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# A feeder link planning method for total supply capability improvement of distribution network

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This study proposes a new feeder link planning method for the distribution network, which can improve total supply capability (TSC). Feeder links are the key component of distribution networks. They are of great significance to the TSC of the distribution network. Therefore, it is necessary to reveal the influence rules of feeder links on TSC and then apply the rules in distribution network planning. First, the indices describing the position, scale, and efficiency of feeder links are defined. Second, the influence rules of feeder links on TSC are revealed. 1) When the feeder geometrical distribution is more balanced, the TSC is higher. 2) When the feeder link scale is larger, the TSC is higher. While for both (1) and (2), the TSC will remain unchanged after reaching a certain value. 3) There always exists an optimal construction order of feeder links, which can ensure the TSC is as high as possible in each planning stage. Third, based on the rules, a model and an algorithm of the feeder link planning are proposed. The method can find an optimal construction order of feeder links, which can ensure that the value of TSC is as high as possible in each feeder link planning stage. Finally, the proposed method is verified on an 8-substation-transformer case grid, which has shown that the proposed method has advantages in feeder link efficiency and feeder-distribution balancing, and especially the TSC can be improved in each planning stage than the traditional methods.

#### KEYWORDS

feeder link planning, total supply capability, influence rule, distribution network, optimal construction order

### 1. Introduction

A distribution network is directly linked to consumers, which is an important part of the distribution system. Also, distribution network planning has a very important impact on the security and reliability of the power system. As a channel of load transfer, feeder links play a key role in improving the reliability and flexibility of power supply capability.

A feeder link planning can not only ensure the N-1 security criterion of the distribution network but also can improve the utilization rate of the equipment. The most important point is that the planning of feeder links can improve the total supply

capability (TSC). When the capacity and number of substation transformers are given, the TSC is determined by the structure of feeder links, which means that the TSC can be maximized by optimizing the feeder links. The optimal feeder construction order can be obtained by solving the optimal balanced degree of the feeder geometrical distribution. The TSC will be the largest during the optimal feeder construction process. Therefore, a distribution network structure can be optimized to improve the maximum total supply capacity. There are many advantages of using feeder link planning for distribution network optimization, such as improving the flexibility and reliability of power supply capability. This is because feeder link optimization is more flexible than substation optimization. Therefore, it is necessary to research the feeder link planning of the distribution network.

TSC is an important index representing the security and efficiency of a distribution network. TSC is defined as the maximum load that a distribution network can serve, which satisfies the N-1 security criterion (Xiao B. et al., 2017). At present, the research about TSC has involved the definition (Guo et al., 2018), index (Xiao et al., 2017b), modeling (Mu and Liu, 2018; Xiao et al., 2021), algorithm (Ge et al., 2011; Zhang et al., 2020), and application (Zhang et al., 2017; Sun et al., 2018; Xiao et al., 2020) of TSC. The main influence factors of TSC include the capacity and number of substation transformers, feeder capacity, and how the feeders link with each other. In the planning stage of a distribution network, the substation transformer capacity, number of substations, and feeder capacity are determined by planning guidelines, which means that their adjustable ranges are limited. However, the adjustment range of the feeder link is large, which means that the feeder link is the key factor to influence TSC. By optimizing the feeder link, the value of TSC can be maximized without increasing the capacity of the substations.

The existing research on feeder link planning targeting TSC is as follows: Xiao et al. (2012) and Xiao et al. (2016) proposed to improve the TSC to meet the increased load demand by planning the feeder link of the distribution network initially and then considered constructing new substations to absorb new loads. Ge et al. (2007) planned the optimal feeder link channel between substation transformers based on the TSC calculation method. Han et al. (2013) carried out the multi-objective link structure planning between substation transformers for the maximum total supply capacity, the smallest number, and the shortest length of feeder link channels, which also considered the actual location of the substation. Ge et al. (2014) calculated the cost of power supply capability and selected the optimal scheme for the feeder link structure. A multi-stage and multiload-scenario active distribution network expansion planning model was proposed, which considered the applications of new distributed generation and construction of feeders at the planning level (Shen et al., 2018), and maximum TSC can be achieved by planning feeder links. In the study by Verma and

Swarup (2017), the optimal feeder link placement problem was solved by focusing on the minimization of penalties incurred by the distribution network, and optimal feeder link location was found by a fundamental loop-based algorithm. The length upper limit estimation method for the optimal planning scheme feeder link is proposed to considerably reduce the search range of the optimal feeder link planning scheme (Hou et al., 2019). In the study by Xiao et al. (2017c), a planning model of link structure among substation transformers based on Pareto optimal was proposed. Meanwhile, the optimal load distribution of the distribution network is obtained by using the feeder load balancing model. A multi-objective planning model of the link structure considering the TSC and the minimum link cost, which is influenced by geographical factors, was established. A planning model based on feeder corridors was proposed to generate a network with minimal investment cost while meeting the specific reliability requirement (Li et al., 2020). Bosisio et al. (2020) addressed the problem of optimally rerouting the feeders of the urban distribution network in Milano, Italy, and also presented a mixed-integer programming approach for the design of a new network configuration satisfying the so-called 2-step ladder layout required by the planner. A novel method to determine the optimal routing of medium-voltage distribution networks in sparse rural areas was presented, and the optimization model was applied to a real rural distribution network in the South-West region of western Australia (Fletcher et al., 2018). A model that can supply the optimal feeder locations and feeder switch types was presented by Jooshaki et al. (2021), which improved the calculation efficiency of complex distribution networks. Shahbazi et al. (2021) presented a planning model for the natural disaster situation, which can minimize the total cost while maintaining the stable operation of the power grid in extreme weather. Mehrtash et al. (2019) presented a transmission expansion planning (TEP) algorithm, which considered the region's characteristics and feeder-link flow with its neighbors. A planning method considering distribution automation functions was developed (Heidari et al., 2015), which used the genetic algorithm to solve the optimization problem.

Most studies are conducive to revealing the mechanism and modeling of the distribution network. However, some basic issues such as searching the roles of TSC in different feeder link positions and the influence of construction order for feeder links on TSC were still not discussed. The real planning is divided into several stages: there are no feeder links at the early construction stage. Then, with the development of the city, the reliability requirements get higher, and the feeder link is gradually established. But, it is impossible and unnecessary to build all feeder links at once. The construction order is the order that feeders be constructed one by one. How to find the best construction order of feeder links that can improve the TSC needs to be solved.



In order to solve the abovementioned problems, this study reveals the influence rules of feeder links on the TSC. By applying the abovementioned rules, a planning method of the optimal construction order for feeder links is proposed. The planning of a distribution network is carried out in several stages, and the construction order for feeder links can arrange the feeder link position and feeder capacity one by one. The effectiveness of the proposed method in this study is verified by comparing it with traditional methods.

### 2. Definitions

In this section, the definitions and indices of feeder links are discussed. Some related definitions of supply capability such as substation supply capability (SSC), network transfer capability (NTC), expandable supply capability (ESC), and maximum supply capability (MSC) are detailed in Supplementary Appendix SA.

The distribution network in this study is simplified to a geometrical figure to observe the feeder link position easily. The comparison between the original figure and the simplified figure is shown in Figure 1.

The feeder link is composed of the normally open switch and short lines on both sides of the switch.

### 2.1 Definitions of feeder links

**Definition 1.** Feeder *F*: The line which makes a substation transformer link with itself or another transformer.

All the feeders between the substation transformer  $T_i$  and  $T_j$  are equivalent to each other and denoted as  $F_{ij}$ . The feeder

capacity is denoted by  $R_F$ , and the feeder link scale is denoted by M, which represents the number of feeders in a distribution network.

**Definition 2.** Feeder link channel *L*: The collection of all feeders between two substation transformers. The feeder link channel between substation transformers  $T_i$  and  $T_j$  is represented by  $L_{ij}$ . The scale of the feeder link channel is denoted by *N*.

**Definition 3.** Single link: Two feeders are only linked by one link.

Definition 4. Full link: All substation transformers are linked.

**Definition 5.** Inner-station link: Link between the substation transformers of the same substation.

**Definition 6.** Feeder links: Two or more feeders are linked through the interconnection switch.

### 2.2 Definitions of the feeder link position

**Definition 7.** Feeder link position *x*: The position of the feeder link between substation transformers  $T_i$  and  $T_j$  is represented by x(i, j).

**Definition 8.** Balanced degree of feeder geometrical distribution  $B_D$ : The matching degree between the number of feeders in one feeder link channel and the average capacity of substation transformers. The calculation steps of  $B_D$  are as follows:



The averaged capacity  $R_{ij (1/2)}$  of substation transformers at both ends of the feeder link channel is calculated as follows:

$$R_{ij(1/2)tot} = 0.5 \times \left(R_i + R_j\right), \left((i, j) \in \Omega^{(i,j)}\right). \tag{1}$$

The link reference degree (k) is calculated as follows:

$$k_{ij} = \frac{R_{ij}(\frac{1}{2})}{R_{ij(1/2)tot}}, ((i, j) \in \Omega^{(i,j)}).$$
(2)

$$R_{ij(1/2)tot} = \sum R_{ij(1/2)}, \left( \forall (i, j) \in \Omega^{(i,j)} \right).$$
(3)

The link reference difference (*D*) is calculated as follows: The number of linked feeders in the feeder link channel  $L_{ij}$  is assumed to be  $X_{ij}$ :

$$D_{ij} = X_{ij} - k_{ij} \times M, \left( \left( i, j \right) \in \Omega^{\left( i, j \right)} \right).$$
(4)

$$D_{s} = \sqrt{\sum D_{ij}^{2}}, \left(\forall \left(i, j\right) \in \Omega^{\left(i, j\right)}\right).$$
(5)

Corresponding to the asymmetric feeder distribution, it is easy to find the largest  $D_s$ , which is recorded as  $D_{smax}$ .

$$B_D = 1 - \frac{D_s}{D_{smax}}.$$
 (6)

 $B_{\rm D} \sim (0, 1)$ , when the distribution of feeder links is balanced,  $B_{\rm D}$  approaches 1; when the distribution of feeder links is uneven,  $B_{\rm D}$  approaches 0.

**Definition 9.** Feeder link efficiency  $T_{\text{CUL}}$ : The averaged network transfer capacity ( $A_{\text{NTC}}$ ) is brought by each feeder link, while the averaged network transfer capacity means that the average amount of the TSC increased by interconnections:

$$T_{CUL} = \frac{A_{NTC}}{M}.$$
(7)

# 3 Influence of feeder links on total supply capability

In this section, the influence of feeder links on the TSC is discussed, which mainly considers the following four key aspects: feeder link position, balanced degree of feeder geometrical distribution, feeder link scale, and different construction orders.

Another four comparative cases and the theoretical analysis of 3.1–3.4 are added in Supplementary Appendix SC, which can prove the obtained conclusions in Section 3.

# 3.1 Influence of feeder geometrical distribution on total supply capability

The basic parameters of case 1 are shown in Supplementary Appendix Table SB1. The capacity of all substation transformers is 40 MVA, and the capacity of feeders is 9 MVA. Every substation transformer has seven feeders each.

It can be seen from Figure 2 that the number of feeders of (A) is 12, which is the same as that of (B), but the feeder geometrical distribution is different. The feeder distribution in (A) is symmetric, while feeders in (B) are concentrated on a few nodes. When the number of feeders between substation transformers is more evenly distributed, the geometric distribution is more balanced. For example,  $B_{D(A)} = 1$  and  $B_{D(B)} = 0.738$ , Figure 2A is more balanced than Figure 2B. The feeder link channel scale N is also different while N(A) = 12 and N(B) = 4. The TSC(A) = 135MVA and TSC(B) = 134 MVA. The detailed model, steps, and codes for calculating the TSC can be seen in Supplementary Appendix SD. Thus, when the feeder geometrical distribution is more balanced, the TSC is higher.



# 3.2 Influence of balanced degree of feeder geometrical distribution on total supply capability

The basic parameters of case 2 are shown in Supplementary Appendix Table SB2. The capacity of substation transformers of S1, S2, S3, and S4 is as follows: 31.5MVA, 40 MVA, 40 MVA, and 63MVA, respectively. All feeder capacity is 8.92 MVA. Every substation transformer has nine feeders.

Under the same feeder link scale, 15 different feeder distribution modes are selected, and then TSC and  $B_D$  are calculated. The rule of TSC increasing with  $B_D$  is shown in Figure 3.

It can be seen from Figure 3 that if  $B_D$  reaches the maximum, the TSC reaches the maximum value at the same time. The three curves in Figure 3 reveal the common rule: when  $B_D$  is larger than 0.8, the TSC remains unchanged after reaching the maximum value. To be consistent with the planning principles and practical experience, the substation transformer with a large capacity should provide more feeders. It can be seen from the abovementioned cases that the balanced degree of feeder geometrical distribution and TSC need not be strictly positively correlated.

# 3.3 Influence of feeder link scale on total supply capability

The feeder link scale is directly related to the complexity of the distribution network. It can be inferred from the last section that if the

link grows with the maximum  $B_D$ , the TSC will increase fastest throughout the process. Therefore, the relation of TSC,  $T_{CUL}$ , and M should be researched with the feeder link position remaining optimal. Using basic parameters of case 2, different feeder capacities are selected to form case 3. The relationship curves of TSC,  $T_{CUL}$ , and M under three different feeder capacity  $R_F$  are shown in Figure 4.

The feeder capacity  $R_F$  keeps the same in one process. It can be seen from the three curves in Figure 4:

- (1) When feeder link positions maintain optimal positions, TSC increases linearly and  $T_{CUL}$  maintains the maximum value, which is half of the feeder capacity  $(0.5R_F)$ . This is because the feeder link scale is small in the early construction stage. During this stage, TSC is only limited by the feeder capacity.
- (2) When the feeder link scale reaches a certain value, TSC remains unchanged and  $T_{CUL}$  continues to decrease. This is because TSC has reached MSC, so the subsequent feeder links are all invalid links that do not contribute to TSC.
- (3) When the TSC approaches the maximum value, the contribution of the unit feeder link to TSC and the corresponding  $T_{\text{CUL}}$  is reduced. This is because the difference between MSC and TSC is less than  $0.5R_F$ , and the increase of NTC brought by a single feeder link does not exceed  $0.5R_F$ .
- (4) When  $R_F = 7.03$  MVA, TSC reaches MSC when *M* is 32. If  $R_F$  continues to decrease, MSC cannot be reached by a single link alone. This is because  $R_F$  is too small, so the capacity of the substation transformer cannot be fully used by feeder links.



# 3.4 Influence of different construction orders on total supply capability

The construction order of feeder links refers to different schemes for the growth of feeder links in the distribution network, which includes two key factors: feeder link position and feeder link scale. The varied position and scale of feeder links lead to different construction orders and have diverse impacts on TSC. A suitable feeder link construction order can improve the value of TSC.

Using the basic parameters of case 2, five feeder link construction orders are selected to form case 4. Order 1, Order 2, Order 3, Order 4, and Order 5 (Table 1) for comparison are as follows.

Feeder link scale M	Order 1	Order 2	Order 3
1	F <sub>68</sub>	$F_{68}$	F <sub>13</sub>
2	$F_{67}$	$F_{67}$	$F_{13}$
3	$F_{58}$	$F_{58}$	$F_{24}$
4	$F_{57}$	$F_{57}$	$F_{24}$
5	$F_{38}$	$F_{68}$	$F_{25}$
6	$F_{37}$	$F_{67}$	$F_{16}$
7	$F_{48}$	$F_{58}$	$F_{25}$
8	$F_{47}$	$F_{57}$	$F_{16}$
9	$F_{18}$	$F_{27}$	F <sub>35</sub>
10	$F_{28}$	$F_{17}$	F <sub>35</sub>
11	$F_{17}$	$F_{28}$	F <sub>35</sub>
12	$F_{27}$	$F_{18}$	F <sub>35</sub>
13	$F_{35}$	$F_{35}$	$F_{46}$
14	$F_{36}$	$F_{36}$	$F_{46}$
15	$F_{45}$	$F_{45}$	$F_{18}$
16	$F_{46}$	$F_{46}$	$F_{27}$
17	$F_{13}$	$F_{13}$	$F_{28}$
18	$F_{23}$	$F_{23}$	F <sub>57</sub>
19	$F_{14}$	$F_{14}$	F <sub>37</sub>
20	$F_{24}$	$F_{24}$	$F_{47}$
21	$F_{15}$	$F_{14}$	$F_{58}$
$A_{BD}$	0.834	0.763	0.642

TABLE 1 Construction orders of feeder links of case 4.

The averaged balanced degree of feeder geometrical distribution  $A_{BD}$  of Order 1, Order 2, and Order 3 decreases sequentially.

Supplementary Appendix Table B3 is the construction orders of feeder link channels which correspond to the construction orders of feeder links in Table 1.

Figure 5 shows the increasing trend of TSC with M under three different construction orders of feeder links.

It can be seen from Figure 5:

- (1) The TSC of Order 2 grows linearly in the early stage. Starting from one feeder, the growth rate slows down. This is because TSC is mainly limited by the feeder capacity at the early stage, which is finally limited by both feeder capacity and substation transformer capacity.
- (2) There is a bottleneck stage in the middle of the construction stage in Order 3. This is because the feeder link position is not suitable in the early construction stage, which leads to several invalid links in the midterm.
- (3) The black TSC curve Order 1 is superior to others, which indicates that the value of TSC keeps the largest among all orders at any time. It also shows that there always exists a construction order which can improve the TSC in the whole construction stage.



# 4 Application in the distribution network planning

In this section, the application of construction orders of the feeder links on TSC is discussed, which mainly considers the following three key aspects: definition, mathematical model, and an algorithm that can improve the TSC. The details are described as follows.

# 4.1 Definition of optimal construction order of feeder links

This study assumes that only one feeder can be constructed at a given period in the feeder link construction. Then, the distribution network will get a new  $TSC_m$  after the construction of  $F_m$ . The position  $x_m$  with the largest  $TSC_m$  can be defined as the optimal position of  $F_m$ .

If each feeder chooses its best position, then the corresponding M is the optimal feeder link scale  $M_{opt}$ , which means that TSC also reaches MSC at this time. The  $TSC_m$  maintains a maximized value throughout the process, while  $T_{CUL}$  will also maintain the maximized value at the same time.

**Definition 10.** Optimal construction order of the feeder links: it means the construction order that TSC maintains the maximum at any stage and reaches MSC, while the total feeder link scale is the smallest. It is a set of number pairs with finite lengths, such as Eq. 8.

$$order = \left[ (x_1, R_{F_1}), (x_2, R_{F_2}), \dots, (x_{M_{opt}}, R_{F_{M_{opt}}}) \right], \quad (8)$$

Substation	Substation transformer	Number of feeders	Feeder capacity $R_F$	Voltage of substation transformer [MVA]	Capacity of substation transformer [MVA]
S1	T1	6	12	110/10	31.5
	T2	6	12	110/10	31.5
S2	Т3	6	12	110/10	40.0
	T4	6	12	110/10	40.0
S3	Т5	6	12	110/10	40.0
	Т6	6	12	110/10	40.0
S4	T7	6	12	110/10	63.0
	Т8	6	12	110/10	63.0

TABLE 2 Basic parameters of case 5.

where  $(x_1, R_{F1}), \ldots, (x_{Mopt}, R_{FMopt})$  are the feeder position and feeder link capacity in time order, and the length of pairs is  $M_{opt}$ .

**Definition 11.** Construction stage: stages of the distribution network when feeder links grow.

In practice, the planning of the feeder link construction order is constructed in stages. Each stage constructs a set of feeder links. After the feeder link construction is completed in one stage, the TSC reaches the maximum value in the current situation, for example, when the construction process needs to be divided into three stages such as a, b, and c, and  $M_a + M_b +$  $M_c = M_{opt}$ . The result of Eq. 8 can be obtained and then divided into stages I ~ III, such as Eq. 9.

$$order = \left\{ \begin{array}{c} [(x_{1}, R_{F_{1}}), \dots, (x_{a}, R_{F_{a}})]_{I}, \\ [(x_{a+1}, R_{F_{a+1}}), \dots, (x_{a+b}, R_{F_{a+b}})]_{II}, \\ [(x_{a+b+1}, R_{F_{a+b+1}}), \dots, (x_{a+b+c}, R_{F_{a+b+c}})]_{III} \end{array} \right\}.$$
(9)

# 4.2 Mathematical model of optimal construction order for feeder links

It can be seen from Section 3 that an optimal feeder link construction order exists in all the construction order schemes. In this order, the TSC at any stage of the feeder construction is greater than that of the other orders. In short, the feeder link construction order is to arrange the position of the feeder link one by one. When the position of each feeder is the best, the linear increase of TSC is the fastest. When the  $B_D$  value is the largest, the construction position of the feeder link is the best.

Therefore, the objective function in the mathematical model reflects that the maximum TSC can be obtained by choosing the positions of the feeder links.

#### 4.2.1 Original model

A mathematical model is established to solve the problems of optimal construction order at first. The essence of the construction order for feeder links is to arrange the feeder link position and feeder capacity one by one, which also makes sure that TSC keeps the maximum throughout the process. Also, the construction is stopped when TSC reaches MSC. The mathematical model is shown as Eq. 10.

$$\begin{cases}
Max TSC_m = f_{TSC} [x_m (i, j), R_{F_m}] \\
s.t. (i, j) \in \Omega \\
t_{exist(i)} \leq t_{max(i)} \\
f_{exist(j)} \leq t_{max(j)} \\
R_{F_m} \geq R_{feeder(i)} , \\
R_{F_m} \geq R_{feeder(j)} \\
C_m = f_c (R_{F_m}, L_m) \\
\sum_{k=1}^m C_k \leq C_{lim}
\end{cases}$$
(10)

where  $TSC_m$  is the value of TSC after constructing the *m*th feeder  $F_{mi}$ ;  $f_{TSC}$  is the calculation method of  $TSC_m$ ;  $x_m$  (i, j) is the position of the feeder  $F_m$ ;  $R_{Fm}$  is the capacity of the feeder  $F_m$ ;  $\Omega$  is the set of all (i, j);  $t_{exist(i)}$  is the number of the feeders from the substation transformer  $T_i$  after adding feeder  $F_m$ ;  $t_{max(i)}$  is the maximum number of feeders of the substation transformer  $T_i$ ;  $R_{feeder(i)}$  is the feeder capacity of substation transformer  $T_i$ ;  $C_m$  is the cost of the *m*th feeder;  $L_m$  is the length of the feeder  $F_m$ ; and  $C_{lim}$  is the total budget for feeder link construction.

#### 4.2.2 Simplified model

This study focuses on the influence of TSC on the distribution network, so model (4) is simplified

The capacity of all feeders is equal. At this time,  $R_F = R_{\text{feeder}}$  and  $TSC_m$  are also simplified to be determined only by the position of  $F_m$ . It is assumed that the length of all feeders is the same as the constant  $L_0$ . There is no strict limit on the total cost, so we assume that  $C_{\text{lim}} = \infty$ .

The simplified model is shown in Eq. 11:

$$s.t. \begin{cases} Max TSC_m = f_{TSC} [x_m(i, j), R_{F_m}] \\ (i, j) \in \Omega \\ t_{exist(i)} \leq t_{max(i)} \\ t_{exist(j)} \leq t_{max(j)} \\ R_{Fm} = \min \left\{ R_{feeder(i)}, R_{feeder(j)} \right\} \end{cases}$$
(11)

The corresponding result is also reduced to Eq. 12 by Eq. 8:

$$rder = |x_1(i, j), x_2(i, j), \dots, x_{Mopt}(i, j)|.$$
(12)

# 4.3 Algorithm of optimal construction order of feeder links

TSC reaches its largest value when  $B_D$  reaches the maximum. Therefore, the optimal construction position of the feeder links is the position that makes  $B_D$  reach the maximum value.

Therefore, the goal "to solve the total supply capacity (TSC) of each construction stage" is transformed into "to solve the maximized balanced degree of feeder geometrical distribution."

The algorithm process includes three steps: 1) calculating the value of ESC ( $A_{\rm ESC}$ ); 2) using  $A_{\rm ESC}$  to calculate  $M_{opt}$ ; and 3) using  $M_{opt}$  to prepare for the calculation of  $B_{\rm D}$ . Different feeders are added and search for the largest  $B_{\rm D}$  is carried out. Then, the optimal construction order of feeder links is obtained.

#### 4.3.1 Calculation of the value of ESC

Expanded supply capacity (ESC) is the basis for calculating the  $M_{opt}$ . The calculation process includes three steps:

- (1) Calculate  $A_{MSC}$ :  $A_{MSC}$  is the value of MSC. MSC is the TSC of a system when it is fully linked. A fully linked distribution system means that every substation transformer has interconnection with all the other transformers in the system. A full-link matrix means the elements of the matrix are all 1. Therefore,  $A_{MSC}$  can be realized by setting the feeder link matrix as a full-link matrix and when the feeder capacity is infinite. Then, input the fulllink matrix into the TSC model in Lingo for calculation. The codes in Lingo can be seen in Supplementary Appendix SD.
- (2) Calculate A<sub>SSC</sub>: A<sub>SSC</sub> is the value of SSC. SSC is the TSC of the system at its lowest level, which means every substation transformer has no connection (through normally open switches) with other substation transformers. Therefore, A<sub>SSC</sub> can be realized by deleting all inter-station links and then putting the inner-station link matrix into the TSC model in Lingo for calculation.

(3) Calculate 
$$A_{\rm ESC}$$
:

$$A_{ESC} = A_{MSC} - A_{SSC}.$$
 (13)

#### 4.3.2 Calculation of the optimal feeder link scale

The optimal feeder link scale  $M_{opt}$  is the basis for calculating  $B_D$ , and the calculation process is as follows:

Under the premise of maintaining the optimal feeder link position, TSC increases linearly, while  $T_{\text{CUL}}$  maintains the maximum  $0.5R_F$ . The optimal feeder link scale  $M_{opt}$  can be calculated in advance:

$$X = \frac{A_{ESC}}{0.5R_F},\tag{14}$$

where *X* is the calculated result. If *X* is not an integer,  $M_{opt} = [X]+1$ , [X] is the integer part of *X*. If *X* is an integer, then  $M_{opt} = X$ . The  $M_{opt}$  is obtained based on the feeder link position *x* and remains optimal in the whole process.

#### 4.3.3. Calculation of optimal construction order of feeder links

After obtaining  $M_{opt}$ , the process of solving the optimal construction order is as follows:

(1) The total number of feeder link positions outside the station is calculated: If the number of substation transformers in the distribution network is  $n_{xx}$ , the total number of feeder link positions  $n_{\text{max}}$  is calculated by Eq. 15, where  $C_{n_x}^2$  means the combinatorial number. This is because the inner-station link does not contribute to TSC.

$$n_{max} = C_{n_x}^2 - 0.5n_x. \tag{15}$$

- (2) The averaged capacity of the substation transformer is calculated at both ends of the channel R (1/2) and the link reference degree k. The details are attached in Definition 8, chapter 2.2.
- (3) The first feeder F<sub>1</sub> (m = 1) is added and all possible feeder link positions are calculated: x (i<sub>1</sub>, j<sub>1</sub>),...,x (i<sub>nmax</sub>, j<sub>nmax</sub>). Then, the corresponding B<sub>D</sub> (i<sub>1</sub>, j<sub>1</sub>),...,B<sub>D</sub> (i<sub>nmax</sub>, j<sub>nmax</sub>) is obtained.
- (4) The maximum value of  $B_D$  in 3) is recorded. The corresponding  $x_1$  (*i*, *j*) is the optimal construction position of  $F_{1.}$
- (5) Set m = 2, repeat steps 3) to 4). The process stopped when m > M<sub>opt</sub>, and the order x<sub>1</sub> (i, j),...,x<sub>Mopt</sub> (i, j) is the optimal construction order.

The calculation process of the optimal construction order of feeder links based on TSC is shown in Figure 6.

Figure 6 will obtain the most efficient construction order of feeder links, which will result in the fastest TSC increase. This is because every feeder is constructed in the best order so that the value of TSC can be improved in the whole construction stage.



# 5 Case verification

In this section, the proposed method is verified by case 5. Also, how the proposed planning method improves TSC is also shown by comparison with the backward-optimization method.

### 5.1 Case grid information

The grid structure of case 5 is shown in Figure 7. The maximum number of feeders from a substation transformer

is six. The feeder capacity is 12 MVA, and the number of total feeders is 48. The voltage of the four substations is 110/ 10 kV, and the total substation transformer capacity is 349 MVA.

This study researches the construction process of feeder link growth from zero, and the construction order of feeder links is diverse. Therefore, Figure 7 only shows a general situation of the feeder link increasing: 12 feeders have been built, which belong to the middle construction stage. There is still potential for additional feeder links to improve the TSC.



# 5.2 The optimal construction order of feeder links

Step 1. Calculate A<sub>ESC</sub>:

- (1) Calculate  $A_{MSC} = 286 \text{ MVA}$
- (2) Calculate  $A_{SSC} = 174.5$  MVA
- (3) Calculate  $A_{\text{ESC}} = A_{\text{MSC}} A_{\text{SSC}} = 111.5 \text{ MVA}$

Step 2. Calculate Mopt:

$$X = \frac{A_{ESC}}{0.5R_F} = \frac{111.5}{0.5 \times 12.0} = 18.58.$$

After taking the integer part, X is 19.

**Step 3.** The preparatory work for the calculation of  $B_{\rm D}$ .

- The calculated total number of feeder link positions is 24. Therefore, there are 24 types of feeder link positions.
- (2) The calculated results of the average capacity of  $T_i$  and  $T_j$   $(R_{(1/2)})$  and link reference degree k are shown in Supplementary Appendix Table B4.

Because the feeder link position corresponds to the feeder link channel, so the  $R_{(1/2)}$ , k of  $L_{ij}$  are the same as that of x (i, j).

**Step 4.** Start from the first feeder  $F_1$  (m = 1) and then traverse 24 feeder link positions. The values of  $B_D$  can be obtained, as shown in Supplementary Appendix Table B5. The largest  $B_D$  (0.919) corresponding to the feeder link position  $x_1(6, 8)$  is the optimal construction position of the first feeder. Then, let m = 2 and continue to increase until m > 19 and stop.

After the four steps, we obtain the optimal construction order of feeder links, which is shown in Table 3.

### 5.3 Result verification

According to Table 3, under the optimal construction order, the trend of TSC when M varies is illustrated in Figure 8.

Throughout the construction process, it can be seen from Figure 8 and Table 3 that the construction order planned in this study remains the maximum of the TSC. Also, it will finally reach the MSC. The TSC increases the fastest in the process. After the completion of the 19th feeder, the MSC =

Feeder link scale M	Feeder between $T_i$ and $T_j F_{ij}$	TSC [MVA]	Balanced degree of feeder geometrical distribution $B_{\rm D}$
1	$F_{68}$	174.5	0.918949
2	F 67	186.5	0.888807
3	F 58	192.5	0.868152
4	F 57	198.5	0.852931
5	$F_{48}$	204.5	0.841570
6	F 47	210.5	0.833278
7	F 38	216.5	0.827611
8	F 37	222.5	0.824315
9	F 28	228.5	0.821812
10	F 27	234.5	0.821181
11	F 18	240.5	0.822402
12	F 17	246.5	0.825514
13	F 46	252.5	0.827029
14	F 45	258.5	0.829937
15	F 36	264.5	0.834312
16	F 35	270.5	0.840274
17	F 26	276.5	0.844853
18	F 25	282.5	0.850763
19	F 24	286.0	0.858170
20	F 23	286.0	0.867326

TABLE 3 Optimal construction order of feeder	links	of	case	5.
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286 MVA. Since the construction of  $F_{20}$ , the TSC has not increased, which shows that the optimal feeder link scale is indeed 19 feeders. It verifies the optimal construction order planning method proposed in this study.

In actual planning, it is not suitable to establish feeder links between substation transformers that are far away. At this time, the grid can be divided into several small areas, and then the planning method of this article can be used in each area.

Substation transformer	Number of feeders	Backward-optimization	Planning number of feeders		
			TSC-based planning method	Method of this study	
T1	6	5	3	2	
T2	6	6	5	6	
Т3	6	4	6	5	
T4	6	4	5	5	
T5	6	6	4	5	
Т6	6	6	6	5	
Τ7	6	9	7	6	
Т8	6	5	7	6	

#### TABLE 4 Total data of feeder links of substation transformers.

TABLE 5 Comparison of traditional methods and the proposed method.

Evaluation index	Backward-optimization method	TSC-based planning method	Proposed method
TSC/MVA	286	286	286
M	21	22	19
T <sub>CUL</sub>	5.31	5.07	5.87
Ν	17	20	19
B <sub>D</sub>	0.697	0.624	0.863
Exceed the maximum number of feeders	Yes	Yes	No
Keep the maximum TSC in the stage	No	No	Yes

# 5.4 Comparison with traditional planning methods

The backward-optimization method (Ge et al., 2014) and the TSC-based planning method (Xiao et al., 2016) are traditional planning methods for the distribution network.

The backward-optimization method first establishes the full link matrix of all substation transformers and then calculates the maximum  $TSC_{max}$ . Second, it deletes the cross-link channels between substation transformers one by one and calculates the corresponding TSC. When the obtained TSC is the same as the  $TSC_{max}$ , the method continues to delete the cross-connection channel. If the obtained TSC becomes smaller, the matrix of the link channel before deletion is the optimal feeder link scheme.

The TSC-based planning method conducts the feeder distribution planning according to the actual distribution of the load. The proposed planning scheme is verified through the N-1 security criterion finally.

The planning results of case 5 using the backwardoptimization method and the TSC-based planning method are compared in Table 4.

A planning scheme is not feasible if the number of feeders from a substation transformer is greater than the allowable

value. It can be seen from Table 4 that the feeder number of  $T_7$  in the backward-optimization method is 9, which is greater than the actual number of feeders 6. The feeder number of  $T_7$  and  $T_8$  in the TSC-based method is both 7, which is greater than the actual number of feeders 6. However, the results of the proposed method do not have this problem. In summary, the comparison results between the proposed method and the traditional methods are obtained as shown in Table 5.

It can be seen from Table 5:

- (1) All methods can reach TSC of 286 MVA, but the feeder link scale of the proposed method is less than that of the traditional methods when they reach TSC. It is on the premise of ensuring the power supply capacity while saving funds for distribution network construction.
- (2) The proposed method in this study can improve TSC, which means that the value of TSC maintains the maximum in all stages, but the traditional methods cannot. This is because the planning scheme of traditional methods does not specify the order of the feeder link construction, so they cannot guarantee that the TSC is maintained at the maximum in all stages.

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(3) The distribution of feeder links is relatively unbalanced when it uses the traditional methods. This is because  $B_D$  is 0.17 lower and 0.24 lower than the proposed method. Also, the corresponding feeder number from  $T_7$  and  $T_7$ ,  $T_8$  exceeds the allowable number, which does not meet the actual requirements. The method proposed in this study overcomes this shortcoming.

Traditional distribution network planning methods require more feeders to reach a certain level TSC, which will increase additional construction costs. However, it is very difficult to build new feeder corridors with the shortage of urban land-use planning. The proposed method in this study obtains the optimal feeder construction order by solving the optimal  $B_D$ so that the TSC keeps the largest and the feeder link scale is the smallest during the feeder construction process. In summary, this study provides a new theoretical basis for optimizing the distribution network structure while saving construction funds.

Comparative references can be applied to fully constructed distribution network planning, while the proposed planning method in this study is mainly used for the planning of new or under-built power grids. It can be a new guidance for eliminating invalid feeder links of a fully constructed distribution network.

### 6 Conclusion

This study proposes a new feeder link planning method, which can improve the value of TSC as high as possible in each planning stage.

By defining the indices of the balanced degree of feeder geometrical distribution, feeder link efficiency, and feeder link position, the influence rules of feeder links on TSC are analyzed quantitatively. Based on the rules we discovered, the model and algorithm of the optimal construction order of feeder links have been proposed. The case study verifies the validity of the proposed method. The main conclusions are as follows:

- (1) When the feeder geometrical distribution is more balanced, the TSC is higher. When the feeder link scale is larger, the TSC is higher. The TSC will remain unchanged after reaching a certain value.
- (2) There always exists an optimal construction order of feeder links which can ensure that the TSC is as high as possible in each planning stage. The optimal order can be obtained by the optimization method based on the balanced degree of feeder geometrical distribution proposed in this study.
- (3) Compared with the traditional backward-optimization method, the proposed method performs better planning schemes in the feeder link efficiency and feederdistribution balancing, especially improving the TSC value in each planning stage.

This study reveals the relationship between TSC and distribution network topology, which lays a theoretical foundation for TSC-based distribution network planning.

# Data availability statement

The original contributions presented in the study are included in the article/Supplementary Material. Further inquiries can be directed to the corresponding author.

### Author contributions

JX: conceptualization, methodology, investigation, formal analysis, validation, resources, writing—review and editing, supervision, and project administration. ZL: conceptualization, methodology, investigation, software, validation, data curation, formal analysis, writing—original draft, visualization, and project administration. GZ: investigation, validation, formal analysis, writing—original draft, review and editing, and provide funding. CS: critical review and commentary.

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# Conflict of interest

The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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# Supplementary Material

The Supplementary Material for this article can be found online at: https://www.frontiersin.org/articles/10.3389/fenrg.2022. 903388/full#supplementary-material

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# Nomenclature

S Substation T Substation transformer  $R_F$  Feeder capacity F Feeder M Feeder link scale L Feeder link channel N Feeder link channel scale  $L_{ij}$  Feeder link channel between  $T_i$  and  $T_j$ x Feeder link position  $B_D$  Balanced degree of feeder geometrical distribution  $T_{CUL}$  Transfer capability provided by unit feeder link  $M_{opt}$  Optimal feeder link scale when each feeder chooses its best position

 $TSC_m$  TSC reached after the construction of the *m*th feeder

 $\boldsymbol{\Omega}$  Set of all feeder link positions (i,j)

 $t_{exit(i)}$  Number of feeders from substation transformer  $T_i$  after add feeder  $F_m$ 

 $t_{\max(i)}$  Maximum number of feeders of substation transformer  $T_i$ 

 $R_{Fi}$  Feeder capacity of substation transformer  $T_i$ 

 $R_{\text{feeder}(i)}$  Feeder capacity of substation transformer  $T_i$ 

 $L_m$  Length of feeder  $F_m$ 

 $C_m$  Cost of the *m*th feeder

 $C_{\lim}$  Total budget for feeder link construction