



# A Flexible Ensemble Algorithm for Big Data Cleaning of PMUs

Long Shen, Xin He, Mingqun Liu, Risheng Qin\*, Cheng Guo, Xian Meng and Ruimin Duan

Electric Power Research Institute of Yunnan Power Grid Company Ltd., Kunming, China

With an increasing application of Phase Measurement Units in the smart grid, it is becoming inevitable for PMUs to operate in severe conditions, which results in outliers and missing data. However, conventional techniques take excessive time to clean outliers and fill missing data due to lacking support from a big data platform. In this paper, a flexible ensemble algorithm is proposed to implement a precise and scalable data clean by the existing big data platform “Apache Spark.” In the proposed scheme, an ensemble model based on a soft voting approach utilizes principal component analysis in conjunction with the K-means, Gaussian mixture model, and isolation forest technique to detect outliers. The proposed scheme uses a gradient boosting decision tree for each extracted feature of PMUs for the data filling process after detecting outliers. The test results demonstrate that the proposed model achieves high accuracy and recall by comparing simulated and real-world Phase measurement unit data using the local outlier factor algorithm and Density-Based Spatial Clustering of Application with Noise (DBSCAN). The mean absolute error, root mean square error and  $R^2$ -score criteria are used to validate the proposed method’s data filling results against contemporary techniques such as decision tree and linear regression algorithms.

**Keywords:** data cleaning, outlier detection (OD), data recovery, phase measurement unit(PMU), apache spark

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### \*Correspondence:

Risheng Qin  
qinrisheng2020@126.com

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## INTRODUCTION

Due to the increasing demand for accurate control and management in smart grids, many advanced online monitoring devices have been installed and provide abundant operating data resources using Phase Measurement Units (PMUs). The data preprocessing is an important step that transforms the raw operating data used in the load forecasting model, user clustering tool, equipment maintenance, and energy theft detection technique. The outcome of data preprocessing has a significant impact on the data modelling process. For instance, a prediction model fed by a raw dataset with noise and bad data will be inefficient and cause inaccuracy. PMU failures, such as communication errors and noises, cause irregular packet data and asymmetric magnitude spikes, which are particularly problematic for smart grid applications. As a result, PMUs’ data cleaning algorithm must maintain high speed and sensitivity to faulty data in order to deliver a highly reliable data mining model. However, designing a data cleaning algorithm that balances high speed and sensitivity is a technological challenge that needs to be addressed.

Data cleaning technologies are a heavily studied domain of data statistics and machine learning. The whole process of extensive data cleaning is illustrated as outlier detection and data filling. The outliers which do not follow the main of the data may be produced by inducing random errors and faulty measurements (Zhao et al., 2019). For outlier detection, with the recent advancement in machine learning techniques, both unsupervised and supervised methods have been investigated for

better accuracy, speed, and computation cost. In supervised models, such as one-class support vector machine (SVM) (Ma and Perkins, 2003), decision forest (Reif et al., 2008), convolutional neural network (Ren et al., 2020), and the long short-term memory network (LSTM) (Wu et al., 2020) can achieve excellent performance by learning massive labeled data. However, labeling massive data is very time-consuming and needs great manual effort, which limits its application at an industrial scale. In comparison, unsupervised outlier detection does not need labeling and can achieve good accuracy in most cases. Even though some of their results are poor in complicated scenarios, unsupervised methods, namely Kmeans, Gaussian Mixture Model (GMM), CURE (Lathiya and Rani, 2016), Density-Based Spatial Clustering of Application with Noise (DBSCAN) (Manh and Kim, 2011), local outlier factor (LOF) (Pokrajac et al., 2007) and isolation forest (iForest) (Liu et al., 2008) are extensively used in real-world scenarios because they are easy to implement. Subsequently, there have been several attempts to use an unsupervised model to clean PMU data in the smart grid. For example, in (Mahapatra et al., 2016), principal component analysis (PCA) is used to detect outliers in PMU measurements. Likewise, PCA is incorporated with an artificial neural network (ANN) to improve detection accuracy (Mahapatra et al., 2017).

Meanwhile, researchers have been drawn to the drawbacks of stand-alone approaches, which produce inconsistent results in complex situations. As a result, various ensemble-based models have been designed to address deficiencies in real-world applications and improve their performance. For example, to improve accuracy, the local outlier factor (LOF) algorithm, correlation outlier probabilities, and single-linkage-based outlier detection methods are used (Kummerow et al., 2018). The DBSCAN, Chebyshev, and linear regression models are combined to predict PMU outliers (Zhou et al., 2019), but the approach cannot distinguish abnormal and regular operations. The Kmeans and local outlier probability methods are used to identify various types of anomalies based on the iForest anomaly score, such as fault detection, transient disturbance, etc. (Khaledian et al., 2020). In complex scenarios, these ensemble methods can present improved performance. However, the performance of extremely big data sets that may be computationally analyzed to discover patterns is rarely mentioned.

With the development and deployment of PMUs, the size of received data risen exponentially for a data center. (Khan et al., 2014; Yang et al., 2015). When dealing with vast amounts of data, conventional data processing methods can take days or weeks, which is insufficient time for data analysis. As a result, to ensure successful data processing, some attempts focus on big data technology. An adaptive hoeffding tree with a transfer learning approach is proposed (Mrabet et al., 2019) to detect the PMU data's events. In another attempt, a feature generation system is well-designed via Apache Spark core, which successfully fits 400 PMUs from the North American power grid (Kumar et al., 2021). A streaming interface based on Apache Spark for the synchrophasor data stream is investigated (Menon et al., 2018). Despite this, the integration and expansion of detection algorithms on existing big data platforms have limitations.

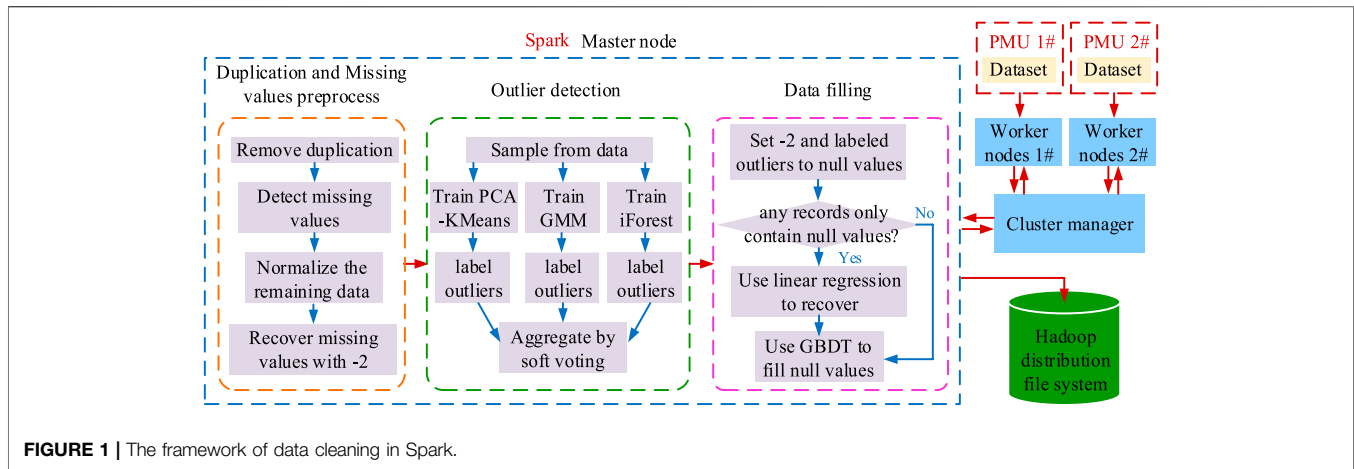
Furthermore, data filling is often addressed in publications as an important step in avoiding missing values. Statistic techniques and machine learning methods can complete the data filling processing. For statistic techniques, an improved cubic spline interpolation method is used to recover the missing data in the transient state and static state of power systems (Yang et al., 2019). A feature component extraction-based approach is proposed to recover a single channel data of PMU, which accounts for more details of the data waveform (Gao et al., 2016), but the relationship between PMUs is ignored. By contrast, an extreme learning machine and a random vector functional link model are introduced to produce good filling results (Li et al., 2019). Besides, artificial neural network technologies are also developed to achieve a good performance against complex scenarios. For example, a least-squares generative adversarial network is adopted to generate adequate monitoring data (Wang et al., 2021). Except for developing a new method, the researchers utilize the potential information in power systems' features to improve the accuracy, such as network topologies and operation mode. In (Ren and Xu, 2019), the network topologies are considered in a recovery program based on a generative adversarial network (GAN). Although the importance of topology in data recovery processing is investigated, publications seldom cover the whole data cleaning process, including outlier detection and data recovery.

Traditional bad data detection algorithms may underperform when dealing with complex scenarios and take a long time to run without big data technologies. Our motivation is to investigate how to apply the complete data cleaning process of PMUs, including outlier detection and data filling, to existing big data platforms to achieve expected performance. A flexible ensemble approach for data cleaning is given in this study to adapt to the failure of a single technique. In outliers detection, we adopt an ensemble method that includes three sub-detectors, the Kmeans combined with PCA, GMM, and iForest. A flexible voting mechanism then aggregates their results, and the aggregation is used to label outliers. After the outliers detection, the Gradient Boost Decision Tree (GBDT) is used and well designed to recover missing data and observed outliers. Apache Spark platform, Spark streaming system, Kafka and Hadoop distributed file system is selected to perform and test the proposed algorithm with massive datasets. In more detail, the contributions of this paper are listed as follows. First, a flexible data cleaning algorithm uses Apache Spark to automate the identification of outliers and retrieve missing data. Second, we propose a flexible voting mechanism for outlier detection to aggregate the outputs of PCA-Kmeans, GMM, and iForest in complex cleaning scenarios.

## PROBLEM DESCRIPTIONS

### The Framework of Proposed Data Cleaning via Spark

Figure 1 depicts a hierarchical data-cleaning framework proposed in this paper. The presented data cleaning algorithm is deployed in the Spark and Hadoop distributed file systems.



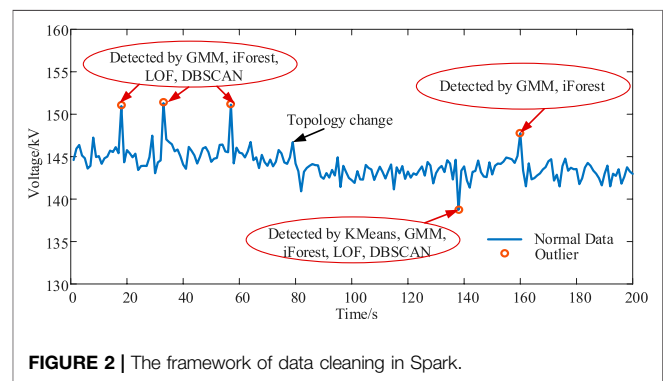
Master nodes and worker nodes are included in the system (2 nodes, as shown in **Figure 1**). When the proposed algorithm interacts with the master node, the master node asks the cluster manager for computing resources. The cluster manager responds by allocating jobs to worker nodes, and the worker nodes perform tasks based on PMU data.

The proposed data cleaning process is divided into three stages, as shown in **Figure 1**. The first step is to prepare the data. In this stage, the PMU data is uploaded to the worker nodes, preparing them for the next cleaning process. The cleaning procedure is preceded by a preprocess duplication and missing values. We remove duplication data and then find missing values. In this condition, the remaining data with noises are normalized. After that, the missing values labelled with “-2” and the normalized data are combined to form the dataset. Choosing -2 is to distinguish missing values from the normalized data (Liu et al., 2020). In the second stage, we randomly sample from the dataset to train PCA-KMeans, GMM, and iForest algorithms to predict outliers using a soft voting mechanism. Note that outliers include noise data. In the third stage, the outliers and missing values with “-2” are replaced with null values due to their abnormal features. If any record only contains null values, linear regression is used to recover this record.

## Outlier Detection

In general, outlier detection algorithms should be unresponsive to normal data, resilient and robust to outliers, and capable of computation. However, only a few algorithms can meet the requirement in most cases, and the algorithm’s output can jeopardize the data analysis credibility. To be more specific, 1) the algorithm may be insensitive to one or more types of outliers, such as bad data or missing values. 2) the model with adjustable parameters generates a high computational cost when cleaning a large dataset and can result in overfitting. 3) The algorithm may be vulnerable to standard power system manual operations, such as network topology changes.

To demonstrate more clearly, we take a section of PMU data shown in **Figure 2**, where five points are identified as outliers and highlighted in the figure. The state-of-the-art detecting algorithms, Kmeans, GMM, iForest, DBSCAN, and LOF, are



compared, with their parameters tuned. Most of the algorithms miss two outliers due to the topology change. However, only a small number of algorithms are capable of detecting all outliers.

To overcome these challenges, combining different findings from different detectors is necessary. The combining model can take advantage of every detector by aggregation and coherently achieve better performance. Its aggregation mechanism is the key to utilize the benefits fully. This paper investigates a flexible voting aggregation mechanism for the ensemble method to identify outliers.

Furthermore, in an ensemble algorithm, sub-detector selection is a critical step. In theory, any outlier detectors can be used for the ensemble, but since the compute resource is limited, the sub-detector number is limited. In the sub-detector selection, the detectors based on different methodologies are welcomed. In this paper, the density-based method, iForest, is chosen because of its high scalability and low memory use. The clustering-based methods, Kmeans and GMM, are used since the Kmeans ease of implementation in distributed computing. The GMM is selected because of its fuzzy clustering, which provides the probability of data points belonging to each cluster and is more flexible than Kmeans. While starting the cleaning process, three detectors are trained by the sampling data and then process the entire data separately and simultaneously using Spark’s pipeline mechanism which can improve computing efficiency.

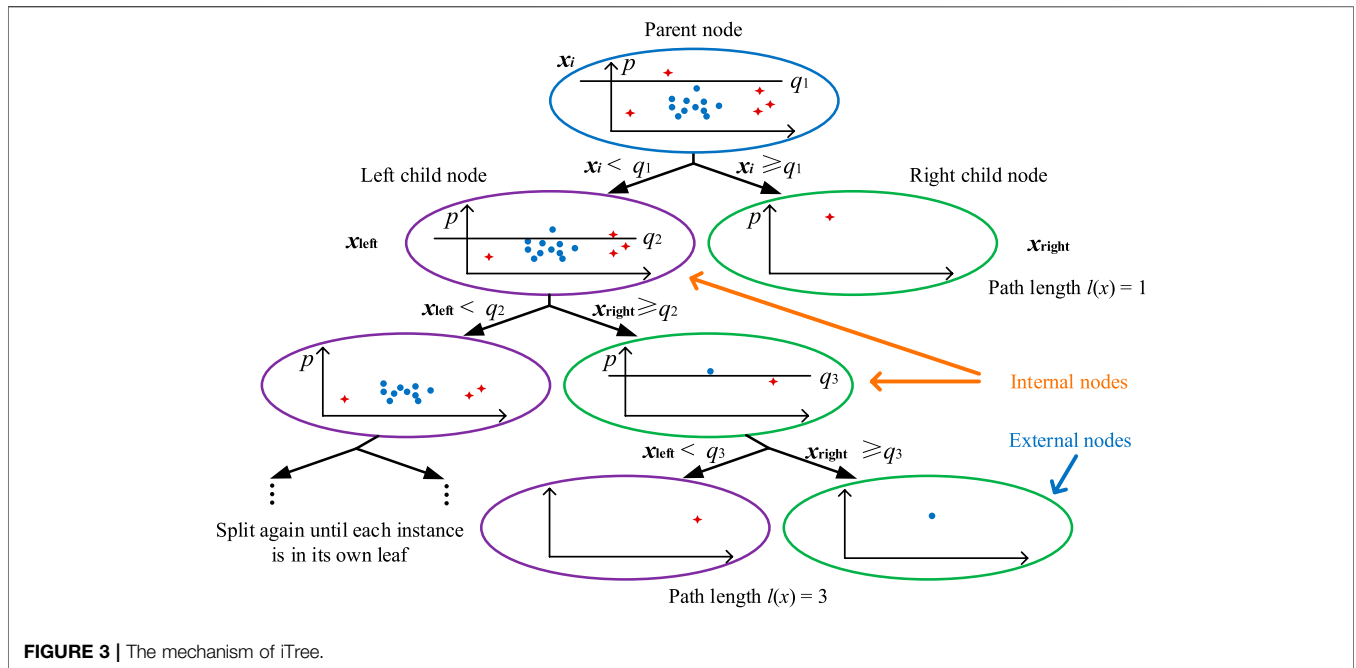


FIGURE 3 | The mechanism of iTree.

### Data Filling

Standard manual operations, such as network topology changes and line maintenance, often occur and cause PMU data to drift. Some filling algorithms, on the other hand, ignore the information and predict a significant error. As a result, such information should be considered when training a filling algorithm.

Furthermore, the filling algorithm's accuracy should be given more consideration. As a famous filling algorithm, GBDT can reach a high accuracy than other filling algorithms. The GBDT is a classic ensemble learning method that creates a strong regression tree by combining weak regression trees (typically train classification and regression tree (CART)). Thereupon, GBDT handles nonlinear relationships well and achieves high accuracy in fragmented datasets. Therefore, we adopt the GBDT method against missing data packets.

## ENSEMBLE MODELING FOR OUTLIER DETECTION

### Data Preparation

In this subsection, an ensemble method based on sub-detector PCA-Kmeans, GMM, and the iForest algorithm is proposed in order to obtain a more accurate detection of an outlier. To clearly illustrate the process, let  $D = d_k, d_{k+1}, d_{k+2}, \dots, d_{k+w}$  be the  $k$ th data window with size  $w$ , while  $D$  is a set of data rows. In which each data row  $d_i$  contains seven components: voltage magnitude, current magnitude, current angle, active power, apparent power, reactive power, and power factor angle.

### PCA-Kmeans Detector

The Kmeans is a classical classifying method that marks the data into several clusters. By analyzing and classifying the clusters, the

clusters of outliers can be detected. However, given the potential vulnerability of the Kmeans on high dimensional data, the PCA approach is combined with Kmeans to reduce the dimension of the data, called the PCA-Kmeans detector. The PCA approach is one of the most popular dimensionality reduction techniques (Mahapatra et al., 2017), aiming to find an orthogonal subspace whose basis vectors correspond to the maximum-variance directions in the original space. By using the output of the PCA model, the Kmeans method can achieve better accuracy. For clarity, let take  $B = \{b_1, b_2, \dots, b_i, \dots, b_w\}$  as the output of PCA. Each  $b_i$  has  $n_{sub}$  features. In the Kmeans method, each  $b_i$  of  $B$  should be assigned to the cluster which has the least squared Euclidean distance (Khaledian et al., 2020). To begin with, the  $k$  number of the centroid is selected randomly as  $m_1^{(1)}, \dots, m_k^{(1)}$ . Whereas a centroid is a data point at the cluster center. Next, iterations are implemented to find the nearest centroid for each  $b_i$ , as given by Eq. 1.

$$C_i^{(t)} = \{b_i : \|b_i - m_i^{(t)}\|^2 \leq \|b_i - m_j^{(t)}\|^2 \forall j, 1 \leq j \leq n\} \quad (1)$$

where  $C_i^{(t)}$  is the serial number of the nearest cluster for  $b_i$  in  $t$  iteration,  $1 \leq C_i^{(t)} \leq n$ .  $m_i^{(t)}$  is the mass point of  $C_i^{(t)}$ .  $n$  is the number of clusters.

After labeling each feature set in every iteration, the centroid in each step will be updated by Eq. 2.

$$m_i^{(t+1)} = \frac{1}{|C_i^{(t)}|} \sum_{b_i \in C_i^{(t)}} b_i \quad (2)$$

Meanwhile, when the centroid difference in an adjacent iteration is less than  $\xi$ , the iteration comes to a halt and gives final labels to each feature set in vector  $B$  based on Eq. 3.

$$m_i^{(t+1)} - m_i^{(t)} \leq \xi \quad (3)$$

where  $E_i$  is the mean of data points in  $C_i$ ,  $\xi$  is a very small positive number. Here, we take the result of the PCA-Kmeans that is a set of cluster labels  $S_{kmeans}$ .

### Gaussian Mixture Model-Based Detector

The GMM is a useful algorithm for detecting outliers based on a density function (De la Torre et al., 2012). Unlike Kmeans, the data is assumed to be modelled by several Gaussian density functions in this method. Each Gaussian density in the  $k$ th is given by a Gaussian function Eq. 4. The GMM model is the weighted sum of several Gaussian densities, illustrated by Eq. 5.

$$g_k(d|\mu_k, \sigma_k) = \frac{1}{\sqrt{2\pi\sigma_k^2}} e^{-\frac{(d-\mu_k)^2}{2\sigma_k^2}} \quad (4)$$

$$g(D; \mu, \pi, \sigma) = \sum_{k=1}^M \pi_k g_k(D; \mu_k, \sigma_k) \quad (5)$$

where  $\pi = \{\pi_1, \dots, \pi_M\}$ ,  $\mu = \{\mu_1, \dots, \mu_M\}$ ,  $\sigma = \{\sigma_1, \dots, \sigma_M\}$ , and  $\pi_k$  is the specific weights of each Gaussian model within a mixture.  $M$  is the number of Gaussian function.  $\mu_k, \sigma_k$  are the means and the covariance matrix of each model, respectively.

To determine the parameters such as  $\pi, \mu, \sigma$  of the Gaussian functions, the maximum likelihood function given by Eq. 6 is used for help by using the Expectation-Maximization (EM Algorithm) (De la Torre et al., 2012). The log-likelihood is used as Eq. 7 to determine if a data point belongs to the Gaussian functions measured earlier. The GMM's output is then assigned the weight of each data point to simple Gaussian density.

$$L(\mu, \pi, \sigma) = \prod_{i=1}^w \sum_{k=1}^M \pi_k g_k(d_i; \mu_k, \sigma_k) \quad (6)$$

$$\log L(\mu, \pi, \sigma) = \sum_{k=1}^M \sum_{i=1}^w z_{ki} \{ \log(\pi_k) + \log(g_k(d_i; \mu_k, \sigma_k)) \} \quad (7)$$

$Z_{ki}$  contains 0 or 1 depending on whether the data  $d_i$  belongs to Gaussian function  $k$ .

The mean log-likelihood criterion is then used to determine if the incoming data in the next window matches with the current GMM or not (Diaz-Rozo et al., 2018); it is calculated using Eq. 8.

$$\overline{\log L}(\mu, \pi, \sigma) = \frac{1}{w} \sum_{i=1}^w \log \left( \sum_{k=1}^M \pi_k g_k(d; \mu_k, \sigma_k) \right) \quad (8)$$

### Isolation Forest Detector

In general, anomalies are less common than normal findings and have different values. The Isolation Forest algorithm takes advantage of this feature to measure a dataset's anomaly ratings, which are then used to distinguish outlier points (Liu et al., 2008). In this subsection, isolation trees (iTree) and path lengths are introduced.

For clarification, let us take a random binary tree as an example; partitioning observations is repeated recursively until all the observations are isolated. As shown in Figure 3, the iTree that uses a binary tree structure is proposed to isolate observations.

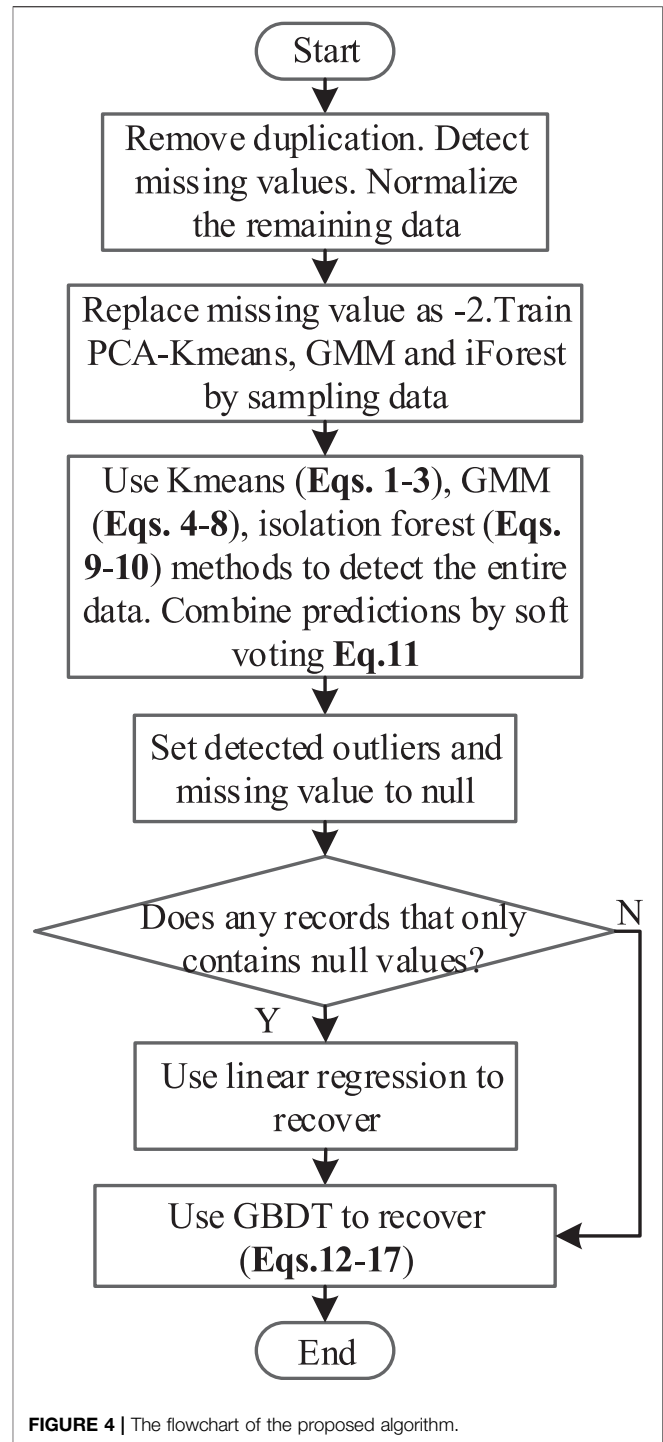


FIGURE 4 | The flowchart of the proposed algorithm.

Definition 1 (iTree): iTree is a random binary tree with no more than two children per node. As shown in Figure 3, internal nodes have exactly two children, while external nodes have none. Each internal node has a randomly chosen function  $q$  and a split value  $p$ , resulting in the node's split into two child nodes according to the condition  $q < p$ . This process is repeated until all of the nodes have just one case.



We denote a training dataset with  $N$  instances by  $X = \{x_1, \dots, x_N\}$ . The subsampled set  $\mathcal{X} \subset X$  is sampled from  $X$  with  $\varphi$  instances, which is utilized for training an iTree. The process of building an iTree is to divide up the subsampled set  $\mathcal{X}$  recursively into subspaces. Note that we adopt only subsampled sets of small fixed sizes to build iTrees, regardless of the dataset's size. This way, we can obtain each iTree very swiftly.

Anomalies are isolated closer to the root node of an iTree and have short path lengths, as seen in Figure 3. On the other hand, standard points are isolated at the deep end of an iTree and therefore have long path lengths. As a result, anomaly scores are a function of path lengths. The length of the route is determined as follows.

**Definition 2 (Path length):**  $l(x)$  is the number of edges between the root node and the external node corresponding to an instance  $x$  in the iTree.

For the same dataset  $X$ , we can build multiple iTrees that are constructed by randomly selected features, split values, and subsampled datasets. To aggregate the results of iTrees and calculate the anomaly score, we first introduce an average path length  $c(\varphi)$  for instances  $\varphi$  in an iTree calculated by Eq. 9. This average path length can represent the length situation of the instances  $\varphi$ , which is used to normalize the length of each component  $x$  in the instances. Next, the anomaly score of each component  $x$  in the instance  $\varphi$  can be obtained by calculating Eq. 10. The anomaly score ranges from 0 to 1, and the data instance will be normal if the score is lower than 0.5 (Liu et al., 2008). Further, the data instance which is closed to 1 can be detected as an outlier.

$$\begin{cases} c(\varphi) = 2H(\varphi - 1) - \frac{2(\varphi - 1)}{\varphi} \\ H(\varphi - 1) \approx \log(\varphi - 1) + e \end{cases} \quad (9)$$

$$\begin{cases} s(x, \varphi) = 0.5 - 2^{-\frac{E(l(x))}{c(\varphi)}} \\ E(l(x)) = \frac{1}{N_{Tree}} \sum_{n=1}^{N_{Tree}} l_n(x) \end{cases} \quad (10)$$

where  $e$  is the Euler constant;  $l(x)$  is the path length of each component  $x$  in the instance  $\varphi$ . The expected path length is represented as  $E(l(x))$ .  $N_{Tree}$  is the number of iTrees.

### Soft Voting Mechanism

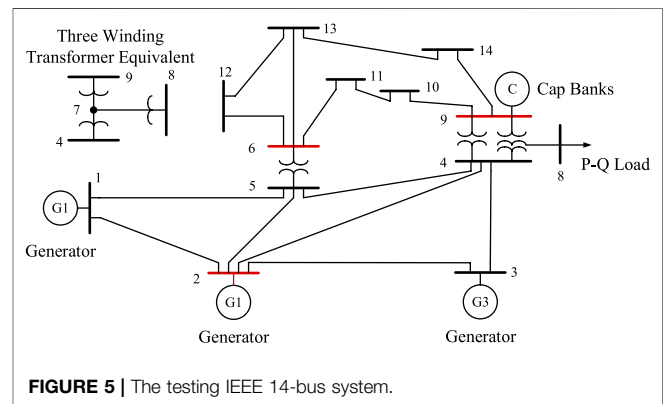
To fully utilize the advantages of sub-detectors, a soft voting mechanism is used to combine the sub-detectors predictions and increase robustness to complex scenarios. In particular, compared to the outlier probability given by GMM and iForest, the prediction of Kmeans is "hard" and has less elasticity against the scenario because it only gives a cluster label to each data point. The Kmeans prediction should be combined with another "soft" approach with a similar mechanism to deal with the poor results. For example, GMM, a soft clustering method, is used to multiple the Kmeans results marked as  $S_{Kmeans}P_{GMM}$ . Although  $S_{Kmeans} = 1$ , which means outlier detected in the Kmeans method, the outlier probability is still driven by GMM. Furthermore, to account for diversity in our voting mechanism's final prediction, the average outlier likelihood of all sub-detectors is used, as seen in Eq. 11.

**TABLE 1 |** The details of outlier detection datasets.

Dataset	Points	Feature	Outliers (%)
Satellite	6,435	36	2036 (32%)
Shuttle	49,097	9	3,511 (7%)
BreastW	683	9	239 (35%)
Http	567,479	3	2,211 (0.4%)

**TABLE 2 |** The results of the proposed method with outlier detection datasets.

Metrics	Datasets			
	Satellite	Shuttle	BreastW	Http
$T_P$	1,343	3,375	222	2,185
$F_P$	145	145	17	84
$T_N$	4,654	45,440	427	565,203
$F_N$	293	137	17	26
Precision	0.90	0.96	0.93	0.96
Recall	0.82	0.96	0.93	0.99



**FIGURE 5 |** The testing IEEE 14-bus system.

$$P = \frac{S_{Kmeans}P_{GMM} + P_{GMM} + P_{iForest}}{3} \quad (11)$$

SKmeans, PGMM, and PiForest are the output of the PCA-KMeans, GMM, and iForest algorithms.  $S_{Kmeans}$  is a binary variable, and  $S_{Kmeans} = 0$  addresses the normal data, while abnormal data is annotated as 1.  $P_{GMM}$  is the probability of outliers for an observation, which is closed to 1, meaning outlier.  $P_{iForest}$  is the anomaly score of the data point.

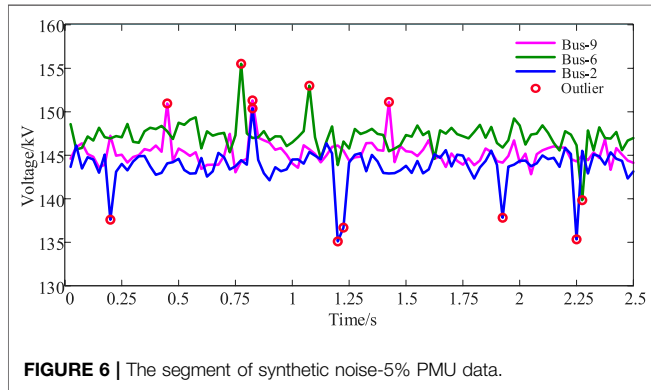
## DATA FILLING PROCESS AND DATA CLEANING FUNCTION

### Gradient Boosting Decision Tree-Based Filler

As discussed in Problem Descriptions, data filling is an important part of data cleaning, and it is a regression problem by definition. For PMU data, it is possible to have missing values for each feature, which presents as single or continuous types in a dataset. To tackle different types of missing values, the GBDT model is trained for each feature of PMU data, respectively. In case of single missing value occurs in a feature, the GBDT model can

**TABLE 3** | The noises injection of simulated scenarios.

Abnormal type	Anomalies calculation in each feature	Abnormal/Data points
Noise 5%	1.p.u *105% + G(x)	569/4,000
Noise 10%	1.p.u *105% + G(x)	1,091/4,000
Noise 15%	1.p.u *105% + G(x)	1,529/4,000



**TABLE 4** | The outlier detection results in simulated scenarios.

Algorithm	Metrics	Abnormal rate		
		5%	10%	15%
Proposed FEA	$T_P$	564	1,077	1,510
	$F_P$	16	14	21
	$T_N$	3,415	2,895	2,397
	$F_N$	5	14	19
	Precision	0.972	0.987	0.986
	Recall	0.991	0.987	0.987
DBSCAN	$T_P$	568	1,090	1,529
	$F_P$	6	15	0
	$T_N$	3,425	2,856	2,430
	$F_N$	1	38	41
	Precision	0.989	0.986	1
	Recall	0.998	0.966	0.974
LOF	$T_P$	550	1,047	1,484
	$F_P$	19	44	45
	$T_N$	3,412	2,891	2,455
	$F_N$	19	18	16
	Precision	0.97	0.960	0.970
	Recall	0.97	0.983	0.989

easily fill it using the other features as input. By contrast, when facing the continuous missing values loss of all features, the topology is the first to be recovered using the last instance. Then, the variables strongly associated with time—such as active power—are recovered by the linear regression method. Next, the other features are retrieved by the GBDT method.

The GBDT is used as a filler and to model an approximation function  $f(X)$  of a specified result  $Y = \{y_1, y_2, \dots, y_n\}$  with a set of the input variable as  $X = \{x_1, x_2, \dots, x_{n_{sp}}\}$ .  $n_{sp}$  is the length. During the approximation process, a loss function is usually adopted to search for the most precise approximation function. As illustrated in Eq. 12, the most precise model is obtained when the loss function is minimum. Here, we select the squared error function as the loss function shown in Eq. 13.

$$F(x) = \arg \min_{f(x)} L(y, f(x)) \quad (12)$$

$$L(y, f(x)) = [y - f(x)]^2 \quad (13)$$

The optimization can be effectively solved by a gradient descent algorithm, and the approximation function can be updated using the results of every iteration, illustrated via Eq. 14. In each iteration, the GBDT model uses the results in the last iteration and a classification and regression tree (CART), which is updated as Eq. 14. Especially in the initial iteration,  $f_0(x) = 0$ .

$$\begin{cases} f(x) = \sum_{m=1}^M f_m(x) \\ f_m(x) = f_{m-1}(x) + \gamma_m \sum_{j=1}^J c_{mj} I, \quad x \in R_{mj} \end{cases} \quad (14)$$

where  $M$  is the length of iterations.  $m$  is the serial number of iteration.  $\sum_{j=1}^J c_{mj} I$  is the result of the CART.  $J$  is the number of leaf nodes of the CART. The area disjointed by each leaf node is  $R_{m1}, R_{m2}, \dots, R_{mj}$ .  $c_{mj}$  is the prediction value of  $j$ th area.  $\gamma_m$  can be calculated by Eq. 15, and  $y_i$  is the actual value of variable  $y$ .

$$\gamma_m = \arg \min_{\gamma} \sum_{i=1}^I L \left( y_i, f_{m-1}(x_i) + \gamma \sum_{j=1}^J c_{mj} I \right) \quad (15)$$

By repeating the above interactive steps, the output of GBDT can be obtained by the final iteration.

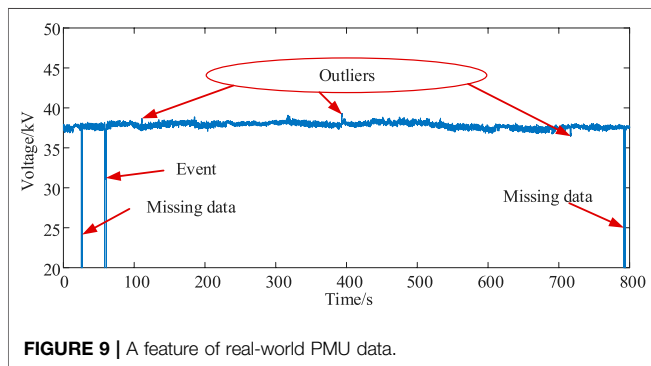
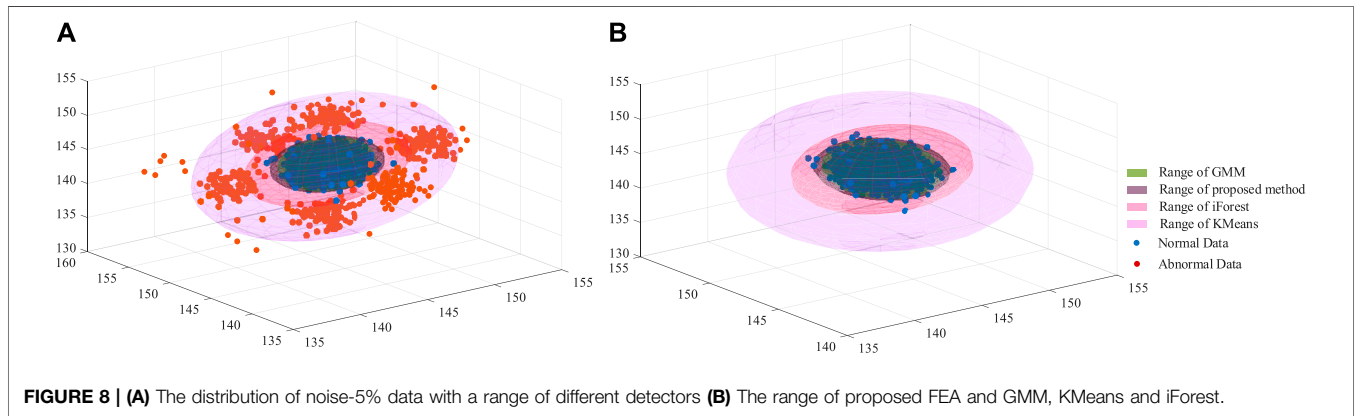
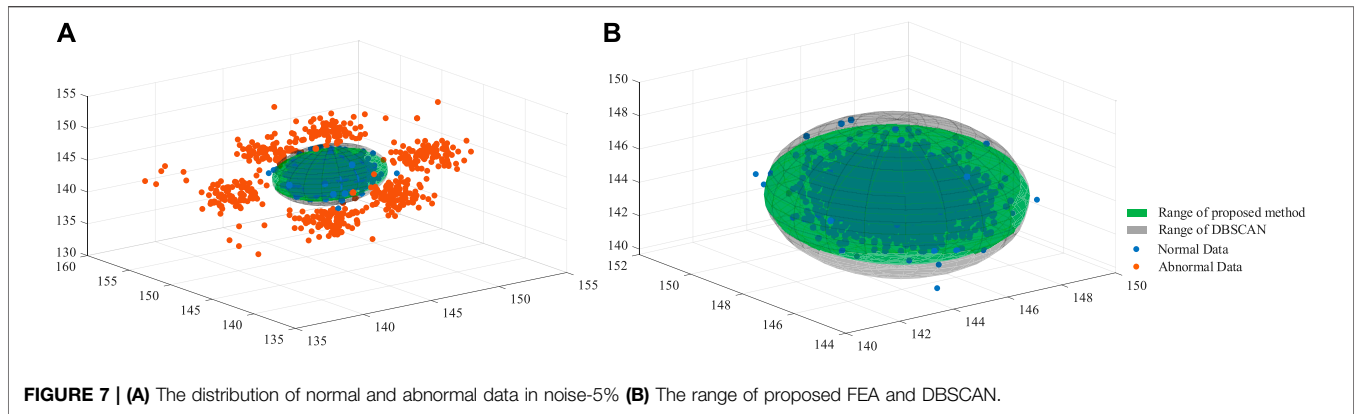
## The Proposed Processing of Data Cleaning

A flowchart of the proposed strategy is shown in Figure 4. Step 1: after eliminating duplication and detecting missing values, normalize the remaining data. Step 2: replace missing values with ‘-2’ and train PCA-KMeans, GMM, and iForest algorithms by sampling the normalized data. Step 3: detect the entire data by Eqs. 1–10 and combine PCA-KMeans, GMM, and iForest to eliminate outliers via a soft voting approach. Step 4: if any record only contains null values, using linear regression recovers the time-dependent features of records and then employing GBDT recovers the entire data. Step 5: otherwise, GBDT is used to recover the entire data.

## NUMERICAL SIMULATION

### Experimental Settings

In this simulation, the detailed experimental evaluation is presented with Spark 2.4.0, Kafka 0.10.1.0, Hadoop 2.4.7 under Ubuntu 16.04 operation system. Three scenarios are presented to demonstrate the feasibility of the proposed process. The outlier



**TABLE 5 |** The outlier detection results in real-world scenarios.

Algorithm	Metrics					
	$T_P$	$F_P$	$T_N$	$F_N$	Precision	Recall
FEA	1,077	10	33,811	46	0.991	0.959
DBSCAN	1,082	71	33,769	22	0.982	0.964
LOF	1,102	51	33,740	51	0.956	0.956

identification function of the proposed approach is firstly evaluated by an industrial dataset from the reference (Liu et al., 2008), considering precision and recall metrics. Secondly, the outlier detection function is examined using

**TABLE 6 |** The data recovery results in real-world scenarios.

Algorithm	Metrics		
	MAE	RMSE	$R^2$ -score
FEA-GBDT	0.354	0.463	0.910
Decision tree	0.366	0.483	0.904
Linear regression	0.378	0.476	0.900

simulated PMU data and real PMU data. Finally, the mean absolute error and the root mean squared error are employed to evaluate the precision of the proposed approach in recovering data compared with the linear regression algorithm and the decision tree approach.

### Outlier Detection of the Public Industrial Dataset

The proposed algorithm (FEA) is recommended in this scenario for detecting real-world datasets from outlier detection datasets and generating a score. Considering Satellite, Shuttle, Breastw, and Http datasets (Liu et al., 2008) illustrated in **Table 1**, a confusion matrix, which includes false positive ( $F_P$ ), false negative ( $F_N$ ), true positive ( $T_P$ ), and true negative ( $T_N$ ), is used to validate the performance of the proposed algorithm. Following that, we can use **Eqs. 18, 19** to measure the recall and precision ratios for further discussion.



$$\text{recall} = \frac{T_p}{T_p + T_N} \quad (18)$$

$$\text{precision} = \frac{T_p}{T_p + F_p} \quad (19)$$

The number of outliers detected as outliers is  $T_p$ , and the number of normal data detected as normal data is  $T_N$ . At the same time,  $F_p$  stands for the number of normal data points that have been identified as outliers. The number of outliers detected as normal data is given by  $F_N$ .

As shown in **Table 2**, the proposed FEA can achieve good performance while cleaning all types of data with large and highly polluted information, although this recall is about 82% for Satellite.

## Outlier Detection of Synthetic PMU Dataset

Using PMU operational data, the proposed method and other methods are compared in this subsection. In PSCAD/EMTDC, simulation data is produced using a model IEEE 14-bus network system with PMUs installed on bus-2,6,9, as shown in **Figure 5**. The length of operation data of PMU is 4,000 points with a sampling rate of 40 frames per second. The data is polluted by outliers and missing values using a Gaussian-distributed random function as  $z = G(x)$ . **Table 3** shows that each PMU data has 5 percent -15 percent noise and 5 percent -15 percent missing values injected into it. As an example, if a data point has a voltage feature of 35kV, the noise is calculated as  $35 \times 105\% + G(x)$ . As illustrated in **Figure 6**, one segment of the synthetic data is added by a noise-5% PMU data.

Changing the ratios of white noises and null values, the proposed FEA can maintain an expected performance, as shown in **Table 4**. For instance, considering the dataset with 15% noise, DBSCAN and FEA have similar results. As illustrated in **Figure 7A**, the normal and abnormal data are used to predict the outliers. As shown in **Figure 7B**, DBSCAN has a little larger cover of normal data than FEA does, which means that DBSCAN can achieve slightly better precision than FEA.

Following that, **Figure 8A** illustrates the range of sub-detectors used in our ensemble method. The details indicate that the KMeans range is the largest but includes some abnormal data, indicating that this method detects more outliers than normal data (FN), as shown in **Figure 8B** iForest has a smaller range than KMeans but perfectly covers all normal data. GMM has a narrow range and may predict more normal data as outliers (FP). By combining the advantages of each sub-detector, the FEA can achieve a normal range size while maintaining a high level of outlier detection performance.

## Outlier Detection of Real-World PMU Dataset

For performance estimation, real-world PMU data from a specific region in southwest China is used, and domain experts label outliers and missing values in the dataset. FEA can detect outliers and missing values, as shown in **Figure 9**. As presented in **Table 5**, the FEA can efficiently clean data with a precision of 99.1 percent and a recall of 95.9 percent. The good performances in real-world PMU data again verify the proposed FEA's effectiveness.

## Data Recovery of Real-World PMU Dataset

The linear regression, decision tree, and GBDT algorithms are introduced in this sub-section to complete the regression training process and fill null values with real-world PMU data. The root squared measurement error (RSME), mean absolute error (MAE), and  $R^2$ -score are respectively calculated to evaluate the performance of the proposed approach in **Eqs. 20–22**.

$$\text{MAE} = \frac{1}{N} \sum_{i=1}^N |y_i - h(x_i)| \quad (20)$$

$$\text{RSME} = \sqrt{\frac{1}{N} \sum_{i=1}^N (y_i - h(x_i))^2} \quad (21)$$

$$R^2 = 1 - \frac{\sum_{i=1}^N (y_i - h(x_i))^2}{\sum_{i=1}^N (y_i - \bar{y}_i)^2} \quad (22)$$

where  $N$  is the size of data,  $y_i$  is data point,  $H(x_i)$  is the prediction with the input  $x_i$ , and  $\bar{y}_i$  is the average of data.

As illustrated in **Table 6**, the performance of the proposed FEA-GBDT is superior to that of the other algorithms because of lower MAE and RMSE and larger  $R^2$ -score.

## CONCLUSION

This paper proposes a modular ensemble-based cleaning approach for PMUs to achieve outlier detection and data filling using big data technologies. The proposed approach considers and aggregates the advantages of different methods such as KMeans, GMM, and iForest for outlier identification, allowing it to perform better. Missing values due to system error are also investigated and retrieved using the proposed process. Notably, computational results show that the proposed approach can effectively process outliers, is resilient to a high percentage of bad data, and performs well with a large dataset. The proposed method achieves accurate prediction as compared to DBSCAN and LOF algorithms. The proposed approach, in particular, can handle large datasets deployed on Hadoop and Spark systems. When data filling is taken into account, our model produces a lower mean absolute error and root squared measurement error and  $R^2$ -score. Furthermore, our algorithm results show that using big data technology, a single detector's poor performance and low efficiency can be replaced by a high-efficiency ensemble approach. PMUs' outlier detection and data filling functions have the potential to clean and use data in real-time for fault detection, data processing, and prediction.

Some factors, such as communication infrastructure and system maintenance, may have an impact on the proposed algorithm's efficiency. As a result, our future work will focus on taking into account the aforementioned considerations and refining the proposed approach in these scenarios.

## DATA AVAILABILITY STATEMENT

The raw data supporting the conclusions of this article will be made available by the authors, without undue reservation.

## AUTHOR CONTRIBUTIONS

Conception and design of study: LS Acquisition of data: ML, XH Drafting the article: RQ, XH Analysis and interpretation of data: LS, RQ, ML, CG Revising the article critically for important intellectual content: RQ, XM, RD.

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