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# Entropy generation associated with natural convection within a triangular porous cavity containing equidistant cold domains

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This study investigates the computational analysis of steady, incompressible, natural convection airflow in a 2D equilateral triangular cavity featuring two stationary cold circular cylinders. The convective phenomena within the cavity have been observed under the variation of uniform porosity. The convective flow has been modeled using the Darcy-Brinkman formulations for porous medium incorporated with the Boussinesg approximation. The governing equations have been simulated using the finite element method with non-uniform triangular meshing. The investigation was conducted with a fixed Prandtl number, Pr = 0.71, and different porosity by varying Darcy number,  $Da = 10^{-5}$  to  $10^{-2}$ . The convective strength has been varied with the Rayleigh number,  $Ra = 10^3$  to  $10^6$ , and the length of the heated and cold segment,  $\varepsilon = 0.1$  to 0.9. Results regarding the fluid flow and temperature distribution are visualized through streamlines and isotherms. The quantity and the quality of heat transfer (HT) have been investigated, respectively, by the Nusselt number (Nu) and the entropy generation ( $E_{aen}$ ). The results reveal that an increase in the length of the hot wall ( $\varepsilon$ ) significantly reduces HT. Also,  $E_{aen}$ increases with the length of active segments ( $\varepsilon$ ), while the Bejan number (Be) consistently rises when the Darcy-Rayleigh (Da-Ra) number increases, i.e., Da-Ra  $\geq 10^2$ . The maximum HT rate was obtained within the range of Da =  $10^{-5}$  to  $10^{-3}$ for a constant value of  $\varepsilon$ . Furthermore, the maximum HT was obtained for the smallest value  $\varepsilon$  for any value of Da or Ra.

#### KEYWORDS

triangular cavity, heat transfer, entropy generation, nusselt number, bejan number

## **1** Introduction

Natural convection (NC), induced by buoyancy forces arising from temperature differences, is readily observed in nature (Bhowmick et al., 2019). It represents a fundamental heat transfer (HT) phenomenon occurring across various geometries, crucial for regulating temperatures within enclosed spaces. Understanding NC is essential for optimizing HT processes in different engineering industries, as it connects

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passive mechanisms, thereby reducing energy consumption and environmental impact (Liu et al., 2019). The various shapes of cavities influence NC by modifying fluid dynamics and HT behavior, leading to optimized thermal efficiency in heat exchangers and enhanced cooling in electronic devices, underscoring the significance of cavity design in engineering applications. NC in V-shaped cavities transitions from conduction at low Rayleigh number (Ra) to asymmetry at moderate Ra and chaos at high Ra (Bhowmick et al., 2019). Furthermore, valley-shaped cavities exhibit two flow phases affected by aspect ratios and Ra, allowing for the prediction of stratification breakup times and Nusselt number (Nu) trends, highlighting the importance of validating field measurements (Bhowmick et al., 2018). Among all cavity shapes, triangular cavities play a crucial role due to their ability to induce complex flow patterns, providing insights into fundamental fluid dynamics and HT phenomena. These cavities are extensively used in designing aircraft wings, heat exchangers, microfluidic devices, rocket nozzles, and various other applications, including heating and cooling (Sharif and Mohammad, 2005). Triangular cavities enhance turbulence, thereby boosting HT efficiency, as evidenced by studies on heater placement demonstrating Nu (Das et al., 2017). Additionally, HT in isosceles triangular geometries is influenced by various factors, with smaller nanoparticles enhancing HT and larger ones causing stagnation (Uddin et al., 2022). A computational study on a zigzag-bottom triangular cavity reveals disrupted symmetric fields with higher Lewis numbers (Le), enhanced HT and mass transfer (MT) at positive buoyancy ratios, and higher Ra values. Furthermore, it uncovers a surprising dominance of conduction over convection at higher Ra values with negative buoyancy ratios, providing insights into the role of buoyancy in MT and HT (Rahman et al., 2012).

Exploring HT in triangular chambers filled with nanofluid reveals complex interactions between buoyancy, Ra, Le, and buoyancy ratio parameters (Sheremet et al., 2017). This understanding is crucial as it unveils three intervals in the average Nusselt number (Nuavg), shedding light on nanofluid (NF) dynamics and critical factors affecting MT and HT. Similarly, investigations into HT and fluid flow in undulated triangular hollows showcase dominant HT, highlighting a complex interaction between parameters and geometry in triangle cavities (Bhardwaj and Dalal, 2013). Additionally, studies on magnetohydrodynamics (MHD) NC in triangular solar collectors confirm that HT improves with higher Ra values while conduction HT dominates at lower Ra values. Adjusting nanoparticle diameter offers insights for optimizing HT efficiency (Rahman et al., 2016). Furthermore, exploring flexible-sided triangular cavities with MHD reveals varied HT effects, providing insights into the intricacies of fluid dynamics and HT (Selimefendigil and Öztop, 2016). Examining radiative and natural convection HT in inclined triangle cavities with nanofluid and magnetic fields indicates increased HT and total Egen for higher Ra values and lower Hartmann number (Ha) (Afrand et al., 2020). Likewise, twophase NC studies in triangular geometries with wavy hot walls and magnetic fields exhibit complex effects of parameters, offering insights for system optimization (Shekaramiz et al., 2021).

Another area of interest in convective HT study deals with mixed convection (MC), involving both buoyancy-driven and

externally-driven forced convection (FC) within a fluid flow and HT system. Numerical simulations in triangular cavities with oscillating lids detect transitions to locked-on flows with repeated HT rate fluctuations. This reveals an increase in  $Nu_{avg}$  with the dimensionless frequency of lid velocity (Chen and Cheng, 2009). Moreover, investigations into mixed convection HT in triangular cavities underscore the impact of external factors like magnetic fields and Reynolds number (Re) on Nu (Soomro et al., 2020). In triangular cavities with nanofluid and internal heating, MC leads to Nu deterioration with increased Richardson number (Ri), highlighting the role of nanoparticle introduction during negative x-direction wall movement for enhancing HT (Selimefendigil and Öztop, 2017). Furthermore, the direction of motion of sliding walls plays a crucial role in controlling temperature and flow fields, maximizing HT in lid-driven cavity flows (Hasanuzzaman et al., 2012). Finally, MC in nanofluid-filled triangular cavities demonstrates enhanced HT influenced by nanoparticle concentrations and Ri, emphasizing the efficiency of solid volume fraction as a control parameter (Rahman et al., 2011).

Examining water based alumina oxide NF within a lid-driven triangular cavity unveils distinct variations in HT rates across different electrical conductivity models, and Nu decreased with the increase of Ri and Ha values (Chamkha et al., 2018). Furthermore, computational analysis of MT and mixed convection HT within a lid-driven right-angled triangular cavity exposes a notable influence of buoyancy ratio and lid movement direction on heat and mass transfer under varying Ri (Ching et al., 2012). Also, analysis using finite element method (FEM) on Cu-H<sub>2</sub>O nanofluid within inclined triangular cavities illustrates an augmented HT with higher nanoparticle concentration, affirming the significant impact of solid volume fraction on thermal fields and flow patterns. It identifies the Grashof number (Gr) and solid volume percentage as pivotal control parameters (Billah et al., 2013). Additionally, a study delves into a viscous fluid in a triangular cavity with a central square obstacle, revealing amplified kinetic energy and convective HT coefficients with increased Ra. Addressing singularity issues through non-uniform heating provides crucial insights into fluid dynamics and thermal behavior in such configurations (Bilal et al., 2020). Moreover, investigating corner-heated triangular cavities with magneto-NF underscores the substantial influence of Ra and cavity orientation on thermo-fluid flow structures and HT rates. Furthermore, escalating Ha compromises HT rates and flow velocity, whereas Al<sub>2</sub>O<sub>3</sub>-H<sub>2</sub>O nanofluid consistently enhances HT properties (Nag et al., 2022). In addition, a numerical exploration of CuO-H<sub>2</sub>O nanofluid within an isosceles triangular geometry demonstrates that a higher nanoparticle percentage enhances HT rates, while an increase in particle diameter restrains the rate of HT. A strong magnetic field diminishes fluid flow circulation and the intensity of HT rates (Uddin et al., 2022). Reversed trends in NF convection within an isosceles triangle are observed in response to changes in the magnetic field (Chatterjee et al., 2022).

Several investigations have explored the intriguing NC phenomenon within triangular cavities containing porous medium. One study investigated HT dynamics in a porous triangular cavity nestled between square tubes, spanning a wide range of parameters. It advocates for using fluids possessing higher Pr to optimize HT in the upper cavity, whereas the lower cavity

demonstrates consistent HT behaviors across different fluid types (Basak et al., 2010). Concurrently, scrutinizing various temperature boundary conditions, another study explores NC flow and HT in a porous triangular cavity. Placing a heater at the bottom wall causes multiple vortex formations, amplifying HT compared to alternative configurations (Varol et al., 2008a). Furthermore, a separate investigation explores NC flow and HT in non-isothermally heated porous triangular cavity, employing finite difference (FD) techniques and Darcy's law to gather insights into the complex dynamics (Varol et al., 2008b). These studies collectively deepen our understanding of NC within triangular cavities and underscore the significance of factors such as fluid properties, boundary conditions, and geometric configurations in governing HT phenomena.

Furthermore, Egen within the cavity during flow and HT underscores the irreversible nature of these processes, attributed to viscous dissipation and temperature gradients. Thus, minimizing  $E_{gen}$ emerges as a critical aspect in enhancing the productivity of flow and HT systems. A numerical investigation delves into the effects of sinusoidal heating and a wavy wall on Egen and HT within a porous right triangular cavity. The findings illustrate a transition from conduction dominance at low Da to intensified convection with undulated walls, resulting in a noteworthy 53% increase in the maximum Nu (Bhardwaj et al., 2015). Similarly, exploration of NC within a triangular cavity hosting a rectangular heat source reveals the occurrence of counter vortexes, heightened effectiveness at higher Ra, and complex HT patterns with varying heat source sizes. Unexpectedly, a proportional increase in temperature with heat source size yields a decrease in Nuavg, particularly along the hot wall, highlighting optimal results at the smallest heat source size and a Ra of 106 (Fayz-Al-Asad et al., 2021). Additionally, examining  $E_{gen}$  within right-angled triangle cavities containing porous media identifies specific locations experiencing maximum  $E_{gen}$ , with overall entropy augmentation corresponding to increasing Da. Also, triangular cavities featuring a 15° top angle demonstrate superior HT rates, enhanced thermal mixing, and diminished total Egen across diverse fluid processing scenarios (Basak et al., 2012). Moreover, the study of NC of non-Newtonian fluid within a magnetic field in triangular cavities shows complex dynamics affecting HT, Nu, Egen, and transmission rates (Li et al., 2020). Some recent research in cavities is also found in (Amidu et al., 2021; Ikram et al., 2021; Kumar et al., 2021; Riahi et al., 2022; Ikram et al., 2023; Kumar et al., 2023; Saboj et al., 2023; Saha et al., 2023; Saha B. K. et al., 2024; Saha G. et al., 2024; Saha T. et al., 2024; Ikram et al., 2024; Saboj et al., 2024).

Drawing from the literature review provided above, the examination of HT and  $E_{gen}$  within a triangular cavity holds significance for enhancing the performance of various systems, including cooling mechanisms, heat exchangers, and fluid flow systems. To the authors' knowledge, there has yet to be any prior exploration into the equilateral triangular cavity scenario featuring constant heat applied on the bottom wall segment coupled with the insertion of two circular cold objects within the cavity. Consequently, this study aims to investigate fluid flow, HT, and porous medium characteristics within such a triangular cavity employing air as the base fluid. The study will assess the impact of Ra, Da, and the size of the length of the applied heat flux on  $E_{gen}$ , fluid flow, and HT behavior. Specifically, the investigation will focus on parameters such as the average Nu, Be, streamlines and isotherms presentation, and  $E_{gen}$  of fluid flow and HT.

In brief, the model's findings can enhance the design of eco-friendly cooling systems for buildings, cutting energy usage and tackling urban heat islands in hot climates. In buildings, especially in regions with hot/ cold climates, effective cooling/heating is crucial in upholding comfortable indoor temperatures while minimizing energy usage. Passive cooling systems utilize natural phenomena, such as convection and radiation, to remove heat from the building without relying heavily on mechanical cooling systems like air conditioners. Porous cavities are often integrated into building designs to facilitate NC and heat dissipation. The model investigated could be used to study  $E_{gen}$ associated with NC within porous cavities, such as those integrated into building designs (Mansouri et al., 2022; Li et al., 2023). By understanding how Egen influences HT and energy efficiency, engineers and architects can optimize the design of these passive cooling systems to enhance their performance and reduce energy consumption.

Moreover, the study investigates NC in a triangular porous cavity with cold domains, focusing on  $E_{gen}$  and HT. It has practical applications in engineering, environmental sciences, and energy systems. Insights from the study can improve cooling systems for electronics, heat exchangers, building features for natural airflow, greenhouse ventilation, filtration systems, solar collectors, and industrial drying chambers. By optimizing the design and geometry of these systems, efficiency and performance can be significantly enhanced, leading to better heat distribution, energy savings, and improved process outcomes.

# 2 Physical model and governing equations

The present research investigates NC within a 2D porous triangular cavity featuring two stationary cold cylinders. The study explores the behavior of different fluids (air and water). Each side of the triangular cavity is assumed to have a length of L, as depicted in Figure 1. The segment of inclined walls, along with the two cylinders, is considered as a cold zone ( $T_C$ ), while the segment of the bottom wall considered as heated zone ( $T_H$ ). The remaining sections of each wall are assumed to be insulated.

#### 2.1 Governing equations

A two-dimensional steady, incompressible, Newtonian fluid for the study of NC flow inside a triangular porous cavity consisting of two cold static circular cylinders (Bejan, 2013):

$$\frac{\partial U}{\partial X} + \frac{\partial V}{\partial Y} = 0 \tag{1}$$

$$U\frac{\partial U}{\partial X} + V\frac{\partial U}{\partial Y} = -\frac{\partial P}{\partial X} + Pr\left(\frac{\partial^2 U}{\partial X^2} + \frac{\partial^2 U}{\partial Y^2}\right) - \frac{Pr}{Da}U$$
(2)

$$U\frac{\partial V}{\partial X} + V\frac{\partial V}{\partial Y} = -\frac{\partial P}{\partial Y} + Pr\left(\frac{\partial^2 V}{\partial X^2} + \frac{\partial^2 V}{\partial Y^2}\right) - \frac{Pr}{Da}V + Ra\operatorname{Pr}\theta \quad (3)$$

$$U\frac{\partial\theta}{\partial X} + V\frac{\partial\theta}{\partial Y} = \left(\frac{\partial^2\theta}{\partial X^2} + \frac{\partial^2\theta}{\partial Y^2}\right)$$
(4)

where



$$X = \frac{x}{L}, Y = \frac{y}{L}, U = \frac{uL}{\alpha}, V = \frac{vL}{\alpha}, \theta = \frac{T - T_C}{T_H - T_C}, P = \frac{pL^2}{\rho\alpha^2},$$
$$Pr = \frac{v}{\alpha}, Da = \frac{K}{L^2}, Ra = \frac{g\beta(T_H - T_C)L^3 Pr}{v^2}$$
(5)

Here, X and Y are considered non-dimensional Cartesian coordinates system, and U and V are correspondingly nondimensional velocity components. Moreover,  $\theta$  is the nondimensional temperature and P is the non-dimensional pressure.

#### 2.2 Boundary conditions

The research investigates the no-slip boundary condition within fluid dynamics, a foundational principle dictating that fluid motion is stopped at solid boundaries within a triangular cavity. Both fluid velocity and temperature boundary conditions are pivotal aspects examined in the study. The outlined boundary conditions for fluid velocity and temperature are provided below:

$$U(X, 0) = V(X, 0) = 0 \text{ on } AB,$$
  

$$U(X, Y) = V(X, Y) = 0 \text{ on } AC \text{ and } U(X, Y) = 0 \text{ on } BC$$
(6)

$$T = T_H \text{ on } l_1 l_2, T = T_C \text{ on } l_3 l_4 \text{ and } l_5 l_6$$
(7)

In the study, the length of the heated bottom wall  $(l_1l_2)$  of triangular cavity is denoted by  $\varepsilon$ , see Figure 1. The numerical experiments conducted in the study involve varying this parameter, with values ranging from 0.2 to 0.8.

#### 2.2.1 Non-dimensional parameters

#### 2.2.1.1 Nusselt number (Saha et al., 2010)

The average Nusselt number  $(Nu_{avg})$  of the hot bottom wall of the triangular cavity is expressed as:

$$Nu_{avg} = \overline{Nu} = -\frac{1}{\varepsilon} \int_{X=0}^{\varepsilon} \left(\frac{\partial\theta}{\partial Y}\right) dX$$
(8)

Entropy generation due to heat transfer (Ilis et al., 2008):

$$E_{HT} = \left(\frac{\partial\theta}{\partial X}\right)^2 + \left(\frac{\partial\theta}{\partial Y}\right)^2 \tag{9}$$

Entropy generation due to fluid friction (Ilis et al., 2008):





$$E_{FF} = \phi \left[ \left( U^2 + V^2 \right) + Da \left\{ 2 \left( \left( \frac{\partial \theta}{\partial X} \right)^2 + \left( \frac{\partial \theta}{\partial Y} \right)^2 \right) + \left( \frac{\partial U}{\partial X} + \frac{\partial V}{\partial Y} \right)^2 \right\} \right]$$
(10)

where,  $\phi = 10^{-4}$  is the irreversibility distribution ratio.

2.2.1.2 Total Entropy generation (Ilis et al., 2008)

$$E_{gen} = E_{HT} + E_{FF} \tag{11}$$

Bejan number (Ilis et al., 2008):

$$Be = \frac{E_{HT}}{E_{gen}} \tag{12}$$

# 3 Numerical method, grid independent test and validation

A numerical approach is employed to investigate natural convection (NC) within a porous triangular cavity containing two stationary circular cylinders. The commercial software COMSOL Multiphysics is utilized to solve Eqs 1–7 using Finite



Element Method (FEM), and simulations are conducted for air. A very fine triangular mesh was applied along the hot and cold walls and around the cold cylinders to calculate the sharp changes in temperature and velocity, as shown in Figure 2. A stationary linear direct solver, PARDISO, was used to solve the equations generated by FEM. PARDISO solver is preferred for a small number of degrees of freedom because it is more stable and faster, although it consumes memory at a high rate. The relative tolerance for the convergence criterion was set to  $10^{-6}$ .

#### 3.1 Grid independent test

We know the grid independent test confirms the accuracy of numerical simulations, ensuring that outcomes converge to consistent solutions regardless of grid refinement. As depicted in Figure 3, the test is performed for  $Nu_{avg}$  with different grid sizes ranging from 3,000 to 48,000. Analysis of Figure 3 reveals that the variation in  $Nu_{avg}$  is insignificant when transitioning from 38,000 to 45,000 mesh elements. Hence, 38,000 mesh elements are selected as the optimal mesh size for our study.

### 3.2 Validation

Figure 4 presents streamlines and isotherms within a triangular cavity at Gr of  $10^3$  and  $10^5$ , showing the present findings. Our study's results demonstrate a notable agreement with Holtzman et al.'s findings. Additionally, validation was conducted by comparing  $Nu_{avg}$  across various Gr values, as detailed in Table 1. The comparison reveals closely aligned values between our findings and those of Holtzman et al. (Holtzman et al., 2000).

# 4 Results

The current numerical simulation explores the fluid flow and HT dynamics within a porous triangular cavity filled with air. Various parameters are analyzed, including  $\varepsilon$  (0.1–0.9), as well as the impact of varying *Ra* (10<sup>3</sup>–10<sup>6</sup>), Pr (0.71), and *Da* (10<sup>-5</sup> to 10<sup>-2</sup>) numbers. Also, results related to Eqs 8–12 are presented qualitatively and quantitatively in this section.

### 4.1 Variation of ra

Figure 5 shows the variation of streamlines, isotherms,  $E_{FF}$ ,  $E_{HT}$ , and Be for different Ra. As we know, higher Ra values indicate the dominant role of convection over conduction in HT. So, the streamline plots exhibit an upward trend with the increase of Ra. Two counter-rotating cellular flows below the cold domain but adjacent to the lower hot wall are prominent in all the cases. Flow patterns are found symmetrical throughout the ranges of the Ra. Isotherms also demonstrate similar upward trends with the rise of Ra with the temperature distribution from the lower hot wall towards both the cold side walls. Increasing buoyant forces with higher Ra makes the fluid flow stronger, and the isotherms shift away from the sidewalls to the center. Hence, relatively hot fluid will pass along the cavity's centreline and rise between the stationary cold cylinders, demonstrating a plume shape in the isotherms at higher Ra. Moreover, EFF and EHT indicate the irreversibility created in the system. The  $E_{FF}$  due to the viscous forces present in the fluid is of much lower value than the  $E_{HT}$  due to the presence of a finite temperature gradient. Also, Figure 5 shows a more uniform pattern for  $E_{HT}$  as compared to  $E_{FF}$  across the Ra. In addition, Be contours in Figure 5 show the share of HT in the total irreversibility. At lower Ra, local Be is found higher in the narrow contrivances (viz. Between the stationary cylinder and the sidewalls) due to a higher velocity gradient. However, with the increase of buoyant force due to the rise of Ra, the

	A = 1.0 and $Nu_{avg}$		
	$Gr = 10^{3}$	$Gr = 10^4$	$Gr = 10^{5}$
Holtzman et al. (2000)	1.00	1.07	1.80
Present results	1.00	1.09	1.90

TABLE 1 Comparison of the present  $Nu_{avg}$  values with Holtzman et al. (Holtzman et al., 2000).

share of HT in the total irreversibility is increased, and hence, higher local *Be* occupied further areas in the attic.

## 4.2 Variation of Da

Figure 6 shows the results of various *Da* on the  $E_{FF}$  and  $E_{TH}$  contours and *Be* plots with  $Ra = 10^6$ ,  $\varepsilon = 0.8$ , and Pr = 0.71. Higher

Da indicates a higher permeability. Hence, more hot fluid will flow through the pores and thus increasing the convection. Hence, the density of  $E_{FF}$  and  $E_{TH}$  contours are increased, especially near the enclosures as evident in Figure 5. The local *Be* contours indicate isentropic spots near the cold pipe walls at lower *Da* values. However, these spots have become wider and denser with the rise of permeability levels aiding HT. However, symmetrical patterns are observed across the *Da* values.

## 4.3 Variation of $\varepsilon$

Figure 7 represents the results of various lengths of heat source ( $\varepsilon$ ) on the streamlines, isotherms,  $E_{FF}$  and  $E_{TH}$  contours and Be plots for different  $\varepsilon$  with  $Ra = 10^6$ ,  $Da = 10^{-2}$ , and Pr = 0.71. At a small  $\varepsilon$  value of 0.2, the cavity exhibits a flow characterized by two streamlined rotating cells: one featuring counterclockwise





fluid heat flow on the left and the other showcasing clockwise fluid heat flow on the right. The isotherms display curved trajectories originating from the cold stationary sources, with intense isotherms gathering near the bottom wall, indicative of the presence of the hot source. Also, isentropic patterns apparent as stretched spot shapes proximal to the walls. It is observe that increasing  $\varepsilon$  value notably alters flow dynamics and temperature distribution. Figure 7 also reveals that an increase in the length of the hot wall ( $\varepsilon$ ) significantly reduces the HT rate, as indicated by the isotherm plot and Nu furnished in Table 2. Additionally,  $E_{FF}$ , and  $E_{HT}$  increases with the elongation of  $\varepsilon$ , while Be consistently rises with the extension of  $\varepsilon$  within the triangular cavity, especially near the cylinder surfaces and at the cavity walls. Flow features indicated by streamlines exhibit a steady and symmetric pattern throughout the variation of  $\varepsilon$ . A small corner vortices are noticed at a lower value of  $\varepsilon$ , however the same disappears at higher  $\varepsilon$ .

### 4.4 Variation of Nu<sub>avg</sub>

Table 2 describes the influence of parameters such as  $\varepsilon$ , Ra, and Da on HT efficiency within a fluid system. Notably, an increase in  $\varepsilon$  from 0.2 to 0.4 leads to a significant decrease in the  $Nu_{avg}$ , indicating reduced HT effectiveness. Further increments in  $\varepsilon$  to 0.6 and 0.8 result in diminishing changes in  $Nu_{avg}$ , suggesting that beyond  $\varepsilon = 0.4$ , the decline in HT becomes less pronounced. Additionally, at  $Ra = 10^4$ ,  $Nu_{avg}$  decreases with increasing Ra for varying  $\varepsilon$  values, implying less efficient HT at lower Ra values.

However, for  $Ra = 10^5$  and  $10^6$ ,  $Nu_{avg}$  increases, indicating improved HT efficiency at higher *Ra* values.

### 4.5 Variation of Egen

Table 3 describes the influence of parameters such as  $\varepsilon$ , Ra, and Da on  $E_{gen}$ . Especially, increasing  $\varepsilon$  leads to a corresponding rise in  $E_{gen}$  for specific values of Ra, suggesting an escalation in irreversibility and entropy production within the system. Likewise, as Ra increases from 10<sup>3</sup> to 10<sup>6</sup> for a fixed  $\varepsilon$ ,  $E_{gen}$  also increases, signifying heightened irreversibility and entropy production at higher Ra values. Furthermore, an increase in  $\varepsilon$  for different values of Da and Ra (=10<sup>6</sup>) results in a proportional increase in  $E_{gen}$ , indicating a direct link between higher  $\varepsilon$  values, as Da rises from 10<sup>-5</sup> to 10<sup>-2</sup>,  $E_{gen}$  also intensifies, highlighting the contribution of higher Da values to greater entropy production in the system.

#### 4.6 Variation of Be

Table 4 describes the influence of parameters such as  $\varepsilon$ , Ra, and Da on Be. The dynamics of Be concerning variations in  $\varepsilon$  and Da reveal interesting patterns. When  $Da = 10^{-5}$ , augmenting  $\varepsilon$  leads to a decline in Be, suggesting that higher  $\varepsilon$  values correspond to improved HT efficiency and diminished irreversibility. Conversely, at  $Da = 10^{-4}$ , elevating  $\varepsilon$  from



0.2 to 0.4 initially results in a decrease in *Be*, indicating enhanced HT efficiency, but further increments to 0.6 and 0.8 cause *Be* to rise, implying a shifting equilibrium between HT and irreversibility. For  $Da = 10^{-3}$  and  $10^{-2}$ , increasing  $\varepsilon$  results in a higher *Be*, indicating a greater presence of irreversibility in the system. Moreover, maintaining a constant  $\varepsilon$  value while increasing *Da* correlates with a decrease in *Be*, potentially reflecting improved HT efficiency and reduced irreversibility for higher *Da* values under specific  $\varepsilon$  conditions.

# **5** Discussions

The numerical simulations conducted in this study reveal significant insights into the behaviour of NC and  $E_{gen}$  within a porous triangular cavity containing two cold circular cylinders. The

variations in Ra, Da, and  $\varepsilon$  demonstrate complex interactions between fluid dynamics and HT.

#### 5.1 Impact of Ra

The increase in Ra from  $10^3$  to  $10^6$  enhances the buoyancydriven convective flow, as evidenced by the upward trends in the streamline and isotherm plots (Figure 5). Higher Ra values indicate a dominant convective HT mechanism over conduction. This is reflected in the formation of plume-shaped isotherms at higher Ra, signifying stronger fluid motion and more efficient heat transport away from the heated wall. The enhanced convective flow also leads to increased  $E_{gen}$  due to both HT and FF, with  $E_{gen}$  due to both HT being more prominent. These results align with the fundamental principles of thermodynamics, where increased

Parameters		<i>ε</i> = 0.2	$\varepsilon = 0.4$	$\varepsilon = 0.6$	$\varepsilon = 0.8$
$Da = 10^{-2}$	$Ra = 10^3$	20.218	8.289	6.5457	5.4892
	$Ra = 10^4$	19.797	8.045	6.5431	5.4895
	$Ra = 10^{5}$	26.919	13.379	11.609	8.2709
	$Ra = 10^{6}$	54.743	31.129	25.315	14.878
$Ra = 10^6$	$Da = 10^{-5}$	19.87	8.1318	6.5222	5.4678
	$Da = 10^{-4}$	8.1318	8.4713	8.3548	6.2286
	$Da = 10^{-3}$	47.926	26.467	21.427	13.287
	$Da = 10^{-2}$	54.743	31.129	25.315	14.878

TABLE 2 Variation of Nuavg for different *ε*, Ra, and Da

TABLE 3 Variation of  $E_{gen}$  for different Da and Ra.

Parameters		<i>ε</i> = 0.2	<i>ε</i> = 0.4	<i>ε</i> = 0.6	<i>ε</i> = 0.8
$Da = 10^{-2}$	$Ra = 10^3$	2.8615	4.2242	6.1193	9.3227
	$Ra = 10^4$	2.8697	4.2545	6.1440	9.3447
	$Ra = 10^{5}$	5.0571	8.5267	11.106	13.906
	$Ra = 10^{6}$	12.399	21.379	27.656	28.096
$Ra = 10^{6}$	$Da = 10^{-5}$	2.8636	4.2391	6.1268	9.3296
	$Da = 10^{-4}$	3.6678	6.1258	8.1408	10.816
	$Da = 10^{-3}$	9.7715	16.625	20.7	22.49
	$Da = 10^{-2}$	12.399	21.379	27.656	28.096

thermal gradients and fluid velocities contribute to higher entropy production.

### 5.2 Impact of Da

Variations in Da from  $10^{-5}$  to  $10^{-2}$  indicate changes in the permeability of the porous medium, significantly affecting the fluid flow and HT. Higher Da values allow more hot fluid to pass through the pores, increasing convective HT and  $E_{gen}$ , particularly near the cavity walls (Figure 6). The local *Be* contours reveal isentropic spots near the cold pipe walls at lower Da values, which become denser with higher permeability, aiding HT. The symmetrical patterns observed across different Da values suggest a consistent influence of permeability on the system's thermal behaviour.

### 5.3 Impact of $\varepsilon$

Increasing the length of the heated segment ( $\varepsilon$ ) from 0.2 to 0.8 results in notable changes in flow dynamics and temperature distribution (Figure 7). A smaller  $\varepsilon$  value (0.2) exhibits two distinct rotating cells, while larger  $\varepsilon$  values reduce the HT rate, as indicated by

TABLE 4	Variation	of B	e for	different	Da	and Ra	1.

		<i>ε</i> = 0.2	<i>ε</i> = 0.4	<i>ε</i> = 0.6	<i>ε</i> = 0.8
$Da = 10^{-2}$	$Ra = 10^3$	0.99999	0.99995	0.99992	0.99992
	$Ra = 10^4$	0.99873	0.99609	0.99512	0.99508
	$Ra = 10^{5}$	0.87358	0.92253	0.94436	0.94639
	$Ra = 10^{6}$	0.3316	0.4146	0.56913	0.62436
$Ra = 10^{6}$	$Da = 10^{-5}$	0.99979	0.99918	0.99887	0.99885
	$Da = 10^{-4}$	0.98059	0.97800	0.97991	0.98049
	$Da = 10^{-3}$	0.62617	0.72729	0.84351	0.86788
	$Da = 10^{-2}$	0.3316	0.41460	0.56913	0.62436

the isotherm plots and  $Nu_{avg}$  values in Table 2. This reduction is due to the increased area over which heat must be dissipated, leading to lower temperature gradients and less efficient HT. Additionally, both  $E_{gen}$  due to FF and HT increase with larger  $\varepsilon$  values, highlighting the role of heated segment length in enhancing  $E_{gen}$  within the cavity.

# **6** Practical implications

The findings from this study have practical implications for the design of eco-friendly cooling systems, particularly in buildings located in hot climates. By optimizing the parameters studied (*Ra*, *Da*, and  $\varepsilon$ ), engineers can design more efficient passive cooling systems that reduce energy consumption and mitigate urban heat island effects. The insights gained from  $E_{gen}$  analysis can inform the development of advanced HT systems, such as heat exchangers and electronic cooling devices, where minimizing entropy production is crucial for enhancing performance and efficiency.

# 7 Conclusion

Our detailed study investigated how physical factors interact in a porous triangular space with two cylinders. We focused on understanding HT, fluid dynamics, and  $E_{gen}$  for air. By analyzing *Ra*, *Da*, and  $\varepsilon$ , we observed changes in the system. Some important findings are presented below:

- At strong convection  $Ra = 10^6$ , the increase in Da from the value of  $Da = 10^{-5}$  to  $Da = 10^{-2}$  led to a sharp rise in HT regardless of the size of the heated segment  $\varepsilon$ .
- $\bullet$  Increasing the active length  $\epsilon$  always reduces the average HT rate.
- The rate of  $E_{gen}$  always rises with the length of heated segment  $\varepsilon$ , convection strength Ra and the permeability of the airflow within the pores.
- Increasing the convection strength leads to the dominant feature, the viscous irreversibility, over HT irreversibility.
- Increasing the airflow through the pores leads to more convective HT and viscous irreversibility.

Future research could explore experimental validation of the numerical results and investigate the impact of different fluid types and boundary conditions on NC and  $E_{gen}$  within porous cavities. Additionally, studies could examine the transient behaviour of the system to understand the time-dependent dynamics of HT and fluid flow.

## Data availability statement

The original contributions presented in the study are included in the article/Supplementary Material, further inquiries can be directed to the corresponding author.

#### Author contributions

AA-W: Formal Analysis, Investigation, Methodology, Visualization, Writing-original draft. ST: Formal Analysis,

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Investigation, Methodology, Writing-original draft. PN: Investigation, Methodology, Writing-review and editing. AP: Supervision, Writing-original draft, Writing-review and editing. GS: Conceptualization, Project administration, Supervision, Writing-review and editing. SS: Project administration, Resources, Supervision, Writing-review and editing.

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# Nomenclature

Α	Aspect ratio
Be	Bejan number
Da	Darcy number
$E_{FF}$	Entropy generation due to fluid friction
Egen	Entropy generation
$E_{HT}$	Entropy generation due to heat transfer
F	Fluid friction
Gr	Grashof number
HT	Heat transfer
На	Hartman number
L	Triangular side length
Nu	Nusselt number
Nu <sub>avg</sub>	Average Nusselt number
Р	Non-dimensional pressure
Pr	Prandtl number
Ra	Rayleigh number
T <sub>C</sub>	Cold temperature
T <sub>H</sub>	Hot temperature
U	Non-dimensional velocity component in the horizontal direction
V	Non-dimensional velocity component in the vertical direction
X	Non-dimensional coordinate in the horizontal direction
Y	Non-dimensional coordinate in the vertical direction
Greek symbols	
Ε	Length of the hot or cold wall
θ	Non-dimensional temperature Subscription
avg	Average
gen	Generation
С	Cold

H Hot