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RECEIVED 02 August 2024

ACCEPTED 13 September 2024

PUBLISHED 24 September 2024

## CITATION

Pan Z, Fu Y, Chen H and Song Y (2024)  
Thermodynamic analysis of a cascade organic  
Rankine cycle power generation system driven  
by hybrid geothermal energy and liquefied  
natural gas.  
*Front. Energy Res.* 12:1474714.  
doi: 10.3389/fenrg.2024.1474714

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# Thermodynamic analysis of a cascade organic Rankine cycle power generation system driven by hybrid geothermal energy and liquefied natural gas

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The combination of renewable energy and liquefied natural gas (LNG) cold energy can effectively improve energy utilization efficiency and achieve the goal of energy conservation and emission reduction, which is one of the important directions of future development. This work proposed a cascade organic Rankine cycle (ORC) driven by a geothermal heat source and an LNG heat sink. Seven organic fluids are chosen as candidates to form different working fluid pairs. The effects of the main design parameters on system performance are carried out through the thermodynamic analysis. Then, the optimal design conditions and fluid selection schemes are searched based on the single-objective optimization results. Finally, the exergy destruction study is conducted under the optimal design conditions and working fluid pair. Results showed that the cascade ORC system using the working fluid pair of R601/R290 had the highest exergy efficiency, which could reach 20.02%. At the same time, under the optimal design conditions, the secondary cycle condenser and LNG direct expansion brought high exergy destruction, which was respectively 29.3% and 25.8%, and followed by the two turbines in the cascade ORC system, which were 16.1%, 11.2% and 7.7%.

## KEYWORDS

hybrid geothermal energy, liquefied natural gas, power generation, cascade organic Rankine cycle, thermodynamic analysis

## 1 Introduction

With the rapid economic development in recent years, energy and environmental problems have become increasingly prominent. Vigorously developing renewable energy and improving the efficiency of energy and resource utilization can effectively alleviate the above problems (Liu et al., 2024; Wang et al., 2024a; Wang et al., 2022; Wang et al., 2024b). Considering much medium- or low-grade heat exists in different kinds of renewable energies, like solar energy (Xiao et al., 2022), geothermal energy (Wang et al., 2023), biomass energy (Sun et al., 2022), etc., power generation is a suitable utilization way to harness the heat. Especially for the geothermal energy, it has the advantages of stable operation, abundant reserves, and non-pollution. Thus, the development of an efficient, and economical technology to explore the application potential of geothermal energy is of great significance.

Until now, many power generation technologies, like the heat engine (Tian et al., 2021), Kalina cycle (Sohrabi et al., 2023), trilateral flash cycle (Lai et al., 2021; Iqbal et al., 2020), etc., are potential selections. Among them, the organic Rankine cycle (ORC) technology with the advantages of simple structure, easy maintenance, low cost, and wide range of installed capacity (Li et al., 2021), has attracted increasing attention in the last decade. In the geothermal field, Li et al. (2024) carried out an experimental study to discuss the dynamic performance of ORC devices with the geothermal heat source temperature decrease. Results showed that the installed capacity and power output were proportional to the geothermal mass flow rate while the enhanced geothermal system's life cycle was inversely proportional to it. Bahrami and Rosen (2024) proposed a novel geothermal-driven zero-emission system for cooling, power, and hydrogen production, which was composed of ORC, half-effect absorption chiller, and PEM electrolysis. Through exergoeconomic analysis and multi-objective optimization, it was found that the proposed system could reach 48% of the exergy efficiency and a hydrogen production rate of 1.1 kg/h at the optimal design conditions. Assareh et al. (2024) explored the application of ORC for building energy management with cooling heating power hydrogen liquefaction generation. Reyes-Antonio et al. (2024) studied the multi-objective design of the ORC system for low-enthalpy applications based on end-user demand variations. At the same time, the effects of the coupling mechanism with energy storage systems were analyzed under the off-grid operating conditions. Wang et al. (2023) studied the multi-mode and exergoeconomic analysis of a CCHP system, composed of ORC, vapor compression heat pump, and vapor compression refrigeration cycle, applied in the geothermal field. The proposed system performances under seven different operation modes were investigated and compared based on the different design conditions.

Except for paying attention to the above application on the heat source side, the use of cryogenic exergy of liquefied natural gas (LNG) can also effectively improve energy utilization efficiency. LNG with features of nontoxicity, cleanliness, and inexpensive has drawn much attention, and the relevant data speculate that the demand quantity of LNG will reach 500 million tons by 2030 (Li et al., 2016). Generally, the LNG storage tank is normally at low temperature (about 111.51 K) and 0.1 MPa conditions (Rao et al., 2013), and the corresponding capacity may be larger than 10,000 m<sup>3</sup>. The volume would be reduced by 625 times than natural gas (NG) which makes LNG easier to transport by sea and road, and safer and more economical than pipeline transportation. When the LNG is heated to ambient temperature, there will be more than 800 kJ/kg cryogenic exergy released (Li et al., 2016) which has great application potential. Mosaffa and Farshi (2021) conducted a thermodynamic feasibility analysis of an innovative salinity gradient solar ponds-based ORC and LNG cold energy. Results showed that the proposed system using R245ca/R236ea (0.6/0.4) had the best thermal performance among all selected fluids. Fang et al. (2023) carried out exergoeconomic, exergoenvironmental investigation and multi-objective optimization of a novel CCHP system for LNG cold energy recovery. They compared the PSO algorithm

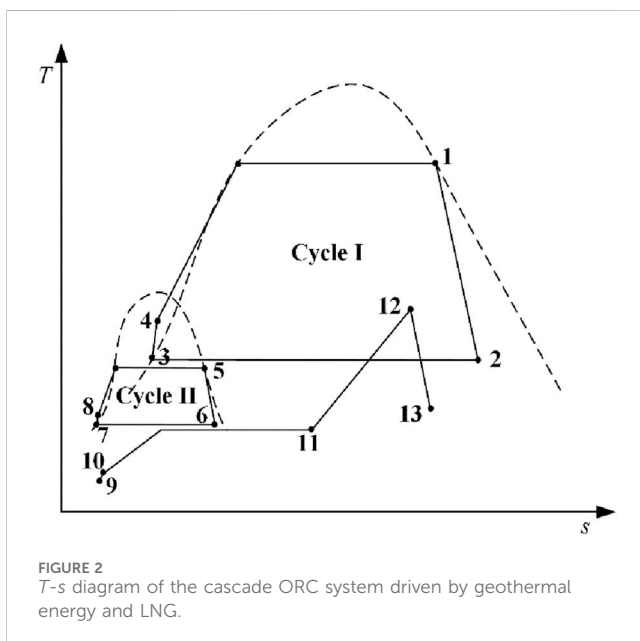
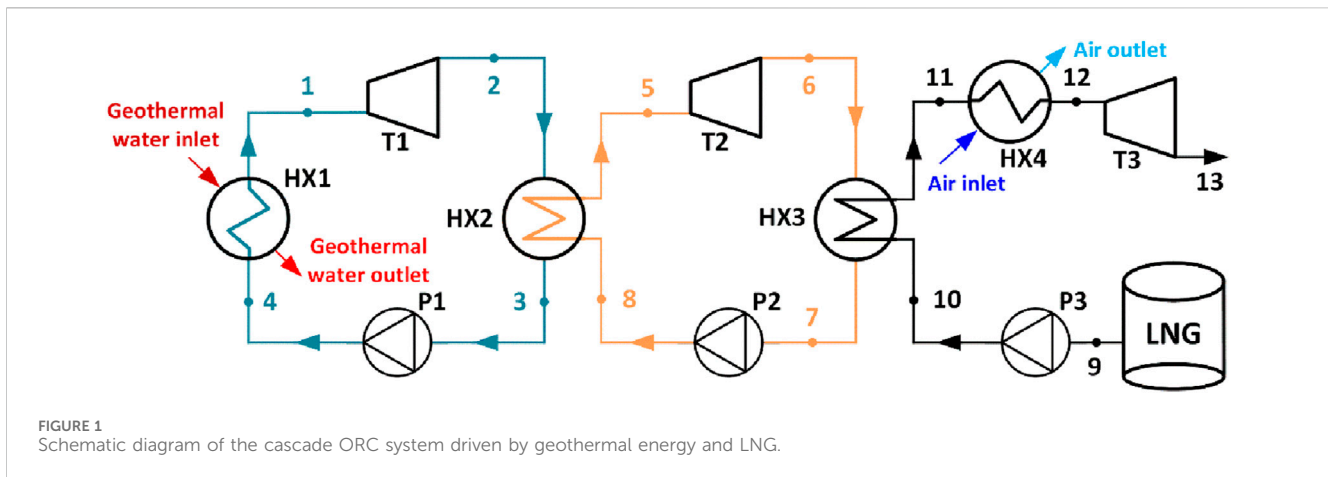
with NSGA-II and results showed that the proposed system had exergy efficiency, product unit cost, and product unit environmental impact of 70.20%, 21.50 \$/GJ, and 57.91 mPts/GJ, respectively. Zheng et al. (2022) studied thermoeconomic performance, working fluid selection, and cost projection of a precooler-integrated dual-stage combined cycle system driven by LNG cold energy. Results found that there was a mismatch between thermodynamic and economic optimal design points, and the economic optimal design points were at a lower pumped pressure.

Combining geothermal energy with LNG would be a desirable application prospect. Mardan Dezfouli et al. (2023) studied a hybrid power generation system of geothermal ORC and LNG. Two separate cycles consisting of CO<sub>2</sub> and C<sub>5</sub>H<sub>12</sub>, which were fed by geothermal water and LNG, were proposed and analyzed in the aspects of energy, exergy, and exergoeconomics. Results showed that the proposed cycle had a net output power of 271.6 kW, an exergy destruction rate of 1,532 kW, and  $f_k$  of 16.5%, respectively, after optimization. This combination could further enhance geothermal resource exploitation efficiency in terms of energy and economics. Emadi and Mahmoudimehr (2019) carried out a modeling and thermo-economic optimization of a novel multi-generation system driven by a geothermal heat source and LNG heat sink. The proposed system realized great improvements in cooling, power generation, and hydrogen production capacities. Results showed that the system designed with an exergy efficiency of 24.92%, a total cost rate of 423.5 (\$/hr), and a hydrogen production capacity of 276.1 (kg/hr) was obtained as the optimal solution. Besides, single-stage is used to realize the power generation in most cases. Considering the large temperature difference (>200 K) between the heat source and heat sink, and the high volume ratio of organic fluid which makes the turbine complicated and expensive, the cascade ORC is proposed with higher efficiency (Xue et al., 2015).

In the current study, most researchers pay more attention to system structure innovation and optimization of design conditions (Habibi et al., 2018; Rejeb et al., 2022; Mehrpooya et al., 2017). Actually, for a cascade ORC system driven by a geothermal heat source and LNG heat sink, the system performances are dramatically affected by the choice of working fluids. However, the impact of different fluid combinations on system performance needs further investigation. In this paper, the pairwise combination of different working fluids is applied to the cascaded ORC system, and after preliminary trial calculations, seven working fluids with better performance, namely R290, R600, R600a, R601, R601a, R125, and R116, are selected and combined into working fluid pairs, and the system performance is analyzed by numerical simulation. The main contributions of this paper are as follows:

- (1) A cascade ORC system driven by geothermal heat source and LNG heat sink is proposed and studied.
- (2) Simulations are conducted to investigate the effect of different parameters on the performance of the system, and the optimal fluid selection schemes are obtained.

The structural framework of this paper is as follows: the system descriptions containing system structure, assumptions, and fluid choice are introduced in Section 2. The detailed mathematical models are illustrated in Section 3. Section 4 is the model



validation. The parametric analysis the fluid selection results, and the main conclusions are put in [Section 5](#) and [Section 6](#), respectively.

## 2 System descriptions

### 2.1 System structure

The schematic diagram of the cascade ORC system driven by geothermal energy and LNG is shown in [Figure 1](#). In the leftmost cycle, the heat in geothermal water is transmitted to the organic fluid in the heat exchanger 1 (HX1). The organic fluid at a high-pressure vapor state (at State 1) enters into turbine 1 (T1) generating mechanical work. After that, the expanded organic fluid (at State 2) is cooled by another stream of organic fluid in the heat exchanger 2 (HX2). The saturated liquid state organic fluid (at State 3) is pressurized by pump 1 (P1) and flows into HX1 again (at State 4) to absorb heat from geothermal water. The process of the middle cycle is similar to that of the leftmost

cycle. In the middle cycle, another high-pressure organic fluid (at State 8) flows into the HX2 being heated into a vapor state (at State 5). Subsequently, the vapor fluid enters turbine 2 (T2) generating mechanical work. Then, the expanded organic fluid (at State 6) is cooled by LNG in the heat exchanger 3 (HX3). The saturated liquid state organic fluid (at State 7) is pressurized by pump 2 (P2) and (at State 8) flows into HX2 again. In the rightmost cycle, the LNG (at State 9) is withdrawn from the storage tank and pumped into HX3. Then LNG (at State 10) is gasified to saturated NG, which is still cryogenic (at State 11). The heat exchanger 4 (HX4) is added to superheat the gas to reach approximately 10 K lower than the ambient temperature (at State 12). Thus, more electricity can be generated when superheated NG enters into the turbine 3 (T3). Finally, the expanded NG is available to the user for direct use or post-processing use. The exhaust stream can be further conveyed to the city gas transmission and distribution network, and the cooled air at the outlet of HX4 can be utilized as well, which is beyond the scope of this paper. The corresponding T-s diagram of the proposed system is shown in [Figure 2](#).

### 2.2 System assumptions

The relative input parameters and calculation conditions are given in [Table 1](#). Some reasonable assumptions for system simulation are as follows:

- Dry and isentropic fluids are in a saturated vapor state while wet fluid is in a superheated vapor state at the inlets of T1 and T2, respectively;
- Working fluids are in a saturated liquid state at the state points 3, 7, and 11, respectively;
- Heat losses and pressure drops in pipes are ignored;
- LNG is composed of methane, ethane, propane, isobutane, butane, isopentane, pentane, and nitrogen, and the corresponding mass fractions are 0.9133, 0.0536, 0.0214, 0.0047, 0.0046, 0.0001, 0.0001, and 0.0022 ([Bao et al., 2017](#));
- The liquid in the LNG storage tank is saturated at ambient pressure, and the evaporation pressure is 3 MPa;
- The outlet pressure of T3 is assumed to be 0.4 MPa.

TABLE 1 Input parameters and calculation conditions.

Parameter	Unit	Value	Reference
Ambient temperature, $T_0$	K	298.15	Nami et al. (2017)
Ambient pressure, $p_0$	MPa	0.1	Nami et al. (2017)
Geothermal water inlet temperature, $T_{gw, in}$	K	353.15	—
Geothermal water outlet temperature, $T_{gw, out}$	K	343.15	—
Geothermal water mass flow rate, $m_{gw}$	kg/s	10	—
Cooling air inlet temperature, $T_{ca, in}$	K	298.15	Li et al. (2016)
Pump isentropic efficiency, $\eta_p$	%	75	Wang et al. (2020)
Turbine isentropic efficiency, $\eta_t$	%	80	Wang et al. (2020)
Generator efficiency, $\eta_{gen}$	%	95	Li et al. (2016)
LNG evaporation pressure, $p_{eva, LNG}$	MPa	3.0	Li et al. (2016)

TABLE 2 Thermo-physical properties of the different working fluids (Tian et al., 2020).

Working fluids	Molecular mass/g mol <sup>-1</sup>	Triple-point temperature/K	$T_{crit}/K$	$p_{crit}/MPa$	GWP 100 year	ODP
R290	44.096	85.525	369.89	4.2512	5	0
R601a	72.149	112.65	460.35	3.378	20	0
R601	72.149	143.47	469.7	3.37	20	0
R125	120.02	172.52	339.17	3.6177	3,170	0
R116	138.01	173.1	293.03	3.048	5,700	0
R600	58.122	134.9	425.13	3.796	4	0
R600a	58.122	113.73	407.81	3.629	20	0

## 2.3 Fluid selection principle

Working fluid selection in ORC systems is an all-important work during the system simulation processes, because the system performance, investment costs, and equipment sizing are influenced by the thermophysical properties of organic fluids. Considering that the application background of this paper is in LNG and geothermal fields, the critical temperature of the working fluid should be higher than the maximum operating temperature. At the same time, the triple-point temperature of the working fluid should be maintained below the minimum operating temperature. Besides, the condensing pressure should be above 5 kPa as it is technically difficult to maintain a vacuum below this value in the condenser. Referring to related works (Li et al., 2016), the following working fluids are selected as candidates for research in this paper, and the thermophysical properties of the selected fluids are shown in Table 2.

## 3 Mathematical models

In the entire system, the universal energy balance equation can be defined as (Equation 1):

$$\sum m_{in} h_{in} + Q = \sum m_{out} h_{out} + W \quad (1)$$

where  $h$  represents the specific enthalpy;  $m$  represents the mass flow rate;  $W$  is the power output, and  $Q$  represents the heat absorption amount.

More precisely, the heat transfer in HX1, HX2, HX3, and HX4 are expressed (Equations 2–5):

$$Q_{HX1} = m_{gw} (h_{gw, in} - h_{gw, out}) = m_{wf1} (h_1 - h_4) \quad (2)$$

$$Q_{HX2} = m_{wf1} (h_2 - h_3) = m_{wf2} (h_5 - h_8) \quad (3)$$

$$Q_{HX3} = m_{wf2} (h_6 - h_7) = m_{LNG} (h_{11} - h_{10}) \quad (4)$$

$$Q_{HX4} = m_{LNG} (h_{12} - h_{11}) = m_{ca} (h_{ca, out} - h_{ca, in}) \quad (5)$$

The power consumption of each pump can be expressed as (Equations 6–8):

$$W_{P1} = m_{wf1} (h_4 - h_3) = m_{wf1} (h_{4s} - h_3) / \eta_p \quad (6)$$

$$W_{P2} = m_{wf2} (h_8 - h_7) = m_{wf2} (h_{8s} - h_7) / \eta_p \quad (7)$$

$$W_{P3} = m_{LNG} (h_{10} - h_9) = m_{LNG} (h_{10s} - h_9) / \eta_p \quad (8)$$

The power output of each turbine can be expressed as (Equations 9–11):

TABLE 3 Model validation for the proposed cascaded ORC system.

Performance parameters	Data from literature	Present work for literature's configuration	
Model validation for the cascade ORC using the data reported by Wang et al. (2023)			
Input parameters	Heat source inlet temperature	423.15 K	423.15 K
	Turbine efficiency	0.80	0.80
	Pump efficiency	0.80	0.80
	Working fluid	R601	R601
	Evaporation temperature	398.65 K	398.65 K
	Condensation pressure	80 kPa	80 kPa
Output parameters	Net output power	1184.00 kW	1184.76 kW

$$W_{T1} = m_{wf1} (h_1 - h_2) = m_{wf1} (h_1 - h_{2s})\eta_t \quad (9)$$

$$W_{T2} = m_{wf2} (h_5 - h_6) = m_{wf2} (h_5 - h_{6s})\eta_t \quad (10)$$

$$W_{T3} = m_{LNG} (h_{12} - h_{13}) = m_{LNG} (h_{12} - h_{13s})\eta_t \quad (11)$$

The net power output of the system ( $W_{net}$ ) can be defined as (Equation 12):

$$W_{net} = (W_{T1} + W_{T2} + W_{T3} - W_{P1} - W_{P2} - W_{P3})\eta_{gen} \quad (12)$$

The thermal efficiency of the system ( $\eta_{th}$ ) is expressed as (Equation 13):

$$\eta_{th} = W_{net}/Q_{in} = W_{net}/[m_{gw}(h_{gw,in} - h_{gw,out})] \quad (13)$$

The cold energy efficiency of the system ( $\eta_C$ ) can be defined as (Equation 14):

$$\eta_C = W_{net}/E_{LNG} = W_{net}/[(h_9 - T_0s_9) - (h_{13} - T_0s_{13})] \quad (14)$$

The exergy efficiency of the system ( $\eta_{ex}$ ) is expressed as (Equation 15):

$$\eta_{ex} = W_{net}/(E_{gw} + E_{LNG}) \quad (15)$$

The exergy destruction of each heat transfer can be expressed as (Equations 16–19):

$$\dot{E}_{d,HX1} = \dot{E}_{gw,in} + \dot{E}_4 - \dot{E}_{gw,out} - \dot{E}_1 \quad (16)$$

$$\dot{E}_{d,HX2} = \dot{E}_2 + \dot{E}_8 - \dot{E}_3 - \dot{E}_5 \quad (17)$$

$$\dot{E}_{d,HX3} = \dot{E}_6 + \dot{E}_{10} - \dot{E}_7 - \dot{E}_{11} \quad (18)$$

$$\dot{E}_{d,HX4} = \dot{E}_{ca,in} + \dot{E}_{11} - \dot{E}_{ca,out} - \dot{E}_{12} \quad (19)$$

The exergy destruction of each turbine can be expressed as (Equations 20–22):

$$\dot{E}_{d,turbine1} = \dot{E}_1 - \dot{E}_2 - \dot{W}_{T1} \quad (20)$$

$$\dot{E}_{d,turbine2} = \dot{E}_5 - \dot{E}_6 - \dot{W}_{T2} \quad (21)$$

$$\dot{E}_{d,turbine3} = \dot{E}_{12} - \dot{E}_{13} - \dot{W}_{T3} \quad (22)$$

The exergy destruction of each pump can be expressed as (Equations 23–25):

$$\dot{E}_{d,pump1} = \dot{E}_3 - \dot{E}_4 + \dot{W}_{P1} \quad (23)$$

$$\dot{E}_{d,pump2} = \dot{E}_7 - \dot{E}_8 + \dot{W}_{P2} \quad (24)$$

$$\dot{E}_{d,pump3} = \dot{E}_3 - \dot{E}_{10} + \dot{W}_{P3} \quad (25)$$

## 4 Model validation

The data reported in the literature are selected to validate the model of the proposed cascade ORC system. The model is validated to be performed separately for the ORC subsystem. Referring to Table 3, the comparison results show the current model and the data obtained from the literature.

## 5 Results and discussions

The following describes and discusses the simulation results based on the aforementioned model. Firstly, the impact of key parameters on system performance is analyzed. Subsequently, research is conducted on the matching of working fluids for the two-stage low-temperature ORC system. The best-performing working fluid in terms of exergy efficiency is selected for single-objective optimization of the system, aiming to find its optimal operating conditions. Finally, exergy destruction analysis is conducted on the system's optimal operating conditions.

### 5.1 Parametric study

Before proceeding with a system optimization analysis, it is critical to investigate the impact of critical parameters on system performance. Therefore, this section focuses on how to perform parametric analysis to understand these influencing factors. Table 4 lists the state parameters (temperature, pressure, and mass flow) at each point of the cascade ORC system under the design conditions.

Figure 3 illustrates the effect of the evaporation temperature ( $T_{eva1}$ ) of the primary ORC cycle system on the system parameters and performance. When  $T_{eva}$  increases from 317.15 to 328.15 K,  $\eta_e$  monotonically increases from 19.55% to 20.08%. The reason is that as  $T_{eva1}$  increases, the  $\Delta T_{eva1}$  in the evaporator gradually decreases from 29.08 to 18.55 K, as shown in Figure 3B. Therefore, under the

TABLE 4 The parameter values for each state point of the cascade ORC system.

State no	Working fluid	Mass flow (kg/s)	Temperature (K)	Pressure (kPa)
1	butane	0.8639	328.15	563.6503
2	butane	0.8639	279.20	69.5525
3	butane	0.8639	263.15	69.5525
4	butane	0.8639	263.43	563.6503
5	propane	0.7202	268.01	244.5183
6	propane	0.7202	227.59	55.2491
7	propane	0.7202	218.15	55.2491
8	propane	0.7202	218.26	244.5183
9	LNG	0.4951	111.15	101.3250
10	LNG	0.4951	112.52	3,000
11	LNG	0.4951	215.77	3,000
12	LNG	0.4951	283.15	3,000
13	LNG	0.4951	190.66	400

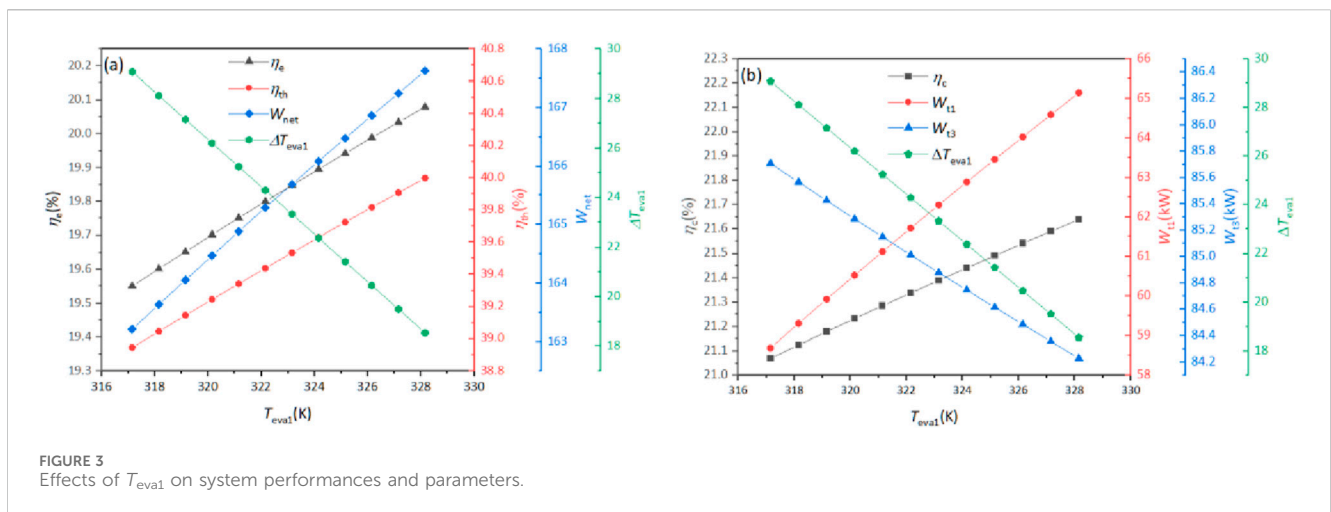


FIGURE 3 Effects of  $T_{eva1}$  on system performances and parameters.

condition of a constant heat source, the average temperature difference between hot and cold fluids in the evaporator decreases, and  $\eta_e$  gradually increases. At the same time, when  $T_{eva1}$  increases from 317.15 to 328.15 K,  $W_{net}$  increases monotonically from 163.21 to 167.63 kW. This is mainly because the  $W_{t1}$  increases with the evaporation temperature, and as the  $T_{eva1}$  increases the inlet pressure of the compressor and reduces its power consumption, the  $W_{t1}$  rises from 58.69 to 65.15 kW. The increase in power generation further improves the thermodynamic and economic performance of the system. In addition, the efficiency of cold energy utilization has also been slightly improved.

Figure 4 illustrates the effect of the condensing temperature ( $T_{con1}$ ) of the primary ORC cycle system on the system parameters and performance. When  $T_{con1}$  increases from 253.15 to 263.15 K,  $\eta_e$  monotonically decreases from 19.60% to 18.89%. The reason for this can be seen in the Carnot cycle: when the endothermic temperature is constant, the increase in the exothermic temperature reduces the

efficiency of the Carnot cycle. In addition, as the condensation temperature of the system increases, the  $W_{net}$  of the system decreases from 163.64 to 157.72 kW, mainly due to the decrease in the outlet temperature of turbine 1, which reduces  $W_{t1}$  from 59.31 to 50.96 kW, as shown in Figure 4B.

Figure 5 illustrates the effect of the evaporation temperature ( $T_{eva2}$ ) of the secondary ORC cycle system on system parameters and performance. When  $T_{eva2}$  increases from 233.15 to 243.15 K,  $\eta_e$  monotonically increases from 18.60% to 19.60%. This is because, as  $T_{eva2}$  increases, the  $\Delta T_{eva2}$  in the evaporator of the secondary ORC recirculating system gradually decreases. Therefore, under the condition of a constant heat source, the average temperature difference between hot and cold fluids in the evaporator decreases, and  $\eta_e$  gradually increases. At the same time, when  $T_{eva2}$  increases from 233.15 to 243.15 K,  $W_{net}$  increases monotonically from 155.24 to 163.64 kW. This is mainly because  $W_{t2}$  increases with increasing evaporation temperature, and as  $T_{eva2}$

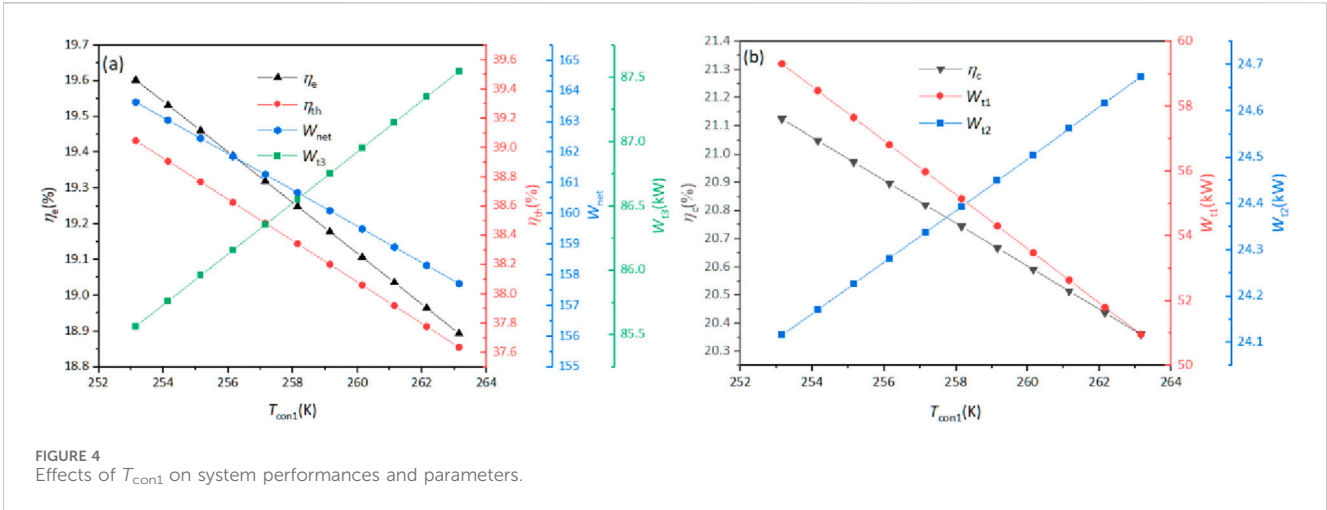


FIGURE 4 Effects of  $T_{con1}$  on system performances and parameters.

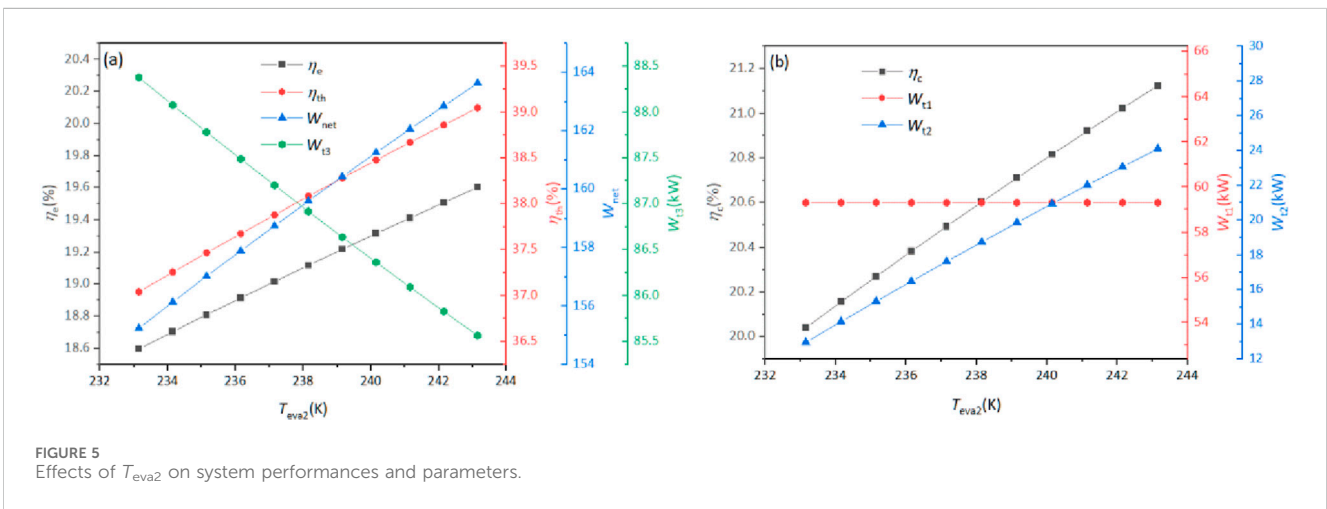


FIGURE 5 Effects of  $T_{eva2}$  on system performances and parameters.

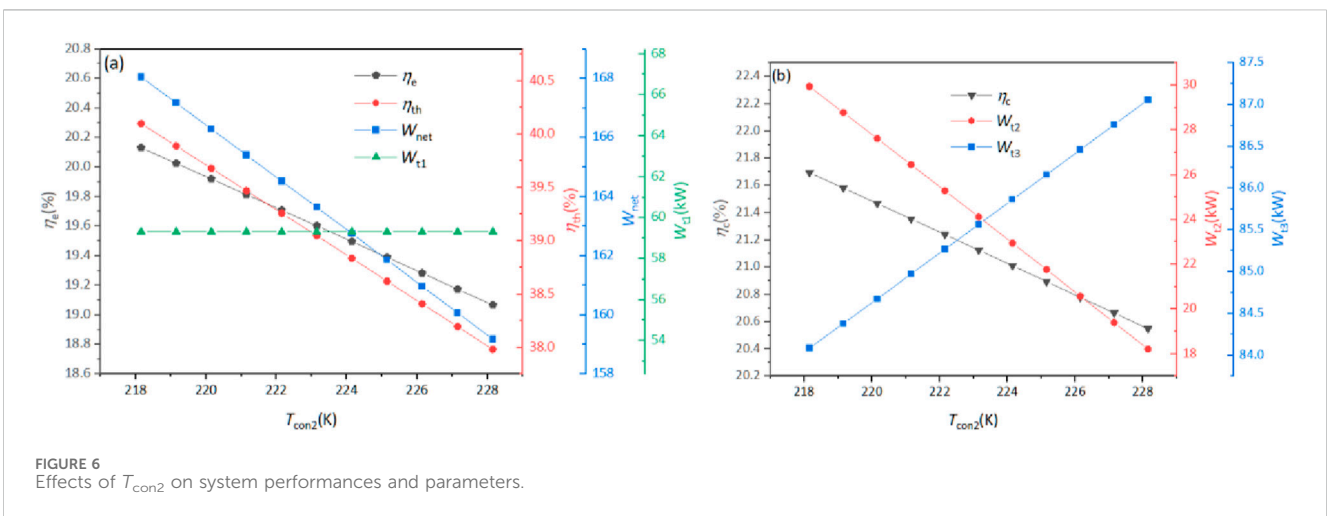


FIGURE 6 Effects of  $T_{con2}$  on system performances and parameters.

increases the inlet pressure of the compressor and reduces its power consumption,  $W_{t2}$  rises from 12.97 to 24.12 kW.

Figure 6 illustrates the effect of the condensation temperature ( $T_{con2}$ ) of the secondary ORC cycle system on system parameters

and performance. When  $T_{con2}$  increases from 218.15 to 228.15 K,  $\eta_e$  monotonicity decreases from 20.13% to 19.07%. The reason for this can also be seen in the Carnot cycle: when the endothermic temperature is constant, the increase in the exothermic

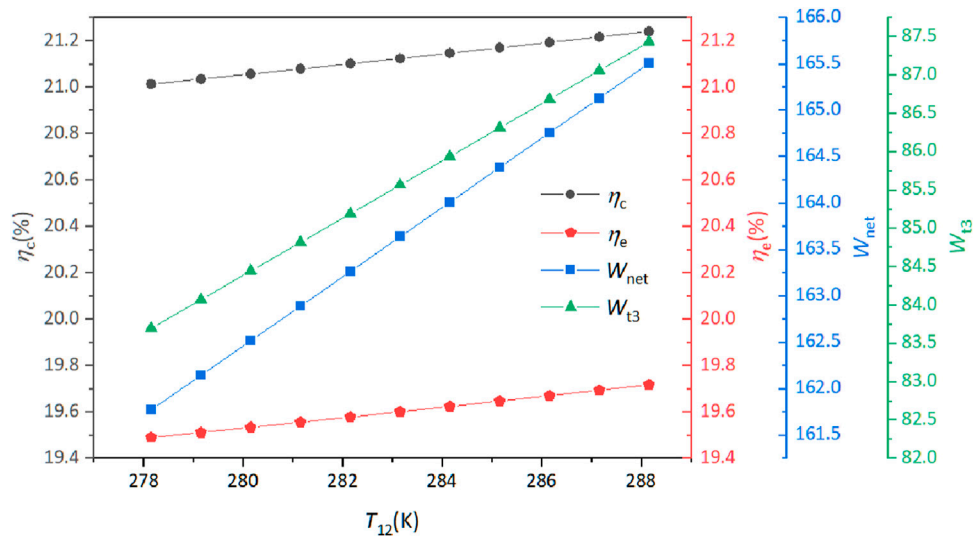


FIGURE 7 Effects of  $T_{12}$  on system performances and parameters.

TABLE 5 Results of single-objective optimization analysis for different working fluid pairs.

Working fluid paris	$\eta_e$ (%)	$\eta_{th}$ (%)	$W_{net}$ (kW)	$W_{pump}$ (kW)	$W_{elc}$ (kW)
R600/R290	20.61245	41.0585	172.0713	5.5924	163.4677
R601a/R290	20.63544	41.1043	172.2632	5.0546	163.6500
R601/R600	20.66111	41.1554	172.4775	4.7021	163.8537
R601/R290	20.66381	41.1608	172.5001	4.9493	163.8751
R600a/R290	20.54239	40.9190	171.4864	6.0715	162.9121
R290/R290	20.46303	40.7609	170.8240	7.1459	162.2828

temperature reduces the efficiency of the Carnot cycle. In addition, as the condensation temperature of the system increases, the  $W_{net}$  of the system decreases from 168.05 to 159.18 kW, mainly due to the decrease in the outlet temperature of turbine 2, which reduces  $W_{t2}$  from 29.95 to 18.21 kW, as shown in Figure 6B.

Figure 7 illustrates the effect of the inlet pressure of the LNG turbine (Turbine 3) on the performance of the system, as the  $T_{12}$  increases from 278.15 to 288.15 K, the system's  $W_{net}$  increases from 161.77 to 165.51 kW, and the increase is almost entirely due to the work done by Turbine 3, which is obvious. In addition, we can see that with the increase of  $T_{12}$ , both  $\eta_e$  and  $\eta_c$  of the system increase slightly.

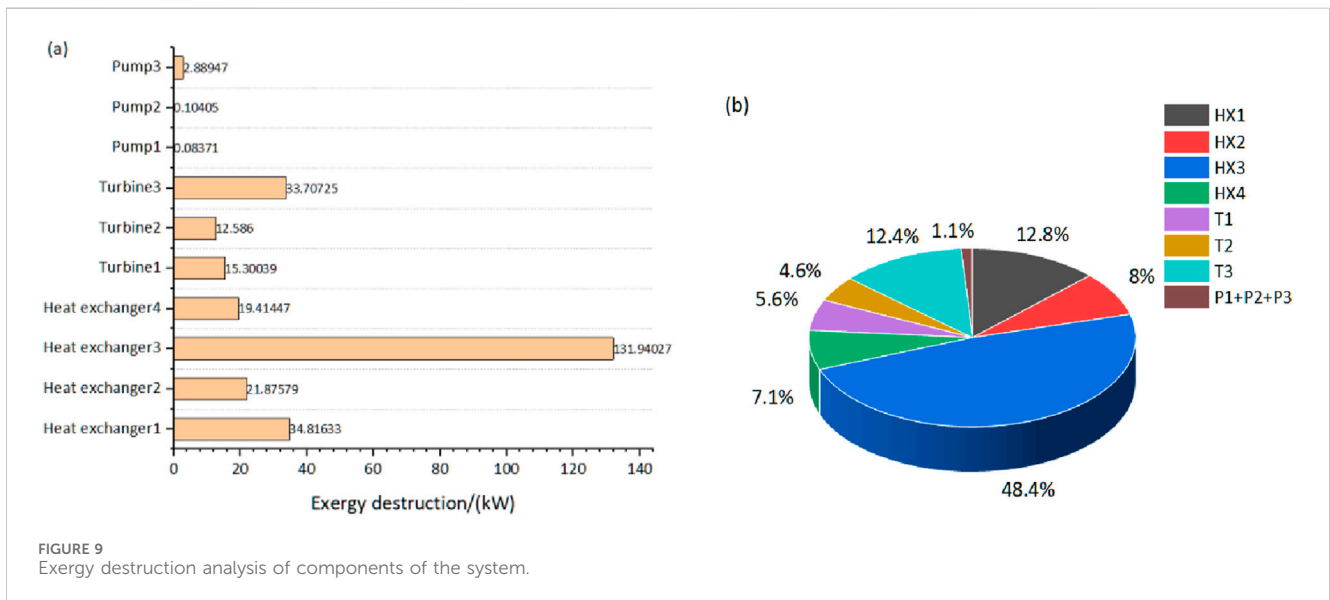
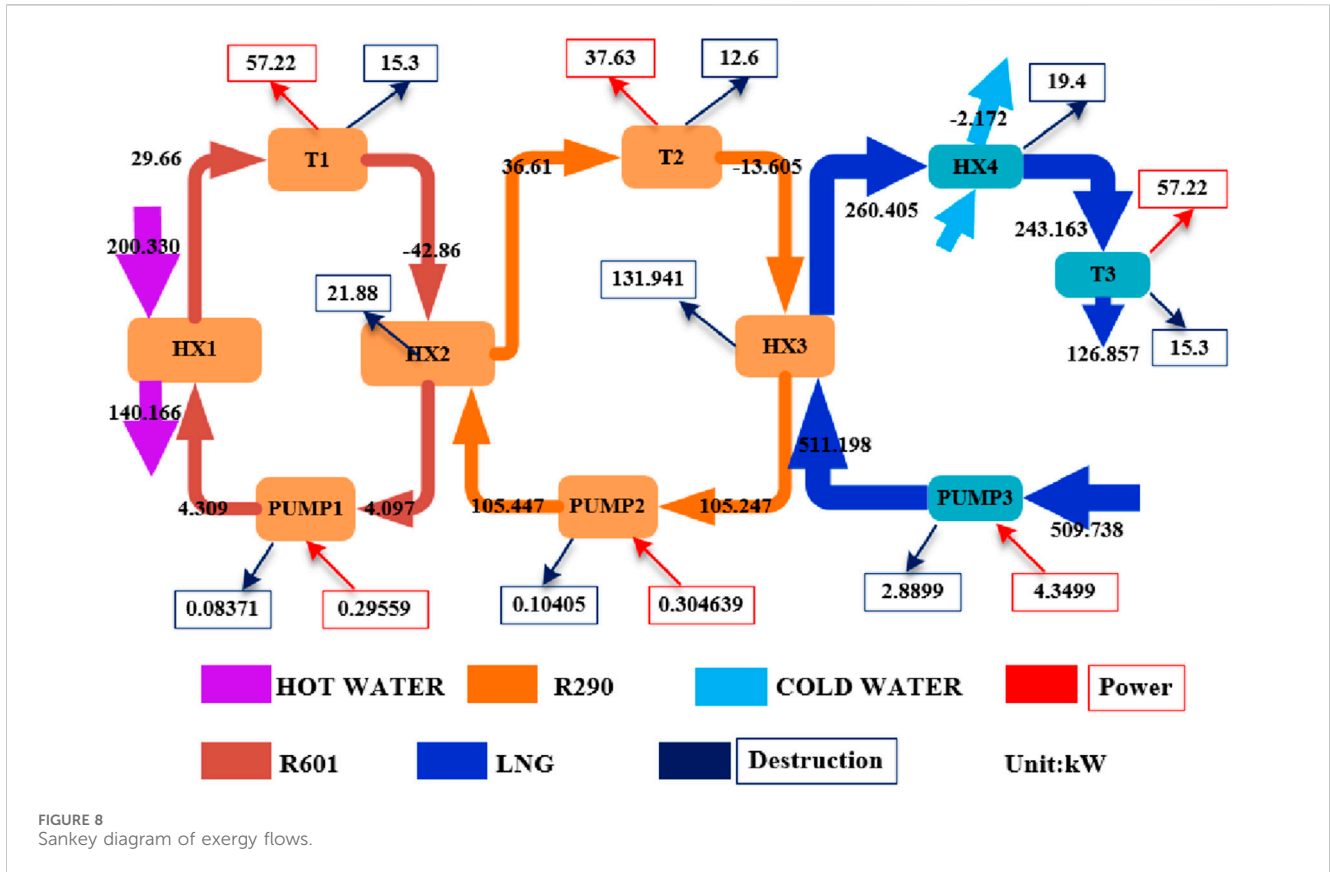
### 5.2 Optimization results and working fluid selection

According to the literature survey and preliminary screening, six working fluid pairs are selected, and the working fluids of the primary and secondary ORC cycles are R600/R290, R601a/R290, R601/R600, R601/R290, R600a/R290, and the two-stage ORC

working fluids both are R290. In order to find the optimal working fluid pair and the optimal operating condition of the cascade ORC system, we take the thermal efficiency of the system as a single objective function for single-objective optimization, and take the  $T_{eva1}$ ,  $T_{con1}$ ,  $\Delta T_{eva1}$ ,  $T_{con2}$ ,  $T_{12}$ , and  $P_{LNG}$  six variables as decision variables. The range of the decision variables is as follows,  $T_{eva1}$  (318.15–328.15 K),  $T_{con1}$  (253.15–263.15 K),  $\Delta T_{eva1}$  (10–20 K),  $T_{con2}$  (218.15–228.15 K),  $T_{12}$  (273.15–283.15 K),  $P_{LNG}$  (2,000–3,000 kPa) (Li et al., 2016). The parameters of single-objective optimization are set as follows, the termination tolerance of the function value is  $10^{-4}$ , the maximum number of iterations is  $10^3$ , the termination tolerance about the current point  $x$  is  $10^{-50}$ , and the maximum number of function calculations is  $10^8$ .

Single-objective optimization of the single-objective function with exergy efficiency is performed, and the results of single-objective optimization are shown in Table 5. We can see that working fluid pairs R601/R600 and R601/R290 have better performance, and R601/R290 has a slightly better performance. So we choose this working fluid pair R601/R290 for the subsequent exergy destruction analysis, and the





optimal working conditions are selected, the evaporation temperatures of the cascade ORC system are 328.15 and 253.15 K, the condensing temperatures of the cascade ORC system are 263.15 and 218.15 K, the inlet temperature of turbine 3 is 283.15 K, and the outlet pressure of the LNG pump is 3,000 kPa.

### 5.3 Exergy destruction analysis

According to the results of single-objective optimization, we select the working fluid pair R601/R290, the optimal operating condition of the system, and then carry out the exergy destruction analysis of the system to explore the areas where the system can be improved. The

Sankey diagram of exergy flows under the design parameters is displayed in Figure 8. And the Figure 9 shows the exergy destruction and proportions of each component of the system. As can be seen from Figure 9, the components with the highest exergy destruction is the condenser of the secondary ORC cycle, accounting for 48.4%. In addition, the second, third, fourth, and fifth major exergy destruction are the primary ORC cycle evaporator, turbine 3, the condenser of the primary ORC cycle and heat exchanger 4, respectively, and the proportion of exergy destruction are 12.8%, 12.4%, 8% and 7.1%, respectively. The main cause of exergy destruction in condensers and evaporators is the significant temperature difference that occurs during the heat transfer of the working fluid. Irreversibility brings about the exergy destruction of compressors and expanders, and improving the isentropic efficiency of components can reduce exergy destruction. Other components of the system, such as pumps, have relatively low exergy destruction and relatively little room for optimization of exergy destruction.

## 6 Conclusion

In this paper, a cascade ORC system driven by a geothermal heat source and an LNG heat sink is proposed and studied. The design parameters of the system performance are studied through numerical analysis, and different fluid options are selected and compared. Finally, the heat loss analysis is carried out under the optimal operating conditions. From the results of the study, the following conclusions can be drawn:

- (1) The cascade ORC system driven by a geothermal heat source and LNG heat sink proposed in this paper, different fluid selection schemes have a great influence on the system performance, and the R601/R290 fluid selection scheme has the highest system exergy efficiency, which can reach 20.02%.
- (2) Under the optimal operating conditions of this system, the condenser of the secondary ORC cycle brings the highest exergy destruction of 48.4%.
- (3) The VR of each turbine in a cascade ORC is much smaller compared to a single-stage ORC, making the design and manufacture of the turbine much easier. As a result, the technical difficulties and high costs associated with multi-stage expansion can be avoided.

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## Data availability statement

The original contributions presented in the study are included in the article/supplementary material, further inquiries can be directed to the corresponding author.

## Author contributions

ZP: Writing—original draft. YF: Writing—review and editing. HC: Resources, Visualization, Writing—review and editing. YS: Supervision, Writing—review and editing.

## Funding

The author(s) declare that financial support was received for the research, authorship, and/or publication of this article. This work was supported by the National Natural Science Foundation of China (grant number 52106199), the Natural Science Foundation of Hebei Province (grant number E2023502067), the Science Research Project of Hebei Education Department (grant number BJK2024065), and the Fundamental Research Funds for the Central Universities (grant number 2023MS122).

## Conflict of interest

Author ZP was employed by Zhanjiang Electric Power Co., Ltd. The remaining authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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## Nomenclature

**A** area of heat exchanger ( $\text{m}^2$ )

**E** exergy rate (kW)

**H** enthalpy (kJ/kg)

**I** exergy loss (kW)

**m** mass flow rate ( $\text{kg s}^{-1}$ )

**p** pressure (kPa)

**Q** heat transfer rate (kW)

**s** entropy ( $\text{kJ kg}^{-1} \text{K}^{-1}$ )

**T** temperature (K)

**W** power (kW)

**X** decision variables

**y** objective function

### **Abbreviations**

**CCHP** combined cooling, heating and power

**GWP** global warming potential

**HX** heat exchanger

**ODP** ozone depletion potential

**ORC** organic Rankine cycle

**LNG** liquefied natural gas

**NG** natural gas

### **Subscripts/superscripts**

**ca** cooling air

**crit** critical

**gen** generator

**gw** geothermal water

**in** inlet

**p** pump

**out** outlet

**t** turbine

**wf** working fluid

**0** ambient state point

**1, 2, 3, 4** state point