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# A two-phase, multi-component model for efficient CO<sub>2</sub> storage and enhanced gas recovery in low permeability reservoirs

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**Introduction:** Carbon dioxide (CO<sub>2</sub>) enhanced gas recovery represents a viable strategy for sequestering CO<sub>2</sub> while concurrently augmenting gas production from subsurface reservoirs. Gas reservoirs, as inherent geological formations, are optimal repositories for gaseous compounds, rendering them suitable for CO<sub>2</sub> storage. Nevertheless, the economic viability of pure CO<sub>2</sub> storage necessitates integration with oil and gas recovery mechanisms to facilitate widespread CO<sub>2</sub> utilization.

**Method:** This study addresses the complexities of CO<sub>2</sub> enhanced gas recovery through a comprehensive approach that combines theoretical model and numerical simulations. A numerical model is developed to simulate three-component diffusion involving CO<sub>2</sub>, and methane (CH<sub>4</sub>) in a two-phase system comprising gas and water.

**Results:** The investigation systematically explores the process of enhanced CH<sub>4</sub> extraction and CO<sub>2</sub> injection into the reservoir and examines the influencing factors on extraction. Simulation results reveal a power-law decrease in CH<sub>4</sub> production rate, stabilizing at a constant extraction rate. Enhanced CH<sub>4</sub> extraction benefits from increased porosity, with higher porosity levels leading to greater CH<sub>4</sub> extraction. Permeability augmentation positively influences CH<sub>4</sub> production, although with diminishing returns beyond a certain threshold. The CO<sub>2</sub> injection rate shows a direct proportionality to CH<sub>4</sub> production. However, elevated CO<sub>2</sub> injection rates may increase reservoir pressure, potentially causing cap rock damage and CO<sub>2</sub> gas flushing.

**Discussion:** This study contributes valuable theoretical insights to the field of CO<sub>2</sub> enhanced gas recovery engineering, shedding light on the intricate dynamics of multi-component fluid transport processes and their implications for sustainable CO<sub>2</sub> utilization.

## KEYWORDS

CO<sub>2</sub> geological storage, CO<sub>2</sub>-EGR, two-phase flow, multi-component diffusion, low permeability reservoir

## 1 Introduction

CO<sub>2</sub> is the main greenhouse gas. In order to mitigate and ameliorate the impact of the greenhouse effect on human life, countries around the world are actively taking measures and countermeasures to reduce CO<sub>2</sub> emissions. Among them, CO<sub>2</sub> geological storage has received great attention globally as an effective method to reduce carbon emissions (Bachu, 2000; Weiyang and Chen, 2005; LIU et al., 2005; U. S. Department of Energy and Office of

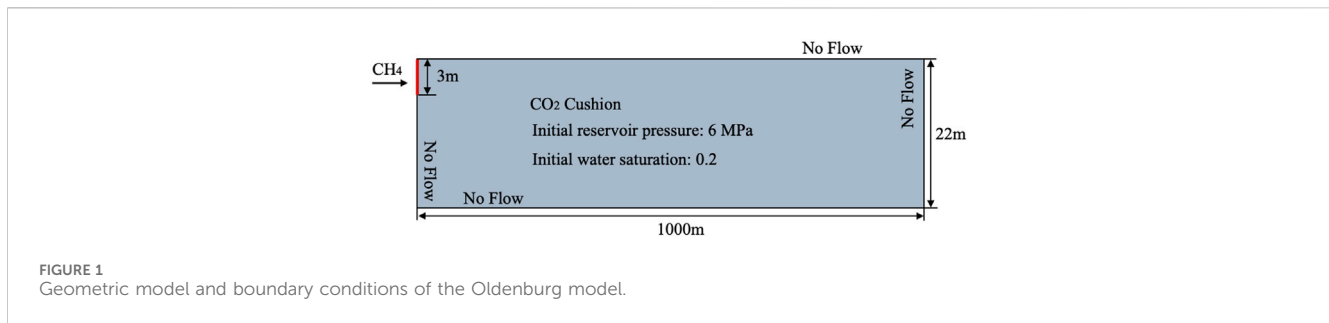


TABLE 1 Parameter properties of the simulation.

Variable	Numerical	Units
Porosity	0.3	[-]
Permeability	$1.0 \times 10^{-13}$	[m <sup>2</sup> ] [m <sup>2</sup> ]
Temperature	313.15	[K] [Pa · s]
Initial pressure	$6.0 \times 10^6$	[Pa] [Pa · s]
CH <sub>4</sub> injection rate	$1.8375 \times 10^{-2}$	[kg/s]
Gas diffusion coefficient	$1.0 \times 10^{-6}$	[m <sup>2</sup> /s]

Fossil Energy and National Energy Technology Laboratory, 2005; Pei et al., 2005; Liu et al., 2005). Common sites for geological storage of CO<sub>2</sub> include deep saline formations, depleted oil and gas reservoirs, unrecoverable reservoirs and oceans (Bonder, 1992; Li and Bai, 2005; XU et al., 2005; Yuchao, 2005; Wu et al., 2008). However, pure CO<sub>2</sub> storage is expensive, so it is necessary to combine the storage with the enhancement of oil and gas recovery to realize the large-scale utilization of CO<sub>2</sub>. The gas storage of gas-bearing reservoirs and the closure of the trap have been fully confirmed in the long-term natural gas storage stage and the development stage of natural gas, so it is feasible to realize the buried storage in the gas reservoir.

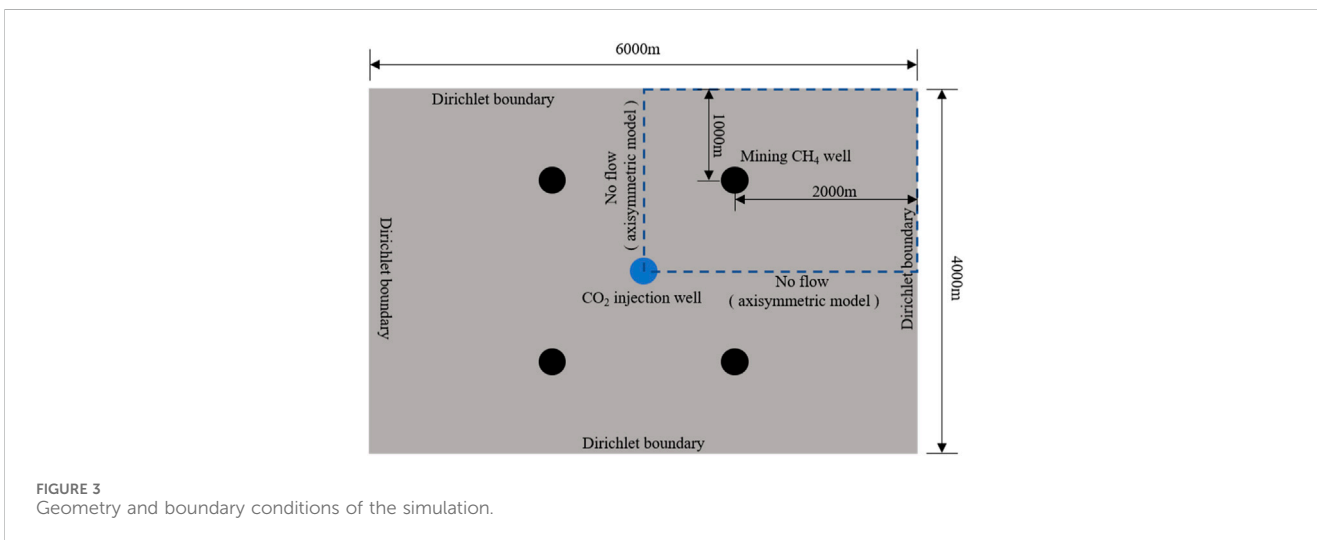
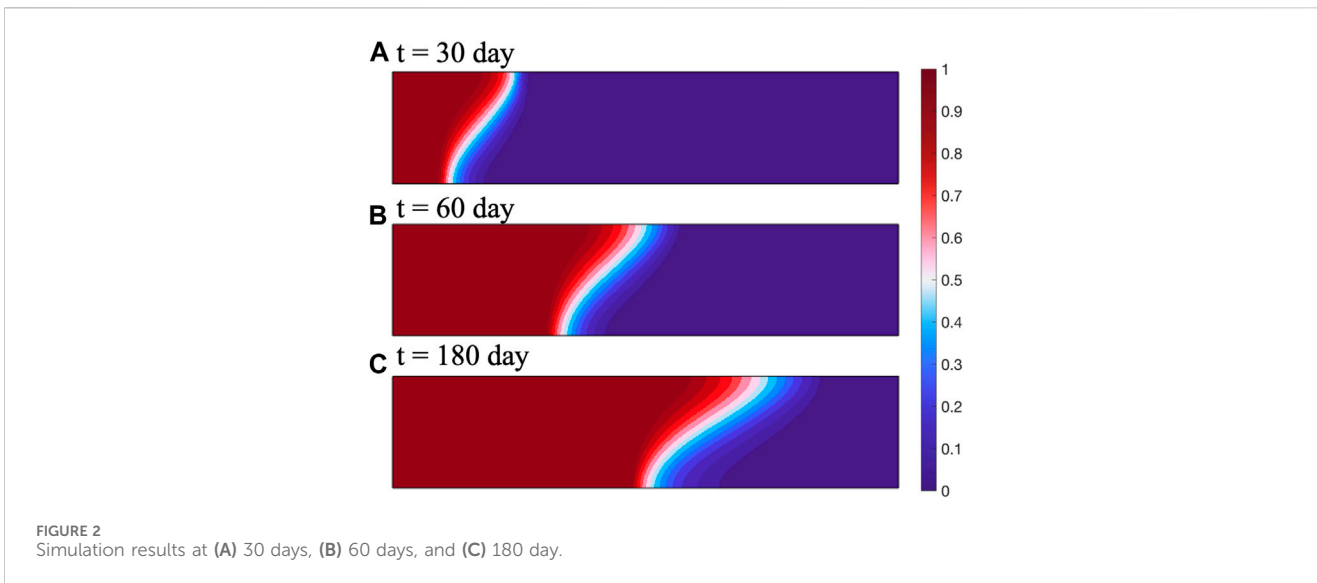
The mechanism of CO<sub>2</sub> to improve gas recovery mainly has the following four aspects: 1. Increase the reservoir pressure gradient to improve the natural gas seepage rate; 2. The significant density difference between CO<sub>2</sub> and natural gas will lead to gravitational differentiation, so the CO<sub>2</sub> at the bottom of the reservoir has a lifting effect on the natural gas; 3. Under the conditions of temperature and pressure of the reservoir, CO<sub>2</sub> tends to be in a supercritical state, and its viscosity is much higher than that of the natural gas, which produces the ratio of the fluidity that is favorable for the replacement; 4. The CO<sub>2</sub> displaces CH<sub>4</sub> in the reservoir through the competition adsorption effect (Busch et al., 2006; Liang et al., 2010; Katayama, 2023). Enhanced gas recovery using CO<sub>2</sub> not only enables geological storage of CO<sub>2</sub>, but also increases CH<sub>4</sub> production (Hamza et al., 2021; Zhang et al., 2023).

The mixing of injected CO<sub>2</sub> and natural gas in the reservoir affects the driving efficiency and leads to the rapid breakthrough of CO<sub>2</sub> in the production wells, resulting in the poor effect of driving the gas to improve recovery, and the CO<sub>2</sub> in the recovered gas further increases the difficulty and cost of the surface treatment process and reduces the comprehensive economic benefits of CO<sub>2</sub>-EGR, so it is of great significance to control the CO<sub>2</sub>-CH<sub>4</sub> mixing. K.

Damen et al. (Damen et al., 2005) analyzed the economics of reservoir geological disposal of CO<sub>2</sub> collected from China using a multi-criteria analysis including technical and socio-economic criteria. Y. Kurniawan et al. (Kurniawan et al., 2006) used numerical simulations to investigate the competitive adsorption of two-component (CH<sub>2</sub>-CO<sub>4</sub>) gas in crack like pore structures; V. Goetz et al. (Goetz et al., 2006) conducted experimental studies on the adsorption of CO<sub>2</sub> and CH<sub>4</sub> mixed gases on activated carbon and obtained adsorption isotherms for different gases. K. Jessen et al. (Jessen et al., 2008) conducted experimental and simulation studies on CH<sub>4</sub> extraction by gas injection, but the coal samples used were powder synthesized specimens; T. Theodore et al. (Theodore et al., 2004) introduced experimental and simulation studies on CO<sub>2</sub> storage in reservoirs jointly conducted by the University of Southern California and the Australian National University, focusing on the impact of reservoir structure on CO<sub>2</sub> geological disposal.

Indoor experiments on CO<sub>2</sub> and reservoir fluids are often limited by time and space, and the experiments cannot effectively reflect the interaction between CO<sub>2</sub> and reservoir fluids across time and space scales in the CO<sub>2</sub>-EGR process. Although numerical simulation can solve the problems of time and space scales, CO<sub>2</sub> and reservoir fluids involve multiphase and multi-component coupling processes. Therefore, numerical models that characterizes the migration of multiple components such as CO<sub>2</sub>, CH<sub>4</sub>, and reservoir water in reservoirs are needed for numerical simulation analysis of CO<sub>2</sub> enhanced CH<sub>4</sub> recovery.

In this article, we derive the control equation for two-phase, three component flow and establish a numerical model for CO<sub>2</sub> injection and production of CH<sub>4</sub> based on the proposed multiphase multi-component flow theory. We use Partial Differential Equation Module (PDE) of COMSOL for solving the governing equations, studying the migration of CO<sub>2</sub>, CH<sub>4</sub>



and water in the process of CO<sub>2</sub> injection and production in the isotropic reservoir. By changing the permeability, porosity and CO<sub>2</sub> injection rate of the reservoir, we studied the influence of reservoir parameters and injection schemes on the distribution of reservoir stress and the extraction of CH<sub>4</sub>.

## 2 Mathematical model

### 2.1 Governing equation of gas-water two-phase flow

Base on the mass conservation of the aquifer fluid, the continuity equation for gas-water two-phase flow is as follows (Martin et al., 2005a; Martin et al., 2005b; Ma et al., 2021; Ma et al., 2023):

$$\frac{\partial m_\alpha}{\partial t} + \nabla \cdot (\rho_\alpha v_\alpha) - q_\alpha = 0, \alpha = w, g \quad (1)$$

where  $m_\alpha$  is the fluid mass,  $q_\alpha$  is the source ( $\alpha = w, g$  represents water and gas, respectively). The fluid velocity is described by Darcy's law:

$$v_\alpha = -\frac{k k_\alpha^r}{\mu_\alpha} (\nabla P_\alpha - \rho_\alpha \mathbf{g}) \quad (2)$$

where  $k$  represents permeability, and  $k_\alpha^r$  is the relative permeability,  $\mu_\alpha$  is fluid viscosity,  $P_\alpha$  is pore pressure,  $\rho_\alpha$  is the fluid density, and  $\mathbf{g}$  is the gravitational acceleration. The mass of each phase can be described as:

$$m_\alpha = S_\alpha \rho_\alpha \phi \quad (3)$$

where  $S_\alpha$  is fluid saturation,  $\rho_\alpha$  is fluid density,  $\phi$  is porosity.

### 2.2 Governing equations of gas diffusion

According to Fick's law, the diffusion flux per unit cross-sectional area perpendicular to the diffusion direction per unit time is directly proportional to the concentration gradient at that

TABLE 2 Case parameter settings.

Variable	Numerical	Units
Porosity	0.07	[-]
Permeability	$2.0 \times 10^{-15}$	[m <sup>2</sup> ] [m <sup>2</sup> ]
Entering capillary pressure	$1.0 \times 10^5$	[Pa] [Pa · s]
Pore distribution index	2	[-]
Residual water saturation	0	[-]
Residual gas saturation	0	[-]
Gas diffusion coefficient	$1.0 \times 10^{-5}$	[m <sup>3</sup> /s] [Pa]

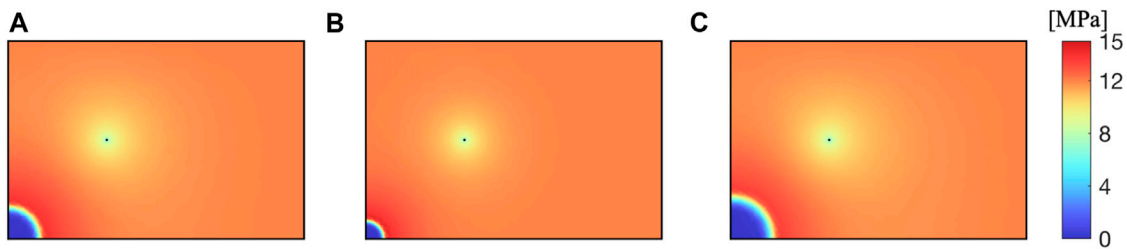


FIGURE 4 (A) 100 days, (B) 300 days, and (C) 500 days results of CH<sub>4</sub> pressure in reservoirs.

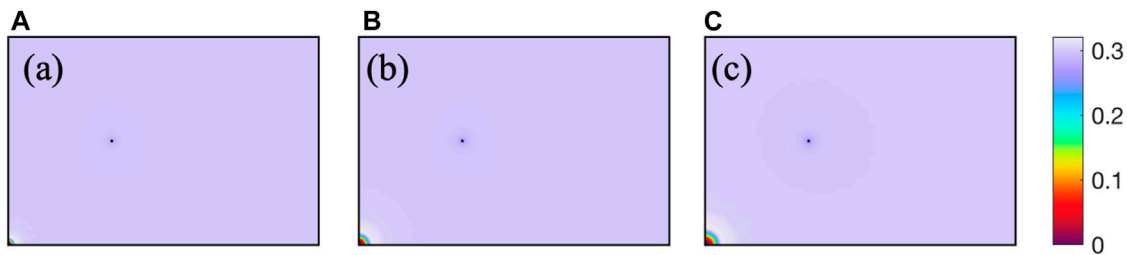


FIGURE 5 (A) 100 days, (B) 300 days, and (C) 500 days reservoir water saturation results.

cross-section (Nie et al., 2000; Qin et al., 2012; Qin et al., 2013; Li, 2015; Wang, 2015):

$$\left[ \frac{\partial}{\partial x} \left( D_{AB} S_g \phi M_A \frac{dC_A}{dx} \right) + \frac{\partial}{\partial y} \left( D_{AB} S_g \phi M_A \frac{dC_A}{dy} \right) + \frac{\partial}{\partial z} \left( D_{AB} S_g \phi M_A \frac{dC_A}{dz} \right) \right] dx dy dz dt \quad (4)$$

$$J_A = -D_{AB} \frac{dC_A}{dz} \quad (5)$$

where  $J_A$  is the diffusion flux per unit area of component A in the  $z$ -direction per unit time;  $D_{AB}$  is the diffusion coefficient between components A and B;  $C_A$  is the gas concentration of component A,  $dC_A/dz$  is the concentration gradient of component A in the  $z$ -direction. In the unit, the molecular diffusion flux  $J_A$  of component A gas in the gas phase on the left side. Within  $dt$  time, the mass of component A gas flowing into the unit through molecular diffusion in the  $x$ -direction is:

$$-D_{AB} S_g \phi M_A \frac{dC_A}{dx} dy dz dt \quad (6)$$

The mass of component A gas flowing out of the unit through molecular diffusion in the  $x$ -direction on the right side of the unit is:

$$\left[ \left( -D_{AB} S_g \phi M_A \frac{dC_A}{dx} \right) + \frac{\partial}{\partial x} \left( -D_{AB} S_g \phi M_A \frac{dC_A}{dx} \right) dx \right] dy dz dt \quad (7)$$

Within  $dt$  time, the mass difference of component A in the unit due to gas diffusion is:

$$-\left[ \frac{\partial}{\partial x} (v_{gx} M_A C_A) + \frac{\partial}{\partial y} (v_{gy} M_A C_A) + \frac{\partial}{\partial z} (v_{gz} M_A C_A) \right] dx dy dz dt \quad (8)$$

In summary, the gas convection diffusion equation is obtained as follows:

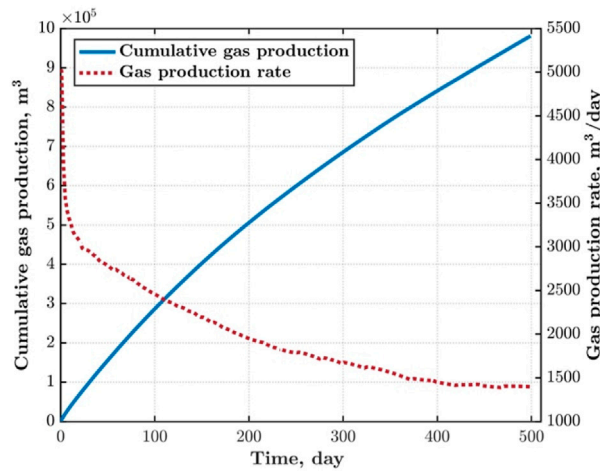


FIGURE 6  
CH<sub>4</sub> production volume and daily productivity.

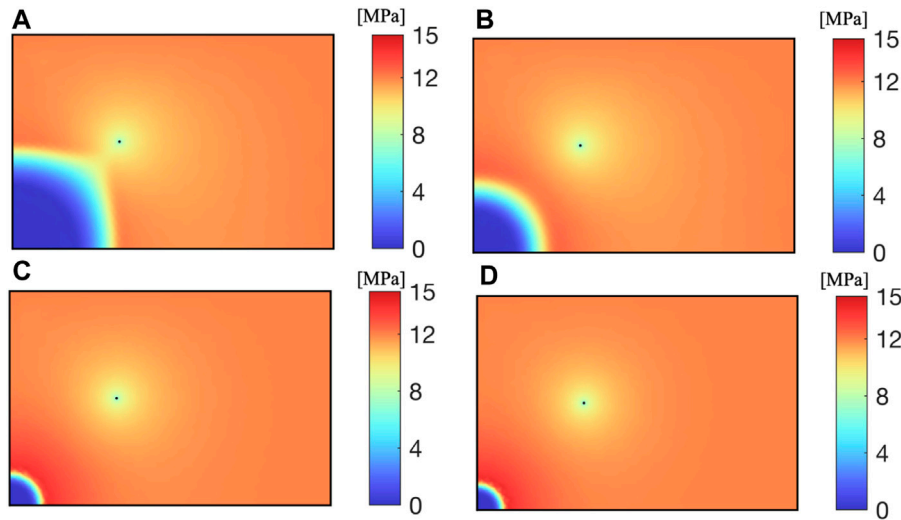


FIGURE 7  
CH<sub>4</sub> pressure with different porosities: (A): 0.0175 (B): 0.035 (C): 0.14 (D): 0.21.

$$\frac{\partial(\phi M_A C_A S_g)}{\partial t} + \nabla \cdot (\mathbf{v}_g M_A C_A) - \nabla \cdot (\phi D_{AB} S_g M_A \nabla C_A) = 0 \quad (9)$$

$$\frac{\partial(\phi M_B C_B S_g)}{\partial t} - \nabla \cdot \left( M_B C_B \frac{k k_{rg}}{\mu_g} (\nabla P_g) \right) - \nabla \cdot (\phi D_{AB} S_g M_B \nabla C_B) = 0 \quad (12)$$

### 2.3 Equation assembly

Substituting Eq. 2 into Eqs 1, 9, the two-phase multi-component seepage model is obtained as follows:

$$\frac{\partial(\phi \rho_w S_w)}{\partial t} - \nabla \cdot \left( \rho_w \frac{k k_{rw}}{\mu_w} (\nabla P_w) \right) = 0 \quad (10)$$

$$\frac{\partial(\phi M_A C_A S_g)}{\partial t} - \nabla \cdot \left( M_A C_A \frac{k k_{rg}}{\mu_g} (\nabla P_g) \right) - \nabla \cdot (\phi D_{AB} S_g M_A \nabla C_A) = 0 \quad (11)$$

where  $M_A$  and  $M_B$  are fixed values for the relative molecular weight of the gas, and  $\rho = MC$ , therefore the equation can be transformed into:

$$\frac{\partial(\phi \rho_w S_w)}{\partial t} - \nabla \cdot \left( \rho_w \frac{k k_{rw}}{\mu_w} (\nabla P_w) \right) = 0 \quad (13)$$

$$\frac{\partial(\phi \rho_A S_g)}{\partial t} - \nabla \cdot \left( \rho_A \frac{k k_{rg}}{\mu_g} (\nabla P_g) \right) - \nabla \cdot (\phi D_{AB} S_g \nabla \rho_A) = 0 \quad (14)$$

$$\frac{\partial(\phi \rho_B S_g)}{\partial t} - \nabla \cdot \left( \rho_B \frac{k k_{rg}}{\mu_g} (\nabla P_g) \right) - \nabla \cdot (\phi D_{AB} S_g \nabla \rho_B) = 0 \quad (15)$$

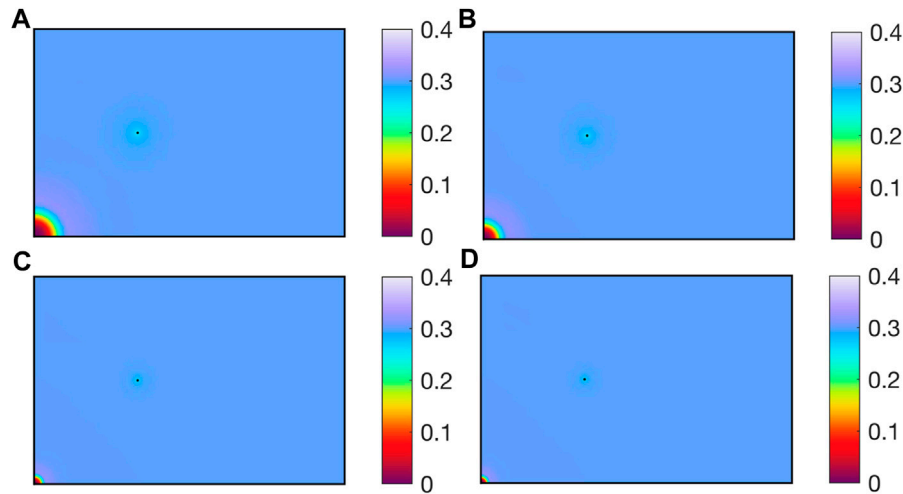


FIGURE 8 Water saturation at different porosities: (A): 0.0175 (B): 0.035 (C): 0.14 (D): 0.21.

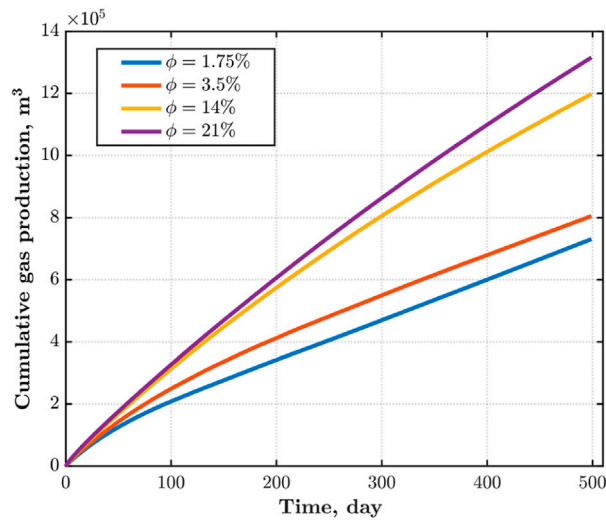


FIGURE 9 CH4 production.

Due to the presence of two gases in the gas phase, the pressures of the two gases are defined as  $p_A$ ,  $p_B$ :

$$p_g = p_A + p_B \tag{16}$$

Substitute the saturation equation and capillary pressure equation into:

$$\begin{cases} S_w + S_g = 1 \\ p_w = p_g - p_c \end{cases} \tag{17}$$

There are five variables for solving the equation system:  $S_w$ ,  $S_g$ ,  $p_w$ ,  $p_A$  and  $p_B$ . There are also five equations, which are closed and solvable. The remaining parameters are calculated using the method of calculating physical properties parameters:  $\rho_i = \rho_i(p_i)$ ;  $\mu_g = \mu_g(p_g)$ ;  $\mu_w = \mu_w(p_w)$ ;  $k_{rw} = k_{rw}(S_w)$ ;  $k_{rg} = k_{rg}(S_w)$ ;  $p_c = p_c(S_w)$ .

Substitute the equations into and eliminate  $S_g$ ,  $p_w$  and  $p_g$ . We obtain a system of equations for variables  $S_w$ ,  $p_A$  and  $p_B$ :

$$\frac{\partial(\phi \rho_w S_w)}{\partial t} - \nabla \cdot \left( \rho_w \frac{k k_{rw}}{\mu_w} (\nabla(p_A + p_B - p_c)) \right) = 0 \tag{18}$$

$$\begin{aligned} \frac{\partial(\phi \rho_A (1 - S_w))}{\partial t} - \nabla \cdot \left( \rho_A \frac{k k_{rg}}{\mu_g} (\nabla(p_A + p_B)) \right) \\ - \nabla \cdot (\phi D_{AB} (1 - S_w) \nabla p_A) = 0 \end{aligned} \tag{19}$$

$$\begin{aligned} \frac{\partial(\phi \rho_B (1 - S_w))}{\partial t} - \nabla \cdot \left( \rho_B \frac{k k_{rg}}{\mu_g} (\nabla(p_A + p_B)) \right) \\ - \nabla \cdot (\phi D_{AB} (1 - S_w) \nabla p_B) = 0 \end{aligned} \tag{20}$$

According to the Brooks Corey model capillary pressure calculation formula, the capillary pressure is as follows:

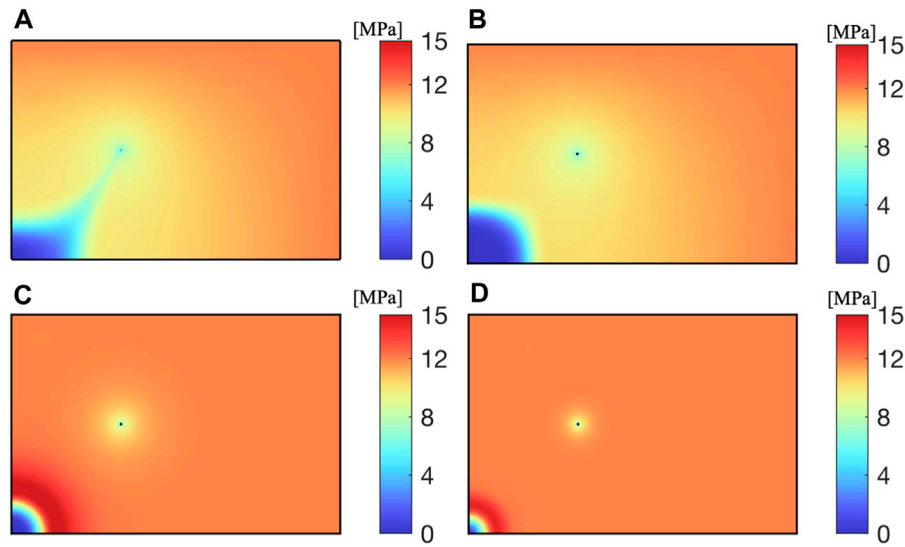


FIGURE 10  
CH<sub>4</sub> pressure at different permeabilities (A):  $2 \times 10^{-13} m^2$  (B):  $2 \times 10^{-14} m^2$  (C):  $2 \times 10^{-16} m^2$  (D):  $2 \times 10^{-17} m^2$

$$\nabla p_c = \frac{dp_c}{dS_w} \nabla S_w = \frac{P_t (-1/\omega) S_e^{-1/\omega-1}}{1 - S_w^r - S_g^r} \nabla S_w \quad (21)$$

$$\frac{\partial p_c}{\partial t} = \frac{dp_c}{dS_w} \frac{\partial S_w}{\partial t} = \frac{P_t (-1/\omega) S_e^{-1/\omega-1}}{1 - S_w^r - S_g^r} \frac{\partial S_w}{\partial t} \quad (22)$$

The final control equation is as follows:

$$\left( \phi \rho_w - \phi \rho_w c_w S_w \frac{dp_c}{dS_w} \right) \frac{\partial S_w}{\partial t} + (\phi \rho_w c_w S_w) \frac{\partial p_A}{\partial t} + (\phi \rho_w c_w S_w) \frac{\partial p_B}{\partial t} - \nabla \cdot \left( \rho_w \frac{kk^r}{\mu_w} (\nabla p_A + \nabla p_B - p_c' \nabla S_w) \right) = 0 \quad (23)$$

$$\begin{aligned} & (-\phi \rho_A) \frac{\partial S_w}{\partial t} + (\rho_A (1 - S_w) + \phi \rho_A' (1 - S_w)) \frac{\partial p_A}{\partial t} + (\phi \rho_A' (1 - S_w)) \\ & \left( \frac{\partial p_B}{\partial t} - \nabla \cdot \left( \rho_A \frac{kk^r}{\mu_g} (\nabla p_A + \nabla p_B) \right) \right) \rho_A \frac{kk^r}{\mu_g} \\ & - \nabla \cdot (\phi D_{AB} (1 - S_w) \rho_A' \nabla p_A) = 0 \end{aligned} \quad (24)$$

$$\begin{aligned} & (-\phi \rho_B) \frac{\partial S_w}{\partial t} + (\phi \rho_B' (1 - S_w)) \frac{\partial p_A}{\partial t} + (\phi \rho_B' (1 - S_w)) \frac{\partial p_B}{\partial t} \\ & - \nabla \cdot \left( \rho_B \frac{kk^r}{\mu_g} (\nabla p_A + \nabla p_B) \right) \rho_B \frac{kk^r}{\mu_g} \\ & - \nabla \cdot (\phi D_{AB} (1 - S_w) \rho_B' \nabla p_B) = 0 \end{aligned} \quad (25)$$

### 3 Verification

This section verifies the accuracy of the proposed two-phase multi-component model by comparing the results of Oldenburg's simulation scheme (Oldenburg, 2003). The reservoir model has a vertical depth of 22 m and a horizontal length of 1000 m. The wellhead is located on the left boundary of the reservoir, 3 m away from the upper boundary. The

remaining boundaries are no-flow. The reservoir model is shown in Figure 1. The reservoir has a constant temperature of 313.15 K, an initial reservoir pressure of 6 MPa, an initial water saturation of 0.2, a gas phase saturation of 0.8, and a gas phase entirely composed of CO<sub>2</sub>. The simulation plan involves injecting CH<sub>4</sub> gas into the injection well at a rate of  $1.8375 \times 10^{-2}$  kg/s for 180 days. The parameter properties of the simulation are listed in Table 1.

The simulation results are shown in Figure 2. As the CH<sub>4</sub> is injected, the CO<sub>2</sub> component is continuously pushed towards the right side of the reservoir, and the diffusion zone gradually increases. The distance between the center of the mixed zone and the wellhead gradually increases, the movement rate gradually decreases. This is consistent with the model results of Oldenburg, indicating the applicability and accuracy of this model in gas diffusion problems.

### 4 Model setup

We set up a reservoir model with a reservoir plane size of 6000 m × 4000 m. The reservoir is homogeneous and isotropic. The initial water saturation of the reservoir is 0.3, and the rest gas is CH<sub>4</sub>. The initial reservoir pressure is 12 MPa, the absolute permeability is  $K = 2.0 \times 10^{-15} m^2$ , and the porosity is 0.07. An injection well is located at the center of the reservoir to inject CO<sub>2</sub>, and extraction wells are set at the four corners of the reservoir. The specific location and boundary conditions are shown in Figure 3. The simulation plan involves injecting CO<sub>2</sub> from the injection well at a rate of 0.25 kg/s for 500 days and analyzing the CH<sub>4</sub> recovery situation. The specific parameters are listed in Table 2.

### 5 Simulation results

In this section, we discussed CO<sub>2</sub> enhanced CH<sub>4</sub> recovery based on the two-phase multi-component seepage equation. Due to the

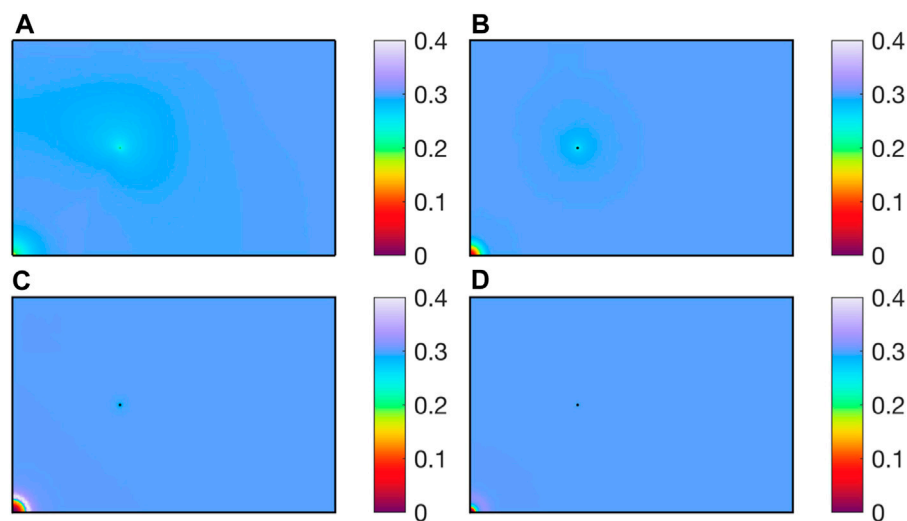


FIGURE 11  
Water saturation at different permeabilities: (A):  $2 \times 10^{-13} m^2$  (B):  $2 \times 10^{-14} m^2$  (C):  $2 \times 10^{-16} m^2$  (D):  $2 \times 10^{-17} m^2$

geometric distribution of CO<sub>2</sub> injection wells and CH<sub>4</sub> extraction wells being symmetric in the simulation domain, in order to improve computational efficiency, we only analyzed a quarter of the CO<sub>2</sub> displacement CH<sub>4</sub> process.

As shown in Figure 4, after CO<sub>2</sub> is injected into the reservoir, CH<sub>4</sub> inside the reservoir is replaced. The gas pressure of CH<sub>4</sub> near the CO<sub>2</sub> injection well sharply decreases, and as the extraction progresses, CO<sub>2</sub> diffuses towards the vicinity of the extraction well. Near the extraction well, CH<sub>4</sub> pressure decreases uniformly, and CH<sub>4</sub> is extracted through the extraction well.

As shown in Figure 5, after CO<sub>2</sub> is injected into the reservoir, CH<sub>4</sub> and reservoir water are driven away together, forming a CO<sub>2</sub> enrichment zone near the injection well. Near the extraction well, due to the lower well pressure, water and CH<sub>4</sub> are extracted together, decreasing the water saturation.

We study the CH<sub>4</sub> production and daily productivity, as shown in Figure 6, of the extraction wells. Among them, the daily productivity of CH<sub>4</sub> shows a power-law decreasing trend, with CH<sub>4</sub> productivity reaching its maximum in the early stages of extraction; As extraction proceeds, the daily CH<sub>4</sub> production rate decreases due to the decrease in reservoir pressure. In the later stage of extraction, CH<sub>4</sub> productivity reaches equilibrium and remains basically unchanged. The growth rate of production decreases as extraction progresses.

## 6 Sensitive analysis

### 6.1 Effect of porosity

In this section, we investigate the distribution of CH<sub>4</sub> pressure, water saturation, and evolution of CH<sub>4</sub> extraction under different reservoir porosities of 0.0175, 0.035, 0.14, and 0.21.

Porosity of reservoir has a significant impact on CH<sub>4</sub> pressure distribution. As shown in the Figure 7, the smaller the porosity of the reservoir, the greater the impact range of CO<sub>2</sub> injection of the same quality. This is because the reduction of pore space results in the

same volume of CO<sub>2</sub> occupying a larger reservoir area. When the porosity of the reservoir is 0.0175, the CO<sub>2</sub> injection well and the CH<sub>4</sub> production well are connected, and all the CH<sub>4</sub> in the middle is driven out. When the porosity is greater than 0.14, the influence of porosity on pore pressure decreases.

As shown in Figure 8, the larger the porosity, the larger the pore volume of the same area reservoir, and more CO<sub>2</sub> needs to be injected to expand its influence area; The smaller the porosity, the larger the impact area of the same CO<sub>2</sub> injection amount, and more CH<sub>4</sub> and water from the reservoir pores are driven out by CO<sub>2</sub>.

As shown in Figure 9, with the increase of porosity, the CH<sub>4</sub> extraction rate increases; The larger the porosity, the more CH<sub>4</sub> stored near the extraction well. Under the same production well pressure and CO<sub>2</sub> injection rate, the greater the CH<sub>4</sub> production.

### 6.2 Effect of permeability

In this section, we investigate the distribution of CH<sub>4</sub> pressure, water saturation, and evolution of CH<sub>4</sub> extraction with permeability being with  $2 \times 10^{-13} m^2$ ,  $2 \times 10^{-14} m^2$ ,  $2 \times 10^{-16} m^2$  and  $2 \times 10^{-17} m^2$ .

The permeability of the reservoir determines the migration ability of fluids in the reservoir. As shown in Figure 10, the higher the permeability of the reservoir, the faster CO<sub>2</sub> diffuses from the injection well to the surrounding area at the same time. When the permeability is  $2 \times 10^{-13} m^2$ , the pressure of the CO<sub>2</sub> injection well and the CH<sub>4</sub> production well interact with each other, and CO<sub>2</sub> flows directly from the injection well to the production well. The lower the permeability, the less CH<sub>4</sub> displaced by CO<sub>2</sub> injection, which is not conducive to CH<sub>4</sub> extraction.

As shown in Figure 11, the influence range of extraction and injection wells is highly correlated with the reservoir permeability. Within the same extraction time, reservoirs with higher permeability can produce more CH<sub>4</sub>; Reservoirs with low permeability face greater difficulties in both CO<sub>2</sub> injection and CH<sub>4</sub> extraction, resulting in lower CO<sub>2</sub> recovery efficiency.



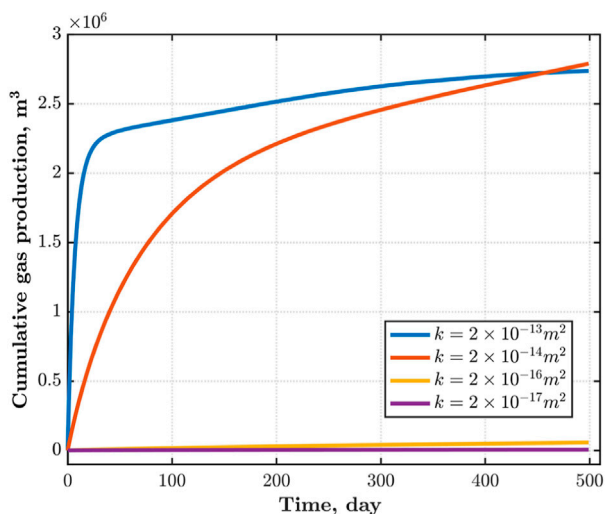


FIGURE 12  
CH<sub>4</sub> production under different permeabilities.

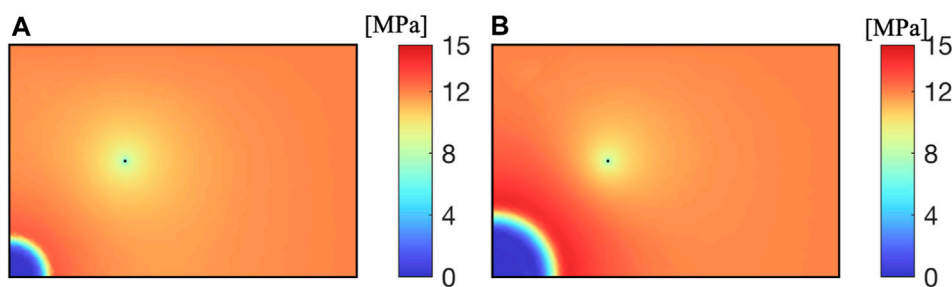


FIGURE 13  
CH<sub>4</sub> pressure at different injection rates (A): 0.125 kg/ (B): 0.5 kg/s.

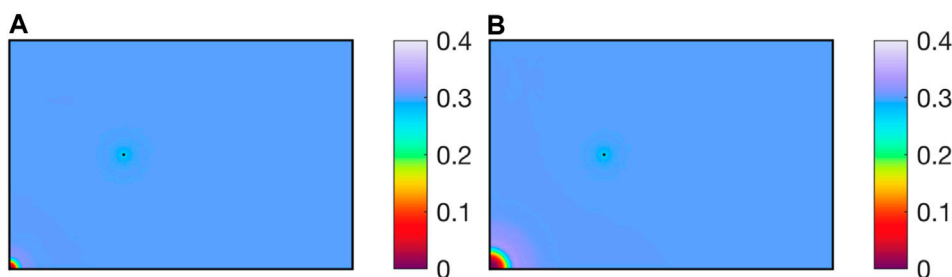


FIGURE 14  
Water saturation at different injection rates (A): 0.125 kg/ (B): 0.5 kg/s.

Permeability has a great impact on CH<sub>4</sub> production. As shown in Figure 12, the greater the permeability, the more CH<sub>4</sub> extraction. However, blindly increasing the permeability of the reservoir has a saturation value for the increase in CH<sub>4</sub> production. When the permeability of the reservoir increases from  $2 \times 10^{-14} m^2$  to  $2 \times 10^{-13} m^2$ , CH<sub>4</sub> production changes slightly. This may be

because the high permeability reservoir causes the injected CO<sub>2</sub> to diffuse to the production well and be extracted. When the permeability reaches a certain level, the reservoir pressure drops too quickly, and the CO<sub>2</sub> injection well and CH<sub>4</sub> production well are connected. After CO<sub>2</sub> breakthrough, The proportion of CH<sub>4</sub> in the production well decreases, making it difficult to extract CH<sub>4</sub>.

### 6.3 Effect of CO<sub>2</sub> injection rate

In this section, we investigate the distribution of CH<sub>4</sub> pressure and water saturation with injection rate being with 0.125 kg/s and 0.5 kg/s.

As shown in Figure 13, the higher the CO<sub>2</sub> injection rate, the greater the reservoir pressure, and the larger the range of CO<sub>2</sub> diffusion. Due to CO<sub>2</sub> injecting water and CH<sub>4</sub> into the pores of the reservoir near the well, the CH<sub>4</sub> pressure near the CO<sub>2</sub> injection well decreases, forming a high-pressure zone at the front of the displacement.

As shown in Figure 14, for water saturation at different injection rates. The higher the CO<sub>2</sub> injection rate, the more water and CH<sub>4</sub> are discharged at the same time, forming a low saturation zone near the injection well. For CH<sub>4</sub> extraction wells, the high pressure brought by high injection rates leads to more CH<sub>4</sub> being extracted, and the high CO<sub>2</sub> injection rate increases CH<sub>4</sub> extraction.

## 7 Conclusion

The process of CO<sub>2</sub>-enhanced CH<sub>4</sub> extraction involves the intricate migration dynamics of gas and water phases, incorporating multiple components within the reservoir. Leveraging the derived two-phase flow and multi-component diffusion model, we present a comprehensive numerical model to elucidate the intricate phenomena associated with the multi-component seepage of CO<sub>2</sub>-EGS. This model considers both the water phase and the gas phase, encompassing two distinct components: CO<sub>2</sub> and CH<sub>4</sub>. The main conclusions are derived as follows.

- 1) With the injection of CO<sub>2</sub>, both water and CH<sub>4</sub> within the reservoir pores are displaced. The CH<sub>4</sub> productivity exhibits a power-law decline, ultimately stabilizing at a constant extraction rate, with a progressively diminishing gradient of productivity increase. In the initial extraction stages, the CH<sub>4</sub> production rate attains its peak, declining subsequently due to the diminishing reservoir pressure. In the latter stage of extraction, CH<sub>4</sub> productivity reaches an equilibrium state, demonstrating sustained constancy.
- 2) Higher porosity levels result in augmented CH<sub>4</sub> reserves proximate to extraction wells. However, heightened porosity diminishes the influence of CO<sub>2</sub> on CH<sub>4</sub> recovery, as it reduces the area affected by the reservoir pressure of CO<sub>2</sub>. Conversely, lower porosity levels extend the influence of a given CO<sub>2</sub> injection volume over a larger reservoir range, driving out CH<sub>4</sub> and water over an expansive area.
- 3) Elevated reservoir permeability accelerates CO<sub>2</sub> diffusion from injection wells to the surrounding region. While increased permeability enhances CH<sub>4</sub> production, an indiscriminate escalation of permeability reaches a saturation point for CH<sub>4</sub> production augmentation.

Excessive permeability poses the risk of connecting CO<sub>2</sub> injection wells with CH<sub>4</sub> extraction wells, impeding CH<sub>4</sub> extraction upon CO<sub>2</sub> breakthrough.

- 4) The CO<sub>2</sub> injection rate directly influences the affected area within the reservoir. A higher injection rate results in increased reservoir pressure, leading to greater CH<sub>4</sub> extraction and improved production. Nonetheless, an excessively high CO<sub>2</sub> injection rate induces heightened reservoir pressure, potentially causing cap rock damage and consequent CO<sub>2</sub> release.

## Data availability statement

The original contributions presented in the study are included in the article/Supplementary material, further inquiries can be directed to the corresponding author.

## Author contributions

XW: Conceptualization, Methodology, Project administration, Visualization, Writing—original draft. QZ: Formal Analysis, Methodology, Visualization, Writing—original draft. YW: Investigation, Methodology, Writing—review and editing.

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## Conflict of interest

Authors XW, QZ, and YW were employed by Shaanxi Yanchang Petroleum (Group) Co., Ltd.

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