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## EDITED BY

Enrico Maria Vitucci,  
University of Bologna, Italy

## REVIEWED BY

Mohamed Salem,  
University of Science Malaysia (USM), Malaysia  
Khaled Obaideen,  
University of Sharjah, United Arab Emirates

## \*CORRESPONDENCE

Wanyu Tao,  
✉ 2452872205@qq.com

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# Model predictive control for single-phase cascaded H-bridge photovoltaic inverter system considering common-mode voltage suppression

Xinwei Wei<sup>1</sup>, Wanyu Tao<sup>1\*</sup> and Xunbo Fu<sup>2</sup>

<sup>1</sup>College of Electrical and Power Engineering, Taiyuan University of Technology, Taiyuan, China, <sup>2</sup>State Nuclear Power Planning Design and Research Institute CO., Ltd, Beijing, China

In this article, a model predictive control (MPC) with common-mode voltage (CMV) suppression is proposed for single-phase cascaded H-bridge (CHB) inverters, which can also simultaneously achieve control objectives of grid-connected current tracking, voltages balancing of different H-bridge submodules on the DC-side and switching frequency reduction. To suppress high-frequency components of the common-mode voltage without additional switching devices, the algorithm proposed designs the predicted and reference values of the CMV and incorporates them in the cost function. At the same time, the capacitor voltages balancing control is integrated in the calculation of the optimal modulation function of the H-bridge, which reduces the complexity of control effectively. Besides, switching times of the MOSFETs are compared in two cycles. The cost function is constructed to represent comprehensive effect of the control. Finally, an experiment is performed on the hardware-in-the-loop experimental platform. The experimental results show that the proposed algorithm can offer a better voltage THD and reduce the times of switch action by nearly half while maintaining high-precision current tracking and maximum power point of photovoltaic modules, which alleviate the potential electromagnetic interference and cabling problem.

## KEYWORDS

model predictive control (MPC), photovoltaic system, cascaded H-bridge (CHB), common-mode voltage (CMV), maximum power point tracking (MPPT)

## 1 Introduction

At present, energy shortage and environmental pollution are becoming more and more serious. To change the traditional mode of economic growth with high energy consumption, most countries regard the development of low-carbon economy based on renewable energy as a focus issue (Zhang et al., 2018). Solar energy is one of the most promising future energy supplies for its high production capacity and low cost among various renewable energy sources, whose power generation has grown continuously at a rate of 20% in the past 20 years. It can be foreseen that the photovoltaic (PV) industry will have greater development space in the future (Ebrahimi et al., 2011).

Multilevel inverters have been widely used in high-voltage and high-power occasion to achieve electric energy conversion because of their advantages of high output waveform quality, low switching frequency, small harmonic distortion, and simple scalability (Vijeh et al., 2019; Poorfakhraei and Emadi, 2021; Salem et al., 2021). The cascaded H-bridge (CHB) has simpler structure and fewer switching devices among multilevel inverter topologies, without flying capacitors and clamp diodes. Each submodule of the CHB inverter is powered by the PV strings on the DC side, whose maximum power point tracking (MPPT) can be achieved independently (Yu et al., 2016). Therefore, the CHB inverter is more suitable for the PV system.

Multilevel inverters are available for decades, while new control strategies and modulation techniques are still being explored to improve the performance. To ensure the safe and stable operation of the system, multi objectives should be achieved simultaneously in the CHB inverter, such as suppressing CMV, increasing fault-tolerant ability, balancing floating capacitors, reducing switching frequency, etc.

One of the key objectives is that the balance of output power for PV modules in different H-bridge submodules when receive varied light intensity (Liu et al., 2021). Since the current of each submodule is constant, submodules with higher fundamental modulation voltage may be over modulation, which will increase the harmonic content of output voltage and affect the quality of grid-connected current, even cause oscillation and overcurrent (Rezaei et al., 2010). Existing control strategies for balancing floating capacitors were mainly based on improved MPPT (Eskandari et al., 2013), hybrid modulation technology (Miranbeigi and Iman-Eini, 2016; Zhao et al., 2018a), reactive power compensation (Rezaei et al., 2011; Liu et al., 2015; Wang et al., 2019), and harmonic compensation (Ko et al., 2017; Zhao et al., 2018b; Ko et al., 2018; Ye et al., 2019; Wang et al., 2020; Zhao et al., 2020). An improved MPPT strategy was proposed in (Eskandari et al., 2013), which increased the DC voltage of the over-modulated submodules and adjusted it to deviate from the maximum power point voltage for avoiding the occurrence of over modulation. However, the active power of the PV system was sacrificed, which against the advantages of the CHB inverter. Different hybrid modulation techniques were proposed to achieve power balancing of submodules to improve the DC voltage utilization of the inverter in (Miranbeigi and Iman-Eini, 2016; Zhao et al., 2018a). However, the fluctuation of DC voltage was increased, which is detrimental to efficiency of the PV system. The reactive power compensation angle was amplified in (Rezaei et al., 2011; Liu et al., 2015; Wang et al., 2019), which could reduce the fundamental amplitude of the output voltage and the probability of over modulation when the DC voltage remain constant. However, the power factor of the PV system was reduced while additional reactive power compensation equipment was required. A series of harmonic compensation methods were proposed in (Ko et al., 2017; Zhao et al., 2018b; Ko et al., 2018; Ye et al., 2019; Wang et al., 2020; Zhao et al., 2020), which could increase the utilization of DC voltage to 1.15 (Ko et al., 2017; Zhao et al., 2018b; Wang et al., 2020) and 1.273 (Ko et al., 2018; Ye et al., 2019; Zhao et al., 2020), respectively. However, the harmonic distribution of the output voltage for the CHB inverter was impacted and existing research lacked quantitative analysis.

The suppression of leakage current is also significant. There is a direct electrical connection between PV modules and the power grid without isolation transformer. Voltage of the parasitic capacitor between the ground and PV modules will change when inverter switches are activated, which result in the leakage current. The leakage current will cause electromagnetic interference and threaten personal safety (Ni et al., 2020). Therefore, suppression of the leakage current is essential for the PV system. In (Li et al., 2015; Chen et al., 2017), modified circuit topologies were applied to the PV system for suppressing leakage current, such as Heric, H5, H6, etc. However, the suppression effect of leakage current is limited. A modified cascaded H5 topology with inductors and capacitors on the AC side was proposed to achieve voltage clamping and division in (Guo and Jia, 2016), whose differential-mode leakage current was suppressed effectively. However, characteristics of output voltage were changed and circuit complexity was increased. Additional filtering inductors and capacitors were configured in each H-bridge in (Zhou and Li, 2014), which achieve better leakage current suppression effect. However, more power loss was caused by filters and the cost is higher. In (Selvamuthukumaran et al., 2015; Wang et al., 2018), a modified phase disposition pulse width modulation was proposed, which could keep the sum of the parasitic capacitor voltages constant and suppress the leakage current of the single-phase CHB inverter effectively. However, the modified modulation was only designed for the single-phase PV inverter with two H-bridges, making it difficult to extend to inverters with more submodules directly.

In recent years, model predictive control (MPC) has been widely used in the field of power electronic equipment control for intuitive control structure and ability of handling multiple control objectives simultaneously (Li et al., 2021). MPC predicts the future values of inverter for the next sampling cycle based on the discrete-time mathematic model. The optimal switching state of inverter is determined through a cost function, which is constructed of different forms of multivariable errors (Ni et al., 2022). The cost function represents the comprehensive control performance of inverter. The control and modulation of inverter are integrated into the cost function by MPC, which provide a powerful alternative to conventional proportional-integral (PI) and proportional-integral resonant (PIR) controllers. A control plane presented by the switching function coordinate was introduced in (He et al., 2023), in which only a subregion was selected to achieve control for reducing the execution time. However, it is only suitable for scenarios that do not require fast dynamic response. The MPC method is combined with the nonlinear sliding mode control in (He et al., 2022), so that fast dynamics can be achieved and control accuracy can be improved. A dual-layer MPC method for the CHB converter was proposed in (Xiao et al., 2023), in which fast output current control is achieved by optimal vector selection and dwell time calculation and the zero-sequence voltage candidate with the minimum predicted cluster voltages was injected to improved balancing speed.

In this article, a high-performance model predictive control is proposed to achieve the four control objectives simultaneously for the CHB-based PV inverter, in which existing overmodulation problem in the traditional control methods can also be avoided. Firstly, the grid-connected current of the PV inverter should be controlled precisely to maintain the power factor at 1. Secondly, the

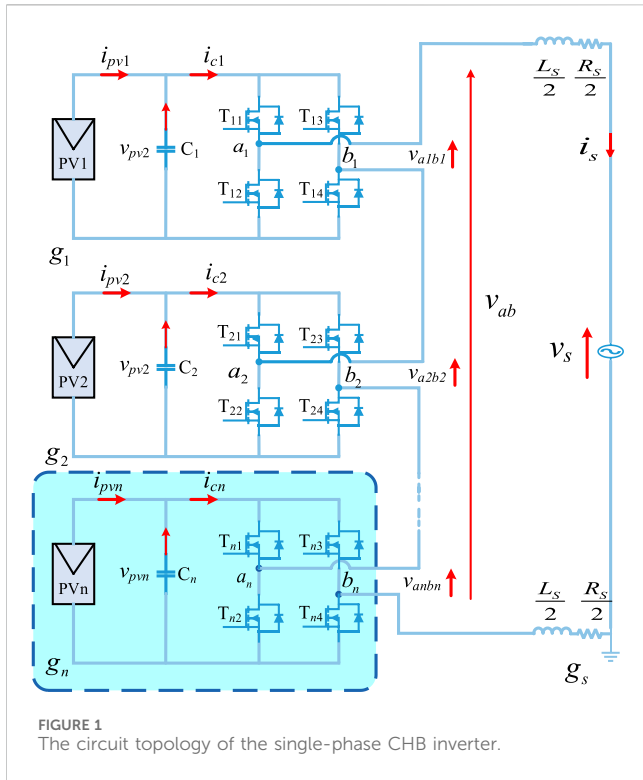


FIGURE 1 The circuit topology of the single-phase CHB inverter.

DC voltage of each H-bridge should be controlled independently so that the PV strings in different submodules can track their respective maximum power points. Besides, the high-frequency components of the CMV should be reduced to suppress the leakage current. Finally, the average switch frequency of the switching devices should be reduced for reducing the power loss.

The rest of this article is organized as follows. Section 2 introduces the topology and the operational principle of the CHB-based PV inverter. Section 3 describes the cost function, in which the predicted and reference values of controlled variables are also derived. Section 4 reports the experimental results. Finally, section 5 concludes the article.

## 2 System description

The single-phase CHB inverter is composed by two inductors and  $n$  H-bridge submodules connected in series, whose circuit topology is shown in Figure 1.  $L_s$  is the inductance of filtering inductors, and  $R_s$  is the parasitic resistance. Each H-bridge consists of the PV strings, a DC capacitor and four MOSFETs with anti-parallel diodes.

The number of PV strings and PV modules in each PV string depends on the rated power of the system, the voltage of grid, the rated voltage of PV modules and the number of H-bridges. Increasing number of the H-bridges will reduce the quantity of PV modules in each submodule and increase the levels of output voltage.

In order to avoid direct connection of H-bridge arm, the upper and lower MOSFETs are taken as opposite. For ease of analysis,  $S_{i1}$  and  $S_{i2}$  respectively denote the switching functions of the left and right arms of the  $i$ th H-bridge, which can be defined by (1).

$$S_{i1} = \begin{cases} 1 & T_{i1} = 1, T_{i2} = 0 \\ 0 & T_{i1} = 0, T_{i2} = 1 \end{cases}, S_{i2} = \begin{cases} 1 & T_{i3} = 1, T_{i4} = 0 \\ 0 & T_{i3} = 0, T_{i4} = 1 \end{cases} \quad (1)$$

The four switching states of H-bridge can output three different levels of voltage ( $+v_{pvi}$ , 0 and  $-v_{pvi}$ ). Therefore, the total number of switching states can reach  $4^n$  when  $n$  H-bridges are cascaded together,  $2n+1$  levels of voltage can be output. Due to the increase of levels for output voltage, the waveform quality is also improved, and the grid-connection can also be achieved by inductor with smaller value.

Analyzing the circuit topology of the single-phase CHB inverter by the Kirchhoff's voltage law (KVL), the continuous state-space mathematical model is given as:

$$\begin{cases} L_s \frac{di_s}{dt} = v_s - v_{ab} - R_s i_s \\ C_i \frac{dv_{pvi}}{dt} = i_{ci} - i_{pvi} \end{cases} \quad (2)$$

where  $v_s$  and  $i_s$  are the grid voltage and current, respectively.  $v_{ab}$  denotes the output voltage of the CHB inverter.  $v_{pvi}$  and  $i_{pvi}$  represent the DC capacitor voltage and output current of the PV strings,  $i_{ci}$  is the output current of submodule, where the subscript  $i$  indicates the order of the cascaded H-bridge.

The relationship between the voltage of capacitor  $v_{pvi}$  on the DC side and the output voltage  $v_{aibi}$  of H-bridge can be described by (3).

$$v_{aibi} = (S_{i1} - S_{i2})v_{pvi} \quad (3)$$

Eq. 2 model the dynamic behavior of the CHB inverter in the continuous state-space domain, in which the grid-current dynamics are controlled by the total generated output voltage of the inverter. On the other hand, equation of the capacitor voltage can be applied to balance the individual capacitor voltage of each H-bridge.

## 3 Proposed MPC with the CMV suppression

### 3.1 Design of the cost function

The MPC algorithm utilized the discrete character of the switching states in inverter to derive the discrete dynamic model of the system, which can relate the control objectives with the switching signals. Then, all switching state combinations are evaluated by using the cost function in the current control cycle. Finally, the switching state minimizing the cost function is selected to drive the MOSFETs. The essence of MPC algorithm is to predict the behavior of the system for each possible output voltage vector.

There are four control objectives should be achieved in the CHB-based PV inverter:

- (1) Tracking grid-connected current.
- (2) Balancing voltage of DC capacitors in different submodules.
- (3) Suppressing the high-frequency components of the CMV.
- (4) Reducing the switching frequency.

Figure 2 shows detailed control structure of the proposed MPC, in which the cost function should include variable quadratic errors

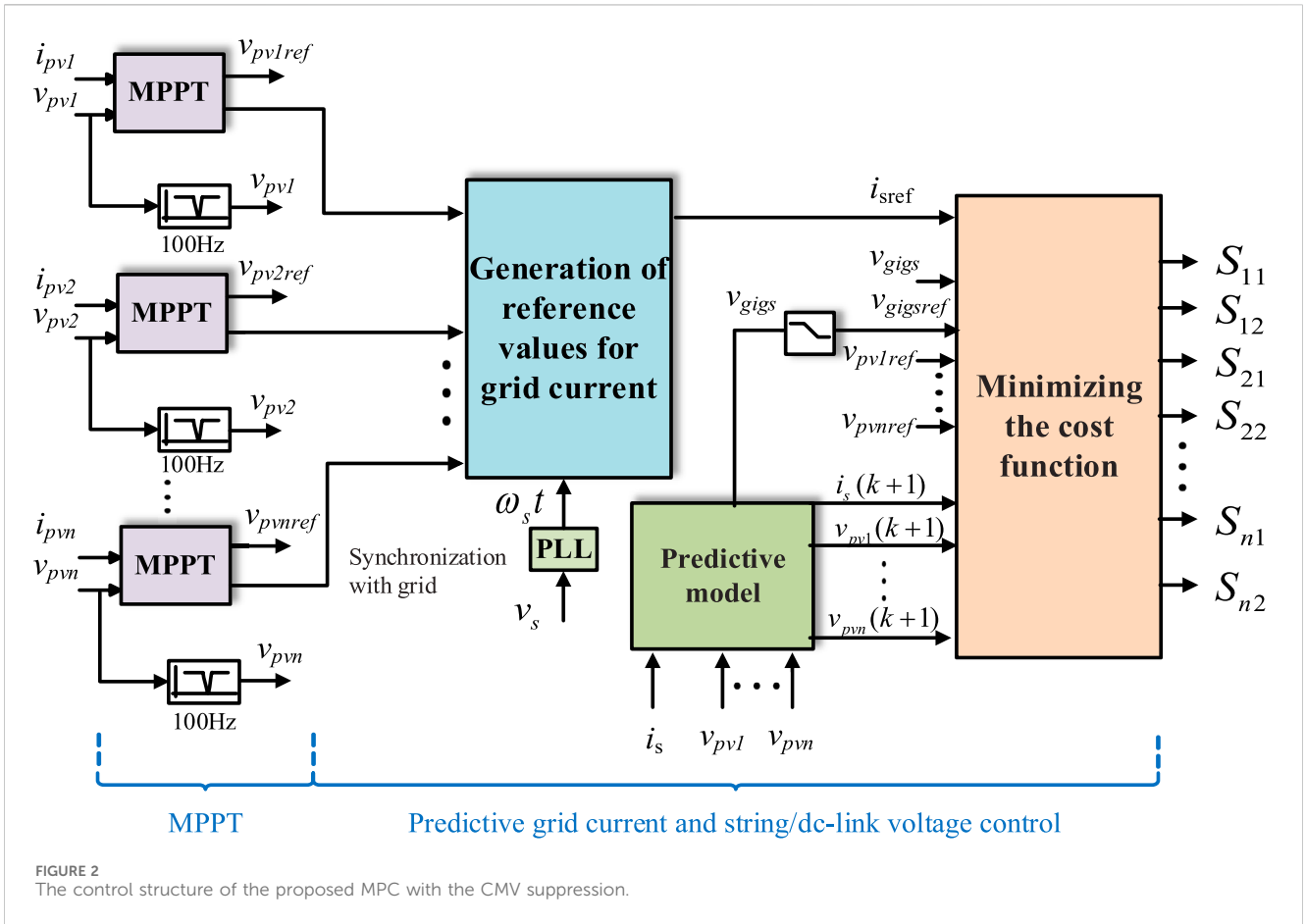


FIGURE 2 The control structure of the proposed MPC with the CMV suppression.

between the predicted and reference values. In this way, the specific expression of the cost function can be represented by (4).

$$\begin{aligned}
 g(k+1) = & \lambda_i [i_{sref}(k+1) - i_s(k+1)]^2 \\
 & + \lambda_v \sum_{i=1}^n [v_{pviref}(k+1) - v_{pvi}(k+1)]^2 \\
 & + \lambda_g \sum_{i=1}^n [v_{gigsref}(k+1) - v_{gigs}(k+1)]^2 + \lambda_c n_c(k+1)
 \end{aligned} \tag{4}$$

$k$  denotes the current control cycle, while  $k+1$  denotes the next control cycle.  $\lambda$  is the weighting factor, which is used for trading off among four objectives; its subscript  $i$  indicates the grid-connected current tracking,  $v$  indicates the capacitor voltages balancing,  $g$  indicates the suppression of the CMV, and  $c$  indicates the reduction of switching frequency.

The first part of the cost function is related to the current tracking performance;  $i_{sref}(k+1)$  and  $i_s(k+1)$  are the reference and predicted values of the grid-connected current. The second part represents DC voltage balance;  $v_{pviref}(k+1)$  and  $v_{pvi}(k+1)$  are the reference and predicted values of the capacitor voltage. The third part is involved with the CMV suppression.  $v_{gigsref}(k+1)$  and  $v_{gigs}(k+1)$  are the reference and predicted values of the CMV. The last part reflects the switching frequency reduction.  $n_c(k+1)$  is the total number of switching actions in the next control cycle.

### 3.2 Calculation of predicted value

From the forward Euler method, the continuous state-space model can be expressed in the discrete-time domain. The prediction of the variable vectors can be obtained in the discrete mathematical model.

#### 3.2.1 Prediction of the grid-connected current

Based on the load current model in (2), the grid-connected current in the next control cycle,  $i_s(k+1)$ , can be predicted as (5).

$$i_s(k+1) = \left(1 - T_s \frac{R_s}{L_s}\right) i_s(k) + \frac{T_s}{L_s} [v_{ab}(k) - v_s(k)] \tag{5}$$

$T_s$  is the control cycle of MPC.  $v_s(k)$  and  $i_s(k)$  should be obtained by measuring and sampling.

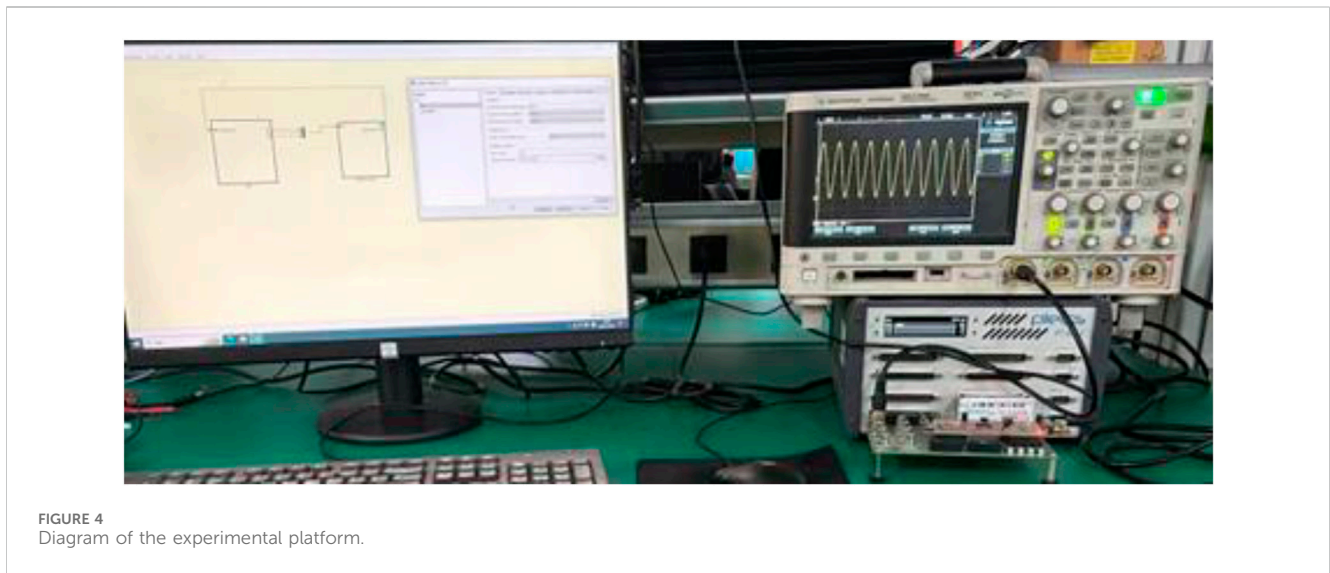
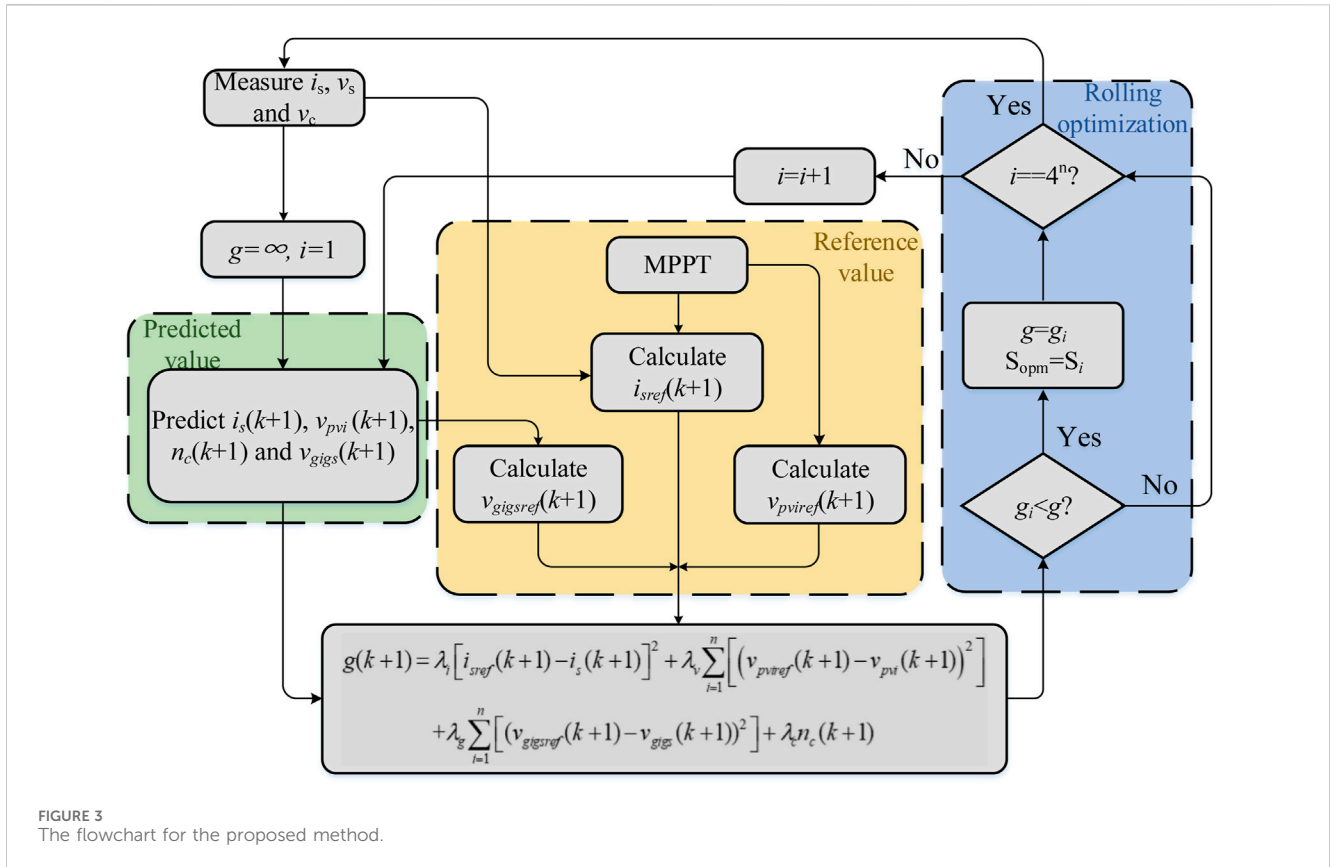
According to Equation 3,  $v_{ab}(k)$  can be calculated by (6).

$$\begin{aligned}
 v_{ab}(k) = & v_{a1b1}(k) + v_{a2b2}(k) + \dots + v_{anbn}(k) \\
 = & \sum_{i=1}^n [S_{i1}(k) - S_{i2}(k)] v_{pvi}(k)
 \end{aligned} \tag{6}$$

#### 3.2.2 Prediction of DC capacitor voltage

The prediction of DC capacitor voltage  $v_{pvi}(k+1)$  of the  $i$ th H-bridge can be calculated as (7).

$$v_{pvi}(k+1) = v_{pvi}(k) + T_s \left[ \frac{i_{pvi}(k) - i_{ci}(k)}{C} \right] \tag{7}$$



$i_{ci}(k)$  can be calculated by (8).

$$i_{ci}(k) = (S_{i1}(k) - S_{i2}(k))i_s(k); \quad i = 1, \dots, n \quad (8)$$

### 3.2.3 Prediction of the switching action times

The total number of switching actions  $n_c(k+1)$  can be obtained by comparing the differences of switching state for the CHB inverter between the current and next control cycles, as shown in (9). It can

be inferred that regardless of whether the MOSFET is turned on or off, the switching action times will be calculated.

$$n_c(k+1) = 2 \sum_{i=1}^n |S_{i1}(k+1) - S_{i1}(k)| + |S_{i2}(k+1) - S_{i2}(k)| \quad (9)$$

### 3.2.4 Prediction of the CMV

There is a direct electrical connection between PV modules and the power grid without transformer isolation, which will occur leakage

TABLE 1 Inverter parameters.

Parameters	Numerical value
Number of H-bridge submodules	3
Filter inductance/mH	5
Grid voltage amplitude/V	200*1.414
Control cycle/us	50
DC-link capacitor/uF	8

TABLE 2 PV module parameters.

Parameters	Numerical value
Maximum power/W	580.01
Open-circuit voltage/V	51.41
Short-circuit current/A	14.22
Maximum power point voltage/V	43.22
Maximum power point current/A	13.42

current on the parasitic capacitor between PV modules and the ground. The leakage current will reduce system reliability, threaten personal safety, and generate electromagnetic interference. To reduce the leakage current and avoid using isolation transformer,  $v_{gigs}$  should be maintained lower, which is the voltage between the negative input terminal ( $g_i$ ) of the  $i$ th submodule and the grounding terminal ( $g_s$ ). It can be calculated as (10).

$$v_{gigs}(k+1) = -S_{i2}(k+1) \cdot v_{pvi}(k+1) + \sum_{j=i+1}^n v_{ajbj}(k+1) + \frac{1}{2} [v_s(k+1) - v_{ab}(k+1)] \quad (10)$$

### 3.3 Calculation of reference value

#### 3.3.1 Calculation of grid-connected current reference value

The reference value  $i_{sref}(k+1)$  of grid-connected current can be obtained based on the principle of power balance on the AC and DC sides. The DC power is determined by PV modules and can be obtained through the MPPT algorithm in the  $i$ th submodule, which is denoted by  $P_{pviref}$ . Therefore, if all PV modules in submodules operate at maximum power points respectively, the reference value of the grid current in the next control cycle should be calculated as (11).

$$i_{sref}(k+1) = \frac{P_{pv1ref}(k+1) + \dots + P_{pvnref}(k+1)}{[v_{s,rms}(k)]^2} v_s(k) \quad (11)$$

$v_{s,rms}(k)$  is the effective value of the grid voltage,  $v_s(k)$  is the instantaneous value of the grid voltage.

#### 3.3.2 Calculation of DC capacitor voltage reference value

The reference value  $v_{pviref}(k+1)$  of DC capacitor voltage is the operating voltage of the PV modules at maximum power point, which is obtained by the MPPT.

Specifically, the operating voltage of the PV modules at maximum power point can be obtained by the MPPT in the first H-bridge, which is also the reference value of the DC capacitor voltage, and can be denoted by  $v_{pv1ref}(k+1)$ . According to the same method, the reference value of DC capacitor voltage for the second, the third, ..., the  $n$ th H-bridge submodule can be obtained and denoted by  $v_{pv2ref}(k+1)$ ,  $v_{pv3ref}(k+1)$ , ...,  $v_{pvnref}(k+1)$ , respectively.

#### 3.3.3 Calculation of the CMV reference value

The CMV contains a large number of harmonic components, which will generate displacement current. Therefore, a digital first-order low-pass filter is designed to filter out the high-frequency harmonic components. Based on the designed filter, the reference value  $v_{gigsref}(k+1)$  of the CMV can be obtained, which is substituted into the cost function  $g$  together with  $v_{gigs}(k+1)$  to suppress the CMV.  $v_{gigsref}(k+1)$  can be calculated based on the predicted reference  $v_{gigs}(k+1)$  of CMV in the next control cycle and the filtered CMV  $v_{gigsref}(k+1)$  in the current control cycle, shown as:

$$v_{gigsref}(k+1) = \alpha v_{gigs}(k+1) + (1-\alpha)v_{gigsref}(k) \quad (12)$$

where  $\alpha = 2\pi f T_D / (1+2\pi f T_D)$ ;  $f$  is the cut-off frequency of the designed first-order low-pass filter; and  $T_D$  is the sampling period of the digital controller.

### 3.4 Controller design procedure

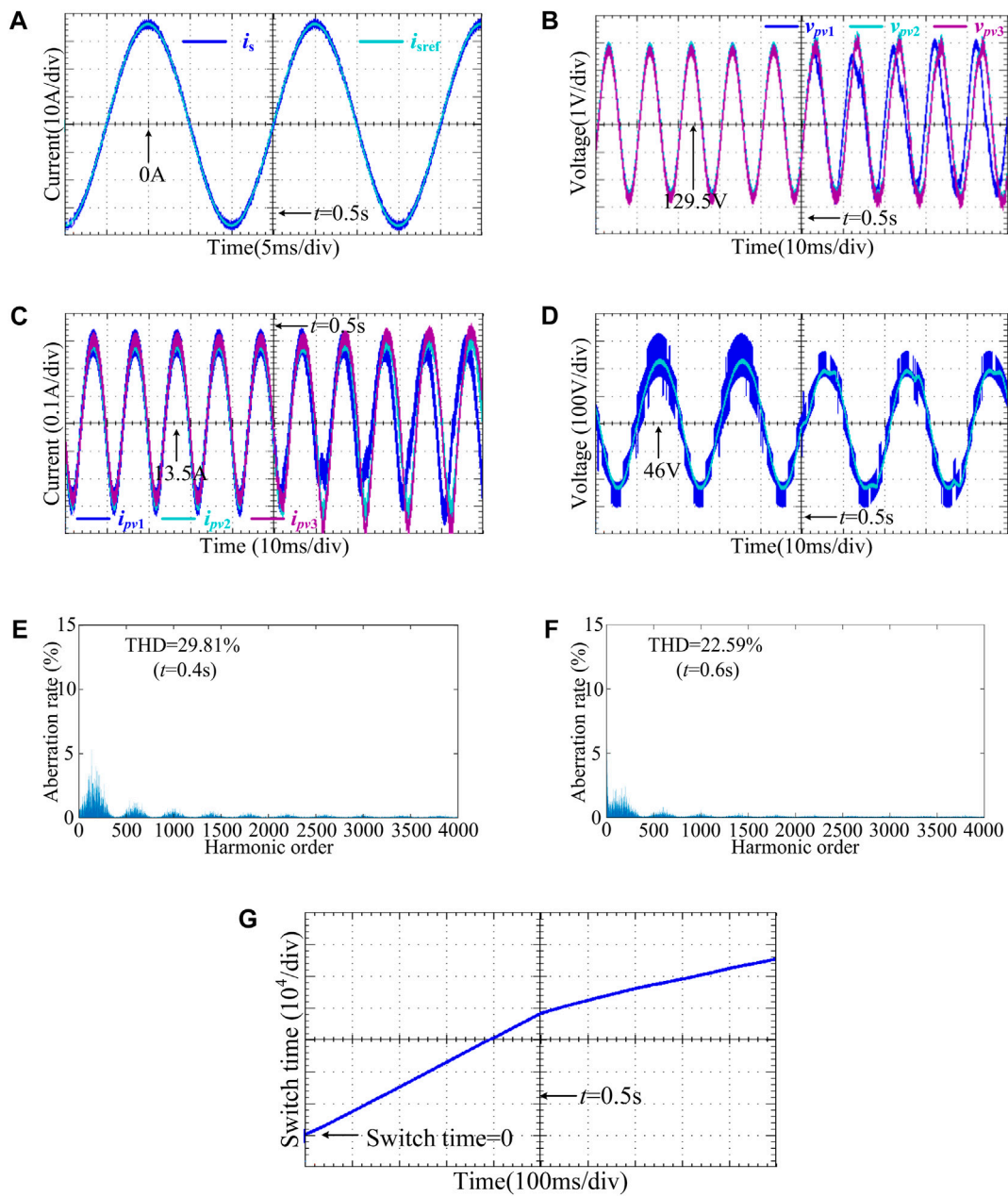
The flowchart of the proposed MPC is shown in Figure 3. The design procedure of the proposed method can be summarized as the following steps:

- (1) Measure the required circuit parameters of the designed method.
- (2) Define matrix  $S$  for all the possible switching states.
- (3) Initialize the controller state and set the initial value for the cost function  $g$ .
- (4) Calculate predicted values of variables using (5), 7, 9, and 10.
- (5) Obtain reference values using (11), 12.
- (6) Select the optimal switching state  $S_{opm}$  through rolling optimization using the cost function  $g$  in (4).

## 4 Experimental results

A semi physical experimental platform as shown in Figure 4 is constructed to verify the feasibility and effectiveness of the proposed MPC with high-frequency CMV suppression in this paper. The control algorithm is implemented in the TMS320F28069 digital controller, while the main circuit is structured by building a simulation model on the RT BOX platform.

Table 1 shows the parameters of the main circuit, which consists of three H-bridge submodules, each submodule is constituted of three PV modules connected in series on the DC side. The main parameters of each PV module are shown in Table 2. The maximum power point voltage of the PV module is 43.22 V, which also means



**FIGURE 5** Experimental results under power balance of three submodules (A) Waveforms of  $i_s$  and  $i_{sref}$ . (B) Waveforms of  $v_{pv1}$ ,  $v_{pv2}$ ,  $v_{pv3}$ . (C) Waveforms of  $i_{pv1}$ ,  $i_{pv2}$ ,  $i_{pv3}$ . (D) Waveforms of  $v_{g1gs}$  and  $v_{g1gsref}$ . (E) The spectrum of  $v_{g1gs}$  at  $t = 0.4$  s. (F) The spectrum of  $v_{g1gs}$  at  $t = 0.6$  s. (G) Waveform of  $n_c$ .

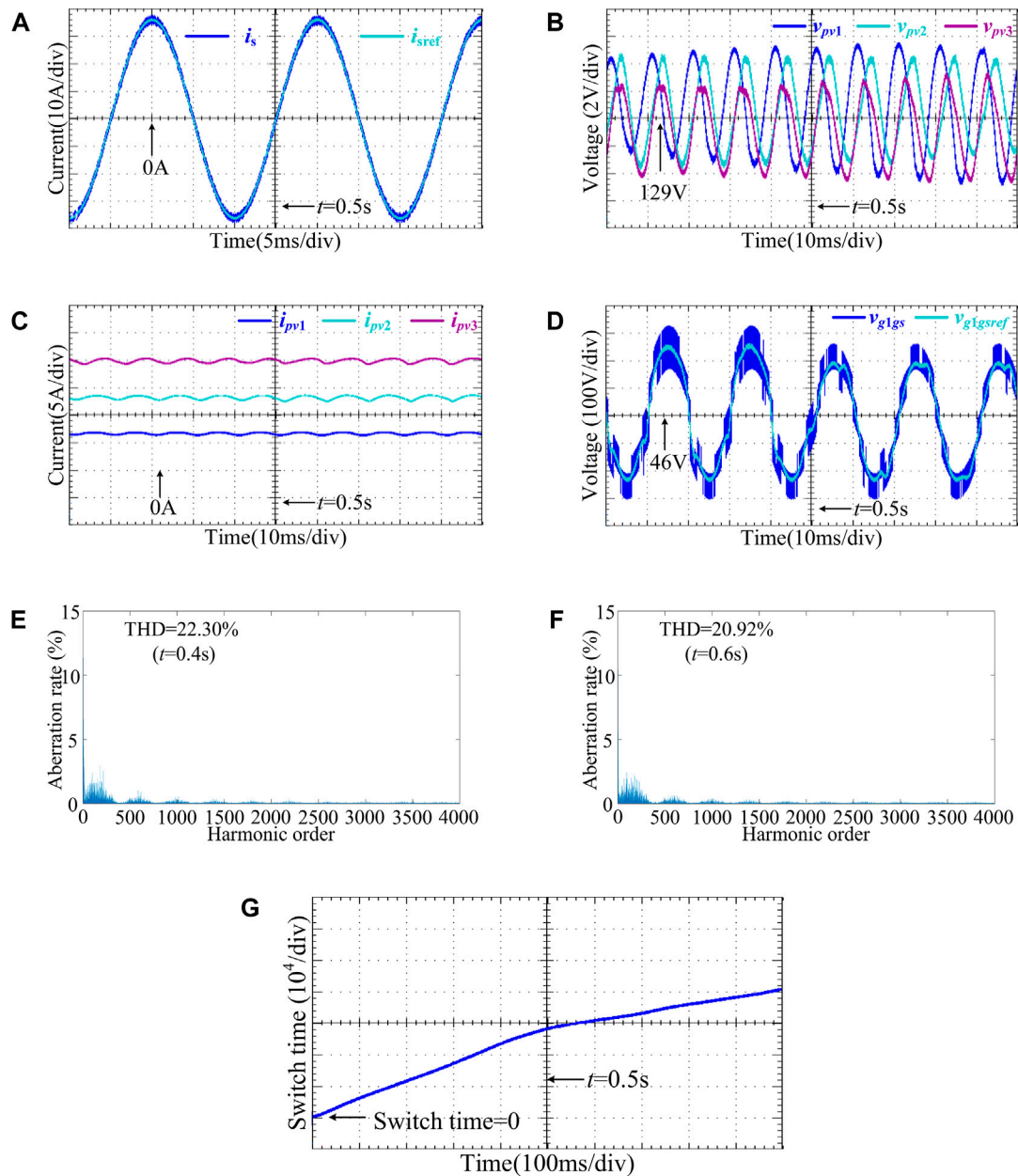
that the DC voltage of each H-bridge is 129.66 V at the maximum power point.

To validate the steady-state and dynamic performance of the proposed MPC to various grid-connected conditions on a seven-level CHB inverter, two groups of experiments are performed, whose sample time  $T_s$  is fixed at 50  $\mu$ s. Before  $t = 0.5$  s, the weighting factor  $\lambda_i$  is set to 5,  $\lambda_v$  is set to 10,  $\lambda_g$  and  $\lambda_c$  are set to 0. After  $t = 0.5$  s,  $\lambda_g$  and  $\lambda_c$  are set to  $1e^{-4}$  and 0.1, respectively. Therefore, the high-frequency components suppression of the CMV and switching frequency reduction are not enabled before 0.5 s. The experimental results are shown in Figures 5, 6 at the effective value for grid voltage of 220 v.

### 4.1 Power balance condition

The experimental results in Figure 5 are obtained under power balance condition of three submodules, in which the light intensity of the PV modules is all set to 1000 W/m<sup>2</sup>, and their ambient temperatures are set to 25°C. The rated power of PV strings on the DC side for each submodule are 1740 W. According to Equation 11, the effective value of the grid-connected current reference value is 142.43 A.

Figure 5A shows the waveforms of  $i_s$  and  $i_{sref}$  in which the grid-connected output current is very smooth. Even after adding CMV suppression and switching frequency reduction at 0.5s,



**FIGURE 6** Experimental results under power imbalance of three submodules (A) Waveforms of  $i_s$  and  $i_{sref}$ . (B) Waveforms of  $v_{pv1}$ ,  $v_{pv2}$ ,  $v_{pv3}$ . (C) Waveforms of  $i_{pv1}$ ,  $i_{pv2}$ ,  $i_{pv3}$ . (D) Waveforms of  $v_{g1gs}$  and  $v_{g1gsref}$ . (E) The spectrum of  $v_{g1gs}$  at  $t = 0.4 s$ . (F) The spectrum of  $v_{g1gs}$  at  $t = 0.6 s$ . (G) Waveform of  $n_c$ .

the grid-connected current still maintains high-precision tracking for reference value without significant current fluctuations.

Figures 5B,C shows the waveforms of  $v_{pvi}$  and  $i_{pvi}$ , respectively. The DC voltages and currents of the three submodules are almost consistent, the voltages on the DC side reach the operating voltage of 129.66 V at the maximum power point of the PV strings. The submodules can output 1640.82 W at the maximum power point. After 0.5 s,  $v_{pvi}$  and  $i_{pvi}$  occur a fluctuation of around 1V–3 V and 0.5 A, respectively, resulting in a decrease in consistency. Then, they tend to stabilize again after 30 ms, and overall balance of the system is still maintained. The PV strings are still operating near the

maximum power point, outputting 1635.46 W. The efficiency of system is 94.3%.

As is shown in Figure 5D for  $v_{g1gs}$  and  $v_{g1gsref}$  the peak value of  $v_{g1gs}$  is larger initially, about 1700v; in addition, the high-frequency components of  $v_{g1gs}$  account for a large proportion, with a THD of 29.81% at 0.4s. After suppressing CMV at 0.5s, the high-frequency components of  $v_{g1gs}$  significantly decreased, in which THD has already dropped to 22.59% at 0.6s and the peak value has dropped at 1300v approximately.

Figure 5E expresses the waveform of  $n_c$ , which indicates that the average switching frequency of the CHB inverter. Before 0.5s, the average switching times of the CHB inverter is  $1.9 \times 10^5$ , after



TABLE 3 Comparison between the proposed method and various voltage balancing strategies.

Approaches	Operating range	Rated power	Power factor	THD
Improved MPPT	Wide	Decrease	1	Low
Hybrid modulation technology	Narrow	Unchanged	1	Low
Reactive power compensation	Wide	Unchanged	<1	Low
Harmonic compensation	Narrow	Unchanged	1	High
Proposed MPC algorithm	Wide	Unchanged	1	Low

TABLE 4 Comparison between the proposed method and various leakage current suppressing strategies.

Approaches	Operating range	Circuit complexity	Suppression effect
Improved circuit topology	Wide	High	Obvious
Add filters	Require for switching frequency	Low	Filtering order is single
Improve modulation strategies	Require for submodules number	Low	Obvious
Proposed MPC algorithm	Wide	Low	Obvious

reducing switching frequency, the number of average switching times is decreased by 52.63%, only need to be activated  $0.9 \times 10^5/s$ . The unnecessary multiple voltage level jumps are reduced to a large extent.

Besides, we conducted efficiency analysis on submodules with light intensities of 300 W/m<sup>2</sup>, 600 W/m<sup>2</sup>, 900 W/m<sup>2</sup>, 1200 W/m<sup>2</sup> and 1500 W/m<sup>2</sup> separately, in which the output power of the system is all around the maximum power point, with an average efficiency of 94.53%.

## 4.2 Power imbalance condition

The experimental results in Figure 6 are obtained under power imbalance condition of three submodules at 25°C, in which the light intensity of the PV modules is set to 500W/m<sup>2</sup>, 1000 W/m<sup>2</sup> and 1500 W/m<sup>2</sup>. The main experimental condition is the same as the first group experiment. The rated power of PV strings on the DC side for each submodule are 872.7 W, 1740 W and 2572 W, respectively. The effective value of the grid-connected current reference value is 141.58 A.

Figure 6A shows the waveforms of  $i_s$  and  $i_{sref}$  under power imbalance condition, in which the grid-connected current always maintains high-precision tracking for reference value without significant current fluctuations around 0.5s.

Figures 6B,C shows the waveforms of  $v_{pvi}$  and  $i_{pvi}$  under power imbalance condition, respectively. The DC voltages and currents of the three submodules are almost different, reaching their operating voltage at maximum power points: 128.05 V, 129.66 V, and 129.92 V. The submodules output the maximum power. After 0.5 s, the distribution of  $v_{pvi}$  and  $i_{pvi}$  are almost identical to 0.5s ago, without falling or rising sharply. This means that the addition of new control objectives makes no difference to the original voltage balance of the system, and the PV strings of each submodule can still operate near respective maximum power point under power imbalance condition.

As is shown in Figure 6D for  $v_{g1gs}$  and  $v_{g1gsref}$  under power imbalance condition, the peak value of  $v_{g1gs}$  is around 1700v; in

addition, the high-frequency components of  $v_{g1gs}$  account for a large proportion, with a THD of 22.30% at 0.4s. After suppressing CMV, the THD of  $v_{g1gs}$  has already dropped to 20.92% at 0.6s and the peak value has dropped at 1300v approximately.

Figure 6E expresses the waveform of  $n_c$  under power imbalance condition. Before 0.5s, the average switching times of the CHB inverter is  $1.9 \times 10^5/s$ , after reducing switching frequency, the number of average switching times has been decreased by 63.16%, need to be activated  $0.7 \times 10^5/s$ .

It can be concluded that, under the imbalanced power condition, the proposed method maintains high precision grid-connected current tracking control, suppresses the high-frequency components of the CMV effectively, and reduces the average switching frequency of the CHB inverter significantly. At the same time, independent control of the DC capacitor voltages is achieved for each submodule. Therefore, the PV modules in different submodules can respectively operate at their own maximum power points, which improves efficiency of the PV system.

## 4.3 Comparison with traditional methods

The experimental results show that the proposed algorithm is applicable to various grid-connected operating condition, which proves the feasibility and effectiveness of the proposed algorithm. Therefore, the comparisons between the proposed method and various strategies are shown in Tables 3 and 4 to better demonstrate the advantages of the proposed method.

Compared with existing methods, all control objectives of the proposed method are achieved through predictive models and cost function, without need of linear model for the system. Based on this, four control objectives previously mentioned are achieved. In addition, the reference values of grid-connected current and capacitor voltages are calculated according to the MPPT algorithm, which further improves the power generation efficiency of the system with a higher accuracy.

## 5 Conclusion

In this article, the proposed algorithm was adopted to select the global optimal modulation function of the CHB inverter in the current predictive control cycle. Four control objectives are simultaneously achieved based on the cost function of proposed MPC. The performance of the proposed method is verified on a controller hardware-in-the-loop experimental platform. The experimental results have shown that the proposed MPC can track the grid-connected current accurately, the PV modules in different submodules can also independently operate at their own maximum power points. Meanwhile, the high-frequency components of the CMV are significantly suppressed, and a lower average switching frequency is also achieved. However, if the proposed method is extended to CHB-based PV inverter containing numerous submodules, the required computational complexity will be a challenge for general digital controllers. Future research should be focused on reducing the computational complexity to improve the availability of the proposed algorithm, and we will also try to apply this method to other multi-level cascaded circuit topologies.

## Data availability statement

The raw data supporting the conclusion of this article will be made available by the authors, without undue reservation.

## Author contributions

XW: Conceptualization, Investigation, Writing—original draft, Methodology. WT: Data curation, Formal Analysis, Software,

Writing—review and editing. XF: Formal Analysis, Project administration, Writing—review and editing.

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## Conflict of interest

Author XF was employed by State Nuclear Power Planning Design and Research Institute CO., Ltd.

The remaining authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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