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# Remaining useful life prediction of lithium-ion batteries using CEEMDAN and WOA-SVR model

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The remaining useful life (RUL) prediction of Lithium-ion batteries (LIBs) is a crucial element of battery health management. The accurate prediction of RUL enables the maintenance and replacement of batteries with potential safety hazards, which ensures safe and stable battery operation. This paper develops a new method for the RUL prediction of LIBs, which is combined with complete ensemble empirical mode decomposition with adaptive noise (CEEMDAN), whale optimization algorithm (WOA), and support vector regression (SVR). Firstly, the CEEMDAN is employed to perform noise reduction in battery capacity data for prediction accuracy improvement. Then, an SVR model optimized by the WOA is proposed to predict the RUL. Finally, the public battery datasets are selected to validate the performance of the CEEMDAN-WOA-SVR method. The RUL prediction accuracy of the CEEMDAN-WOA-SVR method is better than the WOA-SVR method. In addition, a comparison is made between the proposed method and the existing methods (artificial bee colony algorithm-SVR method, ensemble empirical mode decomposition-gray wolf optimization-SVR method). The results show that the accurate prediction of the proposed method is superior to the two methods.

## KEYWORDS

remaining useful life, lithium-ion battery, whale optimization algorithm, CEEMDAN, support vector regression

## 1 Introduction

Lithium-ion batteries (LIBs), as a green energy source, are characterized by high capacity, high reliability, and high safety. They have been widely used in fields involving electric vehicles, mobile phones, and computers (Xue et al., 2020; Ren L. et al., 2021). However, as the number of LIBs operations increases, the batteries will experience aging problems, and the failed batteries will affect the regular operation of the devices (Chen W. et al., 2021). A LIB's remaining useful life (RUL) is the number of remaining charge/discharge cycles before the end of life (EOL). The accurate RUL prediction of LIBs could guide timely battery repair and replacement to ensure safe operation. Therefore, the research on RUL prediction of batteries has attracted extensive attention (Bracale et al., 2021).

Recently, many RUL prediction methods have been developed in the research literature, and these methods are mainly divided into two types: model-based methods and data-based methods (Ge et al., 2021). The model-based methods aim to build a mathematical-physical model to estimate the RUL of LIBs based on the failure mechanisms. Xing et al. (2013) presented an ensemble model that integrated an empirical exponential, a polynomial regression, and particle filtering (PF) for the RUL prediction. Su et al. (2017) developed a new method based on the interacting multiple model particle filter for the RUL prediction. Guha and Patra (2018) presented a regression model combined with the reconstructed electrochemical impedance spectrum, which was applied to the PF method to predict the RUL. Deng et al. (2020) proposed an empirical model to predict the RUL and used the PF method to estimate the parameters of the model. Hong et al. (2022) built an iterative model of the generalized Cauchy process with long-range dependence characteristics for the RUL prediction. The model-based methods are built based on the battery failure mechanisms and could obtain high prediction accuracy. However, the battery operating process is a complex and dynamic system, and many parameters require consideration to construct a model with high prediction accuracy.

The data-based methods are different from the model-based methods, which mainly mine the valid information from historical degradation data without considering failure mechanisms. Machine learning techniques such as the support vector machine (SVM) and artificial neural network (ANN) are used to predict the RUL of LIBs. Qin et al. (2019) proposed a

fusion model based on the PF algorithm and ANN to predict the RUL. Ren X. et al. (2021) developed a novel method to predict the RUL by combining the deep convolution neural network (CNN) and long-short-term memory, and the experimental results demonstrated the effectiveness of the proposed method. Zhang et al. (2022) presented a hybrid parallel residual CNN model for RUL prediction. Tang and Yuan (2022) extracted the health indicators from all the measured parameters and constructed an ANN model to predict the RUL from three aspects of the shape feature. However, the ANN-based prediction methods have high prediction accuracy, which requires more computing time and computational complexity. The support vector regression (SVR) model, as a type of SVM model, has a simple structure and is widely used for RUL prediction. Zhao et al. (2018) extracted health indicators and proposed an SVR model combined with feature vector selection to achieve the prediction of the RUL. Wei et al. (2018) combined a particle filter with the SVR model for the RUL prediction, and the results showed that the proposed method could achieve an accurate result. Wang et al. (2019) developed a hybrid method based on an artificial bee colony algorithm and SVR (ABC-SVR) to predict the RUL, and the results indicated that an accurate prediction was obtained. Yang et al. (2021) presented a hybrid model to predict the RUL, which combined the ensemble empirical mode decomposition (EEMD), gray wolf optimization, and SVR (GWO-SVR). In a data-driven approach, complex historical data are used to predict the RUL effectively, and the feature information extracted from the historical data is crucial.

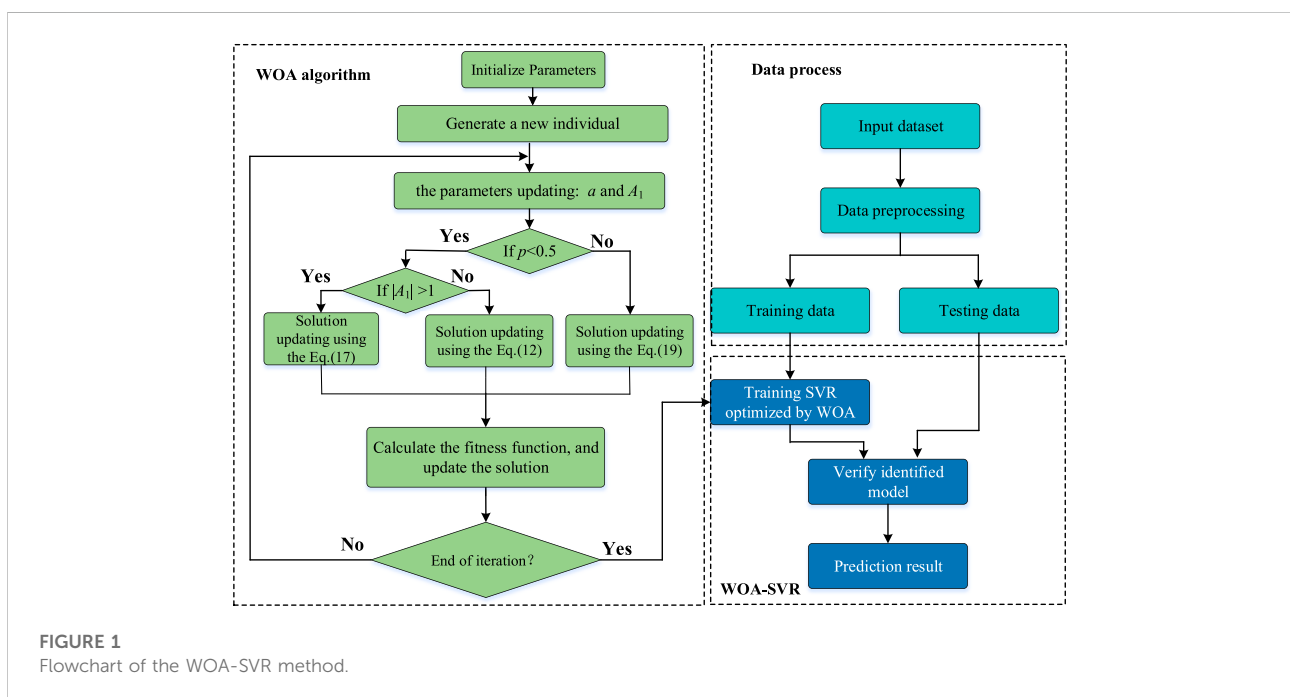
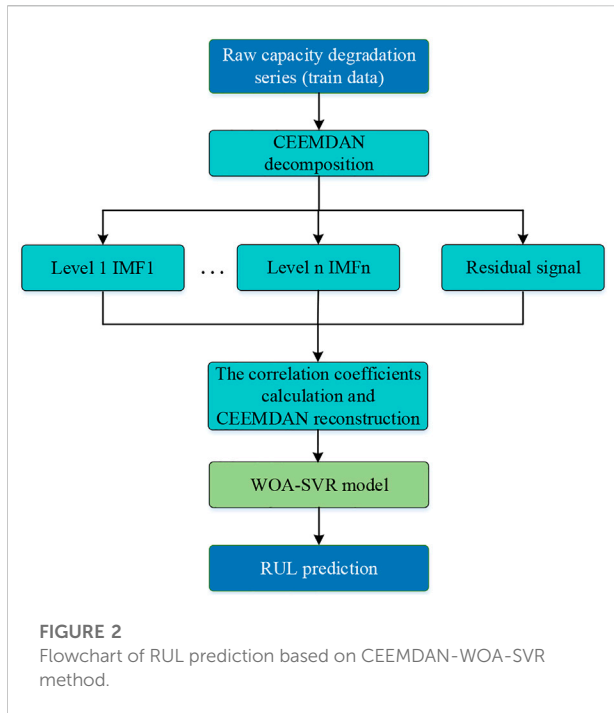
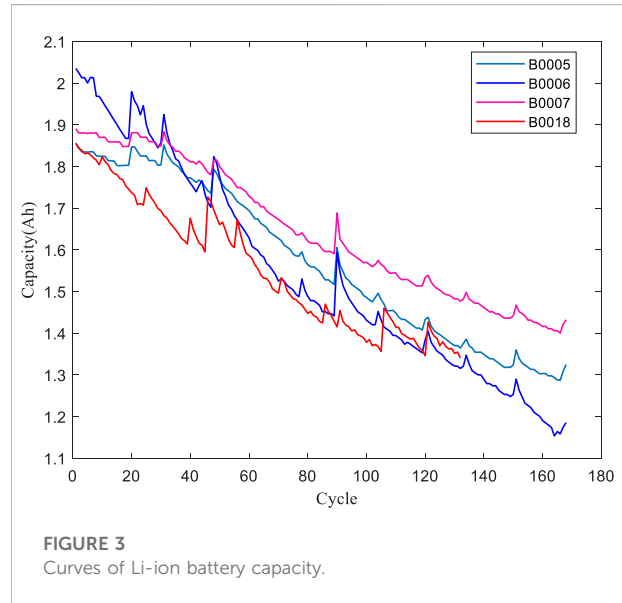


FIGURE 1  
Flowchart of the WOA-SVR method.



Inspired by references (Wei et al., 2018; Wang et al., 2019; Yang et al., 2021), a new data-based method is proposed to predict the RUL in this paper, and the method combines the complete ensemble empirical mode decomposition with adaptive noise (CEEMDAN), whale optimization algorithm (WOA), and SVR model (WOA-SVR). The CEEMDAN method is used firstly for noise reduction processing of battery capacity data, which effectively improves prediction accuracy. The WOA is a new intelligent optimization algorithm and has excellent search capability compared to other optimization algorithms. The SVR model has the advantages of global optimality and high generalization ability in solving nonlinear problems, but there are still some challenges in selecting the parameters of the SVR model (Wang and Mamo, 2018). To address the issue of selecting the SVR method parameters, the WOA is applied to select the kernel parameters to facilitate the RUL prediction of LIBs. Although the WOA-SVR method has been used to solve signal series data problems in many fields (Li et al., 2020; Tikhmarine et al., 2020; Wang et al., 2021), this method is employed for the RUL prediction for the first time. The proposed method is validated using a public battery dataset provided by the NASA Prognostics Center of Excellence (Goebel et al., 2008). The proposed method accurately predicts the RUL of LIBs according to the experimental results, thus enabling timely battery maintenance and replacement.

The remainder of the paper is organized as follows. In Section 2, the principle of the related theory is described,



including the CEEMDAN method, WOA algorithm, and SVR model. Section 3 introduces the RUL prediction for LIBs using the CEEMDAN-WOA-SVR method. Noise reduction processing of the capacity degradation data is analyzed, and the prediction results are discussed in Section 4. Finally, the conclusion and future work are shown in Section 5.

## 2 Related theory

### 2.1 Principle of complete ensemble empirical mode decomposition with adaptive noise

Empirical mode decomposition (EMD) is presented as a signal processing method that transforms the signal sequence into several intrinsic mode functions (IMFs) and a residual (Huang et al., 1998). Although the EMD method has been widely used in signal processing, it has significant problems, such as end effect and modal aliasing. As an improvement of EMD, the CEEMDAN method is proposed by the addition of adaptive white Gaussian noise, which efficiently suppresses the end effect and modal aliasing (Zhang and Hong, 2019).

Assuming that the original signal sequence and Gaussian white noise are  $s(n)$  and  $\nu(n)$ , respectively, and the  $i$ -th composite signal after the addition of Gaussian white noise can be represented as  $s^i(n) = s(n) + \nu^i(n)$ . The detailed steps are given as follows (Chen Z. et al., 2021; Peng et al., 2021):

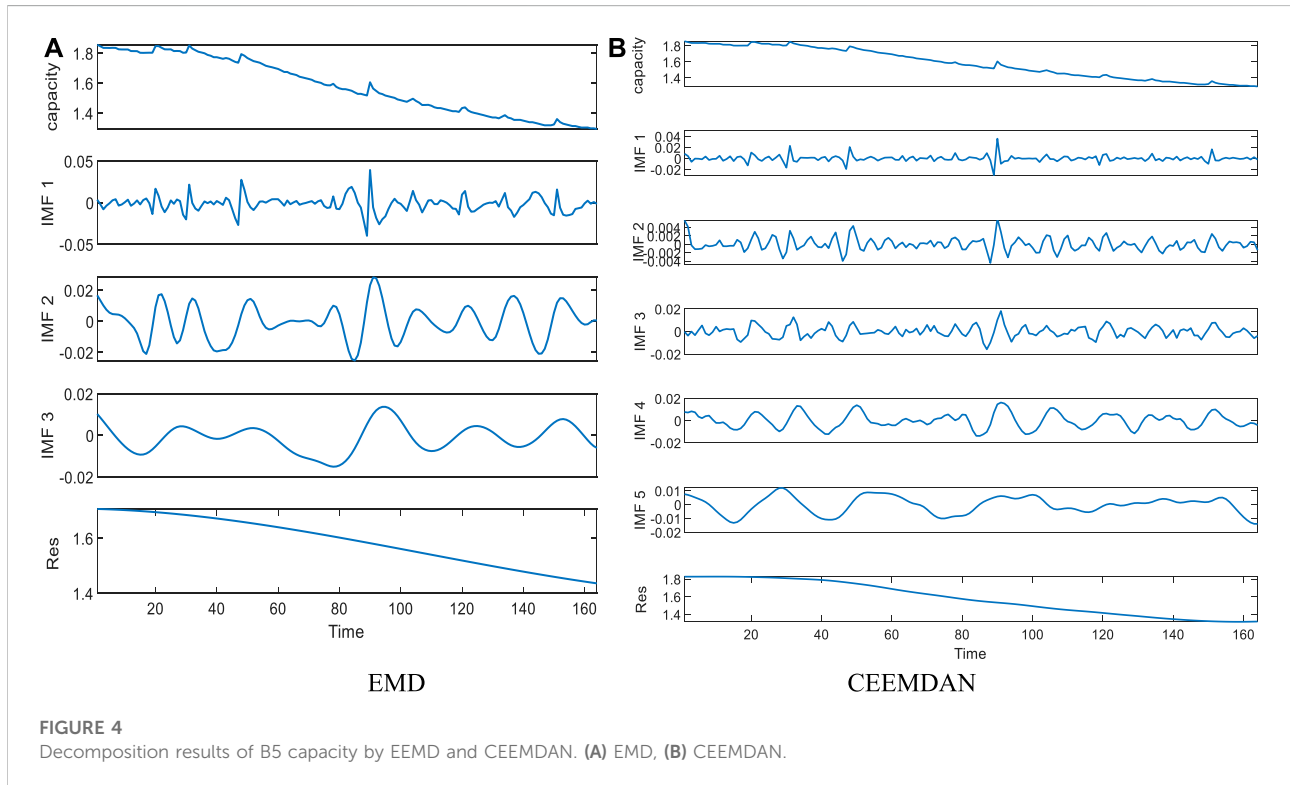


FIGURE 4 Decomposition results of B5 capacity by EEMD and CEEMDAN. (A) EMD, (B) CEEMDAN.

1) The signal time series  $s^i(n)$  is decomposed by the CEEMDAN method. The calculation of the first modal component is represented as:

$$IMF_1(n) = \frac{1}{I} \sum_{i=1}^I IMF_1^i(n) = \overline{IMF_1(n)} \quad (1)$$

where  $I$  represents the decomposition time.

2) The residual sequence is calculated, and the first residual sequence is given by:

$$r_1(n) = s(n) - IMF_1(n) \quad (2)$$

3) Adding  $\varepsilon_1 E_1[v^j(n)]$  to the first residual sequence, the realization  $r_1(n) + \varepsilon_1 E_1[v^j(n)]$ ,  $i = 1, 2, \dots, I$ , is achieved. Then, decompose  $r_1(n) + \varepsilon_1 E_1[v^j(n)]$ ,  $i = 1, 2, \dots, I$ , and the second modal component can be calculated as:

$$IMF_2(n) = \frac{1}{I} \sum_{i=1}^I E_1(r_1(n) + \varepsilon_1 E_1(v^j(n))) \quad (3)$$

4) Similarly, the  $k$ -th residue sequence is calculated in the remaining phase. Then, the next modal component can be given by:

$$r_k(n) = r_{k-1}(n) - IMF_k(n) \quad (4)$$

$$IMF_{k+1}(n) = \frac{1}{I} \sum_{i=1}^I E_1(r_k(n) + \varepsilon_k E_k(v^j(n))) \quad (5)$$

5) The decomposition process is terminated when the residual sequence is unsuitable for further decomposition. The decomposition process is carried out  $K$  times, and the final result of the residual sequence is shown as:

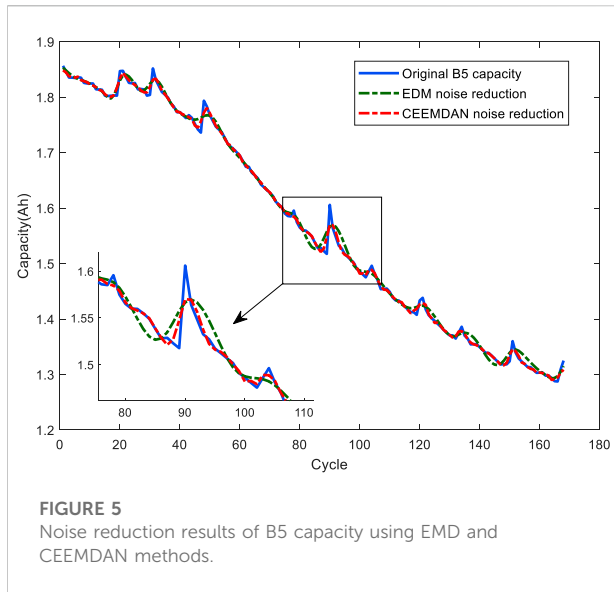
$$R(n) = s(n) - \sum_{i=1}^K IMF_i(n) \quad (6)$$

The original signal series  $s(n)$  can be represented as:

$$s(n) = R(n) + \sum_{i=1}^K IMF_i(n) \quad (7)$$

## 2.2 Support vector regression method

SVR is a type of the SVM model developed through statistical learning (Smola and Schölkopf, 2004). The SVR model can effectively express the nonlinear mapping relationship between input and output data, which has been widely used to solve regression and prediction problems (Amroune et al., 2018; Liu et al., 2021).



**FIGURE 5**  
Noise reduction results of B5 capacity using EMD and CEEMDAN methods.

Supposing that data sample is  $D = \{(x_i, y_i)\}, i = 1, \dots, N$ , where  $x_i$  and  $y_i$  represent the input and output data, respectively. The nonlinear mapping of sample data can be expressed as (Malik et al., 2021):

$$f(x) = \omega \cdot \varphi(x) + b_c \tag{8}$$

where  $f(\cdot)$  denotes the regression function,  $\varphi(\cdot)$  indicates the transfer function,  $\omega$  is the weight parameter, and  $b_c$  represents the intercept parameter.

The regression problem is formulated as:

$$\min R(\omega, b, \zeta) = \frac{1}{2} \|\omega\|^2 + C \sum_i^n (\xi_i + \xi_i^*) \tag{9}$$

$$\text{s.t.} \begin{cases} y_i - \omega \cdot \varphi(x) - b_c \leq \varepsilon + \xi_i \\ \omega \cdot \varphi(x) + b_c - y_i \leq \varepsilon + \xi_i^* \\ \xi_i, \xi_i^* \geq 0. \end{cases} \tag{10}$$

where  $C$  represents the penalty parameter,  $\xi_i$  and  $\xi_i^*$  are the slack variables, and  $\varepsilon$  is the boundary value.

The regression problem is transformed by the Lagrange multipliers and the solution of the nonlinear regression function is obtained by simplification, which can be expressed as:

$$f(x) = \sum_i^n (\alpha_i - \alpha_i^*) K(x_i, x) + b_c \tag{11}$$

where  $K(x_i, x)$  is the kernel function, and  $\alpha_i, \alpha_i^*$  are Lagrange multipliers.

The kernel function has various forms, and this paper selects the radial basis function, represented as:

$$K_{RBF}(x_i, x) = \exp\left(-\frac{1}{2\sigma^2} \|x_i - x\|^2\right) \tag{12}$$

where  $\sigma$  represents the kernel parameter.

**TABLE 1** Parameter setting of the algorithm.

Parameter	Value
Population size, $N_p$	20
Variable dimension, $D_m$	2
Max iteration number, $T$	100
Penalty factor, $C$	[0.01, 100]
Kernel parameter, $\sigma$	[0.01, 100]

For the SVR model, the parameters  $C$  and  $\sigma$  affect the complexity and prediction accuracy of the model. Therefore, intelligent optimization algorithms are used for the optimal selection of parameters.

### 2.3 Whale optimization algorithm algorithm

WOA is a novel metaheuristic algorithm inspired by humpback whales (Mirjalili and Lewis, 2016). The WOA is featured with excellent search capability and simple structure, and has been employed for solving practical optimization problems.

In the WOA, there are three stages for finding superiority: searching for prey, encircling prey, and spiral update of position (Saidala and Devarakonda, 2018; Chakraborty et al., 2021).

Encircling prey ( $p < 0.5$  and  $|A_1| < 1$ ):

$$X_{i,t+1} = X_{best} - A_1 \cdot D, 0 \leq i \leq NP \tag{13}$$

$$D = |C \cdot X_{best} - X_{i,t}| \tag{14}$$

$$A_1 = 2 \cdot a \cdot r - a \tag{15}$$

$$C = 2 \cdot r \tag{16}$$

$$a = 2 - t \cdot (1 - t/T_{max}) \tag{17}$$

where  $X_{i,t}$  denotes the solution in the current generation,  $X_{i,t+1}$  represents the solution in the next generation,  $X_{best}$  is the best solution,  $NP$  is the population number,  $t$  is the current number of iterations,  $T_{max}$  is the maximum number of iterations,  $p$  and  $r$  are random numbers,

Searching for prey ( $p < 0.5$  and  $|A_1| \geq 1$ ):

$$X_{i,t+1} = X_{rand,t} - A_1 \cdot D \tag{18}$$

$$D = |C \cdot X_{rand,t} - X_{i,t}| \tag{19}$$

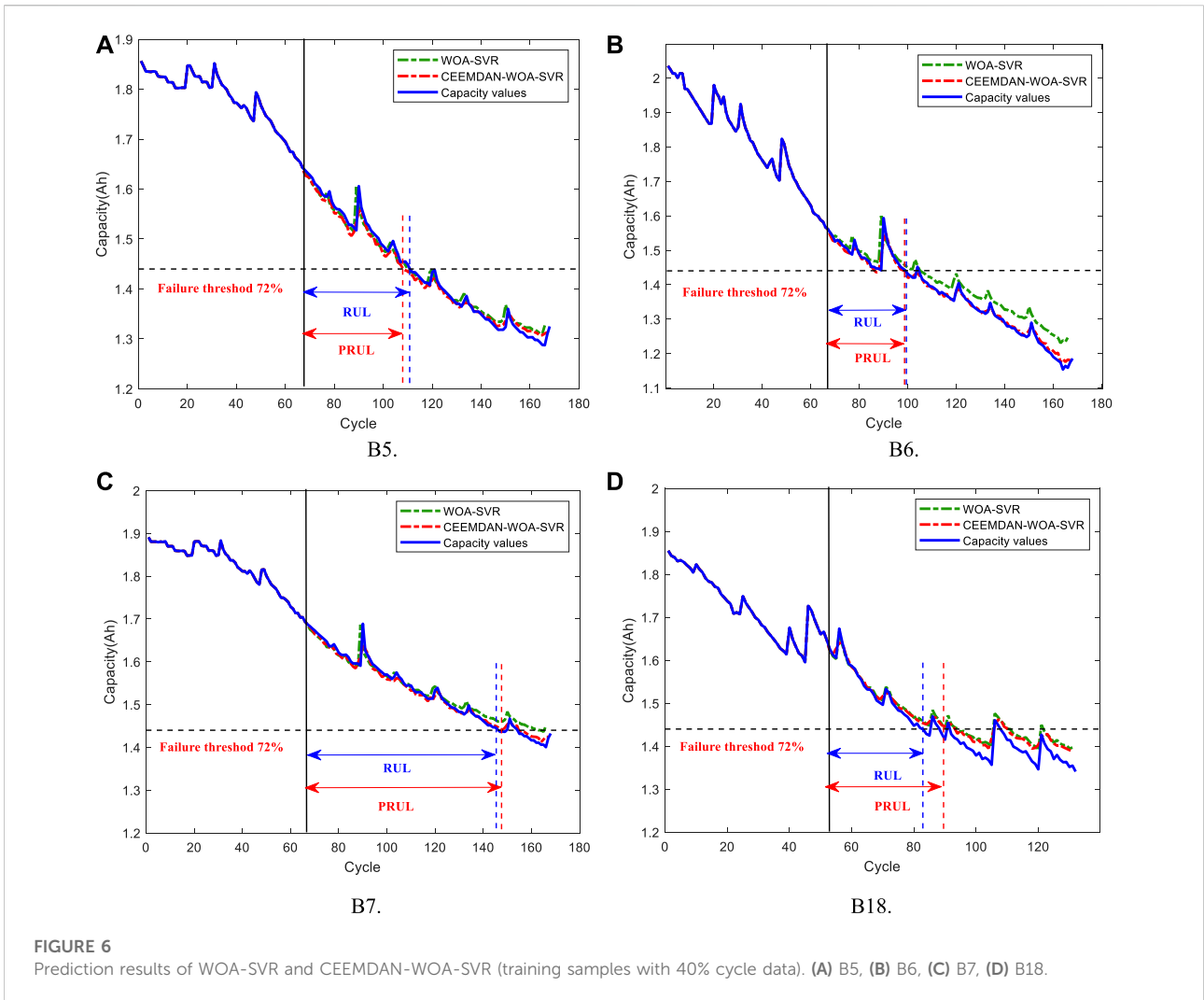
where  $X_{rand,t}$  represents a random solution in the current generation.

Spiral update of position ( $p \geq 0.5$ ):

$$X_{i,t+1} = X_{i,t} + D_p \cdot e^{bl} \cdot \cos(2\pi l) \tag{20}$$

$$D_p = |X_{best} - X_{i,t}| \tag{21}$$

where  $b$  indicates a constant, and  $l$  represents a random number in  $[-1,1]$ .



### 3 Remaining useful life prediction for lithium batteries based on complete ensemble empirical mode decomposition with adaptive noise and whale optimization algorithm-support vector regression methods

#### 3.1 Whale optimization algorithm-support vector regression model

In the SVR model, the penalty factor  $C$  and kernel function parameter  $\sigma$  are critical parameters, and they have a direct impact on the performance of the SVR model. Thus, the WOA is used to optimize the kernel parameters of the SVR model. The flowchart of the WOA-SVR method is shown in Figure 1, and the detailed process is described as follows:

Step 1: The parameters setting.

Before the prediction method execution, the population number  $N_p$ , dimension of variables  $D_m$ , the maximum iteration number  $T$ , the optimal range of  $C$ , and the optimal range of  $\sigma$  are set.

Step 2: Data preprocessing.

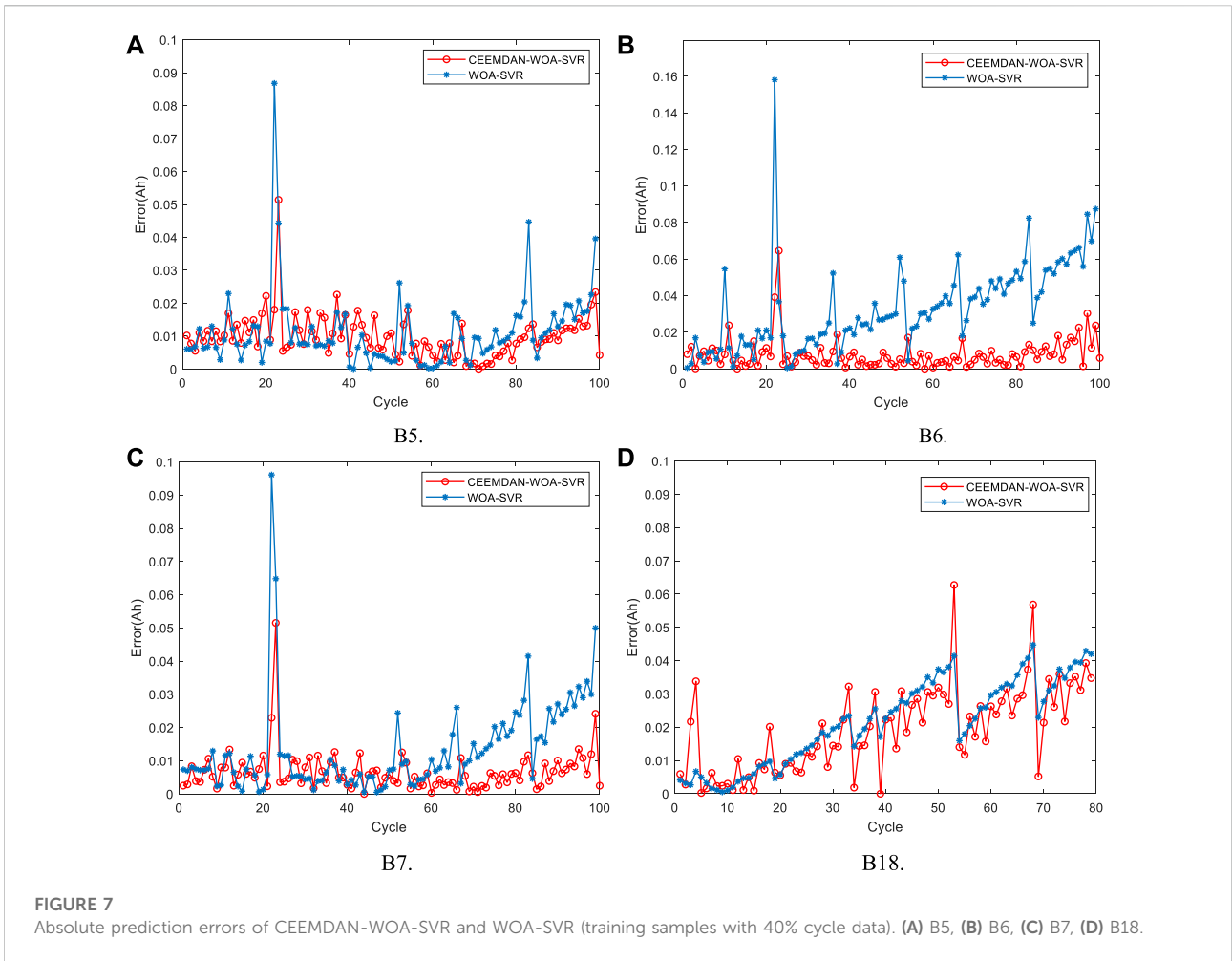
In this step, the battery capacity datasets are normalized, and the capacity values are mapped in the range  $[-1, 1]$  with Eq. 22. The preprocessed data is divided into two parts, one part is training data and the other part is testing data.

$$x_i = 2 \times \frac{x_i - x_{\min}}{x_{\max} - x_{\min}} - 1 \tag{22}$$

where  $x_i$  represents the  $i$ -th battery capacity value,  $x_{\max}$  represents the maximum value of battery capacity, and  $x_{\min}$  represents the minimum value of battery capacity.

Step 3: Setting the fitness function.

The fitness function is established with the mean square error (MSE) between the actual and predicted value, which can be expressed as:



$$MSE = \frac{1}{n} \sum_{i=1}^n (\hat{y}_i - y_i)^2 \quad (23)$$

where  $\hat{y}_i$  and  $y_i$  represent the predicted value and the actual value at the  $i$ -th cycle, respectively.  $n$  indicates the cycle time.

Step 4: Optimizing the kernel parameters of the SVR.

According to the search process of the WOA, the parameters of the SVR are selected in the solution space.

Step 5: The RUL prediction of LIBs: The RUL prediction accuracy of the WOA-SVR model is validated by the testing data.

### 3.2 The remaining useful life prediction of lithium-ion batterie based on CEEMDAN-GWO-SVR

To improve prediction accuracy, the CEEMDAN is firstly used to perform noise reduction in battery capacity series. Figure 2 shows the flowchart of RUL prediction based on

CEEMDAN-WOA-SVR, and the detailed steps are introduced as follows:

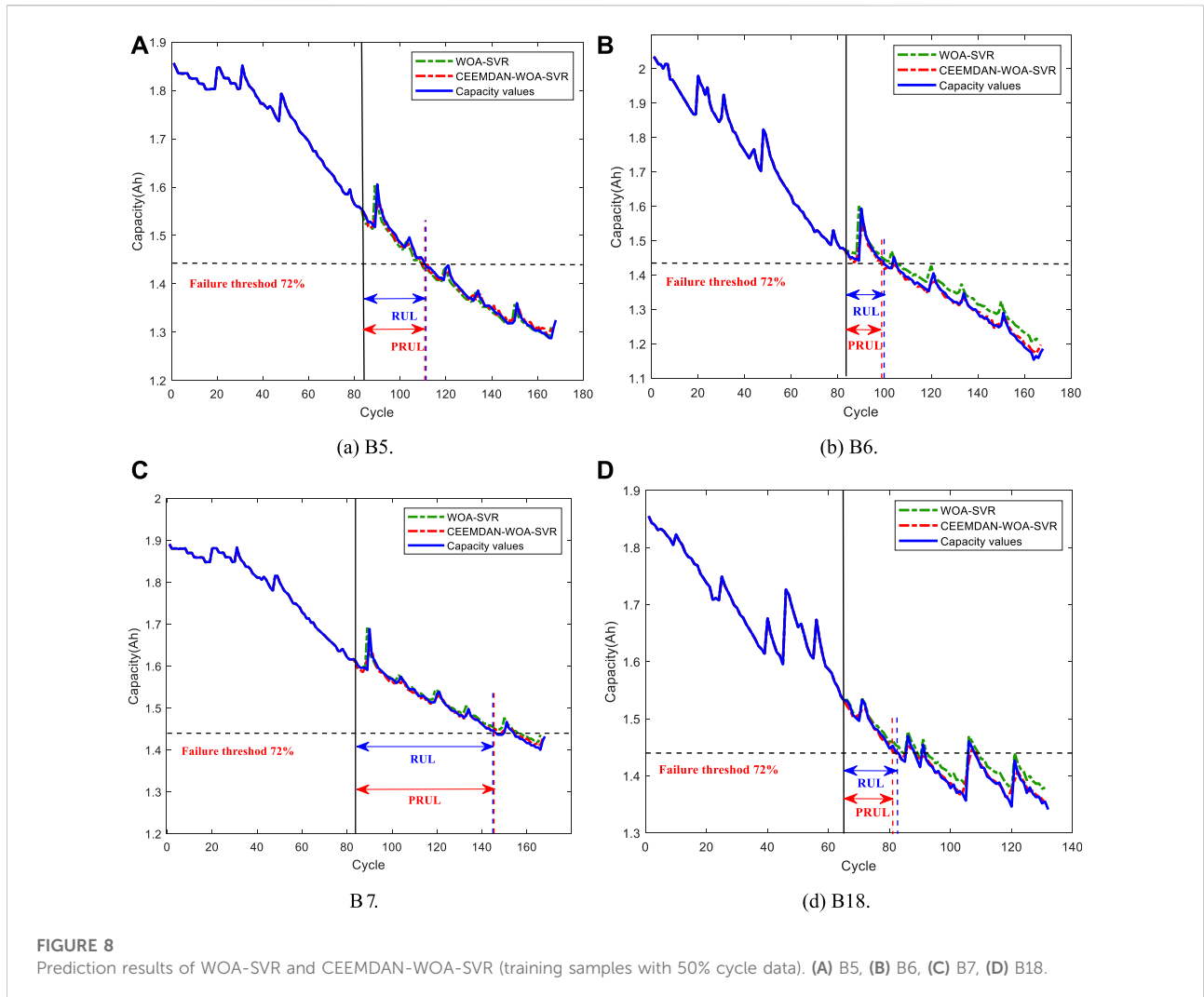
Step 1: Getting the capacity data.

Step 2: Decomposition of capability degradation series into  $IMF_i$  ( $i = 1, 2, \dots, n$ ) and a residual by applying CEEMDAN.

Step 3: To represent the correlation between each  $IMF_i$  component and the original signal, the correlation coefficient is utilized and expressed as Eq. 24. The sensitive IMF components are selected when the correlation coefficient is more than the threshold value.

$$C_i = \frac{\sum_{t=1}^{N-1} IMF_i(t)x(t)}{\sqrt{\sum_{i=1}^{N-1} [IMF_i(t)]^2 \sum_{i=1}^{N-1} [x(t)]^2}} \quad (24)$$

where  $C_i$  denotes the correlation coefficient of the  $i$ -th modal component with the original signal,  $IMF_i(t)$  represents the  $i$ -th modal component,  $x(t)$  represents the original signal sequence value, and  $N$  denotes the length of the time series.



Step 4: The battery capacity sequence is reconstructed according to the selected IMF components and the residual. A WOA-SVR model is constructed for the reconstruction sequence.

Step 5: Obtaining the prediction of RUL.

## 4 Performance evaluation and analysis

### 4.1 Capacity degradation dataset of lithium-ion batterie

In this section, the public battery datasets provided by the NASA Prognostics Center of Excellence (Goebel et al., 2008) are employed to verify the accuracy and validity of the proposed method. These data were obtained from charge and discharge tests at room temperature (24°C) using 18650 LIBs with a capacity of 2 Ah. In the datasets, there are many parameters

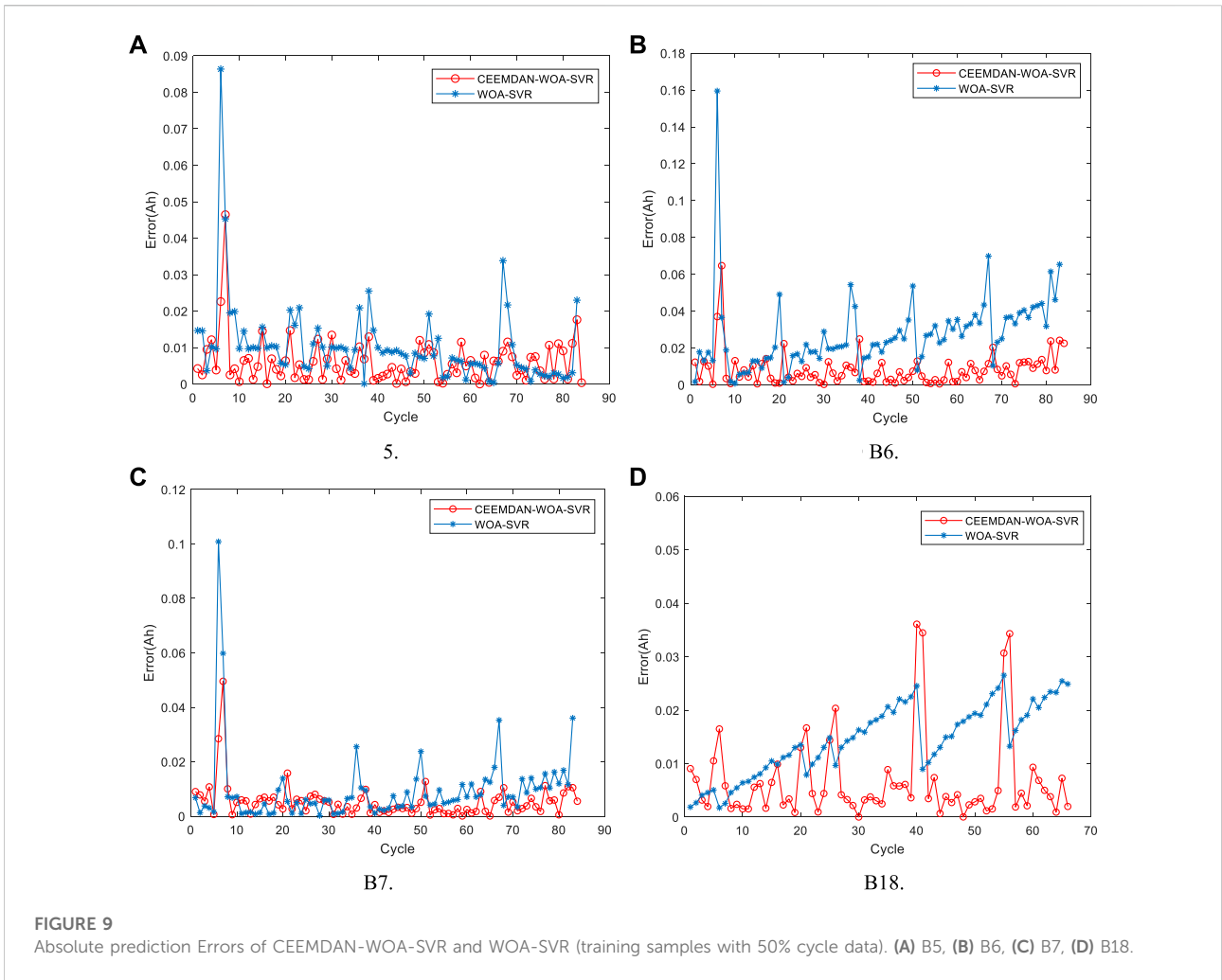
such as voltage, current, and capacity. Because the change in battery capacity directly indicates the degree of battery degradation, the capacity can be applied to the RUL prediction of LIBs. The capacity degradation curves of B5, B6, B7, and B18 are shown in Figure 3.

Generally, it is considered that the EOL of a battery is reached when the capacity degrades by 30%. In the experiment, the cyclic testing of battery charging and discharging test was terminated when the battery degraded to the EOL. However, for battery B7 degradation at 30%, it does not drop to the EOL, so this study resets the failure threshold of the battery, which is set to 72% of the rated battery capacity (1.44 Ah).

### 4.2 Evaluation criterion

To assess the proposed method's performance, the mean absolute error (MAE) and the root mean square error (RMSE) are





selected as the evaluation criteria, denoted as (Wang and Mamo, 2018):

$$MAE = \frac{1}{n} \sum_{i=1}^n |\hat{y}_i - y_i| \quad (25)$$

$$RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^n |\hat{y}_i - y_i|^2} \quad (26)$$

where  $\hat{y}_i$  and  $y_i$  represent the  $i$ -th predicted and the actual capacity value, respectively.  $n$  indicates the estimated number.  $MAE$  is the average error of all prediction results.  $RMSE$  is the root mean square of all prediction errors. However,  $MAE$  and  $RMSE$  are applied to reflect the accuracy of the predicted method.

### 4.3 Noise reduction of lithium-ion batterie capacity sequences

The capacity decay curves of LIBs can be seen that there is a decreasing trend with the charging and discharging cycles, but in some

cycles, the capacity of LIB has a fast and short rise, mainly due to random noise disturbance. To reduce the impact of noise, the capacity data need to be processed for noise reduction before the RUL prediction.

In this paper, the noise reduction process on capacity data is performed using CEEMDAN, and the sensitive IMF components are selected when the threshold value is more than 0.05. In this section, B5 capacity data is chosen to prove the efficacy of the CEEMDAN. Figure 4 shows the decomposition results of EMD and CEEMDAN. The B5 capacity after noise reduction by the EMD and CEEMDAN methods is shown in Figure 5. As can be seen from Figure 5, CEEMDAN can effectively reduce the noise of the capacity data, and the noise reduction effect of CEEMDAN is closer to the original data compared with the EMD method.

### 4.4 Simulation results analysis

To verify the prediction performance of the proposed method, 40% (prediction start: 68, 68, 68, and 53) and 50%

TABLE 2 The RUL prediction results of WOA-SVR and CEEMDAN-WOA-SVR methods.

Battery	Prediction start	RUL	WOA-SVR			CEEMDAN-WOA-SVR		
			PRUL	$E_r$	$pE_r(\%)$	PRUL	$E_r$	$pE_r(\%)$
B5	68	43	42	1	2.3	40	3	7.0
	84	27	25	2	7.4	26	1	3.7
B6	68	31	37	6	19.4	30	1	3.2
	84	15	21	6	40	15	0	0
B7	68	78	96	18	23.1	80	2	2.6
	84	62	71	9	14.5	63	1	1.6
B18	53	30	37	7	23.0	36	6	20
	66	17	18	1	5.9	16	1	5.9

TABLE 3 Results of WOA-SVR and CEEMDAN-WOA-SVR methods for RUL prediction.

Battery	Prediction start	WOA-SVR		CEEMDAN-WOA-SVR	
		MAE	RMSE	MAE	RMSE
B5	68	0.0111	0.0158	0.0100	0.0120
	84	0.0104	0.0154	0.0061	0.0088
B6	68	0.0328	0.0407	0.0079	0.0118
	84	0.0270	0.0341	0.0084	0.0124
B7	68	0.0132	0.0192	0.0066	0.0090
	84	0.0094	0.0164	0.0054	0.0084
B18	53	0.0214	0.0250	0.0192	0.0232
	66	0.0145	0.0160	0.0067	0.0105

(prediction start: 84, 84, 84, and 66) of the total cycle data were used as training samples for prediction with the WOA-SVR method, respectively. The parameters of the WOA are set in Table 1. The prediction results are shown in Figures 6–9, Tables 2, 3.

When the capacity failure threshold of the LIB is reached, the errors between the predicted remaining useful life (PRUL) and the RUL are calculated as:

$$E_r = |PRUL - RUL| \tag{27}$$

$$pE_r = \frac{|PRUL - RUL|}{RUL} \times 100\% \tag{28}$$

$E_r$  is used to reflect the predicted error of RUL, and  $pE_r$  is applied to assess the accuracy of RUL prediction.

In Figures 6, 8; Table 2, the  $E_r$  and  $pE_r$  of the CEEMDAN-WOA-SVR method are less than the WOA-SVR method except for B5 (start = 68). Take the B7 battery as an example (start = 68), the  $E_r$  and  $pE_r$  of the WOA-SVR method are 18 and 23.1% respectively, whereas, the  $E_r$  and  $pE_r$  of the CEEMDAN-WOA-

SVR method are 2 and 2.6% respectively. Compared with the WOA-SVR method, the  $E_r$  and  $pE_r$  of the CEEMDAN-WOA-SVR method are reduced by 89%.

From Figures 7, 9; Table 3, it can be seen that MAEs and RMSEs of the CEEMDAN-WOA-SVR method are less than the WOA-SVR method. For example, when the prediction start number is 84 for the B6 battery, the MAE and RMSE of the WOA-SVR are 0.027 and 0.0341 respectively, whereas, the MAE and RMSE of the CEEMDAN-WOA-SVR are 0.0084 and 0.0124 respectively. Compared with the WOA-SVR method, the MAE of the CEEMDAN-WOA-SVR method is reduced by 69%, and the RMSE is reduced by 64%. Therefore, the accuracy of RUL prediction with the CEEMDAN-WOA-SVR method is better than the WOA-SVR method.

To further verify the effectiveness of the proposed method, the proposed method is compared with the methods in the literature under the same conditions. Wang et al. (2019) proposed an ABC-SVR method to predict the RUL, they employed ABC algorithm to select the kernel parameters of the SVR model. Yang et al. (2021)

TABLE 4 The RUL prediction results of CEEMDAN-WOA-SVR and other methods.

Battery	Method	Prediction start	RUL	PRUL	$E_r$	$pE_r$ (%)	MAE	RMSE
B5	ABC-SVR	68	43	43	0	0	0.0071	0.0132
		84	27	27	0	0	0.0072	0.0139
	EEMD-GWIO-SVR	68	43	46	3	6.9	0.0096	0.0113
		84	27	26	1	3.7	0.0076	0.0096
	CEEMDAN-WOA-SVR	68	43	40	3	7.0	0.0100	0.0120
		84	27	26	1	3.7	0.0061	0.0088
B6	ABC-SVR	68	31	38	7	22.6	0.0418	0.0463
		84	15	19	4	2.6	0.0313	0.0353
	EEMD-GWIO-SVR	68	31	32	1	3.2	0.0075	0.0096
		84	15	18	3	20	0.0121	0.0156
	CEEMDAN-WOA-SVR	68	31	30	1	3.2	0.0079	0.0118
		84	15	15	0	0	0.0084	0.0124
B7	ABC-SVR	68	78	80	2	2.6	0.0075	0.0144
		84	62	64	2	3.2	0.0080	0.0151
	EEMD-GWIO-SVR	68	78	80	2	2.6	0.0131	0.0150
		84	62	60	2	3.2	0.0096	0.0113
	CEEMDAN-WOA-SVR	68	78	80	2	2.6	0.0066	0.0090
		84	62	63	1	1.6	0.0054	0.0084
B18	ABC-SVR	53	30	30	0	0	0.0302	0.0332
		66	17	17	0	0	0.0104	0.0194
	EEMD-GWIO-SVR	53	30	38	8	26.7	0.0101	0.0127
		66	17	15	2	11.8	0.0113	0.0134
	CEEMDAN-WOA-SVR	53	30	36	6	20	0.0192	0.0232
		66	17	16	1	5.9	0.0067	0.0105

presented a hybrid model based on EEMD, GWO, and SVR to predict the RUL, they used EEMD to extract the degradation trend of battery capacity and employed the GWO algorithm to search the parameters of the SVR method. Table 4 lists the detailed comparison results of the CEEMDAN-WOA-SVR method and the two methods.

From Table 4, it is apparent that the prediction errors of the proposed method are also less than those of the existing methods in the literature. Take the B7 battery as an example (start = 84), the  $E_r$ ,  $pE_r$ , MAE, and RMSE of the EEMD-GWO-SVR method are 1, 1.6%, 0.0054, and 0.0084, respectively. Compared with the two methods, the prediction errors of the proposed method are smaller.

Based on the above discussion, it can be concluded that the CEEMDAN method reduces the influence of noise on the prediction, and the CEEMDAN-WOA-SVR method could effectively improve the RUL prediction accuracy of LIBs.

## 5 Conclusion

The accurate RUL prediction of LIB is a critical technology for battery health management, which ensures the safe, stable, and efficient operation of the battery. In this study, a new method

for the RUL prediction of lithium-ion batteries is proposed, which is combined with the CEEMDAN, WOA, and SVR methods. First, the battery capacity data is processed by CEEMDAN to reduce the impact of noise on the data sequence. Then, the WOA is applied to the SVR model for solving the parameter selection problem. Finally, a new method based on CEEMDAN and WOA-SVR is used for the RUL prediction of LIBs. To verify the efficacy of the CEEMDAN-WOA-SVR method, simulation experiments of LIBs RUL prediction using the WOA-SVR and CEEMDAN-WOA-SVR methods are performed. The results show that the  $E_r$  and  $pE_r$  of CEEMDAN-WOA-SVR method are less than the WOA-SVR method, and MAEs and RMSEs of the proposed method are less than the WOA-SVR method. As a result, the noise of the capacity sequence is reduced by CEEMDAN, which effectively improves the prediction performance. In addition, the prediction experiments are performed using the ABC-SVR and EEMD-GWO-SVR methods, and the results indicate that the errors of the CEEMDAN-WOA-SVR method are also smaller than the ABC-SVR method and EEMD-GWO-SVR method. Therefore, the CEEMDAN-WOA-SVR method is an effective tool for the RUL prediction of LIBs.

In this study, the MAE and RMSE are used to demonstrate the effectiveness of the CEEMDAN-WOA-SVR method. Compared with other SVR-based methods, the predicted results of the proposed method do not appear to be significantly improved. In future work, we will use other prognostics metrics, such as the accuracy index, alpha-lambda, and precision index, to verify the method's performance. In addition, we will calculate the lower and upper bounds of the RUL prediction and compare them with the threshold value to achieve the prediction of the RUL.

## Data availability statement

Publicly available datasets were analyzed in this study. This data can be found here: The datasets provided by the NASA Prognostics Center of Excellence.

## Author contributions

XM: methodology, conceptualization, and writing. CC: conceptualization and data curation. YW: conceptualization and editing. QW: software. LT: validation.

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## Conflict of interest

The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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## Nomenclature

### Variables

**$b$**  constant number  
 **$b_c$**  intercept parameter  
 **$C$**  penalty parameter  
 **$C_i$**   $i$ -th correlation coefficient  
 **$D_m$**  variable dimension  
 **$E_r$**  absolute predicted error of RUL  
 **$f(x)$**  regression function  
 **$I$**  decomposition time  
 **$IMF_i(t)$**   $i$ -th modal component  
 **$K(x_i, x)$**  kernel function  
 **$l, p, r$**  random numbers  
 **$n$**  cycle time number  
 **$N$**  length of the time series  
 **$NP$**  population number  
 **$pE_r$**  relative prediction error of RUL  
 **$r_1(n)$**  first residual sequence  
 **$r_k(n)$**   $k$ -th residue sequence  
 **$R(n)$**  residual sequence  
 **$s(n)$**  original signal sequence  
 **$t$**  current number of iteration  
 **$T_{max}$**  maximum number of iteration  
 **$v(n)$**  Gaussian white noise  
 **$x_i$**   $i$ -th battery capacity value  
 **$x_{max}$**  maximum value of battery capacity  
 **$x_{min}$**  minimum value of battery capacity  
 **$X_{i,t}$**  solution in the current generation  
 **$X_{i,t+1}$**  solution in the next generation  
 **$X_{best}$**  best solution in the current generation  
 **$X_{rand,t}$**  random solution in the current generation

**$x(t)$**  original signal sequence value  
 **$\hat{y}_i$**  predicted value at the  $i$ -th cycle  
 **$y_i$**  actual value at the  $i$ -th cycle  
 **$\varphi(x)$**  transfer function  
 **$\omega$**  weight parameter  
 **$\xi_i, \xi_i^*$**  slack variables  
 **$\varepsilon$**  boundary value  
 **$\sigma$**  kernel parameter  
 **$\alpha_i, \alpha_i^*$**  Lagrange multipliers

### Abbreviations

**ABC** artificial bee colony  
**ANN** artificial neural network  
**CEEMDAN** complete ensemble empirical mode decomposition with adaptive noise  
**CNN** convolutional neural networks  
**EEMD** ensemble empirical mode decomposition  
**EMD** empirical mode decomposition  
**EOL** end of life  
**GWO** gray wolf optimization  
**IMF** intrinsic mode function  
**LIB** lithium-ion battery  
**MAE** mean absolute error  
**MSE** mean square error  
**PF** particle filtering  
**PRUL** predicted remaining useful life  
**RMSE** root mean square error  
**RUL** remaining useful life  
**SVM** support vector machine  
**SVR** support vector regression  
**WOA** whale optimization algorithm