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Reserve allocation of high-penetration renewable energy grids considering frequency security

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As the penetration rate of renewable energy in the power grid continues to rise, the reserve criteria for traditional power grids dominated by synchronous generators (SGs) have difficulty meeting system frequency security requirements. This study proposes a frequency security-constrained optimization approach for the allocation of reserve capacity in high-penetration renewable energy grids that utilize multitype reserve resources, including SGs and nonsynchronous units, to address the frequency security issue. First, strategies and models for expanding the sources of frequency regulation reserves are analyzed, including various types of renewable energy generation, such as wind turbine (WT) curtailment and the combination of photovoltaic (PV) cells and battery storage. A refined reserve criterion is then proposed that considers multidimensional evaluation indices from both operational economy and frequency security aspects. Finally, a bilevel optimization model for reserve capacity allocation on multiple timescales that considers frequency security is constructed. The rationality and effectiveness of the proposed reserve allocation scheme were verified using a practical power grid in Southwest China.

KEYWORDS

reserve, frequency security, primary frequency regulation, optimization, allocation

1 Introduction

Accelerating the development of renewable energy is an important goal for achieving energy transformation and China's dual carbon goals (Yuan et al., 2023). The installed capacity of renewable energy units in China (accounting for 53.9% of the total installed capacity) will surpass that of thermal generation units for the first time by the end of 2023 (National Development and Reform Commission of People's Republic of China, 2023). The installed capacity of wind and photovoltaic units has exceeded 1 billion kW, and new energy sources have become the first or second largest installed power sources in 23 provinces. However, wind and solar energy generation are volatile, intermittent, and uncertain (Hakami et al., 2023). When hosting them on a large scale in a power grid, a considerable amount of additional reserve capacity must be allocated. The existing reserve capacity criteria used for traditional power grids, which primarily rely on synchronous generators (SGs), are too crude to be applicable to power grids with a high penetration

of renewable energy (Hedayati-Mehdiabadi et al., 2015). Consequently, determining the optimal allocation of reserve capacity in a reasonable manner is an urgent problem.

Studies have been conducted to expand the reserve capacity sources. These studies primarily focused on retrofitting existing thermal generators and configuring new flexible resources. Various peak-shaving strategies employed during the operation of thermal generators have been analyzed to validate the advantages of their flexibility improvements (Zhao et al., 2018). Some studies have examined the impact of flexibility retrofitting schemes on the operating costs and level of accommodating renewable energy based on dispatch models involving thermal units (Garoarsdottir et al., 2018). From the perspective of peak-shaving markets, a few researchers have integrated the flexibility retrofitting of thermal power units into the market cost (Navid and Rosenwald, 2012). However, simply retrofitting thermal power units cannot effectively cope with the continuous integration of renewable energy generators and the phasing out of old thermal generators in the future. Therefore, it is essential to explore the configuration of new flexible resources to expand the sources of the system reserve capacity. For instance, coordinated planning of battery energy storage (Li and Wang, 2021), thermal storage (Gottwalt et al., 2017), and other equipment can supplement the reserve requirements of high-proportion renewable energy grids. In addition, some authors have investigated existing resources within the system, such as electric vehicles (Zhang et al., 2022) and load demand (Chen et al., 2020), and quantitatively analyzed their potential to provide reserve support (Kong et al., 2023). However, existing studies rarely consider the reserve potential of a large number of renewable energy generation units connected to the power grid, which can not only overcome the limitations of retrofitting thermal power units by leveraging their existing scale but also offer greater economic feasibility than the configuration of flexible resources.

In terms of evaluating reserve allocation, the literature mainly focuses on economic and reliability evaluations, such as determining the optimal reserve capacity based on the cost-benefit method (Ortega-Vazquez and Kirschen, 2009) and evaluating the reserve capacity demand of the system by combining the capacity outage probability table (COPT) and the expected energy not served (ENS) index of the net load prediction error (Shao et al., 2021). Liu and Tomsovic (2012) considered the uncertainty of renewable generation and load and proposed a probabilistic ENS calculation method. Based on this method, the factors of unit failure outages were embedded in the unit commitment model with reliability constraints (Lv et al., 2017). However, a considerable number of SGs are being replaced by renewable energy generators, the rotational inertia level and the frequency support capability of the power grid continue to decrease. With the same active power disturbance, the rate of change of frequency (RoCoF) and maximum frequency deviation of the system will experience a greater increase than those of traditional power grids dominated by SGs (Heylen et al., 2021). When the RoCoF and frequency deviation reach their thresholds, protection relay devices are triggered, causing large-scale power outages (Delkhosh and Seifi, 2021). Therefore, it is necessary to consider the frequency security issue when studying reserve allocation optimization to ensure sufficient frequency regulation reserves and guarantee

the frequency security of power grids with high-penetration renewable generation.

Based on this background, this study describes a frequency security-constrained optimization approach for allocating multitype reserve capacity in high-penetration renewable energy grids. Strategies and models consisting of synchronous and nonsynchronous units that expand reserve sources are analyzed, and a refined reserve criterion is proposed that considers multidimensional evaluation indices from both operational economy and frequency security perspectives. A bilevel optimization model for reserve capacity allocation on multiple timescales, considering frequency security, was developed. The rationality and effectiveness of the proposed reserve allocation scheme were verified using a practical power grid in Southwest China.

2 Reserve strategy of renewable energy units participating in frequency regulation

Frequency control strategies for multitype flexible resources have been developed in response to the frequency security challenges posed by high-penetration renewable energy grids in the future (Xin et al., 2013). This section primarily focuses on the frequency control strategies for renewable energy units, which are anticipated to constitute the largest proportion of future power grids.

2.1 Wind turbine frequency regulation strategy

When there is a power shortage disturbance, wind turbine (WT) participation in system frequency regulation requires that the WT has a certain reserve available. There are two main schemes for providing frequency regulation reserves via WTs: the proportional curtailment strategy (PCS) and the constant curtailment strategy (CCS) (Karbouj et al., 2019). The primary frequency regulation reserve capacity of the WT utilizing the PCS is adjusted according to the real-time output. Equation 1 shows the curtailment capacity of the WT:

$$RU_w = (1 - \alpha) \cdot P_w^{avail}, \quad (1)$$

where RU_w is the upward reserve capacity of the w -th WT, α is the proportion coefficient of the WT curtailment ($0 < \alpha < 1$), and P_w^{avail} is the maximum generating power.

For the CCS scheme, only when the output power of the WT is greater than the threshold $\beta \cdot P_w^{nom}$ (where β is the reserve startup coefficient of the WT, $0 < \beta < 1$, and P_w^{avail} is the rated capacity of the w -th WT) can the WT provide a frequency regulation reserve for the power grid. Using the CCS method in Equation 2, the frequency regulation reserve of the WT is a fixed value, P_{const} :

$$RU_w = P_{const}. \quad (2)$$

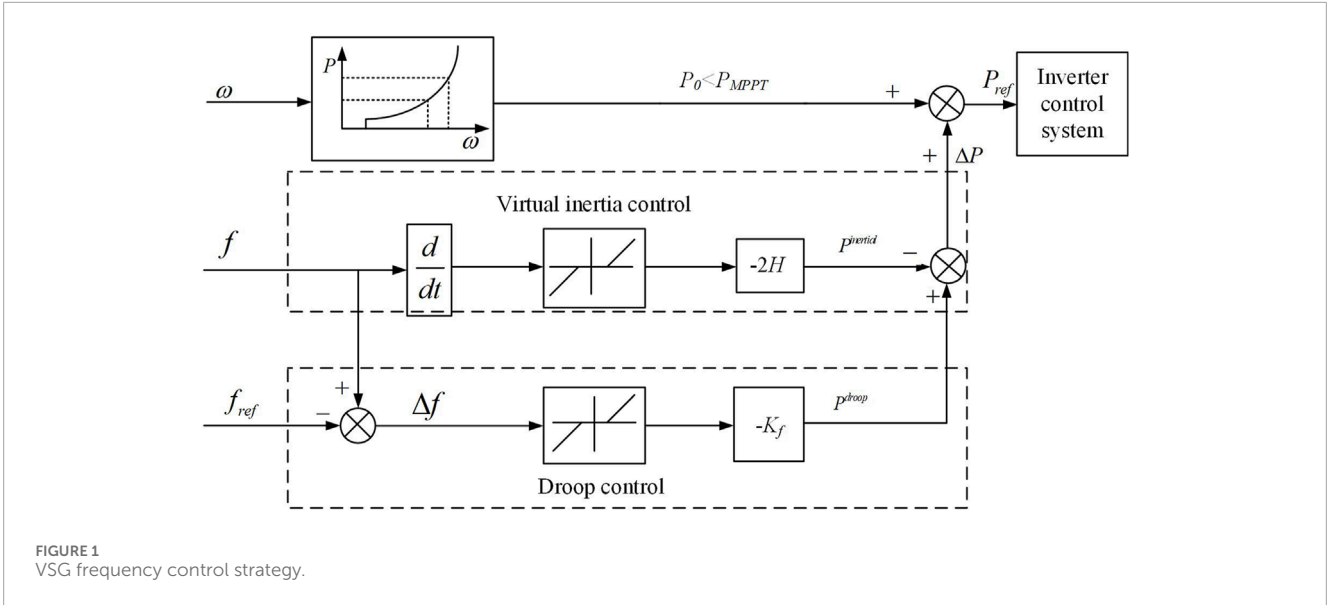


FIGURE 1 VSG frequency control strategy.

The primary frequency regulation control strategy of the WT is similar to that of the SG. A virtual synchronous generation (VSG) control strategy (Ebrahimi et al., 2019) combining virtual inertia support and primary frequency regulation is adopted here. Virtual inertia response can be expressed in terms of a first-order inertia element, and primary frequency regulation can be regarded as a droop control process. A certain proportion of the reserve capacity is reserved for the WT in normal operation conditions, and the WT increases/absorbs active power to the system through the VSG control strategy when a power disturbance occurs in the system. The detailed scheme of the VSG control strategy is shown in Figure 1. With the VSG control strategy, the change in the active power of the WT can be determined by Equation 3:

$$\Delta P = -2H \frac{df}{dt} - K_f \Delta f, \tag{3}$$

where ΔP is the power required for primary frequency regulation of the WT, H is the virtual inertia constant, K_f is the droop coefficient of primary frequency regulation, and Δf is the system frequency deviation.

2.2 Photovoltaic frequency regulation strategy

To maximize the utilization of light energy, photovoltaics (PVs) typically need to provide frequency regulation reserve for the system in combination with battery storage (Rehman et al., 2021). The system frequency deviation is introduced into the battery management module of PV power stations so that the battery has the characteristics of the primary frequency regulation of the SG. Equation 4 shows the power response model:

$$P_m^{droop} = -K_m^{droop} \Delta f, \tag{4}$$

where P_m^{droop} is the discharge power of the m -th battery storage device, and K_m^{droop} is the power regulation coefficient of the m -th battery storage device.

3 Refined reverse criterion considering multidimensional evaluation indices

3.1 Operational economic indices

3.1.1 Total operation cost

The total operational cost of the system includes power generation, reserve, and penalty costs for the curtailment of renewable energy generation. The specific expressions are introduced in detail in Section 4.

3.1.2 Curtailment of WT/PV

The energy utilization efficiency of WTs and PVs can be quantitatively evaluated using the real-time generation penetration rate (Chen et al., 2020) and other indices. In this paper, the system's real-time penetration rate $c_{w,t}, c_{pv,t}$ (Equation 5) and consumption $\eta_{w,t}, \eta_{pv,t}$ (Equation 6) of WTs and PVs are selected as evaluation indices to analyze the applicability of the proposed reserve capacity allocation model.

$$c_{w,t} = \sum_{w \in N_w} \frac{P_{w,t}^{\max} - P_{w,t}}{P_{w,t}^{\max}}, c_{pv,t} = \sum_{pv \in N_{pv}} \frac{P_{pv,t}^{\max} - P_{pv,t}}{P_{pv,t}^{\max}}, \tag{5}$$

$$\eta_{w,t} = \sum_{w \in N_w} \frac{(P_{w,t}^{\max} - P_{w,t})}{P_{w,t}^{\max}}, \eta_{pv,t} = \sum_{pv \in N_{pv}} \frac{(P_{pv,t}^{\max} - P_{pv,t})}{P_{pv,t}^{\max}}, \tag{6}$$

where $P_{w,t}^{\max}$ and $P_{pv,t}^{\max}$ are the predicted power of WT and PV at time t , respectively. $P_{w,t}$ and $P_{pv,t}$ are the actual power output of WT and PV at time t , respectively.

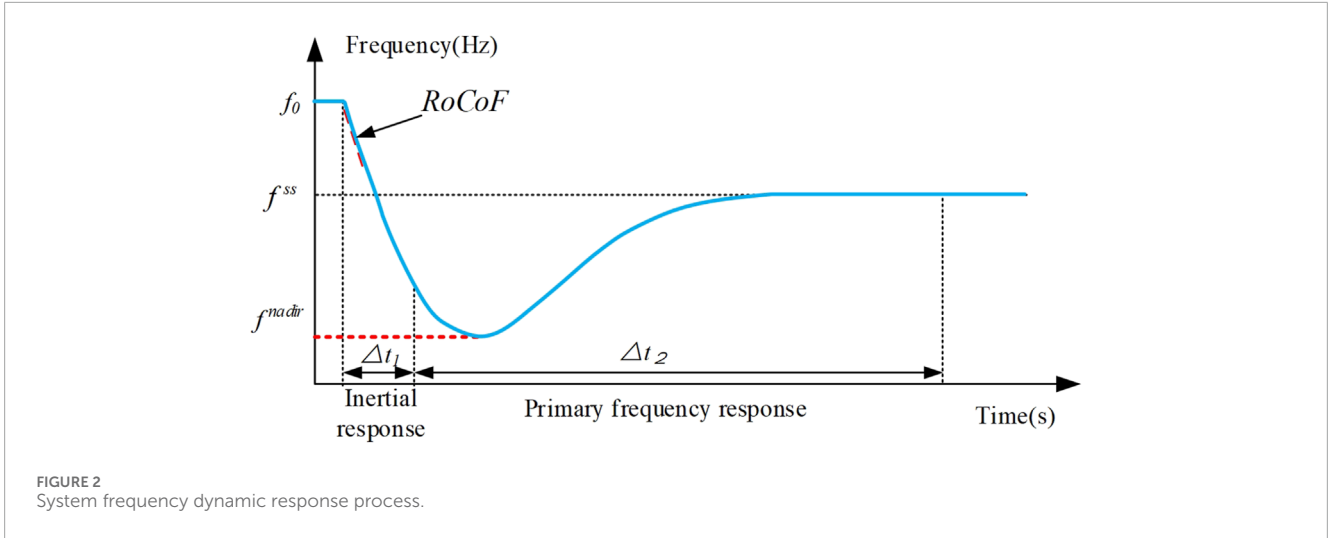


FIGURE 2 System frequency dynamic response process.

3.2 Operational security indices

3.2.1 Inertial level

The inertia level of the system at period t is expressed by the equivalent inertia constant $H_{sys,t}$ of the system (Liu et al., 2021):

$$H_{sys,t} = \frac{E_{sys,t}}{S_{B,sys,t}}, \quad (7)$$

$$E_{sys,t} = \sum_{i \in Ni} P_i^{max} \cdot H_i \cdot u_{i,t} + \sum_{w \in Nw} P_w^{max} \cdot H_w + \sum_{m \in Nm} PD_m^{max} \cdot H_m, \quad (8)$$

$$S_{B,sys,t} = \sum_{i \in Ni} P_i^{max} \cdot u_{i,t} + \sum_{w \in Nw} P_w^{max} + \sum_{pv \in Npv} P_{pv,t}^{max}, \quad (9)$$

where $E_{sys,t}$ (Equation 8) is the total equivalent kinetic energy of the system, and $S_{B,sys,t}$ (Equation 9) is the total startup capacity of the system, both of which are related to the capacity of the SGs participating in frequency regulation and the startup/shutdown status $u_{i,t}$ of the SGs. H_i , H_w , and H_m are the inertia constants of the SGs, WTs, and PV battery storage, respectively.

3.2.2 Multidimensional frequency indices

The dynamic frequency response process of a system with a disturbance is shown in Figure 2. The frequency dynamics can be expressed by Equation 10 using the rotor motion equation of the generator:

$$\frac{2H_{sys}}{f_0} \frac{d\Delta f}{dt} = \frac{\Delta P_m - \Delta P_e}{S_{B,sys}}, \quad (10)$$

where ΔP_m and ΔP_e are the mechanical and electromagnetic power of the generator, respectively, and Δf is the system frequency deviation.

Assuming that the mechanical power input by the generator remains unchanged for a relatively short period after a disturbance, the initial unbalanced power of the system is the disturbance power ΔP . The initial RoCoF can be calculated by Equation 11:

$$RoCoF_0 = \frac{-\Delta P \cdot f_0}{2H_{sys} \cdot S_{B,sys}}. \quad (11)$$

Considering that the power response of the generator governor responds to a power imbalance, the rotor motion equation of the generator can be modified as

$$\frac{2H_{sys}}{f_0} \frac{d\Delta f}{dt} = \frac{v_i^{PFR} \cdot t - \Delta P}{S_{B,sys}}, \quad (12)$$

where v_i^{PFR} denotes the primary frequency response rate of the i -th generator. By integrating both ends of Equation 12 simultaneously, the system frequency deviation in the time domain can be obtained:

$$f(t) = \frac{f_0 \cdot v_i^{PFR}}{4H_{sys}S_{B,sys}} t^2 - \frac{\Delta P \cdot f_0}{2H_{sys}S_{B,sys}} t + f_0 - \Delta f_{db}, \quad (13)$$

where Δf_{db} is the frequency dead band of generator governors.

Using $S_{B,sys}$ as the base power, the frequency regulation parameters of a system comprising multiple units, including renewable energy units, are aggregated. The equivalent inertia parameter for inertia response is presented in Equation 7, and the aggregation of the primary frequency regulation rate parameter in the system frequency deviation model is shown in Equation 14.

$$v^{PFR} = \left(\sum_{i \in Ni} v_i^{PFR} u_{i,t} + \sum_{w \in Nw} v_w^{PFR} + \sum_{pv \in Npv} v_{pv}^{PFR} \right) / S_{B,sys}. \quad (14)$$

Assuming that the primary frequency regulation rate of the generator is constant, it can be seen from Equation 13 that the postfault system frequency deviation $f(t)$ is a quadratic function of time. The frequency nadir will appear at t_{nadir} when $df/dt = 0$. By taking the derivative of both sides of Equation 13 with respect to t , t_{nadir} can be obtained:

$$t_{nadir} = \frac{\Delta P}{v^{PFR}} + \frac{-\Delta f_{db}}{RoCoF_0}. \quad (15)$$

By substituting t_{nadir} into Equation 13, the frequency nadir of the system is

$$f_{nadir} = f_0 - \Delta f_{db} - \frac{f_0 \cdot \Delta P^2}{4H_{sys}S_{B,sys}v^{PFR}}. \quad (16)$$

Combined with Equations 15, 16, the relationship between f_{nadir} and t_{nadir} can be derived as Equation 17:

$$f_{nadir} = f_0 - \Delta f_{db} - \frac{f_0 \cdot \Delta P^2}{4H_{sys} S_{B,sys} \left(\frac{\Delta P}{t_{nadir} + \frac{\Delta f_{db}}{RoCoF_0}} \right)}. \quad (17)$$

The frequency nadir directly determines the actions of the protection relays. Therefore, it is necessary to restrict the system frequency nadir, f_{nadir} , under credible contingencies:

$$f_{nadir} \leq f_{UFLS} \Rightarrow t_{nadir}^{\max} \leq \frac{4H_{sys} S_{B,sys} (f_0 - \Delta f_{db} - f_{UFLS})}{f_0 \cdot \Delta P} + \frac{2H_{sys} S_{B,sys} \Delta f_{db}}{f_0 \cdot \Delta P}, \quad (18)$$

where f_{UFLS} is the threshold of under-frequency load-shedding protection devices. The frequency dynamics are integrated into the reserve model. The constraint of f_{nadir} is transferred to the limitation of t_{nadir} in Equation 18, which means that the frequency regulation of the system should have a sufficient response speed.

Combined with Equation 16, the constraints on the reserve of units participating in primary frequency regulation can be derived as

$$y_i^{up} \leq v_i^{PFR} \cdot t_{nadir}^{\max} = v_i^{PFR} \cdot \left[\frac{4H_{sys} S_{B,sys} (f_0 - \Delta f_{db} - f_{UFLS})}{f_0 \cdot \Delta P} + \frac{2H_{sys} S_{B,sys} \Delta f_{db}}{f_0 \cdot \Delta P} \right], \quad (19)$$

where y_i^{up} represents the upward reserve primary frequency regulation of the i -th unit.

The frequency security limits of the power grid considered in this study are summarized as follows:

1. Maximum RoCoF limit

The RoCoF describes the speed of the system frequency change following a disturbance. To avoid exceeding the threshold $RoCoF^{\max}$, the following constraint is enforced:

$$RoCoF_0 \leq RoCoF^{\max}. \quad (20)$$

2. Frequency nadir limit

To avoid triggering the action of frequency protection relays with power loss/increase disturbance, the frequency nadir of the system should be limited using the upward reserve constraint derived in Equation 19.

3. Quasi-steady frequency limit

The quasi-steady-state frequency deviation Δf_{ss} is related to the system power disturbance, primary frequency regulation rate, and overall primary frequency reserve capacity R^{PFR} and is restricted by

$$|\Delta f_{ss}| = \frac{\Delta P - R^{PFR}}{D \cdot P_{load}} \leq \Delta f_{ss}^{\max}, \quad (21)$$

where D is the load damping constant of the system, and P_{load} is the total load demand.

3.3 Discussion of the proposed frequency security indices

This paper focuses on incorporating the frequency support capability for renewable energy generation units into system frequency

response. However, in addition to renewable energy generation units, energy storage resources such as electrical energy storage and pumped hydro storage can provide rapid frequency support during certain periods. High-voltage direct current (HVDC) is regarded as an ideal resource for frequency support. Hence, this section discusses the applicability of the proposed frequency security indices in incorporating additional flexible resources.

The control strategy for electrical energy storage with converter interfaces participating in frequency response typically employs the VSG strategy, which is consistent with that used for WT. Considering the equivalent frequency response of pumped hydro storage units with turbine-governor dynamics, it aligns with that of hydropower units, and the expression of the latter's frequency response control model is comparable to that of SG (Chen et al., 2022). HVDC can rapidly compensate for power shortages or surpluses within milliseconds through emergency frequency response control strategies with the frequency control model presented in Equation 22, where T_{dci} , T_{Di} are response time constants, and ΔP_{di} is power control amount of the i -th HVDC. Because the time scale of HVDC's emergency frequency response is much shorter than that of other resources (typically in seconds), its response time constant can be neglected (Shi et al., 2022). Thus, HVDC can be treated as the emergency power control amount, as shown in Equation 23. Equation 13 can be transformed into Equation 24 after considering HVDC, which remains computable during the optimization process.

$$\Delta P_{Di} = \frac{\Delta P_{di}}{s} e^{-sT_{dci}} \frac{1}{1 + sT_{Di}}, \quad (22)$$

$$\Delta P_D = \sum_i \Delta P_{di}, \quad (23)$$

$$y_i^{up} \leq v_i^{PFR} \cdot t_{nadir}^{\max} = v_i^{PFR} \cdot \left[\frac{4H_{sys} S_{B,sys} (f_0 - \Delta f_{db} - f_{UFLS})}{f_0 \cdot (\Delta P - \Delta P_D)} + \frac{2H_{sys} S_{B,sys} \Delta f_{db}}{f_0 \cdot (\Delta P - \Delta P_D)} \right]. \quad (24)$$

4 Multiple timescale reserve capacity allocation optimization model

This section describes the bilevel multiple timescale reserve capacity allocation optimization model formulated in this study. The model includes a day-ahead generation schedule and intraday frequency security verification. The timescales of the different levels of the model are shown in Figure 3. Day-ahead scheduling is the first level of the model and uses 1 h as the interval to optimize the startup and shutdown of SGs and the output and reserve of all units. The second level considers the inertial response of the system and primary frequency regulation to cope with credible contingencies. The operating points of each unit determined in the first-level problem are utilized as inputs to the second level to verify the frequency security of the power grid under predefined contingencies.

4.1 Framework of the bilevel optimization model

The first level of the model achieves the economic operation of the system considering system power balance and unit schedule

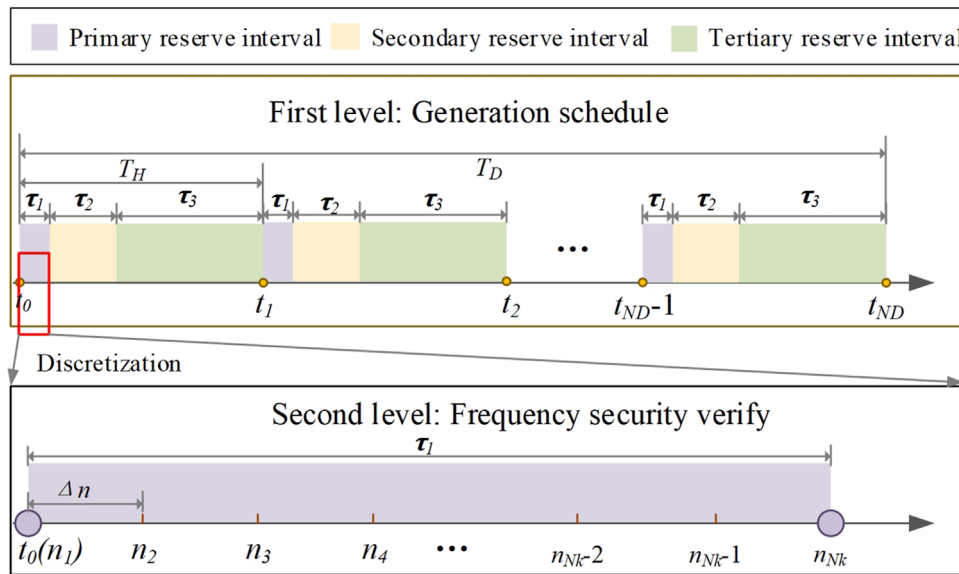


FIGURE 3 Bi-level multi-time scale scheme of the optimization model.

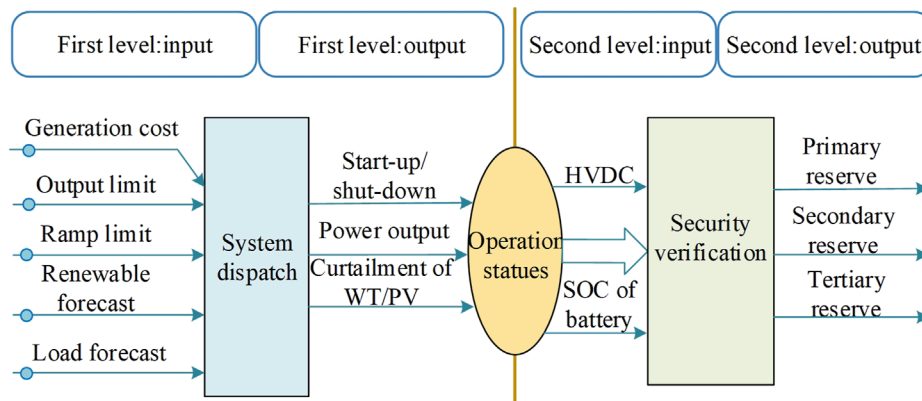


FIGURE 4 Framework of the reserve capacity allocation optimization model.

constraints (Cui et al., 2020). The variables of the first level include the on/off state and power output of each SG unit and renewable curtailment during each dispatch period. The second level uses the operating state and real-time output of all units calculated in the first level as the input. The inertia response and primary frequency regulation of the system are considered, and the primary, secondary, and tertiary reserve capacities of the system are optimized. The framework of the reserve capacity allocation optimization model is shown in Figure 4.

4.2 Reserve allocation optimization model

Considering the power generation costs of SGs and their upward/downward reserve costs, as well as the curtailment

penalty costs of renewable units incurred by setting reserves, the objective of Equation 25 is to minimize the total operating cost within the dispatch period:

$$\min \text{Cost} = \sum_{t \in ND} \sum_{i \in Ni} c_i \cdot u_{i,t} \cdot P_{i,t}^0 + \sum_{t \in ND} \sum_{i \in Ni} cr_i^{up} \cdot u_{i,t} \cdot (P_i^{\max} - P_{i,t}^0) + \sum_{t \in ND} \sum_{w \in Nw} \lambda_w \cdot RU_{w,t}, \tag{25}$$

where ND is the number of time intervals in the dispatch period; N_i and N_w are the number of SGs and WTs, respectively; c_i , cr_i^{up} , and λ_w are the generation cost coefficient of i -th SG, the upward reserve cost coefficient, and the curtailment penalty cost coefficient of the w -th WT, respectively; $P_{i,t}^0$ is the power output of the i -th SG at period t ; P_i^{\max} is the maximum output of the i -th SG; $RU_{w,t}$ is the curtailment

power (upward reserve capacity) of the w -th WT at period t ; and $u_{i,t}$ represents the on/off state of the i -th SG.

4.2.1 Constraints of the generation schedule level

The constraints of the generation scheduling layer include the output of various types of generations, the unit commitment of SGs, and system power balance limitations. The output limits of the generation units are expressed in Equation 26:

$$\begin{cases} u_{i,t} \cdot P_i^{\min} \leq P_{i,t}^0 \leq u_{i,t} \cdot P_i^{\max} \\ 0 \leq P_{w,t}^0 \leq P_{w,t}^{\max} \\ 0 \leq P_{pv,t}^0 \leq P_{pv,t}^{\max} \end{cases} \quad (26)$$

where P_t^0 is the output power of a unit in period t , and the subscripts i , w , and pv represent the SGs, WT, and PV indices, respectively.

The WT must provide some power to participate in the system frequency adjustment. The reserve capacity provided by the w -th WT in period t is denoted by Equation 27:

$$RU_{w,t} = P_{w,t}^{\max} - P_{w,t}^0 \quad (27)$$

Equations 28, 29 determine ramp limits and startup and shutdown times:

$$RG_i^{\text{down}} \leq P_{i,t}^0 - P_{i,t-1}^0 \leq RG_i^{\text{up}}, \quad (28)$$

$$\begin{cases} \sum_{m=0}^{T_i^{\text{on}}-1} u_{i,t+m} \geq T_i^{\text{on}} \cdot (u_{i,t} - u_{i,t-1}), \\ \sum_{m=0}^{T_i^{\text{off}}-1} (1 - u_{i,t+m}) \geq T_i^{\text{off}} \cdot (u_{i,t-1} - u_{i,t}), \end{cases} \quad (29)$$

where RG_i^{down} and RG_i^{up} are the ramp-up/ramp-down limits of the i -th SG, and T_i^{on} , T_i^{off} are the minimum continuous startup/shutdown time of i -th SG.

$$\sum_{i \in Ni} P_{i,t}^0 + \sum_{w \in Nw} P_{w,t}^0 + \sum_{pv \in Npv} P_{pv,t}^0 = \sum_{l \in Nl} P_{l,t} + \sum_{dc \in Ndc} P_{dc,t} \quad (30)$$

Equation 30 limits the power balance of the system. N_l , N_{dc} are, respectively, the number of load and HVDC links, and $P_{l,t}$, $P_{dc,t}$ are the load demand and HVDC power at period t , respectively.

4.2.2 Constraints of the security verification level with infeed power loss disturbance

The second-level model is discretized with a time scale of τ_1 , and the time interval is set to Δn . System frequency security is verified for each time interval.

4.2.2.1 Output constraints

The output constraints can be expressed as Equations 31, 32:

$$P_i^{\min} \cdot u_{i,t} \leq P_{i,t,n} \leq P_i^{\max} \cdot u_{i,t}, \quad (31)$$

$$P_{w,t,n} \leq P_{w,t}^{\max}, \quad (32)$$

where $P_{i,t,n}$ and $P_{w,t,n}$ are the power outputs of the i -th SG and w -th WT after the n -th step of the disturbance occurrence.

The VSG frequency control strategy can be implemented in PV using battery storage, whereas the PV power generation module

still adopts the traditional maximum power point tracking (MPPT) operation strategy, with its actual output equal to the predicted maximum power:

$$P_{pv,t,n} = P_{pv,t}^0 = P_{pv,t}^{\max}, \quad (33)$$

$$PD_m^{\min} \leq PD_{m,t,n} \leq PD_m^{\max}, \quad (34)$$

$$SOC_m^{\min} \leq SOC_{m,t,n} \leq SOC_m^{\max}, \quad (35)$$

where $P_{pv,t,n}$, Equation 33 and PD_m^{\max} and PD_m^{\min} (Equation 34) are the output power of the PV and the maximum and minimum discharging limits of battery storage, respectively; and SOC_m^{\max} and SOC_m^{\min} (Equation 35) are the thresholds for the state of charge of the m -th battery storage.

4.2.2.2 Power distribution and quasi-steady state power balance constraints

The power distribution constraints can be expressed as Equation 36:

$$\Delta P_{t,n} = \Delta P_{t,0} + \sum_{i \in Ni} (P_{i,t,n} - P_{i,t}^0) + \sum_{w \in Nw} (P_{w,t,n} - P_{w,t}^0) + \sum_{m \in Nm} PD_{m,t,n}, \quad (36)$$

where $\Delta P_{t,n}$ is the power loss after the n -th step of the disturbance occurrence.

The quasi-steady-state power balance constraint can be expressed as Equation 37:

$$\begin{aligned} \sum_{i \in Ni} P_{i,t,n_{Nk}} + \sum_{w \in Nw} P_{w,t,n_{Nk}} + \sum_{pv \in Npv} P_{pv,t,n_{Nk}} + \sum_{m \in Nm} PD_{m,t,n_{Nk}} \\ = \sum_{l \in Nl} P_{l,t} + \sum_{dc \in Ndc} P_{dc,t}, \end{aligned} \quad (37)$$

where $P_{i,t,n_{Nk}}$, $P_{w,t,n_{Nk}}$, $P_{pv,t,n_{Nk}}$, and $PD_{m,t,n_{Nk}}$ are the power outputs of the SG, WT, PV, and battery storage under quasi-steady-state conditions.

4.2.2.3 Reserve constraints

The reserve can be divided into primary, secondary, and tertiary reserves based on the frequency recovery process of the system with a predefined disturbance. The overall primary reserve of the system can be expressed as Equation 38:

$$RU_t^{\text{PFR}} = \sum_{i \in Ni} (P_{i,t,n_{Nk}}^k - P_{i,t}^0) + \sum_{w \in Nw} (P_{w,t,n_{Nk}}^k - P_{w,t}^0) + \sum_{m \in Nm} PD_{m,t,n_{Nk}}, \quad (38)$$

where RU_t^{PFR} is the total primary reserve (upward) at period t .

A secondary reserve is used to eliminate frequency deviation and is undertaken by SGs with automatic generation control (AGC) systems. Considering the timescale of secondary frequency regulation in the system (5 min), the secondary reserve constraint is formulated as Equation 39:

$$RU_t^{\text{SFR}} \leq \sum_{i \in Ni} 10v_{i,t}^{\text{SFR}} \cdot u_{i,t}, \quad (39)$$

where RU_t^{SFR} is the total secondary reserve (upward) at period t and v_i^{SFR} is the secondary reserve response rate of i -th SG.

To ensure the frequency security of the system, the power grid must reserve sufficient primary and secondary reserve capacity to

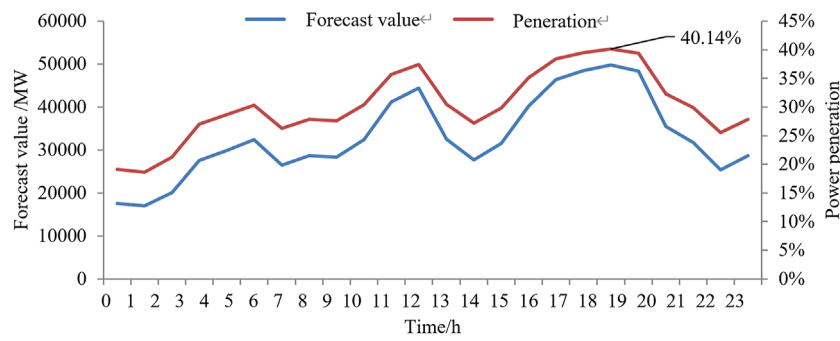


FIGURE 5 Forecast power of renewable energy generation.

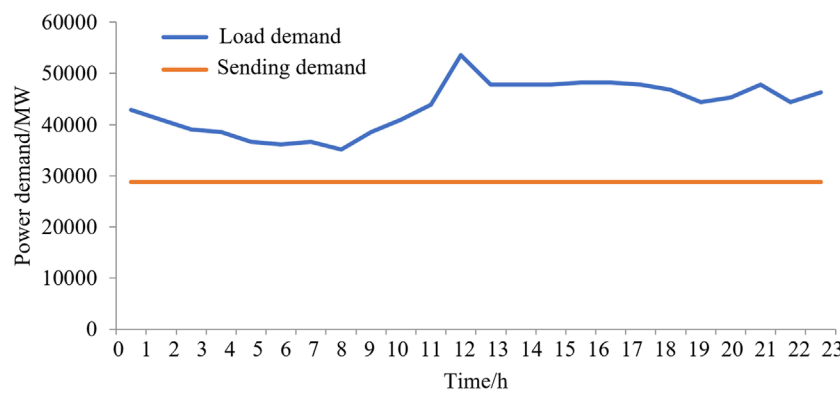


FIGURE 6 Load demand of the test system.

TABLE 1 Total operating cost of the system.

Scenario	Generation cost (10 ² CNY)	Reserve cost (10 ² CNY)	Curtailment (10 ² MW)/cost (CNY)	Total cost (10 ² CNY)
1	899,987.9	46,062.3	1,481/2,132.7	948,182.9
2	862,706.1	47,839.6	0/0	910,545.0
3	1,000,434	41,377.7	4,364/7,754.3	1,082,128.0

return the system frequency to a reasonable range, with the relevant constraints as Equation 40:

$$RU_t^{PFR} + RU_t^{SFR} \geq \Delta P_{t,0}. \tag{40}$$

Tertiary reserves can be provided by SGs with upward regulation space. When a disturbance occurs, the primary and secondary reserves respond first. To ensure that the system has a sufficient response rate to cope with the next disturbance, it is necessary to replace primary and secondary reserves with tertiary reserves after the frequency is restored. The total tertiary reserve of the system can be described as Equation 41:

$$RU_t^{TFR} = \sum_{i \in Ni} (P_{i,t}^{\max} - P_{i,t}^0), \tag{41}$$

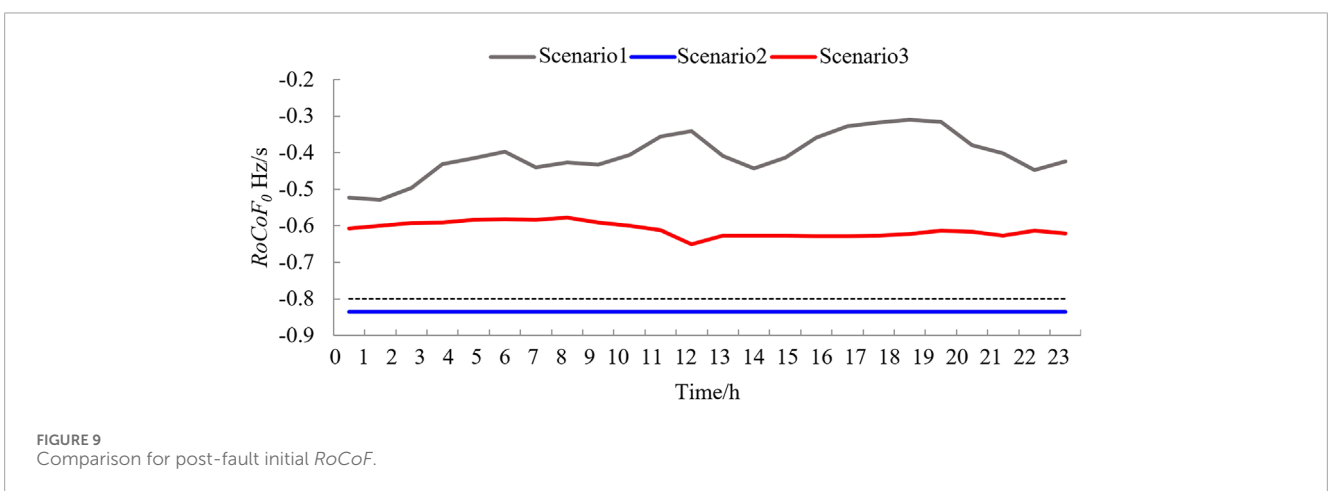
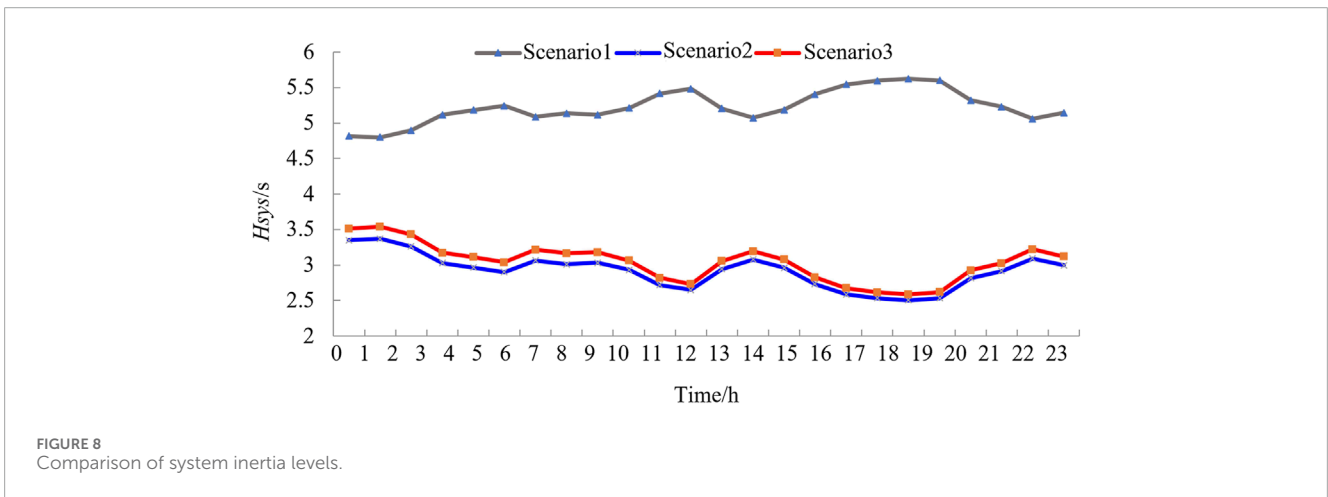
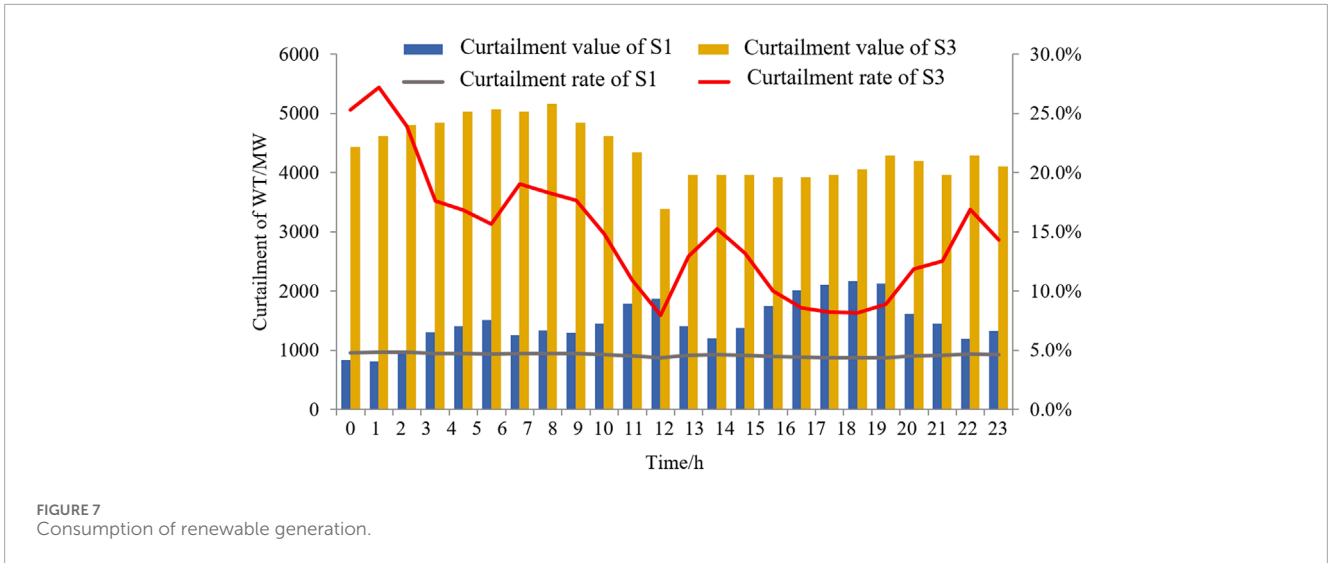
where RU_t^{TFR} is the total tertiary reserve of the system at period t .

In addition, constraints on the system inertia level (Equations 7–9) and multidimensional frequency security limit constraints (Equations 19–21) should be embedded in the model.

5 Case study

5.1 Input data and scenario setting

The effectiveness of the proposed approach was verified and applied to a provincial power grid located in Southwest China. The installed capacity of the SGs in the system was 143,396 MW, and the installed capacity of the renewable energy generators was



91,000 MW (including 71,000 MW for WTs and 22,000 MW for PVs). The forecast data for renewable energy generation in the future operation scenarios are shown in Figure 5. Renewable energy generation is forecast at a high proportion, and the penetration rates of renewable generation at hours 5, 9–12, and 15–20 are higher

than 30%. Figure 6 shows the hourly load demand. The system must transmit a large amount of electricity to the external power grid through DC lines, with a total of six feed-out HVDC lines. The power demand for external transmission is 28,800 MW and represents more than 40% of the total power generation. The inertia constant

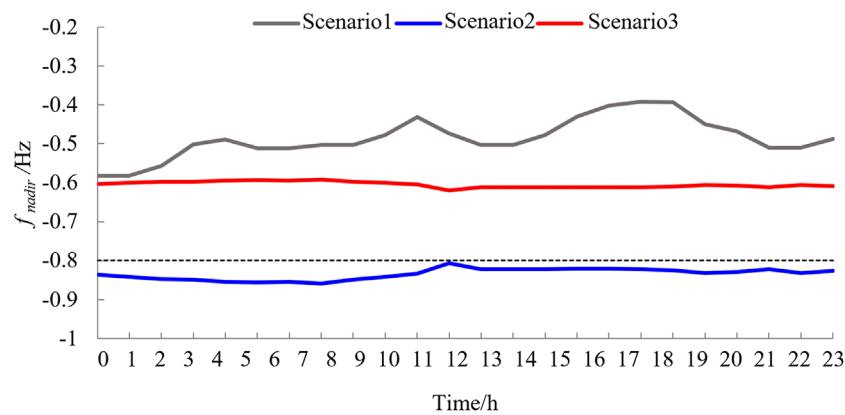


FIGURE 10
Comparison for postfault frequency nadir.

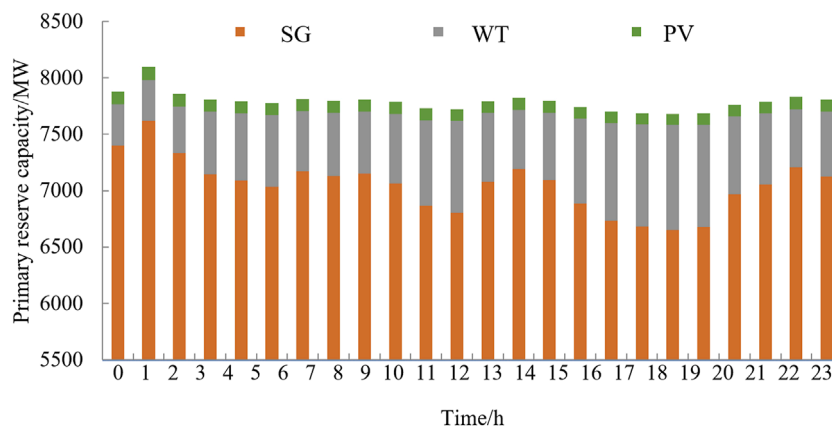


FIGURE 11
Primary reserve allocation in Scenario 1.

of the WT was set as 8 s, and the primary frequency regulation coefficients of the WT and battery storage systems were set to 10. The discharge efficiency of battery storage was $\eta_m^D = 0.95$, and the threshold values of $RoCoF_0$ and f_{nadir} were set at 0.8 Hz/s and 0.8 Hz, respectively. The primary frequency regulation deadband was ± 0.05 Hz. The time scale for the second layer of the reserve optimization model was 20 s, and the power disturbance was set to a power loss of 8000 MW. The upward reserve optimization scheme during the dispatch period was programmed and calculated using the GAMS platform. Three scenarios are set to verify the effectiveness of the proposed reserve allocation optimization model. Among them, Scenario 1 is the proposed reserve capacity allocation model, considering that both SGs and renewable energy generation can provide reserve and frequency support strategies, and the system frequency security indices (Equations 11, 19) are taken into account. Scenario 2 is the traditional reserve distribution scheme that does not consider frequency security constraints, and only SGs can provide a reserve. Scenario 3 further considers the system frequency security indices based on Scenario 2, but only SGs can participate in the system frequency regulation process. The scenario settings are as follows:

Scenario 1: Proposed reserve allocation optimization model considering multitype reserves and system frequency security limits.

Scenario 2: Traditional reserve allocation scheme without considering renewable energy reserves and system frequency security limits.

Scenario 3: Traditional reserve allocation scheme enforcing system frequency security constraints. The frequency support of the renewable energy units was neglected.

5.2 Change of multidimensional evaluation indices

5.2.1 Total operating cost of the system

Table 1 presents the economics of the different scenarios from multiple perspectives, including the generation cost, reserve cost, wind curtailment, and total operating cost. The curtailment provided in the table is the average wind curtailment (MW). The total operating and generation costs of the system in Scenario 2 are the lowest of the three scenarios because Scenario 2 does not consider the WT to provide frequency support,

and system frequency security constraints are not enforced. For Scenario 3, because only SGs ensure system frequency security under predefined disturbances, more WT output is curtailed to maintain a higher SG online capacity; therefore, the curtailment penalty cost is significantly higher than that of Scenario 1.

5.2.2 Consumption of renewable energy

Owing to the utilization of the MPPT operation strategy and participation in frequency regulation through battery storage of PVs, there was no PV curtailment in the three scenarios. The wind curtailment in the power grids of Scenarios 1 and 3 during the dispatch period is shown in Figure 7. In Scenario 1, the wind curtailment rate of the system was maintained below 5%, and the average wind curtailment rate during the entire dispatch period was 4.57%. In Scenario 3, the wind curtailment rate of the system at hour 1 was 27.2%, and the wind curtailment amount was 4615 MW. During the entire dispatch period, the average wind curtailment rate was 13.45%, and more wind-power generation was curtailed.

5.2.3 System inertia

Figure 8 compares the inertia levels in the three scenarios. It can be seen that the proposed optimization model considers the virtual inertia support of renewable energy. Hence, the fluctuation in the system equivalent inertia level in Scenario 1 was smaller and could be maintained at a high level (approximately 5.23 s). Owing to the single source (only SGs) of inertia in Scenarios 2 and 3, the system inertia level was not significantly improved even when the wind curtailment rate reached 13.45%, and the low-inertia risk was noticeable.

5.2.4 Multidimensional frequency security indices

Figure 9 compares the postfault initial RoCoF during the scheduling period of the three scenarios. Scenario 1 had a smaller RoCoF than the traditional reserve optimization methods (Scenarios 2 and 3). Because frequency security is not considered in Scenario 2, the frequency change rate exceeds the threshold, and system frequency security cannot be guaranteed. A comparison of the frequency nadir for the three scenarios is shown in Figure 10. Similar to the frequency change rate index, the proposed reserve optimization method (Scenario 1) had a smaller frequency nadir with the same disturbance as the other traditional methods (Scenarios 2 and 3). The frequency nadir in Scenario 2 exceeded the threshold.

5.3 Reserve capacity allocation result

5.3.1 Primary reserve

Figure 11 shows the detailed allocation optimization results of the primary reserve capacity in Scenario 1. The primary frequency regulation of the system is dominated by SGs, supplemented by WT and PV battery storage. According to the primary reserve Equation 39, the primary frequency regulation reserve capacity of the system is related to the disturbance. Therefore, the primary frequency regulation reserve in Scenario 1 is nearly equal to the initial system disturbance.

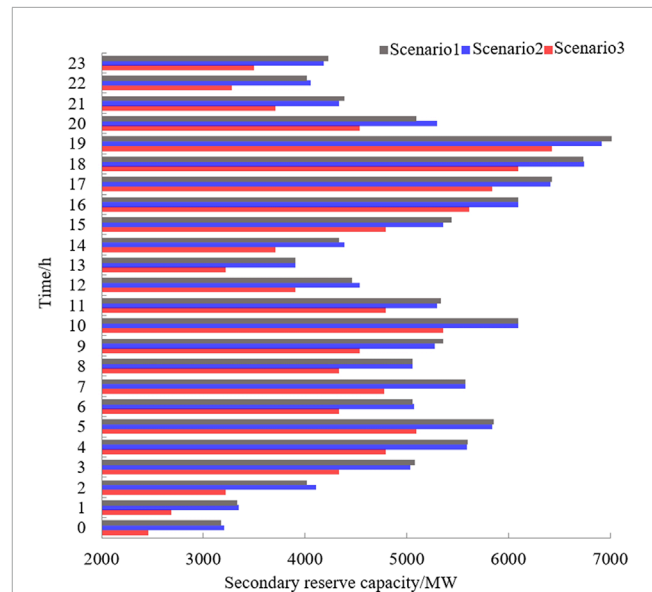


FIGURE 12 Secondary reserve allocation in three scenarios.

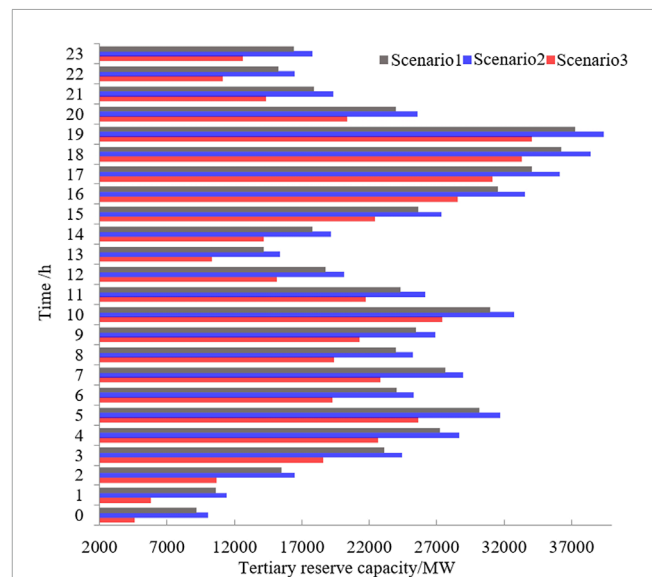


FIGURE 13 Tertiary reserve allocation in the three scenarios.

5.3.2 Secondary reserve and tertiary reserve

Figure 12 shows the configuration results of the secondary reserve capacity for the three scenarios. The upward adjustment space for the secondary reserve capacity of the system fluctuated significantly in all three scenarios. Because of the significant wind curtailment in Scenario 3, the upward adjustment space of the SGs was compressed, and the secondary reserve capacity in Scenario 3 was relatively small. The tertiary reserve capacity of the system during the dispatch period is shown in Figure 13. In Scenario 1, because of the upward reserve reservation for the WT, the SGs support more load demand than in the traditional scheme, and the total tertiary reserve capacity of the system in Scenario 1 is smaller than that in Scenario 2 without wind curtailment measures. Similar to the secondary reserve, the tertiary

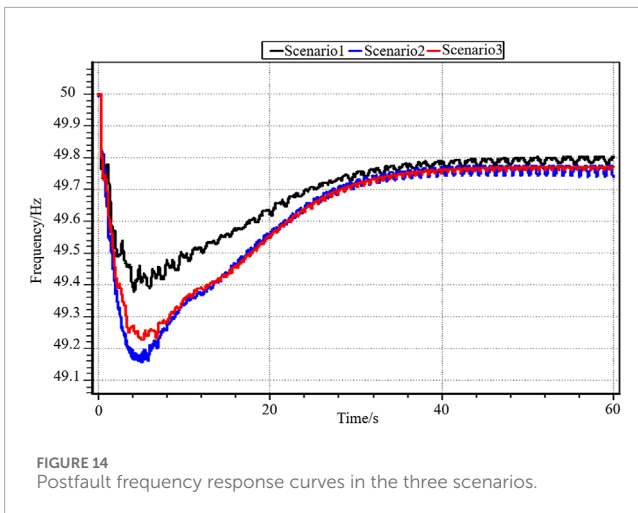


FIGURE 14 Postfault frequency response curves in the three scenarios.

TABLE 2 Comparison of optimization and simulation results.

Disturbance	Solution method	f_{nadir} (Hz)	$RoCoF_0$ (Hz/s)
Power loss	BPA simulation	49.38	-0.38
	GAMS	49.52	-0.34
	Error	0.14	0.04
Power increase	BPA simulation	50.57	0.55
	GAMS	50.57	0.53
	Error	0	0.02

reserve adjustment space for the SGs in Scenario 3, where there is a large amount of wind curtailment, is also compressed. Thus, the total tertiary reserve of Scenario 3 was significantly lower than that of Scenario 2, which had no wind curtailment, and lower than that of Scenario 1, which had only a small amount of wind curtailment.

5.4 Accuracy evaluation of frequency indices

This section simulates and calculates the frequency indices of all reserve scenarios for the test system with 8000 MW power loss using PSD-BPA software. The postfault frequency response curves at 9 h for the three scenarios are shown in Figure 14. In Scenario 1, the frequency nadir is 0.62 Hz ($f_{nadir} = 49.38\text{Hz}$), and the quasi-steady-state frequency is 49.80 Hz. In the traditional reserve Scenario 2, the maximum frequency deviation is 0.85 Hz ($f_{nadir} = 49.15\text{Hz}$), and the quasi-steady-state frequency is 49.76 Hz. In Scenario 3, the maximum frequency deviation is 0.77 Hz ($f_{nadir} = 49.23\text{Hz}$), and the quasi-steady state frequency is 49.75 Hz. To illustrate the applicability of the proposed reserve allocation optimization model, we compared the optimization solution results for the frequency indices of Scenario 1 in GAMS with the simulation results from PSD-BPA. The results are shown in Table 2, where the frequency nadir of the BPA simulation was the highest among all buses. f_{nadir} and $RoCoF_0$ were

similar for the two platforms, indicating that the frequency security indices obtained using the proposed reserve allocation optimization model were highly accurate.

6 Conclusion

This study proposes a reserve capacity allocation optimization approach for high-penetration renewable energy power grids that integrates multiple reserve sources to ensure system frequency security. A reserve criterion based on multidimensional evaluation indices for operational economy and frequency security was constructed. In addition, a bilevel optimization model for reserve capacity allocation that considers frequency security is proposed. Case studies on a practical power grid show that compared with traditional reserve schemes, the proposed method can achieve an optimized reserve capacity distribution with higher economic efficiency and frequency security. Moreover, compared to the PSD-BPA simulation, the calculation deviations for the frequency security indices of the optimization model were within acceptable ranges.

Data availability statement

The original contributions presented in the study are included in the article/supplementary material; further inquiries can be directed to the corresponding author.

Author contributions

FL: formal analysis, project administration, and writing—original draft. YS: investigation, resources, and writing—review and editing. YL: software, validation, and writing—review and editing. DC: data curation, funding acquisition, and writing—original draft. WC: supervision, visualization, and writing—review and editing. LK: conceptualization, methodology, and writing—original draft.

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Conflict of interest

Authors FL, YS, YL and WC were employed by State Grid Sichuan Electric Power Company. The remaining authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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