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EDITED BY

Qingguo Huang,
University of Georgia, Griffin Campus,
United States

REVIEWED BY

Ke Li,
University of Georgia, United States
Norhaliza Abdul Wahab,
Universiti Teknologi Malaysia, Malaysia

*CORRESPONDENCE

E. W. Mtonga,
✉ eddiemtonga@gmail.com

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Comparative study for the performance of pure artificial intelligence software sensor and self-organizing map assisted software sensor in predicting 5-day biochemical oxygen demand for Kauma Sewage Treatment Plant effluent in Malawi

M. H. Mng'ombe^{1,2}, E. W. Mtonga^{1*}, B. A. Chunga¹,
R. C. G. Chidya¹ and M. Malota¹

¹Department of Water and Sanitation, Faculty of Environmental Sciences, Mzuzu University, Mzuzu, Malawi, ²Hydro-Informatics Engineering Centre, Lilongwe, Malawi

Introduction: Modeling plays a crucial role in understanding wastewater treatment processes, yet conventional deterministic models face challenges due to complexity and uncertainty. Artificial intelligence offers an alternative, requiring no prior system knowledge. This study tested the reliability of the Adaptive Fuzzy Inference System (ANFIS), an artificial intelligence algorithm that integrates both neural networks and fuzzy logic principles, to predict effluent Biochemical Oxygen Demand. An important indicator of organic pollution in wastewater.

Materials and Methods: The ANFIS models were developed and validated with historical wastewater quality data for the Kauma Sewage Treatment Plant located in Lilongwe City, Malawi. A Self Organizing Map (SOM) was applied to extract features of the raw data to enhance the performance of ANFIS. Cost-effective, quicker, and easier-to-measure variables were selected as possible predictors while using their respective correlations with effluent. Influent's temperature, pH, dissolved oxygen, and effluent chemical oxygen demand were among the model predictors.

Results and Discussions: The comparative results demonstrated that for the same model structure, the ANFIS model achieved correlation coefficients (R) of 0.92, 0.90, and 0.81 during training, testing, and validation respectively, whereas the SOM-assisted ANFIS Model achieved R Values of 0.99, 0.87 and 0.94. Overall, despite the slight decrease in R-value during the testing stage, the SOM-assisted ANFIS model outperformed the traditional ANFIS model in terms of predictive capability. A graphic user interface was developed to improve user interaction and friendliness of the developed model. Integration of the developed model with

supervisory control and data acquisition system is recommended. The study also recommends widening the application of the developed model, by retraining it with data from other wastewater treatment facilities and rivers in Malawi.

KEYWORDS

adaptive neuro-fuzzy inference system, self-organizing map, biochemical oxygen demand, sewage treatment plant, wastewater, artificial intelligence

Introduction

Monitoring of effluent from wastewater treatment plants is crucial in identifying possible pollutants that may be released into receiving water bodies. Surface water quality is often evaluated using indices such as the 5-day biochemical oxygen demand (BOD₅), a commonly used method for measuring organic load in water resource systems (Arlyapov et al., 2022). However, the traditional method for determining BOD₅ using hard sensors has significant setbacks. As Hassen and Asmare, (2018) point out, this approach is difficult, time-consuming, requiring a 5-day incubation period, making it unsuitable for real-time process control (Arlyapov et al., 2022), which can feed into an integrated resource planning framework. Besides, it requires a certified laboratory equipped with expensive instruments and chemicals to administer. Furthermore, the BOD₅ test is complicated by factors such as the oxygen demand caused by algal respiration within the sample and the probable oxidation of ammonia (Noori et al., 2013a). The conditions under which BOD₅ is measured in laboratories frequently differ from those observed in natural aquatic systems, resulting in significant differences in the interpretation of results and their implications (Noori et al., 2013b).

Biosensors have been developed as a result of efforts to address these challenges (Karube et al., 1977; Arlyapov et al., 2022). However, these endeavors have been unsuccessful for many reasons. Biosensors, while promising, face challenges such as the high cost of purchasing and maintenance, the need for significant calibration, toxicity, and inhibitor interference (Rustum, 2009; Pitman et al., 2015; Liu et al., 2020). Practitioners are pressed with the need to balance between treatment operations and testing costs, which includes instrumentation on one hand and allowing for continuous monitoring with the ability to make instant decisions for remedial works for process control to achieve the treatment plant's desired performance objectives (O'Brien et al., 2011). To resolve such complex processes, researchers are developing an interest in machine learning (ML), a branch of artificial intelligence (AI) to model complex problems and apply deep learning from available data (El Alaoui El Fels et al., 2023).

AI algorithms can be broadly categorized into supervised learning or unsupervised learning paradigms (El Alaoui El Fels et al., 2023). Supervised learning involves training algorithms on labeled data, wherein every input-output pair is explicitly supplied during the training process (Pourzangbar et al., 2023). As a result, the algorithm can learn a mapping from inputs to outputs and use that knowledge to make judgments or predictions on new, unobserved data. Conversely, unsupervised learning involves training algorithms on

unlabeled data, where the algorithm's task is to figure out the data's underlying structure or patterns without direct supervision (El Alaoui El Fels et al., 2023; Pourzangbar et al., 2023). This frequently entails using dimensionality reduction techniques or grouping comparable data elements. AI algorithms like Artificial Neural Networks (ANN) (Hassen and Asmare, 2018; Bekkari and Zeddouri, 2019; Alsulaili and Refaie, 2021; Lin et al., 2022), Random Forests (RF) (Ward et al., 2021), and Support Vector Machines (SVM) (Zhu et al., 2022) have widely been used in wastewater treatment research where most of them are based on supervised learning. However, there remains a significant research gap regarding the application of unsupervised algorithms like Self-Organizing Maps (SOM). Moreover, studies on optimization techniques demonstrate the extensive application of genetic algorithms (GA) in model calibration (El Alaoui El Fels et al., 2023).

This research was an attempt to improve the performance of AI model capacity in predicting BOD₅ with certainty through the integration of various AI algorithms. Integration of ANN with fuzzy inference system (FIS) was performed. ANN and FIS Models have limitations, particularly in manual parameter tuning and interpretation. To address this, researchers have explored innovative approaches, including the integration of the FIS with ANN, leading to the development of the adaptive network-based fuzzy inference system (ANFIS) (Abunama et al., 2019). SOM assisted ANFIS outperforms individual ANN or FIS models by combining neural network learning capabilities with the interpretability and human knowledge representation of FIS. Unlike conventional FIS models, which require manual parameters and fuzzy rule tuning, ANFIS automates this procedure with neural network learning techniques (Karami et al., 2022; Mohanty et al., 2022). Furthermore, it tackles neural networks' black box characteristics by giving clear fuzzy rules (Rustum and Adeloye, 2011a). This integration produces a more accurate and interpretable modeling method while avoiding the limitations of individual systems. ANFIS combines the benefits of neural networks and fuzzy logic systems, resulting in higher modeling accuracy and simpler implementation, making it a better alternative for a variety of applications (Cheng et al., 2018).

Recent studies have investigated the use of the Adaptive Neuro-Fuzzy Inference System (ANFIS) in wastewater treatment plant (WWTP) processes, with an emphasis on predicting effluent removal quality and influent characteristics. Qiao et al. (2023) studied ANFIS's efficacy in forecasting major pollutant elimination and found satisfactory findings with the coefficient of determination (R^2) values greater than 0.950. However, disparities between anticipated and actual results demonstrated that the model's performance certainty needed improvement. Similarly,

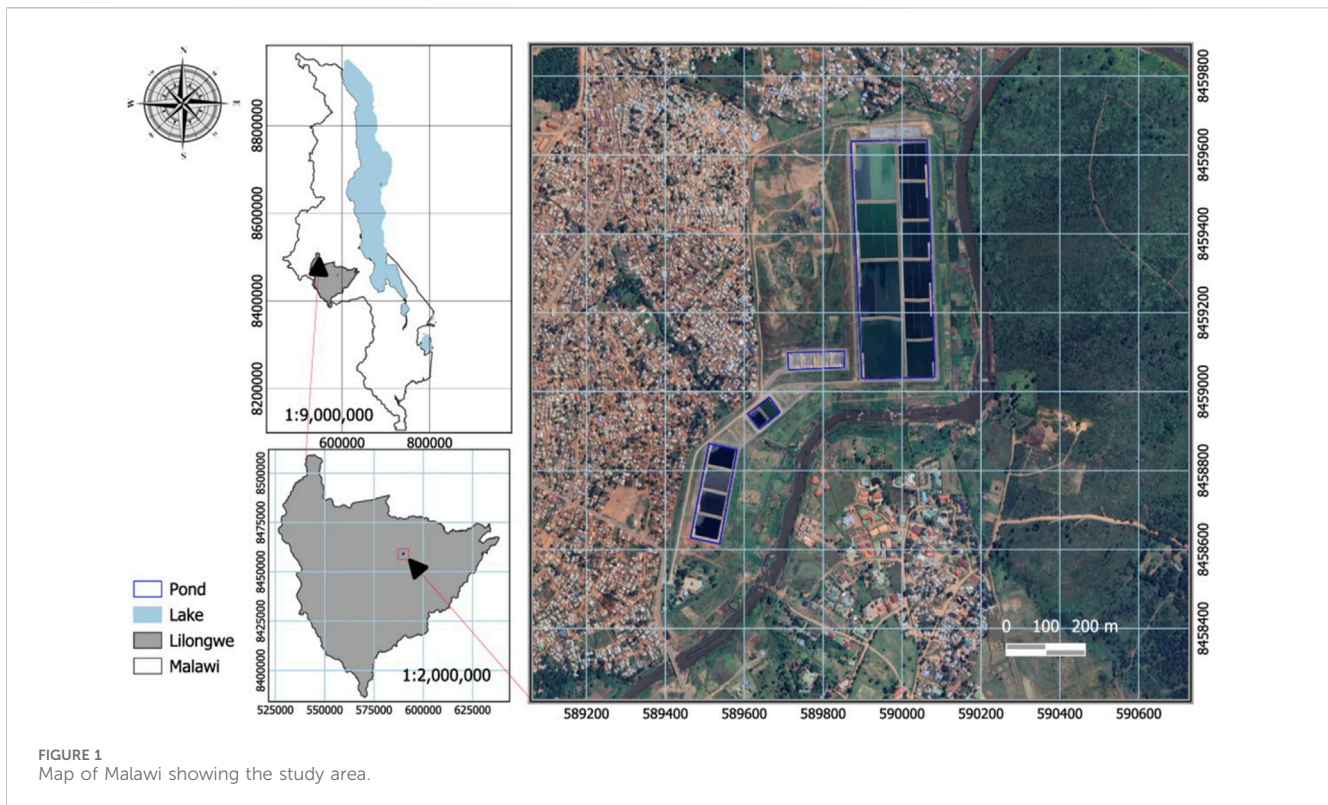


FIGURE 1
Map of Malawi showing the study area.

Cheng et al. (2018) introduced a multi-scale ANFIS methodology that outperformed previous methods for predicting influent characteristics. Okeke et al. (2022) compared ANFIS to Multi-Linear Regression (MLR) for WWTP performance prediction, with MLR demonstrating higher accuracy.

Self-organizing map (SOM) is a nonlinear computational platform introduced by Kasslin et al. (1992) and later by Kohonen et al. (1996). It is an unsupervised learning algorithm with the capacity to establish relationships among process variables. It consists of an array of units arranged in a grid which makes it suitable as a dimensionality reduction technique.

The development of advanced monitoring applications on the SOM platform has been rare and more so in wastewater treatment (Linkkonen et al., 2013). However, integrating ANFIS with SOM or other unsupervised algorithms may address existing accuracy and certainty limitations, demanding further research in this area. This study bridges this gap by investigating the integration of advanced optimization approaches, such as SOM and ANFIS. While these techniques have the potential to improve modeling accuracy, their use is limited, particularly in low-cost wastewater treatment technologies like waste stabilization ponds that are common in developing countries like Malawi (El Alaoui El Fels et al., 2023). Therefore, it was critical to examine this approach in Malawi to establish contextualized monitoring strategies for treatment processes, effectively address local challenges, optimize resource allocation, and promote long-term development in sanitation infrastructure.

The present study employed a modified methodology that uses a SOM algorithm to improve ANFIS precision. SOM-ANFIS models were thoroughly validated with historical wastewater quality data

from the Kauma Sewage Treatment Plant (KSTP) in Lilongwe, Malawi. This study aimed to contribute to the field of wastewater management by improving the synergy between new computational approaches and established modeling frameworks ultimately enhancing predictive accuracy.

Materials and methods

Description of the study area

This research was carried out at the KSTP in Lilongwe, Malawi (Figure 1). The facility receives wastewater from the following sewered areas of the city; 3, 6, 12, 13, 16, 18, 19, 20, 30, 47, and 48. The treatment plant comprises septage lagoons (Figure 2) designed to accommodate fecal sludge transported from various non-sewered areas of the city. Vacuum trucks operated by several private entities also convey and discharge fecal sludge to the treatment facility.

Sampling and data collection procedures

The study utilized both secondary and primary data, with a sole focus on domestic sewage. A comprehensive review of documents related to the KSTP produced secondary data. On the other hand, primary data was collected for 30 days from 11 February 2022, to 17 March 2022, twice per day (morning and evening). Wastewater samples were collected systematically from influent raw wastewater, and composite samples were carefully analyzed using standard

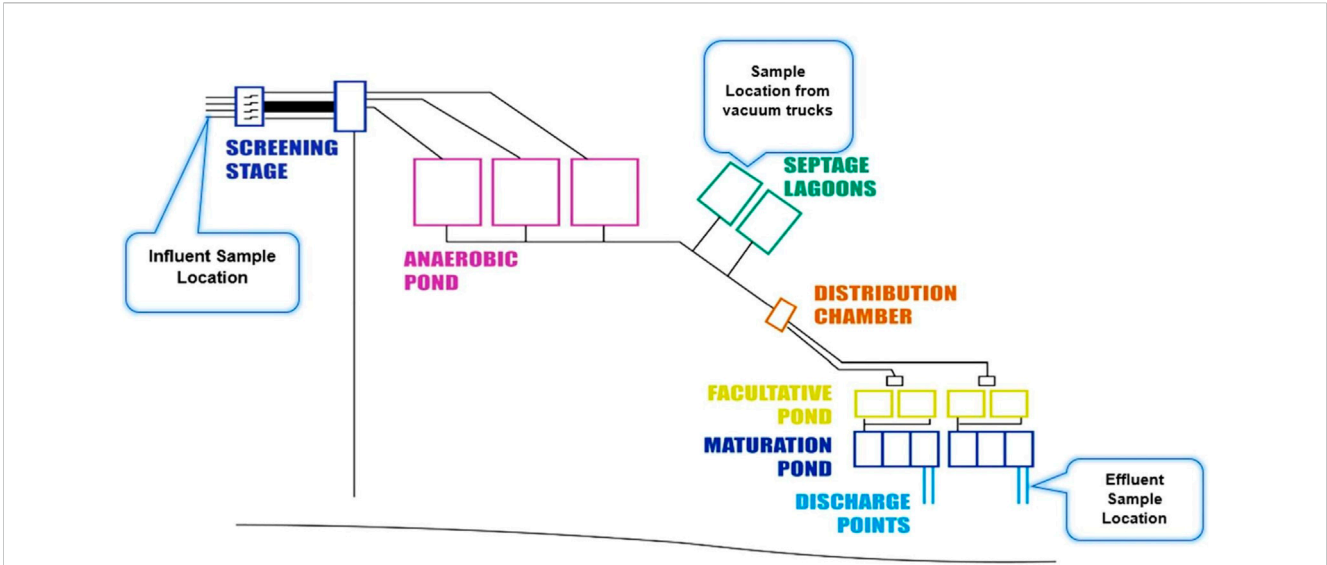


FIGURE 2 A schematic diagram of the Kauma sewage treatment plant. Not drawn to scale (Adapted with permission from Mtethiwa et al., 2008; Ravina et al., 2021).

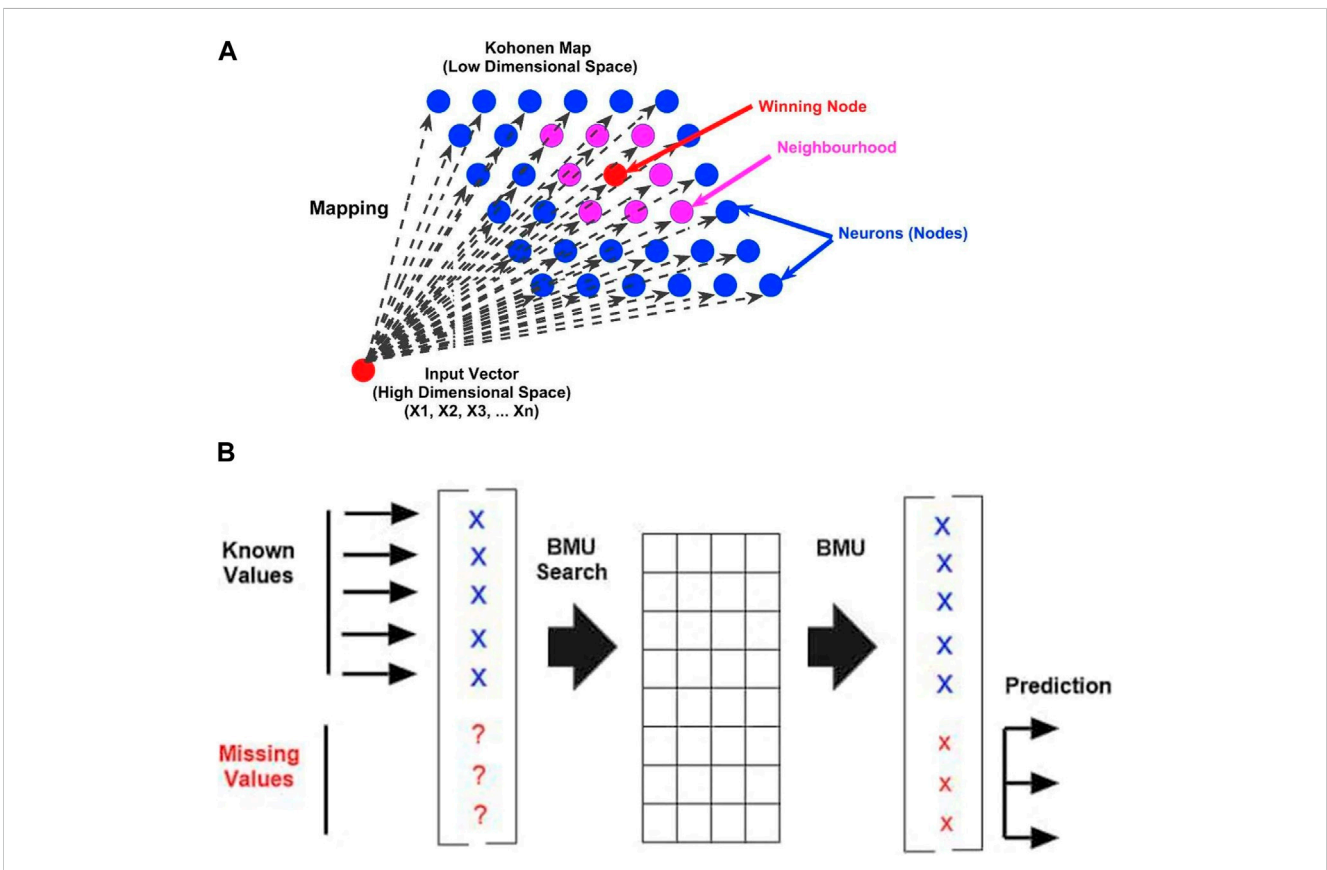
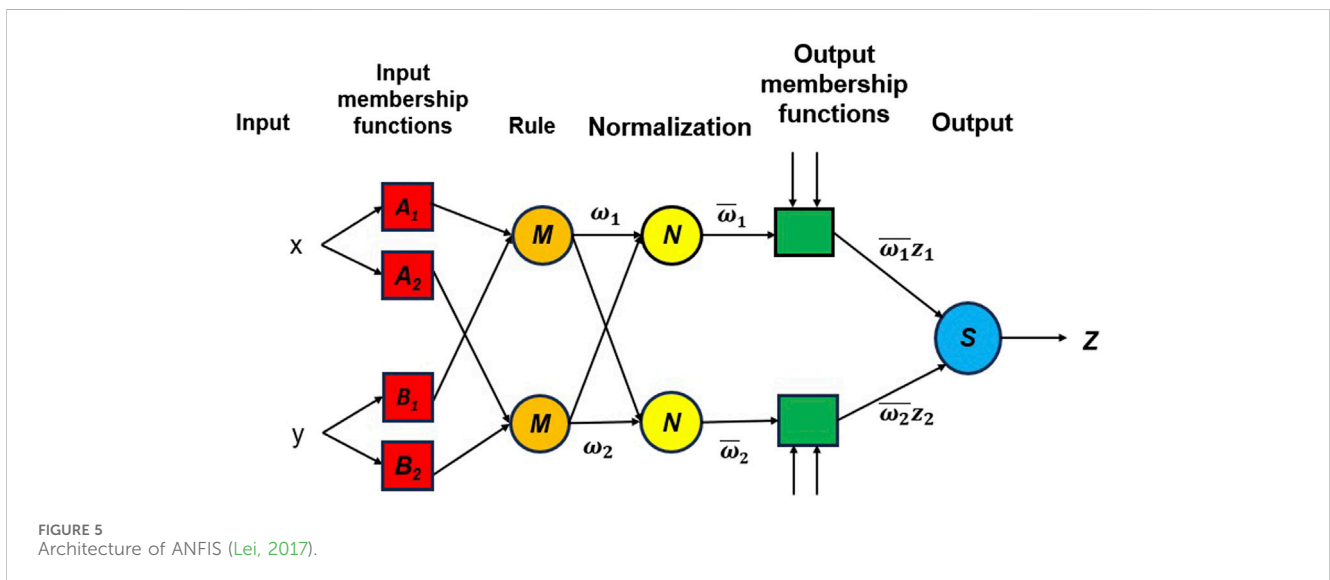
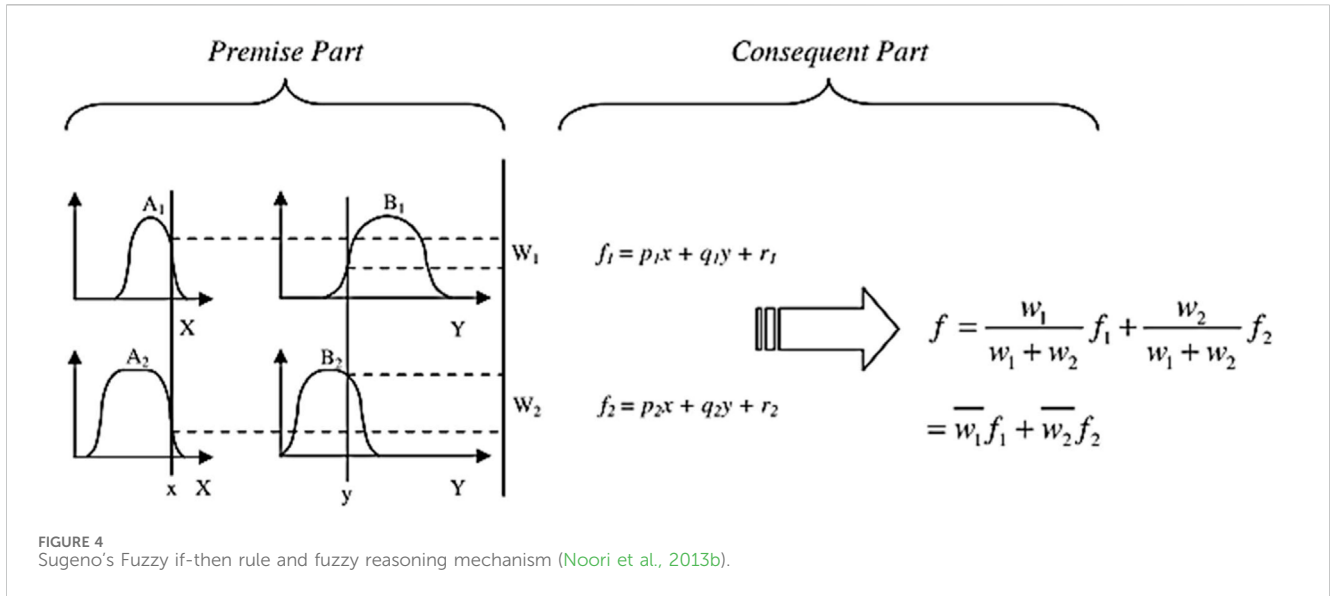


FIGURE 3 (A) Representation of Winning Node and its neighborhood in Kohonen Self Organizing Map (source: Rustum, 2009). (B) Figure 4: Prediction of missing components of the input vector using the Self-Organizing Map (BMU, Best Matching Unit) (Source: Rustum and Adeloje, 2011b).



methods (APHA, 2017; MS682-1:2002, 2002). The pH, COD, total dissolved solids (TDS), total suspended solids (TSS), electrical conductivity (EC), and dissolved oxygen (DO) were all determined. The analyses followed standard methods as prescribed in (APHA, 2017).

Only COD and BOD were determined from samples taken from the Septage lagoon and the effluent-treated wastewater. Samples for the septage lagoon were collected during sludge discharge. To ensure that the samples came from household sources and not from industrial sewage, active attempts were made to consult transporters about the sludge's origin. Each sludge transportation truck produced four 2-L samples: one at the start, two in the middle, and one at the end. These samples were systematically mixed, with double sampling used to ensure quality assurance and homogeneity.

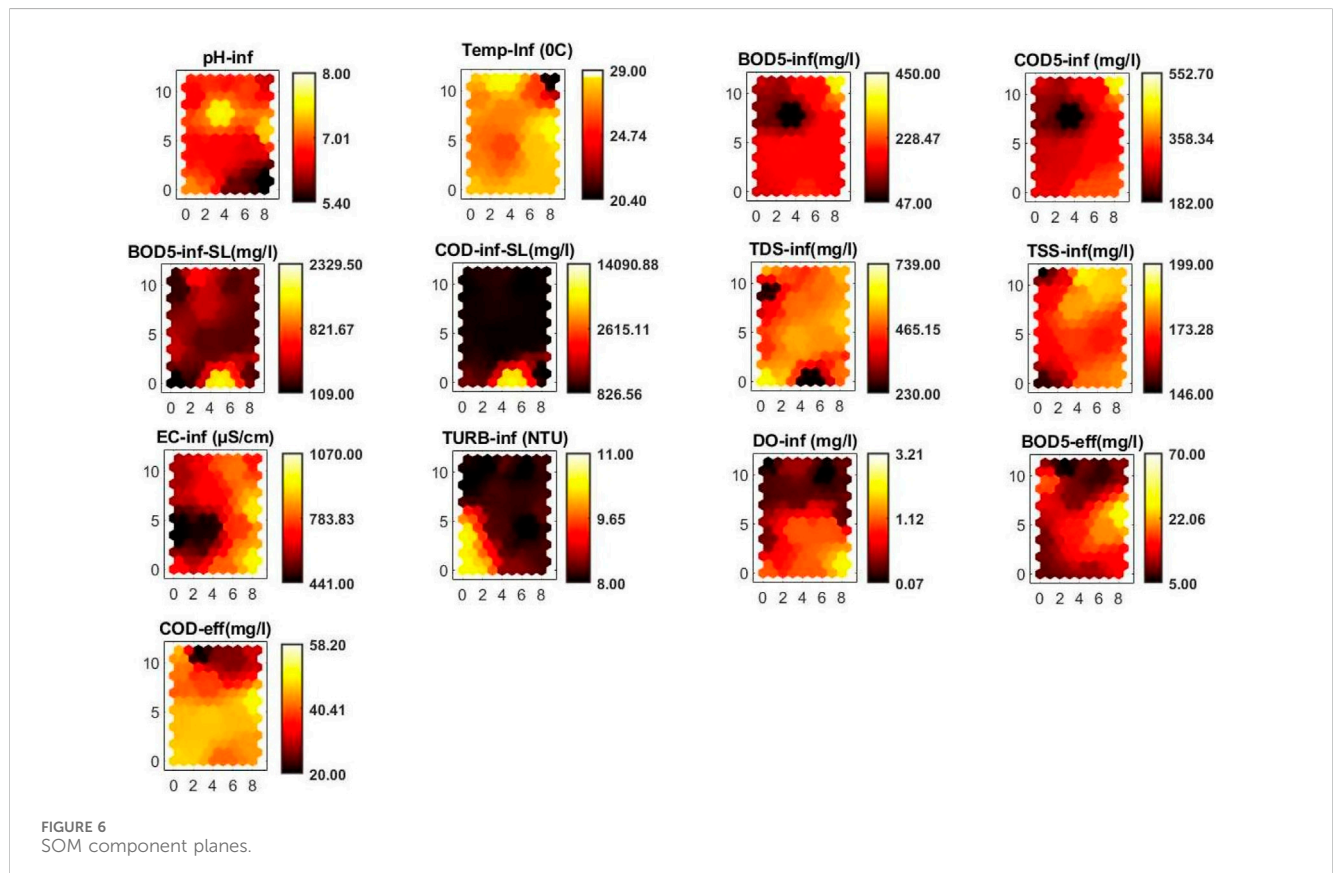
Self-organizing map

The SOM is typically used as a dimensionality reduction approach that can effectively visualize large datasets. This algorithm is based on unsupervised learning and is entirely data-driven. Self-organizing maps are distinguished by their ability to generate internal representations of various aspects of input signals in a spatially organized and effective manner. As a result, the resulting maps closely resemble or mimic topographically structured maps (Kohonen et al., 1996). They operate in a self-study mode, recognizing patterns and grouping them into groups. As this network cannot measure the meaning of the clusters, the users need to interpret the map in a meaningful and useful manner (Rustum, 2009). Self-organizing maps are inspired by neural networks, which are

TABLE 1 Computed descriptive statistics of KSTP data.

Parameter	Unit	Mean	SD	SE	Max	Min	UB	LB
pH _{inf}	—	7.01	0.46	0.02	8.00	5.40	7.05	6.97
Temp _{inf}	°C	24.73	1.83	0.07	29.00	20.40	24.88	24.58
BOD _{5inf}	mg/L	228.47	41.33	2.08	450.00	74.00	232.57	224.38
COD _{inf}	mg/L	358.34	88.49	4.56	552.70	182.00	367.31	349.37
BOD _{inf} SL	mg/L	821.67	542.71	84.76	2329.5	109	992.96	650.36
COD _{inf} SL	mg/L	2615.11	2798.18	437.00	14090.88	826.56	3498.32	1731.89
TDS _{inf}	mg/L	465.15	86.07	3.71	739.00	230.00	472.44	457.87
TSS _{inf}	mg/L	173.28	11.87	0.73	199.00	146.00	174.72	171.85
EC _{inf}	µS/cm	783.83	118.96	4.86	1070.00	441.00	793.38	774.28
TURB _{inf}	NTU	9.649	0.581	0.023	11	8	9.695	9.603
DO _{inf}	mg/L	1.12	0.99	0.04	3.21	0.07	1.21	1.03
BOD _{5eff}	mg/L	22.06	7.16	0.36	70.00	5.00	22.76	21.36
COD _{eff}	mg/L	40.41	12.46	0.63	58.20	20.00	41.65	39.17

SD, standard deviations; SE, standard error; UB, Upper Bound of 95% Confidence Interval for the mean; LB, Lower bound of 95% Confidence Interval for the mean; BOD, biochemical oxygen demand; COD, chemical oxygen demand; TDS, total dissolved solids; TSS, total suspended solids; EC, electrical conductivity; DO, dissolved oxygen; Temp, Temperature; TURB, turbidity. Suffixes: inf, influent; eff, effluent; SL, Septage Lagoons



the foundation of the nervous system. Various philosophies divide the nervous system's signal progression and network constitution into several categories. In one, nearby neurons in

a neural network mutually interact and compete with one another, adapting to become specific detectors of various signal prototypes. The learning is unsupervised or self-

TABLE 2 Correlation matrix for variables in code vectors.

	pH _{inf}	T _{inf}	BOD _{5inf}	COD _{inf}	BOD _{inf} SL	COD _{inf} SL	TDS _{inf}	TSS _{inf}	EC _{inf}	TURB _{inf}	DO _{inf}	BOD _{5eff}	COD _{eff}
pH _{inf}	1												
T _{inf}	0.161	1											
BOD _{5inf}	-0.461	-0.606*	1										
COD _{inf}	-0.615*	-0.510*	0.922**	1									
BOD _{inf} SL	-0.251	0.167	0.043	0.061	1								
COD _{inf} SL	-0.307	0.153	0.144	0.215	0.834**	1							
TDS _{inf}	0.368	-0.125	0.131	0.088	-0.620*	-0.599*	1						
TSS _{inf}	-0.199	-0.319	0.339	0.275	0.249	0.035	-0.196	1					
EC _{inf}	-0.135	0.210	0.193	0.411	0.041	0.130	0.086	0.409	1				
TURB _{inf}	0.167	0.067	-0.009	-0.048	-0.048	0.125	0.162	-0.386	-0.320	1			
DO _{inf}	-0.587*	0.204	0.098	0.269	0.110	0.301	0.003	0.024	0.234	0.163	1		
BOD _{5eff}	-0.013	0.154	0.033	0.066	-0.309	-0.157	-0.008	0.003	0.252	-0.237	0.196	1	
COD _{eff}	0.014	0.166	-0.131	-0.052	-0.285	0.050	0.114	-0.441	-0.100	0.380	0.344	0.625*	1

*Correlation is significant at the 0.05 level (2-tailed).

**Correlation is significant at the 0.01 level (2-tailed).

TABLE 3 The structure of the ANFIS models developed and tested in the study for predicting effluent BOD values using Gaussian membership functions^a.

Model No	Number of input parameters	Input parameters	Number of membership functions in each input (N_{mf})	Number of linear parameters $P_1=l \times (N_{input}+1)$	Number of nonlinear parameters $P_2=N_{input} \times N_{mf} \times 2$	Total number of parameters $P=P_1+P_2$	Number of fuzzy rules $l=(N_{mf})^{N_{input}}$
M1	4 (Raw)	T_{inf} , pH_{inf} , DO_{inf} , COD_{eff}	2	48	16	64	16
M2	2 (Raw)	pH_{inf} , COD_{eff}	2	12	8	20	4
M3	3 (Raw)	pH_{inf} , EC_{inf} , COD_{eff}	4	320	24	344	64
M4	3 (Raw)	$TURB_{inf}$, EC_{inf} , COD_{eff}	2	24	12	36	8
M5	3 (Raw)	TDS_{inf} , TSS_{inf} , COD_{inf}	3	108	18	126	27
M6	3 (Raw)	TDS_{inf} , TSS_{inf} , $COD_{SL_{inf}}$	3	108	18	126	27
M7	4 (Raw)	T_{inf} , pH_{inf} , DO_{inf} , COD_{eff}	3	324	24	348	81
M8	2 (Raw)	pH_{inf} , COD_{inf}	2	12	8	20	4
M9	4 (Features)	T_{inf} , pH_{inf} , DO_{inf} , COD_{eff}	2	48	16	64	16
M10	2 (Features)	pH_{inf} , COD_{eff}	2	12	8	20	4
M11	3 (Features)	pH_{inf} , EC_{inf} , COD_{eff}	4	320	24	344	64
M12	3 (Features)	$TURB_{inf}$, EC_{inf} , COD_{eff}	2	24	12	36	8
M13	3 (features)	TDS_{inf} , TSS_{inf} , COD_{inf}	3	108	18	126	27
M14	3 (Features)	TDS_{inf} , TSS_{inf} , $COD_{SL_{inf}}$	3	108	18	126	27
M15	4 (Features)	T_{inf} , pH_{inf} , DO_{inf} , COD_{eff}	3	405	24	429	81
M16	2 (Features)	pH_{inf} , COD_{inf}	2	12	8	20	4

^aThe choice of Gaussian membership functions was because it has just two modified parameters, the center, and width, hence it requires less training data.

organizing in this classification, which serves as the foundation for the development of self-organizing maps.

The main working strategy of such maps is the geometrical transformation of non-linear and complex correlation among high-dimensional data into a relatively simple low-dimensional view. SOM is made up of neurons arranged on standard one or two-dimensional grids, with each neuron, i , represented by an n -dimensional weight/reference/codebook vector given by,

$$m_i = [m_{i1}, \dots, m_{in}] \tag{1}$$

where n is the input vector dimension. These weight vectors comprise the codebook, which depicts the characteristics of the data or process. Figure 3 demonstrates that each neuron has two locations: one in the prototype vector, which is the input space, and another in the map grid, which is the output space (Vesanto et al., 2000a; 2000b). Thus, self-organizing maps are a vector projection method that converts high-dimensional input to low-dimensional

output. The connection between adjacent n is determined by the neighborhood relationship.

The mapping is performed from the input Euclidean data space \mathcal{R}^n to a two-dimensional nodule lattice. Every node i is connected to a unique reference vector $m_i \in \mathcal{R}^n$. When there is input data $x \in \mathcal{R}^n$, it is compared to all the m_i to find the best match or response. Input is mapped to specific locations during this process. The Euclidean distance $\|x - m_i\|$, as illustrated in Eq. 2 is used to identify the best matching node, m_c , also known as Best Matching Unit as illustrated in Figure 3B (Kangas and Simulation, 2003).

$$\|x - m_c\| = \min_i \{\|x - m_i\|\} \tag{2}$$

The basic steps in the development of the map, according to the SOM toolbox developed by the Helsinki University of Technology (Vesanto et al., 2000a), are initialization, training, and validation. Normalization is a process that prevents process variables from having a greater impact than other variables, ensuring that the entire

TABLE 4 The performance of the ANFIS models to predict BOD₅.

Model No	No of Input parameters (N)	CRM			MPE (%)			R		
		Training	Testing	Validation	Training	Testing	Validation	Training	Testing	Validation
M1	4 (Raw)	-23.36	21.27	26.76	55.92	48.53	51.24	0.18	0.48	0.39
M2	2 (Raw)	21.89	20.11	26.77	39.76	37.58	48.23	0.66	0.71	0.55
M3	3 (Raw)	-35.91	-24.23	13.44	57.49	52.55	47.44	0.13	0.25	0.58
M4	3 (Raw)	19.16	18.22	-22.11	51.11	46.81	57.32	0.57	0.72	0.67
M5	3 (Raw)	9.45	0.01	5.11	43.23	3.33e-6	2.300e-4	0.71	0.91	0.83
M6	3 (Raw)	-0.02	-0.01	-0.01	0.77	1.54	0.69	0.84	0.79	0.91
M7	4 (Raw)	1.124e-7	3.78e-7	0.03	7.51e-5	8.11e-3	4.66e-4	0.92	0.90	0.81
M8	2 (Raw)	21.03	20.05	-18.58	45.7	38.32	5.88	0.51	0.56	0.71
M9	4 (Features)	1.00e-4	-0.44	0.99	12.24	14.55	22.65	0.89	0.73	0.66
M10	2 (Features)	23.22	-12.62	0.004	46.31	35.22	5.19	0.59	0.71	0.81
M11	3 (Features)	-4.56e-5	-0.234	11.24	5.21	7.33	11.23	0.93	0.86	0.77
M12	3 (Features)	-8.11e-4	-0.025	-0.089	6.01	8.31	17.76	0.85	0.81	0.74
M13	3 (features)	0.03	7.6e-2	-2.29-3	7.22e-4	2.65e-10	5.10e-11	0.85	0.91	0.94
M14	3 (Features)	0.004	0.023	0.072	0.43	4.21	14.23	0.92	0.89	0.79
M15	4 (Features)	3.78e-16	1.12e-16	-1.02e-15	1.56e-14	4.13e-10	2.30e-14	0.99	0.87	0.94
M16	2 (Features)	10.68	16.32	8.71	10.78	12.87	9.21	0.82	0.73	0.83

CRM, coefficient of residual mass; MPE, mean percent error; R, correlation coefficient.
The bold values represent the model that had the better performance compared to the rest.

TABLE 5 Statistics summary of the ANFIS models to predict effluent BOD₅.

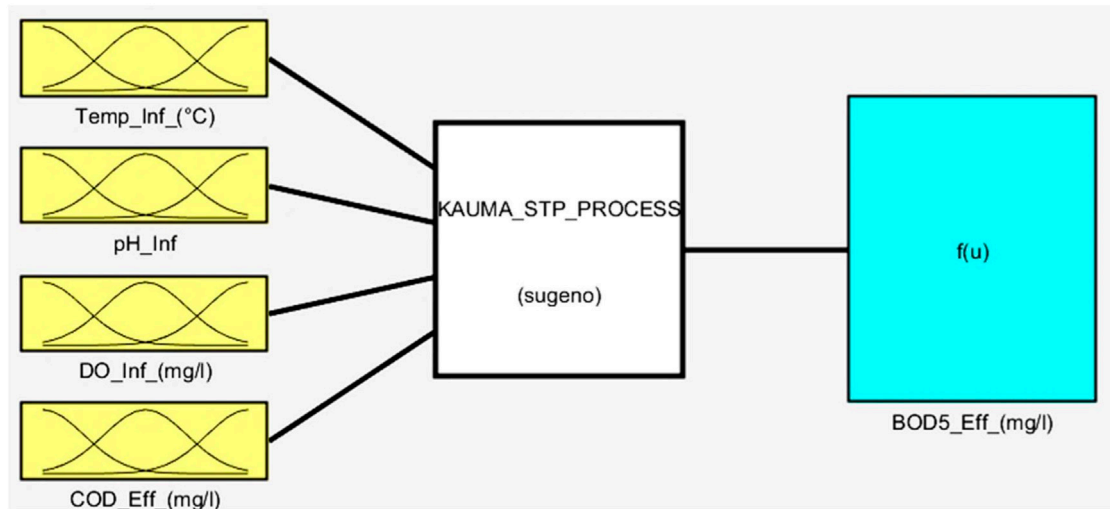
Model No	No of Input parameters (N)	Minimum			Maximum			Mean		
		Training	Testing	Validation	Training	Testing	Validation	Training	Testing	Validation
Observed		9	12	7	56	55	40	22.27	21.87	21.64
M1	4 (Raw)	-14.77	-10.90	5.88	46.74	39.34	31.63	22.67	22.01	19.88
M2	2 (Raw)	-17.75	11.22	-29.15	63.53	48.60	36.66	24.46	18.26	20.71
M3	3 (Raw)	-19.99	-14.67	-28.73	109.00	104.00	98.11	23.77	19.72	20.84
M4	3 (Raw)	-18.66	-11.60	-17.74	206.13	199.06	204.68	22.44	21.50	22.89
M5	3 (Raw)	9.11	14.23	8.45	54.75	58.33	43.41	23.81	20.70	23.77
M6	3 (Raw)	9.51	-12.75	8.23	54.22	56.19	39.73	22.11	21.52	21.71
M7	4 (Raw)	9.21	11.92	7.13	55.47	55.14	42.54	22.76	22.19	22.74
M8	2 (Raw)	-8.45	14.23	8.69	54.89	53.99	39.28	22.66	21.59	22.80
M9	4 (Features)	8.79	11.81	6.73	54.32	54.23	41.45	21.90	21.89	21.23
M10	2 (Features)	9.22	13.43	8.91	60.12	57.90	42.90	22.41	21.66	21.17
M11	3 (Features)	10.16	13.89	8.23	58.61	51.70	58.91	22.90	23.71	22.50
M12	3 (Features)	7.90	11.90	8.90	53.80	57.10	39.88	21.98	22.73	21.70
M13	3 (Features)	8.92	13.74	7.89	53.61	51.82	40.71	22.84	22.81	21.72
M14	3 (Features)	9.66	11.27	9.03	53.47	54.71	43.82	22.17	21.57	21.75
M15	4 (Features)	8.86	14.12	8.19	55.62	43.29	38.56	22.31	20.74	22.08
M16	2 (Features)	9.41	11.45	8.45	55.39	56.29	41.71	23.80	21.67	22.71

M1, Model No 1.

This is descriptive statistics for the model that had better performance compared to the rest. It has been highlighted to reflect its significance.

TABLE 6 Comparative studies in utilization of ANFIS for optimization problems.

Reference	Objective	Nature of the data used	Remarks on the model performance
Qiao et al. (2023)	Employed ANFIS to predict removal of pollutants in Wastewater treatment plant	Utilized data that was first screened by utilizing principal Component analysis (PCA) and Orthogonal Experiments	Satisfactory findings with R^2 values greater than 0.950 were noticed. However, there was disparities between anticipated and actual results
Cheng et al. (2018)	Predicted influent characteristics using integrated Wavelet packet decomposition with ANFIS	Utilized historical data that was first decomposed by wavelet packet decomposition approach prior to feeding the data into ANFIS	Multi-scale ANFIS methodology that outperformed previous methods for predicting influent characteristics
Obasi et al. (2022)	Applied ANFIS, and a classical multi-linear regression analysis (MLR) to predict the performance of Abuja WWTP	Utilized preprocessed data to predict Conductivity, pH, Iron content, BOD, COD, TSS and TDS	MLR model outperformed ANFIS model

FIGURE 7
The structure of Model number 15.

set of variables has the same significance in the construction of maps. Initialization aids the algorithm's convergence to a good result by assigning weight vector values either randomly or linearly. During this process, each neuron is assigned random weight vectors ranging from zero to one (Vermasvuori et al., 2002). The main goal of training is to find the Best Matching Unit (BMU) or winning node among the map units for each input prototype. This unit is very similar to the input pattern. A distance function is commonly used to measure similarity, with closer distances defining greater similarity as defined by the Euclidean distance function. The best matching unit and its neighboring units are updated to reduce the difference between these units and the input pattern (Hsu, 2006). Two types of algorithms are used for updating: sequential training algorithms and batch training algorithms. Once the best matching unit is identified, its weight vectors are shifted closer to the input vector in the input space, a process known as updating. The best matching unit's topological neighbor units are also treated in the same way. The size of the adjustment of the weight vector is determined by the distance of these neighborhood neurons or units from the winner output array. More information on training the map can be found in Vesanto et al. (2000a), Lopez Garca and Machon Gonzalez (2004), Rustum (2009).

The SOM's quality is determined primarily by two error measurements: quantization error (qe) and topographic error (te) (Jorge et al., 2013). The mean Euclidean distance from the input vector to its best matching unit is used to calculate the quantization error.

This, in turn, provides map resolution and aids in identifying outliers. A high quantization error indicates that those input patterns are most likely outliers. The percentage of input vectors for which the best matching unit and the next best are not grid neighbors is referred to as topologic or topographic error. This error indicates the degree of data topology preservation while the map is fitted into the original dataset.

ANFIS

ANFIS modeling is the method of applying various learning techniques developed in the neural network literature to a fuzzy inference system (FIS) (Brown et al., 1994; Brown et al., 1994). The FIS maps its input space to the output space using a fractional non-linear relationship and a set of fuzzy if-then rules (Noori et al., 2013b). A FIS typically has five components: a fuzzification interface,

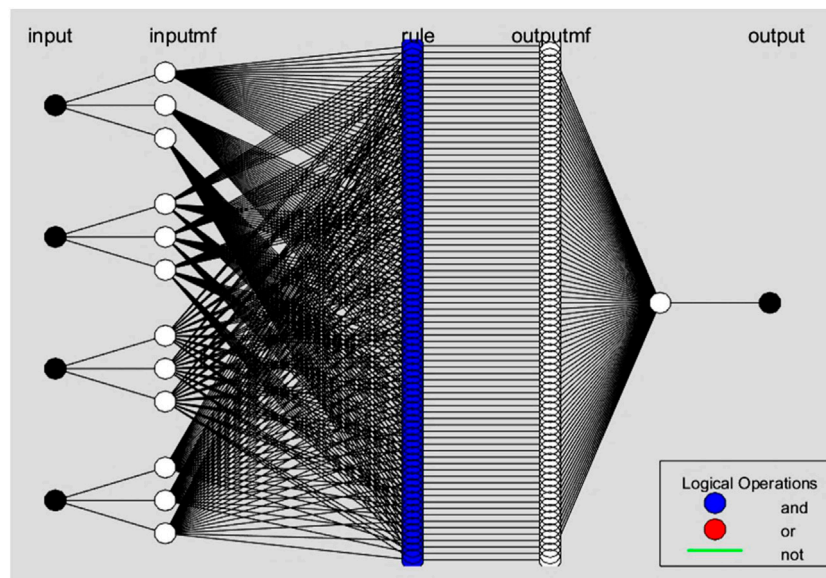


FIGURE 8 Schematic diagram of Model number 15 with 3 membership functions and 81 "IF -THEN" rules.

a rule base, a database, a decision-making unit, and a defuzzification interface. One of the most important steps in ANFIS development is the selection of a FIS type. There are various methods for developing the FIS. The first-order Sugeno FIS with two fuzzy rules (Figure 4) is used in this study as given by Eqs 3, 4:

$$\text{Rule 1: If } x \text{ is } A_1 \text{ and } y \text{ is } B_1; \text{ then } f_1 = p_1x + q_1y + r_1 \quad (3)$$

$$\text{Rule 2: If } x \text{ is } A_2 \text{ and } y \text{ is } B_2; \text{ Then } f_2 = p_2x + q_2y + r_2 \quad (4)$$

where A_1 ; A_2 and B_1 ; B_2 are the membership functions (MFs) for inputs x and y ; respectively; and $p_1; q_1; r_1$ and $p_2; q_2; r_2$ are the parameters of the output function. Also, the output f is the weighted average of the individual rule outputs. To implement these two rules, an equivalent ANFIS structure (Figure 5) should be developed. In Figure 5, the characteristics of each layer are as follows (Jang, 1993; Lei, 2017).

Layer 0: It is called the input layer, and has n nodes where n is the number of inputs to the system

Layer 1: Input membership function—The first layer is used to fuzzificate the inputs, and all the nodes of this layer are adaptive. Its outputs are the membership grade of the inputs as given by Eqs 5, 6

$$o_i^1 = u_{A_i}(x), \quad i = 1, 2. \quad (5)$$

$$o_i^1 = u_{B_{i-2}}(y), \quad i = 3, 4. \quad (6)$$

where $u_{A_i}(x)$ and $u_{B_{i-2}}(y)$ are the fuzzy membership functions. Conventionally, the bell-shaped membership function is used, and it is expressed by Eq. 7

$$u_{A_i}(x) = \frac{1}{1 + \left[\frac{(x-c_i)}{a_i} \right]^{2b_i}} \quad i = 1, 2. \quad (7)$$

where a_i , b_i , and c_i are the parameters of the membership functions

Layer 2: Rule—The nodes in this layer are fixed (Not adaptive). These are labeled M to indicate that they play the role of simple

multipliers. The outputs of this layer represent the fuzzy strengths ω of each rule and can be expressed as

$$o_1^2 = \omega_i = u_{A_i}(x)u_{B_i}(y), \quad i = 1, 2. \quad (8)$$

Layer 3: Normalization—In this layer, the nodes are also fixed. These nodes are labeled with N, which means that they play a normalization role in the fuzzy strengths from the previous layer. The normalization factor is computed by the sum of the weight functions. The outputs of this layer are called normalized fuzzy strengths and are expressed as shown in Eq. 9

$$o_i^3 = \bar{\omega}_i = \frac{\omega_i}{\sum_{i=1}^2 \omega_i}, \quad i = 1, 2. \quad (9)$$

Layer 4: Output membership function—The nodes of this layer are adaptive ones. Its outputs are represented by Eq. 10

$$o_i^4 = \bar{\omega}_i z_i = \bar{\omega}_i (p_i x + q_i y + r_i), \quad i = 1, 2. \quad (10)$$

where p_i , q_i , r_i are the parameters of the membership functions, respectively.

Layer 5: Output—Only one single fixed node, labeled with S, is in this layer. This node performs the sum of the incoming signals. Thus, the overall output is expressed as shown in Eq. 11.

$$o_i^5 = z = \sum_{i=1}^2 \bar{\omega}_i z_i = \frac{\sum_{i=1}^2 \omega_i z_i}{\sum_{i=1}^2 \omega_i} \quad (11)$$

Model evaluation criteria

After fitting the input data into ANFIS or any other model, it is important to evaluate how well the model performs. MATLAB offers "goodness of fit" which has a set of parameters that describe the model's accuracy. Evaluation can be done graphically using residual plots and

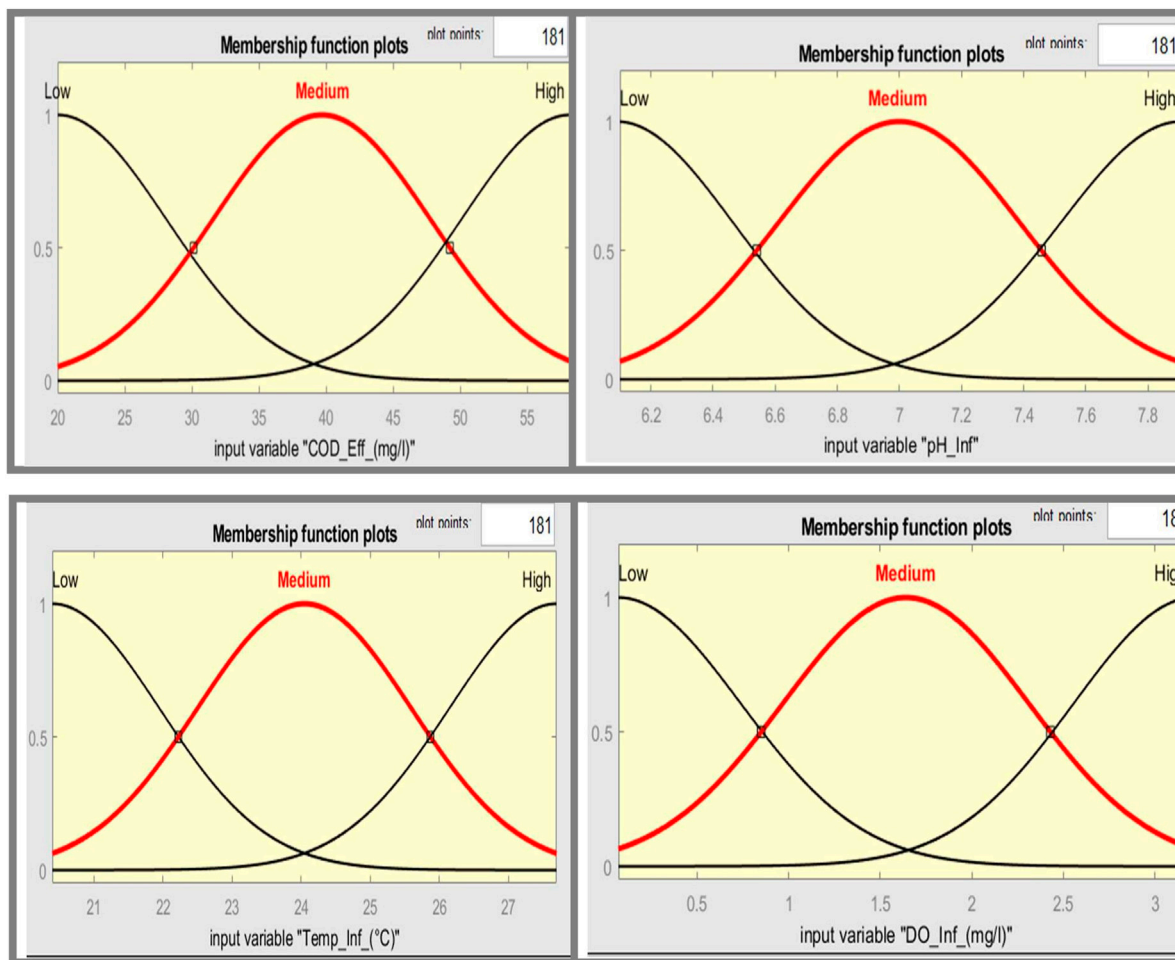


FIGURE 9 Fuzzy membership Functions in the input space.

TABLE 7 The parameters of Gaussian membership functions associated with input variables.

Inputs	Membership function	b (Width)	C (center)
Temp _{Inf}	Low	1.551	20.4
	Medium	1.549	24.05
	High	1.552	27.7
pH _{Inf}	Low	0.3747	6.09
	Medium	0.3893	6.999
	High	0.389	7.908
DO _{Inf}	Low	0.6679	0.06926
	Medium	0.6709	1.639
	High	0.6589	3.216
COD _{Eff}	Low	8.111	20
	Medium	8.11	39.68
	High	8.11	58.2

prediction bounds and numerically using statistical parameters explained below. Graphical measures help the evaluation of the entire dataset at once and can display a wide range of relationships between the model and data (MathWorks, 2020). Numerical evaluation measures include correlation coefficient R, Average Absolute Error (AAE), Mean square error (MSE), and Root Mean Square Error (RMSE). In this study, however, only three indices as given by Eqs 12–14 were used due to their robustness, namely, the correlation coefficient (R) (Wang et al., 2006), the Coefficient of residual mass (CRM) (El-Sadek, 2006), and the Mean percent error (MPE) (Moriassi et al., 2007)

$$R = \frac{N \sum O_i P_i - \sum O_i \sum P_i}{\sqrt{[N \sum O_i^2 - (\sum O_i)^2][N \sum P_i^2 - (\sum P_i)^2]}} \quad (12)$$

$$CRM = \frac{\sum_{i=1}^N O_i - \sum_{i=1}^N P_i}{\sum_{i=1}^N O_i} \quad (13)$$

$$MPE = \sum_{i=1}^N \left(\frac{|O_i - P_i|}{O_i} \right) \times 100\% \quad (14)$$

where P_i is the predicted value, O_i is the observed value and N is the number of data entries.

TABLE 8 Optimised fuzzy rules generated using modeling strategy developed in this study for model number 15.

Rule number	Rule antecedent (IF)				THEN	Consequent parameters				
	Temp _{Inf}	pH _{Inf}	DO _{Inf}	COD _{Eff}		a ₁	a ₂	a ₃	a ₄	a ₀
1	Low	Low	Low	Low		-0.37	-0.51	-0.23	-0.09	42.17
2	Low	Low	Low	Medium		6.44	-16.84	11.48	-1.66	26.5
3	Low	Low	Low	High		66.22	-35.35	-61.86	-3.48	55.61
4	Low	Low	Medium	Low		-27.29	71.38	88.92	7.02	-112.3
5	Low	Low	Medium	Medium		9.94	26	-45.51	-2.56	40.91
6	Low	Low	Medium	High		-6.99	18.29	38.88	4.8	-28.77
7	Low	Low	High	Low		-222.06	30.32	1.27	-500.78	716.3
8	Low	Low	High	Medium		-23.01	25.19	105.33	10.92	-94.69
9	Low	Low	High	High		95.2	-55.45	-97.03	-5.45	87.23
10	Low	Medium	Low	Low		41.8	-12.55	-21.97	-1.23	19.75
11	Low	Medium	Low	Medium		21.75	-9.81	-0.016	-0.96	15.43
12	Low	Medium	Low	High		15.57	-22.43	-1.24	-2.21	35.28
13	Low	Medium	Medium	Low		46.13	-13.43	-23.49	-1.32	21.12
14	Low	Medium	Medium	Medium		62.95	-26.03	-45.55	-2.56	40.95
15	Low	Medium	Medium	High		58.93	-23.36	-40.88	-7.3	36.75
16	Low	Medium	High	Low		-4.54	11.88	20.79	13.17	-18.69
17	Low	Medium	High	Medium		180.37	-134.38	-235.15	-1.21	211.4
18	Low	Medium	High	High		-13.58	35.53	52.17	3.49	-55.89
19	Low	High	Low	Low		22.7	-43.7	-76.46	54.3	68.74
20	Low	High	Low	Medium		-27.63	72.27	90.47	4.11	-113.7
21	Low	High	Low	High		110.96	-65.28	-114.24	-6.42	102.7
22	Low	High	Medium	Low		36.2	-8.38	-14.66	-0.82	13.18
23	Low	High	Medium	Medium		-3.38	25.84	15.46	0.87	-13.9
24	Low	High	Medium	High		-392.69	833.22	1097.55	101.02	-1,616
25	Low	High	High	Low		175.42	288.84	-605.45	-290.41	454.4
26	Low	High	High	Medium		-3.69	25.65	16.89	0.95	-15.18
27	Low	High	High	High		-6.28	16.42	38.73	1.61	-25.83
28	Medium	Low	Low	Low		55	-23.54	-41.19	-2.31	37.03
29	Medium	Low	Low	Medium		40.66	-12.18	-21.31	-1.2	19.16
30	Medium	Low	Low	High		83.7	-46.29	-81	-4.55	72.82
31	Medium	Low	Medium	Low		31.3	-3.4	-5.96	-0.33	5.355
32	Medium	Low	Medium	Medium		44.51	-14.41	-25.22	-1.42	22.67
33	Medium	Low	Medium	High		-26.27	30.71	120.24	6.76	-108.1
34	Medium	Low	High	Low		66.61	-32.98	-57.72	-3.24	51.89
35	Medium	Low	High	Medium		-7.95	20.81	36.41	9.05	-32.73
36	Medium	Low	High	High		47.25	-18.97	-33.19	-1.87	29.84
37	Medium	Medium	Low	Low		35.79	-9.92	-17.36	-0.98	15.61

(Continued on following page)

TABLE 8 (Continued) Optimised fuzzy rules generated using modeling strategy developed in this study for model number 15.

Rule number	Rule antecedent (IF)				THEN	Consequent parameters				
38	Medium	Medium	Low	Medium		55.38	-24.54	-42.95	-2.41	38.61
39	Medium	Medium	Low	High		46.28	-16.43	-28.75	-1.62	25.85
40	Medium	Medium	Medium	Low		40.73	-12.38	-21.67	-1.22	19.48
41	Medium	Medium	Medium	Medium		38.49	-11.75	-20.57	-1.16	18.49
42	Medium	Medium	Medium	High		65.51	-32.73	-57.27	-3.22	51.49
43	Medium	Medium	High	Low		53.96	-23.44	-41.02	-2.31	36.88
44	Medium	Medium	High	Medium		45.13	-16.03	-28.05	-1.58	25.22
45	Medium	Medium	High	High		46.13	-16.04	-28.08	-1.58	25.24
46	Medium	High	Low	Low		29.88	-4.91	-8.6	-0.48	7.732
47	Medium	High	Low	Medium		52.9	-23.44	-41.01	-2.3	36.87
48	Medium	High	Low	High		-57.37	150.08	152.62	14.76	-236.1
49	Medium	High	Medium	Low		84.25	-47.74	-83.55	-4.7	75.11
50	Medium	High	Medium	Medium		-3.83	27.03	17.55	0.99	-15.78
51	Medium	High	Medium	High		129.2	-84.22	-147.39	-8.28	132.5
52	High	High	High	Low		-28.48	74.5	85.37	7.33	-117.2
53	High	High	High	Medium		122.33	-79.33	-138.82	-7.8	124.8
54	High	High	High	High		140.51	-90.26	-157.95	-8.88	142
55	High	Low	Low	Low		50.36	-19.25	-33.68	-1.89	30.28
56	High	Low	Low	Medium		-20.73	56.23	66.91	5.33	-85.32
57	High	Low	Low	High		38.31	-11.28	-19.74	-1.11	17.75
58	High	Low	Medium	Low		32.98	-7.79	-13.64	-0.77	12.26
59	High	Low	Medium	Medium		107.9	-67.76	-118.58	-6.66	106.6
60	High	Low	Medium	High		104.93	-65.22	-114.13	-6.41	102.6
61	High	Low	High	Low		-0.73	24.91	3.34	0.19	-3.002
62	High	Low	High	Medium		86.53	-51.08	-89.38	-5.02	80.35
63	High	Low	High	High		31.99	-5.82	-10.18	-0.57	9.156
64	High	Low	Low	Low		43.22	-13.65	-23.89	-1.34	21.48
65	High	Medium	Low	Medium		42.97	-13.01	-22.77	-1.28	20.47
66	High	Medium	Low	High		-1.95	25.11	8.94	0.5	-8.038
67	High	Medium	Medium	Low		51.25	-21.59	-37.78	-2.12	33.96
68	High	Medium	Medium	Medium		30.94	-5.07	-8.87	-0.5	7.976
69	High	Medium	Medium	High		-2.04	24.33	9.32	0.52	-8.378
70	High	Medium	High	Low		41.02	-13.12	-22.96	-1.29	20.64
71	High	Medium	High	Medium		28.12	-2.94	-5.14	-0.29	4.622
72	High	Medium	High	High		29.61	-4.21	-7.36	-0.41	6.616
73	High	High	Low	Low		42.89	-15.4	-26.94	-1.51	24.22
74	High	High	Low	Medium		42.94	-12.92	-22.6	-1.27	20.32
75	High	High	Low	High		430.33	-319.99	-559.95	-31.47	503.4

(Continued on following page)

TABLE 8 (Continued) Optimised fuzzy rules generated using modeling strategy developed in this study for model number 15.

Rule number	Rule antecedent (IF)				THEN	Consequent parameters				
76	High	High	Medium	Low		-6.03	25.77	27.6	1.55	-24.81
77	High	High	Medium	Medium		95.95	-54.8	-95.9	-5.39	86.21
78	High	High	Medium	High		62.88	-28.82	-50.43	-2.83	45.34
79	High	High	High	Low		55.92	-23.33	-40.82	-2.29	36.7
80	High	High	High	Medium		78.63	-43.49	-76.11	-4.28	68.42
81	High	High	High	High		48.13	-18.65	-32.64	-1.83	29.34

inf, Influent; eff, Effluent; Temp, Temperature; DO, dissolved oxygen; COD, chemical oxygen demand. Fuzzy Inference Diagram for model number 15.

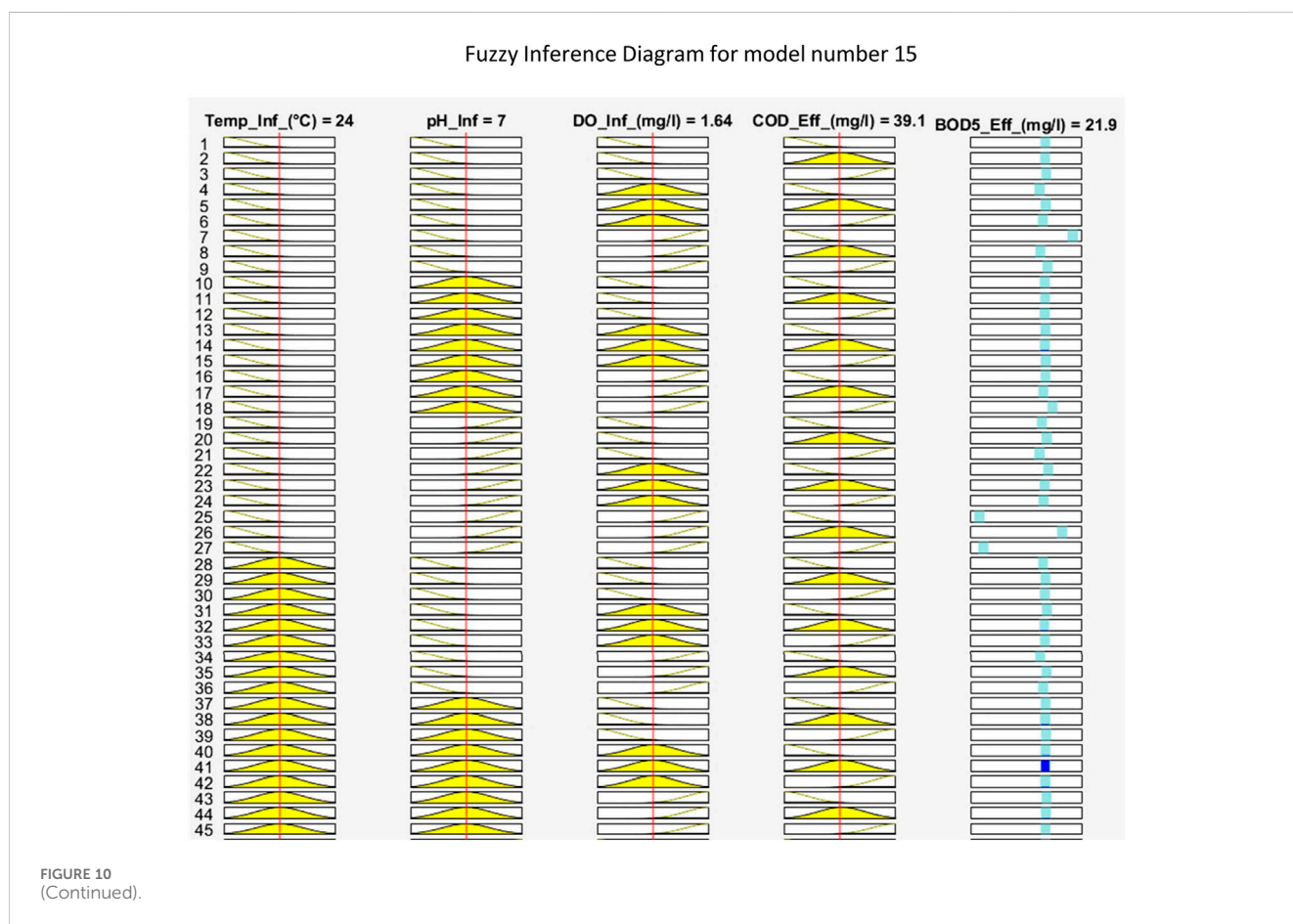


FIGURE 10 (Continued).

The goodness of fit measures the similarity of the shapes of the original and predicted cited time series and ranges between -1 and 1; the absolute value of the correlation coefficient for perfect prediction is unity (Rustum, 2009). The CRM characterizes the tendency to over-estimate CRM < 0 or under-estimate a property (CRM > 0) (Malota et al., 2022) on the other hand, MPE measures the magnitude of errors between the measured and predicted values relative to the measured values. MPE value closer to zero indicates that the predicted values are very close to the measured values (Legates and McCabe, 1999; Malota et al., 2022). To overcome the problem of overfitting, an

early stop rule was applied by dividing the KSTP data into three subsets: training (432 data points), validation (92 data sets), and testing (92 data sets).

Ethical consideration

The study sought clearance from the Mzuzu University Research Ethics Committee (MZUNIREC) Ref No: MZUNIREC/DOR/21/62. Permission was also obtained from Lilongwe City Council to engage Laboratory technicians during data collection processes. Informed

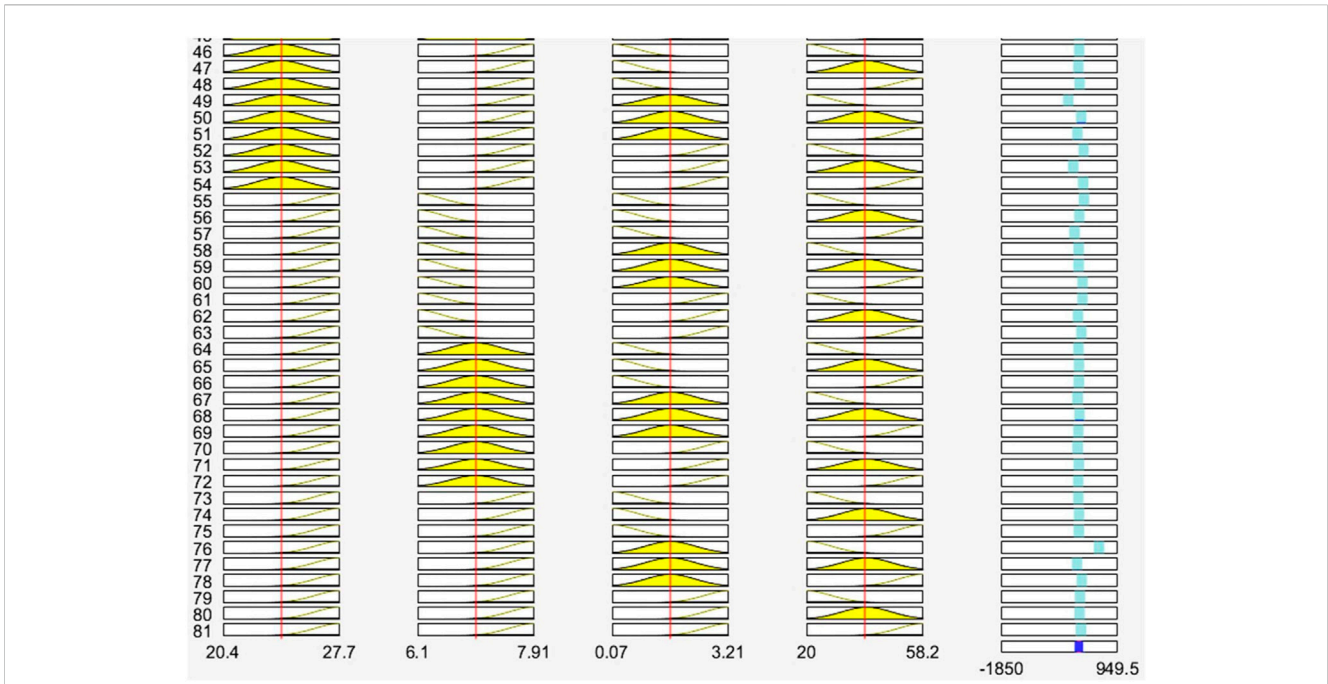


FIGURE 10
(Continued). Fuzzy inference diagram for model number 15 predicting effluent BOD. To obtain the output value as shown in the picture, the user only needs to enter the input values.

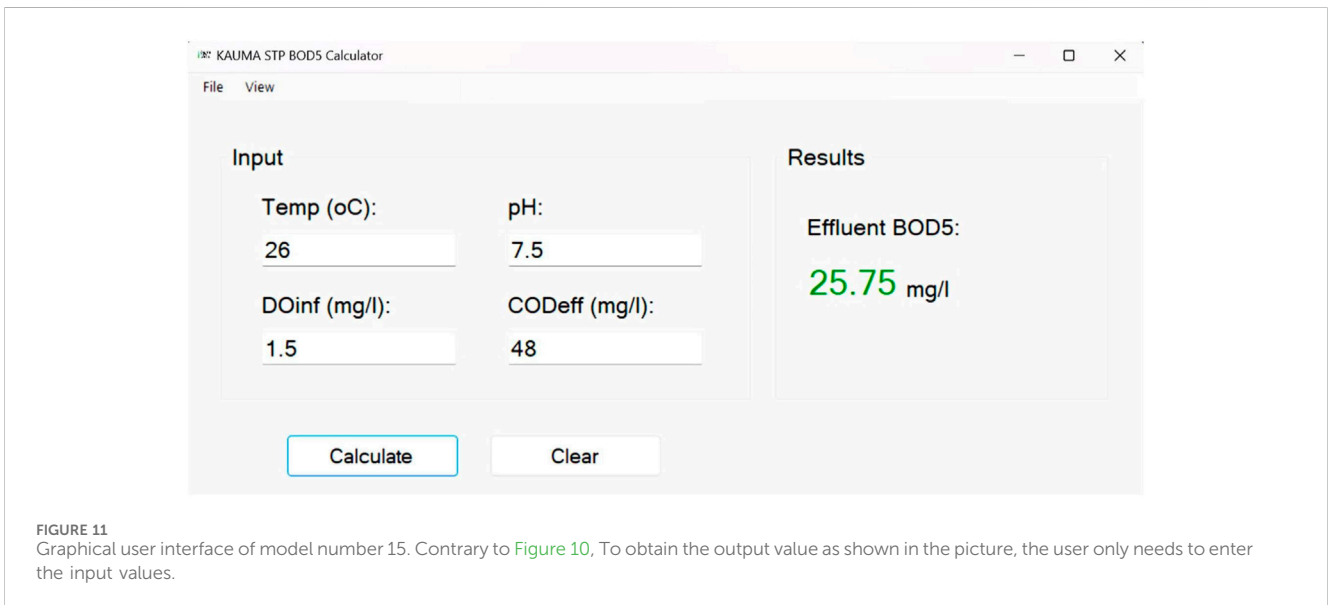


FIGURE 11
Graphical user interface of model number 15. Contrary to Figure 10, To obtain the output value as shown in the picture, the user only needs to enter the input values.

consent was also obtained from the Laboratory technicians and KSTP who participated in the study.

Results and discussions

Descriptive statistics of Kauma sewage treatment plant data

The preprocessed data, with a sample size of 616 data sets per variable, was examined. The estimated descriptive statistics for a

number of variables at the KSTP (Table 1) offered an in-depth overview of influent and effluent characteristics. The pH of the influent wastewater averaged 7.01, indicating slightly alkaline conditions, with a standard deviation (SD) of 0.46, indicating steady pH levels. The upper bound (UB) and lower bound (LB) values (7.05 and 6.97, respectively) set the 95% confidence interval for pH readings. In terms of temperature (Temp inf), the mean of 24.73°C demonstrates a moderate thermal condition, with an SD of 1.83 suggesting variability. UB (24.88) and LB (24.58) determined the 95% confidence interval. BOD_{5inf} and COD_{inf} results, with mean values of 228.47 mg/L and 358.34 mg/L, respectively,

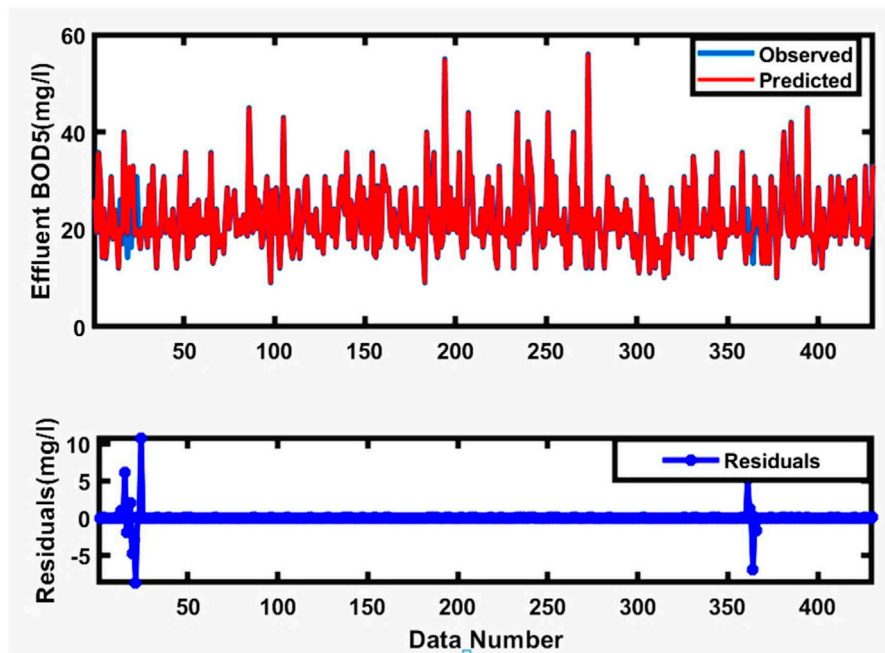


FIGURE 12 Time series plots of observed and predicted BOD during training for model number 15.

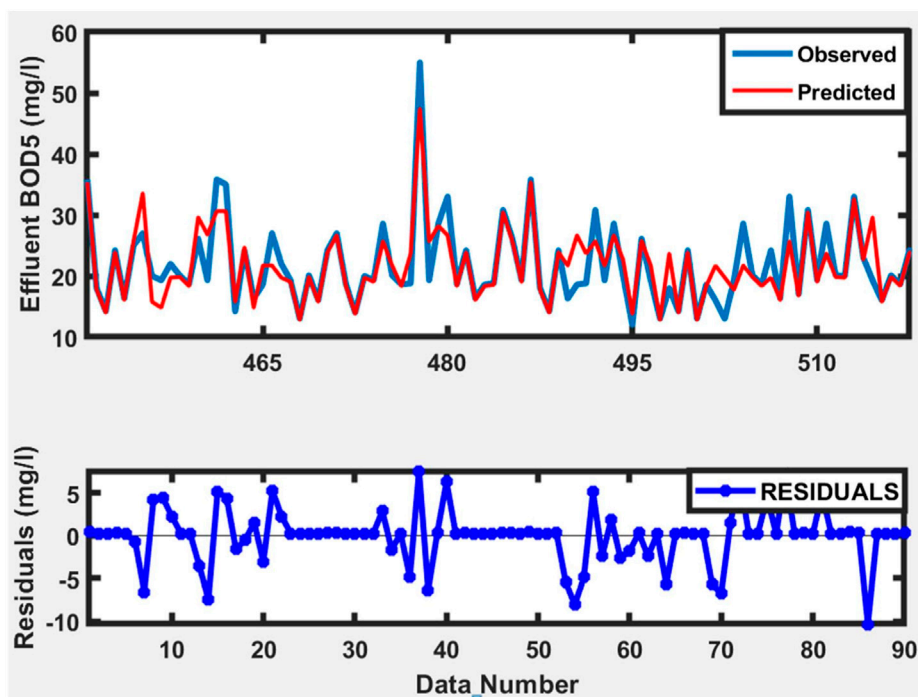


FIGURE 13 Time series plots of observed and predicted BOD during testing for model number 15.

emphasized the organic load in the influent. TDS_{inf} and TSS_{inf} provide information on total dissolved and suspended solids, with values of 465.15 mg/L and 173.28 mg/L, respectively. EC_{inf} (mean: 783.83 S/cm) and $TURB_{inf}$ (mean: 9.649 NTU) measurements

provided information about electrical conductivity and turbidity. The mean DO_{inf} of 1.12 mg/L indicated the concentration of dissolved oxygen, which is essential for aerobic living activity. Effluent BOD_{5eff} (mean: 22.06 mg/L) and COD_{eff} (mean:

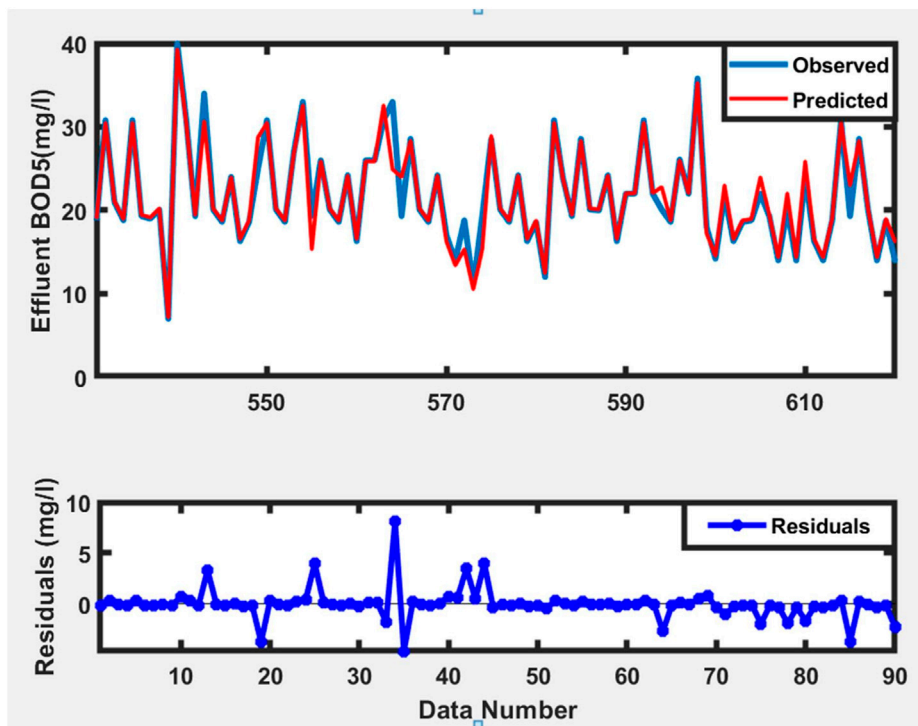


FIGURE 14 Time series plots of observed and predicted BOD during Validation for model number 15.

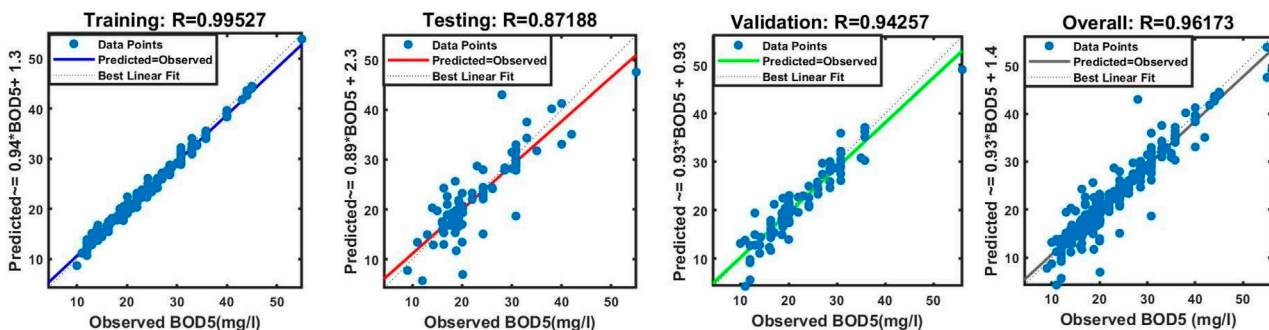


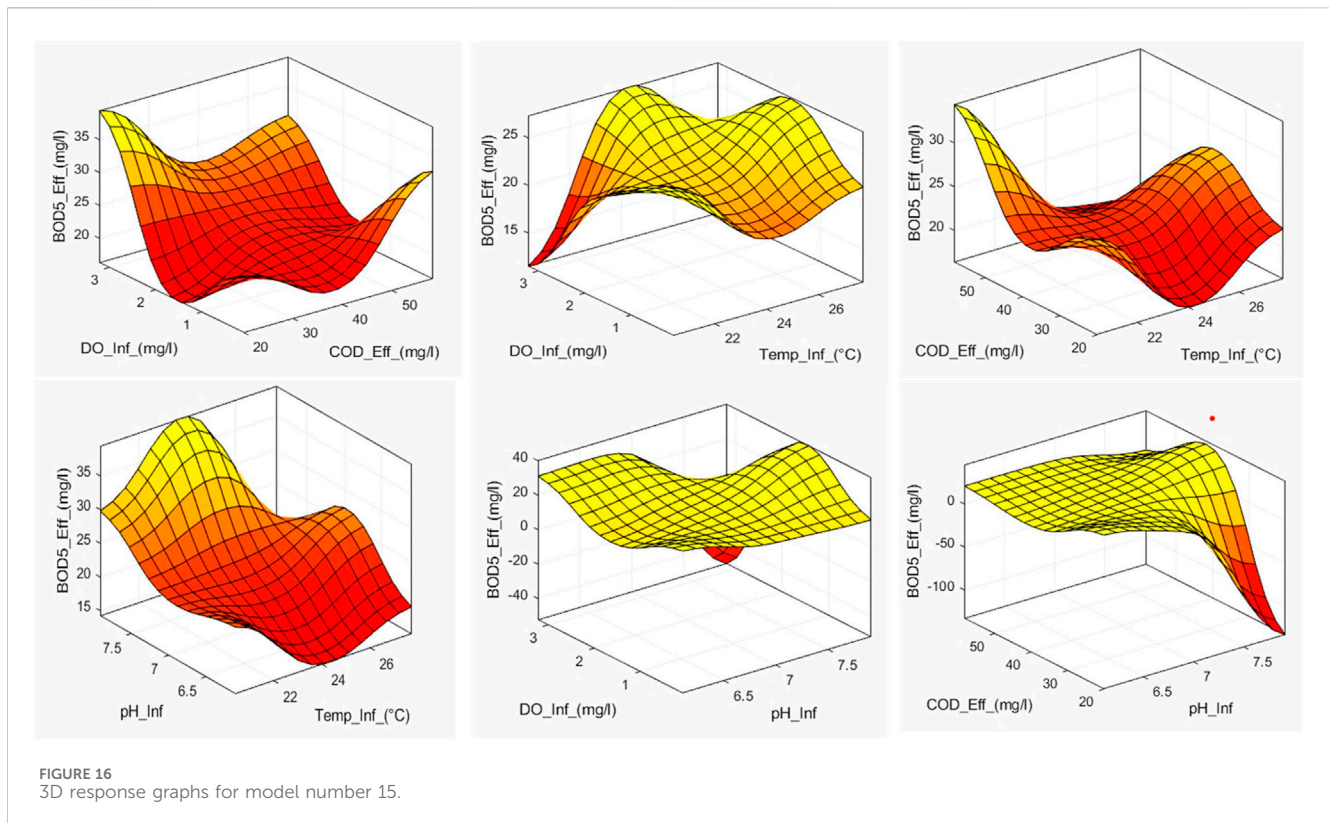
FIGURE 15 The scatter plot of modeled versus observed data during training, testing, and validation for model number 15.

40.41 mg/L) demonstrated a significant reduction in organic and chemical oxygen demand, demonstrating the efficacy of the treatment technology.

The mean COD to BOD₅ ratios were found to be 1.57 and 1.83 for influent and effluent wastewater, respectively. However, samples from septage lagoon had a much higher ratio of 3.18, which is above the average range of 1.25–2.5 for domestic wastewater (Metcalf and Eddy, 2013). This discrepancy stems from various factors as highlighted by Niwagaba et al. (2014). Firstly, wastewater from septic tanks and pit latrines contains more organic and inorganic constituents, such as feces and household chemicals, that can elevate COD levels. In addition, longer retention times in septic tanks and latrines facilitate greater organic decomposition

resulting into high COD than BOD₅ levels. Furthermore, anaerobic conditions prevalent in septic tanks produce non-biodegradable compounds that contribute to COD. Lastly there is minimal dilution in septic systems compared to sewer networks, this maintains higher COD concentrations until discharge (Niwagaba et al., 2014).

Before beginning the modeling process, the entire dataset was divided into three sets: the first set of 432 observations was used to train the model, the second set of 92 observations was used to test the model, and the final set of 92 observations was used to validate the model. The study looked at two scenarios: the first consisted of developing an Adaptive Neuro-Fuzzy Inference System (ANFIS) Model from raw data, and the second involved developing a hybrid



Self-Organizing Map (SOM) and ANFIS model using extracted features.

SOM component planes

The generation of component planes, a key feature of SOMs, is a rigorous procedure that demonstrates relationships between variables in the data. These planes are created during SOM training, which involves mapping the input space onto a two-dimensional grid of neurons. Each neuron corresponds to a weight vector, whose dimensions match those of the input data (Mng'ombe et al., 2023). By iteratively altering these weights, the SOM learns to represent the data's underlying structure. Once trained, component planes are created by assigning colors or intensities to neurons based on the values of specified dimensions in the input data (Kumar et al., 2021a). This visualization technique provides useful insights on the relationships and distributions of distinct elements, making it easier to explore and analyze complex datasets (Nkiaka et al., 2016). These component planes, as shown in Figure 6, represent each variable in the SOM. Each plane is effectively a sliced SOM, with a single vector variable indicating its value in each map unit (Kaltch et al., 2008). To improve readability, the component planes are color-filled or grey-scaled, depicting the feature values of each SOM unit inside the 2-D lattice. Darker hues imply that the associated variable has a lower relative value. This visual depiction efficiently delineates zones where a variable is high, low, or average, allowing for a simple understanding of the correlation between SOM-simulated values of selected wastewater parameters (Kumar et al., 2021b).

A visual analysis of the component planes indicates that the BOD_{5inf} plane's color (or gray) gradient aligns parallel to the COD_{inf}

gradient, demonstrating a correlation where high BOD_{5inf} values are associated with high COD_{inf} values and *vice versa*. Similarly, greater BOD_{5eff} levels correlate with high COD_{eff} levels and *vice versa*. The component planes support a negative association between pH and BOD_{5inf} , COD_{inf} , and DO_{inf} , with low pH values associated with high BOD_{5inf} , COD_{inf} , and DO_{inf} values. The expected positive association between BOD and COD has been validated, correlating with expectations that COD values are often greater than BOD values, with the ratio fluctuating depending on wastewater characteristics (Rai et al., 2019). The entire correlation matrix containing all 11 variables of the prototype vectors is shown in Table 2. While this table is a simple tool for examining the linear relationships between different variables, its findings are consistent with the cross-correlation indications derived from the much more complex SOM analysis, which resulted in the development of the component planes.

Table 2 presents a thorough perspective of the correlation matrix for the variables within the code vectors, giving insights into the complex relationships between different parameters within the wastewater treatment framework. Among the notable findings was a modest positive correlation between pH and temperature (T_{inf}), indicating a minor tendency for both variables to fluctuate together. Furthermore, a strong negative connection occurred between influent BOD_{5inf} and COD_{inf} , which corresponded to the expected inverse association in wastewater. The component planes revealed the influence of the septage lagoon (BOD_{inf} SL and COD_{inf} SL) on numerous parameters, demonstrating a complicated interaction between the septage lagoon and other wastewater properties. Positive correlations between total dissolved solids (TDS_{inf}) and total suspended solids (TSS_{inf}) in

the influent indicated a simultaneous increase in both metrics. In contrast, electrical conductivity (EC_{inf}) exhibited a negative relationship with turbidity ($TURB_{inf}$), implying that higher electrical conductivity is associated with clearer wastewater. DO_{inf} (dissolved oxygen in influent) had a substantial negative correlation with effluent biochemical oxygen demand (BOD_{5eff}), highlighting the relevance of dissolved oxygen in the treatment process. Furthermore, effluent chemical oxygen demand (COD_{eff}) demonstrated a positive association with TSS_{inf} , indicating a possible relationship between suspended solids concentration and chemical oxygen demand in effluent. In conclusion, our correlation matrix gave a foundational understanding of the interplay of several wastewater metrics, stressing the importance of these correlations in describing wastewater quality, as highlighted by the significant correlations at the 0.05 and 0.01 levels.

ANFIS model structure

Table 3 displays the model architectures of several models developed and evaluated with Gaussian membership functions. Multiple models were developed by experimenting with different combinations of input variables and using various membership functions. The association of these input factors to effluent BOD_5 and the promptness with which each variable could be measured influenced their selection. Given the available database, the inclusion of four input variables was assessed to be the maximum number of combinations possible. For example, when using four inputs, each associated with three membership functions, the total number of adjusted parameters, as calculated by Eq. 15, was 430—well within the 432 data points available for training. The evaluation of five parameters, however, using five parameters could exceed the number of training data sets, limiting the model's degrees of freedom.

$$N_{total} = (N_{input} \times N_{mf} \times N_{pp}) + (l \times N_{cp}) \quad (15)$$

$$l = (N_{mf})^{N_{input}} \quad (16)$$

$$N_{cp} = N_{input} + 1 \quad (17)$$

where N_{total} is the total number of modified parameters, N_{input} is the number of inputs, N_{mf} is the number of membership functions associated with each input, N_{pp} is the number of modified parameters per membership function, i. e., in the case of the Gaussian membership function; l in Eq. 16 is the number of rules; N_{cp} in Eq. 17 is the number of modified parameters in the sequence part of each rule

Table 4 presents a detailed summary of the performance of produced models in two scenarios: M1–M8, where models were built using raw data, and M9–M16, where models were built using extracted features using SOM. The results show that model M1–M16's performance was unsatisfactory, as shown by higher values of the Coefficient of Residual Mass (CRM) and Mean Percent Errors (MPE). Furthermore, as seen in Table 5, models developed utilizing raw data produced negative results.

Table 4 shows that improving the raw data by pre-processing with the SOM technique considerably improved model performance. Consider models 7 and 15, which both had the

same structure—four inputs and three membership functions associated with each input. However, model number 15 outperformed model number 7, with the correlation coefficient in the validation dataset increasing from 0.81 to 0.94. This trend is repeated for the remaining models, demonstrating the effectiveness of raw data pre-processing with the SOM algorithm in enhancing overall model performance.

The ANFIS models' performance, as presented in Tables 4, 5, provides a more comprehensive understanding of the predictive abilities for BOD_5 concentrations. The coefficient of residual mass (CRM), mean percent error (MPE), and correlation coefficient for models with raw and extracted features are presented in Table 4. Model M1, which had four raw input parameters, had negative CRM values during testing and validation, indicating a probable model fitting issue. Similarly, during testing, Model M5 demonstrated an MPE close to zero, indicating a near-perfect match. Models M3 and M11, which used three raw input parameters, had negative CRM values, indicating an overestimation of BOD_5 concentrations. The addition of feature extraction in Models M9–M16 significantly increased performance, with the Model M15 exhibiting excellent results including nearly minimal CRM and MPE values and excellent correlation coefficients.

Table 5 summarizes statistics on predicted effluent BOD_5 concentrations, which offer light on the models' ability to mimic observed values. Models containing raw input parameters, such as M3 and M4, had broader ranges and higher mean values, indicating difficulties in predicting extreme concentrations. Model M5 stood out for its consistency with observed values, having a shorter range and closer mean value alignment. Models M9–M16, on the other hand, demonstrated competitive performance with reduced ranges and mean values by leveraging extracted characteristics. Model M15, in particular, displayed distinct match with observed values. However, negative predictions in raw data, as demonstrated in Models M2 and M8, should be taken into account because they may reflect limits in effectively capturing complex relationships. Overall, the introduction of feature extraction demonstrated potential to enhance the predicted accuracy of ANFIS models for effluent BOD_5 values.

These findings are consistent with previous research, as shown in Table 6, and highlight the need of combining ANFIS algorithms with complementing approaches such as SOM to improve model accuracy. Discrepancies discovered in similar studies highlight the complexities of this methodology and its critical role in improving the reliability and overall performance of ANFIS models.

Given Model 15's higher performance as compared to its competitors, an in-depth scrutiny was conducted solely on this model. Model 15 is distinguished by three membership functions associated with each of its four input variables, namely, T_{inf} , pH_{inf} , DO_{inf} , and COD_{eff} , as illustrated in Figures 7, 8. Figure 9 depicts the membership functions and Gaussian membership functions based on the operational range of the model.

Membership functions play an important role in defining and expressing the fuzzy sets that are essential to a fuzzy inference system. Figures 7–9 exemplify how these functions help to express fuzzy thinking and decision-making based on linguistic considerations. Membership functions, in essence, quantify the degree to which an input value aligns with a given fuzzy set. These functions, which typically span a

specific range of input values, assign a membership degree, ranging from 0 to 1, to each value inside that range. This degree of membership indicates the input value's association with the given fuzzy set, providing a deeper understanding of the input's participation in the larger fuzzy set.

The parameters for the Gaussian membership functions related to input variables are summarized in Table 7, which includes the center (c) and width (b) components. The developed model is distinguished by a thorough set of 81 rules that comprise a total of 429 modified parameters. There are 24 non-linear parameters among these, with the remaining 405 linear parameters forming the model's complicated framework.

Table 8 illustrates the optimized fuzzy rules that govern Model 15. These 81 rules define the complex relationships between input and output variables. Figure 10 illustrates the integration process of these rules, which complements this tabular representation. Table 8 systematically details each rule, with discrete parts dedicated to the "IF and THEN" conditions for each rule. The IF component defines a set of criteria depending on input variables, whereas the THEN component defines the expected consequence or action. For example, rule 1 in Table 8 can be understood as follows:

IF (TEMP) is Low and (pH) is Low and (DO_{inf}) is Low and COD_{eff} is low, **THEN** (effluent BOD) is $42.17 - (0.37*temp) - (0.51*pH) - (0.23*DO) - (0.09*COD_{eff})$

Data that was not used in the training phase was used for testing and validation of the trained model. Figures 11–13 depict time series plots of observed and anticipated effluent BOD_5 alongside their corresponding residuals during the training, testing, and validation processes. Figure 14 depicts the modeled data in comparison to the observed data during the training, testing, and validation phases.

To determine the number of rules, the typical fuzzy inference approach relies on an expert judgment which is well-versed in the simulated system. This expert employs heuristic insights gained from vast experience gained from the simulations. In this study, however, the number of membership functions allocated to each input variable was established empirically by trial and error, eliminating the requirement for an expert judgement. The suggested model accurately determines process conditions by combining values from multiple factors. Furthermore, the suggested model is resistant to missing variables and outliers. In comparison to deterministic models, creating a fuzzy logic model is likewise a relatively simple task.

The interactions between numerous input variables and a single output variable are frequently shown via 3D graphs when using the Fuzzy Toolbox in MATLAB. These graphs support decision-making and aid in understanding fuzzy systems' behavior. To understand a 3D graph produced by the Fuzzy Toolbox, it is necessary to examine its shape, contours, and surface properties. As illustrated in Figure 15 the model input variables ($Temp_{inf}$, pH_{inf} , DO_{inf} and COD_{eff}) are represented on the X and Y-axes of the graphs. These variables frequently match up with linguistic concepts or membership algorithms specified in the fuzzy system. For interpretation, it is crucial to comprehend the range and linguistic significance of these variables. On the 3D graph's Z-axis, the output variable ($BOD_{5_{eff}}$) is shown. It displays the system's reaction or output to the supplied inputs. On the graph, the output variable values are typically depicted by color or contour lines.

Conclusion

The current study offers a novel approach for predicting BOD_5 values in wastewater using wastewater data collected from the KSTP in Lilongwe City. To successfully predict effluent BOD_5 , the hybrid SOM-ANFIS model was trained, validated, and tested. Initially, a set of measured raw data was used to train and test the ANFIS model. The model did not work well, though, because the raw data was noisy. To tackle this issue, features from the data were extracted using the SOM. These retrieved features were used to train and evaluate a new set of models, thereby improving their performance. The results showed that the SOM-ANFIS model outperformed the ordinary ANFIS model in terms of modeling capabilities and certainty, even when accounting for varying numbers of inputs and fuzzy membership functions. The SOM-ANFIS model was also able to handle blank spaces in the data or missing values without challenges. This implies that SOM assisted models have greater capabilities compared to ordinary ANFIS in predicting BOD_5 for KSTP. Using MATLAB's app designer, an easy-to-use graphical user interface as demonstrated in Figure 16 was developed to improve usability and user-friendliness. The developed GUI was able to facilitate user interaction and understanding the created fuzzy inference system. The developed model is expected to reduce treatment operation and testing costs, allow continuous monitoring, and consequently protect the environment. Future improvement of the developed model will include integrating it with hardware components through the Supervisory Control and Data Acquisition (SCADA) system. The authors recommend for the development of a specialized model, such as a Convolutional Neural Network, intended exclusively for fecal sludge characterization. Considering the fact that faecal sludge characteristics are highly variable with space and time, it is further recommended that data from other sources such as rivers and other wastewater treatment facilities in Malawi and beyond be collected to update the developed models. This will widen the application of developed models to expose them to a wider range of scenarios.

Software availability statement

The SOM Toolbox (Version 2.2) for MATLAB used in this study is freely available for download from GitHub (<https://github.com/ilarinieminen/SOM-Toolbox>). The study also used the fuzzy logic toolbox available in MATLAB

Data availability statement

The original contributions presented in the study are included in the article/supplementary material, further inquiries can be directed to the corresponding author.

Author contributions

MHM: Conceptualization, Data curation, Formal Analysis, Funding acquisition, Investigation, Methodology, Project administration, Resources, Visualization, Writing—original draft, Writing—review and editing. EM: Conceptualization, Data

curation, Investigation, Methodology, Software, Supervision, Writing—original draft, Writing—review and editing, Formal Analysis, Funding acquisition, Project administration, Resources, Validation, Visualization. BC: Project administration, Supervision, Writing—original draft, Writing—review and editing. RC: Writing—original draft, Writing—review and editing, Methodology.

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Conflict of interest

The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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