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# Research on fault localization of distribution transformers based on frequency response analysis and support vector machine (SVM)

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Distribution transformers are vital to the stability of the power system, but long-term operation and environmental factors can cause distribution transformers to discharge, posing a potential threat. The impulse voltage withstand test rigorously evaluates the insulation of the transformer windings, to prevent accidents caused by insulation breakdown. However, due to the small size of distribution transformers, impulse voltage withstand test breakdown usually cause less damage, and it is challenging to locate the point of failure using traditional methods such as spatial positioning or disassembly. Therefore, the study of the discharge location method based on the characteristic value of the frequency response waveform is of great significance to find and deal with potential faults. This paper discusses the waveform characteristics of different discharge signals transmitted from different positions of the winding to the end. By analyzing the frequency response of different breakdown current signals measured at the end of the transformer winding, support vector machine is used to identify the breakdown position of the distribution transformer. The approximate location of the fault was identified with more than 80% accuracy. The feasibility and effectiveness of this localization method are verified by experiments.

## KEYWORDS

oil-immersed distribution transformers, breakdown current signal, frequency response, support vector machine (SVM), location

## 1 Introduction

Distribution transformer plays a vital role in power system, but due to the influence of long-term operation and environmental factors, it may have breakdown phenomenon, which poses a potential threat to the stability and security of power system. The impulse voltage has the characteristics of high amplitude and high steepness, which can detect small defects in the insulation system, improve the reliability of the transformer, reduce the risk of damage, and extend the life of the equipment, so as to ensure the safe and stable operation of the distribution transformer (Zhang et al., 2020). At present, the impulse voltage withstand test has become

one of the distribution transformer factory must do the test. By studying the transformer fault location method, it can avoid the multiple pendant checks caused by the fault point is not obvious, the operation and maintenance personnel misjudge the fault cause and increase the workload, improve the test efficiency and reduce the waste of manpower and material resources.

At present, common discharge detection methods are divided into non-electrical and electrical measurement methods, mainly including ultrasonic method, Ultra High Frequency (UHF) method, pulse current method, etc., which detect discharge by measuring different physical phenomena (ultrasonic wave, electromagnetic wave, current pulse) simultaneously with discharge (Cavallini et al., 2010; Desai and Sarathi, 2018). Among them, ultrasonic method and UHF method use sensors for discharge detection (Liu et al., 2020). The ultrasonic positioning technology determines the discharge position by measuring the time difference between the ultrasonic signal and the electrical pulse signal (Xie et al., 2013; Al-Masri et al., 2016), and its strong anti-interference ability and portability make it popular in field applications. However, due to the complexity of the internal structure of the transformer, the propagation speed of the ultrasonic wave in different media is difficult to keep constant, and this fixed sound speed assumption often leads to the deviation of the positioning results. UHF positioning technology (Mirzaei et al., 2012; Jahangir et al., 2020) uses the electromagnetic wave signal generated during discharge to locate, and its high anti-interference and fast positioning speed make it a research hotspot. However, the penetration ability of electromagnetic waves in metals and other media is limited, especially in the environment filled with metal parts such as transformers, the signal attenuation problem is particularly prominent, thus limiting the positioning accuracy of the technology. Due to the high sealing of oil-immersed distribution transformers, the installation of sensors is inconvenient, and it is difficult to apply in the transformer factory test (Xiao et al., 2014). Pulse current method can conduct quantitative and qualitative analysis of discharge signals, and is an effective method for locating discharge sources (Cavallini et al., 2010; Okabe et al., 2011). However, it requires input voltage signals and has weak anti-interference ability, so it is not suitable for discharge detection under impulse voltage withstand test (Okabe et al., 2012). In view of this situation, it is important to study the efficient method of breakdown point location of distribution transformer under impact test for transformer fault detection and location.

As the core component that undertakes most of the functions of the transformer, the health of the winding directly determines the safety of the transformer operation. In the incomplete statistics of power transformer failure events, more than half of the cases are caused by winding failure, most of which are caused by insulation problems (Martin et al., 2018). Therefore, the maintenance of good insulation condition of windings and timely detection and maintenance of insulation faults are very important support for stable transmission of electric energy.

With the increasing scale and complex structure of transformers, positioning methods based on measuring signal frequency spectrum have emerged gradually in the 21st century. In these studies, the double exponential pulse signal is used as the analog

signal type. The positioning method based on signal spectrum analysis has gradually emerged and become the mainstream. Reference (Akbari et al., 2002) utilized the measured segmental winding transfer function curve to restore the local discharge waveform to the time-domain curve of each internal point, and positioned it by the degree of waveform coincidence. Reference (Hettiwatte et al., 2002; Wang et al., 2005) proposed a positioning method based on the measured signal itself, by calibrating the formula parameters and measuring the resonance point of the local signal to complete the positioning. These methods based on frequency spectrum analysis effectively deal with the challenges brought by complex transformer structures, and gradually become a reliable positioning technology. Reference (Eldery et al., 2006) used the power spectrum density estimation method based on the period diagram to analyze the voltage signal of the low voltage winding during the local discharge of the high voltage winding, and used the distance function to compare the simulated and measured power spectrum of the local discharge to determine the discharge position. Some studies (Jafari et al., 2008) achieved discharge localization by calculating the reference curve of the fragment transfer function in advance and comparing the distance function with the measured partial discharge spectrum. Reference (Naderi et al., 2008) completes the ratio method electrical positioning by using the all-time wavelet transform of the local discharge signals at the head and end of the winding and the  $\alpha$  value determined by the capacitive component method.

Based on the winding design parameters, reference (Jyabalan and Usa, 2009) uses Gram-Schmidt orthodontic method to process the reference spectrum signal, and then compares with the measured local discharge spectrum and positioning, achieving good results. Later, the scholar studied the winding local discharge positioning based on regression analysis, statistical correlation method and correlation phase analysis (Jeyabalan and Usa, 2011). Based on the reference signal and actual local discharge signal of each node during discharge obtained by simulation of winding model, reference (Guillen et al., 2014) used Laplace wavelet transform and Hellinger distance comparison algorithm to accurately locate the discharge.

However, the discharge pulse signals in actual operation are often more complex and diverse (Mohseni et al., 2016). Therefore, it is of great significance to establish a more accurate simulation model based on real distribution transformers and study the propagation characteristics of discharge pulse signals in windings to improve the accuracy of fault location.

This paper investigates the feasibility of a location algorithm based on the frequency diagram of breakdown current signals for oil-immersed distribution transformers under different signal types. The study focuses on the distinct frequency responses of the transformers to these signals and their implications for identifying and localizing faults within the transformer windings. Through simulation and experimentation, the paper explores how the position of the injected signal within the transformer winding affects the spectrum distribution of the resulting signal, with particular attention paid to the variations in high-frequency components. Ultimately, a method based on the frequency response characteristics of breakdown current signals is proposed

TABLE 1 Layered transformer related parameters.

Parameter name	Parameter value	Parameter name	Parameter value
Layer insulation thickness	1.5 mm	Core diameter	151 mm
Number of high-voltage winding layers	10	Low voltage winding height	574 mm
Height of high-voltage winding	574 mm	Low voltage winding outside diameter	195 mm
Outer diameter of high-voltage winding	336 mm	Low voltage winding bore diameter	151 mm
Inner diameter of high-voltage winding	204 mm	Tank diameter	450 mm
Number of turns per layer of winding	100	Total length of winding	847.78 m

for localization, utilizing the support vector machine (SVM) algorithm.

## 2 Establishment of winding model

The winding model is established based on the layered structure of a 10kV/250kVA oil-immersed distribution transformer winding. Table 1 shows the relevant parameters of the transformer, which are measured based on the transformer. Modeling and simulation are conducted using the winding parameters of the oil-immersed distribution transformer. Due to the frequency range of breakdown current signals being several hundred kHz to several MHz, the capacitance and inductance parameters play a major role in the equivalent circuit. The winding inductance can be considered as an air-core inductance, with the addition of high-frequency resistance that takes into account the skin effect. When modeling, the capacitance distribution between layers is considered, and some lumped parameters are used to replace the distributed parameters. To enhance the accuracy of breakdown localization, each of the ten layers of windings is divided into three sections, resulting in a total of 30 sections. The broadband equivalent distributed parameter model of the transformer is established. The equivalent model of RLC is established based on the layer winding of 10 kV distribution transformer, as shown in Figure 1. Each layer of the winding is divided into  $n$  units, with a total of  $m$  layers.  $C_{WC}$  represents the capacitance between the winding and the iron core,  $C_{WD}$  represents the capacitance between the winding and the oil tank,  $L_{ij}$ ,  $C_{kij}$  and  $R_{ij}$  are the inductance, capacitance, and resistance of each winding unit, respectively, and  $C_D$  is the capacitance between the winding layers. Additionally, there is mutual inductance  $M_{pq}$  between any two units. Calculations are performed using an analytical method. In this paper, the winding consists of 10 layers with three units in each layer.

### 2.1 Capacitance parameter calculation

The geometric capacitance of the winding can be divided into: axial geometric capacitance (interturn geometric capacitance), radial geometric capacitance (interlayer geometric capacitance, winding capacitance to the core, winding capacitance to the fuel tank).

The formula for calculating the interturn geometric capacitance and interlayer geometric capacitance is as follows.

$$C_T = \frac{\epsilon_0 \epsilon_r \pi d_T h}{a_T}$$

$$C_D = \frac{\epsilon_0 \epsilon_{r1} \pi d_T B}{a_s}$$

In the formula:  $\epsilon_r$  represents the dielectric constant of the coil turn insulation;  $\epsilon_{r1}$  represents equivalent dielectric constant of interlayer insulation;  $d_T$  represents Calculate the average diameter of the turns/m;  $h$  represents transformer winding wire width/m;  $B$  is Calculate the interlayer axial height/m of some windings;  $a_T$  represents interturn insulation thickness/m;  $a_s$  represents Layer insulation thickness/m.

The axial capacitance equivalent is ( $w$  is the number of turns):

$$C_k = \frac{w-2}{w^2} C_T + \frac{2}{3} C_D$$

The radial capacitance of winding consists of winding interlayer capacitance, winding to core capacitance and winding to shell capacitance. The geometric capacitance value is obtained by coaxial cylindrical capacitance formula.

The formula for solving the geometric capacitance  $C_{WC}$  of the winding to the core and the geometric capacitance  $C_{WB}$  of the winding to the shell is as follows:

$$C_{WC} = \frac{2\epsilon_0 \epsilon_{r2} \pi H}{\ln(R_{W1}/R_C)}$$

$$C_{WB} = 0.75 \times \frac{2\epsilon_0 \epsilon_{r3} \pi H}{\ln(R_B/R_{W2})}$$

In the formula:  $\epsilon_{r2}$  represents the equivalent dielectric constant of the insulation between the winding and the transformer core;  $\epsilon_{r3}$  represents equivalent dielectric constant of the insulation between the winding and the transformer housing;  $R_B$  represents inside radius of transformer housing/m;  $R_C$  represents core radius/m;  $R_{W1}$  and  $R_{W2}$  are inner and outer radius of transformer winding/m;  $H$  represents transformer winding height/m.

The calculated parameters of longitudinal capacitance, interlayer capacitance and ground capacitance of some windings are shown in the Table 2.

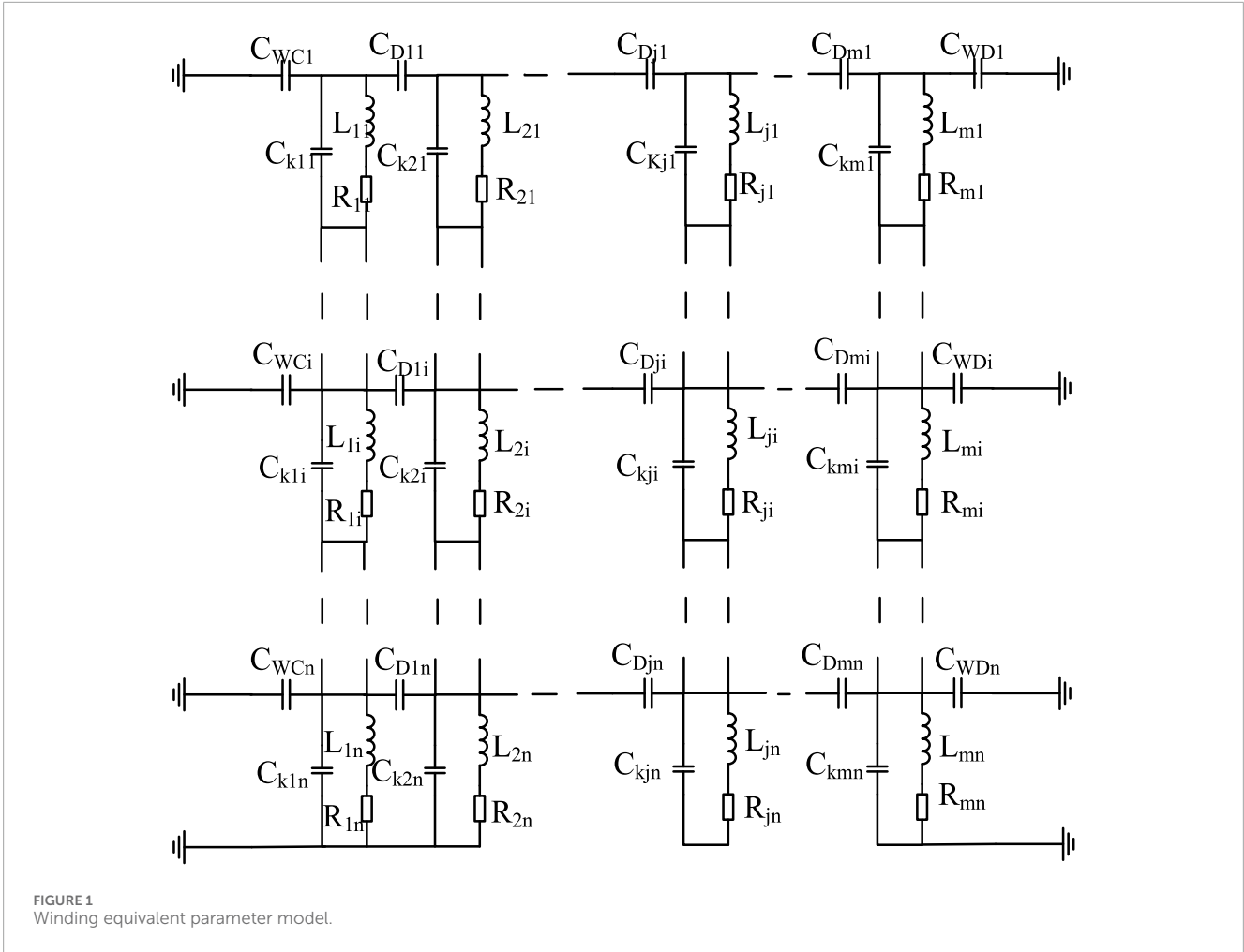


TABLE 2 Calculated capacitance values.

Capacitance	Unit longitudinal capacitance $C_k$	Interlayer capacitance $C_D$	Total capacitance $C_{WC}$ to the core	Total capacitance $C_{WB}$ to the tank
Parameter Value	7.1 nF	2.5 nF	273.92 pF	180.90 pF

2,4,6,8 refers to the different layer positions, and 0 indicates that the signal occurs at the head end.

## 2.2 Inductance parameter calculation

The simplified calculation formula of winding mutual inductance  $M_{ij}$  is as follows:

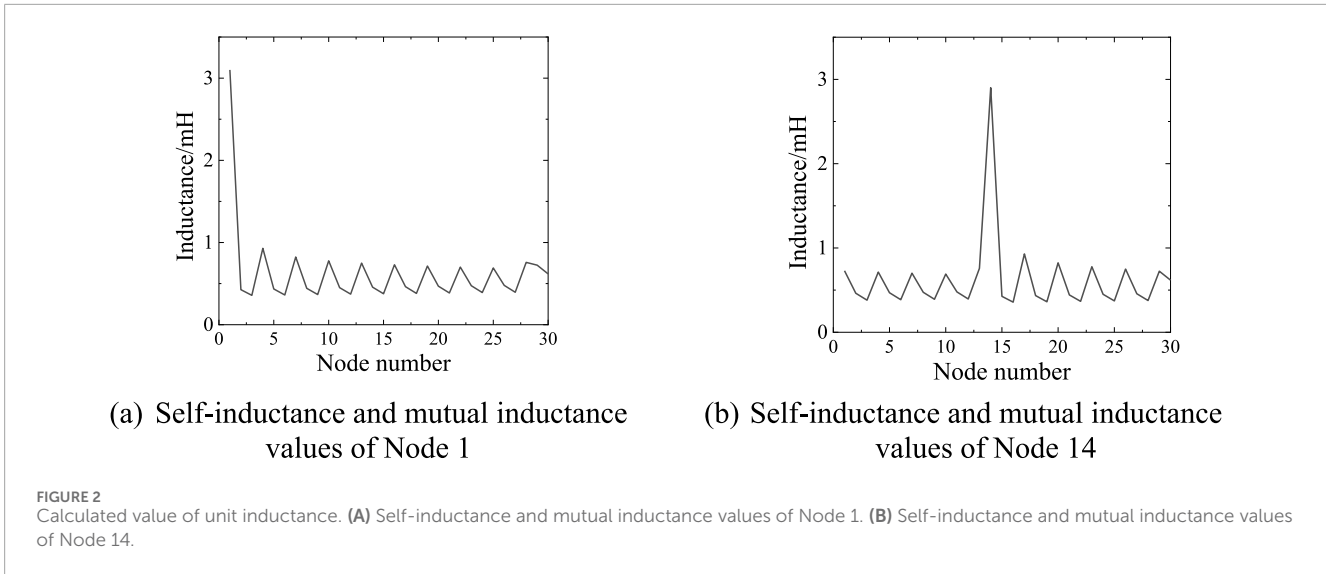
$$M_{ij} \approx \mu_0 N_i N_j \sqrt{a_i a_j} \frac{2}{k} \left[ \left( 1 - \frac{k^2}{2} \right) K(k) - E(k) \right] 4\pi \times 10^{-7}$$

$$k = \sqrt{\frac{4a_i a_j}{z^2 + (a_i + a_j)^2}}$$

In the formula:  $\mu_0$  represents vacuum permeability/  $4\pi \times 10^{-7}$  Wb·A<sup>-1</sup>·m<sup>-1</sup>;  $N_i$  and  $N_j$  respectively represent number of turns in winding  $i$  and winding  $j$ ;  $a_i$  and  $a_j$  respectively represent the

average radius of winding  $i$  and winding  $j$ /m;  $K(k)$ ,  $E(k)$  are complete elliptic integrals of the first and second kinds;  $z$  represents distance between the center point of the section of winding  $i$  and winding  $j$ /m.

The self-inductance of winding  $i$  is calculated, namely:  $L_i = M_{ii}$ ,  $N_i = N_j$ , and  $z = 0.2235(h + w)$ ,  $h$  is the height of the winding,  $w$  is the width of the winding. Figure 2 shows the calculated self-inductance and mutual inductance values for Node 1 and Node 14. The self-inductance values are greater than the mutual inductance values between different nodes. Additionally, due to the layered structure of the winding, the mutual inductance between the same node and different positions within the same layer varies, resulting in a sawtooth pattern.



### 2.3 Resistance parameter calculation

Ignoring the common-ground loop resistance, the skin effect at high frequency is considered in the calculation of the resistance matrix, and the calculation formula for the unit length of the conductor is as follows:

$$R = \frac{1}{2(d_1 + d_2)} \sqrt{\frac{\pi f \mu}{\sigma}}$$

Where:  $d_1$  and  $d_2$  are length and width of matrix conductor cross section/m;  $\mu$  represents the permeability of the winding;  $\sigma$  represents Electrical conductivity of the winding.

### 3 Frequency spectrum distribution under different analog signals

The standard lightning impulse voltage is applied to the first end of the model, and the wave head/wave tail time is 1.2/50  $\mu$ s. The node voltage waveform under the impulse voltage and the measured terminal current waveform are shown in Figure 3.

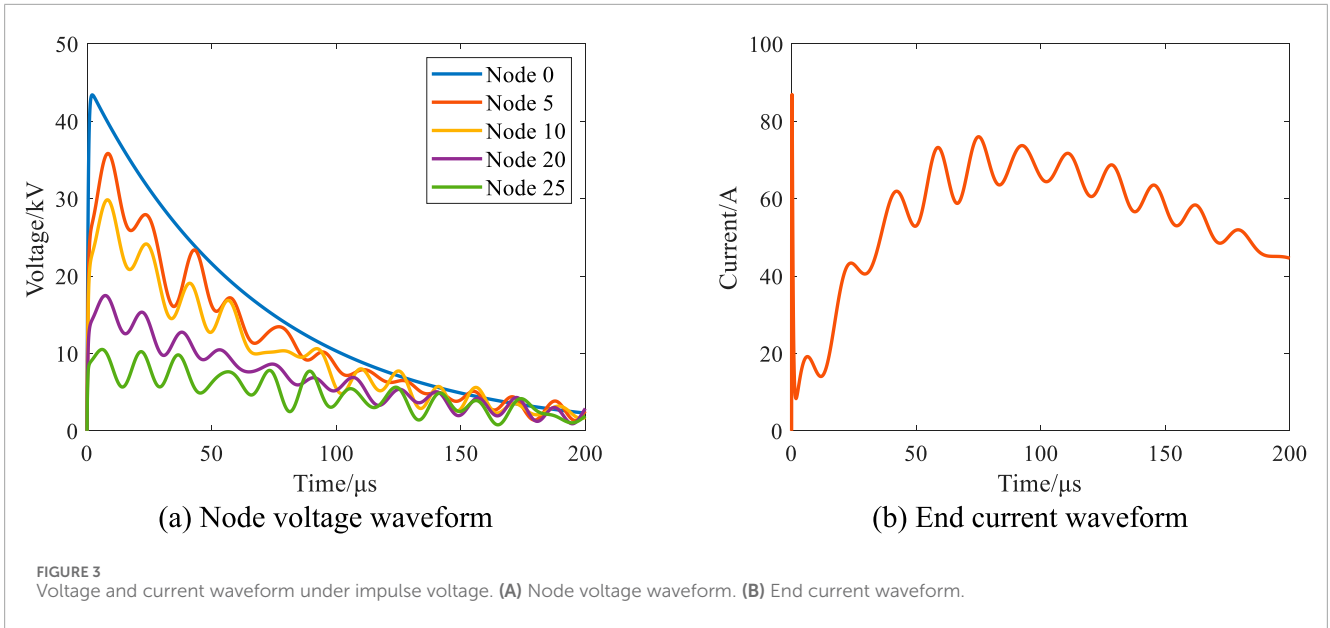
When the impulse voltage starts to act, the initial distribution of potential is determined by the coupling between the winding longitudinal capacitance, ground capacitance and interlayer capacitance. Most of the voltage drop is near the head end of the winding, so the assessment of the longitudinal insulation of the transformer winding is relatively strict. After the shock voltage wavefront time, there are capacitors, inductors and resistors acting in the winding, and oscillation occurs based on the natural frequency of the winding resonance frequency. The voltage signal amplitude of each node in the winding is distributed according to the position, and the voltage value of some points will exceed the shock voltage value. The end current signal is an oscillating waveform after the peak of the tip.

When breakdown faults occur at different positions in transformer windings, the changes in electrical parameters within their equivalent networks exhibit variability. The frequency spectrum curves and the amplitude and phase information of the frequency response curves of the breakdown current also vary with the faults. This paper extracts numerous features based on changes in the amplitude-frequency characteristic curves, transforming the curve variations into numerical feature differences. This significantly enhances the efficiency of identifying winding breakdown faults and the accuracy of localization. Several widely used numerical features are selected for fault identification. The Pearson correlation coefficient serves as a pivotal statistical tool, enabling the precise quantification of the degree of similarity and dissimilarity between fault and normal state curves. Furthermore, the incorporation of Absolute sum of logarithmic error enhances the sensitivity to subtle variations within fault states. In terms of characterizing waveform alterations, statistical metrics including standard deviation, kurtosis, and skewness are utilized to unveil the intricate patterns within the distribution of waveforms. These metrics not only elucidate the inherent characteristics of the waveform but also delve into the profound impacts of faults on its dispersion, sharpness, and symmetry. Additionally, the computation of critical parameters such as root mean square and crest factor offers a holistic assessment of the overall changes in current intensity and the pronounced augmentation of peak characteristics during fault conditions. The calculation formula is as follows:

- (1) Pearson Correlation Coefficient (PCC)

$$PCC = \frac{\sum_{i=1}^N (X_i - \bar{X})(Y_i - \bar{Y})}{\sqrt{\sum_{i=1}^N (X_i - \bar{X})^2 \sum_{i=1}^N (Y_i - \bar{Y})^2}}$$

- (2) Absolute Sum of Logarithmic Error (ALSE)



$$ALSE = \frac{\sum_{i=1}^N |20 \log_{10}|X_i| - 20 \log_{10}|Y_i|}{N}$$

Where  $X_i$  and  $Y_i$  are the amplitudes of the frequency point  $i$ 's frequency response curves for the normal and faulty winding conditions, respectively, and  $N$  is the total number of frequency points.

(3) Standard Deviation (SD)

$$SD = \sqrt{\frac{\sum_{i=1}^N (Z_i - \bar{Z})^2}{N}}$$

(4) Kurtosis (Ku)

$$Ku = \frac{\frac{1}{N} \sum_{i=1}^N (Z_i - \bar{Z})^4}{\left( \frac{1}{N} \sum_{i=1}^N (Z_i - \bar{Z})^2 \right)^2}$$

(5) Skewness (Sk)

$$Sk = \frac{\frac{1}{N} \sum_{i=1}^N (Z_i - \bar{Z})^3}{\left( \frac{1}{N} \sum_{i=1}^N (Z_i - \bar{Z})^2 \right)^{\frac{3}{2}}}$$

(6) Root Mean Square (RMS)

$$RMS = \sqrt{\frac{\sum_{i=1}^N Z_i^2}{N}}$$

(7) Crest Factor (CF)

$$CF = \frac{Z_{max}}{RMS}$$

### 3.1 Signal characteristics under Gaussian pulse injection

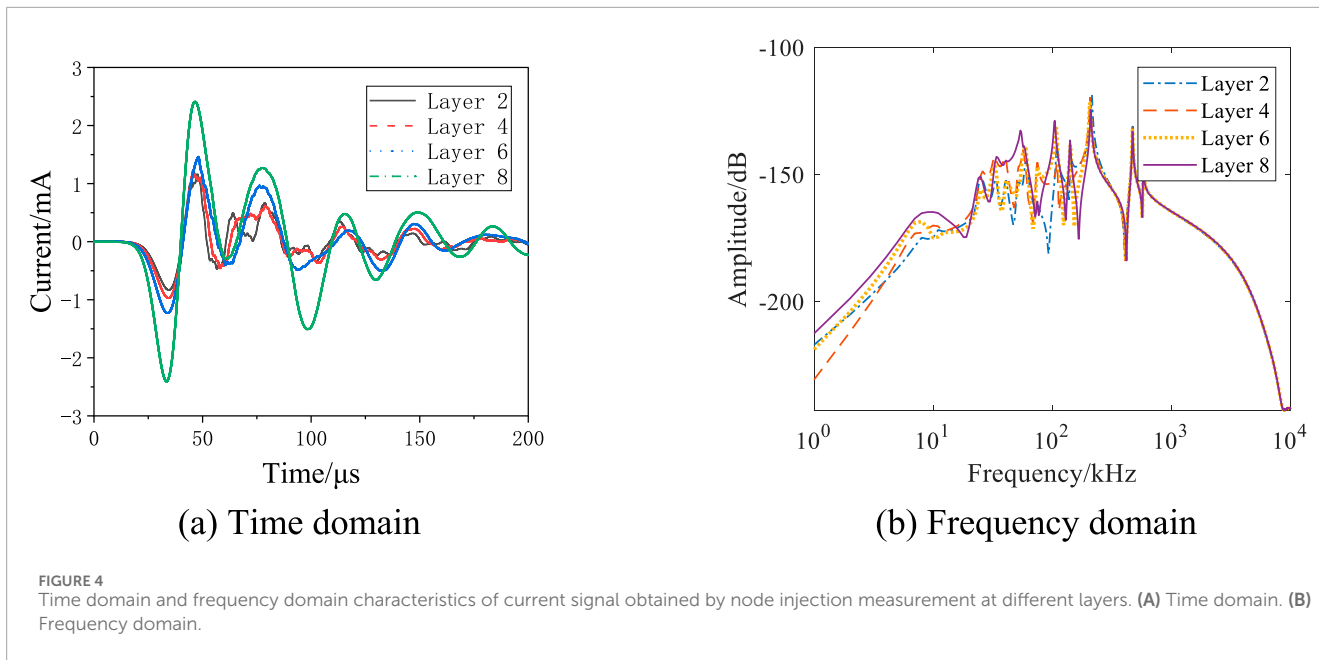
In order to simulate the characteristics of the actual breakdown current waveform, two methods are used to simulate the pulse current source as the input current  $I_{in}$  to simulate the breakdown discharge: Gaussian current pulse and simulated breakdown current pulse. The Gaussian pulse signal has good mathematical and statistical properties and can be used to simulate the discharge process. The formula for the change of Gaussian pulse input  $I_{in-G}$  current with time  $t$  is:

$$I_{in-G} = (1.25 \times 10^{-2}) e^{-4\pi \left( \frac{t-40 \times 10^{-6}}{8 \times 10^{-8}} \right)^2}$$

The parameters are all international system of Units. This pulse has a peak current of 12.5 mA and a duration of about 4  $\mu$ s.

Gaussian pulse signals are injected into the first node of layers 2, 4, 6, and 8 of the model, and the current signal waveforms measured at the end. Figure 4 shows the time-domain and frequency-domain characteristics of the current signals measured at Node 30 after



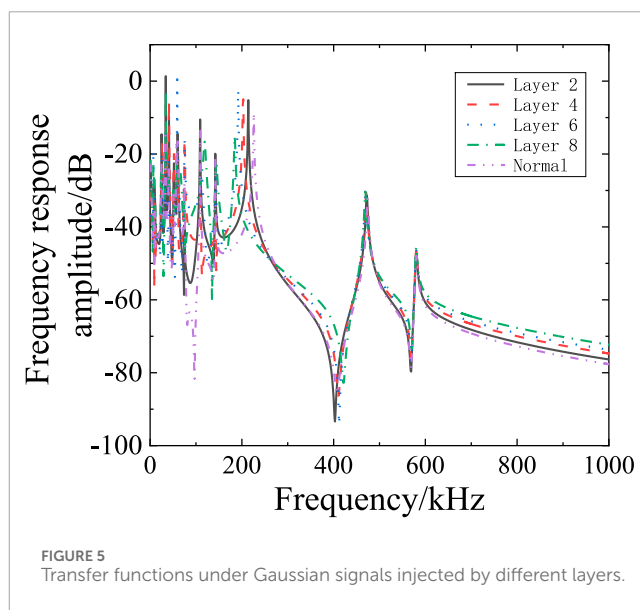


injecting Gaussian pulse signals into the first node of different layers (2, 4, 6, and 8) of the model.

As shown in Figure 4, the time and amplitude of the first peak in the time domain waveform of the resulting current signal correspond to the distance of the layer from the injection point and the characteristic impedance of the winding on that particular layer. The variations in delay and amplitude demonstrate the influence of winding structure on signal propagation. When the Gaussian pulse is input at the upper end of the winding, the amplitude of the spectrum fluctuation of the resulting signal is larger. As the input position of the Gaussian pulse moves toward the lower end, the low-frequency components increase.

In the low frequency band (1 kHz–10 kHz), the spectrum distribution at all locations has a low amplitude, which then rapidly increases as the frequency rises. The amplitude at the layer 2 position increases the fastest, indicating that the Gaussian pulse signal at this position has the greatest impact on the low frequency band. In the middle frequency band (around 100 kHz), the amplitude of the curves at all locations reaches its highest point and exhibits some fluctuation. The fluctuation at the layer 2 position is the most significant in the middle frequency band, while the current signal at other positions shows relatively stable fluctuations. In the high frequency band (100 kHz–10,000 kHz), the amplitude of the curves at all positions begins to decline and displays significant fluctuations. The current signals at layer 2 and layer 6 have the largest fluctuations in the high frequency band, while those at layer 4 and layer 8 have smaller fluctuations but also show a noticeable downward trend.

Furthermore, the signal characteristics of the transfer function are analyzed, and the correlation coefficient between it and the transfer function under normal working conditions, the absolute sum of the logarithm of error, and the waveform characteristics of the obtained amplitude-frequency curve are considered to analyze the relationship between it and the position. Figure 5 shows the frequency response curve of the transfer function obtained under the injection of Gaussian pulse signals at different positions, from



which it can be seen that its amplitude and waveform have changed, and its numerical characteristics are calculated and extracted.

The amplitude-frequency curve waveform characteristics obtained under the injected Gaussian pulse are shown in Table 3. The correlation coefficient, standard deviation and root mean square decrease as the injection position moves to the end, and the absolute sum and skewness of the error logarithm increase as the injection position moves to the end.

In addition, Gaussian pulse signals are injected into each node in the model, and its characteristic parameters are obtained as shown in Figure 6. It can be concluded that the numerical characteristics obtained by different nodes of the same layer winding will also be different, and the results near the end of the injected layer are more obvious.

TABLE 3 Waveform characteristics of amplitude-frequency curve.

Type	Layer	PCC	ALSE	SD	Ku	Sk	RMS	CF
Gaussian pulse injection	2	0.9545	5.2739	4.3184	2.4483	1.4206	65.2844	1.4429
	4	0.9089	6.701	4.1393	2.7349	1.4841	63.8866	1.3695
	6	0.8701	7.8487	4.0974	2.6902	1.4857	63.5047	1.5031
	8	0.8660	9.4300	3.9761	2.7992	1.5213	62.2032	1.3527
	0	—	—	4.1194	2.4970	1.4185	66.2283	1.3119
Direct grounding	2	0.9888	38.3506	3.9788	3.6186	1.7221	69.9971	1.3823
	4	0.9609	37.6210	4.0095	3.4398	1.6749	68.4149	1.2694
	6	0.9314	50.1496	5.4642	1.5077	1.1657	81.7345	1.2617
	8	0.8335	52.5993	3.6629	3.1666	1.6130	84.8000	1.2032
	0	—	—	1.7646	12.2808	3.3022	33.7018	2.0570
Simulate ground faults	2	0.6217	7.1674	2.7168	4.7656	1.9252	33.5272	1.6686
	4	0.4289	9.2781	3.0911	3.3208	1.6488	33.9069	2.0369
	6	0.3500	11.3746	3.2174	2.7692	1.5472	32.5727	1.7145
	8	0.2738	12.6135	3.2770	2.5230	1.4861	31.5266	1.5658
	0	—	—	1.7646	12.2808	3.3022	33.7018	2.0570

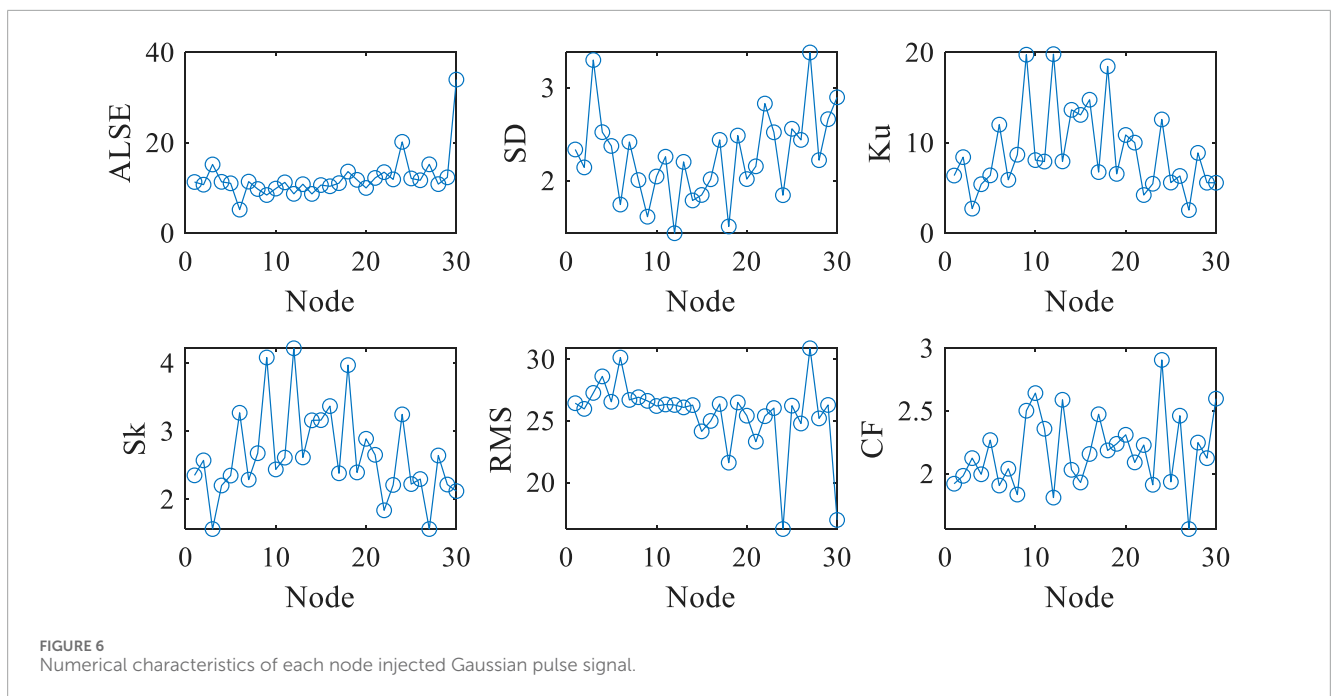


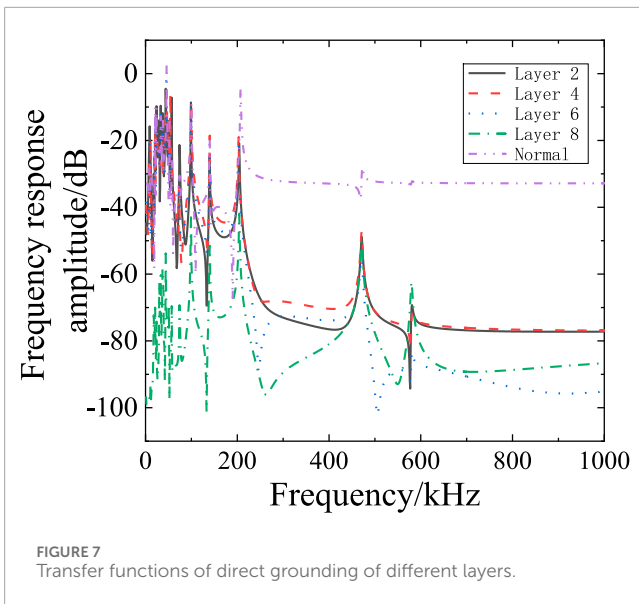
FIGURE 6 Numerical characteristics of each node injected Gaussian pulse signal.

### 3.2 Direct grounding of different nodes

In the model, the winding nodes are grounded successively, the impulse voltage is applied, the grounding current signal and the voltage signal of the head end are measured. Based on the

analysis of grounding conditions at different positions of the winding, waveform characteristics of amplitude-frequency curves directly connected to the ground at different positions are obtained, as shown in Figure 7. It can be seen from the frequency response curves of different ground layers and no ground (0), that applying





impulse voltage in the ground state has influence on both amplitude and resonance point.

The numerical characteristics of the frequency response curve were calculated and extracted, and the characteristic parameters were obtained as shown in Figure 8. It can be concluded that the variation law of characteristic values of the winding is the same as that of waveform characteristics obtained under Gaussian pulse injection. For 2nd, 4th, 6th, 8th layer windings, the correlation coefficient decreases from 0.9888 to 0.8335, and the absolute sum of the logarithm of errors increases from 38.3506 to 52.5993.

### 3.3 Simulate grounding faults at different positions

The impulse voltage is applied to the head end of the winding model and the grounding breakdown fault is simulated by the switch module. The current spectrum distribution obtained is shown in Figure 9. It can be found that the impact of the breakdown current signal at different positions on the spectrum distribution of the measured current signal at the end after the simulated breakdown fault. It can be compared that the fault has little influence on the low frequency band of the signal at different locations, and mainly affects the frequency distribution above 10 kHz.

With the breakdown position moving to the end, the fluctuation of the spectrum distribution in the frequency band near 400 kHz becomes larger, and the distribution change is obvious in the frequency band 10–100 kHz. By analyzing the influence of different fault locations on the frequency response of the system, the characteristics of each fault location and its specific influence on the system are revealed. The frequency response data of the system under normal state and four different fault locations layer 2, layer 4, layer 6 and layer 8 are collected in the experiment, and it is found that the faults at different locations show significant differences in each frequency segment.

In the low frequency band (10 kHz to about 100 kHz), the fault curve at position layer 2 shows a significant high amplitude,

indicating that the fault location has a greater impact on the low frequency band. As the frequency increases, the layer 2 curve shows significant fluctuations and peaks and valleys in the mid-band (about 100 kHz–300 kHz), indicating that the fault at position layer 2 also has a significant impact in the mid-band. In contrast, the fault curve at position layer 4 has a slightly lower amplitude and less fluctuation in the low and mid-frequency bands.

In the high frequency band (300 kHz–1,000 kHz), the fault curve at position layer 8 shows significant fluctuations and multiple peaks, indicating that the fault at this position has a very large impact on the high frequency band. The fault curve of layer 6 position is slightly different in some frequency segments, but the overall trend is similar to that of layer 4 position, indicating that the fault of layer 6 position mainly affects some specific frequencies in the middle and high frequency band.

The low frequency band is mainly affected by the fault at layer 2 position, which shows high amplitude. The fluctuation of the middle frequency band is mainly caused by the fault at layer 2 position, and the fault at layer 4 and layer 6 position also has a certain impact. The high frequency band is most affected by fault at layer 8 position, followed by fault at layer 2 position, showing significant fluctuations and multiple peaks. Under normal condition, the frequency response curve is the most stable and the fluctuation is the least.

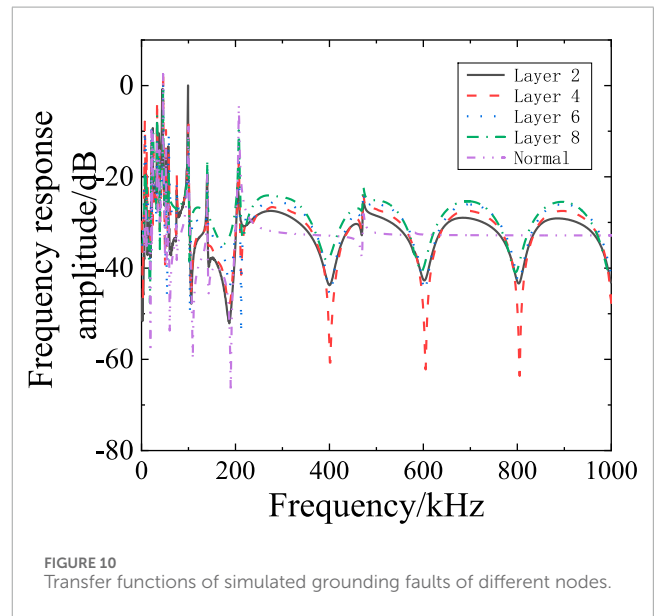
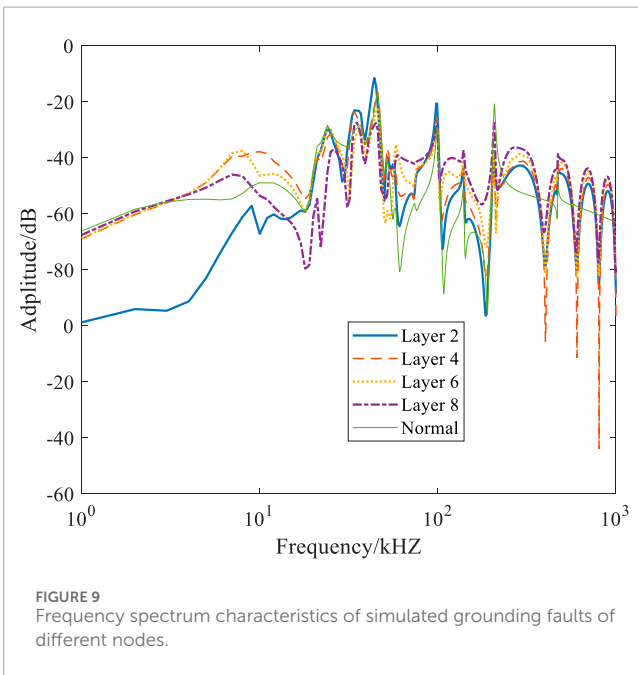
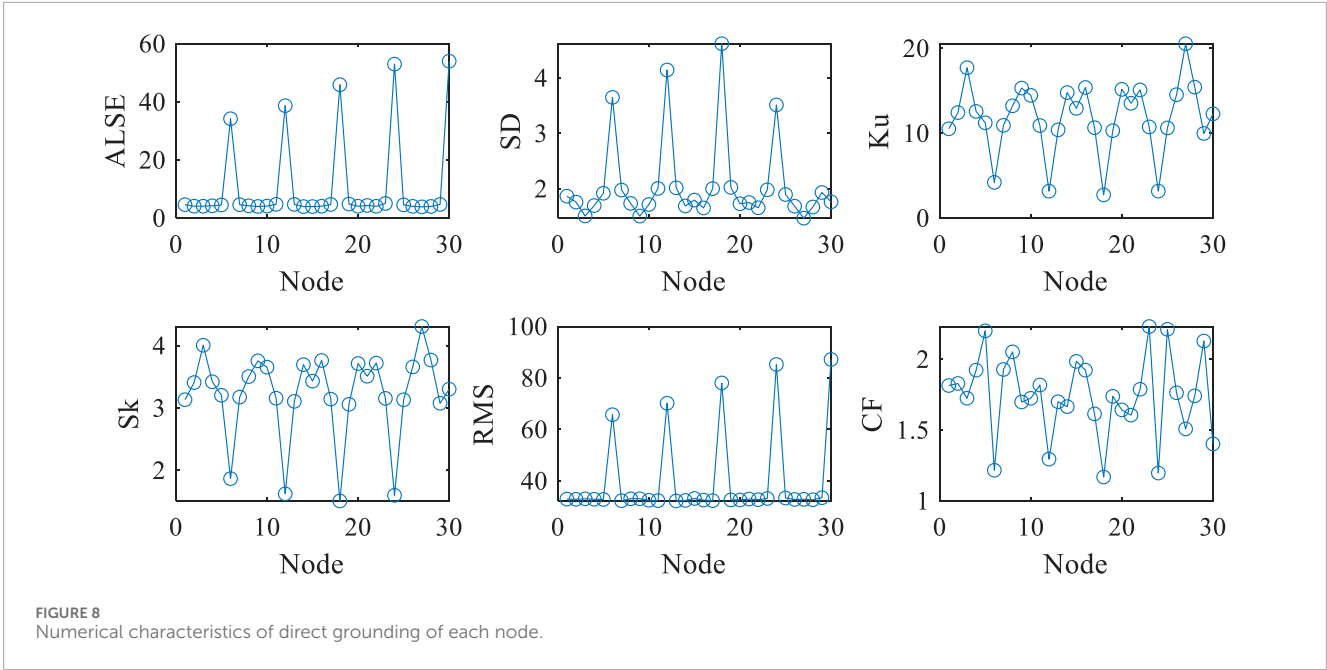
The transfer function of 0–1 MHz obtained under ground faults at different positions under impulse voltage is shown in Figure 10. Under normal condition, the peak value of the transfer function is in the range of 0–200 kHz. After breakdown fault occurs, the fluctuation becomes obvious within the range of 200 k–1 MHz, and multiple resonance points appear, which change with the fault position to the end position. The fluctuation is more severe when the fault occurs in the middle part of the winding.

Based on the results obtained from the three analog signals set, it can be concluded that the fault closer to the first end has a more obvious impact on the winding, and the impact of different fault locations on the frequency response of the system is significantly different in different frequency segments. The fault at layer 2 has the greatest impact on low frequency and middle frequency band, while the fault at layer 6 has a significant impact on high frequency band. The frequency response analysis can effectively identify and locate the fault location and provide an important basis.

### 3.4 Spectral positioning method based on eigenvalues

Support vector machine (SVM) is a supervised machine learning algorithm based on structural risk minimization principle, which can obtain good learning ability and classification accuracy according to limited sample information, and has the best generalization ability while realizing the global optimal solution. Because SVM can obtain the structured concept of data distribution, it performs better on small sample training sets and is suitable for the data set in this paper. Based on the simulation results, a method for distribution transformer spectrum positioning is proposed. The diagnostic flow of support vector machine is shown in the Figure 11.

The specific process is as follows: First, the signal frequency response characteristic value obtained by simulation is used as the basis of data. The data is then normalized to ensure that the



magnitude of different eigenvalues does not affect the results of model training. Then, the simulation data is used as the training set and the experimental data is used as the test set for the training and evaluation of the model. Select an appropriate model support vector machine (SVM), and train on the training set to learn the patterns and features of the data. Use test sets to evaluate the performance of the model and understand how the model performs on classified experimental measurement data through metrics such as accuracy and confusion matrix. Finally, the evaluation results are analyzed to explain how the model effectively identifies and classifies different types of experimental measurement data.

The objective of SVM is to find a maximum margin hyperplane to maximize the robustness of the classification boundary. This can be achieved by solving the following convex optimization problem:

Given the training set  $\{(x_i, y_i)\}_{i=1}^N$ , where  $x_i$  is the input feature, and  $y_i$  is the category label (for multi-class problems, it can be one of multiple categories).

Minimize the constrained objective function:

$$\min_{w,b,\xi} \frac{1}{2} \|w\|^2 + C \sum_{i=1}^N \xi_i$$

where  $w$  is the weight vector,  $b$  is the bias term,  $\xi_i$  is the slack variable, and  $C$  is the penalty parameter.

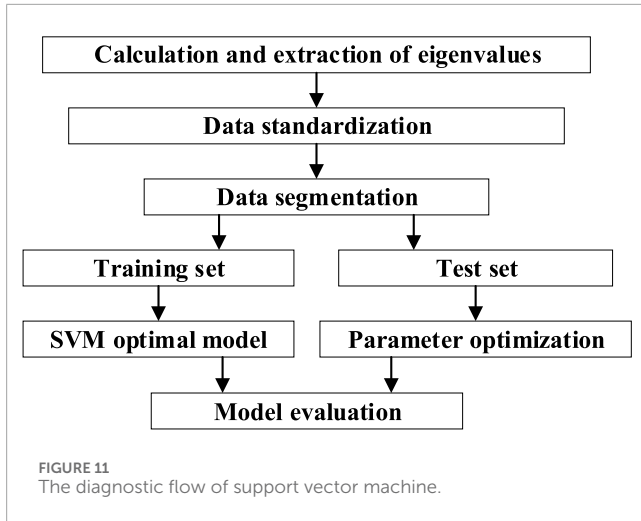


TABLE 4 Identification accuracy of different types.

Type	Identification accuracy
Gaussian pulse injection	76.7%
Direct grounding	86.7%
Ground breakdown	83.3%

The constraint conditions are:

$$y_i(w^T x_i + b) \geq 1 - \xi_i, \xi_i \geq 0$$

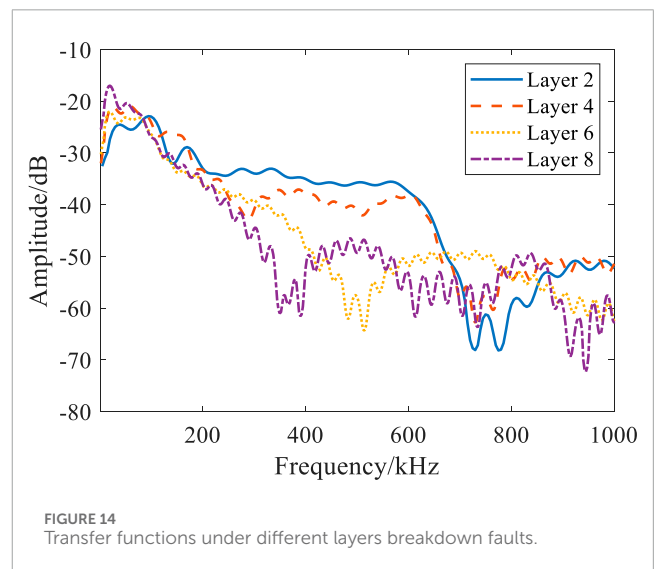
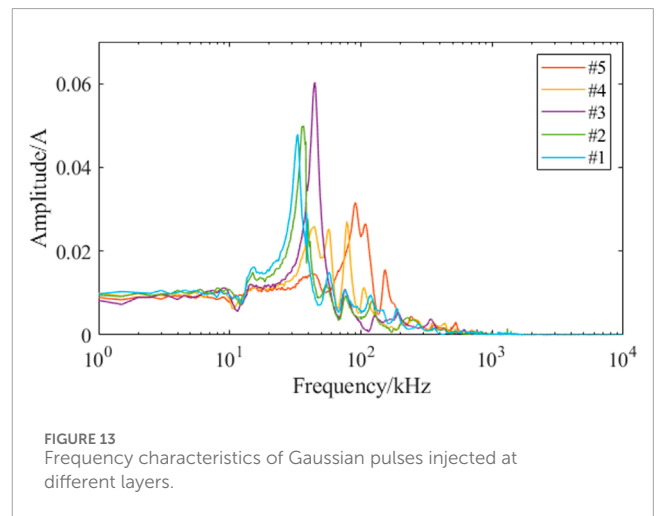
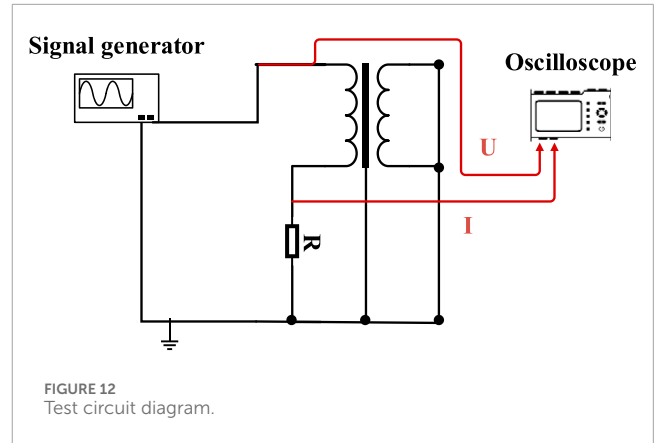
The identification accuracy of simulation data by support vector machine is shown in Table 4.

### 4 Experimental verification

When the transformer winding is pulsed, the Gaussian pulse generated by the signal generator and the fault pulse signal when different winding taps break down to the ground under the impact test are mainly used to obtain the voltage and current signal at the head and end of the winding under different pulse signals. The circuit diagram is shown in Figure 12.

As the injection position of the current signal gradually approaches the end of the winding, the frequency corresponding to the maximum value of the signal spectrum distribution gradually increases. The reason is that when the winding is regarded as a two-port network, the equivalent capacitance of the winding increases while the inductance decreases. For the same signal, a higher frequency signal will be generated. Therefore, different characteristics of spectrum distribution appear in the detection position. The same is true of the signal spectrum distribution under the actual breakdown fault, the closer the breakdown position is to the end, the more high-frequency components in the signal.

As can be seen from Figure 13, there are obvious rules in the spectrum characteristics of signals injected with Gaussian pulses from different nodes. In the low frequency band (1 kHz–10 kHz), the spectrum distribution obtained from different injection



locations is close, and the amplitude is less than 0.01 A. The spectrum features of all nodes cover the frequency range from 1 kHz to 1 MHz. Near 70 kHz, the resonance peak of node layer 3 is the most significant, with A amplitude of about 0.065 A, while the main resonance peak of other nodes is concentrated between 50 kHz and 200 kHz, with A amplitude of about 0.04 A–0.06 A. As the position

TABLE 5 Waveform characteristics under different layers breakdown faults.

Layer	PCC			ALSE	
2	0.9753			7.9890	
4	0.8376			8.7354	
6	0.6774			10.0161	
8	0.7588			10.9209	

Layer	SD	Ku	Sk	RMS	CF
2	2.8414	2.8164	1.5302	32.6469	0.0700
4	2.3870	2.8302	1.6067	22.5057	0.0198
6	3.1499	2.0122	1.3652	27.3774	0.1893
8	3.4028	2.2263	1.4007	24.7962	0.9907

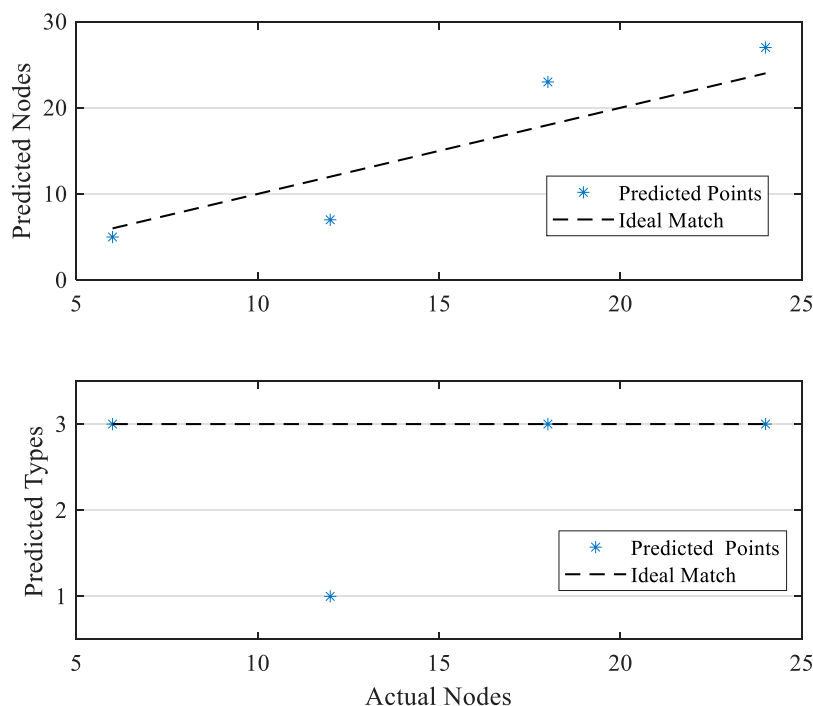


FIGURE 15 Fault location result.

of the node moves towards the end, the frequency corresponding to the resonance peak increases gradually. In addition, each node also has some secondary resonance peaks in the 1 kHz~10 kHz and 200 kHz~1 MHz regions, but the amplitude is small, usually below 0.01A. In general, the spectrum distribution of all nodes is similar, but there are differences in the specific position and amplitude of the main resonance peak. When the frequency is higher than 1,000 kHz, the amplitude of all nodes is significantly reduced to close to zero.

The impulse voltage withstand test after setting defects was carried out on a 10 kV distribution transformer layer winding. In

the test, Marx loop generator was used to generate the impulse voltage, and the maximum amplitude of the impulse voltage could reach 100 kV. The voltage signal at the first end is measured by the voltage divider and the current signal at the end is measured by the damage resistance. A 1 mm thick tungsten steel needle electrode is inserted into the layer winding, so that there is an electrical connection between the electrode and the winding, and the tip is simulated to discharge to the ground, and the distance between the tip and the ground electrode is adjusted to 2 mm, so that the discharge starting voltage of each node is the same. The needle

electrode discharge occurs when the impulse voltage is applied, and the fault location can be located by analyzing the voltage waveform at the first end and the current waveform measured at the end. The signal spectrum characteristics under ground breakdown of different nodes in the impact test are shown in Figure 14. The analysis of the results shows that the measured signal spectrum distribution results are consistent with the simulation results under the impact voltage.

Among them, the curve feature of node layer 2 is particularly significant. In the low frequency band (100 kHz to 1 MHz), the amplitude of the curve is relatively low and stable. With the increase of frequency, the amplitude begins to rise gradually and reaches a peak at a certain frequency point. After that, the amplitude begins to decline, and the decline is the fastest. The numerical characteristic values extracted from the calculation are shown in Table 5.

The characteristic values measured by the experiment are substituted into the support vector machine for solving, and the result of predicting the fault node was obtained, as shown in Figure 15. The actual fault location of the winding could be basically located within the error range of 20%. In addition, the prediction result of the end of the winding is better than that of the middle, and the fault type of the winding can also be predicted.

## 5 Conclusion

In this paper, aiming at the different frequency responses of oil-immersed distribution transformers under different signal types, the feasibility of the location algorithm based on breakdown current signal frequency diagram is studied by simulation and experiment. The main conclusions of this paper are as follows:

- 1) The position of the injected signal in the transformer winding has different effects on the spectrum distribution of the obtained signal. The closer the signal is injected to the end, the higher the high-frequency component of the spectrum distribution
- 2) In the Gaussian pulse injection experiment, the signal spectrum distribution caused by different injection positions is significantly different. Especially in the low frequency zone, the fault effect near the end is more significant, showing a high amplitude and rapid rise trend. In the fault current signal injection experiment, when the breakdown position is near the end, the high frequency component of the signal increases, so that the frequency corresponding to the maximum of the spectrum distribution increases.
- 3) Based on the frequency response characteristics of the signal, support vector machine (SVM) algorithm is used to classify the fault type and location. Under the impulse voltage withstand test, the location of breakdown fault can be located within 20% error.

## Data availability statement

The original contributions presented in the study are included in the article/[supplementary material](#), further inquiries can be directed to the corresponding author.

## Author contributions

XL: Conceptualization, Methodology, Writing–original draft. HW: Writing–original draft. ZG: Writing–original draft. XH: Writing–review and editing.

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## Conflict of interest

Authors XL and HW were employed by State Grid Shanxi Electric Power Company.

The remaining authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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## Supplementary material

The Supplementary Material for this article can be found online at: <https://www.frontiersin.org/articles/10.3389/fenrg.2024.1477556/full#supplementary-material>

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