



# A Multi-Level Investment Allocation Indicator System for Distribution Network Planning

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## INTRODUCTION

With the deepening of the reform of the electric power system in China, infrastructure planning of the power grid, as a complex project, will face greater challenges. As a matter of course, the internal and external uncertain factors, such as the imperfection of the structure of the power grid and the transformation of policy conditions, lead to the increasingly severe and complicated investment environment of power grid enterprises (Santos et al., 2017; Dai et al., 2018; Chen et al., 2020). On the one hand, the level of electrification for residents has gradually improved, and the demand for electricity in the whole society has continued to rise because of the rapid growth of the economy. Thus, the amount of investment in the power grid will gradually increase (Tavares and Soares, 2020; Zhang et al., 2022). On the other hand, due to the independence of transmission and distribution, the profit pattern of enterprises has changed, so the investment plan needs to be adjusted accordingly. Some factors fail to be considered in the existing investment allocation method, such as the distribution network status and investment benefit, resulting in unreasonable investment allocation (Liu et al., 2019; Yang et al., 2021). Therefore, a distribution network investment allocation method, which comprehensively takes the distribution network status and investment benefit evaluation index system into account, is proposed in this article to achieve high precision of investment allocation.

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## INVESTMENT RATIO BASED ON EVALUATION OF DISTRIBUTION NETWORK STATUS

### Indicator System

The indicator system to evaluate the distribution network status is based on systematic, scientific, objective, and practical principles to guide the investment orientation for the power network. The indicator system is constructed from four aspects: network structure, power supply level, electric power equipment level, and economic benefit (Chai et al., 2020; Ming et al., 2020; Ning et al., 2021). The weights of the four first-level indicators are 0.2, 0.3, 0.3, and 0.2, respectively. Moreover, 20 typical evaluation indicators are selected, which can be seen in the following figure.

### Investment Ratio Calculation

According to the distribution network status assessment, the difference between the score of each region and the total score is calculated, and the full score of the distribution network evaluation is 100 points. The results are normalized to obtain the ratio of investment allocation. The formula is as follows:

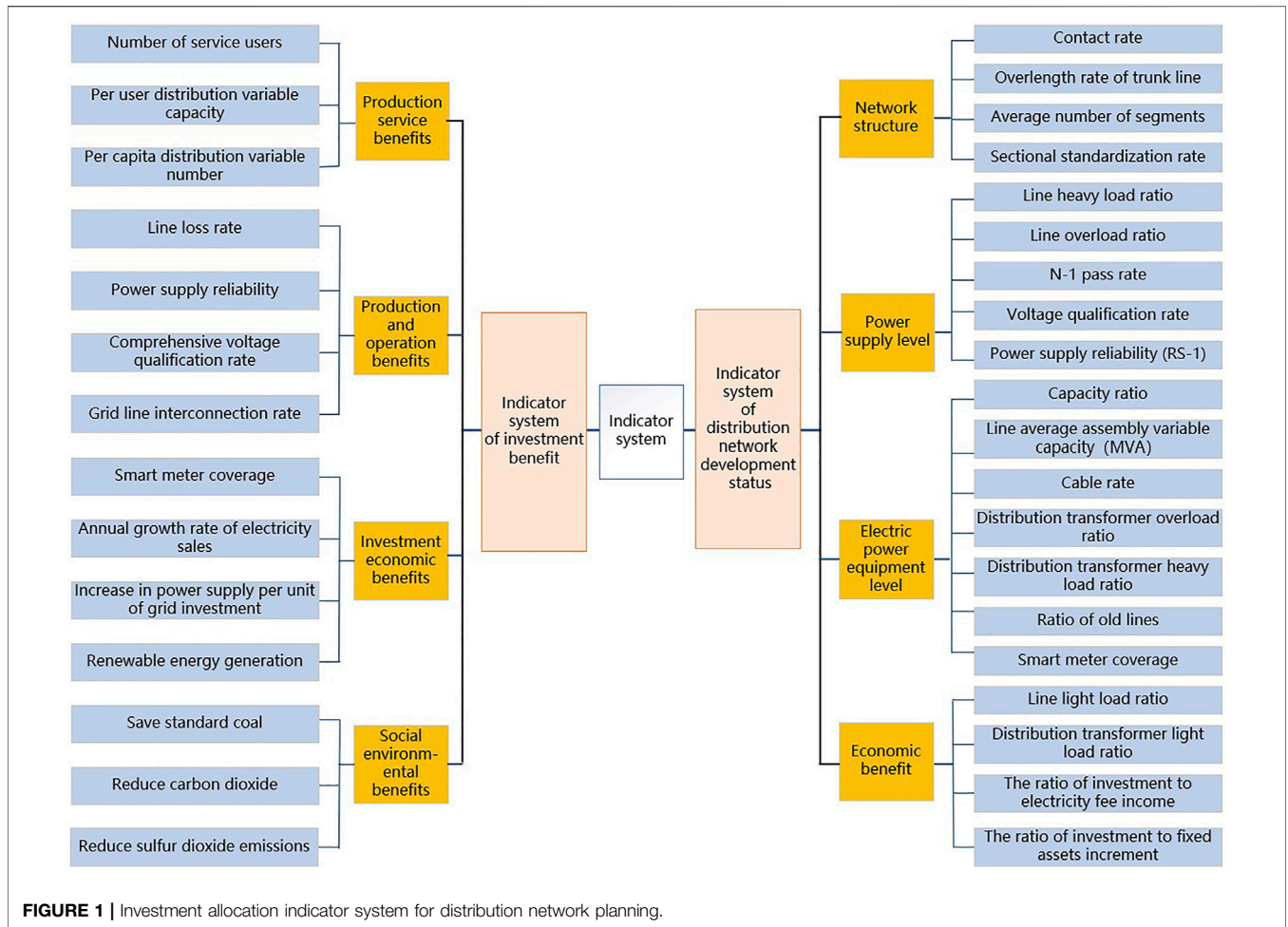


FIGURE 1 | Investment allocation indicator system for distribution network planning.

$$k = \sum_{s=1}^q \left( \left( \sum_{t=1}^m E_{st} \times q_{st} \right) \times E_s \right). \quad (1)$$

$E_s$  refers to the first-level index weight,  $E_{st}$  refers to the next level index weight,  $q_{st}$  is the second-level index score,  $m$  is the number of the second-level indicators under each first-level indicator, and  $q$  is the number of the first-level indicators:

$$P_i = \frac{100 - k_i}{\sum_1^n (100 - k_i)} \times 100\%. \quad (2)$$

$P_i$  is the investment ratio of the  $i$ th area,  $k_i$  is the score of the status of the distribution network of the  $i$ th area, and  $n$  is the number of the planning areas.

## INVESTMENT RATIO BASED ON EVALUATION OF INVESTMENT BENEFIT

### Indicator System

In view of the systematic, comprehensive, and long-term characteristics of the investment benefit analysis of power grid projects, the evaluation indicator system, based on identifying the

factors affecting the investment benefit, contains these parts: production service benefits, production and operation benefits, investment economic benefits, and social and environmental benefits. The indexes selected are enumerated in **Figure 1**.

### Indicator Weight Calculation

The indicator system to evaluate investment benefit includes subjective and objective indicators so that the assessment of investment benefit can be more persuasive. The set-valued iterative method is a subjective weighting method, which can reflect experts' opinions concentratedly. The objective weight can be obtained by the entropy method, and the weight is modified through entropy weight calculation to make the weight scientific, objective, and feasible (Li et al., 2016; Li et al., 2019; Ge et al., 2021). Based on moment estimation theory, this study combines the results of the above two methods to obtain a comprehensive weight.

Considering the thought of moment estimation theory, it follows that the expected values of subjective and objective weight are the actual value of each indicator (Liu et al., 2019; Sakhthivel and Sathya, 2021).

The coefficients of colligation of the subjective and objective weight vector can be calculated using the actual value of each indicator, as shown in the following formula:

$$\begin{cases} \alpha_j = \frac{t_j}{t_j + s_j} \\ \beta_j = \frac{s_j}{t_j + s_j} \end{cases} \quad (3)$$

$\alpha_j$  refers to the subjective weight vector's coefficient of colligation,  $\beta_j$  refers to the objective weight vector's coefficient of colligation, and  $t_j$  and  $s_j$  refer to the  $j$ th index's subjective and objective weight, respectively.

Suppose the indicators are extracted from two sample systems. The coefficients of colligation of the total subjective and objective weight vectors, derived from the moment estimation theory, can be calculated in the following formula:

$$\alpha = \frac{\sum_{j=1}^n \alpha_j}{\sum_{j=1}^n \alpha_j + \sum_{j=1}^n \beta_j} = \frac{\sum_{j=1}^n \alpha_j}{n} \quad (4)$$

$$\beta = \frac{\sum_{j=1}^n \beta_j}{\sum_{j=1}^n \alpha_j + \sum_{j=1}^n \beta_j} = \frac{\sum_{j=1}^n \beta_j}{n} \quad (5)$$

$\alpha$  is the coefficient of colligation of the overall subjective weight vector,  $\beta$  is the coefficient of colligation of the overall objective weight vector, and  $n$  is the number of indicators.

A single-objective optimization model is constructed to minimize the deviation between the comprehensive weight and the subjective and objective weight (He et al., 2018; Zhang et al., 2018; Lai et al., 2019) as follows:

$$\min H = \sum_{j=1}^n \left[ \alpha \times (w_j - t_j)^2 \right] + \sum_{j=1}^n \left[ \beta \times (w_j - s_j)^2 \right] \quad (6)$$

$w_j$  refers to the  $j$ th index's comprehensive weight.

### Comprehensive Evaluation Result

The TOPSIS method can get the closeness of each scheme to the optimal scheme. Based on the combined weight derived from the above weight methods, a TOPSIS evaluation model for investment benefit is established, assessing the pros and cons of the schemes (Zou et al., 2017). The key steps to calculate the comprehensive evaluation value of distribution network investment benefit based on the TOPSIS method are as follows:

#### 1) Multi-objective decision matrix:

Suppose the index set is  $C = (C_1, C_2, \dots, C_m)$ , the plan set is  $M = (M_1, M_2, \dots, M_n)$ , and the evaluation value of scheme  $M_j$  to index  $C_i$  is  $r_{ij} = (i = 1, 2, \dots, n; j = 1, 2, \dots, m)$ . Then, the matrix R of evaluation values is constructed as follows:

$$R = \begin{bmatrix} r_{11} & r_{12} & \dots & r_{1m} \\ r_{21} & r_{21} & \dots & r_{2m} \\ \dots & \dots & \dots & \dots \\ r_{n1} & r_{n2} & \dots & r_{nm} \end{bmatrix} \quad (7)$$

#### 2) Positive and negative ideal solution calculation:

$$h_i^+ = \max(h_{i1}^+, h_{i2}^+, \dots, h_{im}^+), h_i^- = \min(h_{i1}^-, h_{i2}^-, \dots, h_{im}^-) \quad (8)$$

$h_i^+$  is the positive ideal solution vector,  $h_i^-$  is the negative ideal solution vector, and  $h_i$  refers to the ideal solution vector of the  $i$ th indicator.

#### 3) Relative distance calculation:

$$K_j^+ = \sqrt{\sum_{i=1}^n (h_{ij} - h_i^+)^2}, i = 1, 2, \dots, n; j = 1, 2, \dots, m \quad (9)$$

$$K_j^- = \sqrt{\sum_{i=1}^n (h_{ij} - h_i^-)^2}, i = 1, 2, \dots, n; j = 1, 2, \dots, m \quad (10)$$

$K_j^+$  is the difference between the  $j$ th scheme and the positive ideal solution, and  $K_j^-$  is the difference between the  $j$ th scheme and the negative ideal solution.

#### 4) Comprehensive evaluation value:

$$C_j = \frac{K_j^-}{K_j^- + K_j^+}, j = 1, 2, \dots, m \quad (11)$$

$C_j$  refers to the comprehensive evaluation value of the  $j$ th scheme.

### Investment Ratio Calculation

According to the comprehensive evaluation value of investment benefit, the result is normalized, and the investment distribution ratio of each region can be obtained as follows:

$$Q_j = \frac{C_j}{\sum_{j=1}^n C_j} \times 100\% \quad (12)$$

$Q_j$  is the investment ratio,  $C_j$  is the comprehensive evaluation value, and  $n$  refers to the amount of the planning regions.

### INVESTMENT ALLOCATION

After obtaining the investment ratios for the distribution network status assessment and investment benefit assessment, the final investment ratio can be obtained by weighted summation (Mohtashami et al., 2017; Ehsan and Yang, 2019). The calculation formula is as follows:

$$Z_i = \mu a_i + \nu b_i \quad (13)$$

where  $Z_i$  is the final investment proportion of the  $i$ th region,  $a_i$  represents the investment proportion of the  $i$ th planning area for the distribution network status assessment,  $b_i$  is the investment proportion of the  $i$ th planning area for investment benefit assessment, and  $\mu$  and  $\nu$  are the proportion coefficients of  $a_i$  and  $b_i$ , respectively.

In this article, comprehensively considering the network status and investment benefit assessment, the investment in the distribution network can be allocated reasonably. A district's investment allocation proportion of the network is estimated.

When calculating the investment proportion for the distribution network status assessment, the investment proportion is lower for the regions with a higher score of the status of the distribution network. Otherwise, the investment should be increased. When calculating the investment proportion based on the evaluation of investment benefit, the region with a higher score of investment benefit should increase more investment. Otherwise, the investment should be reduced. The estimated investment allocation ratios are reasonable and conform to the above laws. In the end, the investment proportion, which considers the development status of the distribution network and investment benefit, is calculated. A region with a high score of the status of the distribution network has a low investment ratio. After considering the investment benefit, when the investment benefit is excellent, the final investment proportion will be increased. Compared with the methods in the current research, which only consider the status of the distribution network or investment benefit, this method is more reasonable, and the results of investment distribution match the network development trend.

## DISCUSSION AND CONCLUSION

The dimension of the existing investment allocation indicator system for the distribution network is single. It is difficult to achieve high precision of investment distribution. Therefore, this study studies a precise method of investment allocation based on the network status and investment benefit assessment system. Firstly, the distribution network status is evaluated and the investment proportion can be obtained through normalization. Then, an investment calculation model based on the assessment of investment benefit is constructed, and the investment

distribution ratio is estimated by normalizing the comprehensive evaluation value of investment benefit. Finally, an investment forecast model of the distribution network is built by balancing the influence of the status of the distribution network and investment benefit on investment allocation. Applying the research results to the decision-making of the investment distribution in a certain area has a guiding significance for investment allocation of the distribution network. In future studies, it is necessary to increase the hierarchy and diversity of the investment allocation indicator system to achieve a more ideal effect of investment distribution.

## AUTHOR CONTRIBUTIONS

JY and SW drafted the manuscript. ZS, JH, and JL participated in the indicator system building. SL reviewed and edited the manuscript. SW and ZS analyzed and interpreted the calculation results. All authors examined and revised the manuscript.

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