



# Numerical Study on the Effect of Jet Cross Section Shape on the Corium Jet Breakup Behavior With Lattice Boltzmann Method

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In a core meltdown accident in light water reactors, molten corium may drop into the lower plenum of the pressure vessel and interact with water, which is called fuel-coolant interaction (FCI). The behavior of the corium jet breakup in water during FCIs is important for the in-vessel retention strategy and has been extensively studied. While in previous studies, the jet cross-section shapes are naturally assumed to be circular, which is actually not always the case, in this study, the breakup processes of the corium jets with four different elliptical cross-section shapes and three different penetration velocities are simulated with color-gradient lattice Boltzmann method. The effect of the cross-section shape on the hydrodynamic breakup behavior of the corium jet is analyzed in detail. It is found that the effect of the cross-section shape on the jet penetration depth is very limited. With the increase in the aspect ratio under the same penetration velocity, the jet breakup length decreases gradually. In general, the dimensionless corium surface area increases with the increase in the aspect ratio for the jets under the same penetration velocity.

Keywords: fuel-coolant interaction (FCI), corium jet breakup, effect of jet cross-section shape, lattice Boltzmann method, jet breakup length

# **1 INTRODUCTION**

During a core meltdown accident in light water reactors (LWRs), molten corium may drop into the lower plenum of the reactor vessel and interact with water, which is called fuel-coolant interaction (FCI). The design of the in-vessel retention (IVR) strategy requires the full understanding of the physical phenomena related to FCIs, especially the corium jet breakup process which will significantly affect the formation of the debris bed and the subsequent in-vessel cooling. The corium jet breakup behavior in water has been extensively studied with real core material experiments, simulant material experiments, and various simulations (Spencer et al., 1994;Burger et al., 1995;Dinh et al., 1999;Huhtiniemi et al., 1999;Abe et al., 2006;Thakre et al., 2015;Zhou et al., 2017;Iwasawa and Abe 2018;Saito et al., 2018;Shen et al., 2018;Cheng et al., 2019;Cheng et al., 2020; Cheng et al., 2021a;Cheng et al., 2021b). To the best of authors' knowledge, in almost all of the previous studies, the jet cross-section shapes are naturally assumed to be circular, which is actually not always the case. In fact, when the molten corium drops from the edge of the core, through the structures or the cracks of the corium crust, the corium jets are very likely to have different cross-section shapes depending on the specific situations (Corradini et al., 1988). This leads to the

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Cheng H, Cheng S and Wang J (2022) Numerical Study on the Effect of Jet Cross Section Shape on the Corium Jet Breakup Behavior With Lattice Boltzmann Method. Front. Energy Res. 10:834237. doi: 10.3389/fenrg.2022.834237 investigation of the effect of jet cross-section shape on the corium jet breakup behavior, which was generally ignored in previous studies.

Since the interaction between the molten corium jet and water involves very complex thermal hydraulics phenomena such as boiling heat transfer, corium jet breakup, and corium solidification, it is not easy to get the effect of jet cross-section shape directly from the experimental results with such complex phenomena. On the other hand, more quantitative results can be directly extracted from the numerical results, among which the lattice Boltzmann method (LBM) has become a powerful tool in analyzing the complex multiphase flow in recent years (Saito et al., 2017). LBM is the so-called mesoscopic simulation method between the microscopic particle-based (molecular dynamics) and macroscopic Navier-Stokes-based methods. Compared with conventional CFD methods, it has the following advantages: 1) based on the molecular kinetic theory; 2) easy to program and parallelize; 3) interface tracking is not needed; and 4) applicable to complex geometries (Huang et al., 2015;Krüger et al., 2016). As one of the two-phase LBM methods, the color-gradient LBM employs two components to represent two immiscible fluids; one component is the red-colored fluid and the other is the bluecolored fluid. Its main advantages lie in strict mass conservation for each fluid and flexibility in adjusting the interfacial tension (Ba et al., 2016). To simplify the complex situation involved, in the current study, the hydrodynamic phenomena are decoupled from the thermal phenomena and studied separately for the corium jet breakup process with the state-of-the-art GPUaccelerated color-gradient LBM.

In this study, the breakup process of the corium jets with four different elliptical cross-section shapes and three different penetration velocities are simulated with color-gradient LBM. The effect of the cross-section shape on the hydrodynamic breakup behavior of the corium jet is analyzed in detail.

# 2 COLOR-GRADIENT LATTICE BOLTZMANN METHOD

In our previous studies, the improved color-gradient LBM with non-orthogonal central-moment MRT has been successfully developed and used to study the hydrodynamic breakup process of melt jets with circular cross-section in both sodium-cooled fast reactors (SFRs) (Cheng et al., 2020) and LWRs (Cheng et al., 2021b), thanks to its advantages in multiphase flow modeling and the enhanced numerical stability for flows with high Reynolds numbers. Here, this model is adopted in the current work to explore the effect of jet cross-section shape on the corium jet hydrodynamic breakup behavior. The details of the improved color-gradient LBM are introduced as follows.

The D3Q27 lattice is adopted; the discrete lattice velocity  $c_i$  in the D3Q27 framework is defined as

where index i = 0, 1, ..., 26,  $c = \delta_x / \delta_t$  is the lattice speed,  $\delta_t$  is the time step, and  $\delta_x$  is the lattice spacing.

Two immiscible fluids are represented by pseudo red fluid and blue fluid, respectively. The distribution function,  $f_i^k$ , is used to represent the fluid k, namely, k = r denotes "red" color, k = bdenotes the "blue" color, and i is the index of the lattice-velocity direction.  $f_i = f_i^r + f_b^i$  is the total distribution function with evolution equation defined as

$$f_i^k(\mathbf{x} + \mathbf{c}_i \delta_t, t + \delta_t) - f_i^k(\mathbf{x}, t) = \Omega_i^k(\mathbf{x}, t),$$
(2)

where x and t represent the position and time. The collision operator  $\Omega_i^k$  is composed of the following sub-operators

$$\Omega_i^k = \left(\Omega_i^k\right)^{(3)} \left[ \left(\Omega_i^k\right)^{(1)} + \left(\Omega_i^k\right)^{(2)} \right],\tag{3}$$

where  $(\Omega_i^k)^{(1)}$  is the single-phase collision operator,  $(\Omega_i^k)^{(2)}$  is the perturbation operator, and  $(\Omega_i^k)^{(3)}$  is the recoloring operator.

### 2.1 Single-Phase Collision Operator

The single-phase collision operator with non-orthogonal central moment MRT is defined as

$$(\Omega)^{(1)}(|f\rangle) = |f\rangle - M^{-1}N^{-1}KNM(|f\rangle - |f^{(e)}\rangle) + |F\rangle, \quad (4)$$

where transformation matrix M transforms distribution functions from velocity space into raw moment space. The shift matrix N transfers raw moments to central moments. Krepresents the relaxation matrix. Here, "ket" operator  $|.\rangle$  denotes the column vector. For details on the transformation matrix M, the shift matrix N, the non-orthogonal central-moment matrix NM, and the relaxation matrix K, refer to Cheng et al. (2021b).  $|f\rangle$  denotes the discrete forcing term, which is given by

$$|F\rangle = M^{-1}N^{-1}\left(I - \frac{1}{2}K\right)NM|F'\rangle, \tag{5}$$

where I is a unit matrix,  $|F\rangle = (F_0, F_1, \dots, F_{26})^T$ , and  $|F\rangle' = (F'_0, F'_1, \dots, F'_{26})^T$ ,  $F'_i$  is defined as

$$F_i' = \omega_i \left[ 3 \frac{\mathbf{c}_i - \mathbf{u}}{c^2} + 9 \frac{(\mathbf{c}_i \cdot \mathbf{u})\mathbf{c}_i}{c^4} \right] \cdot \mathbf{F} \delta_t, \tag{6}$$

where F is the body force.

In the single-phase collision operator, the enhanced equilibrium distribution function (Leclaire et al., 2017) is used

$$f_{i}^{(e)}(\rho, \mathbf{u}) = \rho \left\{ \varphi_{i} + \omega_{i} \left[ \frac{3}{c^{2}} \left( \mathbf{c}_{i} \cdot \mathbf{u} \right) + \frac{9}{2c^{4}} (\mathbf{c}_{i} \cdot \mathbf{u})^{2} - \frac{3}{2c^{2}} \mathbf{u}^{2} + \frac{9}{2c^{6}} (\mathbf{c}_{i} \cdot \mathbf{u})^{3} - \frac{9}{2c^{4}} (\mathbf{c}_{i} \cdot \mathbf{u}) \mathbf{u}^{2} \right] \right\} + \Phi_{i}.$$
(7)

The weights,  $\omega_i$ , are as follows

$$\omega_i = \begin{cases} 8/27, & i = 0, \\ 2/27, & i = 1, 2, \dots, 6, \\ 1/54, & i = 7, 8, \dots, 18, \\ 1/216, & i = 19, 20, \dots, 26. \end{cases}$$
(8)

Meanwhile, we have

$$\varphi_{i} = \begin{cases} \bar{\alpha}, & |\mathbf{c}_{i}|^{2} = 0, \\ 2(1 - \bar{\alpha})/19, & |\mathbf{c}_{i}|^{2} = 1, \\ (1 - \bar{\alpha})/38, & |\mathbf{c}_{i}|^{2} = 2, \\ (1 - \bar{\alpha})/152, & |\mathbf{c}_{i}|^{2} = 3. \end{cases}$$
(9)

where  $\bar{\alpha}$  interpolates between  $\alpha_r$  and  $\alpha_b$  are as follows:

$$\bar{\alpha} = \frac{\rho_r}{\rho_r + \rho_b} \alpha_r + \frac{\rho_b}{\rho_r + \rho_b} \alpha_b,$$
(10)
$$\Phi_i = \begin{cases}
-3\bar{\nu} (\mathbf{u} \cdot \nabla \rho) / c, & |\mathbf{c}_i|^2 = 0, \\
+16\bar{\nu} (\mathbf{G}: c_i \otimes c_i) / c^3, & |\mathbf{c}_i|^2 = 1, \\
+4\bar{\nu} (\mathbf{G}: c_i \otimes c_i) / c^3, & |\mathbf{c}_i|^2 = 2, \\
+1\bar{\nu} (\mathbf{G}: c_i \otimes c_i) / c^3, & |\mathbf{c}_i|^2 = 3.
\end{cases}$$
(11)

where  $\otimes$  is the tensor product, ": " is the tensor contraction,  $\bar{v}$  is the kinematic viscosity interpolating between red fluid viscosity  $v_r$  and blue fluid viscosity  $v_b$  as

$$\frac{1}{\bar{v}} = \frac{\rho_r}{\rho_r + \rho_b} \frac{1}{v_r} + \frac{\rho_b}{\rho_r + \rho_b} \frac{1}{v_b}.$$
 (12)

 $\phi$  represents the order parameter distinguishing two fluids given by

$$\phi(\mathbf{x},t) = \frac{\rho_r(\mathbf{x},t) - \gamma \rho_b(\mathbf{x},t)}{\rho_r(\mathbf{x},t) + \gamma \rho_b(\mathbf{x},t)},$$
(13)

where  $\gamma$  denotes the density ratio between the red fluid and blue fluid.  $\phi = 1,-1, 0$  represent pure red fluid, pure blue fluid, and the interface. The tensor **G** in **Eq. 11** is given by

$$\mathbf{G} = \frac{1}{48} \left[ \mathbf{u} \otimes \nabla \rho + \left( \mathbf{u} \otimes \nabla \rho \right)^T \right].$$
(14)

To ensure stable interface,  $\gamma$  must satisfy the equation as

$$\gamma = \frac{\rho_r^0}{\rho_b^0} = \frac{1 - \alpha_b}{1 - \alpha_r},\tag{15}$$

where the superscript "0" over  $\rho_r^0$  or  $\rho_b^0$  represents pure fluid density. The fluid pressure is given based on the D3Q27 isothermal equation of state

$$p_k = \rho_k \left( c_s^k \right)^2 = \rho_k \frac{9(1 - \alpha_k)}{19} c^2.$$
(16)

In this study, we chose  $\alpha_b = 8/27$ , so that  $c_s^b = \frac{c}{\sqrt{3}}$  (Saito et al., 2017).

### 2.2 Perturbation Operator

The interfacial tension in the color-gradient LBM is modeled with the perturbation operator given by

$$(\Omega)^{(2)}(f_i) = f_i + A \left| \nabla \phi \right| \left[ \omega_i \frac{(\mathbf{c}_i \cdot \nabla \phi)^2}{\left| \nabla \phi \right|^2} - B_i \right], \tag{17}$$

where  $B_i$  represents the lattice dependent weight and is defined as

$$B_{i} = \begin{cases} -(10/27)c^{2}, & |\mathbf{c}_{i}|^{2} = 0, \\ +(2/27)c^{2}, & |\mathbf{c}_{i}|^{2} = 1, \\ +(1/54)c^{2}, & |\mathbf{c}_{i}|^{2} = 2, \\ +(1/216)c^{2}, & |\mathbf{c}_{i}|^{2} = 3. \end{cases}$$
(18)

The interfacial tension  $\sigma$  is defined as

$$\sigma = \frac{4}{9} A \tau c^4 \delta_t, \tag{19}$$

where  $\tau$  is the relaxation time, and it is assumed here that  $A = A_r = A_b$ .

### 2.3 Recoloring Operator

This operator is employed to maximize the amount of fluid k at interface near the fluid k side while remaining mass and momentum conservation laws. The recoloring operators are given by

$$(\Omega)^{(3)}\left(f_{i}^{r}\right) = \frac{\rho_{r}}{\rho}f_{i} + \beta\frac{\rho_{r}\rho_{b}}{\rho^{2}}\cos\left(\theta_{i}\right)f_{i}^{(e)}\left(\rho,0\right), \tag{20}$$

$$(\Omega)^{(3)}\left(f_{i}^{b}\right) = \frac{\rho_{b}}{\rho}f_{i} - \beta \frac{\rho_{r}\rho_{b}}{\rho^{2}}\cos\left(\theta_{i}\right)f_{i}^{(e)}\left(\rho,0\right),$$
(21)

where  $\beta$  is the segregation parameter related to the interface thickness,  $\theta_i$  is the angle between the lattice velocity and the order parameter gradient.

$$\cos\left(\theta_{i}\right) = \frac{\mathbf{c}_{i} \cdot \nabla\phi}{|\mathbf{c}_{i}| |\nabla\phi|}.$$
(22)

## 2.4 Streaming Operator

$$f_i^k(\mathbf{x} + \mathbf{c}_i \delta_t, t + \delta_t) = f_i^{k*}(\mathbf{x}, t),$$
(23)

where  $f_i^{k*}(\mathbf{x}, t)$  is the post-collision distribution function.

## 2.5 Macro Properties and Gradient Operator

The density of each fluid and the total fluid are defined as

$$\rho_k = \sum_i f_i^k, \tag{24}$$

$$\rho = \sum_{k} \rho_k. \tag{25}$$

The total momentum is defined as

$$\rho \mathbf{u} = \sum_{i} f_{i} \mathbf{c}_{i} + \frac{1}{2} \mathbf{F} \delta_{t}.$$
 (26)

The second-order isotropic central scheme is adopted to define the gradient operator for any function  $\chi$ 

$$\nabla \chi(\mathbf{x},t) = \sum_{i \neq 0} \frac{\omega_i \chi(\mathbf{x} + \mathbf{c}_i \delta_t, t) \mathbf{c}_i}{c_s^2 \delta_t}.$$
 (27)

# 3 COMPUTATIONAL DOMAIN AND PARAMETERS

The computational domain for the corium jet breakup process is presented in **Figure 1**, which includes a water pool and an inlet at the top surface where the corium jet is penetrated. The other surfaces are set as convective boundary conditions so that the dispersion of the corium will not be limited by the boundary of the computational domain. As an example, the convective boundary condition at the bottom surface is given by

$$\frac{\partial f_i^k}{\partial t} + u_z \frac{\partial f_i^k}{\partial z} = 0, \text{ at } z = 0,$$
(28)

where z = 0 denotes the nodes at the bottom surface. Using the first-order explicit discrete scheme, we have

$$f_{i}^{k}(x, y, 0, t + \delta_{t}) = \frac{f_{i}^{k}(x, y, 0, t) - u_{z}(x, y, 1, t) * f_{i}^{k}(x, y, 1, t)}{1 - u_{z}(x, y, 1, t)}.$$
(29)

The body force is given by

$$\mathbf{F}(\mathbf{x}, t) = \left(\rho(\mathbf{x}, t) - \rho_h^0\right)\mathbf{g},\tag{30}$$

where  $\mathbf{g} = (0, 0, -9.81 \ m/s^2)$ .

To study the effect of the jet cross-section shape on the corium jet hydrodynamic breakup behavior, the penetration processes of the corium jets with four different elliptical cross-section shapes and three different penetration velocities are simulated. The parameters for all 12 cases are presented in **Table 1**, where "a" is the semi-major axis of the ellipse, "b" is



the semi-minor axis of the ellipse, and "E = a/b" is the aspect ratio. All these elliptical cross-sections have the same area which is equal to a circular area with 10 mm diameter, so that the penetration flow rates remain the same for the corium jets with the same penetration velocity. The three penetration velocities V (2.21, 4.43, and 8.85 m/s) represent the typical free fall distances of the corium in the pressure vessel of LWRs ranging from 0.25 to 4.0 m.

In the current simulations, the corium is set to a mixture of 80% UO<sub>2</sub> and 20% ZrO<sub>2</sub> (mol%) with a melting point of 2,600°C. It is assumed that corium jet at 3,000°C is penetrated into water at 70°C. The thermophysical properties of the corium at 3,000°C and water at 70°C are presented in **Table 2** (Schins1978; Kirillov2006; Kolev 2015; Kim et al., 2017).

To conduct the simulations with LBM, all parameters are converted from physical units to lattice units based on **Eqs 31–34**, where D is the area equivalent diameter, D<sup>\*</sup> represents the lattice number along the area equivalent inlet diameter,  $\rho_r$  and  $\rho_b$  are the density of the red and blue fluid, respectively, and the jet inlet velocity V<sup>\*</sup> and the jet density  $\rho_r^*$  are set to 0.1 and 1.0, respectively. The parameter  $\beta$  is set to 0.7.

$$\rho_b^* = \frac{\rho_b}{\rho_r} \rho_r^*,\tag{31}$$

$$\nu_r^* = \frac{\mathrm{D}^* \mathrm{V}^*}{\mathrm{D} \mathrm{V}} \nu_r,\tag{32}$$

$$\nu_b^* = \frac{D^* V^*}{D V} \nu_b, \tag{33}$$

$$g^* = {DV^{*2} \over D^* V^2} g,$$
 (33a)

$$\sigma^* = \frac{\mathrm{D}^* \mathrm{V}^{*2} \sigma}{\mathrm{D} \mathrm{V}^2 \rho_r}.$$
 (34)

In our previous studies (Cheng et al., 2020; Cheng et al., 2021b), lattice number independent tests have been conducted by dividing the computational domain into 78\*78\*250,104\*104\*330, 130\*130\*410, and160\*160\*500 lattices, and it is found that the difference of the simulation results can be ignored for the last two; hence, 160\*160\*500 lattices with  $D^* = 30$  are used in the simulation of jet breakup process. The parameters in both physical units and lattice units with this lattice number are shown in Table 3. Meanwhile, the ability of the color-gradient LBM model to precisely predict the jet breakup process has also been validated using the results of molten wood's metal jet breakup experiments; it is found that the morphologies of the melt jet at different times in the experiment and simulation match very well (Cheng et al., 2021b).

## **4 RESULTS AND DISCUSSION**

### 4.1 Morphology of Corium Jet Breakup

The snap shots of corium jet breakup processes along both minor axis direction and major axis direction of the elliptical cross-section in the 12 cases are presented in **Figure 2**, where the interface between the corium and the

TABLE I Parameters of the conum lets with tour eliptical cross-sections and three velocity	TABLE 1	Parameters of the corium	iets with four elliptical	I cross-sections and three velocitie
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Case	Semi-major axis a (mm)	Semi-minor axis b (mm)	Aspect ratio E (-)	Penetration velocity v (m/s)		
1	5.0000	5.0000	1	2.21		
2	5.0000	5.0000	1	4.43		
3	5.0000	5.0000	1	8.85		
4	7.0711	3.5355	2	2.21		
5	7.0711	3.5355	2	4.43		
6	7.0711	3.5355	2	8.85		
7	8.6603	2.8868	3	2.21		
8	8.6603	2.8868	3	4.43		
9	8.6603	2.8868	3	8.85		
10	10.0000	2.5000	4	2.21		
11	10.0000	2.5000	4	4.43		
12	10.0000	2.5000	4	8.85		

#### TABLE 2 | Thermophysical properties of the corium.

Thermophysical properties	(UO <sub>2</sub> ) <sub>0.8</sub> (ZrO <sub>2</sub> ) <sub>0.2</sub>	Water		
Melting point [°C]	2,600	0		
Temperature [°C]	3,000	70		
Density [kg/m <sup>3</sup> ]	8,302	978		
Density ratio to water	8.49	1.0		
Kinematic viscosity [m <sup>2</sup> /s]	7.35e-7	4.13e-7		
Surface tension [N/m]	0.484	-		

water is extracted from the simulation results. It can be seen that for all 12 cases under different conditions, a mushroom-shaped leading edge can be observed immediately after the penetration due to the drag force, and then both the jet leading edge and jet column start to break up under the effect of Rayleigh-Taylor instability and Kelvin-Helmholtz instability, respectively; lots of small fragments are generated along with the penetration process.

Qualitatively, it is easy to find that more fragments are generated with the increase in the penetration velocity for the corium jets with the same aspect ratio (e.g., comparing Case 1, Case 2, and Case 3). The effect of the aspect ratio on the generated fragments for the corium jets with the same penetration velocity is not directly based on these figures, which is further analyzed quantitatively in **Section 4.4** Nevertheless, it can be noticed that with the increase in the aspect ratio, the jet becomes more flat and more fragments are distributed along the major axis direction than along the minor axis direction.

## 4.2 Jet Penetration Depth

The penetration depth versus time of the corium jet under three different penetration velocities is presented in **Figure 3.** From these figures, it can be seen that the effect of the cross-section shape on the jet penetration depth is very limited. The penetration depth changes little even when the aspect ratio changes from 1 to 4. This is because the penetration depth is mainly affected by the drag force; though the aspect ratio changes a lot, the drag force still changes very little for jets with the same penetration velocity and cross-section area.

## 4.3 Jet Breakup Length

The jet breakup length, the distance from free surface to the breakup point, is an important parameter to evaluate whether molten corium will directly come in contact with the lower plenum of the pressure vessel before it sufficiently breaks up.

	Parameters in physical units									
	D[m]	V[m/s]	ρ <sub>r</sub> [kg/m³]	ρ <sub>b</sub> [kg/m³]	ν <sub>r</sub> [m <sup>2</sup> /s]	ν <sub>b</sub> [m <sup>2</sup> /s]	g[m/s <sup>2</sup> ]	σ <b>[N/m]</b>	γ	Re
Case 1, 4, 7, 10	0.01	2.21	8,302	978	7.35e-7	4.13e-7	9.81	0.484	8.49	3.01e4
Case 2, 5, 8, 11	0.01	4.43	8,302	978	7.35e-7	4.13e-7	9.81	0.484	8.49	6.03e4
Case 3, 6, 9, 12	0.01	8.85	8,302	978	7.35e-7	4.13e-7	9.81	0.484	8.49	1.20e5
					Parameters in la	attice units				
	D*	V*	ρ <sub>r</sub> *	$ ho_b^*$	$\nu_r^*$	$\nu^*_b$	g*	σ*	γ	Re
Case 1, 4, 7, 10	30	0.1	1	0.118	9.98e-5	5.61e-5	6.70e-6	3.58e-4	8.49	3.01e4
Case 2, 5, 8, 11	30	0.1	1	0.118	4.98e-5	2.80e-5	1.67e-6	8.91e-5	8.49	6.03e4
Case 3, 6, 9, 12	30	0.1	1	0.118	2.49e-5	1.40e-5	4.18e-7	2.23e-5	8.49	1.20e5

TABLE 3 | Parameters in physical units and lattice units





Once the length is longer than the water depth, the pressure vessel is likely to be melted through by the molten corium, which might cause the radioactive material leakage (Iwasawa



and Abe 2018). In the melt jet breakup experiments, the jet breakup length usually can hardly be measured directly from the observation because the jet column is covered by lots of fragments similar to those in Figure 2, while with the simulations in the current study, the jet breakup length can be easily extracted from the middle cross-sectional density contours as shown in Figure 4, where Case 4 and Case 10 are presented. The breakup position can be easily observed from these figures. It should be noted that the jet column may break up in one middle cross-section view (e.g., major axis direction) but actually still connect in another middle crosssection view (e.g., minor axis direction) since the jet morphology is not axially symmetric. Hence, the jet column should be disconnected in both views when checking the breakup point. Furthermore, the breakup point usually fluctuates during the penetration process; here, the maximum jet breakup length is used as the jet breakup length in this study.

The dimensionless jet breakup length is defined as

$$\frac{L_{brk}}{D} / \left(\frac{\rho_j}{\rho_c}\right)^{0.5},$$
 (35)

where  $L_{brk}$  is the jet breakup length, the area equivalent diameter D is 10 mm for all 12 cases,  $\rho_j$  is the density of the jet, and  $\rho_c$  is the density of the water.

The dimensionless jet breakup length versus aspect ratio in the 12 cases is shown in **Figure 5**. First, it is clear that with the



increase in the penetration velocity under the same aspect ratio, the breakup length decreases gradually. This is because higher penetration velocity will enhance the stripping from the jet column due to the Kelvin–Helmholtz instability, and the material is removed from the jet column faster, which leads to the faster disconnection of the jet column and the shorter breakup length.

It can also be found that with the increase in the aspect ratio under the same penetration velocity, the jet breakup length decreases gradually. This can be explained as follows: The intensity of the stripping is determined not only by the penetration velocity but also by the contact area between the jet and water, since the contact area increases with the increase in the aspect ratio under the same cross-section area, namely, the jet becomes flat, and the stripping is enhanced. On the other hand, the thickness of the jet along the minor axis direction becomes smaller with the increase in the aspect ratio. Hence, the jet column is easier to break up due to stripping at a higher aspect ratio. This phenomenon can be clearly observed in **Figure 4** by comparing Case 4 and Case 10 with an aspect ratio of 2 and 4, respectively.

### 4.4 Degree of the Fragmentation

Since the fragments generated during the jet penetration process are mostly irregular as shown in **Figure 2**, direct measurement of the fragment size will introduce large errors. In this work, the dimensionless corium surface area is used to evaluate the degree of the jet fragmentation. First, the interface between the corium and water is extracted from the simulation results as shown in **Figure 2**; then, the interface area *S* is calculated, and the dimensionless corium surface area is given by

$$\bar{S} = \frac{S}{\pi D^2/4}.$$
(36)

The dimensionless corium surface area versus aspect ratio at approximately the same penetration depth ( $V^*t$ ) in the 12 cases is presented in **Figure 6**. It can be seen that the dimensionless corium surface area increases with the increase in the penetration velocity for the jets with the same aspect ratio, that is, smaller fragments are generated with the increase in the penetration velocity. This is because higher penetration velocity means stronger momentum exchange and stripping, leading to more fragments.

Another observation is that, in general, the dimensionless corium surface area increases with the increase in the aspect ratio for the jets under the same penetration velocity. This trend is not obvious at low penetration velocity (e.g., V = 2.21 m/s), but remarkable at high penetration velocities. The reason has been explained in Section 4.3, namely, with the increase in the aspect ratio under the same cross-section area, the contact area between the jet and water is increased, which enhances the stripping and facilitates the jet fragmentation.





12 cases



# **5 CONCLUSION**

In order to investigate the effect of jet cross-section shape on the corium jet breakup behavior, which is generally ignored in

# REFERENCES

- Abe, Y., Matsuo, E., Arai, T., Nariai, H., Chitose, K., Koyama, K., et al. (2006). Fragmentation Behavior during Molten Material and Coolant Interactions. *Nucl. Eng. Des.*236, 1668–1681. doi:10.1016/j.nucengdes.2006.04.008
- Ba, Y., Liu, H., Li, Q., Kang, Q., and Sun, J. (2016). Multiple-relaxation-time Color-Gradient Lattice Boltzmann Model for Simulating Two-phase Flows with High Density Ratio. *Phys. Rev.* E94, 023310. doi:10.1103/PhysRevE.94.023310

previous studies, in this study, the breakup processes of the corium jets with four different elliptical cross-section shapes and three different penetration velocities are simulated with the state-of-the-art GPU-accelerated color-gradient lattice Boltzmann method. The effect of the cross-section shape on the hydrodynamic breakup behavior of the corium jet is analyzed in detail. Three main conclusions drawn from the simulation results are as follows:

- (1) The effect of the cross-section shape on the jet penetration depth is very limited because the change of the drag force is very small for jets with the same penetration velocity and cross-section area.
- (2) With the increase in the aspect ratio under the same penetration velocity, the jet breakup length decreases gradually mainly due to the decrease in the thickness of the jet along the minor axis direction.
- (3) In general, the dimensionless corium surface area increases with the increase in the aspect ratio for the jets under the same penetration velocity since the contact area increases with the increase in the aspect ratio under the same crosssection area.

# DATA AVAILABILITY STATEMENT

The raw data supporting the conclusions of this article will be made available by the authors, without undue reservation.

# **AUTHOR CONTRIBUTIONS**

HC contributed to the conception and simulations of this study and writing the manuscript; SC and JW contributed to manuscript revision and read and approved the submitted version.

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- Bürger, M., Cho, S. H., Berg, E. v., and Schatz, A. (1995). Breakup of Melt Jets as Pre-condition for Premixing: Modeling and Experimental Verification. *Nucl. Eng. Des.*155, 215–251. doi:10.1016/0029-5493(94)00875-y
- Cheng, H., Chen, X., Ye, Y., and Cheng, S. (2021a). Systematic Experimental Investigation on the Characteristics of Molten lead-bismuth Eutectic Fragmentation in Water. *Nucl. Eng. Des*. 371, 110943. doi:10.1016/j.nucengdes.2020.110943
- Cheng, H., Cheng, S., and Zhao, J. (2020). Study on Corium Jet Breakup and Fragmentation in Sodium with a GPU-Accelerated Color-Gradient Lattice Boltzmann Solver. Int. J. Multiphase Flow126, 103264. doi:10.1016/j.ijmultiphaseflow.2020.103264

- Cheng, H., Zhao, J., Saito, S., and Cheng, S. (2021b). Study on Melt Jet Breakup Behavior with Nonorthogonal central-moment MRTColor-Gradient Lattice Boltzmann Method. *Prog. Nucl. Energ*.136, 103725. doi:10.1016/j.pnucene. 2021.103725
- Cheng, H., Zhao, J., and Wang, J. (2019). Experimental Investigation on the Characteristics of Melt Jet Breakup in Water: The Importance of Surface Tension and Rayleigh-Plateau Instability. *Int. J. Heat Mass Transfer*132, 388–393. doi:10.1016/j.ijheatmasstransfer.2018.12.026
- Corradini, M. L., Kim, B. J., and Oh, M. D. (1988). Vapor Explosions in Light Water Reactors: A Review of Theory and Modeling. *Prog. Nucl. Energ.*22, 1–117. doi:10.1016/0149-1970(88)90004-2
- Dinh, T. N., Bui, V. A., Nourgaliev, R. R., Green, J. A., and Sehgal, B. R. (1999). Experimental and Analytical Studies of Melt Jet-Coolant Interactions: a Synthesis. *Nucl. Eng. Des.* 189, 299–327. doi:10.1016/s0029-5493(98)00275-1
- Huang, H., Sukop, M., and Lu, X. (2015). Multiphase Lattice Boltzmann Methods: Theory and Application.
- Huhtiniemi, I., Magallon, D., and Hohmann, H. (1999). Results of Recent KROTOSFCI Tests: Alumina versus Corium Melts. Nucl. Eng. Des.189, 379–389. doi:10.1016/s0029-5493(98)00269-6
- Iwasawa, Y., and Abe, Y. (2018). Melt Jet-Breakup and Fragmentation Phenomena in Nuclear Reactors: A Review of Experimental Works and Solidification Effects. Prog. Nucl. Energ. 108, 188–203. doi:10.1016/j.pnucene.2018.05.009
- Kim, W. K., Shim, J. H., and Kaviany, M. (2017). Thermophysical Properties of Liquid UO2, ZrO2 and Corium by Molecular Dynamics and Predictive Models. *J. Nucl. Mater*.491, 126–137. doi:10.1016/j.jnucmat.2017.04.030
- Kirillov, P. (2006). *Thermo Physical Properties of Materials for Nuclear Engineering*. Obninsk: Institute for heat and mass transfer in nuclear power plants.
- Kolev, N. I. (2015). Multiphase Flow Dynamics 5: Nuclear thermal Hydraulics. Springer. Krüger, T., Kusumaatmaja, H., Kuzmin, A., Shardt, O., Silva, G., and Viggen, E. M. (2016). The Lattice Boltzmann Method - Principles and Practice.
- Leclaire, S., Parmigiani, A., Malaspinas, O., Chopard, B., and Latt, J. (2017). Generalized Three-Dimensional Lattice Boltzmann Color-Gradient Method for Immiscible Two-phase Pore-Scale Imbibition and Drainage in Porous media. *Phys. Rev. E95*, 033306. doi:10.1103/PhysRevE.95.033306
- Saito, S., Abe, Y., and Koyama, K. (2017). Lattice Boltzmann Modeling and Simulation of Liquid Jet Breakup. *Phys. Rev. E*96, 013317f. doi:10.1103/PhysRevE.96.013317

- Saito, S., De Rosis, A., Festuccia, A., Kaneko, A., Abe, Y., and Koyama, K. (2018). Color-gradient Lattice Boltzmann Model with Nonorthogonal central Moments: Hydrodynamic Melt-Jet Breakup Simulations. *Phys. Rev. E*98, 013305. doi:10.1103/PhysRevE.98.013305
- Schins, H. (1978). On the Surface Tension of Liquid UO2. J. Nucl. Mater.78, 215–216. doi:10.1016/0022-3115(78)90521-4
- Shen, P., Zhou, W., Cassiaut-Louis, N., Journeau, C., Piluso, P., and Liao, Y. (2018). Corium Behavior and Steam Explosion Risks: A Review of Experiments. Ann. Nucl. Energ. 121, 162–176. doi:10.1016/j.anucene.2018.07.029
- Spencer, B., Wang, K., Blomquist, C., Mcumber, L., and Schneider, J. (1994). Fragmentation and Quench Behavior of Corium Melt Streams in Water". Nuclear Regulatory Commission. Washington, DCIL (United States)): United States. Div. of Systems Research; Argonne National Lab.
- Thakre, S., Manickam, L., and Ma, W. (2015). A Numerical Simulation of Jet Breakup in Melt Coolant Interactions. Ann. Nucl. Energ. 80, 467–475. doi:10. 1016/j.anucene.2015.02.038
- Zhou, Y., Chen, J., Zhong, M., Wang, J., and Lv, M. (2017). Numerical Simulation of Metal Jet Breakup, Cooling and Solidification in Water. *Int. J. Heat Mass Transfer*109, 1100–1109. doi:10.1016/j.ijheatmasstransfer.2017.02.083

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