



# Optimal Dispatching Strategy of Active Distribution Network for Promoting Local Consumption of Renewable Energy

Hua Xie<sup>1\*</sup>, Wei Wang<sup>1</sup>, Weixing Wang<sup>2</sup> and Lulu Tian<sup>1</sup>

<sup>1</sup>School of Electrical Engineering, Beijing Jiaotong University, Beijing, China, <sup>2</sup>Research and Development Center, XJ Group Corporation, Xuchang, China

## OPEN ACCESS

### Edited by:

Mingxi Liu,  
The University of Utah, United States

### Reviewed by:

Xiang Huo,  
The University of Utah, United States  
Zongjie Wang,  
University of Connecticut,  
United States

### \*Correspondence:

Hua Xie  
hxie@bjtu.edu.cn

### Specialty section:

This article was submitted to  
Smart Grids,  
a section of the journal  
Frontiers in Energy Research

**Received:** 30 November 2021

**Accepted:** 24 January 2022

**Published:** 08 March 2022

### Citation:

Xie H, Wang W, Wang W and Tian L  
(2022) Optimal Dispatching Strategy of  
Active Distribution Network for  
Promoting Local Consumption of  
Renewable Energy.  
Front. Energy Res. 10:826141.  
doi: 10.3389/fenrg.2022.826141

Large-scale renewable energy sources (RESs) have been integrated into the active distribution network (ADN). For promoting the local consumption of RESs within ADN, an optimal dispatching strategy was proposed with two-stage hierarchical energy management framework. On the spatial boundary, a two-layer energy management framework was designed with the local optimization layer and the global optimization layer. The local optimization layer was for optimal power flow in the branch feeder with the objective functions of minimizing operation costs and maximizing the consumption of RESs. The global optimization layer was for optimal power flow in the main feeder with the objective functions of minimizing power loss and the voltage deviation of nodes. On the time scale, two-stage optimal dispatching models were established, including the day-ahead optimal models and intra-day optimal models. The day-ahead optimal models identified the operation status of the controllable units, and then the intra-day optimal models were updated with the ultra-short-term forecast results. A risk indicator was introduced to quantify the uncertainty of RES, and a non-dominated sorting genetic algorithm with elite strategy was adopted to solve the multi-objective nonlinear programming problem. An actual project in northern China was used as the testing system. The results of case studies verify that the proposed strategy can effectively realize the maximum local consumption of RESs and support the economic operation of ADN.

**Keywords:** active distribution network, dispatching strategy, renewable energy, two-stage, global optimization, local optimization

## INTRODUCTION

The high penetration of renewable energy can pose challenges for the operation of a distribution network due to uncertainty and variability. For the future low-carbon society, it is important to design an optimal dispatching strategy of the active distribution network (ADN) to improve the consumption of renewable energy and enhance the economy of the distribution network (Wu et al., 2021).

The research on the dispatching strategy of ADN mainly focused on economical operation. The objective function of the optimal dispatching model was generally set with minimizing power loss (Gildenhuis et al., 2019; Bi et al., 2020; Wu et al., 2021) and the amount of electricity purchased from grid (Wu et al., 2019; Zhang et al., 2020a; Omaji et al., 2020). Some references considered resilience in

the objective functions (Wang and Wang, 2015; Zhou et al., 2019). Renewable energy sources (RESs) were often integrated with energy storage systems (ESSs) or controllable distributed generators (CDGs) to form microgrids (MGs). Bi *et al.* (2020) proposed a learning-based dispatching strategy of MGs with RES and ESS. Ji et al. (2021) proposed a continuous-control, deep reinforcement learning-based online scheduling method for MGs. Dubuisson et al. (2020) proposed a bacterial foraging optimization algorithm for power management in stand-alone MGs. Omaji et al. (2020) established a cooperative game model for MGs. Younesi et al. (2021) proposed bi-level resilience-oriented stochastic scheduling that integrates the economic perspective considering MG resilience function. In Zhang and Yan (2018), an ADN optimal control strategy for energy storage systems and controllable loads was considered and solved by an improved particle swarm algorithm. The above-mentioned literature greatly benefits this paper on objective functions and constraints.

Actually, the difficulty lies in the uncertainty of RESs. At present, most papers established a stochastic programming model to solve the problems of ADNs with RESs. Sampling and clustering were commonly used in some literature so that deterministic scenarios were derived for ease in solving. Ahmadi et al. (2016) proposed a stochastic programming model for distribution companies trading in the electricity market, in which the variability of wind speed was dealt with roulette wheel mechanism. Somma *et al.* (2017) formulated a stochastic multi-objective linear programming problem for the operation strategies of ADN by using Monte Carlo simulation method to model 24-h scenarios related to solar irradiance. The Monte Carlo simulation in Wang and Wang (2015) was based on the forecasted power and uncertain prediction errors to generate scenarios for distributed generator (DG) outputs. Fang et al. (2017) evaluated the primary frequency response of the power system with important wind power generation, which considered the uncertainty of wind power output. Fan et al. (2021) evaluated the influence of RESs on ADN dynamic performance, in which K-means clustering technique was adopted to select the approximation samples of input variables. Sannigrahi et al. (2019) used K-means algorithm to present a stochastic framework for ADN planning framework. Sampling and clustering algorithms are useful and simple in modeling the uncertainty of RESs. However, multiple scenarios increase the solving times, and it is not convenient for dispatchers to quantitatively evaluate the operation risk caused by the uncertainty of RESs.

There were some studies on the energy management framework of ADNs. Kong et al. (2019) constructed a two-layer distributed optimization model for ADNs and MG with different interests, in which one layer is the active judgment modules and another layer is the active control modules. The active judgment modules included power flow calculation, voltage quality judgment, and supply margining judgment. The active control modules were those controllable units such as CDGs. Li et al. (2018) proposed a three-layer collaborative dispatch system for ADNs, in which the first layer is the distribution network dispatching layer, the second layer is the coordinated control layer, and the third layer is the local control layer. Radhakrishnan and Srinivasan (2016) and Upadhyay and

Sharma (2016) constructed a multi-agent system for the distributed energy management system. The son-agent dealt with the uncertainty of RESs, and the parent-agent dealt with the coordination between son-agents. The energy management framework with multiple layers or agents has a clear architecture and reduces the difficulty of solving complex problems. However, the above-mentioned literature needs to consider the coordination relationship between multiple agents or layers and increases the complexity of the controller.

This paper proposed a two-stage hierarchical optimal dispatching model to promote the local consumption of RESs within ADN. The main contributions of this paper are as follows:

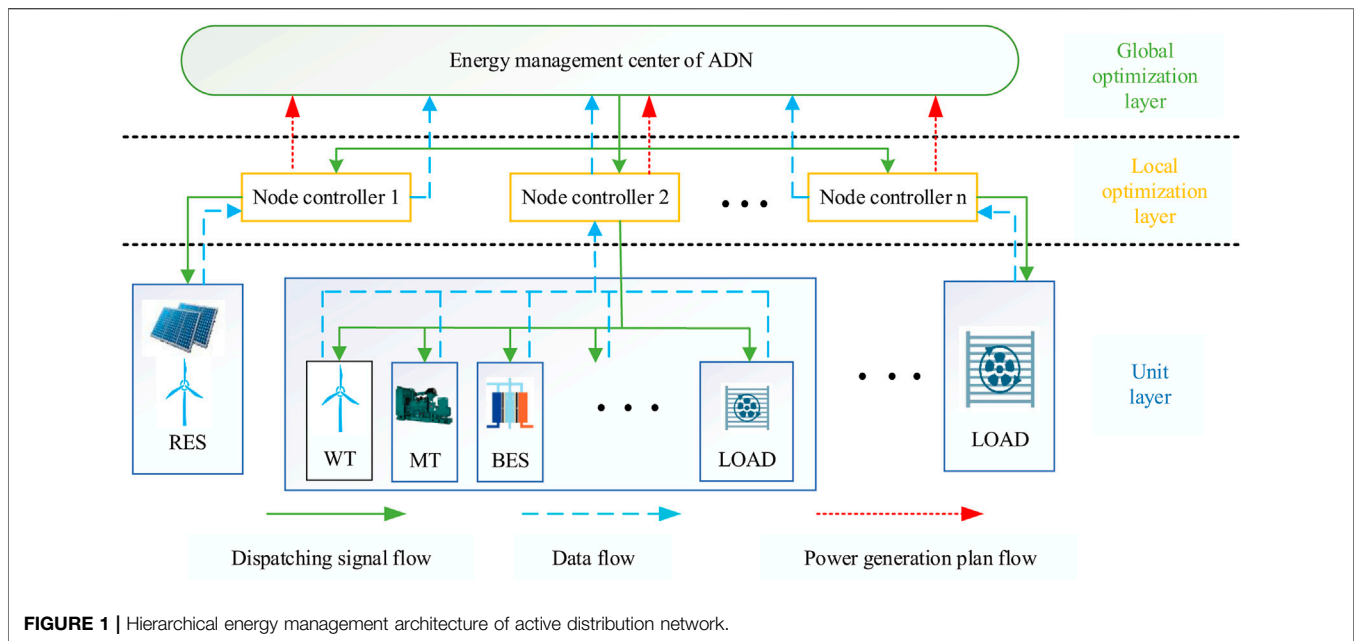
- (1) A hierarchical energy management framework is proposed for ADN. The global optimization layer of ADN optimizes the load flow in the main feeder for improving the consumption of RESs, and the local optimization layer optimizes the load flow in the branch feeder for the local consumption of RESs. The structure of the dispatching system is simple without the additional coordinated controllers.
- (2) The optimal dispatching model is established with two-stage energy management. The day-ahead optimal model identifies the operation status of the controllable units. The intra-day optimal model is updated with ultra-short-term forecast results, and the risk indicator is introduced for quantifying the uncertainty caused by the forecast errors. The optimal dispatching model is easier to be solved.

The rest of this paper is organized as follows: **Section 2** presents the hierarchical energy management framework for optimal dispatching of ADN. **Section 3** establishes a two-stage hierarchical optimal dispatching model of ADN. **Section 4** supports the solving algorithm. Case studies are carried out in **Section 5**. Finally, **Section 6** presents the conclusion of the whole paper.

## PROBLEM FORMULATION

This paper studies an ADN with RESs connected to nodes. As shown in **Figure 1**, the energy management framework for dispatching ADN is divided into three levels, namely, the global optimization layer, the local optimization layer, and the unit layer.

Bi-direction power flow is permitted in the tie line between grids with ADN. The node in ADN may serve as a load to absorb the power from ADN or as a power source to inject power into ADN. The global optimization layer is for energy management of ADN, which issues the power references to the local optimization layer. The local optimization layer is for the energy management of nodes, which is set as the node controller. Unit layer is for energy management of devices connected with nodes, which is responsible for executing the dispatching instructions from the node controller. In the hierarchical energy management architecture, the corresponding demand of dispatching should be considered. Furthermore, the safe operation of ADN should be



satisfied effectively, and renewable energy should be absorbed locally.

The global optimization layer of ADN optimizes the load flow in the main feeder for improving the consumption of RESs. The renewable energy shall be absorbed within ADN as much as possible. If the output of renewable energy is greater than the demand of the load, the curtailed energy can be sold to grid or be stored in energy storage systems. If the output is far less than the demand, the energy will be supplied by grid or regulated by nodes.

The local optimization layer optimizes the load flow in the branch feeder for the local consumption of RESs. It takes the optimized power issued by the energy management center as a constraint, and the regional autonomous control is completed by the unit layer according to the optimization objective of the local optimization layer. The devices in the unit layer are regulated to absorb RESs nearby, which may be CDGs such as hydro, micro-gras turbine (MT), energy storage systems such as battery energy storage (BES), and demand-side response loads (DRLs) such as transferable load (TL) and interruptible (IL).

The information flow in ADN is a loop in which the state information is collected from the unit layer to the local optimization layer and then to the global optimization layer, and the instruction information is released from the energy management center to the node controllers and then to the schedulable units.

At present, the forecast accuracy of renewable energy output is related to the forecast time scale. Generally speaking, the longer the time scale is in the forecast horizon, the worse the forecast accuracy is. In this paper, two-stage hierarchical optimal model will be established for the dispatching strategy of ADN to promote the local consumption of RESs. In the following discussion, day-ahead dispatching plans for the global optimization layer and the local optimization layer will be designed, and then an intra-day optimal dispatching strategy of and will be developed.

## TWO-STAGE HIERARCHICAL OPTIMAL DISPATCHING MODEL OF ACTIVE DISTRIBUTION NETWORK

Two-stage hierarchical optimal dispatching model is established on the spatial and temporal dimensions. On the spatial boundary, there is a two-layer optimal dispatching model with consideration of promoting the local consumption of RESs, in which the local optimization layer is for the branch feeders (BFs) and the global optimization layer is for the main feeders. On the time scale, there is a two-stage optimal dispatching model with the consideration of reducing the negative influence of the forecast error of RESs, in which the day-ahead optimization is for the states of controllable units and the intra-day optimization is for the updated dispatch strategy.

The forecast error of RESs is collected with the history data. The day-ahead forecast outputs of RESs are given by the short-term forecasting system, which will be used in the day-ahead optimal models. The intra-day forecast outputs in each interval are given by the ultra-short-term forecasting system, which is more accurate than the day-ahead forecast outputs. The dispatching interval of ADN is set as 15 min following the grid dispatching intervals.

### Day-Ahead Optimal Model of the Local Optimization Layer

In the local optimization layer, the day-ahead optimal model is for optimal power flow in the branch feeders. The decision variables include the consumption power of RESs connected with the branch feeder, the interactive power of the nodes with the main branch, the outputs and the status of schedulable units connected at the branch feeder, such as the on/off status of CDGs and their generation power, the charge/

discharge status of ESSs and their outputs, and the operation status of DRLs and their power.

## OBJECTIVE FUNCTIONS

In order to improve the local consumption of RESs as much as possible, **Eq. 1** is chosen as the objective function. Meanwhile, the operation cost of the branch feeders should be minimized to manage the economic operation of ADN. Therefore, another objective function is expressed as **Eq. 2**, which includes the generation costs of CDGs (**Eq. 3**), operation cost of ESSs (**Eq. 4**), dispatching costs of schedulable loads (**Eq. 5**), environment cost (**Eq. 6**), and purchasing cost of electricity from the node (**Eq. 7**).

$$\max f_1 = \sum_t (P_{PV,t} + P_{WT,t}) \Delta t \quad (1)$$

$$\min f_2 = \sum_t [C_{CDG,t} + C_{ESS,t} + C_{DRL,t} + C_{e,t} + C_{PE,t}] \quad (2)$$

$$C_{CDG}^t = \sum_{i=1}^{N_{CDG}} \{ \mu_i^t f(P_{CDGi,t}) + (\mu_i^t - \mu_i^{t-1}) \lambda_{CDGi} \} \quad (3)$$

$$C_{ESS,t} = \sum_{j=1}^M \left( C_{inv} \frac{\mu_j^t P_{j,t}^{dis} - \mu_j^t P_{j,t}^{ch}}{2N_{life}(t)E_{Br}} \Delta t + c_{loss} [(1 - \eta_j^{ch}) P_{j,t}^{ch} + (\eta_j^{dis} - 1) P_{j,t}^{dis}] \Delta t \right) \quad (4)$$

$$C_{DRL,t} = \sum_{n=1}^{N_{TL}} c_{TL} P_{TLn,t} \Delta t + \sum_{m=1}^{N_{IL}} c_{IL} P_{ILm,t} \Delta t \quad (5)$$

$$C_{e,t} = \sum_{i=1}^{N_{DG}} \sum_{s=1}^{N_S} V_{es} Q_{is,t} P_{DGi,t} \quad (6)$$

$$C_{PE,t} = c_{grid,t} P_{PE,t} \quad (7)$$

In **Eq. 4** constraints, the cycle life of ESSs was calculated with the charge/discharge depth by the rain flow counting method. For the sake of simple calculation, this paper assumes that all TLs have the same unit scheduling cost and all ILs have the same unit scheduling cost. The environment cost refers to the purification cost of pollutant emissions by CDGs connected with the branch feeder.

## CONSTRAINTS

The power flow balance meets constraint **Eq. 8**. It should be noted that the outputs of RESs are uncertain, and the power supported by grid is limited by tie-line carrying capacity as shown in **Eq. 9**.

$$\sum_{i=1}^{N_{CDG}} P_{CDGi,t} + P_{G,t} + (P_{PV,t} + P_{WT,t}) + \sum_{j=1}^M (\eta_{j,t}^{dis} P_{j,t}^{dis} - \eta_{j,t}^{ch} P_{j,t}^{ch}) = P_{L,t} + P_{TL,t} + P_{IL,t} \quad (8)$$

$$P_{G,t} \leq P_{G,max} \quad (9)$$

**Eqs 10–12** are the operation constraints of CDGs, in which **Eq. 10** limits the output power, **Eq. 11** and **Eq. 12** describe the ramp rate, and **Eq. 13** guarantees the minimum operating time.

$$P_{CDG,min} \leq P_{CDGi,t} \leq P_{CDG,max} \quad (10)$$

$$P_{CDGi,t} - P_{CDGi,t-1} \leq UR \quad (11)$$

$$P_{DGi,t-1} - P_{DGi,t} \leq UD \quad (12)$$

$$T_{d,min} \leq T_{d,s} \leq T_{d,max} \quad (13)$$

The operation constraints of BESSs include **Eqs 14–19**. **Eq. 14** limits the state of charge (SoC) of battery, which is to prevent over-charge and over-discharge. **Eq. 15** guarantees battery capacity to serve the next dispatching cycle, which is usually set at half of the battery capacity. **Eq. 16** and **Eq. 17** calculate the real-time SoC, and **Eq. 18** and **Eq. 19** limit the permitted power in charging and discharging.

$$SoC_{B,min} < SoC_{B,t} < SoC_{B,max} \quad (14)$$

$$SoC_{B,0} = SoC_{B,T} = 0.5 \quad (15)$$

$$SoC_{B,t} = (1 - \delta) SoC_{B,t-1} + \frac{\eta_{ch} P_{ch,t} \Delta t}{E_{Br}} \quad (16)$$

$$SoC_{B,t} = (1 - \delta) SoC_{B,t-1} + \frac{P_{dis,t} \Delta t}{\eta_{dis} E_{Br}} \quad (17)$$

$$0 < P_{ch,t} < P_{ch,max} \quad (18)$$

$$0 < P_{dis,t} < P_{dis,max} \quad (19)$$

The schedulable loads here include ILs and TLs. **Eq. 20** limits the interruptible power of IL, and **Eq. 21** limits the interruptible duration of IL. The **Eq. 22** and **Eq. 23** constrain operation status of IL and TL cannot be changed continuously in adjacent periods. **Eq. 24** demands TL to transfer as a whole.

$$0 \leq P_{IL,t} \leq P_{IL,max} \quad (20)$$

$$T_{IL,min} \leq T_{IL,t} \leq T_{IL,max} \quad (21)$$

$$|\mu_{IL,t} - \mu_{IL,t-1}| = \mu_{IL} \quad (22)$$

$$|\mu_{DL,t} - \mu_{DL,t-1}| = \mu_{DL} \quad (23)$$

$$P_{TL,t} = P_{TL} \quad (24)$$

## Day-Ahead Optimal Model of the Global Optimization Layer

In the global optimization layer, the day-ahead optimal model is for optimal power flow in the main feeders. The decision variables include the consumption power of RESs connected with the main feeder, the power supported by grid, the power of node injected into the branch feeders, and the outputs and the status of schedulable units connected at the main feeder, such as on/off status of CDGs and their generation power, charge/discharge status of ESSs and their outputs, and operation status of DRLs and their power.

## OBJECTIVE FUNCTION

The power flow in the main feeder is optimized to obtain the economic operation of ADN. **Eq. 25** is designed as the objective

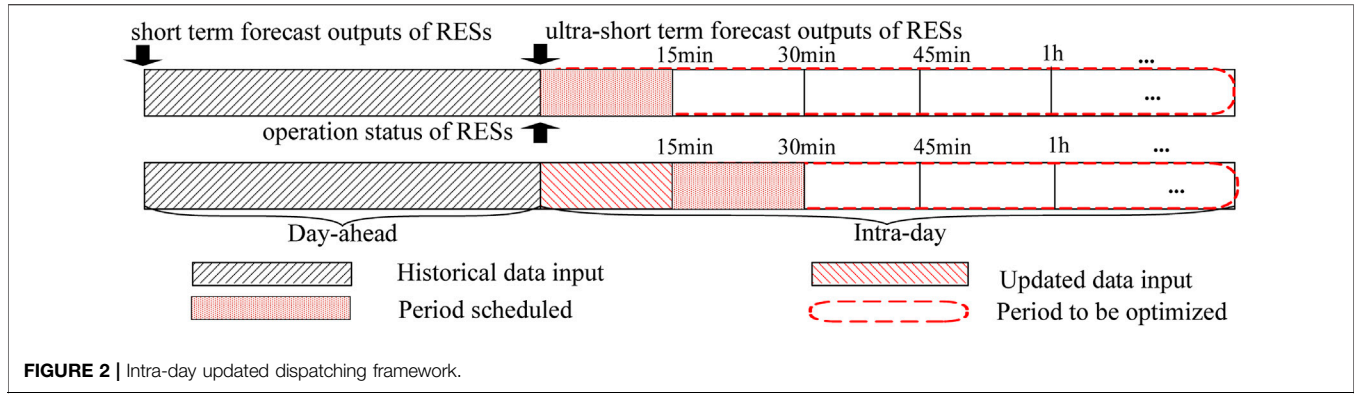


FIGURE 2 | Intra-day updated dispatching framework.

function to promote the local consumption of RESs. The less the power loss is in the main feeder, the more RESs is absorbed locally. Besides this, the key factor restricting the consumption capacity of RESs is the voltage deviation in ADN caused by the fluctuation of RESs. Eq. 26 is designed as the objective function to support the power quality.

$$\min f_3 = \sum_{t=1}^T \sum_{ij \in \Omega_L} \frac{Z_{ij}(P_{ij,t}^2 + Q_{ij,t}^2)\Delta t}{V_{j,t}^2} \quad (25)$$

$$\min f_4 = \sum_{t=1}^T \left| \frac{V_{i,t} - V_N^i}{V_N^i} \right| \quad (26)$$

## CONSTRAINTS

The power flow constraints are expressed as Eq. 27 and Eq. 28, the power interactive with nodes meets Eq. 29, and the node voltage constraints are expressed as Eq. 30. The other constraints include Eqs. 9–24.

$$P_{G,t} - \sum_{i=1}^N P_{i,t} = V_{i,t} \sum_{j=1}^N V_{j,t} (G_{ij} \cos \delta_{ij,t} + B_{ij} \sin \delta_{ij,t}) \quad (27)$$

$$Q_{G,t} - \sum_{i=1}^N Q_{i,t} = V_{i,t} \sum_{j=1}^N V_{j,t} (G_{ij} \sin \delta_{ij,t} - B_{ij} \cos \delta_{ij,t}) \quad (28)$$

$$P_{i,t} \leq P_{i,\max} \quad (29)$$

$$V_{\min} \leq V_{i,t} \leq V_{\max} \quad (30)$$

## Intra-day Updated Optimal Model

It is necessary to update the dispatching strategy designed above because the intra-day forecast outputs of RESs are relatively accurate. Figure 2 shows the intra-day updated dispatching framework. The operation status of units are determined according to the day-ahead optimal model, and the dispatching strategy is updated with intra-day forecast outputs of RESs in every 15-min interval.

As mentioned above, the operation status of the units are known in the intra-day optimal model, including the on/off status of CDGs, the charge and discharge status of EESs, and the

operation status of DRLs. Whether it is the intra-day updated optimal model of the local optimization layer or the intra-day updated optimal model of the global optimization layer, the constraints are the same as that of the day-ahead optimal models. In the following sections, the objective functions will be discussed.

The intra-day optimal model of the local optimization layer is updated with the ultra-short-term forecast outputs of RESs connected with the branch feeder. The decision variables of the intra-day optimal model are the consumption power of RESs, the power of the node injected into the branch feeders, the outputs of CDGs, the outputs of EESs, and the interruptible power of ILs.

For promoting the local consumption of RESs in the branch feeder, Eq. 1 is chosen as the objective function as that of the day-ahead optimal model of the local optimization layer. Besides this, there is another objective function expressed as Eq. 31, which is to minimize the adjustment costs. Adjustment costs refer to the additional operation costs brought about by updating the forecast outputs of RESs.

$$\min f'_2 = \sum_t^T [\Delta C_{CDG,t} + \Delta C_{ESS,t} + \Delta C_{DRL,t}] \quad (31)$$

Since the on/off status of CDGs is determined by the day-ahead scheduling plan, the adjustment cost only considers fuel costs during each dispatching period  $t$ . The adjustment cost of CDGs is calculated as Eq. 32.

$$\Delta C_{CDG,t} = \sum_{i=1}^{N_{CDG}} f(P_{CDG_{i,t}} - P'_{CDG_{i,t}}) \quad (32)$$

Similarly, the adjustment cost of ESSs can be expressed as Eqs 33–35. As to the adjustment cost of DRLs, it is expressed as Eq. 36 for ILs while ignoring TLs which keep the optimal operation status of the day-ahead schedule plan.

$$\Delta C_{ESS,t} = \sum_{j=1}^M (C_{life,t} + C_{loss,t}) - \sum_{j=1}^M (C'_{life,t} + C'_{loss,t}) \quad (33)$$

$$C'_{life,t} = C_{inv} \frac{P_{j,t}^{dis} - P_{j,t}^{ch}}{2N'_{life,t} E_{Br}} \Delta t \quad (34)$$

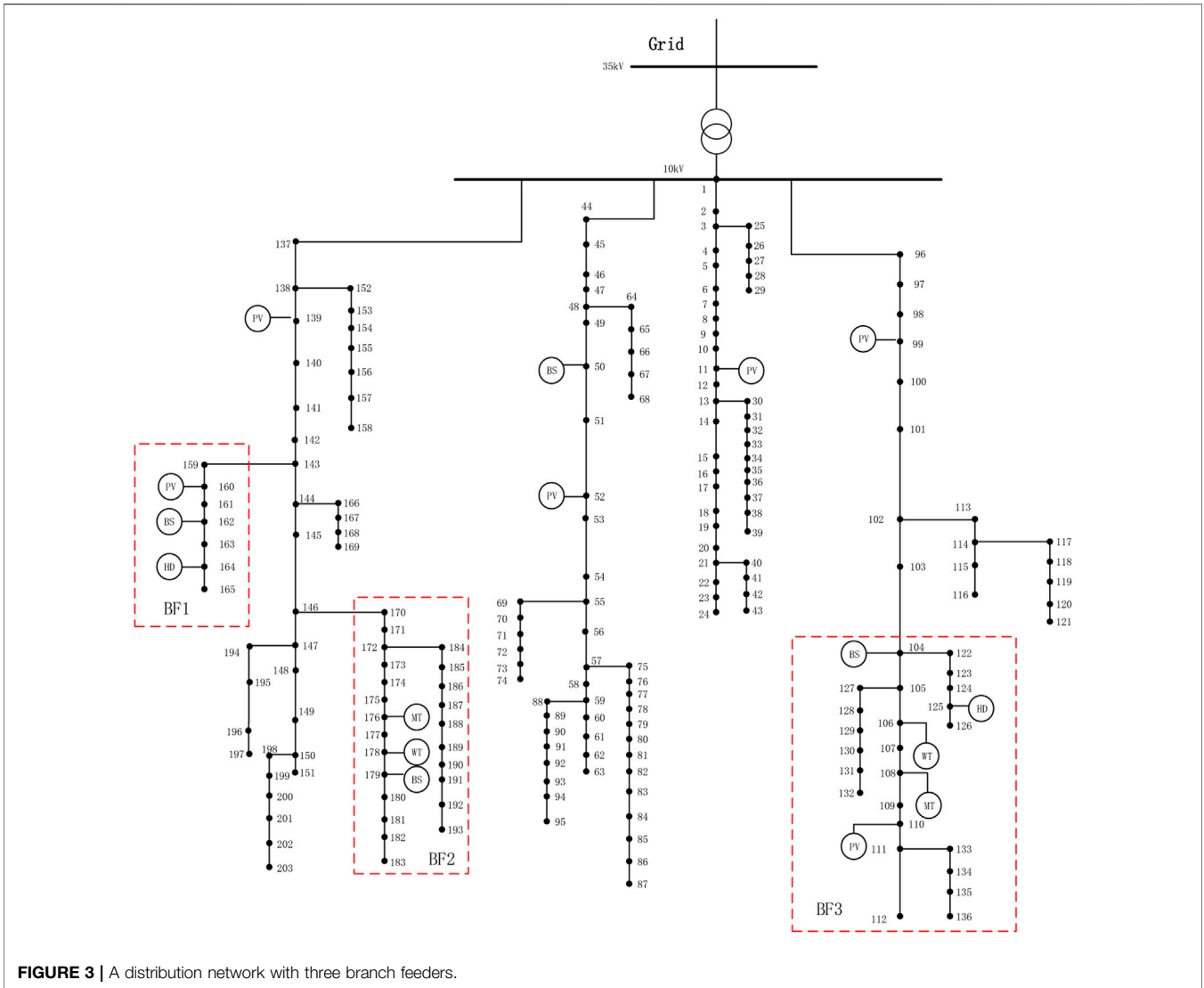


FIGURE 3 | A distribution network with three branch feeders.

$$C'_{loss,t} = c_{loss} \left[ (1 - \eta_j^{ch}) P'_{j,t}{}^{ch} + (\eta_j^{dis} - 1) P'_{j,t}{}^{dis} \right] \Delta t \quad (35)$$

$$\Delta C_{DRL,t} = \left[ \sum_{l=1}^{N_{IL}} c_{IL} P'_{l,t} \Delta t \right] - \left[ \sum_{l=1}^{N_{IL}} c_{IL} P'_{l,t} \Delta t \right] \quad (36)$$

The objective functions of the intra-day optimal model of the global optimization layer is the same as that of the day-ahead optimal model of the global optimization layer.

## SOLVING ALGORITHM

The day-ahead optimal model is a mixed-integer nonlinear programming problem. There are continuous variables, such as the outputs of CDGs, consumption power of RESs, power supported by grid, power of node injected into the branch feeders, and so on, and there are discrete variables such as the on/off status

of CDGs, charge/discharge status of ESSs, operation status of DRLs, and so on. The models can be established as follows:

$$\begin{cases} \min f(P, \mu), P = [P_1, P_2, \dots, P_n], \mu = [\mu_1, \mu_2, \dots, \mu_m] \text{ s.t. } h(P, \mu) \\ = 0 \bar{g} \leq g(P, \mu) \leq \underline{g} P \in R, \mu \in \{0, 1\} \end{cases} \quad (37)$$

The intra-day optimal model is a nonlinear optimization problem. There are continuous variables, such as outputs of CDGs, consumption power of RESs, charging and discharging power of RESs, and so on. The models can be built up as follows:

$$\begin{cases} \min f'(P), \Delta P = [P_1, P_2, \dots, P_n] \\ \text{s.t. } h'(P) = 0 \\ \bar{P} \leq P_j \leq \underline{P}, j = 1, 2, \dots, D \end{cases} \quad (38)$$

**TABLE 1** | Parameters of micro-gas turbine.

Rated power (MW)	Maximum up climbing rate (MW/h)	Maximum down climbing rate (MW/h)	Startup cost (yuan/times)	Fuel cost (yuan/MWh)
1	0.5	0.5	0.96	573

**TABLE 2** | Emission parameters of various electricity generation technologies (g/kWh).

Generation technologies	CO <sub>2</sub>	NO <sub>x</sub>	CO	SO <sub>2</sub>
Thermal power generation	623	2.88	0.1083	6.48
PV	0	0	0	0
WT	0	0	0	0
HD	0	0	0	0
MT	184.0829	0.6188	0.1702	0.000928

**TABLE 3** | Processing costs of pollutant emission (yuan/kg).

Pollution type	CO <sub>2</sub>	NO <sub>x</sub>	CO	SO <sub>2</sub>
Environmental management fee	0.0125	2.5	0.2	1.25

As mentioned above, the historical data set can be derived to describe the probability distribution of the forecast errors of RESs. Eq. 8 can be transformed as Eq. 39 with the forecast errors.

$$\begin{aligned}
 & \sum_{i=1}^{N_{CDG}} P_{CDG_{i,t}} + P_{G,t} + (\bar{P}_{PV,t} + R_{PV,t}) + (\bar{P}_{WT,t} + R_{WT,t}) \\
 & + \sum_{j=1}^M (\eta_{j,t}^{dis} P_{j,t}^{dis} - \eta_{j,t}^{ch} P_{j,t}^{ch}) \\
 & = P_{L,t} + P_{TL,t} + P_{IL,t}
 \end{aligned} \tag{39}$$

Taking into account the uncertainty of the forecast error, a risk indicator is introduced with a certain confidence level of probability distribution. Under the given confidence level  $\alpha$ , the risk indicator can be quantified by quantiles, as shown in Eq. 40.

$$R = CDF^{-1}(1 - \alpha) \tag{40}$$

The optimal dispatching model established is a multi-objective optimization problem. As it is known, a single-objective optimization problem only has one objective function, which makes it relatively easy to get the global optimal solution. However, when multiple objectives are considered, there are often conflicts between these objectives, so it is difficult to find

**TABLE 4** | Energy storage system parameters.

Rated power (kW)	Rated capacity (MW)	Min SOC	Max SOC	Initial SOC	Efficiency (%)
500	2	0.1	0.9	0.5	95

**TABLE 5** | Price of interactive power between branch feeders and active distribution network.

Period	Time	Price (yuan/kWh)	
		Purchasing	Selling
Peak period	18:00–22:00	0.83	0.65
Flat period	7:00–18:00, 22:00–0:00	0.49	0.38
Valley period	0:00–7:00	0.17	0.13

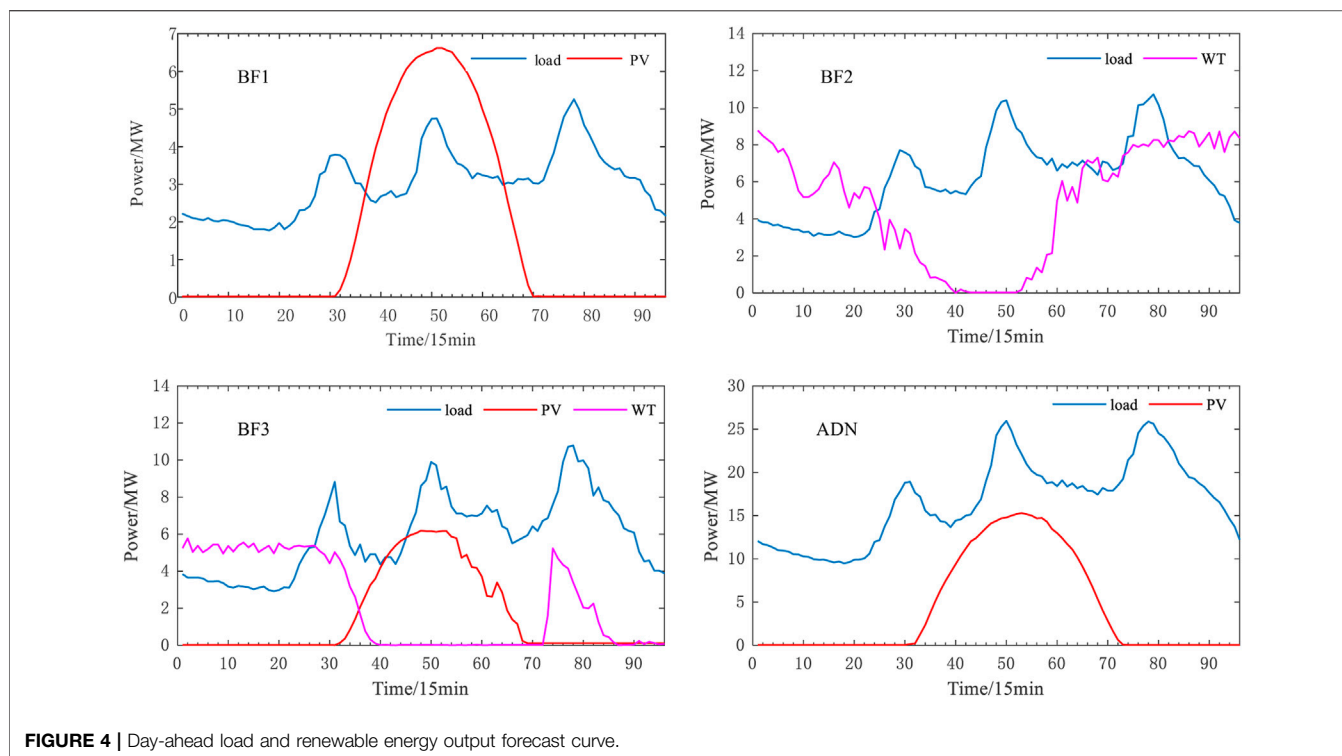
an appropriate solution. It is common that weight coefficients are set for each sub-objective to convert a multi-objective into a single objective. Although it is simple to obtain the solution, the results are influenced by the weights, and the solution quality is not high enough.

This paper adopts the NSGA-II algorithm to obtain the Pareto optimal solution. The NSGA-II algorithm is a multi-objective intelligent optimization algorithm based on the Pareto optimal solution theory, with the advantages of fast operation and good convergence (Zhang et al., 2020b; Pant et al., 2021). The crowding distance comparison operator is used to quickly obtain the fitness values of different elements. It competes between parent and offspring individuals to produce the next-generation population, which is conducive to maintaining excellent individuals and improving the overall evolution level of the population. The algorithm decomposes the multi-objective optimization problem into multiple single-objective optimization sub-problems and efficiently approaches the whole Pareto frontier by setting the weight vector. When the population size is set to  $N$ , the initialization weight vector is  $\{\frac{0}{N-1}, \frac{1}{N-1}, \dots, \frac{N-1}{N-1}\}$ .

The solution process of algorithm is detailed as Algorithm 1:

**Algorithm 1.**

- 1: Input history output data of renewable energy to model the probability distributions
- 2: Set  $\alpha = 0.9$
- 3: Solve (44) to obtain  $R_{PV,t}, R_{WT,t}$
- 4: Set iteration number  $q = 0$ , maximum number of iterations  $G_n$ , population size  $N$ , initial population  $P_0$
- 5: Coded continuous variables  $P$  and discrete variables  $\mu$
- 6: **Repeat**
- 7: Generate offspring population  $Q_0$ , population size  $N$
- 8: Combine  $P_0$  and  $Q_0$  to form  $R_0$ , population size  $2N$
- 9: Fast non-dominated sorting based on objective value
- 10: If the number of solution sets  $F_i < N$ , then **return**
- 11: **Until**  $q = G_n$ , output the optimal  $P$  and  $\mu$
- 12:  $q = q + 1$



## CASE STUDY

### Overview of the Actual ADN in Northern China

A case study was carried out using an actual distribution network in an area of Yiyang, Henan Province, China, as shown in **Figure 3**. The ADN contains 203 nodes. The voltage level of the system is 10 kV. The optimization horizon is 24 h, and the dispatch interval is 15 min. Three optimal models can be established with consideration of the combination RESs, CDGs, BESSs, and loads. BF1 is connected with node 143, BF2 is connected with node 146, and BF3 is connected with node 103. The installed capacity is 10 MW for each PV, 10 MW for each WT, 2 MW for each BESS, 2 MW for each HD, and 1 MW for each MT.

The parameters are displayed in **Tables 1–5**. **Figure 4** shows the forecast curves of the day-ahead load and RESs, and **Figure 5** indicates the forecast curves of the ultra-short-term load and RESs.

### Dispatching Strategy of ADN

The non-dominated genetic algorithm (NSGA-II) is used to solve the multi-objective optimization problem. The parameters of the algorithm are set as follows: population size is set to 100, the maximum iterations of genetic operations is 100, selection probability is 0.9, and mutation probability is 0.1. The simulation took 6.174 s with high model convergence.

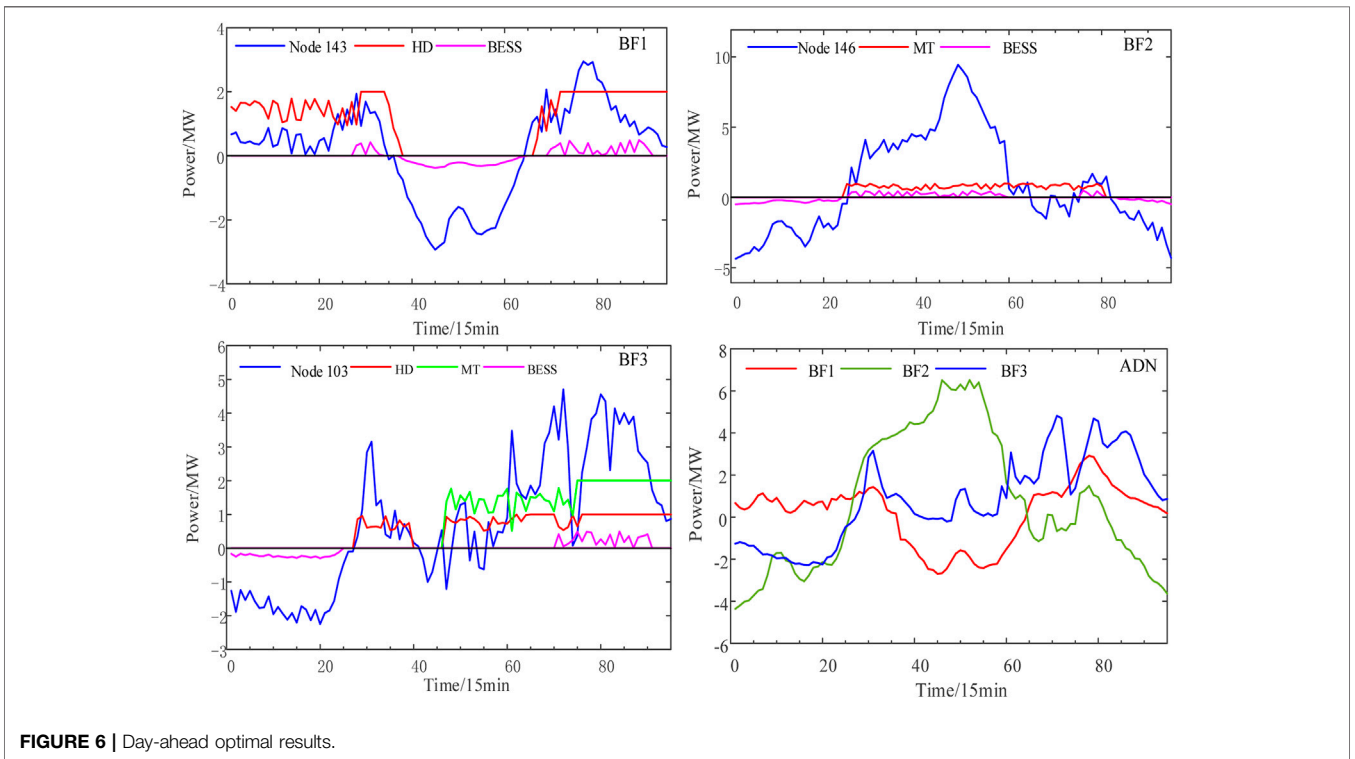
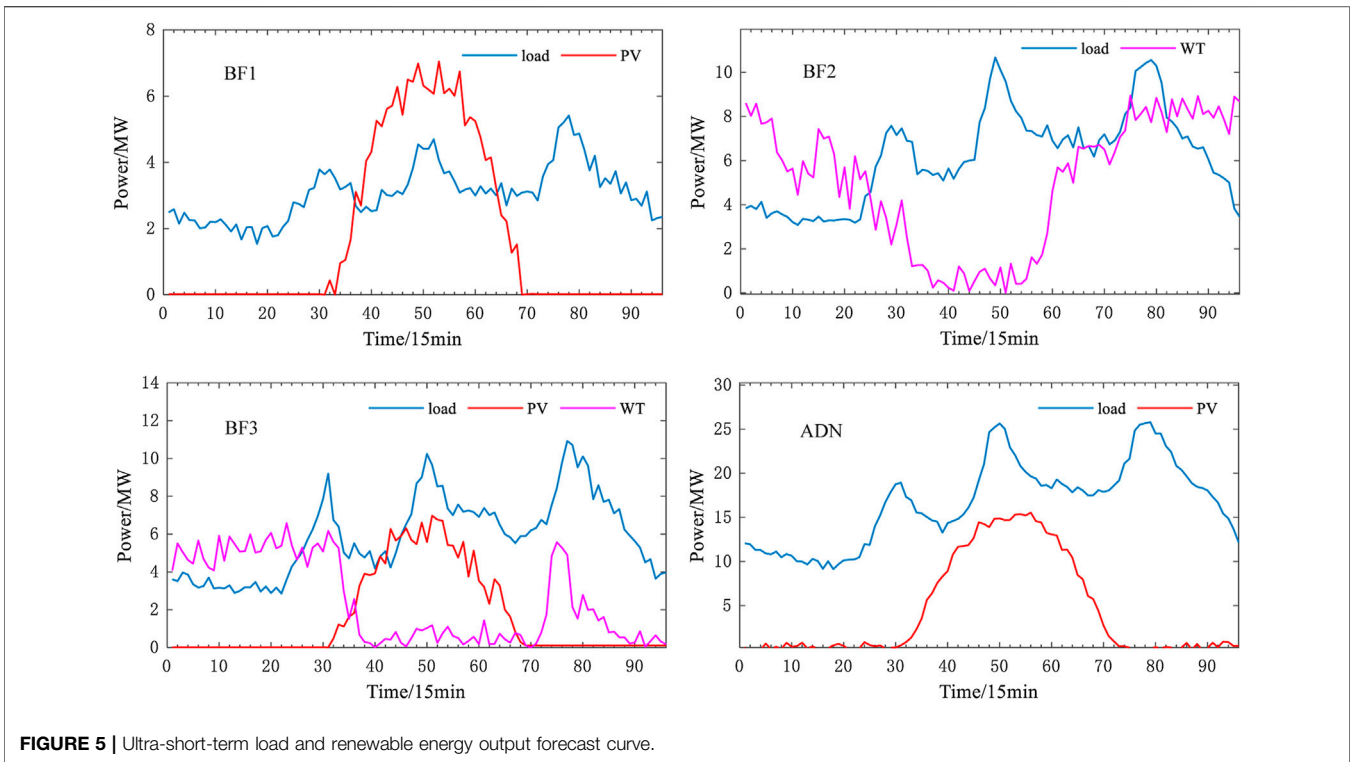
**Figure 6** shows the day-ahead optimal results. When the RESs output is larger than the load, the ESS is charging, and

when the RESs output is less than the load, the ESS is discharging and DGs begin to work. The fluctuation of RES generation is mainly compensated by the ADN when local DGs and ESSs in BFs cannot compensate it. When the PV output cannot meet the load, ESSs start to discharge at this time. HD is on with high-level output power. The total interactive power fluctuates between 7 and -5 MW.

**Figure 7** presents the dispatching strategy of the intra-day optimal model. The intra-day optimal dispatching strategy modifies the outputs of CDGs and BESSs without changing the status set by the day-ahead dispatch plans. There is a certain deviation between the dispatch command of the BFs obtained with optimizing the operation of the ADN and the interactive power curve obtained with optimizing the operation of the BFs. This is due to the different focus of optimal dispatching. In the optimized results, the nodes with BFs are equivalent to the controllable distributed power source, which accepts the dispatching instructions from the energy management center of ADN. Therefore, the local optimization layer executes the dispatching instructions of the globe optimization layer and adjusts the outputs of the controllable units in the branch feeders in time.

According to the power flow calculation, the equivalent voltage amplitude of BF2 is lower than 0.93. Therefore, the intra-day dispatching program of the main feeder needs to be started. The main feeder is optimized with minimizing the node voltage deviation. Then, the node controller accepts the dispatching instructions from the energy management center. Therefore, the outputs of the controllable units connected with branch feeders will be adjusted in time.





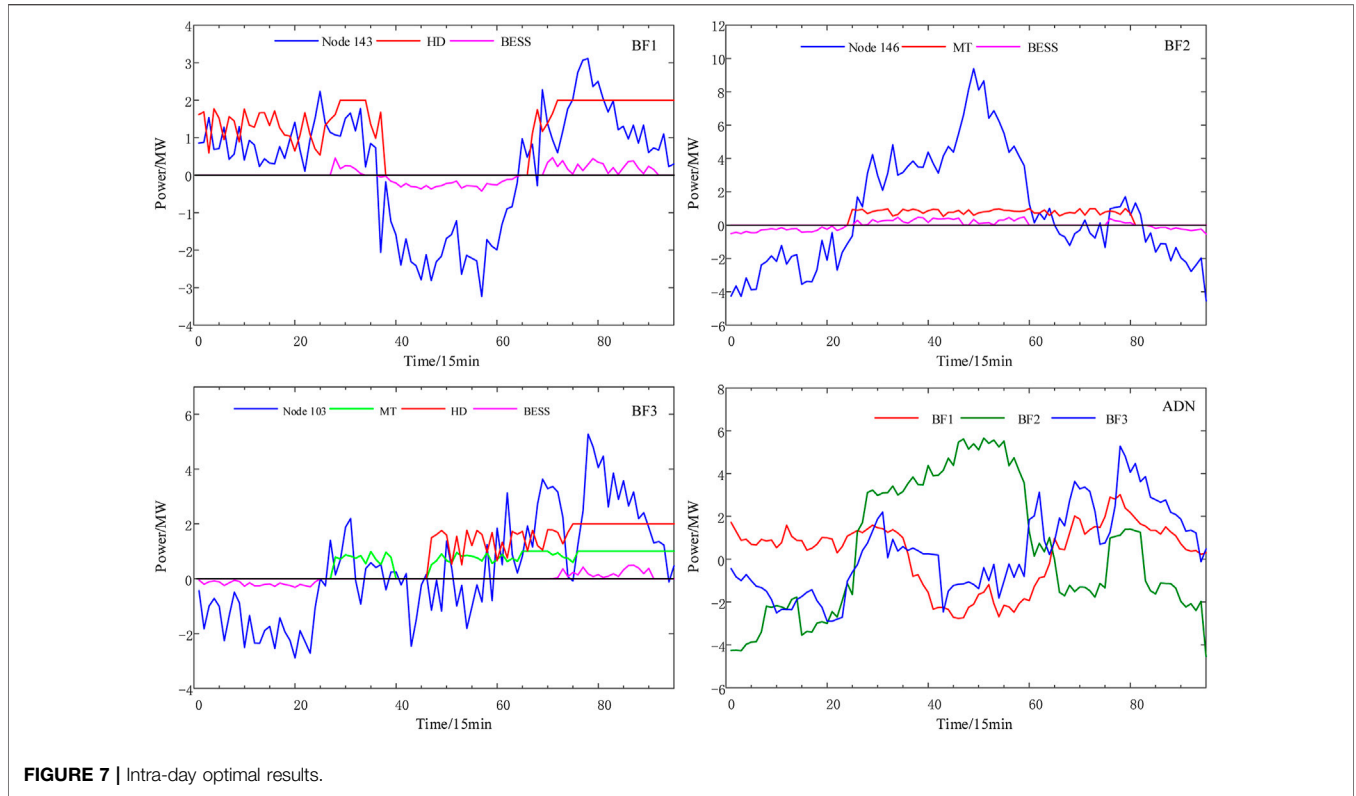


FIGURE 7 | Intra-day optimal results.

TABLE 6 | Renewable energy consumption rate on site of branch feeder.

BFs	Day-ahead	Intra-day	SO, $\sigma$ (%)	HO $\sigma$ (%)	After adjustment, $\sigma$ (%)
	SO, $\sigma$ (%)	HO, $\sigma$ (%)			
BF1	63.71	68.14	64.91	69.82	69.35
BF2	76.53	79.75	80.21	87.04	86.98
BF3	86.27	87.8	87.18	87.73	87.71

### Local Consumption of RESs

The local consumption rate of RESs is defined as Eq. 41. It is the proportion consumed by the branch feeder and the maximum output of RESs. The forecast results are used as the maximum outputs of RESs.

$$\sigma = \frac{\sum_{t=1}^T P_{RES}^{real}(t)}{\sum_{t=1}^T P_{RES}^{max}(t)} \Delta t \quad (41)$$

For a convenient illustration, SO is corresponding to the optimal results with single-layer energy management framework, and HO is corresponding to the optimal results with hierarchical energy management framework proposed in this paper. Table 6 presents the local consumption rate on site of BF.

As shown in Table 6, the dispatching strategy proposed in this paper can effectively promote the local consumption of RESs. If the node voltage exceeds the operation limit, the global optimization layer optimizes the power curve of the interaction between the nodes and the main feeder with the voltage deviation as the objective. The node controllers will adjust the outputs of the controllable units at the same time with maximizing the local consumption of renewable energy. On the one hand, it can reduce the power loss caused by power transmission. On the other hand, nodes accept the dispatching instructions of ADN center, which is convenient for management without an additional coordinated controller. Upon comparing

TABLE 7 | Day-ahead optimal operation cost of branch feeders.

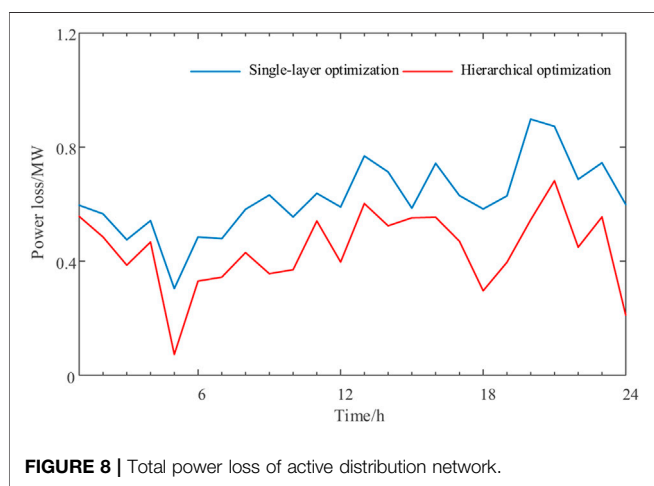
Type	BF1	BF2	BF3	HO	SO	HO
	SO	HO	SO			
Environmental cost (yuan/day)	390.59	377.97	1,164.59	1,083.91	708.27	713.65
Operation cost of battery energy storage system (yuan/day)	611.28	570	532.56	524.88	555.096	545.88
MT cost (yuan/day)	—	—	6,876.12	6,446.25	8,251.43	7,671.03
Electricity cost (yuan/day)	4,734.18	4,357.37	16,728.55	16,241.52	18,911.59	16,468.8
Total cost (yuan/day)	6,916.05	6,437.22	25,301.82	24,296.56	28,426.386	25,399.36

**TABLE 8 |** Intra-day optimal operation cost of branch feeders.

Type	BF1	BF2	BF3	HO	SO	HO
	SO	HO	SO			
Environmental cost (yuan/day)	459.33	459.33	1,067.23	914.25	637.22	587.13
Operation cost of battery energy storage system (yuan/day)	617.19	572.52	541.23	532.43	552.17	547.96
Micro-gas turbine cost (yuan/day)	—	—	6,776.12	7,092.3	8,251.43	7,385.97
Electricity cost (yuan/day)	5,334.08	5,321.9	16,728.55	11,547.3	14,931.74	12,069.22
Total cost (yuan/day)	6410.6	6322.93	25113.13	20086.28	24392.05	20590.28

**TABLE 9 |** Total cost in different confidence levels (yuan/day).

Confidence level (%)	BF1	BF2	BF3	Intra-day	Day-ahead	Intra-day
	Day-ahead	Intra-day	Day-ahead			
90	6,437.22	6,322.93	24,296.56	20,086.28	25,399.36	20,590.28
95	6,503.23	6,365.56	24,330.82	20,138.96	25,469.16	20,637.26



the results of day-ahead optimization and intra-day optimization, it was shown that the forecast errors of loads and RESs affect the optimal results and verifies the proposed method with two-stage hierarchical optimization.

Table 7 and Table 8 give the day-ahead and intra-day optimal operation cost of BFs, respectively.

By comparing the calculation results SO and HO, it is shown that the energy management strategy proposed in this paper can reduce the operating cost of nodes. At the same time, considering the voltage quality of the main feeder, the operating costs of BFs are increased less than before. The cost of purchasing electricity from the main feeder still occupies a large proportion.

The confidence level of the forecast error of RES affects the operation economy of ADN. The smaller the confidence level is set, the worse the operation economy is shown to be. Table 9 shows a list of the total operation cost of ADN under different confidence levels. It shows that a larger confidence level can help

**TABLE 10 |** Voltage deviation of active distribution network (ADN).

Time (h)	SO (p,u)	HO (p,u)	Time (h)	SO (p,u)	HO (p,u)
1	2.265	2.044	13	2.770	2.155
2	2.269	2.042	14	2.676	2.157
3	2.264	2.044	15	2.472	2.148
4	2.276	2.051	16	2.463	2.151
5	2.615	2.133	17	2.605	2.151
6	2.774	2.246	18	2.771	2.246
7	2.881	2.262	19	2.847	2.242
8	3.082	2.559	20	3.150	2.583
9	2.588	2.067	21	2.906	2.437
10	2.453	2.050	22	2.801	2.569
11	2.582	2.075	23	2.460	2.343
12	2.877	2.256	24	2.282	2.059

The day-ahead voltage deviation of ADN, with SO, is 63.129 p.u. By implementing the proposed dispatching strategy, the voltage deviation of ADN decreases to 53.07 p.u—that is, it decreases by 15.93%. It identifies that the proposed strategy can effectively reduce the voltage deviation of ADN.

reduce the operation cost of ADN. In engineering projects, the confidence level should be selected reasonably.

Figure 8 shows the total power loss of ADN.

As shown in Figure 8, the power loss of ADN is 10.570 MW, and it is reduced by 29.06%, in contrast with the power loss of SO at 14.9 MW. It indicates that the proposed strategy can effectively reduce power loss.

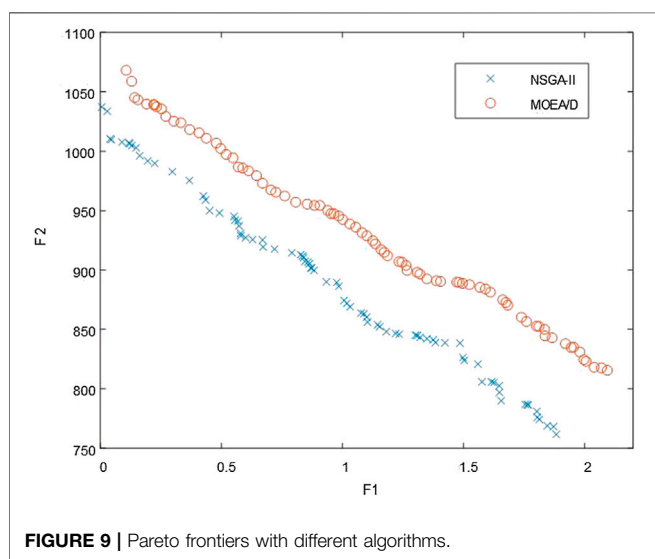
Table 10 presents the voltage deviation of ADN in day-ahead optimization results.

Table 11 imposes the carbon emissions at all scheduled times.

In Table 11, before optimal dispatching, the total carbon emission of all BFs was 79,676.357 kg. Using the energy management strategy proposed in this paper, the total carbon emission of all BFs was 62,217.997 kg, and the carbon emission was reduced to 17,458.36062 kg. That is, the carbon emission is reduced by 21.91%. It shows that the proposed strategy in this paper can effectively reduce carbon emissions. On the one hand,

**TABLE 11** | Carbon emissions at all scheduled times.

Time(h)	Carbon emissions (kg)		Time (h)	Carbon emissions (kg)		SO	HO
	SO	HO		SO	HO		
1	880.219	357.493	13	6,929.482	6,344.616		
2	825.083	501.824	14	4,611.475	4,327.891		
3	795.179	254.827	15	3,414.025	2,851.513		
4	701.729	269.516	16	2,501.120	2,084.275		
5	701.729	171.921	17	2,452.211	2,214.638		
6	803.590	483.388	18	4,340.106	3,630.196		
7	2,417.627	1,725.690	19	4,048.019	2,695.415		
8	5,163.787	4,372.198	20	7,266.420	5,365.835		
9	3,534.150	3,197.696	21	5,500.492	3,917.355		
10	3,038.716	2,992.126	22	4,972.577	3,294.039		
11	3,341.260	2,973.446	23	3,806.736	2,110.375		
12	5,102.475	4,927.074	24	2,528.150	1,154.650		



**FIGURE 9** | Pareto frontiers with different algorithms.

it reduces the amount of fossil fuels, and on the other hand, it reduces the emissions of environmental pollutant gases.

In order to verify the superiority of NSGA-II algorithm, the multi-objective evolutionary algorithm based on decomposition (MOEA/D) (Zhang and Li, 2007) is selected as the comparison algorithm to solve the proposed model. MOEA/D is also commonly used in multi-objective optimization models to avoid local optimization and approach the Pareto frontiers efficiently. The same parameters are set in two algorithms, and the confidence level is 90%. **Figure 9** shows the Pareto frontiers with different algorithms.

**Figure 9** indicates that the result of NSGA-II algorithm is more economical than that of MOEA/D. Besides this, the calculation time used by NSGA-II algorithm is 6.174 s, and the calculation time used by MOEA/D algorithm is 7.351 s. Therefore, the NSGA-II algorithm applied in this paper has an

advantage in solving the multi-objective complex optimization model.

In summary, the dispatching strategy proposed in this paper can effectively promote the local consumption of RESs and the economy operation of ADN and reduce carbon emission and power loss while supporting the power quality of nodes.

## CONCLUSION

This paper proposes the optimal dispatching strategy of ADN for promoting the local consumption of RESs. The two-stage hierarchical energy management framework is proposed, in which the structure of the dispatching system is simple and the optimal dispatching model is easier to be solved. The power flow in the main feeder and in the branch feeder is respectively optimized to improve the local consumption of RESs and the economical operation of ADNs. Besides this, the operation risk caused by the uncertainty of RES is quantified, so optimal results are friendly to the operators of ADNs.

## DATA AVAILABILITY STATEMENT

The original contributions presented in the study are included in the article/Supplementary Material, further inquiries can be directed to the corresponding author.

## AUTHOR CONTRIBUTIONS

HX: writing-original draft preparation, conception of the study, and methodology; WW: methodology and software; WW: software and data analyses; LT: data analyses and editing. All authors contributed to the article and approved the submitted version.

## REFERENCES

- Ahmadi, A., Charwand, M., Siano, P., Nezhad, A. E., Sarno, D., Gitizadeh, M., et al. (2016). A Novel Two-Stage Stochastic Programming Model for Uncertainty Characterization in Short-Term Optimal Strategy for a Distribution Company. *Energy*. 117, 1–9. doi:10.1016/j.energy.2016.10.067
- Bi, W., ShuDong, Y. W., and Yang, Q. (2020). “Real-time Energy Management of Microgrid Using Reinforcement Learning,” in 2020 19th International Symposium on Distributed Computing and Applications for Business Engineering and Science (DCABES), 38–41. doi:10.1109/dcabes50732.2020.00019
- Dubuisson, F., Chandra, A., and Rezkallah, M. (2020). *A Bacterial Foraging Optimization Technique and Predictive Control Approach for Power Management in a Standalone Microgrid*[C]//2020 IEEE Electric Power and Energy Conference (EPEC). Edmonton, AB: IEEE.
- Fan, M., Li, Z., Ding, T., Huang, L., Dong, F., Ren, Z., et al. (2021). Uncertainty Evaluation Algorithm in Power System Dynamic Analysis With Correlated Renewable Energy Sources. *IEEE Trans. Power Syst.* 36 (6), 5602–5611. doi:10.1109/tpwrs.2021.3075181
- Fang, W., Liu, H., Chen, F., Zheng, H., Hua, G., and He, W. (2017). DG Planning in Stand-Alone Microgrid Considering Stochastic Characteristic. *J. Eng.* 2017 (13), 1181–1185. doi:10.1049/joe.2017.0515
- Gildenhuis, T., Zhang, L., Ye, X., and Xia, X. (2019). Optimization of the Operational Cost and Environmental Impact of a Multi-Microgrid System. *Eng. Proced.* 158, 3827–3832. doi:10.1016/j.egypro.2019.01.865
- Ji, Y., Wang, J., Xu, J., and Li, D. (2021). Data-Driven Online Energy Scheduling of a Microgrid Based on Deep Reinforcement Learning. *Energies*. 14 (8), 2120. doi:10.3390/en14082120
- Kong, X., Yong, C., and Wang, C. (2019). Optimal Strategy of Active Distribution Network Considering Source–Network–Load. *IET Generation, Transm. Distribution*. 13 (1), 5586–5596. doi:10.1049/iet-gtd.2018.5781
- Li, Y., Fan, X., and Cai, Z. (2018). Optimal Active Power Dispatching of Microgrid and Distribution Network Based on Model Predictive Control[J]. *Tsinghua Sci. Technology*. 23 (3), 11. doi:10.26599/tst.2018.9010083
- Omaji, S., Javaid, N., and Khalid, A. (2020). Towards Real-Time Energy Management of Multi-Microgrid Using a Deep Convolution Neural Network and Cooperative Game Approach[J]. *IEEE Access*. 8, 161377–161395. doi:10.1109/ACCESS.2020.3021613
- Pant, M., Snasel, V., and Verma, S. (2021). A Comprehensive Review on NSGA-II for Multi-Objective Combinatorial Optimization Problems[J]. *IEEE Access*. 9, 57757–57791. doi:10.1109/ACCESS.2021.3070634
- Radhakrishnan, B. M., and Srinivasan, D. (2016). A Multi-Agent Based Distributed Energy Management Scheme for Smart Grid Applications. *Energy*. 103, 192–204. doi:10.1016/j.energy.2016.02.117
- Sannigrahi, S., Ghatak, S. R., and Acharjee, P. (2019). Multi-Scenario Based Bi-level Coordinated Planning of Active Distribution System under Uncertain Environment[J]. *IEEE Trans. Industry Appl.* 56 (1), 850–863. doi:10.1109/TIA.2019.2951118
- Somma, M. D., Graditi, G., and Heydarian-Forushani, E. (2017). Stochastic Optimal Scheduling of Distributed Energy Resources with Renewables Considering Economic and Environmental Aspects[J]. *Renew. Energy*. 116, 272–287. doi:10.1016/j.renene.2017.09.074
- Upadhyay, S., and Sharma, M. P. (2016). Selection of a Suitable Energy Management Strategy for a Hybrid Energy System in a Remote Rural Area of India. *Energy*. 94, 352–366. doi:10.1016/j.energy.2015.10.134
- Wang, Z., and Wang, J. (2015). Self-Healing Resilient Distribution Systems Based on Sectionalization into Microgrids. *IEEE Trans. Power Syst.* 30 (6), 3139–3149. doi:10.1109/tpwrs.2015.2389753
- Wu, K., Li, Q., Chen, Z., Lin, J., Yi, Y., and Chen, M. (2021). Distributed Optimization Method with Weighted Gradients for Economic Dispatch Problem of Multi-Microgrid Systems. *Energy*. 222, 119898. doi:10.1016/j.energy.2021.119898
- Wu, X., Cao, W., and Wang, D. (2019). A Multi-Objective Optimization Dispatch Method for Microgrid Energy Management Considering the Power Loss of Converters[J]. *Energies*. 12 (11), 1–19. doi:10.3390/en12112160
- Younesi, A., Shayeghi, H., Siano, P., and Safari, A. (2021). A Multi-Objective Resilience-Economic Stochastic Scheduling Method for Microgrid. *Int. J. Electr. Power Energy Syst.* 131 (1), 106974. doi:10.1016/j.ijepes.2021.106974
- Zhang, Q., and Li, H. (2007). MOEA/D: A Multiobjective Evolutionary Algorithm Based on Decomposition. *IEEE Trans. Evol. Computat.* 11 (6), 712–731. doi:10.1109/tevc.2007.892759
- Zhang, B., and Yan, N. (2018). “Research on Economic Dispatching Method of Active Distribution Network based on Multi-microgrids[C]//International Conference,” on perconductivity and Electromagnetic Devices, Tianjin, China (Chen Yang, China: Shenyang University of Technology), 1–2.
- Zhang, L., Chi, F., and Liu, H. (2020a). “Day-ahead Optimal Dispatch of Active Distribution Network with Micro-energy Grid Considering Demand Response [C]//2020,” in IEEE Sustainable Power and Energy Conference (ISPEC), Chengdu, China (Chengdu, China: IEEE), 1491–1498.
- Zhang, L., Ge, H., Ma, Y., Xue, J., Li, H., and Pecht, M. (2020b). Multi-Objective Optimization Design of a Notch Filter Based on Improved NSGA-II for Conducted Emissions. *IEEE Access*. 8, 83213–83223. doi:10.1109/access.2020.2991576
- Zhou, X., Ai, Q., and Yousif, M. (2019). Two Kinds of Decentralized Robust Economic Dispatch Framework Combined Distribution Network and Multi-Microgrids[J]. *Appl. Energy*. 253, 113588.1–113588.16. doi:10.1016/j.apenergy.2019.113588

**Conflict of Interest:** WW is employed by XJ Group Corporation.

The remaining authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

**Publisher’s Note:** All claims expressed in this article are solely those of the authors and do not necessarily represent those of their affiliated organizations or those of the publisher, the editors, and the reviewers. Any product that may be evaluated in this article or claim that may be made by its manufacturer is not guaranteed or endorsed by the publisher.

Copyright © 2022 Xie, Wang, Wang and Tian. This is an open-access article distributed under the terms of the Creative Commons Attribution License (CC BY). The use, distribution or reproduction in other forums is permitted, provided the original author(s) and the copyright owner(s) are credited and that the original publication in this journal is cited, in accordance with accepted academic practice. No use, distribution or reproduction is permitted which does not comply with these terms.

## GLOSSARY

**ADN** active distribution network

**BESS** battery energy storage system

**BF** branch feeder

**CDG** controllable distributed generator

**DRL** demand-side response loads

**ESS** energy storage system

**HD** hydro

**HO** hierarchical optimization

**MT** micro gas turbine

**PV** photovoltaics

**RESs** renewable energy sources

**SoC** state of charge of battery

**SO** single-layer optimization

**WT** wind turbine

**TL** transferable load

**T** index of scheduling periods,  $t = 1, 2, \dots, T$

**I** index of controllable DGs,  $i = 1, 2, \dots, N_{DG}$

**j** index of ESSs,  $j = 1, 2, \dots, M$

**N** index of transferable load,  $n = 1, 2, \dots, N_{TL}$

**M** index of interruptible load,  $m = 1, 2, \dots, N_{IL}$

$\alpha$  confidence level

$\sigma$  local consumption rate

### Parameters

$P_{G,\max/\min}$  maximum/minimum exchange power between ADN and BF

$P_{G,t}$  purchase and sale of electricity at time  $t$

$P_{CDG_{i,t}}$  output power of the  $i$ th CDG at time  $t$

$P_{CDG,\max/\min}$  maximum/minimum power of CDG

$P_{L,i}$ 、 $Q_{L,i}$  active and reactive load of ADN at time  $t$

$N_{\text{life}}$  life cycle of ESS at corresponding discharge depth/cycle life at charge/discharge depth

$P_{TL_{n,t}}$  dispatching power of the  $n$ th TL at time  $t$

$P_{IL_{m,t}}$  dispatching power of the  $m$ th IL at time  $t$

$P_{j,t}^{\text{ch/dis}}$  charging/discharging power of  $j$ th ESS at time  $t$

$P_{\text{ch/dis,max}}$  maximum charge/discharge power of ESS

$P_{\text{line},t}$  transmission power of the ADN

$P_{\text{line,max}}$  maximum transmission power of ADN

$P_{\text{RES}}^{\max}(t)$  the maximal output power of RESs at time  $t$

$\bar{P}_{\text{PV/WT},t}$  forecast power of PV/WT at time  $t$  in the BF

$P_{\text{PV/WT},t}$  power of PV/WT at time  $t$  in the BF

$P_{Tk,i,t}$ 、 $Q_{Tk,i,t}$  active power and reactive power from  $k$ th BF at time  $t$

$N_{\text{TL/IL}}$  number of transferable/interruptible loads

$P_{\text{PCC},i,t}$ 、 $Q_{\text{PCC},i,t}$  active and reactive power from the upper grid

$P_{T,\max/\min}$  maximum and minimum exchange power between ADN and BF

$P_{\text{PCC,max}}$  maximum power injected by the upper grid

$P_{\text{RES}}^{\text{real}}(t)$  the power of RESs consumed by BFs at time  $t$

$P_{\text{PE},t}$  purchase and sales of electricity at time  $t$

$P_{ij,t}$  active power flowing through the line  $ij$  at time  $t$

$Q_{ij,t}$  reactive power flowing through the line  $ij$  at time  $t$

$R_{\text{PV/WT},t}$  forecast error power of PV/WT at time  $t$  in the BF

$c_{\text{CDG},t}$  generation cost of CDGs at time  $t$

$c_{\text{ESS},t}$  operation cost of ESSs at time  $t$

$C_{\text{inv}}$  the initial investment cost of ESS

$c_{\text{PE},t}$  electricity purchasing cost at time  $t$

$c_{\text{TL}}$  unit dispatch cost of transferable load

$c_{\text{IL}}$  unit dispatch cost of interruptible load

$c_{\text{DRL},t}$  dispatching cost of schedulable loads at time  $t$

$c_{e,t}$  environment cost at time  $t$

$c_{\text{grid},t}$  electricity purchase and sale cost at time  $t$

$c_{\text{loss}}$  unit charge and discharge loss cost of ESS

$N_{\text{life}}$  life cycle of ESS at corresponding discharge depth/cycle life at charge/discharge depth

$\mu_j^{\text{ch/dis}}$  charging/discharging efficiency of  $j$ th ESS

$D_{oD,t}$  dispatch depth of ESS at time  $t$

$E_{\text{Br}}$  rated capacity of BESS

$\eta_j^{\text{ch/dis}}$  charge/discharge efficiency of ESS

$\text{SoC}_{\text{B},t}$  state of charge of BESS at time  $t$

$\text{SoC}_{\text{B,max/min}}$  maximum and minimum SOC of BESS

$X_{ij}$  reactance of branch  $k$  between node  $i$  and  $j$

$G_{ij}$ 、 $B_{ij}$  real and imaginary parts of the admittance matrix between node  $i$  and node  $j$

$Z_{ij}$  impedance of line  $ij$

$V_{ij,t}$  end voltage of line  $ij$  at time  $t$

$V_{i,t}$  the voltage amplitude of node  $i$  at time  $t$

$V_N^i$  the rated voltage of node  $i$

$V_{\max/\min}$  maximum and minimum voltage

$V_{\text{es}}$  environmental value of class  $s$  pollutants

$\delta_{ij,t}$  voltage phase difference between node  $i$  and  $j$

$T_{d,s}$  operating time of CDG

$T_{d,\min}$  minimum operating time of CDG

$T_{d,\max}$  maximum operating time of CDG

**UR** maximum ramp down rate of CDG

**UD** maximum ramp up rate of CDG

$\mu_i^t$  operating status of the  $i$ th CDG at time  $t$

$\lambda_{\text{CDG}_i}$  startup cost of the  $i$ th CDG

$Q_{i,s,t}$  emission of class  $s$  pollutants of the  $i$ th CDG at time  $t$

$\Delta t$  scheduling interval