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# Stability analysis and stabilization control of a grid-forming VSC-HVDC system

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As the penetration of the integrated intermittent and fluctuating new energy (e.g., wind and photovoltaic power) increases, the conventional grid-following voltage source converter (VSC)-based high voltage direct current (HVDC) transmission system faces the problem of interactive instability with the grid. A novel grid-forming control strategy is proposed to overcome these issues, which adopts the dynamics of a DC capacitor to realize the function of self-synchronization with the grid. Moreover, the per-unit DC voltage can automatically track the grid frequency, acting as a phase-locked loop. Next, the small-signal model of the grid-forming VSC-HVDC system is established, and the stability of the system is analyzed using the eigenvalue analysis method and the complex power coefficient method. In addition, the stabilization controller is proposed for the grid-forming (GFM) control structure, which further enhances the grid-forming VSC-HVDC system's stability and helps it operate stably under both stiff and weak grid conditions. Research results show that the VSC-HVDC system under the proposed grid-forming control can work stably in both stiff and weak grids. The grid-forming VSC-HVDC system is robust and can maintain stable operations with a large range variation of the parameters in the current and voltage control loop. Simulations are carried out on the PSCAD/EMTDC platform to verify the proposed grid-forming control strategy.

## KEYWORDS

grid-forming control, VSC-HVDC, state-space modeling, interaction stability, weak grid, stabilization control

## 1 Introduction

In recent years, new energy sources, including wind and photovoltaic power, have developed rapidly in response to the energy crisis (Liu et al., 2024). The proportion of new energy integrated into the grid and the proportion of power electronic converters in the power system have been continuously increasing (Ma et al., 2024). The renewable energy-based power system is forming a “dual high” development trend (Zhang et al., 2023). At the same time, the power grid tends to exhibit weak grid characteristics (Sang et al., 2018; Zhu et al., 2020), which can cause problems such as low inertia and abnormal interaction phenomena (Wu Q. et al., 2019), posing severe challenges to the stability of renewable power generation.

The VSC-based high voltage direct current (HVDC) system is an effective way to solve the transmission issues of high-ratio new energy. As a key component of the HVDC system, the control strategy of the VSC plays a significant role in ensuring system stability and the

quality of output power. At present, the control modes of grid-connected VSCs mainly include the grid-forming (GFM) control and the grid-following (GFL) control (Zhang et al., 2021). Under these two control modes, the grid-connected VSCs reflect the external characteristics of the current source and voltage source, respectively (Zhang et al., 2023; Pawar et al., 2021). The conventional VSC adopts the GFL control strategy, where the phase-locked loop (PLL) is employed to measure the voltage phase in the point of common connection (PCC) and adjust the output current to control the grid-connected power. However, due to the abnormal interference between the PLL and the grid's impedance, the interactive stability margin of the grid-connected VSC gradually decreases with the reduction of the short-circuit ratio (SCR), triggering oscillation instability. Wang et al. (2020) and Wang et al. (2019) noted that the dynamic coupling between the PLL and grid impedance occurs under weak grid conditions, and the coupling degree will exacerbate with the increase of the PLL's bandwidth. To improve the stability of the GFL VSC, Huang et al. (2022) present a voltage regulation control strategy that improves the synchronous operating performance of GFL VSC by automatically adjusting the input of PLL. Shao et al. (2021) proposed a modified design method of the PLL's parameters to reduce the negative impact of PLL dynamics under weak grid conditions.

Compared with the GFL VSC, the VSC under the GFM control has better stability in a weak grid (Fu et al., 2021). Unlike the GFL strategy, the GFM control strategy does not need PLL and realizes the autonomous synchronization with the grid according to the power or DC-link voltage synchronization principle. The GFM control strategies mainly include the virtual synchronous generator (VSG) control, the droop control, and the matching control (Pan et al., 2020). Meng et al. (2019) proposed a generalized droop control strategy, where the inverter can offer virtual damping and virtual inertia without large overshoot and oscillation by adding an auxiliary controller. In addition, Meng et al. (2019) also noted that the generalized droop control can be equivalent to the droop control or VSG control strategy by adjusting the parameters. Aiming at the problem of low inertia and lacking frequency fluctuation caused by the renewable energy integration, Zha et al. (2021) adopted the electric torque model to analyze the inertia support characteristics and the system stability and noted that the VSC had better inertia support characteristics under the generalized droop control. Ge et al. (2023) established the model of the VSG-based VSC, and the support effect of VSG-based VSC was deeply studied with different inertia parameters. The sequence impedance model of VSG-based VSC was built and compared with that of the conventional VSC by Wu W. et al. (2019) through the harmonic linearization method, and the analysis results indicated the VSG-based VSC's sequence impedance is essentially the same as the grid impedance, which means the VSG-based VSC is more stable than the conventional VSC under weak grid conditions. Li et al. (2022) analyzed the voltage and frequency stability of VSG-based VSC by establishing the small-signal model and proposed an improved control method to enhance the inertia and damping. However, these above droop and VSG control strategies Wu W. et al. (2019), Meng et al. (2019), Pan et al. (2020), Zha et al. (2021), Li et al. (2022), and Ge

et al. (2023) take the active power as control targets and are applicable to grid-connected VSCs with stable and controllable motive power. With respect to the receiving end converter (REC), that is, the grid-connected VSC in the HVDC transmission system with intermittent and fluctuating input motive power, it is still essential to investigate a novel GFM control strategy with the DC-side voltage as the control target.

Recently, a kind of GFM control method with the DC-side voltage as the control objective has been proposed. A GFM control method called inertia synchronization control (ISynC) was presented by Sang et al. (2019) based on the matching principle between the DC voltage and the synchronous generator (SG). In Shao et al. (2019a) and Shao et al. (2019b), the ISynC-based GFM control strategy was applied to the doubly fed induction generator (DFIG)-based wind turbine, which makes the DC-side voltage track the grid frequency instantaneously, thus, the inertia response of the DFIG-based wind turbine can be achieved. Yang et al. (2018) utilized the ISynC-based GFM control method in the VSC-HVDC system, and the frequency tracking capability was useful in realizing the function of inertia support. Moreover, in Yang et al. (2020), the ISynC-based GFM control method was further expanded to the multi-port VSC-HVDC, which was able to establish the DC grid based on the droop control. Nevertheless, there is no current control loop in the ISynC-based GFM VSC (Shao et al., 2019a; Shao et al., 2019b; Sang et al., 2019), which cannot limit the output current and is not conducive to practical engineering applications.

Oriented to the VSC-HVDC transmission system with intermittent and fluctuating input motive power, a novel GFM control method taking the DC-side voltage as the control target is proposed in this article, which has the function of autonomously synchronizing the grid. The internal current control loop is added to the GFM structure; thus, the function of limiting the output current can be achieved, which makes the proposed GFM control strategy suitable for practical engineering applications. The GFM VSC-HVDC's small-signal model is built, and the stability of the system is analyzed using the eigenvalue analysis method and the complex power coefficient method. In addition, the stabilization controller is proposed for the GFM control structure, which further enhances the GFM VSC-HVDC's stability and helps it operate stably under both stiff and weak grid conditions.

## 2 Configuration of VSC-HVDC and grid-forming control

### 2.1 System configuration

Figure 1 presents the configuration of the VSC-HVDC transmission system, where renewable energy (e.g., wind farm) is integrated into the sending-end converter (SEC). The DC line is between the SEC and the REC, the voltage of the DC-side equivalent capacitor is  $u_{dc}$ , the SEC is integrated into the utility grid via an LC filter, and  $R_d$  is the damping resistor.

As seen in Figure 1, the dynamic equation of the REC's capacitor voltage can be expressed in Eq. 1 as

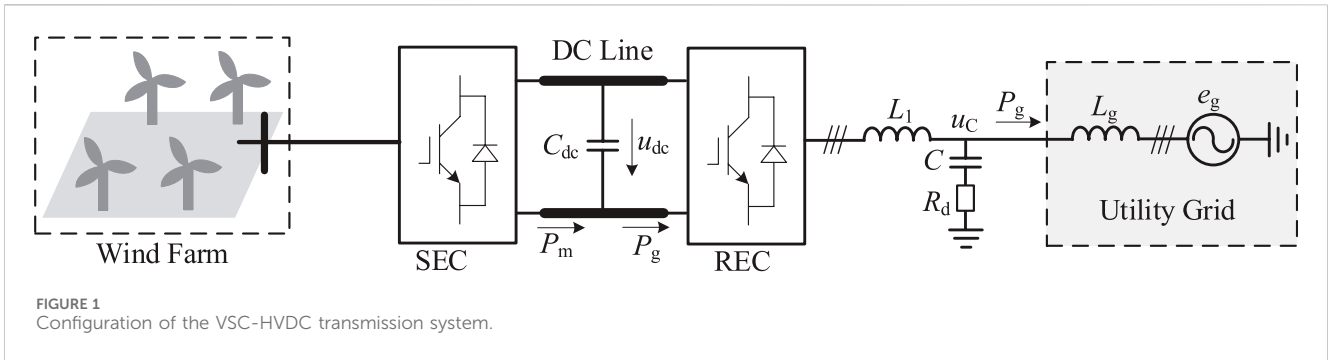


FIGURE 1 Configuration of the VSC-HVDC transmission system.

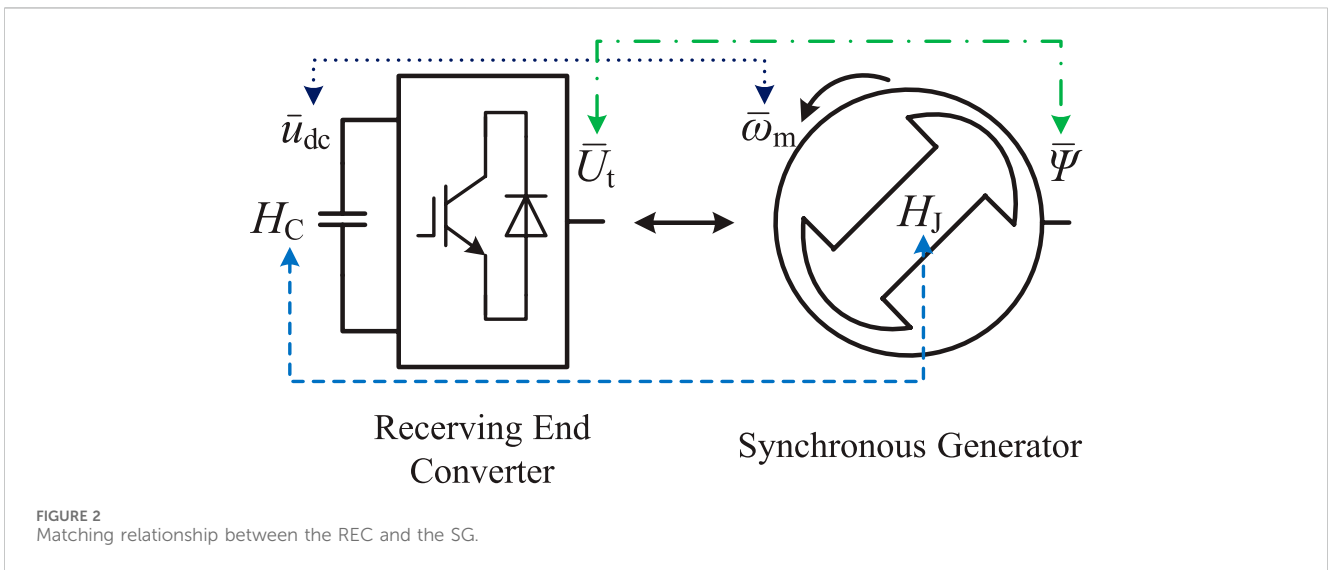


FIGURE 2 Matching relationship between the REC and the SG.

$$2H_C \left( \bar{u}_{dc0} \frac{d\bar{u}_{dc}}{dt} \right) = \bar{P}_m - \bar{P}_g, \tag{1}$$

$$\bar{P}_M = \frac{\bar{\psi} \bar{\omega}_m \bar{E}_g}{\bar{x}_g} \sin \delta_G, \tag{4}$$

where  $\bar{P}_g$  is the REC's output per-unit active power,  $\bar{P}_m$  is the SEC's output per-unit active power,  $\bar{u}_{dc}$  is the DC-side voltage in the per-unit form,  $\bar{u}_{dc0}$  is the steady-state DC-side voltage in the per-unit form, and  $H_C$  is the DC-side capacitor's equivalent time constant.

The REC's output active power  $\bar{P}_g$  is derived in Eq. 2 by

$$\bar{P}_g = \frac{\bar{u}_{dc} \bar{U}_t \bar{E}_g}{\bar{x}_g} \sin \delta, \tag{2}$$

where  $\bar{U}_t$  is the SEC's modulation voltage amplitude in the per-unit form,  $\bar{E}_g$  is the grid voltage amplitude in the per-unit form,  $\bar{x}_g$  is the grid line inductance in the per-unit form, and  $\delta$  is the power angle.

With respect to SG in the grid, the motion equation of the rotor is represented in Eq. 3 as

$$2H_J \left( \bar{\omega}_m \frac{d\bar{\omega}_m}{dt} \right) = \bar{P}_M - \bar{P}_e, \tag{3}$$

where  $\bar{P}_M$  is the SG's input active power in the per-unit form,  $\bar{P}_e$  is the SG's electromagnetic power in the per-unit form,  $\bar{\omega}_m$  is the SG's rotor speed in the per-unit form, and  $H_J$  is the equivalent time constant of the SG's rotor.

The SG's input active power  $\bar{P}_M$  is expressed in Eq. 4 as

where  $\bar{\psi}$  is the SG's per-unit flux linkage and  $\delta$  is the power angle of the SG.

Comparing (1) with (3) shows that the dynamical equation of the REC's capacitor voltage is similar to the motion equation of the SG's rotor. According to the similarity principle, the analogy relationship between the REC and the SG can be obtained, as shown in Figure 2. Comparing (2) with (4), the REC's per-unit modulation voltage amplitude  $\bar{U}_t$  is analogized to the SG's per-unit flux linkage  $\bar{\psi}$ , and the time constant  $H_C$  of the DC-link equivalent capacitor is analogized to the time constant  $H_J$ .

## 2.2 Grid-forming control strategy

The control target of the presented grid-forming control method is the converter's DC-side voltage. Currently, according to different control objectives, existing grid-forming control methods can be divided into two groups, namely, the GFM control under the active power control mode and the GFM control under the DC-side voltage control mode. The VSG control belongs to the GFM control under the active power

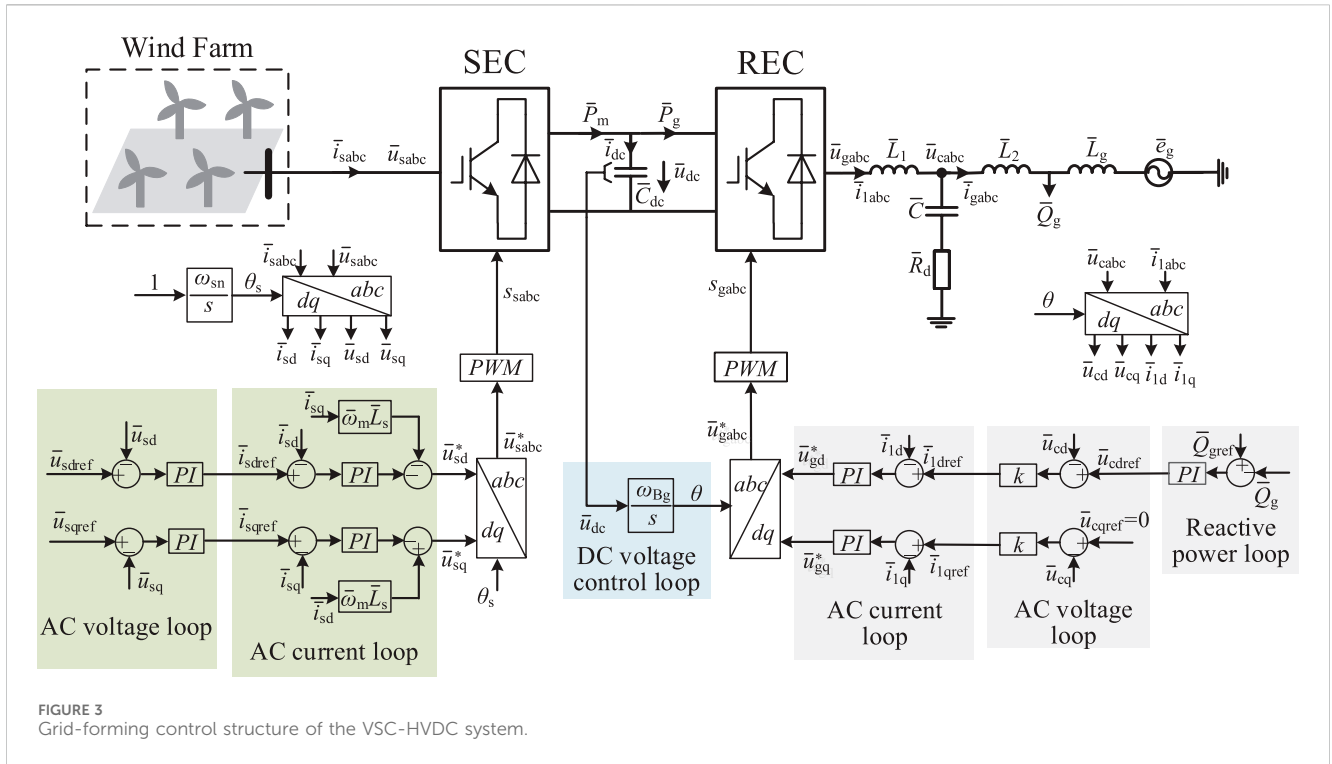


FIGURE 3 Grid-forming control structure of the VSC-HVDC system.

control mode, which is suitable for scenarios with a controllable input source, such as energy storage. Different from the VSG control, the proposed GFM control takes the DC voltage as the control objective, which is suitable for the two-stage conversion scenario with intermittent and fluctuating input motive power.

Figure 3 gives the VSC-HVDC system's grid-forming control structure, where the REC adopts the grid-forming control strategy with three cascaded loops, and the SEC utilizes the conventional two cascaded loops. The REC takes the DC-side voltage and the reactive power as the control objectives. In the REC's control diagram, the DC-side voltage of the REC passes through an integrator whose gain is the rated value of the grid's angular frequency  $\omega_{Bg}$ , and the output is the phase  $\theta$  of the REC's modulation voltage.

According to the matching relationship in Figure 2, the DC-side voltage of the REC can be analogized to the SG's rotor speed. The linkage between the AC-side angular frequency of the REC and the DC voltage is established so that it meets the following conditions:

$$\bar{\omega}_{REC} = \bar{u}_{dc}, \quad (5)$$

where  $\bar{\omega}_{REC}$  is the AC-side angular frequency of the REC.

Based on the control principle given by Equation 5, when the active power sent by the SEC to the DC capacitor increases, the DC-side voltage increases. According to the relationship in Equation 5, the AC-side angular frequency  $\bar{\omega}_{REC}$  of the REC increases, corresponding to an increase in the power angle  $\delta$ , thus increasing the REC's output active power and maintaining the DC-side voltage constant. This method achieves self-synchronization according to the DC-side capacitor's inertia.

In the outer reactive power control loop of the REC, the difference between the reactive power reference  $\bar{Q}_{gref}$  and the feedback-reactive power  $\bar{Q}_g$  passes through a PI regulator to obtain the d-axis reference  $\bar{u}_{cdref}$  of the AC capacitor voltage. The q-axis reference  $\bar{u}_{cqref}$  of the AC capacitor voltage is 0. In the middle AC voltage control loop of the REC, the differences between the d-axis and q-axis reference of the AC capacitor voltage and the feedback value, respectively, multiplied by the virtual impedance coefficient  $k$  are the d-axis and q-axis references of the REC's output current. In the inner AC current control loop of the REC, the difference between the d-axis and q-axis references of the AC current and the feedback value, respectively, passes through the PI regulator, and the output is the d-axis and q-axis components of the REC's modulation voltage.

Different from the ISynC-based GFM control (Wu W. et al., 2019; Li et al., 2022; Ge et al., 2023), the inner current loop is added to the GFM structure in this article, which can limit the output current. The control structure shown in Figure 3 can enable the REC to provide frequency support and realize the grid-forming function.

The SEC takes the AC voltage as the control objective. In the control diagram of the REC, the rated per-unit value of the SEC's AC frequency, that is, 1 p.u., passes through an integrator whose gain is the rated value of the SEC's rated angular frequency  $\omega_{sn}$ , and the output is the phase  $\theta_s$  of the SEC's modulation voltage. In the outer AC voltage control loop of the SEC, the difference between the d-axis reference  $\bar{u}_{sdref}$  and the q-axis reference  $\bar{u}_{sqref}$  of the SEC's AC voltage and the feedback value, respectively, multiplied by the PI regulator are the d-axis reference  $\bar{i}_{sdref}$  and the q-axis reference  $\bar{i}_{sqref}$  of the SEC's input current. In the inner AC current control loop of the SEC, the difference between the d-axis reference  $\bar{i}_{sdref}$  and the q-axis reference  $\bar{i}_{sqref}$  of the AC current and the feedback value,



TABLE 1 Parameters of the grid-forming VSC-HVDC system.

Variable	Description	Value
$e_{gl}$	Effective value of the grid line voltage	100 kV
$f_n$	Rated frequency of the grid	50 Hz
$f_s$	Switching frequency of the converter station	2 kHz
$U_{dc}$	Rated DC-link voltage	200 kV
$C_{dc}$	DC-link capacitance	70 $\mu$ F
$P_{gn}$	Rated output active power	200 MW
$Q_{gn}$	Rated output reactive power	0 Var
$k_{qp}$	Reactive power control loop's proportional gain	0.01
$k_{qi}$	Reactive power control loop's integral gain	10
$k$	Virtual impedance coefficient	0.75
$k_1$	Current control loop's proportional gain	0.05
$k_2$	Current control loop's integral gain	1

The state-space matrix  $H$  can be represented in Eqs 8–11 as

$$H = A + BC, \tag{8}$$

where

$$A = \begin{bmatrix} \frac{\bar{I}_{gd}\bar{U}_g}{2H_C} - \frac{\bar{I}_{gq}\bar{U}_g}{2H_C} - \frac{\bar{U}_g}{2H_C} & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ \omega_{Bg} & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ \frac{\omega_{Bg}\bar{U}_g}{L_1} & 0 & -\frac{\omega_{Bg}\bar{R}_d}{L_1} & \omega_{Bg} & \frac{\omega_{Bg}\bar{R}_d}{L_1} & 0 & -\frac{\omega_{Bg}}{L_1} & 0 & 0 \\ 0 & \frac{\omega_{Bg}\bar{U}_g}{L_1} & -\omega_{Bg} & -\frac{\omega_{Bg}\bar{R}_d}{L_1} & 0 & \frac{\omega_{Bg}\bar{R}_d}{L_1} & 0 & -\frac{\omega_{Bg}}{L_1} & 0 \\ 0 & 0 & \frac{\omega_{Bg}\bar{R}_d}{\bar{L}_2 + \bar{L}_g} & 0 & -\frac{\omega_{Bg}\bar{R}_d}{\bar{L}_2 + \bar{L}_g} & \omega_{Bg} & \frac{\omega_{Bg}}{\bar{L}_2 + \bar{L}_g} & 0 & 0 \\ 0 & 0 & 0 & \frac{\omega_{Bg}\bar{R}_d}{\bar{L}_2 + \bar{L}_g} & -\omega_{Bg} - \frac{\omega_{Bg}\bar{R}_d}{\bar{L}_2 + \bar{L}_g} & 0 & \frac{\omega_{Bg}}{\bar{L}_2 + \bar{L}_g} & 0 & 0 \\ 0 & 0 & \frac{\omega_{Bg}}{C} & 0 & -\frac{\omega_{Bg}}{C} & 0 & 0 & \omega_{Bg} & 0 \\ 0 & 0 & 0 & \frac{\omega_{Bg}}{C} & 0 & -\frac{\omega_{Bg}}{C} & -\omega_{Bg} & 0 & 0 \\ 0 & 0 & -k_2 & 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}, \tag{9}$$

$$B = \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & k_2 \end{bmatrix}^T, \tag{10}$$

$$C = \begin{bmatrix} 0 & 0 & -k\bar{R}_d & 0 & k\bar{R}_d & 0 & -k & 0 & 0 \\ 0 & 0 & -k_1 - kk_1\bar{R}_d & 0 & kk_1\bar{R}_d & 0 & -kk_1 & 0 & 1 \end{bmatrix}. \tag{11}$$

### 3.2 Small-signal stability analysis

The characteristic equation of the grid-forming VSC-HVDC system is derived in Eq. 12 as

$$f = \det(\lambda I - H), \tag{12}$$

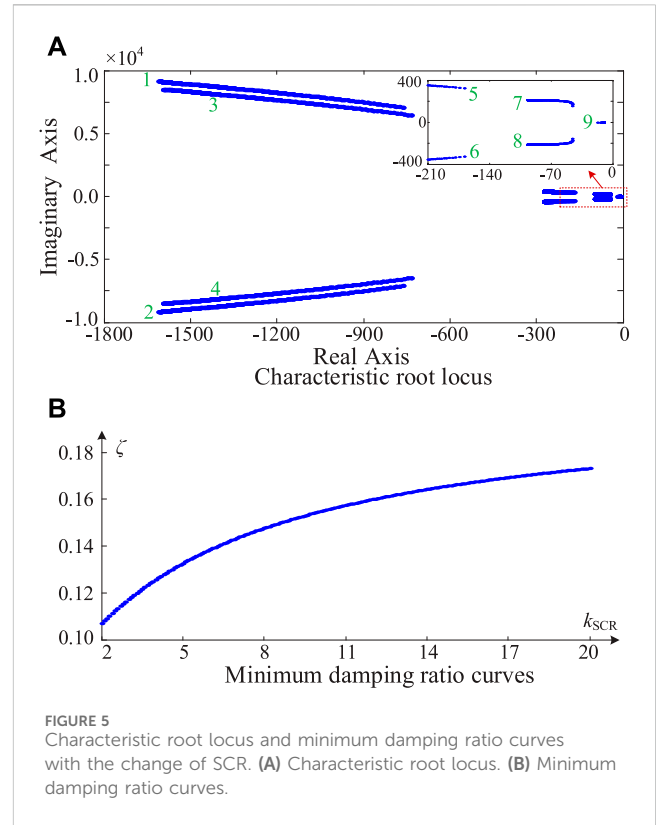


FIGURE 5 Characteristic root locus and minimum damping ratio curves with the change of SCR. (A) Characteristic root locus. (B) Minimum damping ratio curves.

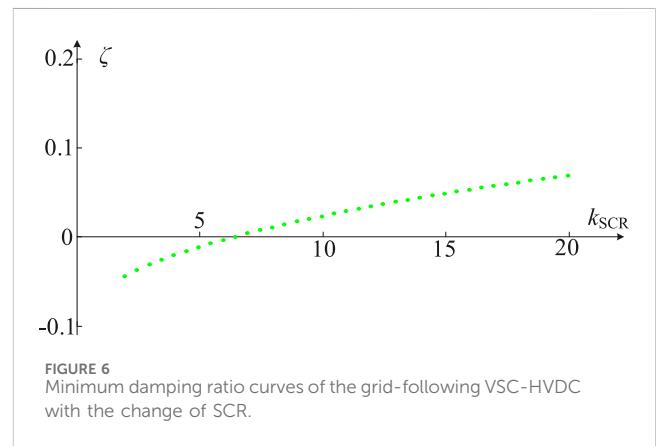


FIGURE 6 Minimum damping ratio curves of the grid-following VSC-HVDC with the change of SCR.

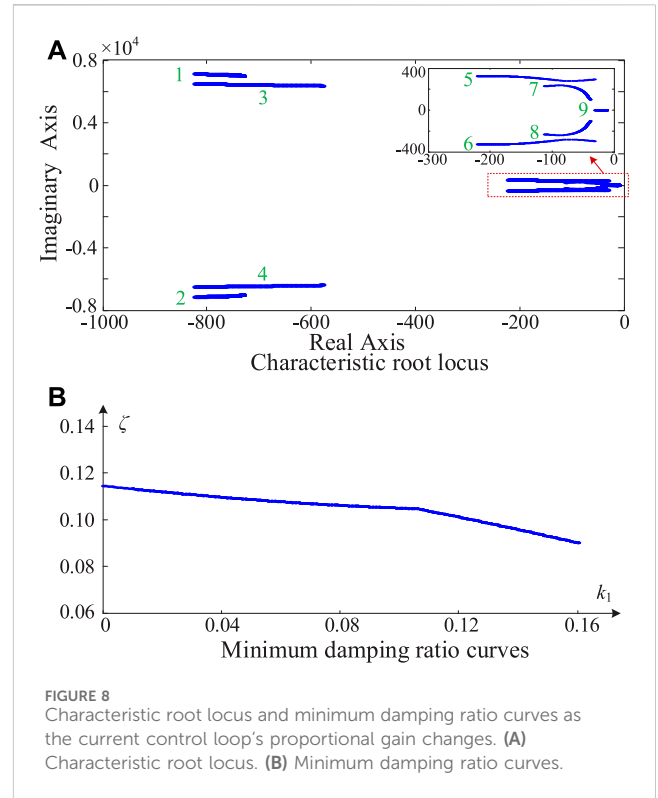
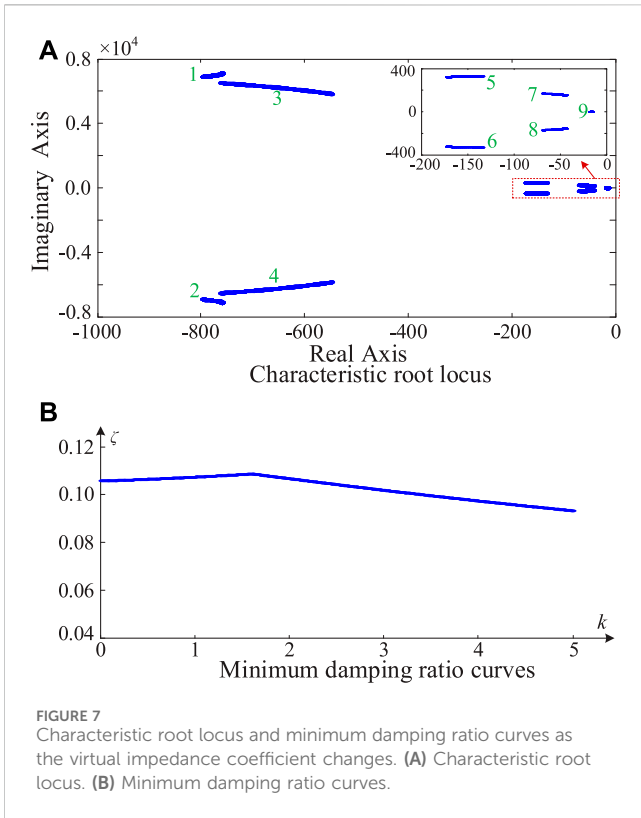
where  $\lambda$  is the eigenvector, and  $I$  is the identity matrix.

The eigenvalues  $\lambda_1, \lambda_2, \dots, \lambda_n$  of the GFM VSC-HVDC system can be derived by setting the value of (12) to 0. The quantitative index of small-signal stability margin for the grid-forming VSC-HVDC system is obtained as

$$\zeta = \min_{i=1 \rightarrow n} \left[ \frac{-\text{real}(\lambda_i)}{|\lambda_i|} \right], \tag{13}$$

where  $\text{real}(\lambda_i)$  represents the real part of the eigenvalues  $\lambda_i$ , and  $|\lambda_i|$  represents the amplitude of the eigenvalues  $\lambda_i$ .

It can be seen from Equation 13 that the quantitative index  $\zeta$  represents the system's characteristics of electrical damping, which can measure the small-signal stability margin. If the value of  $\lambda$  is



greater than 0, the GFM VSC-HVDC system can work stably. If the value of  $\lambda$  is negative, the GFM VSC-HVDC system cannot work stably.

Based on parameters in Table 1 and the state-space model, Figure 5 presents the characteristic root locus and minimum damping ratio curves with the change of the short-circuit ratio (SCR)  $k_{SCR}$ , where  $k_{SCR}$  is equal to the reciprocal of the grid line inductance  $\bar{L}_g$  in the per-unit form. In Figure 5A, with the change of  $k_{SCR}$  from 20 to 2, the nine root trajectories are all located in the left half plane, which means the grid-forming VSC-HVDC system can work stably in both stiff and weak grids. In Figure 5B, the quantitative index  $\zeta$  of the small-signal stability margin for the grid-forming VSC-HVDC system decreases slowly as  $k_{SCR}$  declines from 20 to 2, but the value of  $\zeta$  is still greater than 0.1. Research results in Figure 5 indicate that the presented grid-forming method has good grid adaptability, which can guarantee the stable working of the VSC-HVDC system.

For the grid-following VSC-HVDC system (Yang et al., 2020), Figure 6 presents the minimum damping ratio curves as the SCR changes, where the REC adopts the conventional vector control, the outer DC voltage loop's control bandwidth is 20 Hz, the inner current loop's control bandwidth is 200 Hz, and the PLL's control bandwidth is 50 Hz. It can be seen from Figure 6 that with the decrease of the SCR from 20 to 2, the minimum damping ratio curves of the grid-following VSC-HVDC gradually decrease below 0, which shows that the grid-following VSC-HVDC can operate stably under the stiff grid condition and will lose stability in a weak grid. Comparing Figures 5, 6 demonstrates that the proposed grid-forming control strategy in this article has better stability than the conventional grid-following VSC-HVDC.

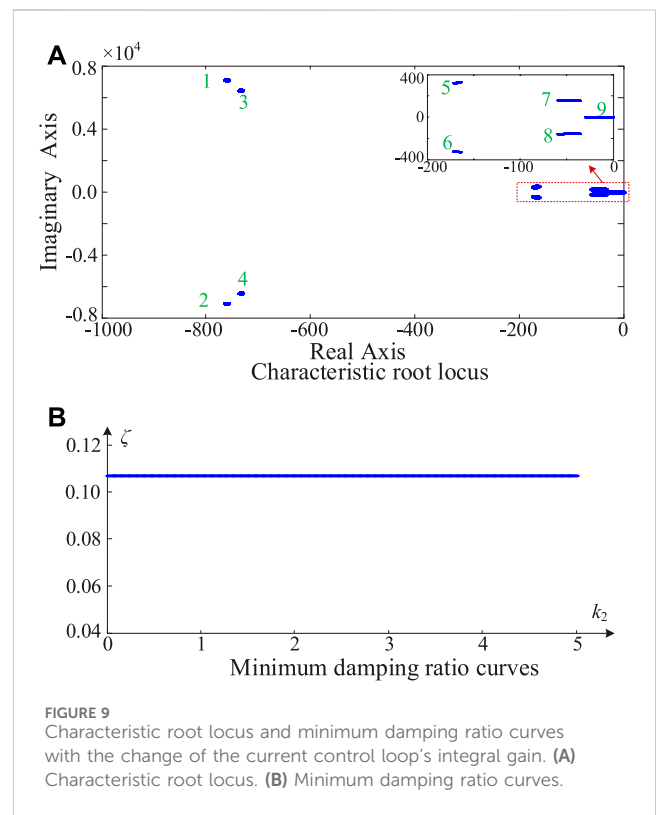


Figure 7 presents the characteristic root locus and minimum damping ratio curves with the change of the virtual impedance coefficient, where the SCR is 2, the current loop's proportional gain  $k_1$  is 0.05, and the current loop's integral gain  $k_2$  is 1. It can be seen

from Figure 7A that when the virtual impedance coefficient  $k$  increases from 0 to 5, the nine root trajectories of the system are all distributed in the left half plane, corresponding to the stable operations of the grid-forming VSC-HVDC system. Furthermore, when the virtual impedance coefficient  $k$  increases from 0 to 5, the minimum damping ratio of the system first increases and then decreases, but it is always greater than 0. Research results shown in Figure 7 illustrate that the VSC-HVDC system under the proposed grid-forming control is robust and can maintain stable operations with a large range variation of the voltage loop parameters.

Figure 8 presents the characteristic root locus and minimum damping ratio curves as the proportional gain  $k_1$  of the current control loop changes, where the SCR is 2, the virtual impedance coefficient  $k$  is 0.75, and the current loop's integral gain  $k_2$  is 1. In Figure 8A, when the current loop's proportional gain  $k_1$  increases from 0 to 0.16, the nine root trajectories of the system are all distributed in the left half plane, corresponding to the stable operations of the grid-forming VSC-HVDC system. Moreover, in Figure 8B, when the current control loop's proportional gain  $k_1$  increases from 0 to 0.16, the minimum damping ratio of the system decreases, but it is always greater than 0. Research results in Figure 8 demonstrate that the VSC-HVDC system under the proposed grid-forming control is robust and can maintain stable operations with a large range variation of the current control loop's proportional gain.

Figure 9 presents the characteristic root locus and minimum damping ratio curves as the current control loop's integral gain  $k_2$  changes, where the SCR is 2, the virtual impedance coefficient  $k$  is 0.75, and the current loop's proportional gain  $k_1$  is 0.05.

Figure 9A shows that when the current loop's integral gain  $k_2$  increases from 0 to 5, the nine root trajectories of the system are all located in the left half plane and almost remain unchanged, corresponding to the stable operations of the grid-forming VSC-HVDC system. In addition, in Figure 9B, when the current control loop's integral gain  $k_2$  increases from 0 to 5, the minimum damping ratio of the VSC-HVDC almost remains unchanged and is always greater than 0.1. Research results shown in Figure 9 demonstrate that the VSC-HVDC system under the proposed grid-forming control is robust and can maintain stable operations with a large range variation of the current control loop's integral gain.

## 4 Mechanism analysis and stabilization control

### 4.1 Interaction mechanism analysis

This article utilizes the complex power coefficient method (Sang et al., 2019) to reveal the interaction mechanism between the grid-forming VSC-HVDC system and the grid. First, the REC's grid-connected active power of the VSC-HVDC system can be derived in Eq. 14 by

$$\bar{P}_g = \frac{\bar{u}_{dc}\bar{U}_t\bar{E}_g}{\bar{X}_f + \bar{X}_g} \sin \delta, \tag{14}$$

where  $\bar{X}_f$  is the per-unit inductive reactance of the REC's filter inductor,  $\bar{X}_g$  is the inductive reactance of the line inductor in the per-unit form,  $\bar{U}_t$  is the per-unit modulation voltage's amplitude of the REC, and  $\bar{E}_g$  is the amplitude of the grid voltage in the per-unit

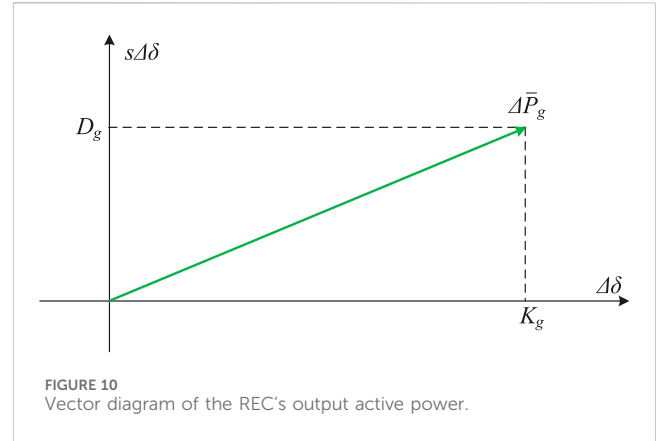


FIGURE 10 Vector diagram of the REC's output active power.

form.  $\delta$  is the phase of the REC's output voltage leading the grid voltage.

Linearizing the grid-connected active power of the REC in (14) gives

$$\begin{aligned} \Delta \bar{P}_g &= \frac{\bar{u}_{dc0}\bar{U}_{t0}\bar{E}_g}{\bar{X}_f + \bar{L}_g} \cos \delta \Delta \delta + \frac{\bar{U}_t\bar{E}_g}{\omega_{Bg}(\bar{X}_f + \bar{L}_g)} \sin \delta s \Delta \delta, \\ &= K_g \Delta \delta + D_g s \Delta \delta \end{aligned} \tag{15}$$

where  $\bar{u}_{dc0}$  is per-unit steady-state DC voltage of the REC,  $\bar{U}_{t0}$  is per-unit steady-state modulation voltage's amplitude of the REC,  $K_g$  is the synchronous power coefficient of the REC, and  $D_g$  is the damping power coefficient of the REC.

According to the linearized output active power in Eq. 15, the vector diagram of the REC's output active power can be obtained in Figure 10. The synchronous power coefficient  $K_g$  of the REC is greater than 0, and the damping power coefficient  $D_g$  of the REC is greater than 0. Because the REC's output active power is not related to the DC voltage, the variation of the REC's output active power  $\Delta \bar{P}_g$  is independent of  $\Delta \delta$ . Substituting  $\Delta \bar{P}_g$  and  $\Delta \bar{P}_m$  into (1), the characteristic equation of the grid-forming VSC-HVDC system is derived as

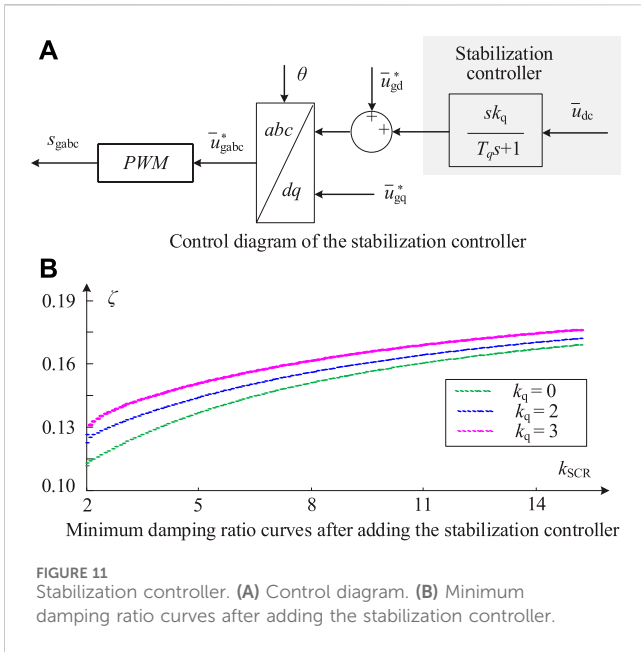
$$\frac{2H_C}{\omega_{Bg}} s^2 \Delta \delta + D_g s \Delta \delta + K_g \Delta \delta = 0. \tag{16}$$

It can be seen from Equation 16 that the characteristic equation of the grid-forming VSC-HVDC system is a second-order equation, and the stability of the system is decided by the damping coefficient  $D_g$ . Because the value of  $D_g$  is greater than 0, the VSC-HVDC system under the proposed grid-forming control is always stable, whether the grid is weak or stiff. The above mechanism analysis results are in accordance with the conclusions of numerical analysis in Section 3, further validating the correctness of the conclusion.

### 4.2 Stabilization control strategy

Although the minimum damping ratio  $\zeta$  of the grid-forming VSC-HVDC system is greater than 0, the value of  $\zeta$  is not big enough; that is, the stability margin is inadequate. Therefore, it is essential to propose a stabilization controller to further improve the system's small-signal stability. As is well known, a power system





stabilizer (PSS) can be added to the excitation system of the SG. The PSS usually takes the rotational speed of the SG as the input signal, and its output is superimposed on the excitation signal to increase the electrical damping. In the proposed GFM control structure of the REC, the modulation voltage amplitude can be analogized to the flux linkage of the SG. Therefore, imitating the stabilization mechanism of the PSS, this section proposes a damping injection strategy according to the DC voltage feedback to change the modulation voltage amplitude of the REC.

Figure 11 presents the control diagram of the stabilization controller and minimum damping ratio curves after adding the stabilization controller. In Figure 11A, a stabilization controller is added to the original grid-forming structure. The input of the stabilization controller is the DC-side capacitor voltage, and the output of the stabilization controller is superimposed on the per-unit d-axis modulation voltage  $\bar{u}_{gd}^*$ . The per-unit d-axis modulation voltage  $\bar{u}_{gd}^*$  and per-unit q-axis modulation voltage  $\bar{u}_{gq}^*$  are transferred to  $\bar{u}_{gabc}^*$  by the rotation transformation. The stabilization controller's transfer function is given in Eq. 17 as

$$H(s) = \frac{sk_q}{T_q s + 1}, \tag{17}$$

where  $s$  is the Laplace operator,  $k_q$  is the stabilization controller's gain, and  $T_q$  is the stabilization controller's time constant.

Figure 11B presents the minimum damping ratio curves of the grid-forming VSC-HVDC system after adding the stabilization controller, where  $T_q$  is 0.1. It can be seen that with the increasing of the stabilization gain,  $k_q$ , from 0 to 2 and 3, the small-signal stability quantitative index  $\zeta$  is promoted overall. The research result shown in Figure 11B illustrates that the proposed stabilization controller can further enhance the grid-forming VSC-HVDC's stability, whether under stiff or weak grid conditions.

Figure 11A shows that the parameters needed to be designed are  $k_q$  and  $T_q$ . The high-pass filter in the stabilization controller can pass through signals with a frequency greater than  $1/T_q$  rad/s. When designing the time constant  $T_q$ , it is essential to enable the signal of

resonant frequency to pass through. Increasing the value of the stabilization controller's gain  $k_q$  can improve the stability of the GFM VSC-HVDC. Because increasing the DC-side voltage during the dynamic process will increase the modulation ratio of the REC after adding the stabilization controller, the REC's modulation ratio  $m$  is represented in Eq. 18 as

$$m = \frac{k_q \Delta \bar{u}_{dc} U_{dcb} + \bar{U}_g U_b}{\bar{u}_{dc0} U_{dcb}}, \tag{18}$$

where  $\bar{U}_g$  is the AC voltage amplitude of the REC in the per-unit form,  $U_b$  is the base value of the AC voltage,  $U_{dcb}$  is the base value of the DC-side voltage, and  $\Delta \bar{u}_{dc}$  is the variation of the DC-side voltage.

Because the per-unit DC-side voltage can track the per-unit grid frequency, the variation of the DC-side voltage  $\Delta \bar{u}_{dc}$  is taken as 0.01 p.u. in this article. The maximum value  $k_{qmax}$  of the stabilization controller's gain is limited by the maximum modulation ratio of the REC. According to (18), the maximum value  $k_{qmax}$  can be obtained in Eq. 19 as

$$k_{qmax} = \frac{m_{max} - \bar{U}_g U_b / (\bar{u}_{dc0} U_{dcb})}{0.01}, \tag{19}$$

where  $m_{max}$  is the maximum value of the REC's modulation ratio.

According to the range of  $k_q$  and  $T_q$ , designing the gain and time constant of the stabilization controller follows the steps below.

**Step 1.** The potential resonant frequency of the GFM VSC-HVDC system can be derived by building the GFM VSC-HVDC's state-space model.

**Step 2.** The time constant  $T_q$  of the stabilization controller is tuned based on the derived potential resonant frequency.

**Step 3.** A value for the stabilization controller's gain  $k_q$  is provided and substituted into the state-space model of the GFM VSC-HVDC system.

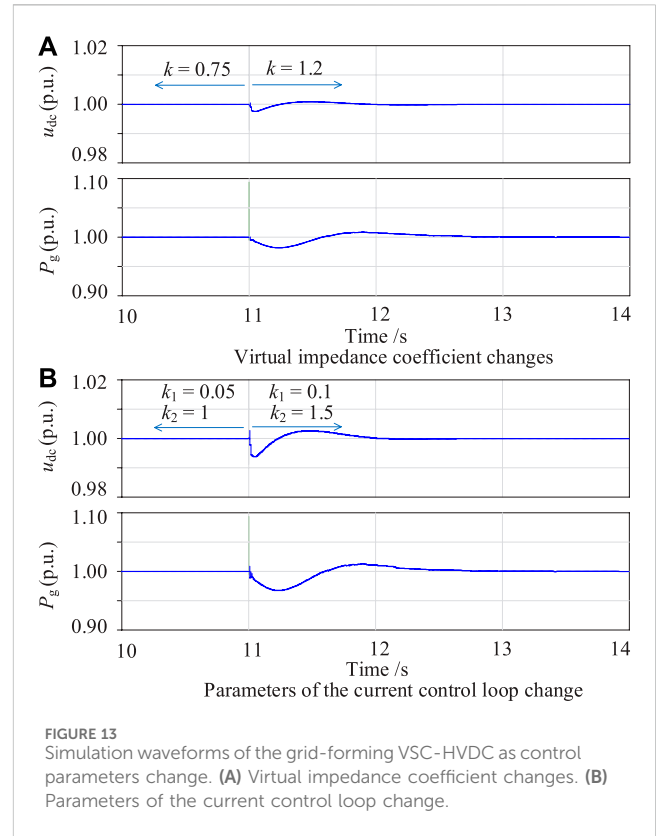
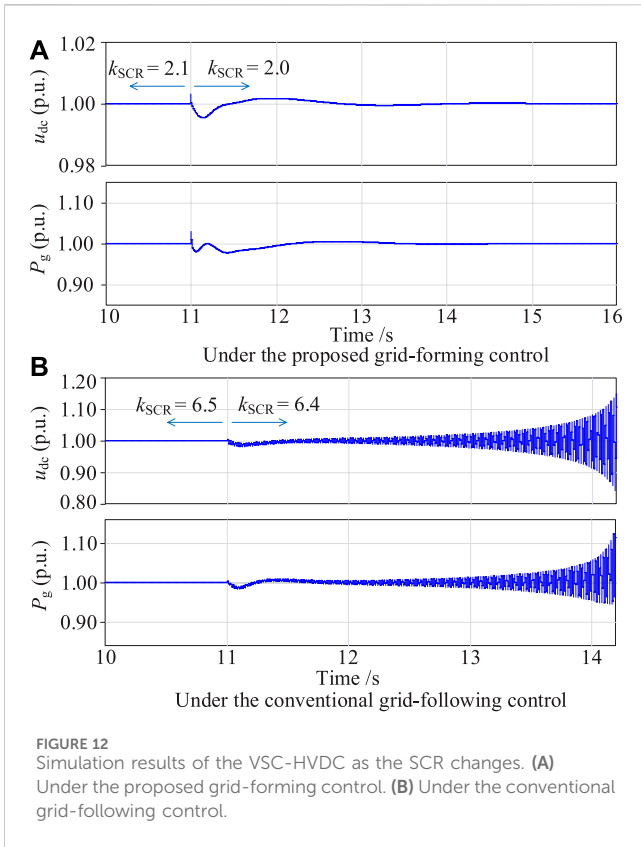
**Step 4.** If the electrical oscillation is suppressed and the stability margin is big enough, the design of the stabilization controller is completed. Otherwise, return to step 2 and redesign the parameters.

In contrast, as shown in Figure 11A, a variation related to  $\bar{u}_{dc}$  is superimposed on the amplitude of the modulation voltage  $\bar{U}_t$ . After adding the stabilization controller, linearizing the output active power of the REC in (14) yields

$$\begin{aligned} \Delta \bar{P}_g &= K_g \Delta \delta + D_g s \Delta \delta + \frac{\bar{u}_{dc0} \bar{E}_g}{X_f + X_g} \sin \delta \Delta \bar{U}_t, \\ &= K_g \Delta \delta + (D_g + D_s) s \Delta \delta \end{aligned} \tag{20}$$

where  $D_s$  is the system's damping coefficient provided by the stabilization controller.

According to the control diagram of the stabilization controller in Figure 11A, because the stabilization controller's time constant is fixed, the variation of the modulation voltage's amplitude  $\bar{U}_t$  is related to the stabilization gain  $k_q$  and the DC-side voltage. Thus, the damping coefficient  $D_s$  provided by the stabilization controller is proportional to the stabilization gain  $k_q$ . Combining Eq. 1 and the linearized active power in Eq. 20, the damping power coefficient of



the GFM VSC-HVDC system can be obtained as  $(D_g + D_s)$ . In addition, adding stabilization control and properly adjusting the stabilization gain  $k_q$  can increase the value of  $(D_g + D_s)$ , therefore improving the stability margin of the grid-forming VSC-HVDC. The above mechanism analysis results are in accordance with the research results in Figure 11B.

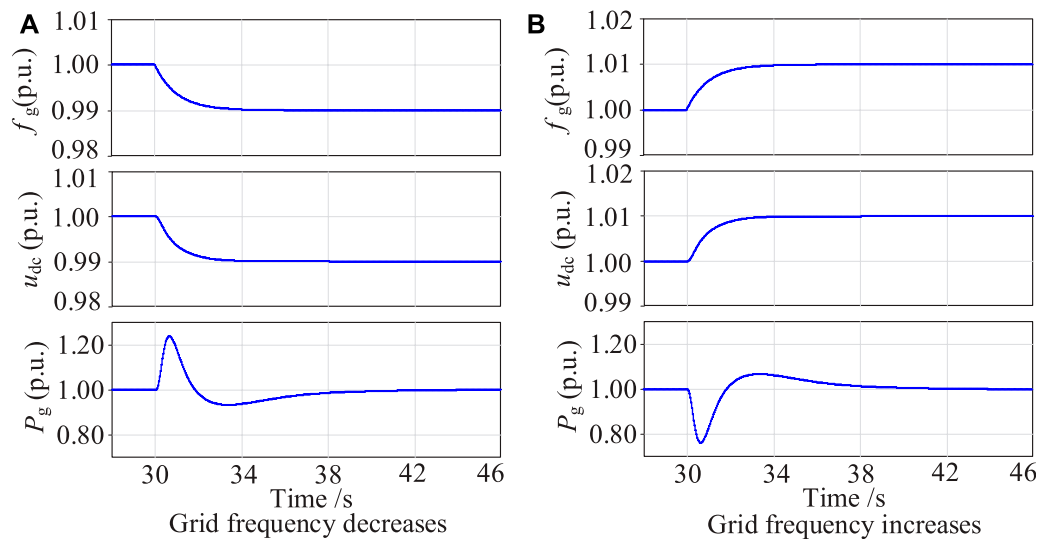
### 5 Simulation verification

To further prove the practicability of the presented GFM strategy for the VSC-HVDC system and demonstrate the correctness of stability analysis, simulations have been carried out based on the PSCAD/EMTDC. The electrical and control parameters of the simulation system are shown in Table 1.

Figure 12 presents the simulation results of the VSC-HVDC transmission system as the SCR changes. In Figure 12A, where the VSC-HVDC adopts the presented grid-forming control in this article, and the grid’s short-circuit ratio  $k_{SCR}$  decreases from 2.1 to 2.0, the DC-side voltage fluctuates and then returns to a stable state. The VSC-HVDC system’s grid-connected active power fluctuates and then recovers stability. Simulation results in Figure 12A show that the VSC-HVDC under the proposed grid-forming control can work stably in weak grids. In Figure 12B, where the VSC-HVDC utilizes the conventional grid-following control, the bandwidth of the outer DC voltage control loop is 20 Hz, the inner current loop’s control bandwidth is 200 Hz, and the control bandwidth of the PLL is 50 Hz. The DC-side voltage and the grid-connected active power of the VSC-

HVDC gradually oscillate and diverge with the grid’s short-circuit ratio  $k_{SCR}$  decreasing from 6.5 to 6.4, demonstrating that the stability of the conventional grid-following VSC-HVDC deteriorates when the grid’s stiffness decreases. Simulation results in Figure 12A illustrate that the VSC-HVDC under the proposed GFM control can work stably when the SCR decreases from 2.1 to 2.0, which is in accordance with the numerical analysis conclusions shown in Figure 5. The critically stable value of the SCR in Figure 12B is 6.5, which is approximately equal to the value shown in Figure 6. The simulation results shown in Figure 12B are in accordance with the numerical analysis conclusions in Figure 6. Furthermore, comparing Figure 12B with Figure 12A, the VSC-HVDC under the presented GFM control has better stability than that under the conventional GFL control in weak grids.

Figure 13 shows the simulation results of the grid-forming VSC-HVDC as control parameters change. In Figure 13A, where the SCR is 2, the current control loop’s proportional gain  $k_1$  is 0.05, the integral gain  $k_2$  of the current control loop is 1, and the voltage control loop’s virtual impedance coefficient  $k$  changes from 0.75 to 1.2. The DC-side voltage and the grid-connected active power of the GFM VSC-HVDC system fluctuate slightly and then recover. No oscillations occur in the DC-side voltage and the grid-connected active power, demonstrating that the VSC-HVDC under the presented GFM control is robust and can maintain stable operations with a large range variation of the voltage loop parameters. Simulation results in Figure 13A illustrate that the VSC-HVDC under the proposed GFM control can work stably when the virtual impedance



**FIGURE 14** Simulation waveforms of the grid-forming VSC-HVDC system when providing the inertia response. **(A)** Under the proposed grid-forming control. **(B)** Under the conventional forming control.

coefficient  $k$  increases from 0.75 to 1.2, which is in accordance with numerical analysis conclusions in Figure 7. In Figure 13B, where the SCR is 2, the virtual impedance coefficient  $k$  is 0.75, the current control loop's proportional gain  $k_1$  changes from 0.05 to 0.1, and the current control loop's integral gain  $k_2$  changes from 1 to 1.5. Small-amplitude oscillations occur in the DC-side voltage and grid-connected active power of the grid-forming VSC-HVDC system, indicating that the VSC-HVDC system under the proposed grid-forming control is robust and can maintain stable operations with a large range variation of the current control loop's integral gain. Simulation results in Figure 13B illustrate that the VSC-HVDC under the proposed GFM control can work stably when the parameters of the current control loop change, which is in accordance with numerical analysis conclusions in Figure 8.

Figure 14 presents simulation waveforms of the grid-forming VSC-HVDC system when providing inertia response, where the SCR is 2, the current control loop's proportional gain  $k_1$  is 0.05, the current control loop's integral gain  $k_2$  is 1, and the virtual impedance coefficient  $k$  of the voltage control loop is 0.75. In Figure 14A, when the grid frequency falls from the rated value to 99% of the rated value, the DC voltage of the grid-forming VSC-HVDC can automatically track grid frequency, acting as the PLL. Based on the DC-side voltage in the per-unit form, the source renewable energy (e.g., wind farm) increases the output active power to provide inertia response to the grid. The grid-connected active power  $P_g$  of the grid-forming VSC-HVDC increases by 0.24 p.u. and then recovers. In Figure 14B, the DC-side voltage of the grid-forming VSC-HVDC can automatically track the grid frequency as the grid frequency increases from the rated value to 101% of the rated value. According to the DC-side voltage in the per-unit form, the source of the renewable energy (e.g., wind farm) reduces the output active power to provide inertia support to the grid. The output active power  $P_g$  of the REC grid-forming VSC-HVDC system decreases by 24% and then recovers.

Simulation results in Figure 14 demonstrate that the presented grid-forming control can make the VSC-HVDC automatically sense the grid frequency and realize the function of inertia response.

## 6 Conclusion

A novel grid-forming control strategy with the function of limiting the output current is proposed to deal with the interaction instability issues between a conventional grid-following VSC-HVDC system and the grid. A state-space model of the grid-forming VSC-HVDC system is established to research the small-signal stability, and the eigenvalue analysis method is adopted. Moreover, the complex power coefficient method is utilized to reveal the interaction mechanism between the grid-forming VSC-HVDC system and the grid. To further improve the stability margin of the grid-following VSC-HVDC system, a stabilization controller is proposed for the original grid-forming structure, which can introduce positive electrical damping. Conclusions are obtained as follows:

- 1) The grid-forming control strategy makes the REC realize the function of self-synchronization with the grid through the dynamics of the DC capacitor. The per-unit DC voltage can automatically track the grid frequency, acting as a phase-locked loop.
- 2) Different from the conventional grid-following VSC-HVDC, which loses stability in a weak grid, the VSC-HVDC system under the proposed grid-forming control can work stably in both stiff and weak grids.
- 3) The VSC-HVDC system under the proposed grid-forming control is robust and can maintain stable operations with a large range variation of the parameters in the current and voltage control loop.

## Data availability statement

The raw data supporting the conclusions of this article will be made available by the authors, without undue reservation.

## Author contributions

YL: formal analysis, writing—original draft, and writing—review and editing. GS: validation, writing—original draft, and writing—review and editing. QC: investigation, resources, and writing—original draft. PQ: software and writing—review and editing. JZ: Investigation, supervision, and writing—review and editing. RY: project administration and writing—review and editing. JZ: funding acquisition and writing—review and editing.

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## Conflict of interest

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