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# [PV array recon](https://www.frontiersin.org/articles/10.3389/fenrg.2022.971628/full)figuration with [electrical energy storage system](https://www.frontiersin.org/articles/10.3389/fenrg.2022.971628/full) [for power system frequency](https://www.frontiersin.org/articles/10.3389/fenrg.2022.971628/full) [regulation](https://www.frontiersin.org/articles/10.3389/fenrg.2022.971628/full)

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In this work, a novel PV station participating FR technique based on PV array reconfiguration and battery energy storage system (BESS) is put forward. Through the PV array reconfiguration under Partial shading condition, photovoltaic (PV) system can adjust the output power according to the power dispatch instruction. And with the help of BESS, The PV station can achieve continuous power output. Specifically, a joint PV energy storage system model combining profit maximization and power deviation minimization is established. In order to two conflicting goals simultaneously, multi-objective golden eagle optimizer and improved ideal point decision making method are applied. And Lagrange function is given to determine the weight coefficients of each objective more fairly. Two cases are designed and tested. In the high frequency response simulation test, the profit is increased by 8.4% and the power deviation from FR signal is decreased by 19.98%; meanwhile the profit is increased by 10.07% and power deviation is decreased by 67.69% in the low frequency response test. Therefore, the simulation results verify that the proposed method contributes to the frequency response of PV station.

#### KEYWORDS

PV array reconfiguration, battery energy storage system, frequency regulation, multiobjective golden eagle optimizer, optimizing operation

# Introduction

With the increasing severity of environmental problems and the consumption of fossil fuels, solar energy has become one of the most widely used renewable energy sources due to its huge reserves, clean and environmentally friendly [\(Yang et al., 2021\)](#page-10-0). Driven by the national strategy of "carbon neutral, emission peak", the proportion of Photovoltaic (PV) power generation in the power system will continue to grow [\(Yang et al., 2021](#page-10-0)) [\(Kaushika](#page-10-1) [and Gautam, 2003](#page-10-1)). In the context of high proportion of renewable energy in new power system, the traditional frequency regulation (FR) control means are stretched, as a result PV system participating in power grid FR is inevitable ([Sai Krishna and Moger, 2019\)](#page-10-2). Therefore, the research on the FR strategy based on PV reconfiguration coordinated with energy storage carried out in this work has important value for the frequency safety of the new power system.

Partial shading condition (PSC) [\(Laudani et al., 2018](#page-10-3)), ([Ajmal et al., 2020](#page-10-4)) is one of the most common environmental factors which effecting the PV power generation efficiency and maximum power point tracking (MPPT) efficiency. Changing the connection topology of PV modules can equivalently disperse the originally concentrated shadows to the entire array, so as to reduce the influence of PSC and improve the output power ([Rani et al., 2013\)](#page-10-5). In recent years, researchers have developed a variety of PV array reconfiguration methods, mainly divided into two categories: static and dynamic.

The literature ([NamaniRakesh and Madhavaram, 2016](#page-10-6)) studies the performance of three different topologies (parallel, total-cross-tied (TCT) and bridge structure) of PV array in PSC proposes that TCT topology extract the maximum power of the array. Sudoku scheme is used to reconfigures PV modules in literature (Horoufi[any and Ghandehari, 2018](#page-10-7)). Literature ([Shams](#page-10-8) [El-Dein et al., 2013\)](#page-10-8) introduces mathematical formulas based on mixed integer quadratic programming to disperse the shadow of TCT-connected PV arrays. In addition, static technique is a onetime reconfiguration method which can hardly settle timevarying shadow.

However, dynamic reconfiguration can adjust the switch matrix in real time according to the shadow change, so as to achieve the purpose of dynamically changing the electrical topological structure of the array [\(Deshkar et al., 2015](#page-10-9)), ([Balraj and Stonier, 2020](#page-10-10)). The literature ([Sanseverino et al.,](#page-10-11) [2015\)](#page-10-11) proposes a PV array reconfiguration method based on knapsack problem, and uses additional unshaded PV components to compensate for components that are heavily shaded. In recent years, the application of meta-heuristic algorithms to PV array reconfiguration has become a new trend, such as genetic algorithm ([Deshkar et al., 2015](#page-10-9)), particle swarm optimization ([Babu et al., 2018](#page-10-12)), and grasshopper optimization algorithms ([Fathy, 2018\)](#page-10-13), butterfly optimization algorithm [\(Fathy, 2020\)](#page-10-14) and artificial ecological optimization algorithm ([Yousri et al., 2020a\)](#page-10-15).

None of the current PV reconfiguration studies have taken the application of PV reconfiguration techniques to grid frequency regulation into account ([Zhang et al., 2021](#page-10-16)), so this work proposes a PV array reconfiguration of grid frequency regulation strategy based on multi-objective golden eagle optimizer (MOGEO) ([Mohammadi-Balani et al., 2021](#page-10-17)) which has strong global exploration ability and optimization stability. At the same time, the battery energy storage system (BESS) is introduced to coordinate the PV system so that the reconfiguration can achieve linear continuity response to FR instructions [\(Yousri](#page-10-18) [et al., 2020b\)](#page-10-18) ([González-Castaño et al., 2021](#page-10-19)).

From the view of PV power station, the PV system and BESS are considered to participate frequency regulation at the same time, to provide ancillary services ([Krishnan et al., 2020\)](#page-10-20), ([Bi et al.,](#page-10-21) [2020\)](#page-10-21). According to the electric price, operation cost, the PV array reconfiguration optimization economic model is established to determine the required energy storage power, power generation

planning and charging and discharging strategy of PV power plant under different shadows and frequency regulation capacity, so as to maximize the joint PV energy storage system. Leave out the dynamic interaction with the system frequency, the system frequency is regarded as the known input of the model, so the final model can be solved by heuristic algorithm.

# Design of multi-objective golden eagle optimizer

### Spiral movement and prey selection

Each golden eagle can remember its best prey and cruises around its own prey or others' preys. Prey selection strategies play an important role in MOGEO. For the sake of enhancing the exploration efficiency of agents, a one-to-one mapping program is proposed in MOGEO so that each prey can be randomly assigned to only one golden eagle. And then every golden eagle cruises and attacks the chosen prey. And the schematic diagram of one-to-one mapping program is shown in [Figure 1.](#page-2-0)

### Exploitation and exploration

<span id="page-1-0"></span>The golden eagle's attack behavior can be viewed as a vector. The starting point of this vector is the current position of the golden eagle and the destination is the prey. So, the attack vector which emphasizes the development stage in MOGEO of agent  $i$ can be modeled by [Formula \(1\)](#page-1-0).

$$
\vec{A}_i = \vec{X}_f^* - \vec{X}_i \tag{1}
$$

where,  $\vec{X}_{f}^{*}$  denotes the position of prey; and  $\vec{X}_{i}$  represents the position of the eagle  $i$  in current iteration.

<span id="page-1-1"></span>The speed direction of cruising vector is perpendicular to the attack vector. The cruising vector can be obtained only when the equation of the tangent hyperplane is calculated. Hence the expression of the n-dimensional hyperplane can be calculated by [Eq. 2](#page-1-1).

$$
h_1x_1 + h_2x_2 + \dots + h_nx_n = d \Rightarrow \sum_{j=1}^n h_jx_j = d
$$
 (2)

The steps of golden eagle randomly seeking the destination position C located on a n-dimensional cruising hyperplane are as follows:

Step 1 A variable is randomly selected to assigned as the fixed variable from whole variable set other than whose corresponding attack vector is 0.

Step 2 Except for the pth variable whose value is fixed, appoints random figures to all variables.

<span id="page-1-2"></span>Step 3 Use [Eq. 3](#page-1-2) to acquire the value of the fixed parameter.

$$
c_k = \frac{d - \sum_{i,j \neq p} a_j}{a_p} \tag{3}
$$



<span id="page-2-0"></span>where,  $c_k$  is the pth member of destination position C;  $a_i$  denotes the *j*th member in the vector set  $\vec{A}_i$ ; *d* represents the distance.

# Updating of location

<span id="page-2-2"></span>The position movement of the golden eagle consists of two parts, attack and cruise, which affect and restrict each other, as shown in the following equation.

$$
\begin{cases} \Delta x_i = r_1 p_a \frac{\vec{A}_i}{\|\vec{A}_i\|} + r_2 p_c \frac{\vec{C}_i}{\|\vec{C}_i\|} \\ x(t+1) = x(t) + \Delta x_i(t) \end{cases}
$$
(4)

where,  $p_a$  and  $p_c$  are attack and cruise coefficient respectively, whose computing method can refer to original MOGEO research paper; these two coefficients adjust the attack or cruise tendency of golden eagle;  $r_1$  and  $r_1$  are random vectors, respectively; and  $\vec{A}_i$ represents the attack vector;  $\vec{C}_i$  indicates cruising vector;  $x(t + 1)$ denotes the position of agent in the  $(t + 1)$  iteration.

When the new position of the golden eagle is better than the original position, the original position is replaced by the new coordinates; Instead, keep the original position. In the next iteration, compute the new attack vector and cruise vector, and move to the new position. Iteration is not stopped until the loop termination condition is met.

### Mathematical modeling of combined photovoltaic energy storage system revenue

### Modeling of total-cross-tied structure photovoltaic arrays

Many individual PV cells form a PV module, and multiple PV modules form a PV array by series and parallel connection,



<span id="page-2-1"></span>and correspondingly, multiple PV arrays can form a PV system. For ease of study, the PV cell can be seen as a current generator. According to the general model of PV cell, the current of PV cell can be expressed as below:

$$
I_{\text{cell}} = I_{\text{Light}} - I_{\text{d}} - I_{\text{sh}} \tag{5}
$$

where  $I_{cell}$  represents the output current of the PV cell,  $I_{Lieht}$ denotes the photo-generated current;  $I_d$  is the current of diode;  $I_p$ represents the current of parallel resistance.

Since the TCT topology is less affected by shadows under PSC, the output power is more stable, which is widely used in the <span id="page-3-0"></span>study of PV arrays. A  $10 \times 10$  scale TCT structured PV array is shown in [Figure 2](#page-2-1), each of which is connected in parallel by 9 PV modules, and then such 9 lines are connected in series by Kirchhoff's voltage law (KVL) and KCL provide output voltage and current for the entire PV array:

$$
V_{\rm D} = \sum_{p=1}^{10} V_{\rm ap} \tag{6}
$$

<span id="page-3-1"></span>
$$
I_{\rm D} = \sum_{q=0}^{10} \left( I_{pq} - I_{(p+1)q} \right) = 0, \ p = 0, 1, 2, \dots, 9 \tag{7}
$$

where  $V_D$  is the output voltage of the array,  $V_{ab}$  represents the row voltage of pth row, and  $I_D$  means the total output current,  $I_{pq}$ indicates the output current of the PV module in  $q$ th column and pth row.

### **Constraints**

#### 1) Constraints of battery.

In order to ensure the safe operation and life of the battery, it is necessary to constrain its charge and discharge power and the remaining capacity of the battery, as shown below:

$$
P_{\rm bess}^{\rm min} \le P_{\rm bess}(t) \le P_{\rm bess}^{\rm max}, \ t \in T \tag{8}
$$

$$
SOC_{\rm bess}^{\rm min} \cdot E_{\rm bess} \le E_{\rm bess}(t) \le SOC_{\rm bess}^{\rm max} \cdot E_{\rm bess}, t \in T \tag{9}
$$

$$
SOC_{\rm bess}(t) = \begin{cases} SOC_{\rm bess}(t-1) + P_{\rm bess}(t) \cdot \Delta t \cdot \eta_{\rm ch} / E_{\rm bess}, \text{if } P_{\rm bess}(t) \ge 0\\ SOC_{\rm bess}(t-1) + P_{\rm bess}(t) \cdot \Delta t / (\eta_{\rm dis} \cdot E_{\rm bess}), \text{ otherwise} \end{cases} \tag{10}
$$

Where,  $P_{\rm{bess}}^{\rm{max}}, P_{\rm{bess}}^{\rm{min}}$  are the maximum and minimum charging power of BESS, respectively.  $SOC_{\rm bess}^{\rm max}$  and  $SOC_{\rm bess}^{\rm min}$  severally represent the maximum and minimum state of charge (SOC) of BESS;  $\eta_{ch}$  and  $\eta_{\text{dis}}$  are the charging and discharging efficiency;  $\Delta t$  denotes the control period; and Ebess means the rated capacity of BESS.

#### 2) Balance constraint of frequency regulation power.

The power responded to high frequency and low frequency from joint PV energy storage system is provided by PV array and energy storage systems together, which can be expressed as follows:

$$
P_{\rm fr}^+(t) = PV_{\rm fr}^+(t) + E_{\rm b,fr}^+(t) / \eta_{\rm ch}
$$
 (11)

$$
P_{\rm fr}^-(t) = PV_{\rm fr}^-(t) + E_{\rm b,fr}^-(t) / \eta_{\rm dis}
$$
 (12)

where,  $PV_{\text{fr}}^{+}(t)$  and  $PV_{\text{fr}}^{-}(t)$  are the decreased power generation for higher system frequency and the increased power generation for lower system frequency; the sum of  $P_{\text{fr}}^{+}(t)$  and  $P_{\text{fr}}^{-}(t)$  is the total frequency regulation power.

#### 3) Full response constraint of frequency regulation power.

As the frequency response is the mandatory auxiliary service of the power system, the frequency regulation power provided by combined PV energy storage system must be satisfied with the frequency regulation capacity calculated according to the gridconnection guidelines requirements.

$$
P_{\text{fr}}\left(t\right) = P_{\text{req}}\left(t\right) \tag{13}
$$

where,  $P_{\text{req}}(t)$  is the required frequency modulation capacity calculated by the grid-connected guidelines in time period t, which is related to the percentage of the current output in the installed PV power station.

#### 4) Constraints of PV power sale.

$$
P_{\rm g}(t) = P_{\rm pv}(t) - P_{\rm fr}^+(t) + P_{\rm fr}^-(t) \tag{14}
$$

where,  $P_g(t)$  is power sale quantity in electric quantity market;  $P_{\text{pv}}(t)$  denotes the maximum power generation of PV array which id depending on the sunlight conditions. This constraint reflects that in the power market, the electricity sale in the conventional market and the frequency regulation electricity participating in the auxiliary service are calculated separately.

### Objective function

In order to increase the power generation income of the PV storage power station and make the power response to the FM signal at the same time, two conflicting goals are considered in this paper, the first goal is to minimize the average power deviation between the power output of the PV array coordinated energy storage battery and the FR signal  $f_1$ . The second is to maximize the power generation revenue of the PV storage power station  $f_2$ , which is equivalent to the difference between the electricity sales revenue of PV power generation and the operating cost of energy storage batteries. In the electric power market, the electric quantity market and the auxiliary service market are generally separated, so the two parts of electric quantity are charged separately in calculation, and both of them are regarded as the income of the optical storage combined system in the market. In summary, the objective function proposed in this article can be defined as follows:

$$
\begin{cases}\n\min f_1 = \frac{1}{T} \sum_{t \in T} \left| P_{\text{FR}}(t) - \left[ P_{\text{pv}}(t) - P_{\text{bess}}(t) \right] \right| \\
\max f_2 = \lambda_1 \cdot \sum_{t \in T} \left[ P_{\text{pv}}(t) - P_{\text{bess}}(t) \right] + C_{\text{p}} + M_{\text{p}} - C_{\text{bess}}\n\end{cases} \tag{15}
$$

Where,  $T(\Delta T)$  represents the response to the FM time,  $P_{\text{bess}}(t)$  is the charging power of energy storage,  $\lambda_1$  is the conventional electricity price,  $C_p$  means the FM capacity compensation income,  $M<sub>p</sub>$  indicates the FM mileage compensation income, C<sub>bess</sub> denotes the cost of energy storage batteries.

$$
C_{\rm p} = \lambda_2 C \cdot A \tag{16}
$$

where,  $\lambda_2$  represents the capacity compensation standard; A is the AGC operation performance index, assigned 1; C means the

<span id="page-4-0"></span>limited range capacity that the AGC can automatically adjust within 5 min during dispatch period, of which the upper limit is assigned the predicted output of the PV storage power station, and the lower limit is assigned 60% of the installed capacity of PV station.

$$
M_{\rm p} = \lambda_3 \sum_{t \in T} \left[ P(t+1) - P(t) \right] \cdot A \tag{17}
$$

where,  $\lambda_3$  is the mileage compensation standard; the value of A is 1;  $P(t)$  is the predicted output of the optical storage power station.

For the convenience of research, the cost of energy storage here only considers the charge and discharge cost of the battery during operation.

$$
C_{\text{bess}} = \sum_{t \in T} [\Delta E_{\text{bess}}(t) \cdot \lambda_{\text{ch}}] \tag{18}
$$

where,  $\Delta E_{bess}(t)$  is the amount of energy change in the energy storage battery in the tth minute,  $\lambda_{ch}$  represents the unit cost of charge and discharge.

During the practical operation process of MOGEO, in order to fit the characteristics of the algorithm, it is necessary to appropriately adjust the objective function so that the fitness function of the algorithm program is calculated as follows:

$$
\begin{cases}\n\min f_1' = f_1 + \psi \cdot h \\
\min f_2' = -f_2 + \psi \cdot h\n\end{cases} \tag{19}
$$

where,  $\psi$  is the penalty factor which usually defined a large positive number;  $h$  is the number of violated constraints for [Eqs](#page-3-0).  $6-12$  $6-12$  $6-12$ ;  $Pe(t)$  reflects the constraints in the [Eq. 7](#page-3-1). The introduction of penalty function method can help to discard the incomprehension beyond the constraints. Specifically, the solution obtained during algorithm iterations will be retained to the next iteration if it is in the solution space. While he solution that violates the constraint is discarded.

### Application design of photovoltaic reconfiguration solution based on pareto

The MOGEO proposed in this work is a multi-objective intelligent optimization algorithm, so the key problems including variable processing, fitness function, solution screening and compromise decision must be mainly solved in the model solution of joint PV energy storage system ([Yousri et al., 2020c](#page-10-22)).

### Variable processing and fitness function

PV array reconfiguration optimization and charge-discharge optimization of BESS contain both continuous and discrete variables [\(Mahmoud et al., 2019\)](#page-10-23). Continuous variables can be

processed according to normal optimization; The discrete variables can be rounded by the values of the continuous space, and the upper and lower limits of the continuous optimization space are the upper and lower limits of the corresponding discrete variables (Horoufi[any and Ghandehari,](#page-10-24) [2017](#page-10-24)).

The fitness function of the algorithm must effectively combine the objective and constraint conditions of the proposed model, which can be performed by [Eq. 17](#page-4-0).

### Storage and screening of pareto solutions

In the iteration process of MOGEO, the number of Pareto solutions will persistently grow. And the solutions will be put into a finite sized storeroom. The new non-dominant solution obtained by the MOGEO is compared with the non-dominant solution set in the storeroom. Based on the comparison result, the new non-dominant solution is determined whether to put in the storeroom or not. Like the general multi-objective optimization algorithm, the judgment process is divided into the following three situations.

- 1) If the new solution dominates one or more solutions in the storeroom, replace them with the new solution;
- 2) If the new solution is dominated by at least one solution in the storeroom, the new solution is discarded;
- 3) If the new solution does not have a dominant relationship with all the solutions in the storeroom, the new solution is added to the storage pool.

To improve the computing efficiency of the algorithm, the storeroom stores only a limited number of dynamic nondominant solutions. Therefore, when the number of nondominant solutions in the storeroom exceeds the threshold, redundant non-dominant solutions need to be removed. In order to screen out non-dominant solutions with crowded distribution, the algorithm removes them according to the number of adjacent solutions of each non-dominant solution. On the basis of obtaining the number of adjacent solutions of each non-dominant solution in the storeroom, the method of roulette is adopted to eliminate the non-dominant solutions whose adjacent solutions exceed the limit amount. The more the number of adjacent solutions of non-dominant solutions is, the greater the probability of being eliminated is.

### Improved ideal point decision making method

According to the optimal Pareto front obtained by MEGEO, the target ideal point of the current optimization problem to be solved and the square of the Euclidean distance from each non<span id="page-5-2"></span>TABLE 1 The procedure pseudocode of joint PV energy storage system reconfiguration.

- 1: Input: weather condition, frequency capacity demand, and electricity prices, etc.
- 2: Initialize the parameters of MOGEO and proposed model

3: Initialize the random solutions

4: Set  $i = 1$ 

5: For  $i \leq \text{Itera}_{\text{max}}$ 

6: Compute the fitness of all agents' through [Eqs 17](#page-4-0)–[21](#page-5-0)

7: Rank all the solutions, and calculate the number of adjacent solutions of each non-dominant solution in the storeroom

8: Update the non-dominated solution set based on the dominant relationship between the new solution and the solutions in storeroom

9: Update the position of the golden eagles based on [Eqs 1](#page-1-0)–[4](#page-2-2)

10: Update the solutions of all golden eagles

11: Set  $i = i+1$ 

12: End

13: Output: the Pareto front including PV array topology and charge/discharge power of BESS

14: Pick up the best compromise solution by improved ideal point decision making method given by [Eqs 22](#page-6-0)–[26](#page-9-0)

<span id="page-5-3"></span>TABLE 2 Key parameters of the joint PV energy storage system.



<span id="page-5-4"></span>TABLE 3 Input parameters of MOGEO.



<span id="page-5-1"></span>dominant solution to the ideal point can be computed. First, the objective function value of the non-dominant solution is normalized, as shown in the formula below.

$$
y_j(i) = \frac{f'_j(i) - f'_j^{(\min)}(i)}{f'_j^{(\max)}(i) - f'_j^{(\min)}(i)}, \quad i = 1, 2
$$
 (20)

where,  $y_j(i)$  indicates the normalized value of objective function *i* of the *j* th non-dominant solution;  $f'_i$ <sup>min</sup> and  $f'_i$ <sup>max</sup> are minimum and maximum value of j th non-dominant solution.

<span id="page-5-0"></span>Therefore, the ideal point of pareto frontier after normalization is (0, 0). So that the squared Euclidean distance from each nondominant solution to the ideal point is calculated by following formula.

$$
D_j = \sum \left[ y_j(i) - 0 \right]^2 \rho(i)^2 \quad i = 1, 2 \tag{21}
$$

where,  $D_j$  is squared Euclidean distance from the ideal point to the *j* th non-dominant solution;  $\rho(i)$  denotes the weight coefficient of the i th objective function.



<span id="page-6-1"></span><span id="page-6-0"></span>The optimal weight model is constructed to give the weight coefficients of each objective more fairly, as shown in [Eq. 20.](#page-5-1)

$$
\begin{cases}\n\min Z = \sum_{j=1}^{k} D_j \\
s.t. \sum \rho(i) = 1, \quad \rho(i) > 0\n\end{cases}
$$
\n(22)

where,  $k$  is maximum number of non-dominant solution in the storeroom. By constructing the Lagrange function, the aforementioned optimal weight coefficients are obtained as below:

$$
\rho(i) = \frac{1}{\sum_{\left[y_j(i)-0\right]^2} \cdot \sum \left[\left[y_j(i)-0\right]^2\right]}
$$
\n(23)

Hence, the decision compromise solution is determined by the following formula:

$$
x_{\text{best}} = \arg \min_{j = 1, 2, ..., k} \sum [y_j(i) - 0]^2 \rho(i)^2 \qquad (24)
$$

In conclusion, the detailed steps of joint PV energy storage system participating frequency regulation is tabulated in [Table 1](#page-5-2).

# Case studies

In order to verify the contribution of the joint PV energy storage system on improving the frequency condition of the grid based on proposed PV plant reconfiguration model, two simulation tests are designed and executed. In the studied cases, the installed capacity of PV power station is 25 MW, and the capacity of BESS is 15 MW. Moreover, the key parameter settings of the joint PV energy storage system model are shown in [Table 2](#page-5-3).

The PV system consists of 25 subsystems, each of which is the same  $10 \times 10$  PV array. In addition, the PV system is equipped with a 15 MW energy storage battery, which is used to cooperate with PV power generation, to alleviate the fluctuation of PV output, reduce the abandonment of sunlight, and realize better response to frequency regulation signal. As mentioned above, the joint PV energy storage system composed of PV system and BESS not only participates in the conventional electricity market, but also provides auxiliary services. Specifically, according to the operation rules of Yunnan Province frequency regulation auxiliary service market, the adopted parameters of auxiliary service compensation and input parameters of algorithm in the case studies are tabulated in [Table 3](#page-5-4).

The shading which is varying with time of each subsystem is assumed same, and the shading condition of PV array in 10 minutes is depicted in [Figure 3](#page-6-1). Besides, all case studies are performed on Matlab R2019b.

### Response to high frequency of grid

When the practical frequency of power grid is higher than power frequency, the joint PV energy storage system will receive



#### <span id="page-7-0"></span>FIGURE 4

(A) Shading distribution of PV array after reconfiguration. (B) Power curves of BESS, joint PV-BESS station and PV plant without optimization. (C) Comparison of power deviation and profit.



#### <span id="page-8-0"></span>FIGURE 5

(A) Shading distribution of PV array after reconfiguration. (B) Power curves of BESS, joint PV-BESS station and PV plant without optimization. (C) Comparison of power deviation and profit.

a FR command of decreasing power output from dispatch department. Therefore, the FR signal under high grid frequency is designed as below:

$$
P_{\text{FR}}(t) = \begin{cases} 16, & \text{1min} \le t < 2\text{min} \\ 15, & 3\text{min} \le t < 8\text{min} \\ 16, & 9\text{min} \le t < 10\text{min} \end{cases} \tag{25}
$$

After the optimization of PV reconfiguration by MOGEO, the shadow is dispersed to the whole array as demonstrated in [Figure 4A.](#page-7-0) Moreover, the power curves of BESS, joint PV-BESS station and PV plant without optimization are depicted in [Figure 4B.](#page-7-0) Obviously, the proposed reconfiguration method based on MOGEO effectively mitigate the impact of PSC and consequently enhance the upper limit of PV output. With the cooperation of BESS, the proposed technique achieves the aim of reducing the deviation between output power of joint PV-BESS and FR signal than that without reconfiguration optimization. In addition, the power biases from FR signal and profits before and after optimization are shown in [Figure 4C](#page-7-0).

### Response to low frequency of grid

<span id="page-9-0"></span>Apart from high frequency response, the simulation test for low frequency response is also performed, and the FR signal is designed as follows:

$$
P_{FR}(t) = \begin{cases} 24, & \text{1min} \le t < 2\text{min} \\ 22, & \text{3min} \le t < 5\text{min} \\ 23, & \text{6min} \le t < 8\text{min} \\ 22, & \text{9min} \le t < 10\text{min} \end{cases} \tag{26}
$$

The shadow distribution after PV reconfiguration is demonstrated in [Figure 5A.](#page-8-0) Moreover, the power curves of BESS, joint PV-BESS station and PV plant without optimization are depicted in [Figure 5B.](#page-8-0) And the power output of PV station is more closed to FR signal than that of high frequency response. Besides, the proposed reconfiguration model effectively enhances the upper limit of PV output and consequently enhance the margin space of power modulation. What's more, the power biases from FR signal and profits before and after optimization are shown in [Figure 5C.](#page-8-0)

# Conclusions and perspectives

In this work, a novel PV station participating FR technique based on PV array reconfiguration and BESS is put forward. And the simulation results verify that the proposed method contributes to the frequency response of PV station. Two cases are designed and tested. The main conclusions of this work are summarized as below:

- 1) MOGEO can effectively find satisfactory solution which can meet both of profit maximization and power deviation minimization;
- 2) The improved ideal point decision making method is proposed to get optimal weight coefficients of each objective more fairly;
- 3) By proposed technique, the profit of PV station is increased by 8.4 and 10.07% respectively in the high and low frequency response simulation tests; meanwhile the power deviation from FR signal is decreased by 19.98 and 67.69% in the high and low frequency response tests.

The future works will focus on the following issues:

- Hardware-in-the-loop experiments should be executed to testify the practical influence and algorithm convergence rate of proposed technique;
- Hardware implementation method of PV array reconfiguration deserves more attention.

# Data availability statement

The original contributions presented in the study are included in the article/supplementary material, further inquiries can be directed to the corresponding author.

# Author contributions

JZ: Conceptualization, Writing-Original Draft, Formal analysis; CL: Formal analysis, Software, Supervision; KL: Project administration, Resources.

# Conflict of interest

Author JZ was employed by the company State Grid Corporation of China.

The remaining authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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