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# Two-stage distributionally robust optimization operation of virtual power plant considering the virtual energy storage of electric vehicles

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Virtual Power Plant (VPP) is a key to aggregate various distributed energy sources. With the vigorous rise of various distributed energy sources, the direct access of large-scale electric vehicle load will increase the complexity of VPP coordinated operation. Hence, this paper proposes a VPP optimization method for Electric Vehicle Virtual Energy Storage (EV-VES). Firstly, the travel characteristics of electric vehicles are analyzed, and EV-VES model is established to coordinate and manage the charge-discharge behavior of EV. Secondly, the "carbon charge rate" model of energy storage (ES) is introduced to establish the relationship between carbon emission and electricity price, and the VPP operation model considering the "carbon charge rate" of energy storage is established. Finally, the two-stage robust optimization operation model of VPP is constructed, Wasserstein distance is used to describe the confidence set of uncertain probability distribution of wind power generation and load, and the uncertainty of system source and load are described by the confidence set. The Column and Constraint Generation (C&CG) algorithm was used to determine the optimal operational benefit solution. The effectiveness of the proposed VPP optimal operation model was validated through case study.

## KEYWORDS

electric vehicles, carbon charge rate, wasserstein distance, two-stage robust, C&CG

## 1 Introduction

The problem of energy crisis and global warming is becoming more and more obvious, which has aroused people's wide attention. Virtual power plant uses advanced communication technology and control theory to aggregate massive distributed resources and coordinate scheduling to realize effective allocation of internal resources (Zhang et al., 2023). Electric Vehicles (EVs) have developed rapidly in recent years and have played a significant role as an important way to alleviate energy shortages (Guo et al., 2022; Zhang, 2022a).

With the development of EV network access technology, its aggregation as flexible virtual energy storage has broad application prospects. Existing literature has studied

the effects of EV renewable energy consumption (Zhang, 2022b), wind and landscape fluctuation reduction, and peak cutting and valley filling (Wang et al., 2024) from the aspects of EV flexible regulation potential (Kaile et al., 2020), orderly charge and discharge control strategy (Yao et al., 2022), and temporal and spatial distribution. In terms of EV modeling, similar EVs or charging piles are regarded as an aggregate by fuzzy C-means (Li et al., 2022) or self-organizing mapping neural network (Sun et al., 2021) according to EV charging time and other characteristics. Above literature have a fixed probability distribution in EV modeling, which is a simple aggregation of numerical relations. While the generalized load of electric vehicles with the dual attributes of power generation and electricity consumption can realize the increase or decrease of energy demand in a certain period of time to a certain extent, which is similar to physical energy storage, so it can be modeled as virtual energy storage.

In the VPP optimization scheduling problem, the wind-driven force is usually a non-linear optimization problem. The existing methods to deal with uncertainty mainly focus on stochastic optimization and robust optimization. Literature (Sui et al., 2020) improves the existing robust optimization method by finiting discretization of the uncertain domain, generates the uncertain domain boundary with echelon deviation, and expands the “bad scenario set.” Literature (Xu et al., 2022; Qi et al., 2023) uses the two-stage robust optimization theory to construct the uncertainty set of wind power and load, and seeks the optimal solution of system optimization operation under the worst scenario. The stochastic programming method builds several typical scenarios based on historical data and the probability distribution function of un-certain factors to analyze the randomness of load and renewable energy (U. Akram et al., 2021; Li et al., 2019). However, stochastic optimization requires accurate probability distribution function, which makes stochastic optimization lack robustness, and the robust optimization value considers the optimal solution of the uncertain set in the worst case, and the result is too conservative. Literature (Liu et al., 2020) uses the 1 norm and  $\infty$  norm constraints in the maximum scheduling to restrict the confidence interval. Compared with the above two methods, the distributionally robust optimization (Yang et al., 2021; Yang et al., 2022) does not require a completely accurate distribution function and has stronger robustness. At the same time, it makes up for the shortcoming that the result of robust optimization is too conservative because the probability distribution is not considered.

In summary, the current research on optimal scheduling of VPPs only considers electric-hydrogen energy storage, without considering the ES capacity of flexible load and the carbon emission model of energy storage equipment. Therefore, this paper proposes a two-stage robust optimal operation model considering EV-VES and the “carbon charge rate” of energy storage. The proposed method has several advantages.

- (1) The research in this paper breaks through the limitations of the existing virtual power plant optimal scheduling and fills in the field other than the consideration of electric-hydrogen energy storage. Through in-depth analysis of the travel characteristics of electric vehicles, an innovative EV-VES power model is

established, which not only improves the flexibility of virtual power plant scheduling, but also enhances its ability of peak cutting and valley filling.

- (2) The concept of “carbon charge rate” is proposed, which closely combines carbon emission with energy storage system, and provides a new perspective for constructing the relationship between carbon emission and trading price.
- (3) A two-stage robust optimal operation model is proposed, which uses Wasserstein distance to describe the uncertainty of wind power generation and load demand, and effectively describes the uncertain probability distribution set of the source load of the system.

## 2 EV-VES model

By statistical analysis of the historical data of EV, the distribution function of parking time, driving distance and parking time of electric vehicles can be obtained (Chen et al., 2024). The charging time, discharging time and remaining capacity of the EVs when they arrive at the station can be expressed as Equations 1–3:

$$\begin{cases} \Delta E^{k,k+1} = E^{k+1} - E^k \\ \Delta E^{k,k+1} = \omega_{ev} L_s^{k,k+1} \end{cases} \quad (1)$$

$$\begin{cases} S_{ev}^{n,k+1} = S_{EV}^{n,k} - \frac{\Delta E^{k,k+1}}{E_{rate}} \\ S_{need}^{n,k} = \frac{E_{min} + \Delta E^{k,k+1}}{E_{rate}} \end{cases} \quad (2)$$

$$\begin{cases} T_{cha}^{n,k} = (S_{need}^{n,k} - S_{ev}^{n,k}) \cdot E_{rate} / (\eta_c \cdot P_{evc}^{n,t}), \\ S_{need}^{n,k+1} \geq S_{ev}^{n,k+1} \\ T_{dis}^{n,k} = (S_{ev}^{n,k} - S_{need}^{n,k}) \cdot E_{rate} / (\eta_d \cdot P_{evd}^{n,t}), \\ S_{ev}^{n,k} \geq S_{need}^{n,k} \end{cases} \quad (3)$$

where,  $E^k$  and  $E^{k+1}$  are the remaining capacity of the EV at different stations,  $S_{ev}^{n,k+1}$  is the SOC state of the  $n$  EV when it arrives at station  $k + 1$ ,  $S_{ev}^{n,k}$  is the SOC state of the  $n$  EV when it leaves station  $k + 1$ , and  $S_{need}^{n,k}$  is the SOC state required of the  $n$  EV when it leaves station  $k + 1$ .  $L_s^{k,k+1}$  is the driving distance of the EV after leaving station  $k$ ,  $\omega_{ev}$  is the energy consumption per kilometer of the EV, and  $E_{rate}$  is the rated capacity of the EV.  $\Delta E^{k,k+1}$  is the electricity required by the EV from station  $k$  to station  $k + 1$ ,  $T_{cha}^{n,k}$  and  $T_{dis}^{n,k}$  are the charging time and discharging time of the EV  $n$  at station  $k$ ,  $E_{min}$  is the minimum battery power of the EV,  $\eta_c$  and  $\eta_d$  are the charge-discharge efficiency of the EV,  $P_{evc}^{n,t}$  and  $P_{evd}^{n,t}$  are charge-discharge power of the EV.

Considering the factors discussed above, the feasible range of electric power for a single electric vehicle under the limit condition is established as Equation 4:

$$\begin{cases} E_{n,k+1,t,max}^{ev} = \min \{ E_{n,k,t}^{ev} + P_{n,max}^{evc} (t - T_{cha}^{n,k}), E_{max} \} \\ E_{n,k+1,t,min}^{ev} = \max \{ E_{n,k,t}^{ev} - P_{n,max}^{evd} (t - T_{dis}^{n,k}), E_{min} \} \end{cases} \quad (4)$$

where,  $E_{n,k+1,t,max}^{ev}$  and  $E_{n,k+1,t,min}^{ev}$  are the maximum and minimum limits of EV  $n$  at station  $k + 1$  during  $t$ ,  $E_{n,k,t}^{ev}$  is the power of EV  $n$  at station  $k$  during  $t$ ,  $E_{max}$  and  $E_{min}$  are the battery power limits of EV,

$P_{n,max}^{evc}$  and  $P_{n,max}^{evd}$  are the maximum charge-discharge power of EV,  $T_{cha}^{n,k}$  and  $T_{dis}^{n,k}$  are the total charge and discharge time respectively.

Thus, the upper and lower limits of the power of electric vehicles in the limit condition are obtained, as Equation 5:

$$\begin{cases} P_{n,k,t}^{ev,max} = \min \{ E_{n,k+1,t,max}^{ev} - E_{n,k,t,min}^{ev}, P_{n,max}^{evc} \} \\ P_{n,k,t}^{ev,min} = \max \{ E_{n,k+1,t,min}^{ev} - E_{n,k,t,max}^{ev}, P_{n,max}^{evd} \} \end{cases} \quad (5)$$

where,  $P_{n,k,t}^{ev,max}$  and  $P_{n,k,t}^{ev,min}$  pertain to the maximum and minimum bounds of the power of the lower EV.

Aggregating electric vehicles into VES, the energy boundary is as Equation 6:

$$\begin{cases} E_{t,p}^{ev} = \sum_n \sum_k E_{n,k,t,p}^{ev} \\ P_{t,p}^{ev} = \sum_n \sum_k P_{n,k,t,p}^{ev} \end{cases} \quad (6)$$

where,  $p$  is max or min indicates the maximum and minimum limits respectively. The capacity  $E$  and power  $P$  of virtual energy in each time period must adhere to the constraints of upper and lower limits.

### 3 Virtual power plant operation model considering "carbon charge rate" of energy storage

#### 3.1 Energy storage "carbon charge rate" model

After integrating the energy storage device, since it functions as a unique electrical load during charging, it will absorb part of the carbon emissions while charging, and it is considered to be a special power generation device when the energy storage is discharged. Therefore, carbon emissions will not be conserved in real time when extending the translation of energy storage at the energy level to the translation of carbon emissions level, but in a scheduling cycle. Energy storage "carbon charge rate" model is established as Equations 7–10.

$$c_t^{es,cha} = P_t^{es,cha} \rho_t^{es,cha} \quad (7)$$

where,  $es$  represents the collection of virtual energy storage and batteries;  $c_t^{es,cha}$  is the carbon emission of  $es$  charged during  $t$ ;  $P_t^{es,cha}$  is the charging power of  $es$  stored during  $t$ ;  $\rho_t^{es,cha}$  is the carbon emission density of  $es$  charged during  $t$ ; In this case, energy storage is used as the load model.

$$c_t^{es,dis} = P_t^{es,dis} \rho_t^{es,dis} = \frac{P_t^{es,dis}}{\eta_d} \rho_{t-1}^{es} \quad (8)$$

where,  $c_t^{es,dis}$  is the carbon emissions charged into the energy storage  $es$  during  $t$ ,  $P_t^{es,dis}$  is the discharge power of  $es$  during  $t$ ,  $\rho_t^{es,dis}$  is the carbon emission density of  $es$  during  $t$ , and  $\rho_{t-1}^{es}$  is the carbon charge rate of  $es$  during  $t - 1$ . In this case, the energy storage is used as a power generation model.

$$\rho_t^{es} = \frac{\rho_{t-1}^{es} S_{t-1}^{es} E_{es} + c_t^{cha} - c_t^{dis}}{S_t^{es}} \quad (9)$$

where,  $S_t^{es}$  is the charged state of  $es$  stored during  $t$ ;  $E_{es}$  is the capacity of  $es$  stored;  $c_t^{cha}$  and  $c_t^{dis}$  are the charging and discharging carbon emissions respectively.

$$\lambda_t^E = \lambda_t^{E0} + \left( \pi P_t^C + \kappa_1 \sum_i^{es} \rho_t^{i,dis} - \kappa_2 \sum_i^{es} \rho_t^{i,cha} \right) \quad (10)$$

where,  $\lambda_t^E$  is the actual price of electricity,  $\lambda_t^{E0}$  is the initial price of electricity,  $\kappa_1$  and  $\kappa_2$  are the carbon tax for carbon emissions of ES,  $\pi$  is the carbon emissions of traditional power generation units, and  $P_t^C$  is the traditional power.

#### 3.2 Virtual power plant operation model

VPPs aim to minimize operating costs, as Equation 11, VPP operation constraints are shown in Equations 12–16:

$$\begin{aligned} \min \sum_{t \in T} \lambda_t^E (P_t^{buy} - P_t^{sell}) - c_t u_t^C - c_v P_t^C \\ - c_{ev} P_t^{ev} - c_w \cdot (P_t^{WA} - P_t^W) \end{aligned} \quad (11)$$

where,  $P_t^{buy}$  and  $P_t^{sell}$  are the purchased and sold power of VPP in the energy market respectively,  $u_t^C$  is the variable of traditional power generation state, and  $P_t^{ev}$  is the virtual energy storage power;  $P_t^W$  is wind power;  $P_t^{WA}$  is wind power cap;  $c_t$  and  $c_v$  represent the fixed cost and generation cost of traditional power plants respectively,  $c_{ev}$  represents the cost of virtual storage, and  $c_w$  represents the cost of curtailment.

##### 3.2.1 Power balance constraints

$$P_t^W + P_t^C - P_t^{ev} + P_t^{SD} - P_t^{SC} + P_t^{evd} - P_t^{evc} - P_t^E - P_t^L = 0 \quad (12)$$

where,  $P_t^C$  is the power generation of traditional power plants;  $P_t^E$  is the transaction power;  $P_t^L$  is the demand load;  $P_t^{SC}$  and  $P_t^{SD}$  are the charge-discharge power.  $P_t^{evc}$  and  $P_t^{evd}$  are the charge-discharge power of EV.

##### 3.2.2 Energy market trading constraints

$$-P_{max}^E \leq P_t^E \leq P_{max}^E \quad (13)$$

where,  $P_{max}^E$  indicates the limit of the trading power; when  $P_t^E < 0$ , it indicates that VPP purchases power; when  $P_t^E > 0$ , it is *vice versa*.

##### 3.2.3 Constraints on battery charging and discharging

$$\begin{cases} u_t^{SC} P_{min}^{SC} \leq P_t^{SC} \leq u_t^{SC} P_{max}^{SC} \\ u_t^{SC} + u_t^{SD} \leq 1 \\ S_t = S_{t-1} + \eta^{SC} P_t^{SC} - \eta^{SD} P_t^{SD} \\ S_{min} \leq S_t \leq S_{max} \end{cases} \quad (14)$$

where,  $P_{min}^{SC}$  and  $P_{max}^{SC}$  represent the limits of the battery charging power,  $u_t^{SC}$  and  $u_t^{SD}$  represent the charge-discharge state variables,  $S_t$  indicates the remaining battery power,  $S_{min}$  and  $S_{max}$  indicate

the limits of battery power,  $\eta^{SC}$  and  $\eta^{SD}$  indicate the charging and discharging efficiency.

### 3.2.4 Operation constraints of traditional power plants

$$\begin{cases} P_{\min}^C u_t^C \leq P_t^C \leq P_{\max}^C u_t^C \\ P_t^C - P_{t-1}^C \leq R_u^C u_{t-1}^C \\ P_{t-1}^C - P_t^C \leq R_d^C u_{t-1}^C \end{cases} \quad (15)$$

where,  $P_t^C$  is the power generation of traditional power plants;  $P_{\min}^C$  and  $P_{\max}^C$  represent the limits of power generation of traditional power plants;  $R_u^C$  and  $R_d^C$  respectively represent the ascending and descending power of traditional power plants;  $u_t^C$  represents the variable of the generation state of the traditional power plant. When  $u_t^C = 1$ , the traditional generator set generates electricity, and when  $u_t^C = 0$ , the traditional generator set stops.

### 3.2.5 Electric vehicle virtual energy storage constraints

$$\begin{cases} E_{t,\min}^{ev} \leq E_t^{ev} \leq E_{t,\max}^{ev} \\ P_{t,\min}^{ev} \leq P_t^{ev} \leq P_{t,\max}^{ev} \\ u_{n,t}^{evc} P_{n,\min}^{evc} \leq P_{n,t}^{evc} \leq u_{n,t}^{evc} P_{n,\max}^{evc} \\ u_{n,t}^{evd} P_{n,\min}^{evd} \leq P_{n,t}^{evd} \leq u_{n,t}^{evd} P_{n,\max}^{evd} \\ u_{n,t}^{evc} + u_{n,t}^{evd} \leq 1 \end{cases} \quad (16)$$

where,  $E_{t,\min}^{ev}$  and  $E_{t,\max}^{ev}$  represent the limits of virtual energy storage capacity of electric vehicles respectively;  $P_{n,\max}^{evc}$  and  $P_{n,\max}^{evd}$  are the maximum charge-discharge power of EV;  $P_{n,\min}^{evc}$  and  $P_{n,\min}^{evd}$  are the minimum charge-discharge power of EV;  $P_{t,\min}^{ev}$  and  $P_{t,\max}^{ev}$  represent the limits of VES power of EVs;  $u_{n,t}^{evc}$  and  $u_{n,t}^{evd}$  are respectively electric vehicle charging and discharging state variables.

## 4 Two-stage distributionally robust optimization operation model for virtual power plant

### 4.1 Model transformation

The deterministic optimization model (11) is changed to the two-stage distributionally robust optimization model (17). In the first stage, the internal unit combination problem of VPP is solved, and in the second stage, the operation result of the maximum benefit of VPP is solved under the worst case of source load uncertainty.

$$\min_x a^T x + \max_u \sum_i^k p_i \min_y (b^T y_i + c^T \xi_i) \quad (17)$$

where,  $x$  and  $y$  are the decision variable of the first and the second stage respectively,  $u$  is the uncertain set,  $a, b$  and  $c$  are the vector matrix,  $y_i$  is the decision variable of the second stage under scenario  $i$ ,  $\xi_i$  is the uncertainty of load under scenario  $i$ , and  $k$  is the total number of scenario,  $p_i$  is the probability of scenario  $i$ .

Formula 17 is a two-stage max-min max problem that cannot be solved directly, so the C&CG algorithm is used to solve the main problem and sub-problem iteratively. The main question is expressed as Equation 18:

$$\begin{aligned} & \min_x a^T x + \vartheta \\ & \begin{cases} \vartheta \geq r^T y_{v'} \\ Ay_{v'} + Gx \leq b + Hu_{v'} \\ By_{v'} + Dx = d + Fu_{v'} \\ v' = 1, 2, \dots, v \end{cases} \end{aligned} \quad (18)$$

where,  $x, y$  and  $u$  represent the optimization variables of the main problem, subproblem and uncertain set respectively;  $v'$  represents the number of iterations, and the constraint of the iterative solution of the main problem includes the value of each iteration of the subproblem;  $u_{v'}$  and  $y_{v'}$  are solved in place of the main problem as the known quantity obtained by solving the uncertain set and the subproblem respectively.  $A, B, D, G, H$  and  $F$  are the constrained medium constant coefficient matrix;  $r, b$  and  $d$  are the constraint column vector with constant coefficients.

Solve the main problem and get  $x^*$ . Introduce the subproblem, which is expressed as Equation 19:

$$\begin{aligned} & \max_u \sum_i^k p_i \min_y b^T y_i + c^T \xi_i \\ & \begin{cases} Ay + Gx^* \leq b + Hu \\ By + Dx^* = d + Fu \end{cases} \end{aligned} \quad (19)$$

The main problem passes the combination solution to the sub-problem, and solves the maximum VPP payoff in the worst case. Since the subproblem is a Min-Max two-layer problem, the two-layer problem needs to be transformed into a max single-layer problem as Equation 20 by KKT condition or duality theory.

$$\begin{aligned} & \max (b + Hu)^T \lambda_1 + (d + Fu)^T \lambda_2 \\ & \begin{cases} (b - Gx^*)^T \lambda_1 + (d - Dx^*)^T \lambda_2 \geq z \\ \lambda_1 \geq 0 \\ \lambda_2 \text{ no constraints} \end{cases} \end{aligned} \quad (20)$$

where,  $\lambda_1$  and  $\lambda_2$  are the dual auxiliary variable of inequality constraint and equality constraint respectively.

### 4.2 Uncertain set

In this paper, Wasserstein distance (Grani and Hanasusanto, 2018; Zhao and Guan, 2016) is used to construct fuzzy uncertainty sets. Wasserstein distance is defined as Equation 21:

$$d_w(Q_1, Q_2) = \inf_{\Pi} \int_{\Xi^2} d(\xi_1 - \xi_2) \Pi(d\xi_1, d\xi_2) \quad (21)$$

where,  $Q_1$  and  $Q_2$  are the edge distribution of the uncertain parameter,  $\xi_1$  and  $\xi_2$  are the distributions of the uncertain parameter,  $d(\xi_1 - \xi_2)$  is the distance measure between the two distributions, and  $\Pi(d\xi_1, d\xi_2)$  is the joint probability distribution of  $Q_1$  and  $Q_2$ .

Taking the empirical distribution as the center, the source load prediction error probability distribution set, also known as fuzzy uncertainty set, is constructed. The uncertainty set  $\Omega$  is as Equation 22:

$$\Omega = \{P \in \Xi | d_w(P, \hat{P}_N) \leq \theta\} \tag{22}$$

where,  $\Xi$  is all possible probability distributions of the uncertain parameters,  $\hat{P}_N$  is the empirical distribution of the uncertain parameters, and  $\theta$  is the radius of the uncertain set as Equation 23.

$$\theta = D \sqrt{\frac{2}{N} \ln\left(\frac{1}{1-\beta}\right)} \tag{23}$$

where,  $N$  is the number of historical data,  $\beta$  is the confidence level, and  $D$  is the coefficient.

The uncertain set  $\Xi$  is specified by the upper and lower bounds of the uncertain parameters as shown in Equation 24:

$$\Xi = \{\xi | \xi_i^{\min} \leq \xi \leq \xi_i^{\max}\} \tag{24}$$

where,  $\xi_i^{\max}$  is the maximum prediction error vector composed of the maximum prediction error of the source load in each scheduling period, and  $\xi_i^{\min}$  is the minimum prediction error vector composed of the minimum prediction error of wind power in each scheduling period. Equation 25 represents the relationship between the radius  $\theta$  of the uncertain set and the initial probability  $p_i$ .

$$\sum_i^k p_i \|\xi - \xi_i\| \leq \theta \tag{25}$$

where,  $\xi$  is a  $1 \times 24$ -dimensional vector composed of the source load prediction error;  $\xi_i$  is the  $i$ th historical prediction error vector,  $p_i$  is the initial probability corresponding to the historical data, and  $\|\bullet\|$  is the norm of the vector.

### 4.3 Model solving procedure

- Step 1: Set the lower bound  $LB = 0$ , the upper bound  $UB = +\infty$ , initialize the number of iterations  $r$  and the initial probability distribution  $p_\omega^0$ .
- Step 2: Solve the main problem, pass the solution  $x^*$  to the subproblem, and update the  $UB = \min\{UB, \lambda^*\}$ .
- Step 3: Solve the main problem according to  $x^*$  to get  $p_\omega^*$ , update the  $LB = \max\{LB, f(x^*)\}$ .
- Step 4: If  $UB - LB < \varepsilon$ , the iteration ends, the solution is output; otherwise, the subproblem solution  $p_\omega^*$  is passed back to step 2, the main problem is solved, and the iteration number  $r = r + 1$  is updated.

## 5 Example analysis

This paper optimizes the operation of the VPP with a cycle of 24 h. The maximum tradable power is 50 MW, the efficiency of storage equipment is 0.9, the fixed cost of the traditional power plant is 200 yuan, and the power generation cost is 450 yuan. The time-based electricity price is shown in Table 1, and the load and wind power generation forecast data are indicated in Figure 1.

TABLE 1 Time of use price.

Time frame	Time frame	Price (yuan/MW)
Valley segment	00:00–07:00	240
Flat section	08:00,12:00–18:00	450
Crest segment	09:00–11:00,19:00–23:00	675

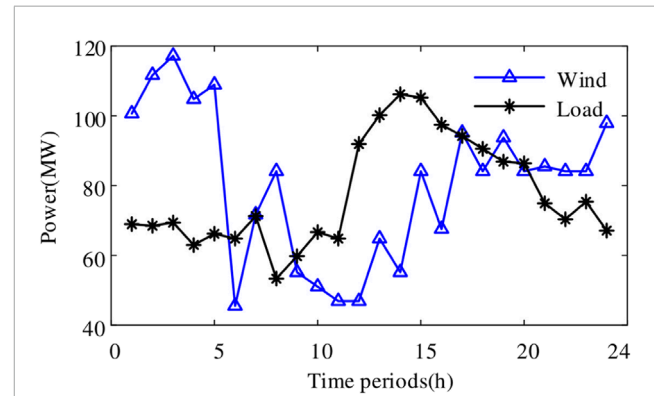


FIGURE 1 Forecasted values.

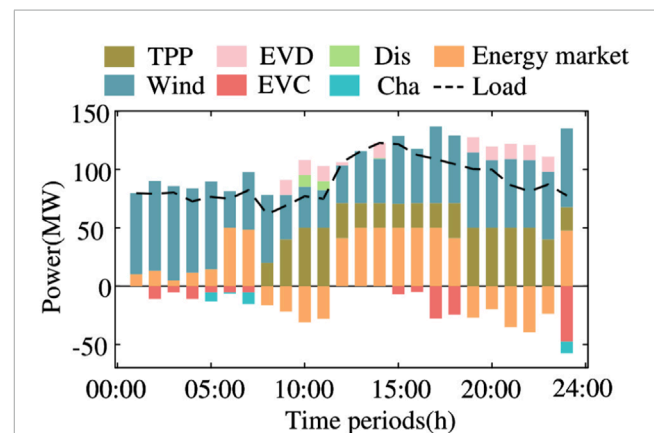


FIGURE 2 VPP scheduling result.

The results of VPP internal resource scheduling are shown in Figure 2. During 9:00–11:00 and 19:00–23:00, when the load demand is high and the wind power level is low, the electric vehicle discharges. A positive trading power in the energy market indicates the purchase of energy, and a negative one is the opposite. The trading price of the power market peaks at 9:00–11:00 and 19:00–23:00, and VPP tends to sell energy during the period of high electricity price, virtual energy storage and battery discharge promote the sale of energy by VPP, thus reducing the operating cost of VPP.

The charge and discharge power of VES and EVs are shown in Figure 3. EVs engage in the optimization scheduling of VPPs according to the guidance of price signals. From 0:00 to

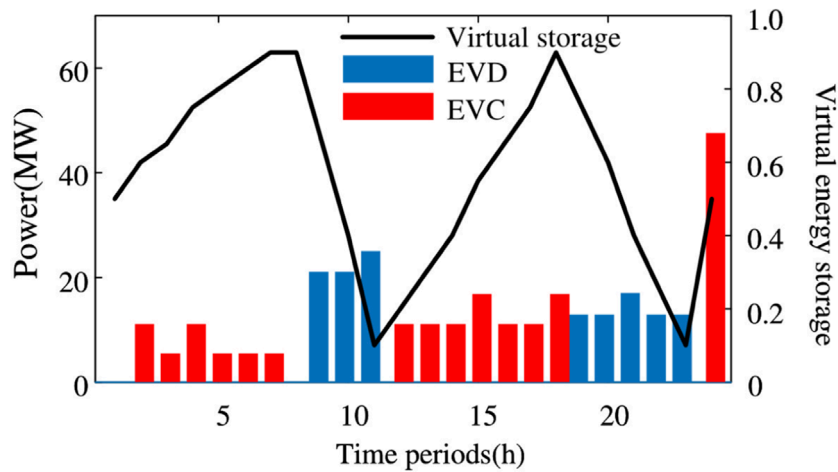


FIGURE 3 Storage capacity of virtual energy storage.

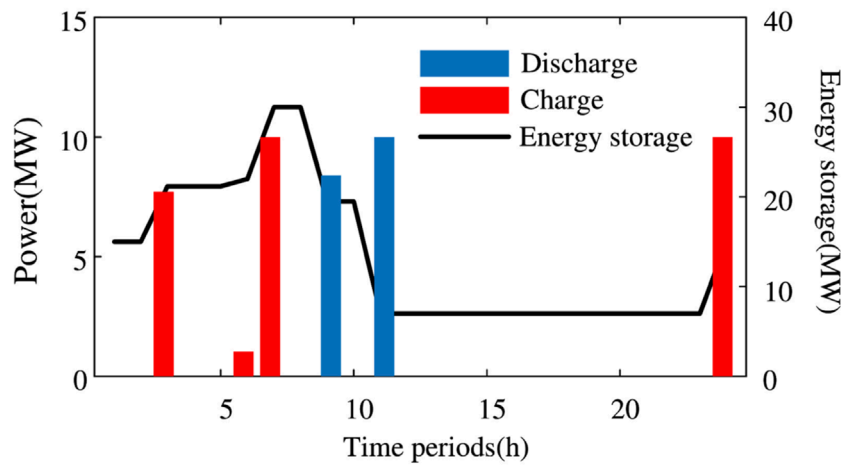


FIGURE 4 Storage capacity of battery.

7:00, electric vehicles purchase electricity from the market to supply VES and batteries. The power market trading price is at its peak between 9:00–11:00 and 19:00–23:00, and VES discharged during this period, improving the operating profit of VPP.

The charge-discharge power of the battery is shown in Figure 4. At 9:00–11:00 when the load demand is high and the wind power level is low, the energy storage discharge relieves the pressure of the VPP load demand.

As indicated in Table 2, after utilizing the “carbon charge rate” of energy storage to participate in the VPP market pricing mechanism, the operating cost of VPP decreases and the carbon emission increases.

The relationship between robust confidence and VPP profit is shown in Table 3. With the increase of confidence level

TABLE 2 Data comparison before and after pricing.

Type	Running cost (10 <sup>4</sup> yuan)	Carbon emission (kg)
Before pricing	5.9114	6,214
After pricing	5.8233	6,084

TABLE 3 VPP cost for different confidence sets (10<sup>4</sup>yuan).

Confidence sets	$\beta = 0.9$	$\beta = 0.8$	$\beta = 0.7$	$\beta = 0.6$
Running cost	5.9114	5.7782	5.3722	4.9782

$\beta$ , the radius of Wasserstein's sphere increases, the robustness of the model also increases, the uncertainty of the source charge in the VPP operating model increases, the VPP operating is more conservative, and its operating cost increases.

## 6 Conclusion

To improve the benefit ability of VPP in the power market, this paper analyzes the travel characteristics of electric vehicles, establishes the virtual energy storage power model of electric vehicles, proposes the coupling of carbon emission and energy storage system with "carbon charge rate" of energy storage, and constructs the relationship between carbon emission and transaction price. Finally, a two-stage robust optimization operation model of VPP considering the VES model of EV and the carbon charge rate model of ES is established. With simulation, conclusions can be drawn:

- 1) Creating a simulated ES model for EVs, ascertaining the controlled power output of this virtual storage to integrate into VPPs, optimizing within designated charge and discharge thresholds, thereby enhancing the VPP's capability for peak shaving and load balancing.
- 2) This paper puts forward the concept of "carbon charge rate" of energy storage, which represents the ratio between the carbon emissions absorbed in the energy storage and the stored electricity, that is, the amount of carbon emissions per unit of electricity in the energy storage. The "carbon charge rate" model can be well applied to systems containing energy storage and carbon emissions, and combined with its pricing mechanism can change the operation of VPP.
- 3) Aiming at the uncertainty of system source load, a two-stage robust optimization operation model is proposed. With the increase of Wasserstein sphere radius, the operational robustness of VPP is also enhanced, and its operating cost is increased.

In general, by introducing electric vehicles as virtual energy storage resources and considering carbon emissions, this paper provides a new perspective and method for the optimal scheduling of virtual power plants. It is of great significance to improve the competitiveness and adaptability of virtual power plants in the power market. The extended application of "carbon charge rate" model is also a possible direction of this research in the future, and it is considered to combine it with other environmental impact indicators (such as the value of ecosystem services, water resources

consumption, etc.) to conduct a comprehensive environmental impact assessment.

## Data availability statement

The original contributions presented in the study are included in the article/supplementary material, further inquiries can be directed to the corresponding author.

## Author contributions

BW: Methodology, Software, Writing—original draft. YJ: Resources, Writing—review and editing. MJ: Project administration, Writing—review and editing. KM: Data curation, Writing—review and editing.

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## Conflict of interest

Authors BW, MJ, and KM were employed by Economic and Technological Research Institute of Jilin Electric Power Co., LTD. Author YJ was employed by State Grid Jilin Electric Power Co., LTD.

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