhere to the following principles. In the initial phase of iterations, the step size should be large to ensure global optimization performance. On the contrary, in the later stage, the step size should be small to ensure local search performance.

Therefore, there are a few successful algorithms for the improvement of step size of fruit flies, such as the decreasing step fruit fly optimization algorithm (DSFOA) (Hu et al., 2017), self-adaptive step fruit fly optimization algorithm (FFOA) (Yu et al., 2016), and improved fruit fly optimization algorithm (IFFO) (Pan et al., 2014). In the DSFOA and IFFO, the step size decreased quickly in the initial phase of iteration, which cannot guarantee the global optimization performance of the algorithm. In this paper, we propose the multivariate adaptive step size, which can be demonstrated as follows:

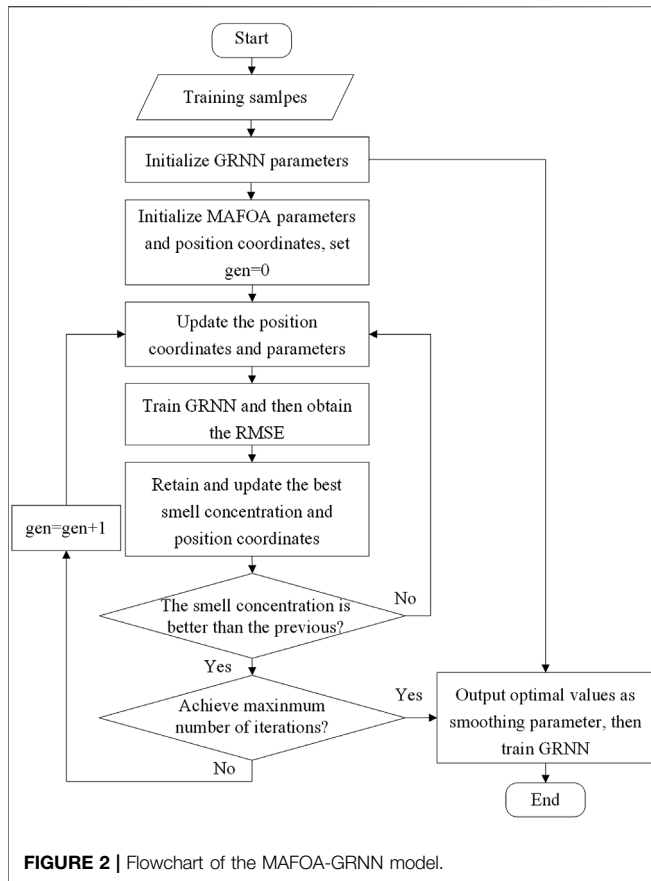


FIGURE 2 | Flowchart of the MAFOA-GRNN model.

$$L_i = L_0 \cdot \exp \left[-N \left(\frac{G_i}{G_{\max}} \right)^\alpha \right], \quad (8)$$

where L_0 is the initial step size, G_i is the current number of iterations, G_{\max} is the maximum number of iterations, N is a positive integer, and the exponential factor α is a constant within $(0, 10)$. The positive integer N and the exponential factor α control the decreasing rate of step size and realize the better local search performance. In order to choose proper values of N and α , the convergence ability of algorithm under different parameter values is compared. The initial step size L_0 is set to 20, and the maximum number of iterations G_{\max} is set to 100. **Figure 1** gives the variations of step size in **Eq. 8** corresponding to different values of α when $N = 10$, $N = 15$, $N = 20$, and $N = 25$, respectively.

As shown in **Figure 1**, the step size decreases gradually from 20 to 0 with the increasing iteration number and different values of α correspond to different step size change trends. In the initial stage of iterations, the algorithm has the largest step size, which can guarantee the global optimum. As the iteration number increases, the capability of local search is gradually enhanced to find the local optimum value, which can be seen from the rapid decline in the curves. Therefore, the dynamic step size can realize the balance of global search capability and local optimization ability.

Besides, from the subfigures in **Figure 1**, the step size changes relatively symmetrical when $\alpha = 3$, $\alpha = 5$, and $\alpha = 7$. When $\alpha = 1$, the curve drops sharply from the beginning, which means the step size will become small even before achieving the global optimum, and the step size cannot achieve 20 at the beginning of iteration. The moment when step size begins to decline is a bit later when $\alpha = 9$. There seems to be no difference in convergence performance when N takes different values. So in *Empirical Analysis*, we will test the performance of the proposed model with different values of N and α to search for the optimal value, and we will substitute the optimal N and α into the model for short-term load forecasting.

IMPROVEMENT OF GENERALIZED REGRESSION NEURAL NETWORK

Generalized Regression Neural Network

The GRNN is a kind of neural network using the radial basis function and has been very popular in applications in recent years. It can establish the implicit mapping relationship according to the sample data, so that the output can converge the optimal regression surface. Once the sample is determined, the only goal is the determination of smoothing parameter in the kernel function (Ozturk and Turan, 2012; Kumar and Malik, 2016).

Assuming that $f(x, y)$ is the joint probability density function of random variable X and variable Y , the observed value of X is x_0 , and the regression of Y with respect to X is

$$\hat{Y}(x_0) = \frac{\int_{-\infty}^{\infty} y f(x_0, y) dy}{\int_{-\infty}^{\infty} f(x_0, y) dy}. \quad (9)$$

Based on the Parzen non-parametric estimation, the density function $f(x_0, y)$ can be estimated by the sampled dataset $\{x_i, y_i\}_{i=1}^n$:

$$f(x_0, y) = \frac{1}{n(2\pi)^{\frac{p+1}{2}} \sigma_1 \sigma_2 \dots \sigma_p \sigma_y} \sum_{i=1}^n e^{-d(x_0, x_i)} e^{-d(y, y_i)}, \quad (10)$$

$$d(x_0, x_i) = \sum_{j=1}^n \left[\frac{(x_{0j} - x_{ij})}{\sigma_j} \right]^2, \quad (11)$$

$$d(y, y_i) = (y - y_i)^2, \quad (12)$$

where n is the sample size, p is the dimension of random variable X , and σ is the width coefficient of the Gaussian function, which is called the smoothing parameter.

Substituting **Eq. 10** into **Eq. 9** yields

$$\hat{Y}(x_0) = \frac{\sum_{i=1}^n \left(e^{-d(x_0, x_i)} \int_{-\infty}^{\infty} y e^{-d(y, y_0)} dy \right)}{\sum_{i=1}^n \left(e^{-d(x_0, x_i)} \int_{-\infty}^{\infty} e^{-d(y, y_0)} dy \right)}. \quad (13)$$

Note that $\int_{-\infty}^{\infty} z e^{-z^2} dz = 0$, (**Eq. 13**) can be simplified as follows:

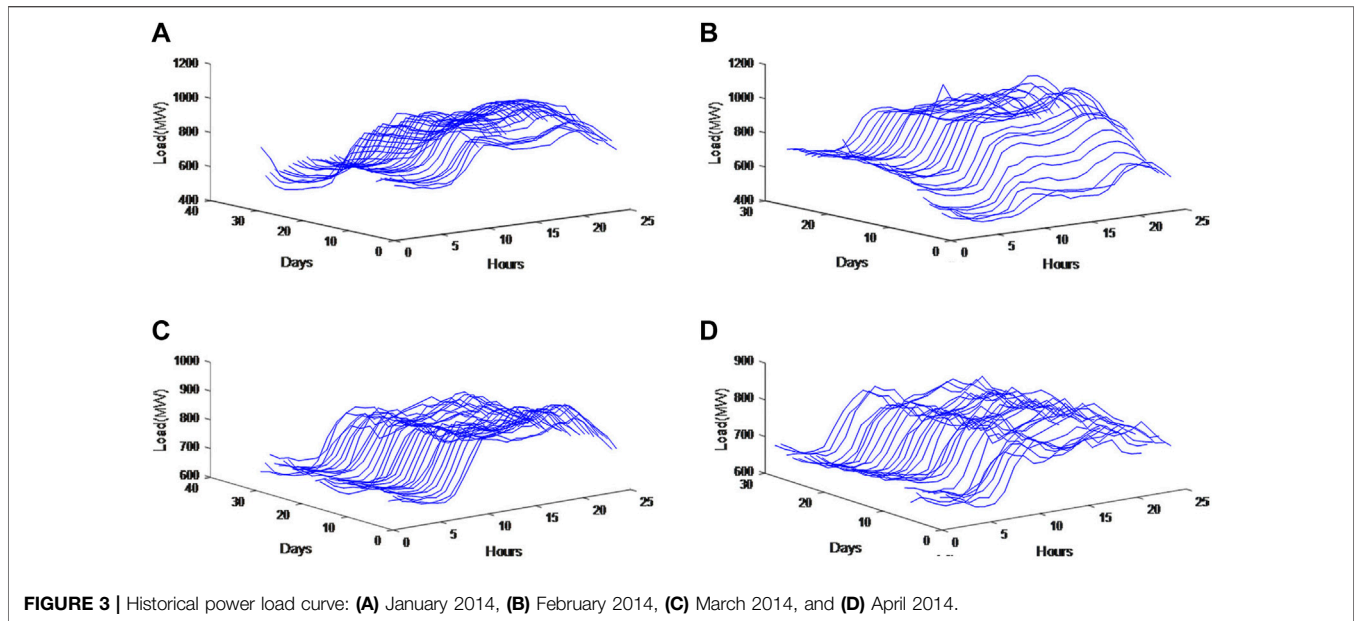


FIGURE 3 | Historical power load curve: **(A)** January 2014, **(B)** February 2014, **(C)** March 2014, and **(D)** April 2014.

$$\hat{Y}(x_0) = \frac{\sum_{i=1}^n y_i e^{-d(x_0, x_i)}}{\sum_{i=1}^n e^{-d(x_0, x_i)}} \quad (14)$$

The predicted value in Eq. 14 is the weighted sum of the observations of the dependent variable, and the weights are $e^{-d(x_0, x_i)}$. The GRNN is composed of input layers, pattern layers, summation layers, and output layers. Once the learning samples are determined, the structure of neural network and the connection weights between neurons are completely determined. Therefore, the GRNN does not need to adjust the connection weight values between neurons, but to adjust the transfer function of each unit by changing the smoothing parameter to obtain the best regression result, which is different from the traditional error backward propagation algorithm. Thus, a key step in the GRNN is to determine the value of the smoothing parameter.

Optimization of Generalized Regression Neural Network Based on Multivariate Adaptive Step Fruit Fly Optimization Algorithm

In this paper, the MAFOA is applied to optimize the smoothing parameters in the GRNN. The MAFOA-GRNN takes the root mean square error (RMSE) of GRNN as the fitness function of MAFOA, so as to calculate the smell concentration in each iteration. Part of the training data are used in the MAFOA to select the best parameters for the GRNN. When the algorithm reaches the maximum number of iterations, the location of the fruit fly with best smell concentration is obtained. Then, these optimal parameters will be used in the GRNN to get the optimal prediction model. The flowchart of the MAFOA-GRNN model is shown in Figure 2.

EMPIRICAL ANALYSIS

In this section, the power load data in Wuhan are used to test the performance of MAFOA-GRNN. The data description is introduced in *Data Description*. Then, *Data Processing* is discussed. The evaluation criteria and empirical results are further discussed in *Evaluation Criteria* and *Experimental Analysis*.

Data Description

The power load data used in this paper are hourly and obtained from a power grid in Wuhan with 2,880 observations ranging from January 1, 2014, to April 30, 2014, which are shown in Figure 3. In this section, we predict the power load of the last day of each month. The in-sample data are power load data of each month except the last day, and the out-of-sample data are the power load data of the last day of each month.

As shown in Figure 3, the short-term power load has obvious periodicity. Therefore, historical load data are an important reference for forecasting. In order to accurately predict the power load, the factors influencing the power load should be considered as much as possible. The factors related to load forecasting include date classification (weekday, weekend, holiday), daily temperature (maximum, minimum, average temperature), and weather condition.

Combining the influence factor, the improved GRNN adopts a three-layer network structure. The input variables of the GRNN are shown in Table 1, and the corresponding output vector is the power load value at t o'clock on day d .

Data Processing

The original load data are normalized to eliminate the impact of the dimensions between indicators. In addition, the input variables of GRNN in Table 1 should be numerical data, so we quantify the above weather factors and date type factors.

TABLE 1 | Input variables of the GRNN.

Number	Input variables
1	Power load value at t o'clock on day $d - 2$
2	Power load value at $t - 1$ o'clock on day $d - 2$
3	Maximum temperature on day $d - 2$
4	Minimum temperature on day $d - 2$
5	Weather condition on day $d - 2$
6	Date type on day $d - 2$
7	Power load value at t o'clock on day $d - 1$
8	Power load value at $t - 1$ o'clock on day $d - 1$
9	Maximum temperature on day $d - 1$
10	Minimum temperature on day $d - 1$
11	Weather condition on day $d - 1$
12	Date type on day $d - 1$
13	Maximum temperature on day d
14	Minimum temperature on day d
15	Weather condition on day d
16	Date type on day d

Meanwhile, we propose an efficient interval partition technique to handle temperature and weather types:

- 1) Normalization of load data. All load data are normalized by using the linear transformation method, given by

$$y = \frac{x - x_{\min}}{x_{\max} - x_{\min}}, \tag{15}$$

where x_{\min} is the minimum load value in the dataset and x_{\max} is the maximum load value in the dataset.

- 2) Quantization of temperature. In the previous studies, temperature is standardized by direct standardization (Hu et al., 2017). When the temperature changes in a suitable range, the effect of the load is small. However, when the temperature increases or decreases to a certain extent, the effect on the load will be larger gradually. Therefore, standardization may not be an appropriate choice. In this work, we propose an efficient interval partition technique. The temperature is partitioned by intervals, and different quantitative values are taken according to the situation. For example, when the temperature is 0°C, the temperature is coded as 1; when the temperature is 5°C, the temperature is coded as 0.8. The specific code value can be adjusted within a small range according to the previous prediction result.

Therefore, the temperature is partitioned by intervals, as shown in **Table 2**.

- 3) Quantization of weather types. The weather types can be divided into six categories, as shown in **Table 2**, which can affect the power load by influencing the use of lighting equipment and other household appliances. Their corresponding quantized values are also shown in **Table 2**.
- 4) Quantization of date types. As a result of the social production modules, the electricity consumption generally shows the alternation of work and rest. The date types can be divided into three categories: weekday (Monday to Friday), weekend (Saturday to Sunday), and holiday (holiday or major event day). On holiday, people often go out to relax or take a rest, which has a substantial impact on the changes in power load. According to the degree of influence on power load, the date type is coded as three categories: weekday is coded as 0, weekend is coded as 0.5, and holiday is coded as 1.

Evaluation Criteria

This paper uses the normalized root mean square error (NRMSE), mean absolute error (MAE), and mean absolute percentage error (MAPE) as the evaluation criteria, given by

$$NRMSE = \frac{100}{\bar{y}} \sqrt{\frac{1}{N} \sum_{i=1}^N (y_i - \hat{y}_i)^2}, \tag{16}$$

$$MAE = \frac{1}{N} \sum_{i=1}^N |y_i - \hat{y}_i|, \tag{17}$$

$$MAPE = \frac{1}{N} \sum_{i=1}^N \left| \frac{y_i - \hat{y}_i}{y_i} \right|, \tag{18}$$

where \bar{y} is the mean of value, \hat{y}_i is the predicted value, y_i is the observation value, and N is the number of data.

Although the NRMSE, MAE, and MAPE can be used as criteria to obtain model predicted loss values, it cannot be verified whether the comparison result is statistically significant. To solve this problem, Diebold and Mariano (1994) proposed the Diebold–Mariano (DM) test to test the statistical significance of different prediction models. Assume that model B and model T do the forecasting task in period t at the

TABLE 2 | Quantitative value of meteorological factors.

Temperature (°C)	Quantitative value	Weather type	Quantitative value
-5-0	(0.7, 1.0)	Sunny	(0, 0.1)
0-5	(0.5, 0.8)	Sunny-cloudy	(0.1, 0.2)
5-10	(0.3, 0.6)	Cloudy	(0.2, 0.4)
10-15	(0.2, 0.4)	Cloudy-rainy	(0.3, 0.6)
15-20	(0.1, 0.2)	Rainy	(0.5, 0.8)
20-25	(0, 0.1)	Snowy	(0.7, 1.0)
25-30	(0.1, 0.4)		
30-35	(0.4, 0.7)		
35-	(0.1, 1.0)		

same time, and we wonder if there are significant differences in the performance between the two models. The original hypothesis is that the forecast accuracy for two models is the same, which is equivalent to the mean value of relative loss function of 0. The DM statistics is defined as follows:

$$DM = \frac{\bar{d}}{\sqrt{\frac{2\pi f_d(0)}{T}}} \tag{19}$$

where

$$\bar{d} = \frac{1}{T} \sum_{t=1}^T d_t \tag{20}$$

is the sample mean loss differential, in which

$$d_t = Loss_T - Loss_B \tag{21}$$

is the relative loss function, where $Loss_T$ and $Loss_B$ are the loss function of predicted errors of test model T and benchmark method B at time t, respectively.

Note that, in this paper, the mean-squared prediction error (MSPE) is used as the loss function:

$$Loss_i = \frac{1}{N} \sum_{i=1}^N (y_t - \hat{y}_{it})^2, \tag{22}$$

where \hat{y}_{it} is the predicted value of model i at time t.

$$f_d(0) = \frac{1}{2\pi} \sum_{\tau=-\infty}^{\infty} \gamma_d(\tau) \tag{23}$$

is the spectral density of relative loss function at frequency zero.

$$\gamma_d(\tau) = E[(d_t - \mu)(d_{t-\tau} - \mu)] \tag{24}$$

TABLE 3 | Errors of the test set for different α and N .

n	Error type	$\alpha = 1$	$\alpha = 3$	$\alpha = 5$	$\alpha = 7$	$\alpha = 9$
$N = 10$	NRMSE	33.3898	22.8639	15.8455	7.3671	7.4929
	MAE	7.2234	7.0068	6.5260	5.2611	6.1537
	MAPE	0.0093	0.0083	0.0080	0.0072	0.0081
$N = 15$	NRMSE	34.4198	23.7839	27.4610	1.0415	5.5455
	MAE	7.0454	7.0378	6.5378	6.5242	6.6737
	MAPE	0.0086	0.0087	0.0089	0.0087	0.0097
$N = 20$	NRMSE	38.8445	35.8757	10.7160	4.7947	0.0072
	MAE	7.3071	6.5455	5.8260	5.6311	6.2587
	MAPE	0.0098	0.0083	0.0080	0.0076	0.0081
$N = 25$	NRMSE	39.7045	20.3099	11.6360	5.6547	8.2882
	MAE	7.2102	6.5139	6.5072	5.9937	6.8254
	MAPE	0.0098	0.0094	0.0093	0.0084	0.0082

is the autocovariance of d_t at displacement τ , where μ is the population mean loss differential.

If the p -value corresponding to DM is less than the significant level, which normally is 0.01 or 0.05, the original hypothesis is rejected; otherwise, it cannot be rejected.

Experimental Analysis

To determine the values of parameters α and N , we apply $\alpha = 1, 3, 5, 7, 9$ and $N = 10, 15, 20, 25$ into the model to test the performance of the model. In this section, the data from January 1, 2014, to January 30, 2014, in Wuhan are used as training data, and the load data on January 31, 2014, are regarded as test data. Finally, the anti-normalization processing is carried out, and the NRMSE, MAE, and MAPE are calculated.

Table 3 shows the prediction errors for different α and N . We can see that whatever value N takes, three types of errors are obviously higher than others when $\alpha = 1$. When $\alpha = 3$ and

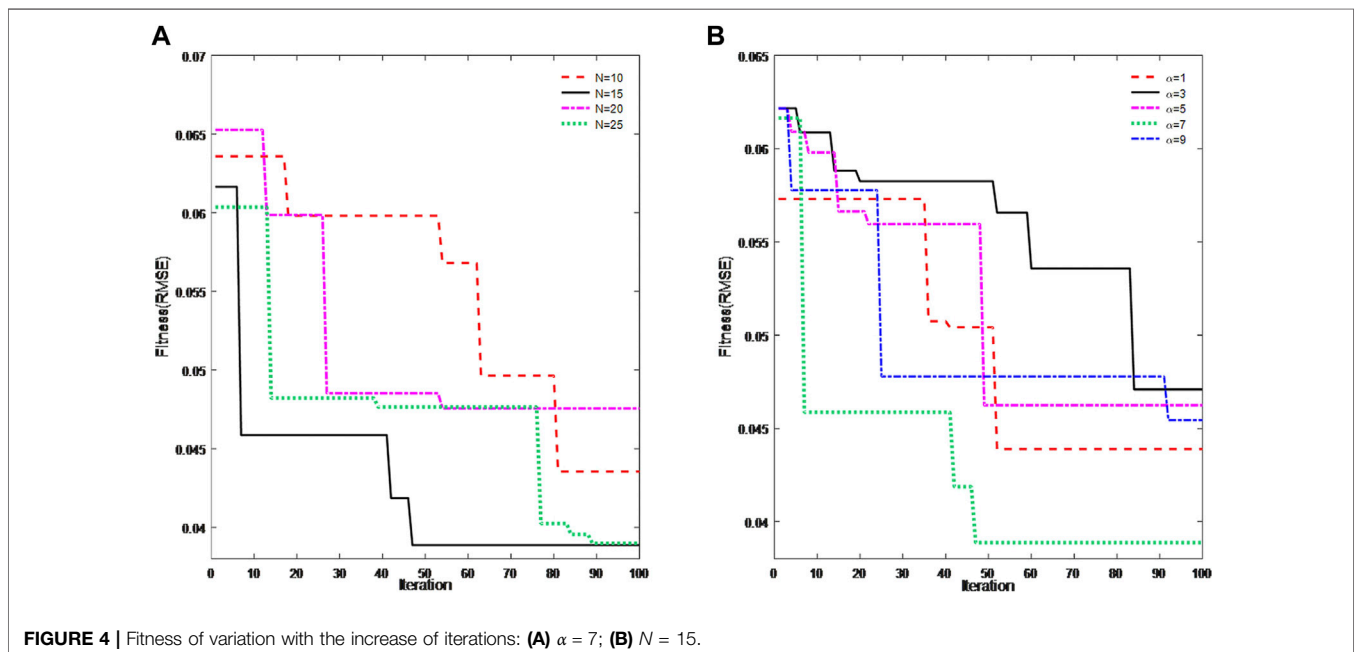
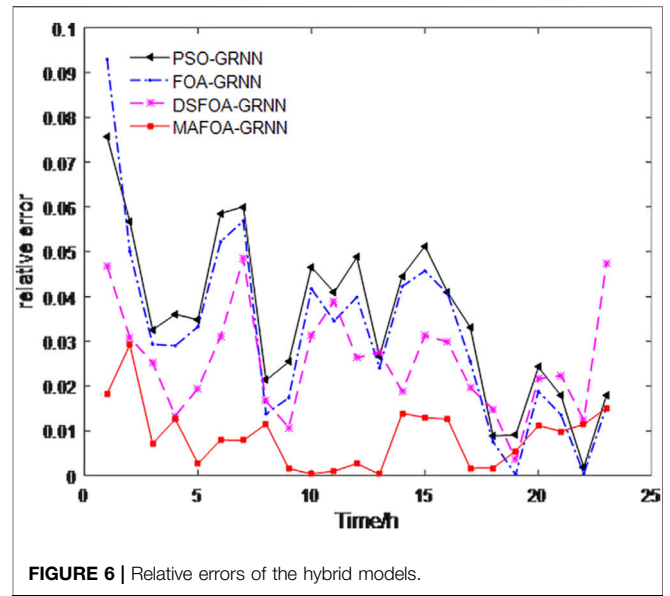
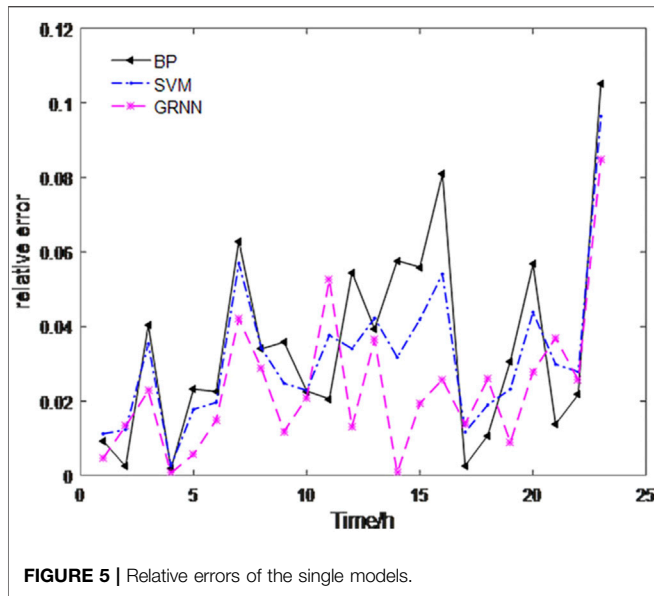


FIGURE 4 | Fitness of variation with the increase of iterations: (A) $\alpha = 7$; (B) $N = 15$.

TABLE 4 | Forecast results of power load.

Time	January			February			March			April		
	Actual values	Forecast values	Relative errors	Actual values	Forecast values	Relative errors	Actual values	Forecast values	Relative errors	Actual values	Forecast values	Relative errors
	(MW)	(MW)	(%)	(MW)	(MW)	(%)	(MW)	(MW)	(%)	(MW)	(MW)	(%)
1:00	677.40	689.79	0.0183	709.82	720.35	0.0148	692.63	690.92	0.0025	658.30	657.68	0.0009
2:00	653.06	672.15	0.0292	694.35	685.74	0.0124	680.72	675.48	0.0077	647.19	645.88	0.0020
3:00	653.51	658.18	0.0071	670.91	672.69	0.0027	673.70	673.74	0.0001	637.70	637.16	0.0009
4:00	642.52	650.65	0.0127	677.20	661.16	0.0237	670.04	670.97	0.0014	630.18	644.47	0.0227
5:00	639.44	641.16	0.0027	662.21	660.71	0.0023	671.82	671.71	0.0002	637.72	643.55	0.0091
6:00	653.05	658.27	0.0080	684.66	687.16	0.0036	698.88	686.72	0.0174	676.44	667.54	0.0132
7:00	690.42	695.86	0.0079	731.70	729.71	0.0027	745.87	747.82	0.0026	722.95	717.03	0.0082
8:00	803.07	812.36	0.0116	814.08	814.16	0.0001	795.26	812.49	0.0217	751.95	762.93	0.0146
9:00	874.77	873.36	0.0016	889.29	889.97	0.0008	833.28	835.70	0.0029	788.23	791.43	0.0041
10:00	853.36	853.67	0.0004	885.28	888.98	0.0042	814.67	809.35	0.0065	777.08	776.24	0.0011
11:00	851.10	850.23	0.0010	884.13	880.51	0.0041	803.69	804.61	0.0011	767.25	769.31	0.0027
12:00	813.58	811.36	0.0027	848.45	846.00	0.0029	783.17	769.67	0.0172	745.26	740.57	0.0063
13:00	809.11	808.87	0.0003	831.73	828.58	0.0038	786.08	771.60	0.0184	730.55	722.46	0.0111
14:00	788.90	799.90	0.0139	818.47	822.24	0.0046	777.79	779.13	0.0017	742.14	731.85	0.0139
15:00	790.56	800.82	0.0130	826.27	826.70	0.0005	780.92	779.61	0.0017	739.81	742.17	0.0032
16:00	797.75	807.82	0.0126	824.00	830.17	0.0075	788.51	784.73	0.0048	753.58	737.04	0.0219
17:00	826.79	825.41	0.0017	856.85	847.88	0.0105	797.58	803.80	0.0078	771.64	770.39	0.0016
18:00	859.40	857.91	0.0017	859.35	865.93	0.0077	787.30	787.15	0.0002	748.37	753.00	0.0062
19:00	899.44	894.48	0.0055	896.94	899.66	0.0030	814.22	807.29	0.0085	756.61	767.41	0.0143
20:00	894.75	904.78	0.0112	909.69	911.58	0.0021	804.24	809.36	0.0064	760.59	770.73	0.0133
21:00	871.66	880.29	0.0099	887.56	883.48	0.0046	779.43	786.43	0.0090	728.23	741.39	0.0181
22:00	828.78	838.28	0.0115	824.59	828.39	0.0046	760.20	767.66	0.0098	707.18	717.41	0.0145
23:00	776.42	788.16	0.0151	760.49	764.49	0.0053	739.43	751.64	0.0165	696.21	707.82	0.0167



$N = 25$, the NRMSE and MAE are small. The NRMSE, MAE, and MAPE are small at the same time when $\alpha = 5$ and $N = 20$, which is consistent with that reported in the FFOA proposed by Yu et al. (2016). When $\alpha = 9$ and $N = 20$, the NRMSE and MAPE are both small. But the smallest values of NRMSE, MAE, and MAPE are obtained when $\alpha = 7$ and $N = 15$, which means the forecasting performance is the best at this moment. So, we can initially claim that when $\alpha = 7$ and $N = 15$, the step size can realize the balance of global search capability and local optimization ability. **Figure 4** shows the fitness curves of MAFOA when $\alpha = 7$ and $N = 15$.

Figure 4 provides the fitness variation with the increase of iteration number. **Figure 4A** shows the convergence situation of different N when $\alpha = 7$, and **Figure 4B** shows the convergence performance of different α when $N = 15$. It can be seen that, under the condition of $\alpha = 7$, when we choose $N = 15$, the algorithm has the minimal fitness value and arrives at its optimal value much more quickly than other conditions; under the condition of $N = 15$, when we choose $\alpha = 7$, the algorithm has the same performance. Accordingly, $\alpha = 7$ and $N = 15$ are perceived as an ideal choice in the step size formula.

After choosing $\alpha = 7$ and $N = 15$, we train the power load data of each month except the last day to predict the load of the last day of each month. **Table 4** shows the prediction results obtained by the MAFOA-GRNN algorithm from January to April 2014, respectively. The relative errors are basically within 2%, and the accuracy is high.

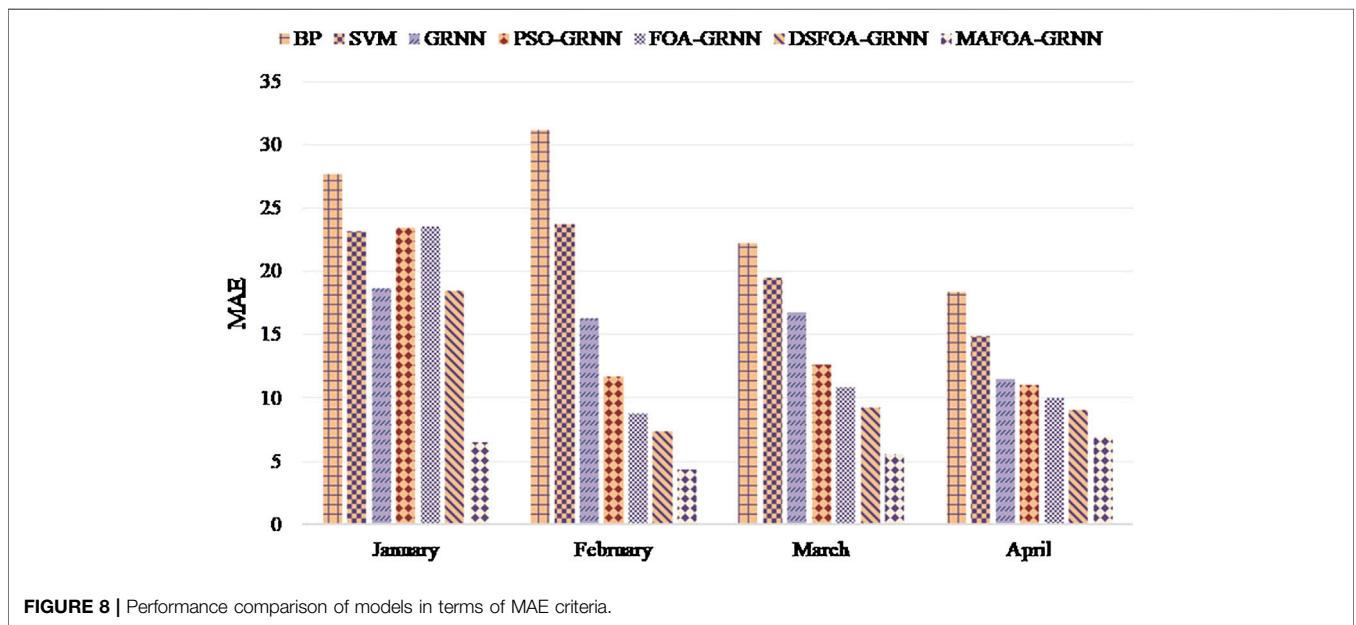
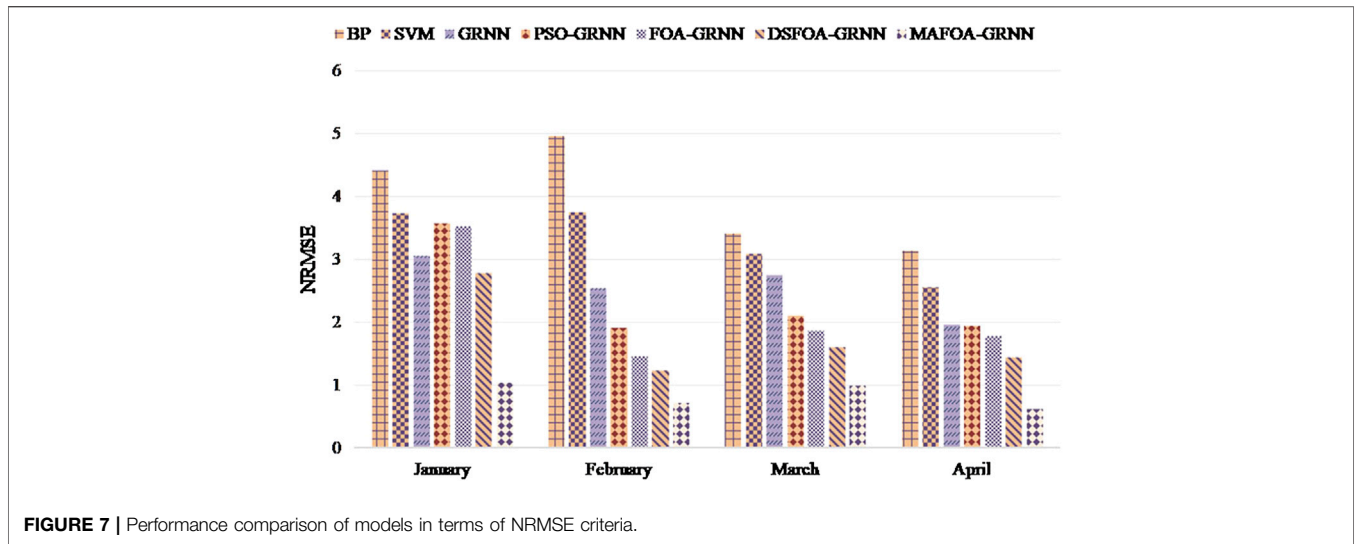
In order to test the forecasting performance of the proposed model, the backpropagation (BP) neural network, support vector machine (SVM), GRNN, PSO-GRNN, FOA-GRNN, and DSFOA-GRNN are regarded as benchmark models to be compared with MAFOA-GRNN in short-term power load forecasting. The PSO was proposed by Kennedy and Eberhart in 1995, which was inspired by the swarm behavior of birds. The FOA proposed by Pan in 2012 was

also used in this work. Since PSO and FOA are both classical optimization algorithms that have been widely utilized in research, we have chosen PSO-GRNN and FOA-GRNN as benchmark models. The DSFOA proposed by Hu et al. in 2017 is an improvement algorithm of FOA. With the decreasing step size in mind, the DSFOA performed well in optimizing the spread parameter of GRNN. The flight distance is updated referring to the sigmoid function. So, DSFOA-GRNN has also been compared with our proposed model. Besides, some other basic prediction models are also taken into account, such as the BP neural network and SVM. **Figure 5** shows the relative error curves of the single models on January 31. **Figure 6** shows the relative error curves of the hybrid models on January 31.

It can be seen from **Figure 5** that, in the commonly applied forecasting methods, the GRNN has the best prediction ability. **Figure 6** shows that the proposed method can accurately predict the overall trend of power load, and the fitting effect is very good. From the relative error curves, it can be seen that MAFOA-GRNN can offer a better predicting performance and higher precision than DSFOA-GRNN, FOA-GRNN, and GRNN. In addition, the relative errors of MAFOA-GRNN are more stable, and the majority are below 0.02, which demonstrates that the improved FOA is perceived as an ideal method in optimizing model parameters during GRNN training.

Then, the anti-normalization processing is carried out, and the comparison results of NRMSE, MAE, and MAPE evaluation criteria are shown in **Figures 7–9**. **Table 5** shows the error analysis of the training set and test set.

Obviously, MAFOA-GRNN has the smallest NRMSE, MAE, and MAPE, followed by FOA-GRNN, but the BP neural network has the worst performance. Besides, the prediction error of the training set and test set has no obvious difference, which indicates that MAFOA-GRNN



has high generalization performance. According to the comparison results, it can be concluded that MAFOA-GRNN outperforms other models in both accuracy and stability. Table 5 demonstrates the same conclusions as above.

Although the NRMSE, MAE, and MAPE can be used as criteria to obtain model-predicted loss values, it cannot be verified whether the comparison result is statistically significant. To statistically compare the differences between the prediction accuracy of different models, the DM statistics test is carried out in this paper, and the results are shown in Table 6. For all the benchmark

models, the values of the MAFOA-GRNN model proposed in this paper are below 0.05, which indicates that the predictive ability of the MAFOA-GRNN model is better than that of DSFOA-GRNN, DSFOA-GRNN, GRNN, SVM, and BP neural network under the confidence interval of 95%.

According to the above comparisons, the following three main conclusions can be summarized:

- 1) The proposed MAFOA-GRNN outperforms the GRNN, which indicates that the MAFOA can optimize the smoothing parameter of GRNN effectively.

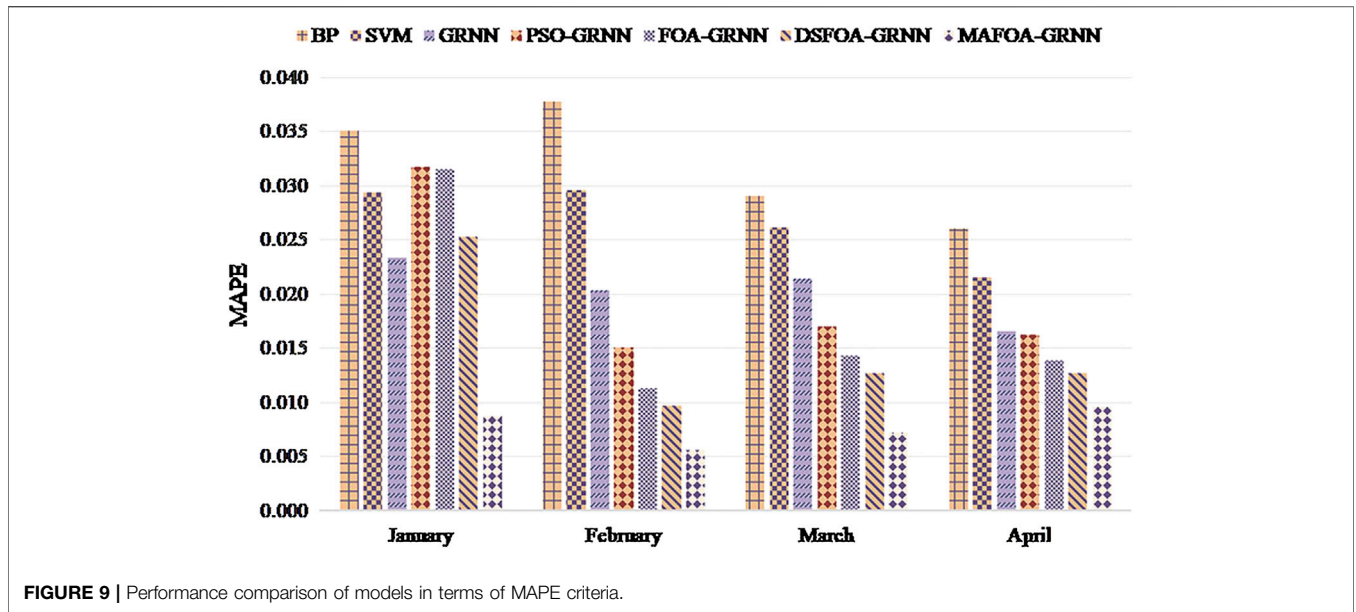


FIGURE 9 | Performance comparison of models in terms of MAPE criteria.

TABLE 5 | Error comparison between MAFOA-GRNN and the benchmark models.

Month	Error type	BP	SVM	GRNN	PSO-GRNN	FOA-GRNN	DSFOA-GRNN	MAFOA-GRNN
January	NRMSE	4.4106	3.7301	3.0477	3.5618	3.5189	2.7762	1.0415
	MAE	27.6808	23.1618	18.6411	23.4856	23.5662	18.4538	6.5242
	MAPE	0.0351	0.0293	0.0234	0.0317	0.0315	0.0253	0.0087
February	NRMSE	4.9501	3.7416	2.5321	1.9097	1.4507	1.2274	0.7050
	MAE	31.1464	23.7110	16.2740	11.7292	8.7336	7.4065	4.3071
	MAPE	0.0378	0.0296	0.0204	0.0151	0.0113	0.0096	0.0056
March	NRMSE	3.4144	3.0825	2.7506	2.1027	1.8578	1.5972	0.9859
	MAE	22.2451	19.4858	16.7246	12.6088	10.8888	9.2868	5.5455
	MAPE	0.0291	0.0262	0.0214	0.0171	0.0143	0.0127	0.0072
April	NRMSE	3.1352	2.5490	1.9609	1.9380	1.7843	1.4344	0.6178
	MAE	18.3732	14.9324	11.4907	10.9833	9.9950	9.0616	6.8816
	MAPE	0.0260	0.0216	0.0166	0.0163	0.0139	0.0128	0.0096

TABLE 6 | DM results of the different models.

Tested model	Benchmark model (January)					
	DSFOA-GRNN	FOA-GRNN	PSO-GRNN	GRNN	SVM	BP
MAFOA-GRNN	2.4083 (0.0036)	4.9502 (0.0120)	-2.5780 (0.0073)	2.8360 (0.0048)	-2.5430 (0.0160)	-3.4426 (0.0012)
DSFOA-GRNN		3.8311 (0.0280)	-3.7578 (0.0260)	4.1183 (0.0000)	-3.5324 (0.0180)	4.3981 (0.1802)
FOA-GRNN			-1.1790 (0.0370)	0.5811 (0.7165)	-3.5824 (0.0000)	-1.5424 (0.0686)
PSO-GRNN				4.4083 (0.0480)	-1.8246 (0.0190)	3.2784 (0.0735)
GRNN					-2.4083 (0.0370)	-2.6555 (0.0072)
SVM						4.1736 (0.0078)

- 2) The performance of MAFOA-GRNN is better than that of FOA-GRNN, which shows that the multivariate adaptive step can effectively improve the optimization ability of FOA.
- 3) From January to April 2014, MAFOA-GRNN has reached high prediction accuracy, which shows that the proposed algorithm is a stable and effective forecasting framework.

CONCLUSION

In this paper, we have proposed MAFOA-GRNN and applied it to short-term load forecasting. Firstly, we discussed a number of external factors including weather types and date types as input variables of the GRNN, in order to optimize the structure of NNs. Then, we propose an efficient interval segmentation technique for temperature types and weather types. Finally, we use the MAFOA to obtain the optimal GRNN model instead of the ordinary FOA, which solves the problem of local optimum in the implementation of FOA. The hybrid model proposed in this paper has a higher accuracy than the BP neural network, SVM, GRNN, PSO-GRNN, FOA-GRNN, and DSFOA-GRNN, and the majority of relative errors are below 0.02.

The proposed models can accurately predict the load of the power system, especially in short-term load forecasting. Electric energy cannot be stored in large quantities, and its generation and consumption are almost completed at the same time. Therefore, in order to arrange the work of power plants economically and reasonably, short-term load forecasting is indispensable. Furthermore, the proposed model can also predict other time series by adjusting the input vector and parameters.

In addition to short-term load forecasting, the proposed MAFOA-GRNN can be applied to solve other complex multivariable problems, including solar radiation forecasting, crude oil price forecasting, and wind load forecasting. Furthermore, the factors considered in this article are limited, and the forecasting performance may be better if other valuable

factors are taken into consideration. Finally, further research may improve the performance of proposed model such as training the data of weekdays and holidays separately.

DATA AVAILABILITY STATEMENT

The raw data supporting the conclusion of this article will be made available by the authors, without undue reservation.

AUTHOR CONTRIBUTIONS

FJ contributed to conception and design of the study. WZ and ZP conducted the data analysis, wrote the original draft, and edited the paper. All authors have read and agreed to the published version of the manuscript.

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