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# [Characteristics of a novel fluidic](https://www.frontiersin.org/articles/10.3389/fenrg.2023.1236087/full) [oscillator with movable feedback](https://www.frontiersin.org/articles/10.3389/fenrg.2023.1236087/full) [channels and resonators](https://www.frontiersin.org/articles/10.3389/fenrg.2023.1236087/full)

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In this study, a novel fluidic oscillator suitable for use as a key component of a flow control device is proposed and investigated through numerical simulations. The new layout adds resonators to a typical fluidic oscillator with dual feedback channels, and the length of the feedback loop is designed to be adjustable. This fluidic oscillator with movable feedback channels and resonators can generate a jet with an adjustable frequency, and it has smaller total pressure loss than the baseline model. Numerical results show that the movement of the feedback channels regulates the degree of coupling between the feedback channels and resonators to generate different orders of jet frequencies. This self-excited fluidic oscillator with adjustable jet frequency is more adaptive than typical designs when dealing with complex flow separation conditions, and it will be more stable because the frequency adjustment requires neither high-frequency movable mechanisms nor external energy input. Moreover, the frequency switching phenomenon is observed in special cases, which may help improve the efficiency of the compressor blades with a drastically changed dominant frequency under off-design conditions or with multiple dominant frequencies, such as tip leakage flow and shock–boundary layer interaction.

#### KEYWORDS

fluidic oscillator, feedback channel, resonator, unsteady flow control, numerical simulation

# 1 Introduction

The efficiency and stability of compressors at high loads directly affect the performance of aeroengines. When blade loads are increased to levels far above the current aerodynamic design level, flow separation usually occurs due to high inverse pressure gradients or shock–boundary layer interaction, causing a dramatic decrease in fluid mechanical efficiency and even engine surge. Through flow control techniques, flow separation can be reduced or even eliminated, thereby improving the pressure ratio, efficiency, and stability margin of compressors considerably [\(Liu et al., 2019;](#page-14-0) [Qin et al., 2020;](#page-15-0) [Lu et al., 2022\)](#page-15-1).

Flow control mainly includes steady and unsteady flow control. In recent decades, researchers have shown great interest in unsteady flow control techniques that utilize flow instabilities.The main difference between steady and unsteady flow control techniques lies in whether or not the flow control excitation is time-dependent.The advantage of unsteady flow control over steady flow control is that it can achieve the same control effect with an energy saving of one to two orders of magnitude [\(Greenblatt and Wygnanski, 2000\)](#page-14-1). Therefore, unsteady flow control has elicited attention from researchers and has become a focus of flow control research.

Unsteady flow control mainly includes acoustic excitation [\(Lepicovsky et al., 1986;](#page-14-2) [Nishioka et al., 1987;](#page-15-2) [Açıkel and Genç,](#page-14-3) [2016\)](#page-14-3), synthetic jets [\(Glezer and Amitay, 2002\)](#page-14-4) [\(Cao et al., 2020\)](#page-14-5), unsteady blowing and suction [\(Kim et al., 2017\)](#page-14-6), wall oscillation [\(Choi et al., 2002\)](#page-14-7), and traveling wave wall control [\(Wu et al., 2003\)](#page-15-3) [\(Lu et al., 2019\)](#page-14-8). Belonging to unsteady blowing, fluidic oscillators are devices that can create a sweeping jet with a fixed frequency through a stable mass flow input. Oscillation in fluidic oscillators is produced by the Coanda effect, which attaches the fluid stream alternatively to one of the adjacent walls in the mixing chamber. The produced oscillation is self-induced and self-sustained [\(Tomac](#page-15-4) [and Sundström, 2019\)](#page-15-4). If the inlet and outlet of a fluidic oscillator are connected to a high-pressure and a low-pressure air source, respectively, the fluidic oscillator can utilize the flow instability to enable the outlet to generate a periodic sweeping jet, which can be used as the unsteady excitation required for unsteady flow control. As an unsteady flow control method, self-excited fluidic oscillators have a simple, reliable, low-maintenance geometry and can generate a self-sustaining and oscillating periodic jet without the use of movable parts. Thus, they have good application prospects. Their potential has been explored in many areas, such as fluid mechanics and aeronautics. Therefore, the demand for fluidic oscillators in engineering applications has increased considerably.

Fluidic oscillators have the potential to function as flow control devices by producing oscillating velocity fields. However, their utilization as unsteady flow control devices has received wide attention from researchers since 2010s. Many typical fluidic oscillators are very efficient in generating oscillating velocity fields and their effects and mechanism have been thoroughly studied in recent years due to their robustness and potential to meet most of the application requirements. Cerretelli and Kirtley [\(Cerretelli](#page-14-9) [and Kirtley, 2009\)](#page-14-9) experimentally investigated the control effect of a fluidic oscillator on flow separation in a diffuser and found that the fluidic oscillator can save 60% jet momentum compared with steady flow control when the flow field is fully reattached. Koklu [\(Koklu, 2018\)](#page-14-10) compared the jet generated by a fluidic oscillator with those generated by several common flow control methods, such as steady jet, vortex-generating jet, and vortex generator through experiments and reported that the control performance of the fluidic oscillator is better than that of the steady jet and vortex-generating jet in the separation flow of the ramp structure. Wang et al. [\(Wang et al., 2019\)](#page-15-5) proposed the concepts of highpressure compressed wave and low-pressure expansion wave and used pressure wave reflection theory to explain oscillation behavior. Ostermann et al. [\(Ostermann et al., 2017\)](#page-15-6) [\(Ostermann et al., 2019\)](#page-15-7) addressed the flow control mechanism of fluidic oscillators and found that because the sweeping jet is on a plane perpendicular to the external crossflow, the effect of the jet is similar to that of the streamwise vortical structures generated by a vortex generator. Tomac and de Luzan [\(Tomac and de Luzan, 2020\)](#page-15-8) experimentally and numerically investigated and characterized a synchronized fluidic oscillator, which is especially helpful for solving flow control problems exhibiting two separation points, such as flowover cylinders or surfaces exposed to differential pressure (i.e., wingtips). Some researchers have also focused on self-excited fluidic oscillators for engineering applications and have conducted full-scale experiments and numerical simulations. Cerretelli et al. [\(Cerretelli et al., 2010\)](#page-14-11) used a built-in fluidic oscillator to control a DU96 airfoil representing a typical wind turbine blade and discovered that appropriate control parameters can increase the airfoil lift by up to 60%. Shmilovich et al. [\(Shmilovich et al., 2018\)](#page-15-9) placed an array of multiple fluidic oscillators on the vertical tail of an aircraft and verified the effectiveness of this flow control approach through numerical simulations and experiments at the whole-aircraft level of the B757 demonstrator.

Unsteady flow control devices require a broad range of excitation frequencies for effective operation in some cases. For example, in a compressor at an off-design point, the dominant frequency of the separated flow differs from that at the design point. This condition means that the optimum flow control frequency also changes, so the frequency of unsteady flow control devices, such as fluidic oscillators, needs to be adjusted under different operating conditions. Flows with tip leakage, corner separation, or shock–boundary layer interactions also have two different dominant frequencies. Under different operating conditions, modes with different dominant frequencies need to be controlled. Thus, researchers have attempted to establish methods to change the frequency of flow control devices. As unsteady fluid control devices, fluidic oscillators typically adjust the sweeping frequency of the output jet through its mass flow rate. However, other existing methods can be used to adjust the jet frequency. For example, Tomac and Sundström [\(Tomac and Sundström, 2019\)](#page-15-4) added two control jets in the fluidic oscillator mixing chamber. This approach can change the jet frequency of the oscillator through the K-H instability between the two control jets and the mainstream to generate ultra-high frequency jets. Culley [\(Culley, 2006\)](#page-14-12) added a solenoid pressure valve to the inlet of the oscillator to regulate the pressure in the control channel and thus control the frequency of the jets generated by the devices. The highest frequency measured from this experimental device is 312 Hz due to the limitations in the switching speed of the solenoid valve. This frequency may still be relevant for some applications, but this device cannot handle flow control situations that require frequencies higher than 312 Hz. In addition, the constant external excitation and high-frequency motion of the components increase the energy consumption and reduce mechanical reliability. Moreover, Gregory et al. [\(Gregory et al., 2009\)](#page-14-13) used a piezoelectric bender to control the frequency of a fluidic oscillator. Their design is similar to these with solenoid valves. Given that a bending tube is added, the frequency is affected by the characteristics of the moving parts when this method is adopted. In the frequency range of 0–250 Hz, oscillation frequency is independent of supply pressure. However, the efficiency of this approach decreases at frequencies exceeding the piezoelectric bender's resonance frequency (121 Hz). Analysis of the existing techniques for changing the frequency of fluidic oscillators indicates that changing the frequency by adding movable parts, electric devices, or additional accessories may raise new issues, such as reduced engineering reliability, increased maintenance costs, shortened service life, and reduced energy utilization efficiency.

Aside from fluidic oscillators that can adjust jet frequency, we consider a new configuration that avoids using external excitation, high-frequency movable parts, or electromagnetic actuators. At present, there are two typical types of wall-attachment fluidic oscillator designs: with feedback channels and with resonators [\(Gregory and Tomac, 2013\)](#page-14-14). For the fluidic oscillator with feedback channels, the frequency of the jet generated by the device is proportional to the flow rate through the oscillator [\(Ostermann et al., 2019\)](#page-15-7). Thus, jet frequency can be adjusted via the flow rate. However, generating ultra-high-frequency jets is difficult. For the fluidic oscillator consisting of a conjugate acoustic resonator [\(Tesař et al., 2013\)](#page-15-10), jet frequency is constant and independent of the flow rate through the fluidic oscillator. Ultra-high-frequency jets can be generated, but the jet frequency is difficult to adjust because it is determined by the geometry of resonators. Thus, we consider a new fluidic oscillator with movable feedback channels and resonators and attempt to combine the advantages of both, namely, the ability to adjust the frequency by flow rates while generating high frequencies and the ability to modulate the Strouhal number of the oscillator by moving the feedback channels, thus changing the oscillator characteristics.

In this study, the characteristics of the fluidic oscillator with feedback channels and resonators are studied numerically. In [Section 2,](#page-2-0) the concept of the fluidic oscillator is introduced in terms of structural design ideas and principles. In [Section 3,](#page-3-0) the numerical method used in this study is presented together with the structural parameters, mesh generation, and solver settings. Simulation reliability is also verified through a comparison with existing experimental results. In [Section 4,](#page-4-0) we present the theoretical basis for the sweeping frequency in fluidic oscillators with only feedback channels and those with only resonators. In [Section 5,](#page-7-0) we analyze the numerical results to express our understanding of the unique characteristics of the new fluidic oscillator. With this study, we hope to improve the understanding and application of fluidic oscillators with adjustable frequencies.

## 2 Concept of a fluidic oscillator with movable feedback channels and resonators

We propose a new fluidic oscillator with adjustable jet frequencies and sweeping amplitudes. For easy distinction, we refer to the baseline model used for reference as the "prototype model" and to the new proposed oscillator as the "modified model". In terms of geometry, on the basis of the prototype fluidic oscillator shown in [Figure 1A](#page-2-1) (adopted from Ref. [\(Cerretelli et al., 2010\)](#page-14-11)), we add resonators at the beginning and end of each of the two feedback channels so that the fluidic oscillator has both feedback channels and resonators. We expect this design to combine the advantages of the two typical types of oscillators mentioned in the Introduction. The feedback channel is designed to move laterally within the stroke, thus allowing the adjustment of the oscillation characteristics to produce sweeping jets with different characteristics.

The specific structure of the fluidic oscillator with feedback channels and resonators is shown in [Figure 1B.](#page-2-1) It includes an inlet, a mixing chamber, and an outlet, which are sequentially located on the central axis of the device and constitute the main flow path. A feedback loop consisting of a feedback channel and a resonator is provided both on the left and right, respectively, of the central axis of the device. If the resonator is not considered, the main flow path in the mixing chamber will adhere to the left or right wall surface of the mixing chamber due to the Coanda effect. For example, if the main flow path is attached to the right wall of the mixing chamber, the jet will be attached to the left wall of the outlet and form a right feedback loop, and the flow along the right feedback loop will push the main flow path at the entrance of the mixing chamber to attach it to the left wall of the mixing chamber. Next, the jet will flow along the right wall of the outlet and form a left feedback loop. These two processes

<span id="page-2-1"></span><span id="page-2-0"></span>



<span id="page-3-1"></span>occur alternately, thus forming a certain frequency of the sweeping jet at the outlet. Moreover, if the feedback channel is not considered, a standing wave with a fixed frequency will be generated at the entrance of the mixing chamber due to the presence of resonators on both sides of the entrance of the mixing chamber, making the jet frequency consistent with this standing wave frequency [\(Field and](#page-14-15) [Fricke, 1998\)](#page-14-15).

Given that resonators and feedback channels exist simultaneously, the characteristics of the oscillator in this study are formed by the joint action and mutual coupling of resonators and feedback channels. By changing the feedback loop length through the movement of the feedback channel, the jet characteristics are likely to be changed. And the jet sweeping angle and frequency can be adjusted through the different degrees of coupling between the feedback channels and resonators. This approach can effectively control the flow for different separation vortex frequencies and improve the adaptability of the device to the working conditions.

# 3 Numerical methods

In this study, the sweeping jet is generated by a fluidic oscillator with both feedback channels and resonators [\(Figure 2\)](#page-3-1). This oscillator is a modification of a prototype oscillator, which has been examined and characterized in various studies (e.g., [Ostermann et al., 2018\)](#page-15-11). The spatial oscillations of the jet are induced only by internal dynamics and geometry, so the generated jet is selfinduced and self-sustained. With reference to the modified fluidic oscillator, the width  $d$  of the outlet (i.e., throat) is 25 mm, the length of the resonator (denoted as  $L_R$ ) is 128 mm, and the outlet semi-spread angle is 50° [\(Table 1\)](#page-3-2). The compressibility effect can be ignored in this study because the highest Mach number at the throat is estimated to be 0.28 under the maximum mass flow rate supply.

<span id="page-3-2"></span>



<span id="page-3-0"></span>A computational fluid dynamics (CFD) approach is used to evaluate the characteristics of the fluidic oscillator in different modes, including the effect of the length of the feedback channels on the sweeping frequency of the fluidic oscillator and the total pressure loss of the oscillator. The simulations are implemented on a workstation that uses an octa-core Intel Core i7 9700 CPU. An unsteady flow case needs about 20 h to finish computation. The validity and feasibility of the numerical method are verified based on the prototype. The modified model includes the design of the feedback channel as a movable mechanism so that the total length of the feedback loop can be adjusted within a certain range, which may also result in a variation in the Strouhal number.

To simulate the sweeping jet generated by the fluidic oscillator with moveable feedback channels and resonators, a structured mesh is constructed using ANSYS ICEM. The mesh topology is shown

A

B



<span id="page-4-1"></span>

in [Figure 3,](#page-4-1) and 16 3D blocks are used. A grid-independence test is performed based on the prototype, and [Figure 4](#page-4-2) shows that the jet frequency and total pressure loss coefficient generated by the prototype are nearly invariant for grid numbers larger than 860,000. Therefore, using the grid number of about 1,000,000 can save computational resources while obtaining a sufficiently high computational accuracy. The grid of the feedback channel part is divided independently, and the moving mesh is used to generate meshes at different positions. Before the mesh is moved to the designed position, the translational speed is maintained at a low level to avoid unsteady effects.

The ideal air model is selected as the fluid model. The k-omega shear stress transport (k-ω SST) turbulence model is used in ANSYS Fluent to calculate the steady flow as the initial field, and unsteady numerical simulations are performed using large eddy simulation (LES). In LES, the wall-adapting local eddy–viscosity (WALE) subgrid model is selected. Given that the mesh of the feedback channels and the main body of the oscillator structure are divided separately, interfaces are set between the moving mesh (feedback channel mesh) and the stationary mesh (the rest of the mesh) so that each part of the mesh is connected. The boundary condition at the inlet of the fluidic oscillator is constrained by a given mass flow rate, and a constant static pressure of standard atmosphere is provided at the outlets. Moreover, a periodic boundary is set in the staggered direction, thus reducing the cost of the 3D LES calculation. In



<span id="page-4-2"></span>this calculation, dual time stepping is employed, and the physical time step is set to  $1 \times 10^{-3}$  s. The flow losses of the device are evaluated by the total pressure loss coefficient, which is defined as follows:  $\mathbf{r}^*$ 

<span id="page-4-3"></span>
$$
\omega = \frac{P_0^* - P_1^*}{0.5\rho V^2},\tag{1}
$$

where  $P_0^*$  is the time-average total pressure at the inlet,  $P_1^*$  is the time-average total pressure at the outlet,  $\rho$  is the density of the fluid, and V is the velocity magnitude of the sweeping iet

<span id="page-4-0"></span>The numerical simulation (CFD) results of the prototype fluidic oscillators are compared with the experimental results [\(Ostermann et al., 2018\)](#page-15-11), as illustrated in [Figures 5A, B.](#page-5-0) [Figure 5A](#page-5-0) shows the transient sweeping jet angle of the prototype fluidic oscillator obtained by the simulation (operating at a jet velocity of 19 m/s) and experiment (the experimental data obtained from Ref. [\(Ostermann et al., 2018\)](#page-15-11)). [Figure 5B](#page-5-0) presents the jet frequency as a function of velocity obtained from the numerical simulations and experiments. In CFD, the jet angle is obtained by monitoring the normal and tangential flow velocity components at the throat of the outlet, whereas in the experiments, the sweeping angle is monitored on a section at a certain distance from the outlet. Thus, the two results show some differences. According to [Figures 5A, B,](#page-5-0) the CFD results generally agree with the experimental results. The sweeping angle of the jet obtained by CFD demonstrates a cyclic trend that approximates a sinusoidal function, which is consistent with the experimentally obtained results. In addition, the experimental dominant frequency of the jet is 9.31 Hz, which is very close to the value of 9.66 Hz obtained by CFD. [Figures 5A, B](#page-5-0) illustrate that the numerical method can predict the transient characteristics of the unsteady flow field of the oscillator. Therefore, this numerical method can be applied to the numerical computation of the modified fluidic oscillator in the subsequent sections.



# <span id="page-5-0"></span>4 Theory of sweeping frequency in two types of fluidic oscillators

In the prototype, jet frequency is proportional to velocity at low jet velocities, but the jet frequency of the fluidic oscillator with resonators is related only to the structural parameters (e.g., length of the resonator).The modified fluidic oscillator combines the structural features of the two oscillators. So, the following sections analyzes the frequency characteristics of the prototype and modified fluidic oscillator theoretically.

## 4.1 Fluidic oscillators with feedback channels only

In this section, we analyze the theoretical formulation of jet frequency in the prototype oscillator and apply numerical data to it.

For fluidic oscillators with feedback channels only, jet sweeping frequency is related to the geometry and mass flow rate of the oscillator. Ostermann et al. [\(Ostermann et al., 2019\)](#page-15-7) and Simões et al. [\(Simões et al., 2005\)](#page-15-12) proposed the equation for the sweeping jet frequency of a fluidic oscillator with feedback channels as follows:

<span id="page-5-1"></span>
$$
f = \frac{1}{T} \approx \frac{1}{2} \frac{1}{\left(\frac{L_f}{c} + \frac{\xi L}{V_y}\right)},\tag{2}
$$

where  $L_f$  is the length of the feedback channel,  $c$  is the speed of sound,  $V_{y}$  is normal (y-axis direction as illustrated in [Figure 2\)](#page-3-1) jet velocity,  $L$  is the length of the mixing chamber, and  $\xi$  is the empirical constant for correction. When  $V_y \ll c$ ,  $\frac{L_y}{c}$  $\frac{c}{c}$  is considered

to be a negligible quantity, and Eq. **[2](#page-5-1)** can be simplified as follows:

<span id="page-5-2"></span>
$$
f \approx \frac{1}{2} \frac{V_y}{\xi L}.
$$
 (3)

Thus,  $f$  is proportional to  $V_y$  (referred to as linear relation, and this situation is illustrated in [Figure 5\)](#page-5-0). When  $O(V_y/c) = 1$ , that is, when the compressibility of the fluid needs to be considered,  $f$  and  $V_y$  are nonlinearly related (referred as nonlinear relation).

We use the relations in Eqs **[2](#page-5-1)**, **[3](#page-5-2)** to fit the numerical simulation results of the prototype, as shown in [Figure 6.](#page-6-0) In [Figure 6,](#page-6-0) when the jet velocity is below 30 m/s, the Mach number is much lower than 0.3, and the compressibility effect is negligible. Under this circumstance, the frequency of the jet generated by the oscillator is approximately proportional to the jet velocity, and the Strouhal number obtained from the numerical simulation is calculated from this slope as 0.0157, which basically coincides with the experimental value of 0.015 in Ref. [\(Ostermann et al., 2018\)](#page-15-11). When the jet velocity is higher than 30 m/s, the increment in jet frequency decreases with the increase in the Mach number, indicating a nonlinear relationship.

In Eq. [2](#page-5-1),  $\xi$  is an empirical constant. According to Ref. [\(Simões et al., 2005\)](#page-15-12), the value of  $\xi$  for an oscillator varies with velocity and oscillation frequency. From the numerical simulation results, we find that in this case, the empirical constant ξ obtained is approximately proportional to the inlet flow rate or normal jet velocity  $V_y$  [\(Figure 7\)](#page-6-1), and the fitting relation is

<span id="page-5-3"></span>
$$
\xi = 0.0515V_y + 3.6877.\tag{4}
$$



<span id="page-6-0"></span>

<span id="page-6-1"></span>By substituting  $ξ$  in Eq. [4](#page-5-3) into Eq. [2](#page-5-1), we obtain the nonlinear relation between the oscillation frequency and jet velocity of the prototype. As illustrated by the nonlinear relation in [Figure 7,](#page-6-1) the nonlinear Eq. [2](#page-5-1) obtained by considering the relation of  $\xi$  and  $V<sub>y</sub>$  is in good agreement with the numerical simulation results. Considering that the fluidic oscillator analyzed in this study is proposed by modifying the prototype, we use this relation as the basis for evaluating the effect of geometric parameters when we investigate the characteristics of the modified model in the following sections.

#### 4.2 Fluidic oscillator with dual quarter-wave resonators

In this section, we derive the jet frequency law of the fluidic oscillator with dual quarter-wave resonators. The relationship between jet frequency and resonator length in a fluidic oscillator with a single quarter-wave resonator has been proposed in Ref. [\(Field and Fricke, 1998\)](#page-14-15). The relationship between jet frequency and resonator length needs to be derived for oscillators with dual resonators because modified fluidic oscillators have two symmetrical resonators. The derived equations for an oscillator with two symmetrical resonators are similar to those with a single quarterwave resonator.

In a bounded medium, such as resonator structures in an oscillator, a quarter-wave resonator has two boundaries where reflection can occur: the open end and the closed end. Unlike a progressive wave in an unbounded medium, a wave set in a linear system, such as a fluidic oscillator with a resonator, is reflected off the two boundaries. Therefore, it propagates continuously between the two boundaries. Each time a vibratory source acts on the open end of the resonator, the vibratory source transfers energy to the air in the resonator cavity. This process forms standing waves in the cavity, creating a resonant state.

Next, the frequency equation of the modified fluidic oscillator (with two resonators) is derived. The wave generated in one direction is

$$
\varphi_1 = a \sin[2\pi(kx - ft) + \alpha],\tag{5}
$$

where  $a$  is the wave amplitude,  $k$  is the wave number,  $f$  is the frequency, and  $\alpha$  is the wave initial phase.

The wave generated in the other direction is

$$
\varphi_2 = a \sin[2\pi(kx + ft) + \beta],\tag{6}
$$

where  $\beta$  is another wave initial phase. The two expressions are known solutions of the wave equation. The superposition principle can be used because the wave equation is a second-order linear differential equation. As a result of the superposition of the incident and reflected waves, the formation of a standing wave can be expressed as

<span id="page-6-2"></span>
$$
\varphi = \varphi_1 + \varphi_2 = 2a \sin \left( 2\pi k x + \frac{\alpha + \beta}{2} \right) \cos \left( 2\pi f t + \frac{\alpha - \beta}{2} \right). \tag{7}
$$

We know that  $x = 0$  and  $x = 2L_R$  are rigid ends of the resonator, and  $x = L_R$  is in the open, where LR is the length of a quarter-wave resonator. Thus, the boundary conditions at the two rigid ends are

$$
\begin{cases}\nx = 0, \varphi = 0 \\
x = 2L_R, \varphi = 0\n\end{cases}
$$
\n(8)

In accordance with the first boundary condition, the following expression is obtained:

$$
2a\sin\left(\frac{\alpha+\beta}{2}\right)\cos\left(2\pi ft + \frac{\alpha-\beta}{2}\right) = 0.
$$
 (9)

Therefore,  $\frac{\alpha+\beta}{2} = 0$ , i.e.,  $\beta = -\alpha$ . From Eq. [7](#page-6-2), we derive

$$
\varphi = 2a\sin(2\pi kx)\cos(2\pi ft + \alpha). \tag{10}
$$

From the second boundary condition, the following expression is obtained:

$$
2a\sin(4\pi kL_R)\cos(2\pi ft + \alpha) = 0.
$$
 (11)

Thus,  $sin(4\pi kL_R) = 0$  or  $4kL_R = n$  (*n* is a positive integer). According to the relations between wave number k and frequency f,

$$
k = \frac{1}{\lambda} = \frac{f}{c}.\tag{12}
$$

Hence, we can deduce that

<span id="page-7-1"></span>
$$
f = \frac{nc}{4L_R}, (n = 1, 2, 3...). \tag{13}
$$

The minimum value of  $n$  is 1, so the minimum or characteristic frequency calculated by Eq. **[13](#page-7-1)** describing the dual symmetrical resonator fluidic oscillator is:

$$
f = \frac{c}{4L_R}.\tag{14}
$$

When the modified model has resonators only, the two nearinlet resonators play the main role in determining the jet frequency. The frequency of the jet may be fractional or integral multiples of the characteristic frequency of the resonators (i.e., subharmonic or harmonic frequency) because of the nonlinear effect in the flow field and the coupling between the resonator and feedback channel.

For the prototype fluidic oscillator [\(Ostermann et al., 2019\)](#page-15-7), when the shape of the fluidic oscillator is fixed, the value of the Strouhal number is nearly invariant. Strouhal number St is related to jet frequency  $f_j$ , width of the throat  $d$ , and jet velocity  $V_{y}$ , as shown by the following equation:

$$
St = \frac{f_j d}{V_y}.\tag{15}
$$

However, the present study changes the structure of the feedback loops through the movement of the movable feedback channels, thus causing St to change accordingly.

Given that the jet frequency generated by the fluidic oscillator with resonators is fixed, according to Eq. **[16](#page-7-2)**, St is inversely proportional to  $V_{y}$ , that is, as the flow rate through the jet changes, the Strouhal number also changes [\(Field and Fricke, 1998\)](#page-14-15). The modified fluidic oscillator discussed in this work has the structural features of fluidic oscillators with feedback channels and those with resonators, which may adjust both the Strouhal number and the frequencies by the movable feedback channel and flow rate. The characteristics, such as flow losses, oscillation amplitude, and unsteady characteristics, are unknown and will be discussed below by simulation.

## <span id="page-7-0"></span>5 Numerical results and analysis—characteristics of the fluidic oscillator with both feedback channels and resonators

In this study, the feedback channel is designed as a movable component on the basis of the prototype model. To reflect the



<span id="page-7-3"></span>relative length of the feedback channel, the ratio of feedback channel length to resonator length is defined as

<span id="page-7-2"></span>
$$
R = \frac{L_f}{L_R}.\tag{16}
$$

Thus, three typical states represented by  $R = 1.62, 2.07,$  and 2.51 are investigated, and each state is given three different inlet mass flow rates (corresponding to inlet velocities of 10, 20, and 40 m/s) in the unsteady calculations.

## 5.1 Flow loss characteristics

The fluidic oscillator, as a flow control method, is designed to suppress external flow separation losses, and it requires a low level of flow losses within itself. In the numerical simulation, the total pressure loss coefficient (Eq. **[1](#page-4-3)**) is used to evaluate the flow loss characteristics of the device, and [Figure 8](#page-7-3) shows the comparison of total loss coefficients between the prototype and the modified model  $(R = 1.62, 2.07,$  and 2.51) at different inlet mass flow rates.

Numerical calculations of the prototype and the modified fluidic oscillator with different  $R$  values are performed at three given mass flow rates. The total pressure loss coefficient of the prototype increases slightly with the increasing normal jet velocity  $V<sub>y</sub>$  (reflecting the mass flow rate), as shown in [Figure 8.](#page-7-3) Also, compared with the total pressure loss coefficient of the prototype, that of the modified model at  $R = 1.62$ ,  $R = 2.07$ , and  $R = 2.51$  is 14%, 28.1%, and 37.7% lower, respectively, at the jet velocity of 96 m/s.

The modified oscillator in the  $R = 1.62$  condition only differs from the prototype in terms of the resonator (the lengths of the feedback channels are approximately equal). In comparison with the prototype model, in the modified model of  $R = 1.62$ , the total pressure loss coefficient is 2.8% lower at a jet velocity of 24 m/s, 3.7%



<span id="page-8-0"></span>lower at 48 m/s, and 14.0% lower at 96 m/s due to the existence of feedback channels. A decrease in the total pressure loss coefficient occurs in the modified model as  $V_y$  increases. Moreover, the cases with other different R values ( $R = 2.07$  and 2.51) show that the modified model has smaller internal flow loss than the prototype model over a wide range of jet velocities.

Furthermore, with the increase in R, the decrement degree of the total pressure loss coefficient expands when  $V_y$  is increased. As  $R$ increases, the farther the movable feedback channel is from the main flow path, the more considerable the influence of the resonators becomes. Therefore, we believe that the resonators are the dominant factor in the loss reduction.

#### 5.2 Frequency characteristics

The sweeping frequencies for different  $R$  values at different jet velocities are calculated with Eq. **[2](#page-5-1)**, as shown in [Figure 9.](#page-8-0) According to the theoretical model, difference in jet sweeping frequency at different R values is not significant, indicating that theoretically, for the fluidic oscillator with both mixing chamber and feedback channels, regulating the jet sweeping frequency substantially by simply adjusting the length of the feedback channels is difficult.

In [Figure 10,](#page-8-1) the theoretical jet frequency of the fluidic oscillator is calculated with Eq. **[2](#page-5-1)**, and the theoretical characteristic frequency of the fluidic oscillator with symmetrical resonators is calculated with Eq. **[4](#page-5-3)**. The one-third and one-quarter theoretical frequencies of the resonator are also plotted. Analysis is conducted by comparing the theoretical relations and simulated results. Observation of the corresponding frequencies at three velocities in the condition  $R =$ 1.62 suggests that the relationship between frequency and velocity in this condition is roughly in accordance with the nonlinear relation of the prototype model with only feedback channels. Therefore, when the feedback channel is short ( $R = 1.62$ ), the feedback channel is



<span id="page-8-1"></span>Simulated (for different R values) and theoretical frequency versus jet velocity.



<span id="page-8-2"></span>close to the main flow path, and the jet frequency characteristics are dominated by the feedback channels. The self-excitation mechanism of this modified model ( $R = 1.62$ ) is similar to that of the prototype model.

Notably, we obtain a new finding, as shown in [Figure 10.](#page-8-1) The red dot  $(R = 1.62)$  in [Figure 10](#page-8-1) at the jet velocity of 96 m/s indicates frequency bifurcation, which means the sweeping frequency alternately switches between 27 Hz and 73 Hz, where 27 Hz is in accordance with the theoretical relation and 73 Hz is unexpected. The sweeping angle also presents the switching

<span id="page-9-0"></span>

<span id="page-10-0"></span>



<span id="page-11-0"></span>phenomenon, which will be discussed further in [Section 5.3.](#page-13-0) This phenomenon is the state of switching from a low frequency and a high amplitude to a high frequency and a low amplitude over time [\(Figure 12C,](#page-9-0) which illustrates the time-domain curve ofthe sweeping angle). Given that this phenomenon is only observed in cases with high jet velocity, the phenomenon occurs beyond a certain Reynolds number threshold. As shown in [Figure 10,](#page-8-1) the low frequency is determined by the feedback channel, and the high frequency is related to the resonator. The authors suggest that the phenomenon is relevant to the competition of the feedback channel and the resonator for dominating the main stream alternately, but a certain randomness exists in the domination at a certain moment [\(Figure 12C\)](#page-9-0), which will be described in detail in [Section 5.4.](#page-13-1)

[Figure 10](#page-8-1) also depicts the simulated corresponding frequencies at three different velocities in the  $R = 2.07$  condition, and the relationship between the frequencies and velocities in this condition is consistent with the theoretical calculation of the modified model at  $R = 2.07$ . Therefore, the dominant mechanism factor of model action in the  $R = 2.07$  condition is similar to that of the prototype with a feedback channel. Compared with  $R = 1.62$  and  $R = 2.07$ conditions, the  $R = 2.51$  condition shows a substantial change in jet frequency, particularly when the jet velocity is high. For the

modified model in the  $R = 2.51$  condition, the frequency at low jet velocities is more than twice the frequency of the modified model at  $R = 2.07$ . At high velocities, the frequencies are roughly equal to the subharmonic frequencies of the characteristic frequency of the fluidic oscillators with resonators only. A possible reason for the high frequency in the  $R = 2.51$  condition is that the feedback channel and the mixing chamber are far apart, so the feedback channel cannot effectively affect the frequency of the jet, and the jet frequency is dominated by resonance and determined mainly by the length of the resonant cavity. Thus, a high-frequency jet is generated.

The role of this oscillator is to adjust the frequency. The movement of the feedback channel changes the length of the feedback loop (denoted by different R values) and the characteristics of the oscillator. Then, through the feedback channel and resonators with different degrees of coupling, the sweeping angle and frequency of the jet are adjusted. At a constant mass flow rate, a considerable change in frequency occurs when the feedback channel length is adjusted. At a low jet velocity ( $V_v = 24$  m/s), the frequency changes by about a factor of two from the shortest feedback channel ( $R =$ 1.62) to the longest ( $R = 2.51$ ). At a high jet velocity ( $V<sub>v</sub> = 48$  and 96 m/s), the sweeping frequency increases up to 8.8 times, which



#### FIGURE 15

<span id="page-12-0"></span>Transient velocity contour of the flow field at **(A)** 1/67<sub>1</sub>, **(B)** 2/67<sub>1</sub>, **(C)** 3/67<sub>1</sub>, **(D)** 4/67<sub>1</sub>, **(E)** 5/67<sub>1</sub>, **(F)** 6/67<sub>1</sub>, **(G)** 1/67<sub>2</sub>, **(H)** 2/67<sub>2</sub>, **(I)** 3/67<sub>2</sub>, **(I)** 4/67<sub>2</sub>, **(K)** 5/6 $\mathcal{T}_2$ , and **(L)** 6/6 $\mathcal{T}_2$  modes ( $\mathcal{T}_1$  is one oscillation period at a lower frequency, and  $\mathcal{T}_2$  is one oscillation period at a higher frequency. The figure presents a process of frequency switching from period  $T_1$  to  $T_2$ . The time required for this process varies and the figure shows a typical transition. (*R* = 1.62 and  $V_y = 96$  m/s in this figure).

is impossible for a typical oscillator with a mixing chamber and feedback channel (a change in the length of the feedback channel has little effect on frequency, as shown in [Figure 9\)](#page-8-0). This is an important advantage of the proposed solution in this study.

#### 5.3 Sweeping magnitude characteristics

This section analyzes the sweeping angle magnitude of the jet. A data processing method is needed to obtain the effective sweeping angle amplitude because the jet angle curve is only approximately sinusoidal. We treat the jet angle as an oscillation described as  $u = U_m \cdot \sin(\omega t + \phi)$ , where  $U_m$  is the amplitude,  $\omega$  is the circular frequency, and  $\phi$  is the initial phase. We know that the electrical voltage described as  $u = U_m \cdot \sin(\omega t + \phi)$  has the following relation,

$$
U_m = \sqrt{2} \cdot U,\tag{17}
$$

where U is the effective or root mean square voltage, which can be calculated using the following discretized relation:

$$
U = \sqrt{\sum_{i=1}^{n} (u_i - \overline{u})^2 \over n - 1}.
$$
 (18)

where  $\overline{u}$  is the averaged  $u_i$ . Through this method, the effective value (U) of voltage is obtained (the amplitude is difficult to be determined directly, so it is processed indirectly) and then multiplied by the square root of 2 to derive the voltage amplitude  $(U_m)$ .

By imitating the calculation of voltage magnitude and using Eqs. (17) and (18), we can obtain the magnitude of the sweeping angle produced by the fluidic oscillator. [Figure 11](#page-8-2) shows a comparison of the amplitude values of the prototype and the modified model with different R values at different jet velocities. The maximum sweeping angle of the jet is close to 45° for both the prototype and  $R = 1.62$ . Given different R values at the same jet velocity, the figure indicates that the long feedback channel model ( $R = 2.51$ ) has lower amplitudes compared with the prototype and the modified model with shorter ( $R = 1.62$  and 2.07) feedback channels. At this point, the sweeping jet with high frequency and low amplitude is mainly produced by the dominant action of the resonators. Under a varying jet velocity at the same R value, the amplitude decreases as the jet velocity increases because as the velocity increases (i.e., an increase in the Reynolds number), the fluid inertia effect increases, and the viscous effect decreases. Meanwhile, the Coanda effect is related to viscosity, thus making the jet less likely to produce oscillation at this time. In addition, the amplitude of the sweeping angle switches between 17° and 49° when  $R = 1.62$ ,  $V_v = 96$  m/s, as illustrated in [Figure 12C.](#page-9-0) This unusual unsteady characteristic will be discussed in detail in [Section 5.4.](#page-13-1)

## <span id="page-13-1"></span>5.4 Unsteady characteristics

This section analyzes some special unsteady characteristics due to different parameters of jet velocity  $V_{y}$  and different values of R. In consideration of these characteristics, two typical states with minimum  $(R = 1.62)$  and maximum  $R$   $(R = 2.51)$  are used to analyze and demonstrate the transient sweeping angle <span id="page-13-0"></span>and flow field. A comparison of sweeping angle versus time for different jet velocities at  $V_v = 24$ , 48, and 96 m/s in the  $R = 1.62$  condition is presented in [Figures 12A–C.](#page-9-0) In [Figure 12C,](#page-9-0) the frequency switching phenomenon can be seen clearly. The dominant frequencies obtained from the frequency-domain plots [\(Figures 12D–F\)](#page-9-0) are 14 Hz, 20 Hz and 27 Hz (with a subdominant frequency around 70 Hz) when  $V_y = 24$ , 48 and 96 m/s, respectively. However, the frequency switching phenomenon is not significantly reflected in the frequency domain plots. We attribute this to the small amplitude of the oscillations around 70 Hz, which is therefore not significant in the frequency domain diagram. Moreover, the sweeping angle in  $R = 2.51$  condition [\(Figures 13A–C\)](#page-10-0) shows that the amplitude of the sweeping angle decreases as the inlet mass flow rate gradually increases. As illustrated in [Figures 13D–F,](#page-10-0) frequencydomain plots show that the frequency switching phenomenon is presented obviously (See [Figure 13E\)](#page-10-0). Therefore, the frequency switching phenomenon appears to be related to the R value and jet velocity.

To clearly illustrate the frequency switching phenomenon, two typical unsteady flow fields at  $R = 1.62$  are selected for demonstration. By comparing the unsteady flow field between  $R = 1.62$ ,  $V_v = 24$  m/s [\(Figure 14\)](#page-11-0) and  $R = 1.62$  and  $V_v = 96$  m/s [\(Figure 15\)](#page-12-0), we find that when  $V_v = 24$  m/s, the flow fields are similar to those of the prototype. When  $V<sub>v</sub> = 96$  m/s, initially, the jet characteristics are similar to those when  $V<sub>v</sub> = 24$  m/s. However, after some time, they change to a higher frequency and smaller sweeping angle (because of the low flow rate and weak mobility of the flow in the feedback channels, the effect of the feedback channel can be ignored), and a clear frequency and amplitude switching phenomenon can be observed. The authors suggest that this frequency switching phenomenon may be applied in some flow control scenarios having two dominant modes with different frequencies and weights, such as shock–boundary layer interaction and blade tip leakage flow.

# 6 Conclusion

In this study, we propose a fluidic oscillator with feedback channels and resonators and investigate its characteristics in terms of internal flow losses, jet frequencies, sweeping angles, and unsteady flow field characteristics through numerical simulation. The main conclusions are as follows.

- 1. The total pressure loss of the prototype fluidic oscillator will increase by 5.6% when the normal velocity of the sweeping jet  $V_{\nu}$ ranges from 24 m/s to 94 m/s. By comparison, the total pressure loss of the modified fluidic oscillator with movable feedback channels and resonators decreases by 6.7% ( $R = 1.62$ ), 16.3%  $(R = 2.07)$  and 18.9%  $(R = 2.51)$  when  $V_y$  increases from 26 m/s to 112 m/s. In addition, the decrement degree of the total pressure loss expands with the increase in  $V_y$ . The above phenomenon indicates that the new fluidic oscillator has better economic benefits when utilized as a flow control device.
- 2. The analysis of jet frequency indicates that theoretically, a change in the feedback channel length (denoted by a nondimensional parameter R in this study) has little effect on frequency. However, in the simulation, the frequency changes up to 8.8 times when the R value is gradually enlarged. Specifically, when

the R value changes from 1.62 to 2.51, the frequency ranges from 27Hz to 238 Hz. The reason for its change is that the change in the feedback channel length results in a weakened role of the feedback channel, which is in a state where the resonators dominate the role and produce high frequency. The fluidic oscillator can produce jets with different frequencies and sweeping angles under the combination of flow velocity and feedback channel length changes.

3. Frequency switching, a phenomenon where the jet randomly switches from 27Hz frequency and 49<sup>∘</sup> amplitude to 73Hz and 17°, is observed in the  $R = 1.62$ ,  $V_y = 96$  m/s mode. The authors suggest that this phenomenon arises as the feedback channels and resonators compete for control and alternately dominate the mainstream, but randomness still exists with regard to which one dominates at a given moment. This finding may provide a potential solution to the problem of controlling flow with more than one dominant frequency in highly loaded compressors that require varying jet frequencies at off-design point conditions., such as tip leakage flow and shock–boundary layer interaction, which can produce two different dominant frequencies.

# Data availability statement

The raw data supporting the conclusion of this article will be made available by the authors, without undue reservation.

# Author contributions

ZY: date Curation, Writing—Original Draft. YL: date Curation, Writing—Original Draft. XY: Writing—Original Draft. QD: Date Curation. WL: conceptualization, Methodology, Writing—Review and Editing. All authors contributed to the article and approved the submitted version.

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# Conflict of interest

The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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