



# [Research on the Unstable Branch](https://www.frontiersin.org/articles/10.3389/fenrg.2021.835440/full) [Screening Method for Power System](https://www.frontiersin.org/articles/10.3389/fenrg.2021.835440/full) [With High-Proportion Wind Power](https://www.frontiersin.org/articles/10.3389/fenrg.2021.835440/full)

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The sooner the system instability is predicted and the unstable branches are screened, the timelier emergency control can be implemented for a wind power system. In this paper, aiming at the problem that the existing unstable branch screening methods are lack prejudgment, an unstable branch screening method for power system with highproportion wind power is proposed. Firstly, the equivalent external characteristics model of the wind farm was deduced. And based on this, the out-of-step oscillation characteristics of the power system with high proportion wind power was analyzed. Secondly, based on the oscillation characteristics, line weak-connection index (LWcI) was proposed to quantify the stability margin of a branch. Then an instability prediction method and an unstable branch screening method were proposed based on LWcI and voltage phase angle difference. Finally, the rapidity and effectiveness of the proposed method are verified through the simulation analysis of IEEE-118 system.

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# 1 INTRODUCTION

With the proposal of "carbon peaks" and "carbon neutralization" goals, the penetration of renewable energy is increasing rapidly. However, different from synchronous generator, wind power and other renewable energy units have the disadvantages of low inertia and weak poor disturbance immunity, which have a profound impact on the stability of the grid [\(Liu et al., 2019](#page-8-0); [Shen and](#page-8-1) [Raksincharoensak, 2021a\)](#page-8-1). Power outage accidents ([Nagpal et al., 2018](#page-8-2); [Alhelou et al., 2019](#page-7-0); [Liu,](#page-8-3) [2019;](#page-8-3) [Yang et al., 2021c](#page-8-4)) in recent years indicate that due to the replacement of synchronous machines by renewable energy sources, the risk of power angle instability is greatly increased, and the development rate of chain fault is greatly accelerated. Therefore, how to prejudge the instability of the system and screen unstable branches as early as possible, so as to reserve more time to guarantee the implementation of emergency control, has become a research hotspot.

Currently, research results about instability criteria are mainly from traditional power systems. For example, Yang ([Yang et al., 2006](#page-8-5)) proposed to use the extended equal area criterion (EEAC) to analyze the transient stability. Yan ([Yan et al., 2011\)](#page-8-6) used the maximal Lyapunov exponent (MLE) to prejudge the rotor angle stability. Saunders ([Saunders et al., 2014](#page-8-7)) analyzed transient stability by constructing transient potential energy functions. Yang ([Yang et al., 2021b\)](#page-8-8) adopted data-driven method to study power system security and stability problem. This paper was the first study for SCUC problems, it can accommodate the mapping samples of SCUC, and consider the various input factors that affect SCUC decision-making, possessing strong generality, high solution accuracy, and efficiency over traditional methods. The above methods can prejudge the transient stability of the grid quickly using generator information such as rotor angle, but the further application in the



<span id="page-1-0"></span>

emergency control such as the splitting control is limited because the splitting section cannot be determined directly. Therefore, some scholars designed some new instability criterion using the branch response information, such as ucosφ criterion [\(Yang et al.,](#page-8-9) [2013](#page-8-9); [Zhang et al., 2021](#page-8-10)), phase angle criterion [\(Regulski et al.,](#page-8-11) [2018](#page-8-11); [Shen et al., 2021a](#page-8-12)), bus voltage frequency criterion ([Zhang](#page-8-13) [et al., 2019;](#page-8-13) [Yang et al., 2022](#page-8-14)), apparent impedance differential method ([Sreenivasachar, 2021;](#page-8-15) [Shen and Raksincharoensak,](#page-8-16) [2021b](#page-8-16)) and so on. Compared with methods using generator response information, these methods can not only prejudge the unstable state of the system, but also accurately capture the unstable branches and the splitting section. However, the disadvantage is that these methods do not start until the instability accident has occurred (or approach to instability), thus it is difficult to reserve sufficient time for emergency control.

Research on the instability criterion of the high proportion renewable energy power system is still in the preliminary stage, and relevant work is mainly focused on the influence of wind power integration on transient stability ([Ma et al., 2017](#page-8-17); [Liu et al.,](#page-8-18) [2017](#page-8-18); [Zheng et al., 2019](#page-8-19); [Shen et al., 2021b\)](#page-8-20). As for the research on the instability criterion, Wei [\(Wei et al., 2021](#page-8-21); [Yang et al., 2021a\)](#page-8-22) and Qin [\(Li et al., 2021;](#page-7-1) [Qin et al., 2021](#page-8-23)) respectively analyzed the influence of wind and photovoltaic power integration on oscillation center migration, but failed to propose oscillation center identification method and instability criterion. Chen ([Chen et al., 2020;](#page-7-2) [Li et al., 2021](#page-7-1)) proposed a new transient stability prediction method by defining a new stability index, but still failed to capture the unstable branch. Liu [\(Liu et al., 2020\)](#page-7-3) proposed to use the slow coherency theory to study the coherency group of wind power system, but the impact of actual faults cannot be fully considered.

Therefore, aiming at the problem that the existing instability criterion lacks prejudgment, a system instability prediction method and an unstable branches screening method are proposed in this paper. which can predict power angle instability earlier and screen unstable branches accurately.

The rest of this paper is organized as follows. In [Section 2](#page-2-0), the out-of-step oscillation characteristics of the high proportion wind power system is analyzed. In [Section 3](#page-3-0), the line weak-connection index (LWcI) is proposed to quantify the stability margin, and the unstable branches screening method is proposed. Case study and discussion are shown in [Section 4](#page-6-0). [Section 5](#page-7-4) concludes this study by summarizing key findings and contributions of this paper.

# <span id="page-2-0"></span>2 OUT-OF-STEP OSCILLATION CHARACTERISTICS OF WIND POWER **SYSTEM**

## 2.1 Equivalent External Characteristic Model of Wind Farm

Taking doubly-fed induction generator (DFIG) as an example, the control strategy is shown in [Figure 1A](#page-1-0) ([Wang et al., 2015](#page-8-24)). In steady state, DFIG adopts Maximum Power Point Tracking (MPPT) control strategy. When the system is disturbed, DFIG limits the active power output under the fault ride-through control, and outputs reactive power to support the grid. After the fault is cleared, DFIG switches back to MPPT control.

Obviously, without additional control, DFIG cannot actively respond to the disturbance of the system. When the system is disturbed, the output power of DFIG do not oscillate like a synchronous generator, but quickly return to the original state. Therefore, there is no power angle swing between DFIG and synchronous generator in electromechanical time scale. Thus, DFIG can be regarded as a power source without inertia, and its equivalent external characteristics can be equivalent to negative resistance and negative reactance in parallel:

$$
r = -\frac{u_s^2}{P_{\text{gen}}}
$$
  

$$
x = -\frac{u_s^2}{Q_{\text{gen}}}
$$
 (1)

Where the negative sign indicates the power injected into the bus.

In addition, if the system is still transient stable after the fault is cleared, DFIG can quickly recover to the pre-fault state and the output power also quickly resumes stability. So the equivalent impedance can be considered constant. If the system is already unstable, the output power of DFIG will oscillate due to the oscillation of the grid voltage. And the equivalent impedance also oscillates. Considering that there is a certain inertia in the system, it takes a certain amount of time from fault removal to complete instability, during which the output power of DFIG does not change dramatically, so it can be simply considered that the equivalent impedance during this period is constant.

# <span id="page-2-2"></span>2.2 Out-of-step Oscillation Characteristics of Wind Power System

Taking an equivalent two-machine system with a DFIG-based wind farm integrated as an example to analyze the out-of-step oscillation characteristics of wind power system. As shown in [Figure 1B](#page-1-0), bus O is the common coupling point of the wind farm, and the voltage vector can be expressed as  $U_o \angle \theta_o$ . r and x are equivalent resistance and reactance of the wind farm respectively.  $E_1$  and  $E_2$  are the equivalent potentials of generator  $G_1$  and  $G_2$ respectively, and  $\delta$  is the rotor angle difference.  $X_1$  and  $X_2$  are equivalent resistance between  $G_1$  and bus O, bus O and  $G_2$ , respectively. For convenience analysis, the  $X_2$  is divided into 10 equivalents by points  $n_1~n_1$ , and each branch section is represented by  $B_{1-2} \sim B_{10-11}$ . The voltage vector of any point M between the bus O and  $G_2$  is expressed as  $U_m\angle\theta_m$ , and its position function is  $\lambda = X_m/X_2$ ,  $\lambda \in [0,1]$ .

<span id="page-2-1"></span>Based on the node voltage method, the voltage vector of bus O can be expressed as:

$$
\dot{U}_o = \frac{Z_{\Sigma}}{jX_1}E_1e^{j\delta} + \frac{Z_{\Sigma}}{jX_2}E_2
$$
 (2)

Where  $Z_{\Sigma} = \frac{1}{G + \frac{1}{jX_1} + \frac{1}{jX_2}}$ ,  $G = \frac{1}{r} + \frac{1}{jx}$ .

Considering that the active power output of DFIG is limited under low voltage ride-through (LVRT) control, so the  $\frac{1}{r}$  is very

<span id="page-3-1"></span>small, and the real part of  $Z_{\Sigma}$  can be ignored. Thus, the expression of the voltage vector at bus O can be rewritten as:

$$
\dot{U}_o = |Z_{\Sigma}| \left( \frac{E_1 e^{j\delta}}{X_1} + \frac{E_2}{X_2} \right)
$$
 (3)

As shown in [Eq. 3](#page-3-1), the integration of wind farm changes the amplitude of  $Z_{\Sigma}$ , thereby changing the voltage amplitude of the common coupling point. The larger the wind farm output power, the greater the  $Z_{\Sigma}$ , the greater the voltage amplitude of the common coupling point.

In addition, according to Yang [\(Yang et al., 2013\)](#page-8-25), the unequal voltage on both sides of the branch is one of the reasons for the migration of out-of-step center. When the voltage amplitude on both sides of the branch is unequal, the out-of-step center migrates to the side where the voltage amplitude is smaller. Therefore, the integration of wind power increases the voltage amplitude of the common coupling point, resulting in the unequal voltage amplitude on both sides of the branch, which in turn leads to the migration of the out-ofstep center to the side where the voltage amplitude is smaller.

<span id="page-3-2"></span>Then, according to Ohm's law, the following equation exists:

$$
\frac{\dot{U}_o - E_2}{jX_2} = \frac{\dot{U}_o - \dot{U}_m}{jX_m}
$$
(4)

Therefore, based on [Equation 2](#page-2-1) and [Equation 4](#page-3-2), the voltage vector of point M can be expressed as:

$$
\dot{U}_m = \frac{Z_{\Sigma}}{jX_1} (1 - \lambda) E_1 e^{j\delta} + E_2 \left[ \lambda + \frac{Z_{\Sigma}}{jX_2} (1 - \lambda) \right]
$$
(5)

<span id="page-3-3"></span>Ignoring the real part of  $Z_{\Sigma}$ , the expression of voltage amplitude and phase angle at point M can be written as:

$$
U_m =
$$
\n
$$
\sqrt{\left(\frac{Z_{\Sigma}(1-\lambda)}{Z_1}E_1\cos\delta + E_2\left[\lambda + \frac{Z_{\Sigma}(1-\lambda)}{Z_2}\right]\right)^2 + \left(\frac{Z_{\Sigma}(1-\lambda)}{Z_1}E_1\sin\delta\right)^2}
$$
\n
$$
\theta_m = \arctan\frac{Z_{\Sigma}}{Z_1}(1-\lambda)E_1\cos\delta + E_2\left[\lambda + \frac{Z_{\Sigma}}{Z_2}(1-\lambda)\right]
$$
\n(6)

According to [Eq. 6](#page-3-3), the  $U_m$  and  $\theta_m$  are related to the position function  $\lambda$ , the output power of wind farm, the power angle difference and so on. Thus, assuming that  $E_1 = E_2 = 1.0$ ,  $X_2 = 3X_1$  0.3, and the output power of the wind farm under LVRT control is  $0.1 + j0.5$ , the temporal and spatial distribution law of voltage amplitude  $U_m$  and  $\theta_m$  are shown in **[Figures 1C](#page-1-0)–[H](#page-1-0)**.

[Figures 1C](#page-1-0)–[E](#page-1-0) show that with the increase of  $\delta$ , the voltage  $U_m$ at any position on the branch decreases and then increases, getting the minimum value when  $\delta = 180^{\circ}$ . Meanwhile, the variation amplitude of  $U_m$  varies from location to location, so there is always a point where the variation is the most drastic, called the out-of-step center. According to [Figure 1E](#page-1-0), the out-ofstep center is located between  $n_4$  and  $n_5$ .

According to [Figures 1F](#page-1-0)–[H](#page-1-0), when  $\delta$  increases from 0° to 180°, for the node between the out-of-step center and  $G_1$ ,  $\theta_m$  changes

monotonically in (0°, 180°). While for the node between the outof-step center and  $G_2$ ,  $\theta_m$  firstly increases and then decreases, and the maximum value is no more than 90° . Therefore, only for the branch where the out-of-step center is located, the voltage phase difference  $\Delta\theta_m$  variation rule is consistent with the power angle difference δ.

According to [Figures 1I,J](#page-1-0), as the output power of wind farm increases, the  $U_m$  at point  $n_4$  increases, and the maximum value of  $\Delta\theta_{\rm m}$  at B<sub>5-6</sub> increases until the  $\Delta\theta_{\rm m}$  changes monotonically between (0° , 180° ), indicating that the out-of-step center migrates from point  $n_4$  to point  $n_5$ , until it completely enters into  $B_{5-6}$ .

In summary, the output power of wind farm changes the flow distribution and voltage level of the system, ultimately affecting the system transient stability and the out-of-step center position. However, the phenomenon that voltage amplitude drops sharply, and the voltage phase angle difference of the branch where the out-of-step center located increases monotonously are still exist, which can be used to predict the transient stability of the system and capture the unstable branch.

# <span id="page-3-0"></span>3 INSTABILITY PREJUDGMENT CRITERIA AND UNSTABLE BRANCH SCREENING METHOD

#### 3.1 Line Weak-Connection Index (LWcI)

According to the conclusion in [Section 2](#page-2-0), when the out-of-step oscillation occurs, one or more branches loses stability, resulting in a sharp drop of voltage at each point of the branches. Considering that the voltage reduction at the oscillation center is the most severe ([Yang et al., 2013](#page-8-25)), so the voltage of the oscillation center can be used to measure the stability margin of a branch. However, if the oscillation center is not on the branch due to the oscillation center migration, the voltage at one end of the branch is the minimum voltage, which is much greater than the oscillation center voltage. And the result can be conservative and misjudgment can occur. Therefore, in order to prevent misjudgment as the oscillation center migrates outside the branch, the terminal voltage can be used to correct the out-of-step center voltage. Thus, Line weak-connection Index (LWcI) is defined to reflect the stability margin of a branch:

<span id="page-3-4"></span>
$$
LWcI =
$$
\n
$$
\begin{cases}\nU_A U_B |\sin \Delta \theta| \\
\sqrt{U_A^2 + U_B^2 - 2U_A U_B \cos \Delta \theta}, & U_{AB} > U_{ha} \text{ and } U_{AB} > U_{hb} \\
\min \{U_A, U_B\}, & U_{AB} < U_{ha} \text{ or } U_{AB} < U_{hb}\n\end{cases}
$$
\n(7)

Where  $U_A$  and  $U_B$  are terminal voltage amplitude of a branch,  $\Delta\theta$ is the voltage angle difference on both sides of a branch, all of which can be obtained through the WAMS system.  $U_{AB} = \sqrt{U_A^2 + U_B^2 - 2U_A U_B \cos \theta}, \quad U_{hA} = \sqrt{U_A^2 - U_h^2}$  $U_{AB} = \sqrt{U_A^2 + U_B^2 - 2U_AU_B\cos\theta}, \quad U_{hA} = \sqrt{U_A^2 - U_h^2}, \quad U_{hB} =$  $U_B^2-U_h^2$  $\sqrt{U_B^2-U_h^2}$ .



<span id="page-4-0"></span>According to [Eq. 7](#page-3-4), there is a negative correlation between LWCI and  $\Delta\theta$ . The larger the  $\Delta\theta$ , the smaller the branch stability margin, the smaller the LWcI. Therefore, LWcI can be used to prejudge the transient stability of the wind power system.

Further, according to **[Section 2.2](#page-2-2)**, only the  $\Delta\theta$  of the unstable branch varies monotonously in (−180°, 180°). Thus, there are significant differences in the trajectories between the unstable branches and others in the plane with  $\Delta\theta$  as the horizontal axis and LWcI as the vertical axis.

Taking the wind power system in [Figure 1B](#page-1-0) as an example, the trajectory of each branch in LWcI- $\Delta\theta$  plane when the system is stable and unstable is shown in [Figure 2](#page-4-0).

<span id="page-4-2"></span>As shown in [Figures 2A,B](#page-4-0), the  $\Delta\theta$  of all branches constantly oscillate and decays when the power angle is stable. Taking one period as an example, during  $t_1 \sim t_2$ , the ∆ $\theta$  increases, and the stability margin of all branches decreases, so the trajectories in LWcI- $\Delta\theta$  plane shows a monotonically decreasing trend, that is:

$$
\begin{cases}\text{LWcl}(t_i) - \text{LWcl}(t_{i-1}) < 0\\ \Delta\theta(t_i) - \Delta\theta(t_{i-1}) > 0\end{cases}
$$
\n(8)

<span id="page-4-1"></span>During  $t_2 \sim t_3$ , the ∆ $\theta$  of each branch decreases and the stability margin increases, as shown in [Eq. 9](#page-4-1). Therefore, an "upward inflection point" appears on the trajectory in LWcI- $\Delta\theta$  plane, indicating that there is no risk of instability in this cycle.

$$
\begin{cases}\text{LWcl}(t_i) - \text{LWcl}(t_{i-1}) > 0\\ \Delta\theta(t_i) - \Delta\theta(t_{i-1}) < 0\end{cases}
$$
\n(9)

As shown in **[Figure 2C](#page-4-0)**, only the  $\Delta\theta$  of B<sub>5-7</sub> exceeds 180<sup>°</sup>, ich is the unstable branch. Corresponding to **Figure 2D**, only which is the unstable branch. Corresponding to [Figure 2D](#page-4-0), only the trajectory of  $B_{5-7}$  monotonically decreases, satisfying [Eq. 8](#page-4-2). While for a branch which is still stable, because the extreme value of  $\Delta\theta$  exists, a "downward inflection point" appears. After crossing the "downward inflection point", as the system is already unstable, the voltage of each node is still decreasing, so the LWcI and  $\Delta\theta$  both decrease, as shown in.

$$
\begin{cases}\text{LWcl}(t_i) - \text{LWcl}(t_{i-1}) < 0\\ \Delta\theta(t_i) - \Delta\theta(t_{i-1}) < 0\end{cases}
$$
(10)

Therefore, the "unstable branch capture area", which is shown in [Figure 2D](#page-4-0), can be used to prejudge the system instability and screen the unstable branch. If the trajectory of a branch always satisfies [Eq.](#page-4-2) [8](#page-4-2) and enters into the "unstable branch capture area", which can be expressed as in [Eq. 11](#page-4-3), the stability margin of the branch is significantly reduced and the system is at risk of instability.

$$
\left\{\frac{\text{LWcl}}{\Delta \theta} < \text{LWcl}(t_i) < \overline{\text{LWcl}}\\ \n\frac{\Delta \theta}{\Delta \theta} < \Delta \theta(t_i) < \overline{\Delta \theta} \n\tag{11}
$$

<span id="page-4-3"></span>Where LWcI and LWcI represent the lower and upper limits of LWCI, respectively.  $\Delta\theta$  and  $\Delta\theta$  represent the lower and upper limits of  $\Delta\theta$ , respectively.

### 3.2 Unstable Branch Screening Process

The system instability prediction and unstable branch screening process proposed in this paper is shown in [Figure 3](#page-5-0). After the

<span id="page-5-0"></span>



<span id="page-6-3"></span>

<span id="page-6-1"></span>fault is cleared, the voltage phase angle difference of each branch is firstly calculated. As shown in [Eq. 12](#page-6-1), if it is greater than the threshold, the stability margin of the branch needs further analysis.

$$
\Delta\theta_i > \Delta\theta_{th} \tag{12}
$$

<span id="page-6-2"></span>Secondly, calculate LWcI of the branch which satisfies [Eq. 12](#page-6-1). If the value is lower than the threshold as shown in [Eq. 13](#page-6-2), the stability margin is already small, and it is necessary to monitor the trajectory in the LWcI- $\Delta\theta$  plane.

$$
LWcl_i \leq LWcl_{th}
$$
 (13)

Thirdly, if the trajectory of the branch satisfying [Eq](#page-6-1)[uatio](#page-4-2)[n 12](#page-6-1) and [Equation 13](#page-6-2) in the LWcI- $\Delta\theta$  plane always satisfies Eq. 8, the stability margin of the branch keeps decreasing and the risk of instability keeps increasing. When the trajectory satisfies [Eq. 11](#page-4-3), that is, it enters into the "unstable branch capture area", the branch can be considered as an unstable branch.

Finally, traverse all branches in turn, and then repeat the steps above based on the data at the next sampling moment until all unstable branches constitute a splitting section.

## <span id="page-6-0"></span>4 CASE STUDY

In order to verify the effectiveness of the method proposed in this paper, the IEEE-118 system with wind farm integrated is built on the PSS/E platform. As shown in [Figure 4A](#page-6-3), the synchronous generators on the bus 89, 100 and 103 are replaced by wind farms, the capacity of which is 450, 300 and 300 MVA, respectively. Meanwhile, another wind farm with capacity of 75MVA is integrated at the bus 25. Assume that the output power of wind farms equals to the rated power, and the load power is 4252 MW, so the penetration rate of wind power is 26.46%.

According to [Eq. 7](#page-3-4), when the voltage on both sides is equal and the  $\Delta\theta$  is equal to 130°, LWcI = 0.41. Considering that the system is still stable at that time, so set  $LWcl_{th} = 0.4, \theta_{th} = 20^{\circ}$ . According to the variation rule of  $\Delta\theta$  of an unstable branch, set  $LWcI = 0$ , and  $\overline{LWcI} = 0.2$ ,  $\Delta\theta = 80^{\circ}$  and  $\overline{\Delta\theta} = 180^{\circ}$ . It is worth mentioning that the setting parameters of the "unstable branch capture area" can be adjusted. The larger the  $\Delta\theta_m$  and the smaller the LWcI, the stronger the reliability of the criterion but the worse the speed.

Assume that a three-phase short circuit failure occurs on branch 8–30 at 0.1 s, and lasts 0.2 s. The transient response of the system is shown in [Figures 4B](#page-6-3)-[E](#page-6-3). Considering that there are too many branches, only the branches whose voltage phase angle difference is greater than 20° are displayed. According to [Figures 4B,C](#page-6-3), the power angle of  $G_{10}$  and  $G_{12}$  increases rapidly after the fault is cleared, and the voltage phase angle difference of branch 8–30 13–15 14–15 and 16–17 continues to increase, indicating that  $G_{10}$ and  $G_{12}$  lose stability compared with other generators, and the outof-step center is located on branch 8–30 13–15 14–15 and 16–17.

As shown in **[Figure 4D](#page-6-3)**, the LWcI of each branch is monotonically decreasing when the fault is removed, indicating that the stability margin of each branch declines continuously. Around 0.39s, the LWcI of branch 8–<sup>30</sup> firstly decreases to 0.4, satisfying [Eq. 13](#page-6-2). And the program begins to monitor the trajectory of each branch in the LWcI- $\Delta\theta$  plane to screen the unstable branches. Corresponding to [Figure 4E](#page-6-3), the trajectories of the branch 8–30 13–15 14–15 and 16–17 in the LWcI- $\Delta\theta$  plane are always monotonously decreasing, and enter into the " unstable branch capture area" at 0.45, 0.47, 0.48 and 0.49 s respectively. It indicates that the above branches are all unstable and constitute a splitting section, as shown by the red dashed line in [Figure 4A](#page-6-3). By contrast, at 0.49 s, the trajectories of the branch 9–8, 10–9, 11–13 are located at points B, C and D respectively. Obviously, there have been inflection points in the trajectories of branch 9–8 and 10–9, indicating that there is no out-of-step center on branch 9–8 and 10–9. For branch 11–13, the trajectory still drops monotonically, so it still needs to be monitored. But according to "upward inflection point" in the trajectory during the period of 0.49–0.51 s, it can be judged that branch 11–13 are not unstable branch, either.

In summary, the unstable status of the system can be prejudged and all unstable branches can be accurately screened at 0.49 s using the method in this paper. If the traditional method ([Tang et al., 2015](#page-8-26)) is adopted, the complete splitting section cannot be obtained until the system is already unstable at 0.57 s. Therefore, compared with other methods, the

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method proposed in this paper can prejudge unstable status of the system and screen all the unstable branches earlier under the premise of ensuring correctness, and thus reserve more time for emergency control such as splitting control.

#### <span id="page-7-4"></span>5 CONCLUSION

An instability prediction method and an unstable branch screening method are proposed in this paper. Some conclusions are summed up as follows. Firstly, when the wind power system loses stability, the bus voltage amplitude drops, and the voltage phase angle difference of the unstable branch increases, which are the key response information mapped on the branch. Secondly, according to the response information, an indicator called line weak-connection index (LWcI) is built to assess the stability margin of a branch. The smaller the LWcI, the smaller the stability margin of the branch. Thirdly, the trajectories of different branches are different in the plane composed of LWcI and voltage phase angle difference. Only the trajectory of the unstable branch shows a monotonically decreasing trend, while there are "upward inflection points" or "downward inflection points" in the trajectories of other branches. Depending on the difference of trajectory characteristics, the unstable branch can be accurately screened.

#### DATA AVAILABILITY STATEMENT

The original contributions presented in the study are included in the article/supplementary material, further inquiries can be directed to the corresponding author.

### AUTHOR CONTRIBUTIONS

FT was responsible for methodology and revision of the manuscript. XW was responsible for writing the original draft. YG and JQ were responsible for data processing and supervision. JX and XL were responsible for visualization and supervision. All authors contributed, read, and approved the submitted version.

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