



# Production Performance Analysis for Deviated Wells in Carbonate Gas Reservoirs With Multiple Heterogeneous layers

Jianlin Guo, Bo Ning\*, Haijun Yan, Chengye Jia and Yilong Li

*Petro China Research Institute of Petroleum Exploration and Development, Beijing, China*

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### \*Correspondence:

Bo Ning  
ningbo07@petrochina.com.cn

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Deviated wells are used to improve the performance of carbonate reservoirs with multiple heterogeneous layers and penetrate the “sweet spot” of each layer, which is full of fractures and vugs. It is difficult to consider in-layer and inter-layer heterogeneities simultaneously, and predict the production performance for these wells accurately. Therefore, a semi-analytical model to analyze the production performance of deviated wells in a multilayer heterogeneous stress-sensitive carbonate gas reservoir is proposed. For each layer, the inner region is a fractured-vuggy porous medium, while the outer region is merely a tight formation with matrix and formation properties, and penetrated inclination angles may be distinct. Pseudo-time/pressure factors are introduced to consider fracture stress sensitivity. Through the application of Laplace transformation, Fourier transform and inverse, Duhamel convolution, and Stehfest numerical inversion, the presented model is solved. The validity of this model is verified through comparison with single-layer composite formation with different porous mediums and vertical well in a multilayer carbonate gas reservoir. Moreover, by matching bottom-hole pressure data collected from a slanted well in the Anyue gas field, the applicability of this model is validated. A synthetic case, which has two composite formations, the first (upper) layer is more permeable than the second (lower) layer, is used to study the variations of inner region radius, fracture/matrix permeability, and inclination angles on production behaviors. The results show the properties of the first layer determine well bottom-hole pressure, whereas the rise of permeability, inner region radius and penetrated angle for the second layer can improve the gas recovery of this layer. In practice, to maintain well bottom-hole pressure with a relatively high level and enhance gas recovery of the tight layer, the inclination angle should be larger than 60° for each layer, and be increased to as large as possible. The findings of this study can help for a better understanding of the production behaviors of deviated wells in multilayer heterogenous reservoirs and could provide some guidance for the design of well trajectory.

**Keywords:** production behavior, deviate well, composite formation, stress sensitivity, multilayer carbonate gas reservoir

## 1 INTRODUCTION

In many carbonate gas reservoirs, there are multiple distinct layers, and there is strong heterogeneity in different directions. Some regions have rich natural fractures, vugs, and are named the “sweet spot,” while other areas are tight and contain only matrix (Jia and Yan, 2014; Ma, et al., 2021; Yan, et al., 2020b). Through the utilization of advanced 3D seismic inversion technology, we can precisely determine the location of the “sweet spot” for each layer. As the distribution of the “sweet spot” is random, to improve the production performance and economic benefits, a deviated well is always used to penetrate the “sweet spot” of different layers. However, the range of the “sweet spot” is limited, which makes the formation exhibit composite properties, and it is difficult to consider this distribution pattern for different layers simultaneously (Jia, et al., 2013; Jia, et al., 2014; Yan, et al., 2020a). Moreover, the gas flow in the slanted wellbore is always complicated, and it is difficult to estimate the production performance. Hence, a reasonable model that can describe the gas flow in a deviated wellbore for multi-layer heterogeneous carbonate gas reservoir is essential. In addition, this model can also be used to differentiate the production contribution for each layer.

For each layer in a multi-layer heterogeneous carbonate gas reservoir, it is an independent composite formation. For vertical wells in a composite reservoir, many mathematical models have been developed and analytical or semi-analytical solutions obtained. Some researchers employ these models to analyze pressure transient behaviors, to estimate production performance, and to acquire the reservoir and technical parameter values, such as the formation radius, reservoir permeability, and skin factor (Olarewaju and Lee, 1987; Prado and Da, 1987; Olarewaju and Lee, 1989; Turki, et al., 1989; Kikani and Jr, 1991; Olarewaju and Lee, 1991; Satman, 1991). In the above mentioned models, under diverse circumstances, the inner area can be a fractured dual-porosity or triple-porosity formation, while the outer area is a tight reservoir. Except for the conventional reservoirs, these models have been widely used in unconventional reservoirs. For unconventional reservoirs, after stimulated reservoir volume (SRV) fracturing with horizontal wells, it is always assumed that the region surrounding the horizontal wellbore is dual porosity or triple-porosity media, while the other regions are tight formations. After reasonable modifications on the previous models, various composite models for describing MFHWs are presented to estimate the pressure and production rate transient behaviors (Zeng, et al., 2015; Zhao, et al., 2014; Wang, et al., 2017). Due to the difficulties of solving these mentioned models, finite element and boundary elements have been employed to obtain numerical solutions (Fan, et al., 2015; Rana and Ertekin, 2012; Wu, et al., 2018). Except for vertical and horizontal wells, recently, Meng, et al. (2018) presented a composite model for deviated wells, where the natural triple-porosity reservoir is in the inner area and the outer area is the tight matrix. However, currently, this proposed model can only be used in a composite formation with a single layer.

In terms of vertical wells in multi-layer reservoirs, many studies have analyzed for pressure and production behaviors, and these studies always assume that the pressure, reservoir and

fluids properties, and boundary conditions are different from each other. (Cobb, et al., 1972; Raghavan, et al., 1974; Larsen, 1981; Kuchuk and Wilkinson, 1991; El-Banbi and Wattenbarger, 1996; El-Banbi and Wattenbarger, 1997; Vieira Bela, et al., 2019). For some complex well types, the methods to obtain production behaviors are different from traditional approaches. Through comprehensive reviews, there are primarily three methods that can model gas flowing process, equivalent approximation, numerical, and analytical or semi-analytical approaches. For the equivalent approximation method, the wellbore in the perforated formation is approximately simplified into uniform flux fracture and modified with transient skin factor (Larsen, 1999; Larsen, 2000), which is greatly different from real circumstances. Numerical approaches, for example, the boundary or finite element method, can be utilized to obtain the pressure or production solution for complex wells in a multi-layer reservoir (Jongkittinarukorn and Tiab, 1998; Kuchuk and Habashy, 1996; Kuchuk and Saeedi, 1992), while it is difficult to use and time-consuming. Through the combination of the reflection and transmission principle, and the methods of Laplace transformation, Fourier transformation, and inversion, semi-analytical or analytical solutions can be acquired for these complex-structure wells in multi-layer formation with or without crossflow (Basquet, et al., 1999; Medeiros, et al., 2010; Pan, et al., 2010), whereas the accuracy for these solutions is not satisfied.

Through the above introductions for composite reservoir and multi-layer formation with diverse well structures, studies on composite models mainly apply to vertical and horizontal wells, although Meng et al. (2018) presented the composite model for deviated wells in carbonate gas reservoirs, they assumed that the reservoir has one layer merely. In addition, Meng et al. (2021) proposed a model for analyzing the production performance of slanted wells in multilayer carbonate reservoirs, whereas the interlayer heterogeneity is ignored. For the modeling of multi-layer formation in a complex well structure, the accuracy, efficiency, and applicability for the mentioned three methods should be improved further. Hence, in this article, a semi-analytical model is presented for deviated wells in multilayer heterogeneous carbonate gas reservoirs, where the individual layer is represented with triple-porous media in the inner region and a single porous medium in the outer region. The main novelty of this study lies in the consideration of in-layer and inter-layer heterogeneities simultaneously for stress-sensitive carbonate gas reservoirs with multiple layers. Furthermore, through the combination of some approaches, such as Laplace transform, Stehfest numerical inverse, Fourier transformation and inversion, Duhamel convolution, the pressure and production solutions for deviated wells are obtained.

The structure of this paper first presents physical and mathematical models, and the detailed solution process for this model is given. The validity of this presented model is then verified through a comparison of results with published data and a gas field case. Finally, the influences of prevailing factors, such as radius and natural fractures permeability for the inner region, matrix permeability for the outer region, and the penetrated inclination angle, on the production performance of individual layers are discussed and analyzed.



**TABLE 1** | Definition of dimensionless variables for layer  $j$ .

Variables	Equation	Variables	Equation
Dimensionless length of $x$ coordinate	$x_{jD} = \frac{x}{r_w} \sqrt{\frac{1}{k_{fij}}}$	Dimensionless production rate	$q_{jD} = \frac{q_{s2} B_{gj}}{(Q_{sc} B_{g1})}$
Dimensionless length of $y$ coordinate	$y_{jD} = \frac{y}{r_w} \sqrt{\frac{1}{k_{fij}}}$	Dimensionless pseudo-pressure for fractures system	$m_{fjD} = \frac{(k_{fi} h / \mu_{gi})(m_{ij} - m_{fi})}{a_p (Q_{gs} B_{g1})}$
Dimensionless vertical distance	$z_{jD} = \frac{z}{r_w}$	Dimensionless pseudo-pressure of vugs system	$m_{vjD} = \frac{(k_{vi} h / \mu_{gi})(m_{ij} - m_{vi})}{a_p (Q_{gs} B_{g1})}$
Dimensionless length of mid-perforation in $x$ coordinate	$x_{wjD} = \frac{x_{wi}}{r_w} \sqrt{\frac{1}{k_{fij}}}$	Dimensionless pseudo-pressure of matrix in inner region	$m_{m1jD} = \frac{(k_{m1} h / \mu_{gi})(m_{ij} - m_{m1})}{a_p (Q_{gs} B_{g1})}$
Dimensionless length of mid-perforation in $y$ coordinate	$y_{wjD} = \frac{y_{wi}}{r_w} \sqrt{\frac{1}{k_{fij}}}$	Dimensionless pseudo-pressure of matrix in outer region	$m_{m2jD} = \frac{(k_{m2} h / \mu_{gi})(m_{ij} - m_{m2})}{a_p (Q_{gs} B_{g1})}$
Dimensionless vertical space of mid-perforation	$z_{wjD} = \frac{z_{wi}}{r_w}$	Dimensionless pseudo-pressure at initial condition	$m_{ijD} = \frac{(k_{fi} h / \mu_{gi})(m_{ij} - m_i)}{a_p (Q_{gs} B_{g1})}$
Dimensionless radius	$r_{jD} = \frac{r}{r_w} \sqrt{\frac{1}{k_{fij}}}$	Dimensionless wellbore pseudo-pressure with unit rate	$m_{wfjD} = \frac{(k_{fi} h / \mu_{gi})(m_{ij} - m_{wfj})}{a_p (Q_{gs} B_{g1})}$
Dimensionless radius of inner region	$R_{1jD} = \frac{R_{1j}}{r_w} \sqrt{\frac{1}{k_{fij}}}$	Dimensionless wellbore transient pseudo-pressure	$m_{wfjD} = \frac{(k_{fi} h / \mu_{gi})(m_{ij} - m_{wfj})}{a_p (Q_{gs} B_{g1})}$
Dimensionless radius of outer region	$R_{2jD} = \frac{R_{2j}}{r_w} \sqrt{\frac{1}{k_{fij}}}$	Dimensionless wellbore pseudo-pressure	$m_{wD} = \frac{(k_{fi} h / \mu_{gi})(m_{ij} - m_{wD})}{a_p (Q_{gs} B_{g1})}$
Dimensionless infinitesimal variable	$\varepsilon_{jD} = \frac{\varepsilon}{r_w} \sqrt{\frac{1}{k_{fij}}}$	Dimensionless pseudo-time	$t_D = a_t \left[ \frac{k_{fi}}{(\varphi C_1)_{(1+m_1+c_1)\mu_{gi}}} + \frac{k_{m2}}{(\varphi C_1)_{m_2\mu_{gi}}} \right] \frac{\beta t}{r_w^2}$
Dimensionless formation thickness	$h_{jD} = \frac{h_j}{r_w}$	Interporosity flow coefficient of fractures and matrix	$\lambda_{m1j} = \alpha_{m1j} \frac{k_{m1j}^2}{k_{fij}} \frac{1}{r_w}$
Diffusivity coefficient ratio of inner region	$\eta_{1jD} = \frac{\eta_{1j}}{\eta_i}$	Interporosity flow coefficient of fractures and vugs	$\lambda_{vj} = \alpha_{vj} \frac{k_{vj}^2}{k_{fij}} \frac{1}{r_w}$
Diffusivity coefficient ratio of outer region	$\eta_{2jD} = \frac{\eta_{2j}}{\eta_i}$	Storativity ratio of matrix for inner region	$\omega_{m1j} = \frac{(\varphi C_1)_{m1j}}{(\varphi C_1)_{(1+m_1+c_1)j}}$
Mobility coefficient ratio of inner region	$M_{1j} = \frac{(k_{fi} h / \mu_{gi})}{(k_{vi} h / \mu_{gi})}$	Storativity ratio of vugs for inner region	$\omega_{vj} = \frac{(\varphi C_1)_{vj}}{(\varphi C_1)_{(1+m_1+c_1)j}}$
Mobility coefficient ratio of outer region	$M_{2j} = \frac{(k_{m2} h / \mu_{gi})}{(k_{vi} h / \mu_{gi})}$	Storativity ratio of fractures for inner region	$\omega_{ij} = 1 - \omega_{m1j} - \omega_{vj}$

Since the perforated inclined wellbore in the individual layer is seamed as the line source with uniform flux, based on the superposition principle, and the rotation transform of coordination developed by Ozkan and Raghavan (1991a), Ozkan and Raghavan (1991b), the dimensionless pressure in Laplace space for the deviated well section in layer  $j$  could be acquired by integrating on Eq. 2 numerically, and the expression can be written as

$$\begin{aligned} \bar{m}_{wfjD} = & \frac{m_{ijD}}{s} + \frac{1}{sM_{1j}L_{wjD}} \int_{-L_{wjD}/2}^{L_{wjD}/2} \left[ \frac{q_{0j}U_{0j} - \frac{M_{2j}}{M_{1j}}T_{0j}S_{0j}}{q_{0j}W_{0j} + \frac{M_{2j}}{M_{1j}}T_{0j}V_{0j}} I_0(q_{0j}\tilde{r}_{jD}) \right. \\ & \left. + K_0(q_{0j}\tilde{r}_{jD}) \right] d\xi \\ & + \frac{2}{sM_{1j}L_{wjD}} \int_{-L_{wjD}/2}^{L_{wjD}/2} \sum_{n=1}^{\infty} \left[ \frac{q_{nj}U_{nj} - \frac{M_{2j}}{M_{1j}}T_{nj}S_{nj}}{q_{nj}W_{nj} + \frac{M_{2j}}{M_{1j}}T_{nj}V_{nj}} I_0(q_{nj}\tilde{r}_{jD}) \right. \\ & \left. + K_0(q_{nj}\tilde{r}_{jD}) \right] \cos\left(n\pi \frac{\tilde{z}_{wjD}}{h_{jD}}\right) \cos\left(n\pi \frac{z_{wjD}}{h_{jD}}\right) d\xi \end{aligned} \tag{3}$$

where

$$\begin{aligned} \tilde{r}_{jD} = & \sqrt{[x_{jD} - (x_{wjD} + \xi \sin \theta'_j)]^2 + (y_{jD} - y_{wjD})^2}, \tilde{z}_{wjD} \\ = & z_{wjD} + \xi \cos \theta'_j \\ L_{wjD} = & \frac{L_{wj}}{r_w} \sqrt{\frac{k_{fij}}{k_{fiij}} \sin^2 \theta_j + \frac{k_{fij}}{k_{fiij}} \cos^2 \theta_j}, \theta'_j = \arctan \left( \tan \theta_j \sqrt{\frac{k_{fviij}}{k_{fiij}}} \right) \end{aligned} \tag{4}$$

$L_{wjD}$  is the dimensionless length for the deviated well section in layer  $j$  and  $\theta'_j$  is equivalent inclination angle. If the deviated wellbore is treated as an infinite-conductivity line source, it is more similar to reality. An equivalent point is then chosen to obtain the well bottom-hole flowing pressure (Wang, et al., 2012). The coordination of this point is:

$$\begin{aligned} x_{jD} = x_{wjD} + \frac{0.3L_{wj} \sin \theta_j}{r_w} \sqrt{\frac{k_{fij}}{k_{fiij}}}, y_{jD} = \sqrt{\frac{k_{fij}}{k_{fiij}}}, \\ z_{jD} = z_{wjD} + \frac{0.3L_{wj} \cos \theta_j}{r_w} \sqrt{\frac{k_{fij}}{k_{fviij}}} \end{aligned} \tag{5}$$

### 2.3.2 Evaluation on Production Performance for Deviated Wells

As the formation pressure and properties are different for diverse layers, the gas production rate for each layer may vary with time. For this situation, it could be handled with the Duhamel theorem (Spath, et al., 1990), and the general formula could be obtained:

$$m_{wfjD} = m_{ijD} + \int_0^{t_D} q_{jD} \frac{\partial}{\partial \tau} m_{wfjD}(t_D - \tau) d\tau \tag{6}$$

According to the principle of Laplace transformation, Eq. 6 can be transformed as:

$$\bar{m}_{wfjD} = \frac{m_{ijD}}{s} + \bar{q}_{jD} (s\bar{m}_{wfjD} - m_{ijD}) \tag{7}$$

The bottom-hole flowing pressure for any layer is seen as equally:

$$\bar{m}_{wfjD} = \bar{m}_{wD} \tag{8}$$

After the simple transformation on Eq. 7, the dimensionless production rate in the Laplace domain  $\bar{q}_{jD}$  for layer  $j$  can be expressed by:



$$\bar{q}_{jD} = \frac{\bar{m}_{wfjD} - \frac{m_{ijD}}{s}}{s\bar{m}_{wfjD} - m_{ijD}} = \frac{\bar{m}_{wD} - \frac{m_{ijD}}{s}}{s\bar{m}_{wfjD} - m_{ijD}} \quad (9)$$

It can be seen from Eq. 6 that the sum of dimensionless production rate for all layers is equal to one. After the Laplace transformation about dimensionless production rate term, substituting Eq. 9 into Eq. 7, then the dimensionless bottom-hole flowing pressure in Laplace domain could be written as:

$$\bar{m}_{wD} = \frac{1 + \sum_{j=1}^n \frac{m_{ijD}}{s\bar{m}_{wfjD} - m_{ijD}}}{\sum_{j=1}^n \frac{s}{s\bar{m}_{wfjD} - m_{ijD}}} \quad (10)$$

Substituting the solution of the inclined well section,  $\bar{m}_{wfjD}$ , Eq. 3 into Eq. 10, thus in Laplace space the dimensionless well bottom-hole flowing pressure could be obtained, and  $\bar{q}_{jD}$  could also be calculated through the substitution of Eqs 3, 10 into Eq. 9.

The Stehfest numerical inverse presented by Schmittroth (1960) is used in Eqs 9, 10, to acquire the dimensionless pressure and production data in real space. According to the definitions of these two dimensionless variables in Table 1, for layer  $j$ , the gas production rate and pseudo well bottom-hole flowing pressure can be obtained. Through the utilization of the method presented by Meng et al. (2018), the gas production rate of individual formation and the well bottom-hole flowing pressure can be calculated at each time step. The detailed solution procedures can also be found in the paper by Meng et al. (2018).

### 3 MODEL VALIDATION

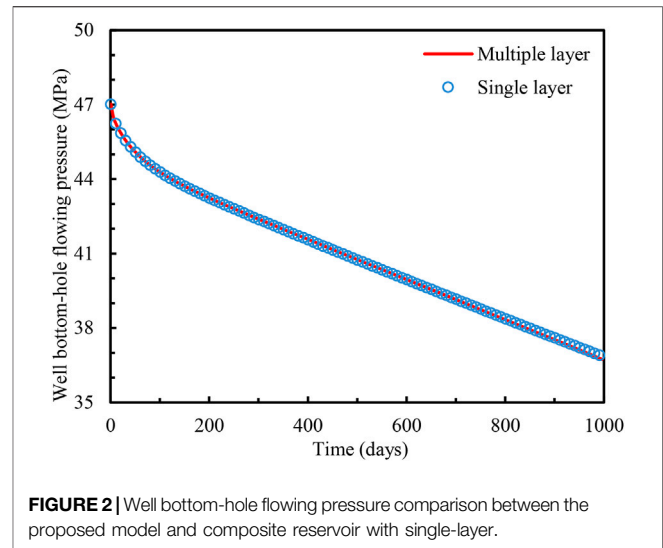
#### 3.1 Comparisons With Previous Models

##### 3.1.1 Comparison With Composite Single-Layer Reservoir

Meng et al. (2018) first presented the solution for deviated wells in composite formation with a single layer, which is the basis of the multilayer composite reservoir model in this paper. In their model, the inner region is naturally fractured-vuggy formation, while the outer region is tight formation, and the slanted wellbore is just located in the inner region, which is identical with the assumption in this paper. When formation properties and inclination angle are the same for different layers, then the multilayer reservoir is simplified into the single-layer reservoir theoretically. With the synthetic case constructed by Meng et al. (2018) (the data can be found in their published paper), the well bottom-hole pressure can be calculated. Since Meng et al. (2018) do not give the value of well production rate, hence, in this case, the production rate is set to be 100,000 m<sup>3</sup>/d. Figure 2 shows the comparison result of calculated well bottom-hole flowing pressure solution between single-layer formation and multilayer reservoir with uniform properties. As shown in Figure 2, there is a good match between the single-layer and multilayer reservoir, which verifies the accuracy of the proposed model.

##### 3.1.2 Comparison With Vertical Well in Carbonate Gas Reservoir With Multiple Layers

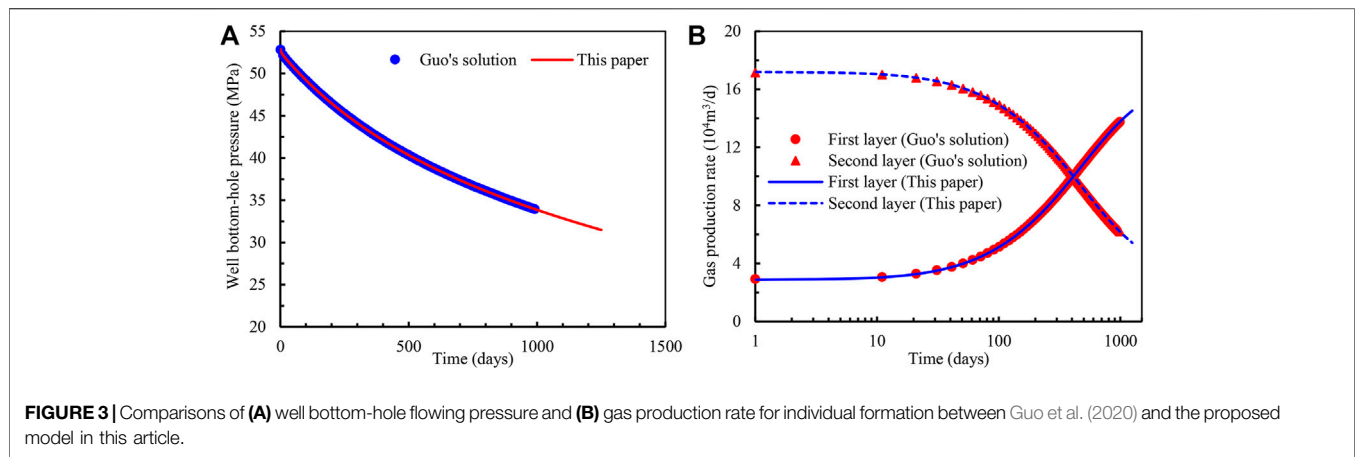
Guo et al. (2020) present semi-analytical solutions for vertical wells in multi-layer gas reservoirs. For the proposed model in this



paper, when the deviated angle is approaching 0°, the properties of the inner and outer regions for the individual layer are identical. The model in this paper is then simplified into the model presented by Guo et al. (2020). The comparisons of bottom-hole pressure and production rate of each layer for these two models are shown in Figure 3. The relevant data to calculate the results can be found in the published paper by Guo et al. (2020), in which the synthetic case in this paper is used. It can be seen from Figure 3 that there is a good match of bottom-hole pressure and production rate of individual layers for these two models, which verifies the validity of the proposed model. In addition, compared with the model presented by Guo et al. (2020), besides the application on the vertical wells in multilayer reservoirs, the proposed model can also be employed in the production behavior evaluation of inclined wells, which indicates that the proposed model in this paper is more general.

#### 3.2 Match With Field Data

To validate the proposed model further and demonstrate its applicability in practice, a case study was chosen, the Anyue carbonate gas reservoir. In this case, the reservoir has two layers, and both 3D seismic interpretation and drilling data show that the deviated well penetrates the “sweet spot” for each layer, where the region surrounding the wellbore is a fractured-vuggy formation that has lots of natural fractures, and the region far from the well is a tight formation with matrix. In this multilayer reservoir, for each layer, through the method of well logging, the formation thickness, porosity, and water saturation for fractures, vugs and matrix are obtained and through the method of well-testing analysis, the permeability, inter-porosity flowing coefficients, initial pressure and temperature of the reservoir can be acquired. The well trajectory and inclination angle can be obtained from drilling data. The detailed formation and fluid information for this case are given in Table 2. It should be noted that formation anisotropy represents the horizontal-vertical permeability ratio.



**FIGURE 3** | Comparisons of (A) well bottom-hole flowing pressure and (B) gas production rate for individual formation between Guo et al. (2020) and the proposed model in this article.

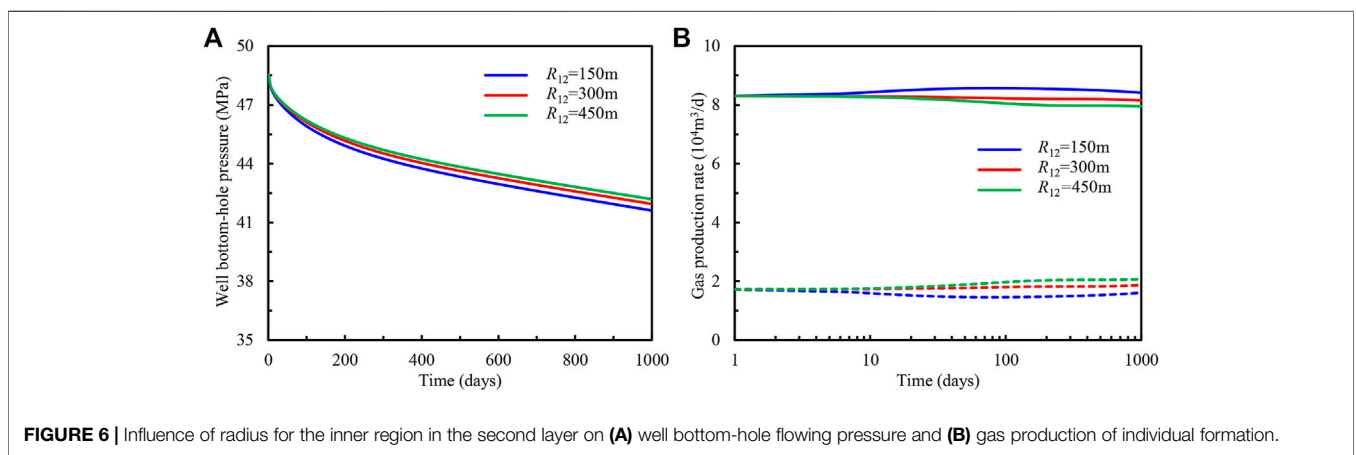
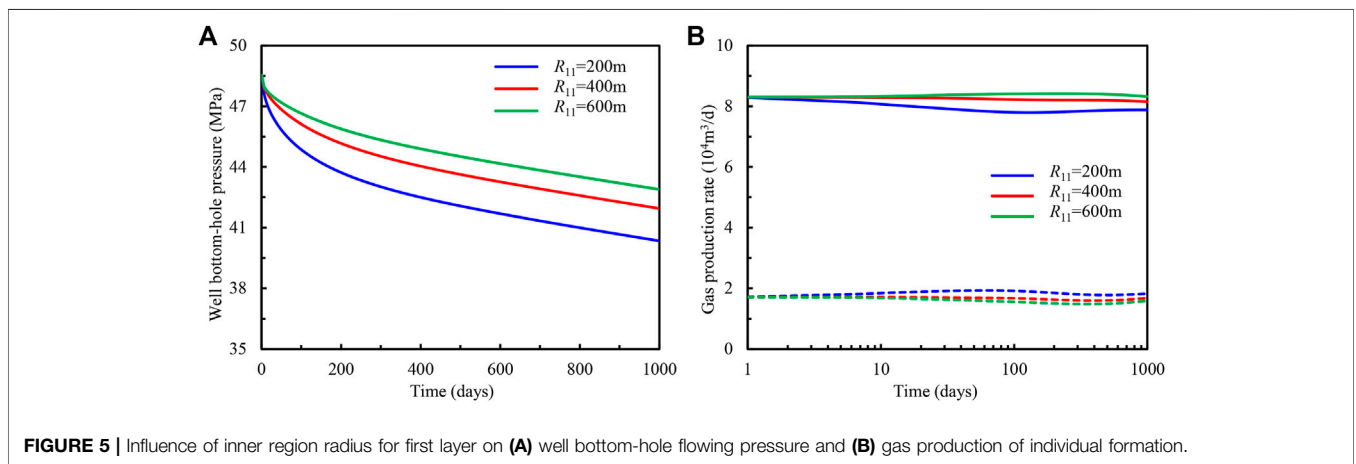
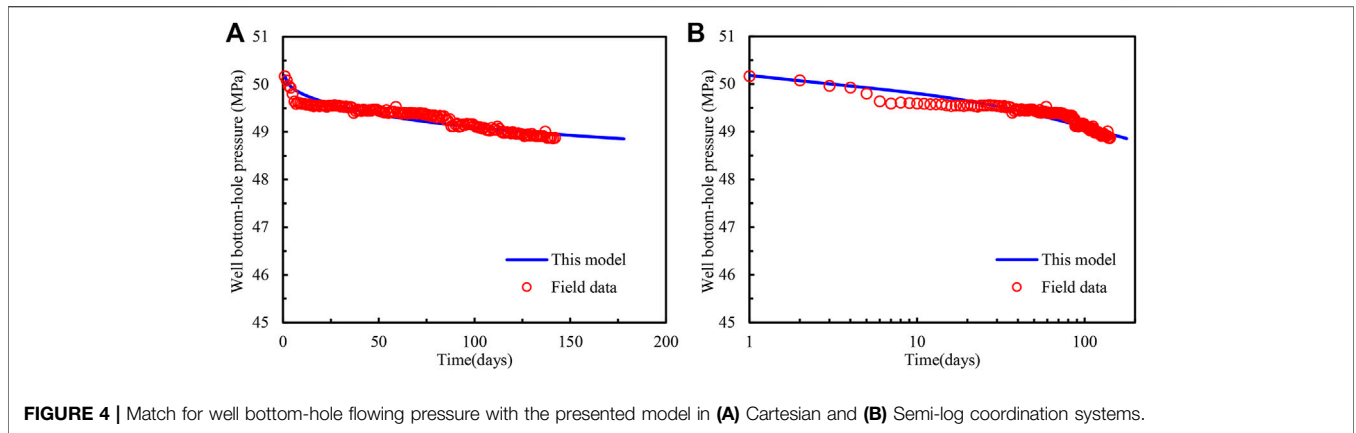
**TABLE 2** | Reservoir, fluids, and production data applied on the field and synthetic cases.

Parameters	Field case		Synthetic case	
	Value (first layer)	Value (second layer)	Value (first layer)	Value (second layer)
Formation thickness/m	24.1	1.2	15	10
Formation radius/m	2,895.8	1,224.5	2,000	1,500
Inner region radius/m	510.5	201.4	400	300
Natural fractures porosity/%	0.15	0.1	0.15	0.1
Vugs porosity/%	1.84	1.21	1.5	2
Matrix porosity of inner region/%	1.5	1.5	2.5	1.5
Matrix porosity of outer region/%	2.06	1.51	3	2.5
Initial fractures horizontal permeability of inner region/ $10^{-3}\mu\text{m}^2$	2.03	0.35	1.5	0.5
Initial matrix horizontal permeability of outer region/ $10^{-3}\mu\text{m}^2$	0.95	0.11	0.5	0.1
Formation anisotropy degree	6.1	6.1	6	6
Water saturation of matrix/%	13.2	23.7	10	20
Interporosity flowing coefficient of natural fractures and matrix	$1 \times 10^{-7}$	$1 \times 10^{-7}$	$1 \times 10^{-7}$	$1 \times 10^{-7}$
Interporosity flowing coefficient of natural fractures and vugs	$1 \times 10^{-5}$	$1 \times 10^{-5}$	$1 \times 10^{-5}$	$1 \times 10^{-5}$
Stress-sensitive power exponent	0.738	0.738	0.738	0.738
Initial reservoir pressure/MPa	51.4	51.8	51	51.5
Overburden stress/MPa	137.9	138.9	134.6	141.3
Reservoir temperature/ $^{\circ}\text{C}$	153	154.3	150	155
Inclination angle/ $^{\circ}$	75	71	75	60
Wellbore radius/m	0.1		0.1	
Gas production rate/( $\text{m}^3/\text{d}$ )	99,500		100,000	
Production time/d	150		1,000	
Specific gravity	0.59		0.59	
Critical pressure/MPa	4.82		4.82	
Critical temperature/K	199.3		199.3	

Since there is a lack of separate layer test information, the well bottom-hole flowing pressure information is acquired to match calculated data with the presented model. Figure 4 shows the comparison of well bottom-hole pressure in Cartesian and semi-log coordination systems. The goal of the introduction of the semi-log scale is the presentation of the initial fitting effect. It can be seen that whether for the Cartesian or semi-log coordination system, the curves fit perfectly between the testing well bottom-hole pressure and this model, which indicates this model could calculate the well bottom-hole flowing pressure precisely, and verifies the practicality of it in examining multilayer heterogeneous carbonate gas reservoirs.

### 4 SENSITIVITY ANALYSIS ON THE PRODUCTION PERFORMANCE

According to the information of the field case, a synthetic case, which is shown in Table 2, was constructed to analyze the influences of prevailing factors for multilayer heterogeneous composite reservoirs, such as the radius of the inner region, horizontal permeability of fractures, horizontal permeability of matrix and penetrated inclination angle of the individual layer on production performance, which include the well bottom-hole flowing pressure and gas production rate of individual formation.

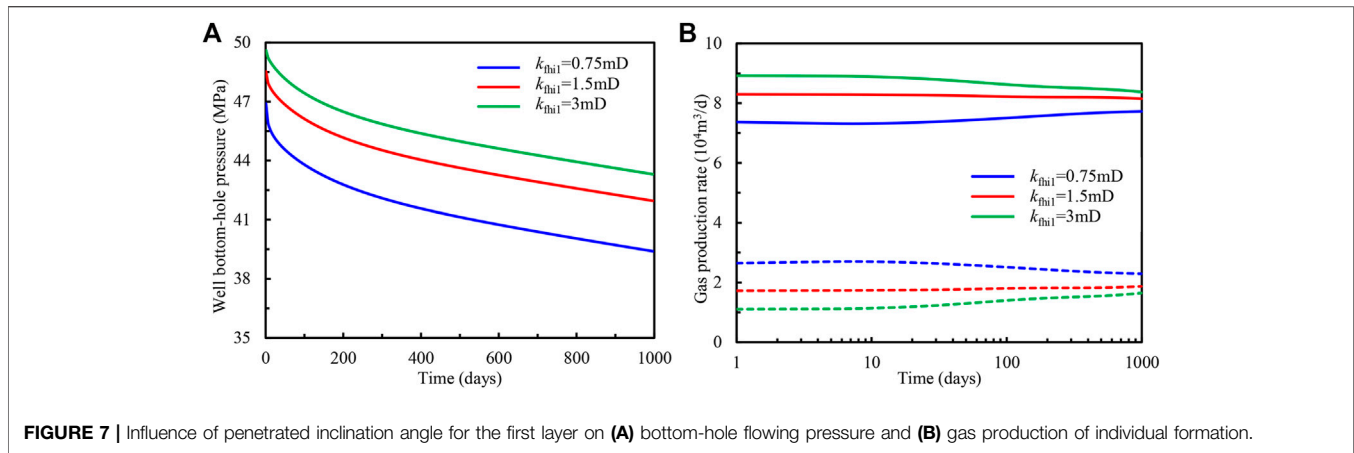


### 4.1 Inner Region Radius

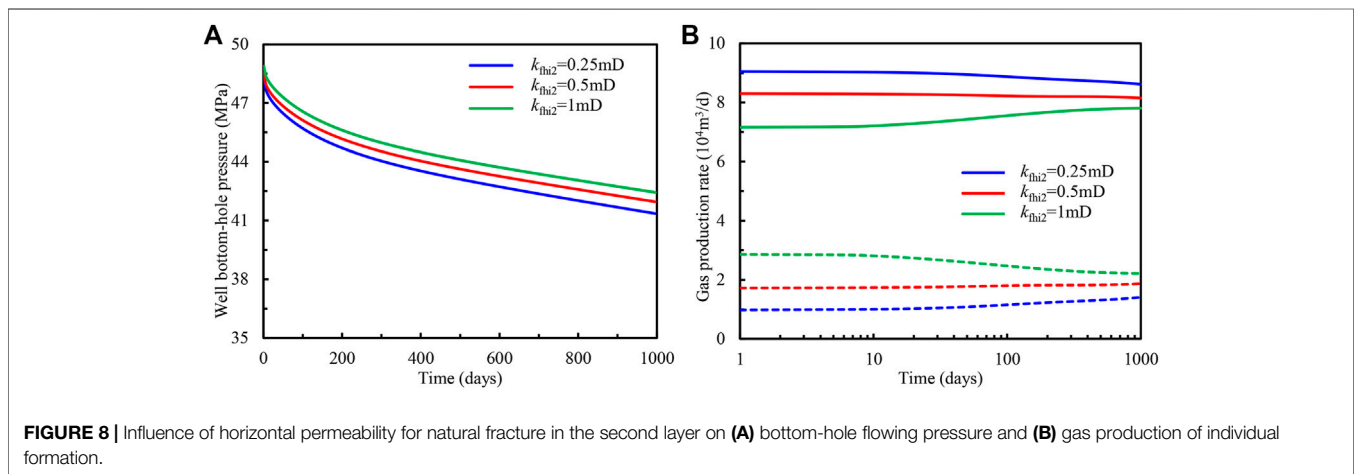
Figures 5, 6 show the influences of inner region radius for first and second formations on the production performance of deviated well and individual layers. It should be noted that in Figures 5B, 6B, the gas production rate for the first layer and second layer are represented with solid and dashed lines,

respectively To clearly show the early production distribution, the semi-log scale is used in these figures.

Through the comparison of Figures 5A, 6A, it is easy to see the variation of radius for the inner region in the first layer has a greater effect on well bottom-hole pressure. The reason for this phenomenon is that the first layer has a larger thickness,



**FIGURE 7** | Influence of penetrated inclination angle for the first layer on (A) bottom-hole flowing pressure and (B) gas production of individual formation.



**FIGURE 8** | Influence of horizontal permeability for natural fracture in the second layer on (A) bottom-hole flowing pressure and (B) gas production of individual formation.

porosity, and formation permeability (see **Table 2**), which is the main layer in this multilayer heterogeneous carbonate gas reservoir. The increase of inner region radius for this layer can greatly improve the level of well bottom-hole pressure. Since the gas production mainly derives from the inner region initially, hence, before the pressure response reaches the interface between the inner region and outer region, the production rate of gas for each layer is identical. As the inner region has larger porosity and permeability, on the condition of constant well production rate, with the increase of range for the inner region, the production rate of gas for any layer increases with the rise of inner region radius for this layer. In addition, the increase of inner region radius will delay the time of reaching this interface, then in **Figures 5B, 6B**, the time of emerging discrepancy for different cases increases with the inner region radius.

#### 4.2 Horizontal Permeability of Fractures

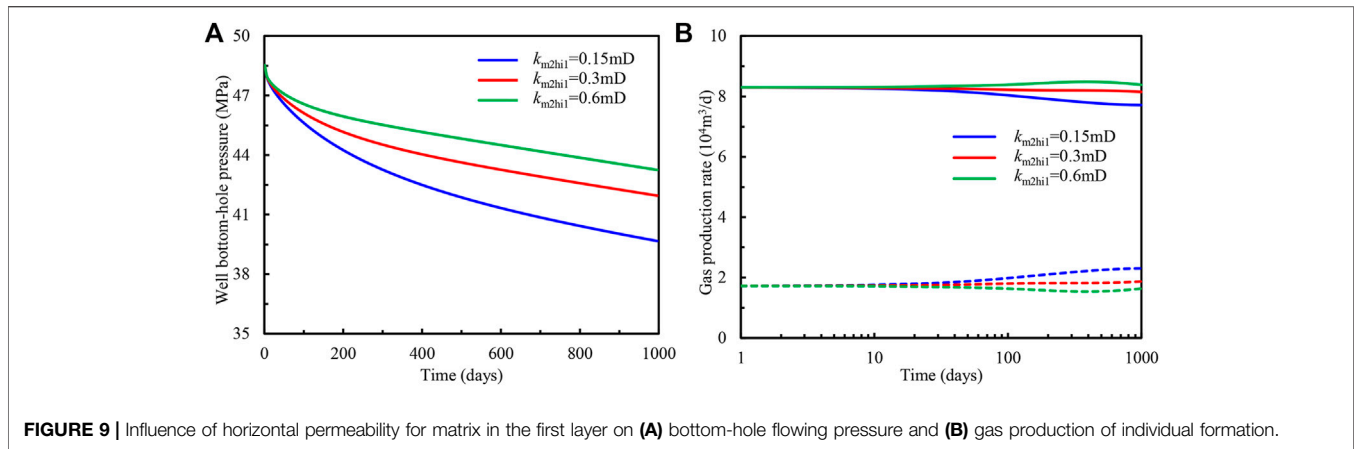
The influences of horizontal permeability for natural fracture in the inner region on production behaviors are given in **Figures 7, 8**. As the first layer is the main formation in this multilayer heterogeneous carbonate gas reservoir, the variation law in **Figures 7A, 8A** is

analogous to the curves in **Figures 5A, 6A**, and the rise of fracture horizontal permeability for the first layer can increase the well bottom-hole pressure significantly, whereas the fracture horizontal permeability of the second layer has little effect on the well bottom-hole pressure. However, since the inner region contributes mostly to the well gas production at the initial stage, and the flowing capacity increases with the fracture horizontal permeability, in contrast with **Figures 5B, 6B**, in **Figures 7B, 8B** gas production rate for any layers has a huge initial gap for different scenarios. When the gas production rate from the outer region occupies the larger ratio, the impact of the inner region decreases, and the gaps for different cases reduce continuously. It should be noted that because we assumed that the deviated well produces with a constant rate, while the gas production rate for some formations increases, for other formations it would certainly decline. For example in **Figure 7B**, with the rise of the horizontal permeability of natural fractures for the first formation, the production rate for this formation increases, while for the second layer, the production rate decreases.

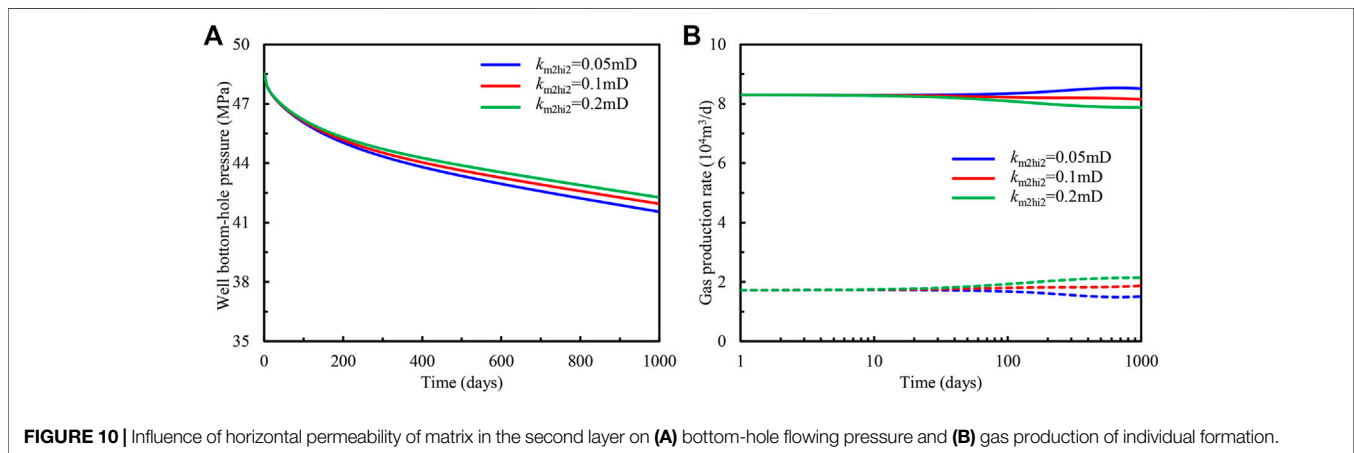
#### 4.3 Horizontal Permeability of Matrix

Since the outer region has a larger area than the inner region, it is important to evaluate the influences of horizontal permeability of





**FIGURE 9** | Influence of horizontal permeability for matrix in the first layer on (A) bottom-hole flowing pressure and (B) gas production of individual formation.



**FIGURE 10** | Influence of horizontal permeability of matrix in the second layer on (A) bottom-hole flowing pressure and (B) gas production of individual formation.

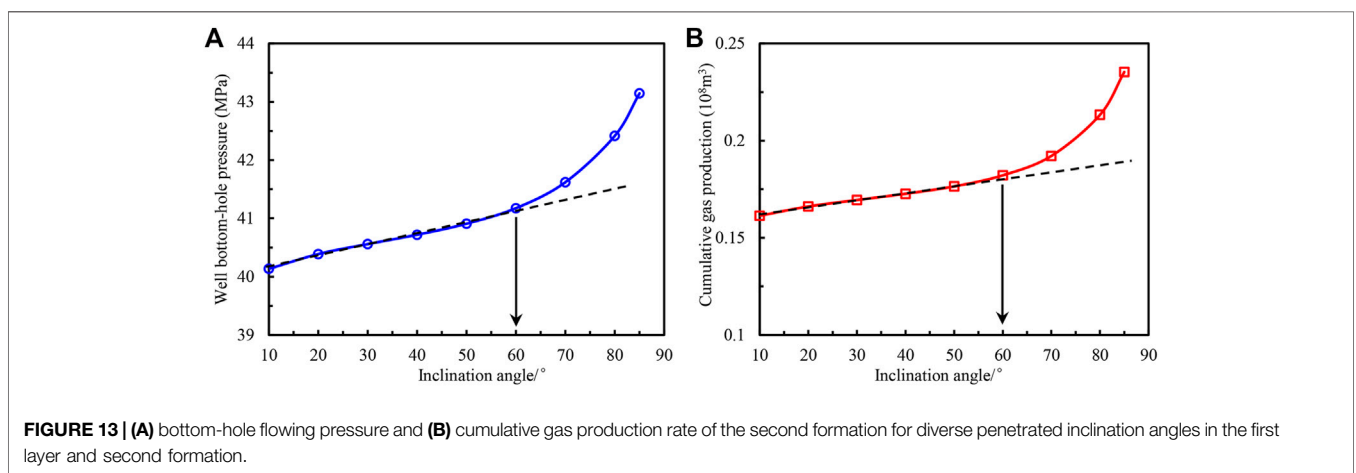
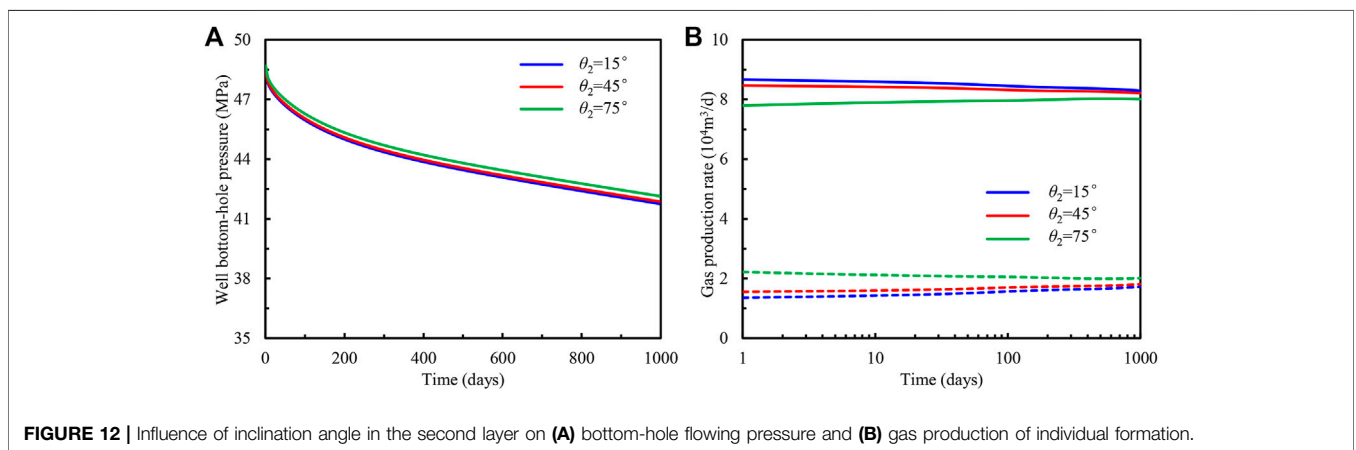
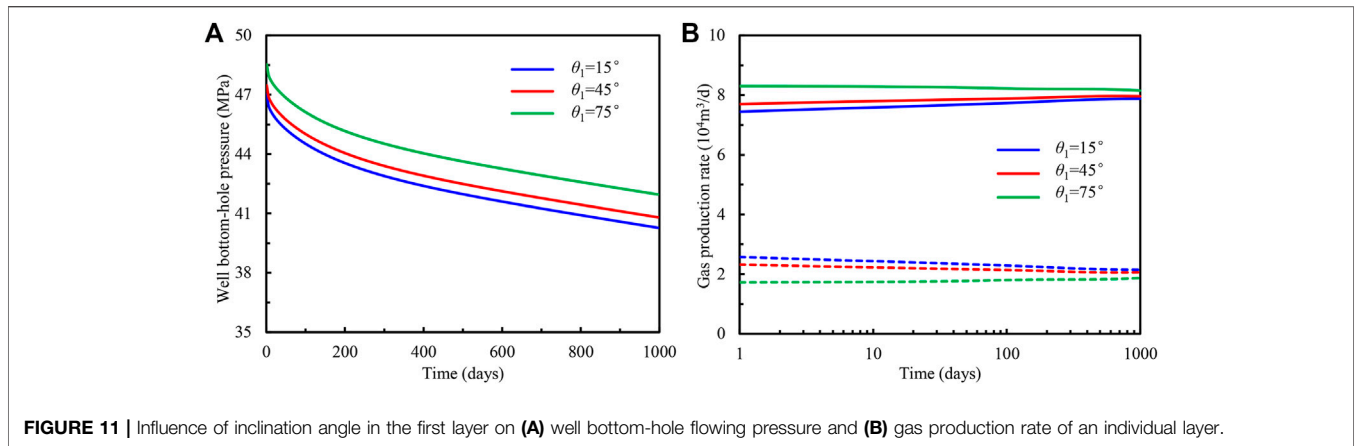
matrix on production behaviors, which are given in **Figures 9, 10**. It can be seen that as the gas supply capacity of the outer region increases with the matrix horizontal permeability, although the well bottom-hole flowing pressure and production rate of gas for different layers are the same for different cases initially, when the time is larger than 30 days, whether for the first or second layers, obviously, these two production index increase with the matrix horizontal permeability of this layer. Compared with **Figures 5B, 6B** and **Figures 7B, 8B**, in **Figures 9B, 10B**, as the radius of the inner region and permeability of natural fractures are equal, hence, there are no discrepancies of well bottom-hole flowing pressure and production rate initially, and the moment of appearing difference are nearly the same for different cases. Furthermore, through the comparison of **Figures 7A, 9A**, it can be seen that the smaller variation of matrix permeability can cause the huge gaps of bottom-hole pressure, which indicates that the properties of the outer region determine the production behaviors of the deviated well.

#### 4.4 Inclination Angle

During the exploitation of the multilayer reservoir with the deviated well, the design of the well trajectory is an important task. It is then crucial to investigate the influence of the

inclination angle for each layer on the production performance of individual zone and well bottom-hole flowing pressure (**Figures 11, 12**). Since the contact area between the slanted wellbore and formation increases with the inclination angle, as shown in **Figures 11, 12**, the well bottom-hole flowing pressure and gas production rate of the first or second layer increase with the penetrated inclination angle in this layer. As it was assumed that the slanted wellbore is located only in the inner region, the variation of inclination angle influences the production rate distribution at the early stage (**Figures 11B, 12B**), which is analogous to **Figures 7B, 8B**. **Figure 10** shows the increase of inclination angle for the first layer with larger gas reserve and permeability, the well bottom-hole pressure can be improved largely. Therefore, to keep the well bottom-hole pressure at a high level, the penetrated inclination angle must be greater than a certain value. In addition, as shown in **Figure 12**, the inclination angle for the second layer has few influences on the well bottom-hole flowing pressure, whereas it can greatly increase the production rate of gas for this layer, which demonstrates the gas recovery of tight formation can be enhanced by enlarging the inclination angle in this layer.

To determine the critical values of inclination angle for the first and second layers, we plot the curves of the inclination angle



for the first layer versus bottom-hole flowing pressure and the inclination angle for the second layer versus cumulative gas production, which is shown in **Figure 13**.

Note that the bottom-hole flowing pressure and the cumulative gas production are collected on the 1,000th day. While the inclination angle is smaller than 60°, there is a linear relationship between the

inclination angle and bottom-hole flowing pressure or cumulative gas production. When the inclination angle is larger than 60°, the bottom-hole flowing pressure and cumulative gas production increase drastically, whether it is the first layer or the second layer, the critical value of inclination angle for these two layers is 60°. To keep the bottom-hole pressure at a relatively high level and enhance

the gas recovery of the tight layer, the penetrated inclination angle should be greater than  $60^\circ$ , and be enlarged as much as possible.

## 5 SUMMARY AND CONCLUSION

In this paper, a semi-analytical model is proposed to evaluate the production behaviors for slanted wells in commingled carbonate gas reservoirs with multiple heterogeneous layers. Through the comparison with the bottom-hole flowing pressure for a slanted well in a single layer, composite fractured-vuggy carbonate gas reservoir, the validity of this model is verified. Furthermore, a field case in the Anyue carbonate gas reservoir is employed to demonstrate the applicability of this model in practice. Through sensitivity analysis for some prevailing factors, several important conclusions can be drawn:

- (1) The rise of radius for the inner region, horizontal permeability of fractures, horizontal permeability of matrix, and inclination angle for some layers can lead to the increase of well bottom-hole flowing pressure and enlarge the production rate of gas for this formation.
- (2) The main layer with larger permeability and gas reserve determines the level of well bottom-hole flowing pressure and contributes mostly to the production of deviated wells. The influence of inner region properties, such as fracture horizontal permeability and radius, is limited, and the well production performance mainly depends on the properties of the outer region.
- (3) To keep the well bottom-hole pressure at a relatively high level and enhance the gas recovery from the less permeable layer, the penetration inclination angle for the first and second layers should be larger than  $60^\circ$ , and be enlarged as much as possible.

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## DATA AVAILABILITY STATEMENT

The raw data supporting the conclusion of this article will be made available by the authors, without undue reservation.

## AUTHOR CONTRIBUTIONS

JG and BN proposed original ideas for this paper. HY and CJ contributed to the modeling, programming, result analysis, and discussion. This paper was written by HY and YL. JG and BN provided technical guidance for research work and reviewed the paper.

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## SUPPLEMENTARY MATERIAL

The Supplementary Material for this article can be found online at: <https://www.frontiersin.org/articles/10.3389/fenrg.2022.861780/full#supplementary-material>

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## GLOSSARY

$B_g$	Gas formation volume factor, $m^3/sm^3$	$\alpha_m, \alpha_c$	Shape factors of matrix and vugs, $1/m^2$
$C_g$	Gas compressibility, $MPa^{-1}$	$\beta$	Pseudo-time factor
$C_t$	Total compressibility, $MPa^{-1}$	$\lambda$	Interporosity flow coefficient, dimensionless
$h$	Formation thickness, mHorizontal direction	$\omega$	Storativity ratio, dimensionless
$k$	Permeability, $10^{-3} \mu m^2$	$\eta$	Hydraulic diffusivity, dimensionless
$k_{ra}$	Formation anisotropy degree	$\theta$	Inclination angle, degree
$L_w$	Slanted well length, m	$\mu_g$	Gas viscosity, mPa-s
$m$	Pseudo-pressure, MPaMatrix system	$\varphi$	Porosity, fraction
$m_{wf}$	Wellbore pseudo-pressure, MPa	$\sigma_s$	Overburden pressure, MPa
$M$	Mobility ratio	$a_t, a_p$	Constants, $a_t = 86.4, a_p = 1.842 \times 10^{-3}$
$p$	Pressure, MPa	$i$	Initial condition
$p_{avg}$	formation average pressure, MPa	$0$	Standard condition
$p_{wf}$	Wellbore pressure, MPa	$m$	Pseudo-pressure, MPaMatrix system
$q_g$	Gas production rate, $m^3/d$	$f$	Natural fractures system
$\tilde{q}$	Production rate from point source, $m^3/d$	$c$	Vugs system
$r$	Radial distance, mReference condition	$r$	Radial distance, mReference condition
$r_w$	Wellbore radius, m	$w$	Wellbore
$R_c$	Formation radius, m	$j$	$j$ th layer
$s$	Laplace transform variable	$1$	Inner region
$t$	Time, day	$2$	Outer region
$x, y, z$	Directional coordinates	$h$	Formation thickness, mHorizontal direction
$x_w, y_w, z_w$	Distance of mid-perforation in $x, y$ and $z$ coordinates, m	$v$	Vertical direction
$\alpha$	Stress-sensitive power exponent, dimensionless	$D$	Dimensionless
		$\bar{\phantom{x}}$	Laplace domain
		$\hat{\phantom{x}}$	Fourier domain