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Research on damage and degradation of coal-bearing sandstone under freeze-thaw cycles

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Comprehending the effect of freeze-thaw cycles on the damage and degradation of coal-bearing sandstones is crucial for the end-wall slope stability of open-pit mines in cold areas. In this study, freeze-thaw cycle tests on water-saturated coal-bearing sandstone samples under different freezing temperatures and different freeze-thaw cycles were conducted by a fully automatic low-temperature freeze-thaw testing system, and the effects of freeze-thaw cycle parameters on P-wave velocity and porosity of sandstone samples were obtained. With the assistance of CT scanning imaging technology, the microscopic damage and deterioration mechanism of sandstone samples under freeze-thaw cycles was further revealed, and a characterization method for the damage and deterioration of sandstone samples under freeze-thaw cycles was established, and damage and degradation effects of freeze-thaw cycles on the sandstone samples were predicted. The research results suggest that as the freezing temperature decreases and the number of freeze-thaw cycles increases, the P-wave velocity of the sandstone sample decreases, while the volume of the sandstone sample increases. The relative change rate of P-wave velocity and porosity increment of the sample are positively correlated with freezing temperature, and negatively correlated with the number of freeze-thaw cycles. The CT scan results show that with the decrease of the freezing temperature and the increase of the number of freeze-thaw cycles, the number and geometric size of pores on the sample cross section increase significantly. Additionally, the evolution equation of freeze-thaw damage factors was established with freezing temperature and number of freeze-thaw cycles as parameters, and the internal mechanism and physical characterization of freeze-thaw damage degradation of coal measure sandstone were revealed. This research provides a reference for the safety and stability evaluation and technology research and development of related rock engineering in cold areas.

KEYWORDS

freeze-thaw cycle, coal-bearing sandstone, pore structure, damage and deterioration, microscopic mechanism

1 Introduction

The large-scale open-pit coal mines in China are mainly distributed in high-latitude and seasonal frozen areas such as Inner Mongolia, Shanxi, Xinjiang, Liaoning, and Heilongjiang Provinces. The slope rock mass of the mining end-wall in the open-pit coal mines in high-latitude cold areas has long been subjected to temperature differences caused by seasonal changes and day-night changes (Lin et al., 2021; Yu et al., 2022); Coupled with the effect of ambient water, when the ambient temperature is lower than 0°C, the pore water in the rock mass undergoes a water-ice phase transition and then expands in volume. Under the combined action of ice segregation and water migration, the ice permeator in the pore structure expands, resulting in an enlargement of the initial rock body's pore structure and emergence of new pore structures. When the ambient temperature rises above 0°C, the ice melts into water and penetrates into the new pore structure system of the rock mass and the softening of the rock mass occurs, which may induce the freezing damage and deterioration of the rock mass in the next freeze-thaw cycle. Under such reciprocating freeze-thaw cycles, the structure and physico-mechanical properties of the rock mass are significantly damaged and deteriorated (Li et al., 2023a; Li et al., 2023b). As a result, the damage and deterioration induced by repeated freeze-thaw cycles have emerged as an important cause of slope instability at the end-wall of open-pit coal mines in cold regions (Ke et al., 2021; Yuan et al., 2023).

The effect of rock damage and degradation can partially account for the changing patterns of macroscopic mechanical parameters of the slope rock (Chen et al., 2022; Jia et al., 2024; Shi et al., 2023a). However, the existing research on rock damage and degradation under freeze-thaw cycles mainly focuses on determining damage degree and its evolution mechanisms of rock mass. At present, the common detection methods for rock damage mainly include mercury intrusion measurement, CT non-destructive testing (Song et al., 2019), nuclear magnetic resonance (NMR) testing (Baldwin and Yamanashi, 1989) and electron microscopy measurement. Through mercury injection tests on limestone samples under freeze-thaw cycles, Fogue Djombou et al. (Fogue-Djombou et al., 2019) comparatively analyzed the relationship between the microstructure and macroscopic mechanical damage of the rock samples. V.G.R.D. Argandona et al. (Ruiz De Argandona et al., 1999) performed a three-dimensional reconstruction of the internal pore structure of Spanish dolomite samples under the freeze-thaw effect by using CT scanning and image processing techniques and obtained the porosity evolution of dolomite samples under the freeze-thaw effect. By scanning electron microscope (SEM) and CT scanning, J. Park et al. (Park et al., 2015) illustrated the changes in the internal microstructure of rocks after freeze-thaw cycles, and compared the three-dimensional pore structure of rocks. It was found that cracks are initiated and expanded around the central hole, indicating that the increase in rock porosity can be attributed to internal particle separation, crack formation and crack expansion. Li and Jiang et al. (Jiang, 2018; Jielin et al., 2018) conducted non-destructive tests on rock structures under freeze-thaw cycles by NMR and discussed the intrinsic relationship between the macroscopic mechanical properties and microstructural degradation of rock samples. Mousavi et al. (Mousavi et al., 2020) observed rock samples after freeze-thaw

cycles by SEM. The results showed that the increase in rock porosity under freeze-thaw cycles is caused by the crack expansion and formation of new cracks and pores. In addition, techniques such as fluorescent agent calibration technique, acoustic emission (AE) detection testing, and laser scanning microscopy can also be used to analyze the microscopic porosity evolution of rock or rock-like material (Maji and Murton, 2020; Niu et al., 2021; Wang et al., 2024; Wu et al., 2020; Wu et al., 2024; Shi et al., 2023b).

The existing research mainly focuses on the rock media of geotechnical engineering within cold areas, such as red sandstone, mudstone, granite, limestone and dolomite (Ma et al., 2018; Berisavljević, 2019; Park et al., 2020; Yu et al., 2022). However, there is limited systematic research conducted on coal-bearing sandstone in open-pit mines. Different rocks exhibit distinct damage and degradation characteristics and mechanisms under freeze-thaw cycles. The coal-bearing sandstone in open-pit mines has low strength, weak cementation, development of primary/secondary cracks, high permeability coefficient, high porosity, and the presence of clay minerals (Yang et al., 2024). These characteristics aggravate the damage and deterioration effect of coal-bearing sandstone under freeze-thaw cycles, potentially leading to slope instability in open-pit mines during mining. The deterioration of the physical and mechanical properties of slope rocks in the freeze-thaw environment poses severe challenges to the stability and efficient operation of open-pit slope projects. In this study, the coal-bearing sandstone in open-pit mines in cold areas was taken as the research object, and the damage and deterioration of sandstone samples under the action of freeze-thaw cycles were investigated. Specifically, the effects of freeze-thaw cycles on the P-wave velocity and porosity of coal-bearing sandstone samples were obtained; the change rules of porosity and pore structure characteristics of coal-bearing sandstone samples before and after freeze-thaw cycles were analyzed by the microscopic imaging method of pore structure characteristics (CT scanning imaging technology); a characterization method for the damage and deterioration of coal-bearing sandstone samples under freeze-thaw cycles was established, and damage and degradation effects of freeze-thaw cycles on the sandstone samples were predicted. This research provides an important basis for the end-wall slope stability prediction, evaluation and design of open-pit mines in cold areas.

2 Freeze-thaw cycle tests on coal-bearing sandstone

2.1 Sample preparation

The sandstone samples used in the test were taken from the Antaibao Open-pit Coal Mine in Pingshuo City, Shanxi Province, China. This area is a typical high-latitude and seasonal frozen area, with an average annual minimum temperature of -14.9~-26.7°C. According to the *International Society of Rock Mechanics Test Procedures* (ISRM 2007), sandstone samples were prepared into a standard cylinder with a diameter of 50 mm and a height of 100 mm. To reduce the discreteness of the test results, samples with obvious primary defects, cracks, and local defects were eliminated. Additionally, the P-wave velocity of the sample was measured by the P-wave velocity measuring instrument, and sandstone samples

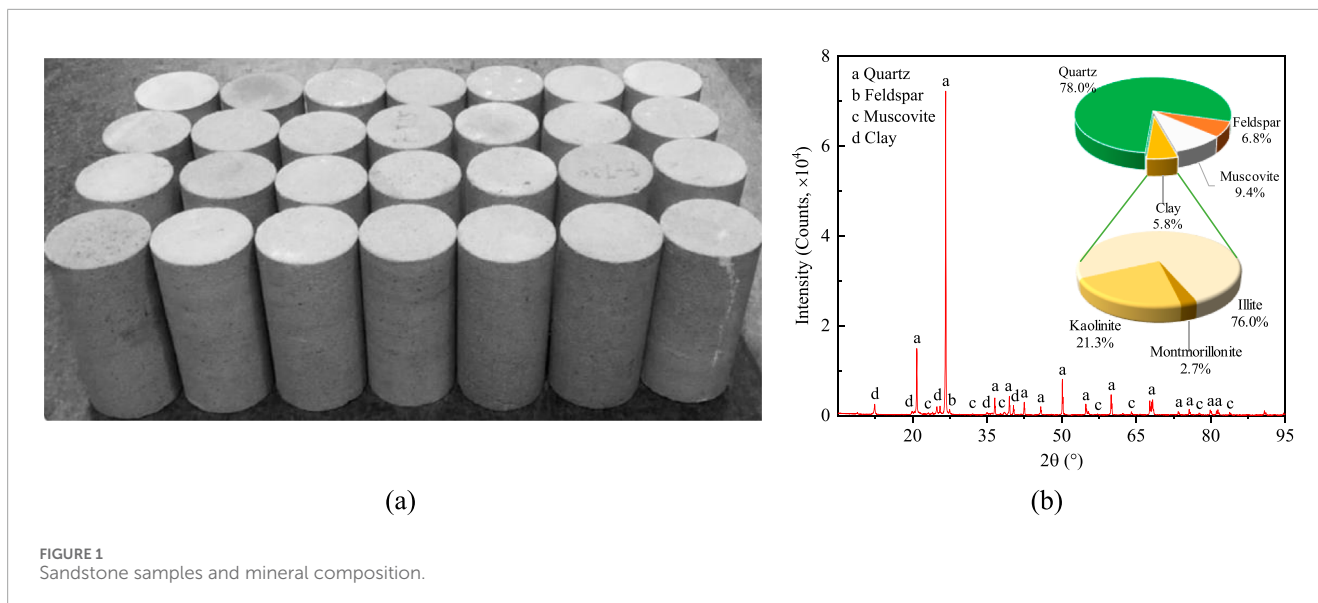


TABLE 1 Basic physical and mechanical parameters of coal-bearing sandstone.

Density (kg/m ³)	Moisture content (%)	Poisson's ratio	Elastic modulus, (GPa)	Peak strength (MPa)
2437.0	0.897	0.22	2.704	27.02

with similar P-wave velocity were used for the subsequent tests to reduce the test error. [Figure 1A](#) shows part of the sandstone samples after processing. Through X-ray diffraction testing (XRD), the material composition and content were as follows: quartz of 78.0%, feldspar of 6.8%, muscovite of 9.4%, and clay minerals of 5.8%. The clay minerals were composed of 76% illite, 21.3% kaolinite and 2.7% smectite, which was a typical medium-coarse sandstone, as shown in [Figure 1B](#).

The AutoPore IV 9520 fully automatic mercury intrusion meter was used to conduct mercury intrusion tests on rock samples^[14]. The results showed that the average porosity of the sandstone was 11.14%. In addition, uniaxial compression tests on sandstone samples were conducted, and the basic physical and mechanical parameters of sandstone were obtained, as shown in [Table 1](#).

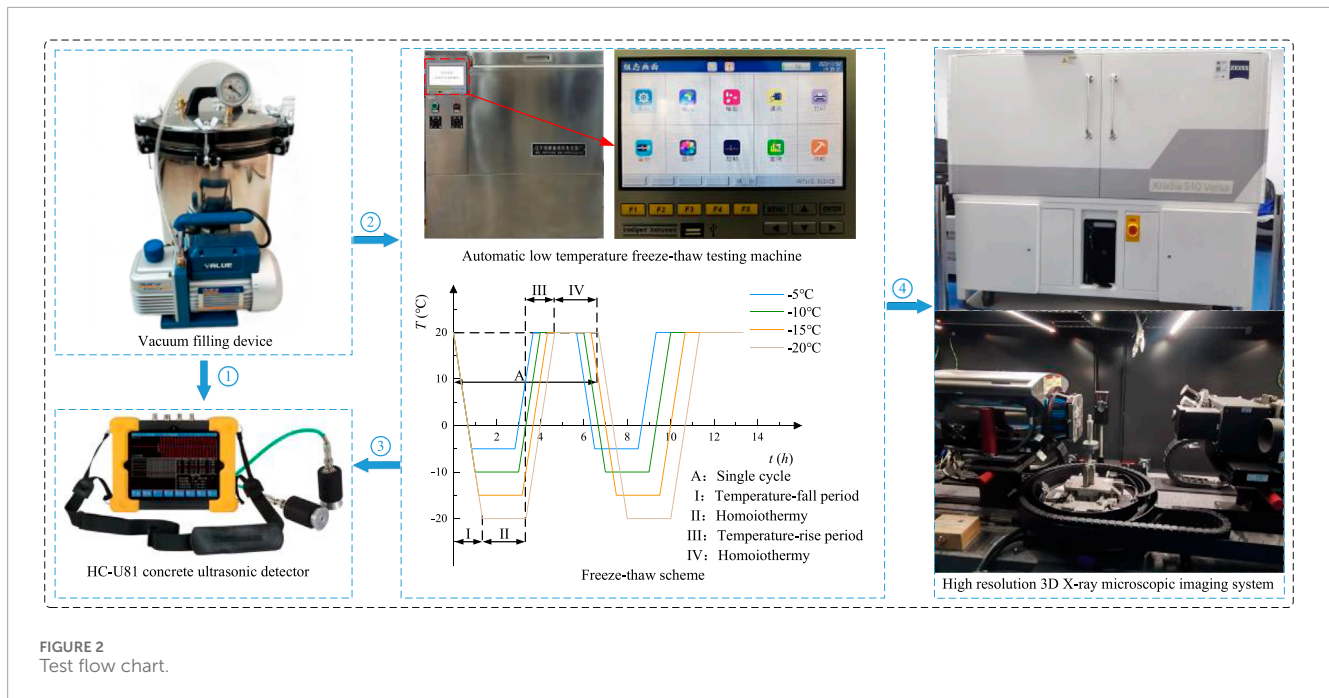
According to the composition structure characteristics and basic physical and mechanical properties of rock samples, the mechanical properties of the sample were weak, the pore structure was rich, and the rock mass was nearly weakly cemented ([Wu et al., 2024](#)). This type of rock mass is particularly sensitive to freeze-thaw cycles in high-latitude cold areas, especially under conditions with sufficient moisture content ([Li et al., 2021](#); [Chen et al., 2024](#)). At present, there are abundant research results on the effects of moisture content on rock deformation and damage mechanisms under the action of freeze-thaw cycles. Existing research has shown that as the moisture content increases, the freeze-thaw cycle is more likely to induce the strength weakening, deformation and failure of the rock mass; Besides, the freeze-thaw cycle has the greatest weakening effect on saturated rocks ([Yani et al., 2019](#); [Liu J. et al., 2024](#)). To obtain the weakening effect of freezing temperature and freeze-thaw cycles on

coal-bearing sandstone, all rock samples were subjected to saturated treatment.

2.2 Experimental scheme

In this study, the effects of the number of freeze-thaw cycles and freezing temperature on the damage and deterioration of sandstone were mainly examined. The freezing temperature range was set to $-5^{\circ}\text{C} \sim 20^{\circ}\text{C}$, $-10^{\circ}\text{C} \sim 20^{\circ}\text{C}$, $-15^{\circ}\text{C} \sim 20^{\circ}\text{C}$, $-20^{\circ}\text{C} \sim 20^{\circ}\text{C}$, the number of freeze-thaw cycles was set to 5, 10, 15, 20. A total of 16 groups of tests were carried out, and eight samples were used for each test. The heating rate and cooling rate were both $0.5^{\circ}\text{C}/\text{min}$. Once it reached freezing or thawing temperature (20°C), it was maintained for 2 h to avoid additional stress caused by excessive temperature gradient inside the sample. [Figure 2](#) shows the specific test process.

- (1) The sample is placed in a vacuum tank, and the air inside the vacuum tank is extracted to form a negative pressure environment. Open the valve and slowly inject distilled water into the vacuum tank until the water level is below the top of the sample. Continuous vacuum pumping for 24 h to ensure that water completely permeates the pores of sandstone samples.
- (2) After vacuum saturation, the P-wave velocity, volume and other physical parameters of sandstone samples before the freeze-thaw cycles were measured by ultrasonic detectors and drainage methods as the control group. Subsequently, rock samples were wrapped with plastic film, and the ends were sealed with wax to ensure a constant state of water saturation within the rock sample.



- (3) The saturated sample was put into the freeze-thaw cycles testing machine according to the designed freezing temperature range (such as $-5^{\circ}\text{C}\sim 20^{\circ}\text{C}$). Then the setup program was initiated until the desired number of freeze-thaw cycles was completed.
- (4) After the completion of freeze-thaw cycles, the P-wave velocity, volume and other physical parameters of the sample were measured.
- (5) By using CT scanning imaging technology, a rock core of $\phi 8\text{ mm} \times 12\text{ mm}$ on the same sample was drilled, and the core was fixed on the sample platform for CT scanning. The visualization software Avizo was used to analyze the changes in pore structure characteristics under freezing temperature (-10°C and -20°C) and number of freeze-thaw cycles (5, 10, and 20).

3 Analysis of test results

3.1 Variation characteristics of P-wave velocity of coal-bearing sandstone under freeze-thaw cycles

The P-wave velocity is an important parameter that reflects the internal structural characteristics of the material, and the internal defects of the sample directly affect the P-wave propagation velocity (Zhang et al., 2018; Shen et al., 2020). When the sample contains a higher number of pores, its wave impedance experiences an increase, leading to a decrease in P-wave velocity; conversely, an increase in P-wave velocity is observed when the sample has fewer pores. Since the P-wave velocity of the sample after freeze-thaw cycles is related to the P-wave velocity before freeze-thaw cycles, the relative change rate of the P-wave rate of the sample is introduced to reflect

the deterioration effect of the freeze-thaw cycle on the sample. The calculation function is shown in Equation 1.

$$\eta_p = \frac{v_1 - v_0}{v_0} \times 100\% \quad (1)$$

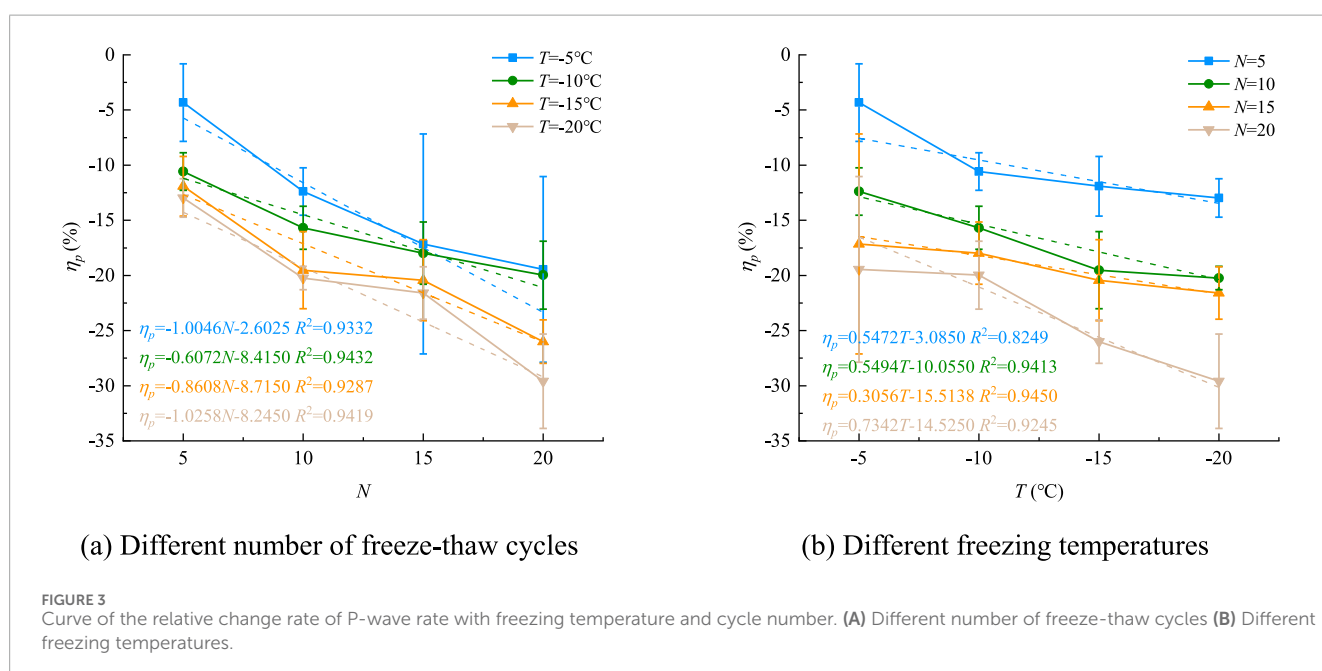
where η_p is the relative change rate of the P-wave velocity of the sample; v_1 is the P-wave velocity of the sample after freeze-thaw cycles; v_0 is the P-wave velocity of the sample before freeze-thaw cycles.

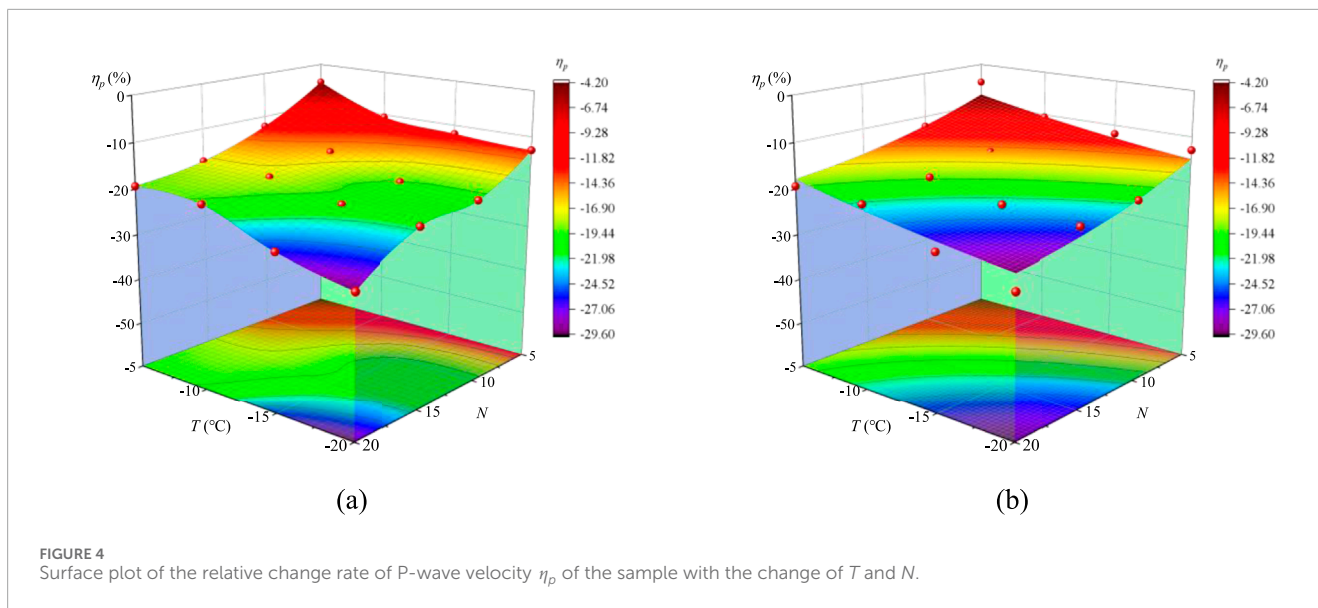
To reduce the impact of discreteness on the test results, the measured data of eight samples in each group were averaged. The test results are shown in Table 2. To analyze the influence of freezing temperature and the number of freeze-thaw cycles on the change of P-wave velocity of the sandstone sample, the relative change rate of P-wave velocity with freezing temperature and cycle number is plotted based on the data in Table 2, as shown in Figure 3.

As shown in Figure 3 and Table 2, ① the P-wave velocity v_p of the sample decreases as the decrease in freezing temperature T and the increase in the number of freeze-thaw cycles N . ② When the freezing temperature T is constant, as the number of freeze-thaw cycles N increases, the average relative change rate of the P-wave velocity before and after freeze-thaw cycles approximately decreases linearly, and its linear fitting correlation coefficient R^2 is greater than 0.92. ③ When the number of freeze-thaw cycles N is constant, as the freezing temperature T decreases, the average relative change rate of the P-wave velocity of the sample before and after freeze-thaw cycles decreases approximately linearly, and its linear fitting correlation coefficient R^2 ranges from 0.82 to 0.95. The above test results show that the freeze-thaw cycle has a significant damage and deterioration effect on the coal-bearing sandstone, and as the freezing temperature T decreases and the number of freeze-thaw cycles N increases, the deterioration damage effect is accumulated and intensified. ④ The slope of the fitted straight line a_N changes with the number

TABLE 2 Data of P-wave velocity of samples before and after freeze-thaw.

Sample group	Freezing temperature (°C)	Number of freeze-thaw cycles	v_p (km/s)	v_p' (km/s)	η_p (%)
			Mean value	Mean value	Mean value
1	-5	5	3.5156	3.3652	-4.28
2	-5	10	3.6282	3.1808	-12.33
3	-5	15	3.6701	3.0346	-17.32
4	-5	20	3.5459	2.8593	-19.36
5	-10	5	3.5218	3.1507	-10.54
6	-10	10	3.5341	2.9807	-15.66
7	-10	15	3.6006	2.9558	-17.91
8	-10	20	3.6516	2.9245	-19.91
9	-15	5	3.5209	3.1000	-11.95
10	-15	10	3.5863	2.8872	-19.49
11	-15	15	3.4851	2.7707	-20.50
12	-15	20	3.7600	2.7840	-25.96
13	-20	5	3.7077	3.2283	-12.93
14	-20	10	3.6988	2.9512	-20.21
15	-20	15	3.7365	2.9313	-21.55
16	-20	20	3.6011	2.5379	-29.58





of freeze-thaw cycles, ranging from -0.6072 to -1.0258 , and the slope of the fitted straight line a_T changes with the change of freezing temperature, ranging from 0.3056 to 0.7342 , and the absolute value of a_T is relatively small. This indicates that compared with freezing temperature, the number of freeze-thaw cycle is more likely to induce damage and deterioration of coal-bearing sandstone samples.

The above analysis and discussion were conducted on the damage and deterioration effects of freezing temperature and the number of freeze-thaw cycles on coal-bearing sandstone. In fact, these factors mutually influence the damage and degradation processes in coal-bearing sandstone. Figure 4 shows the change surface of the relative change rate of the P-wave velocity of the sample with the parameters of T and N . Figure 4A is the folded surface formed by the data in Table 2 and Figure 4B is the fitting surface of Figure 4A and its fitting function (surface equation):

$$\eta_p = 0.0109T^2 + 0.0261N^2 + 0.7271T - 1.4490N + 0.0063NT + 3.7819 \quad (2)$$

The fitting correlation coefficient R^2 of Equation 2 is 0.9368.

As shown in Figure 4 and Equation 2, ① η_p as the freezing temperature decreases and the number of freeze-thaw cycles increases, the damage and deterioration effect on the coal-bearing sandstone is increased. ② Examining the changing characteristics of the surface shape with the freezing temperature and the number of cycles, the coefficient values of T^2 , T and N^2 , N in Equation 2 are compared. It can be found that the number of freeze-thaw cycles has a higher deterioration effect on coal-bearing sandstone rather than freezing temperature. ③ The coefficient size of the NT term in Equation 2 reflects the coupling effect of the number of freeze-thaw cycles and freezing temperature. It should be noted that T is a negative value and the NT term is always negative. This indicates that the increase in the number of freeze-thaw cycles or the decrease in freezing

temperature can increase the deterioration effect on coal-bearing sandstone.

3.2 Variation characteristics of porosity in the coal-bearing sandstone under freeze-thaw cycles

In addition to the P-wave velocity of the sample, the volume change of the sample is also a significant factor contributing to its degradation and damage under the action of freeze-thaw cycles. The change in sample volume indicates the rock deformation and the change in the internal microstructure. If the volume of the sample increases after freeze-thaw cycles (without considering the deformation effect of the sample matrix), it indicates that the internal porosity of the sample increases (Chu et al., 2023; Feng et al., 2023). In this section, the damage and deterioration effects of freeze-thaw cycles on the coal-bearing sandstone are studied based on the changes in sample volume and porosity. The porosity increment is introduced to reflect the deterioration effect of volume changes before and after freeze-thaw cycles on the sample. Its calculation function is shown in Equation 3.

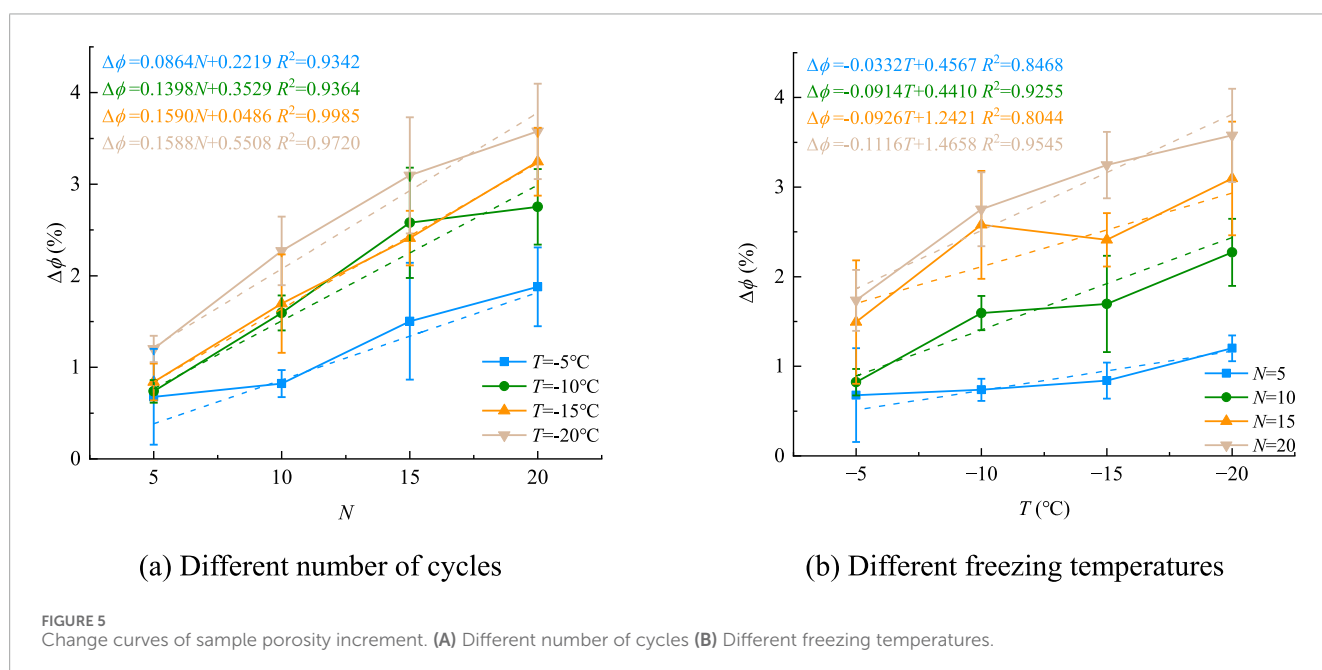
$$\Delta\Phi = \frac{V_1 - V_0}{V_0} \times 100\% \quad (3)$$

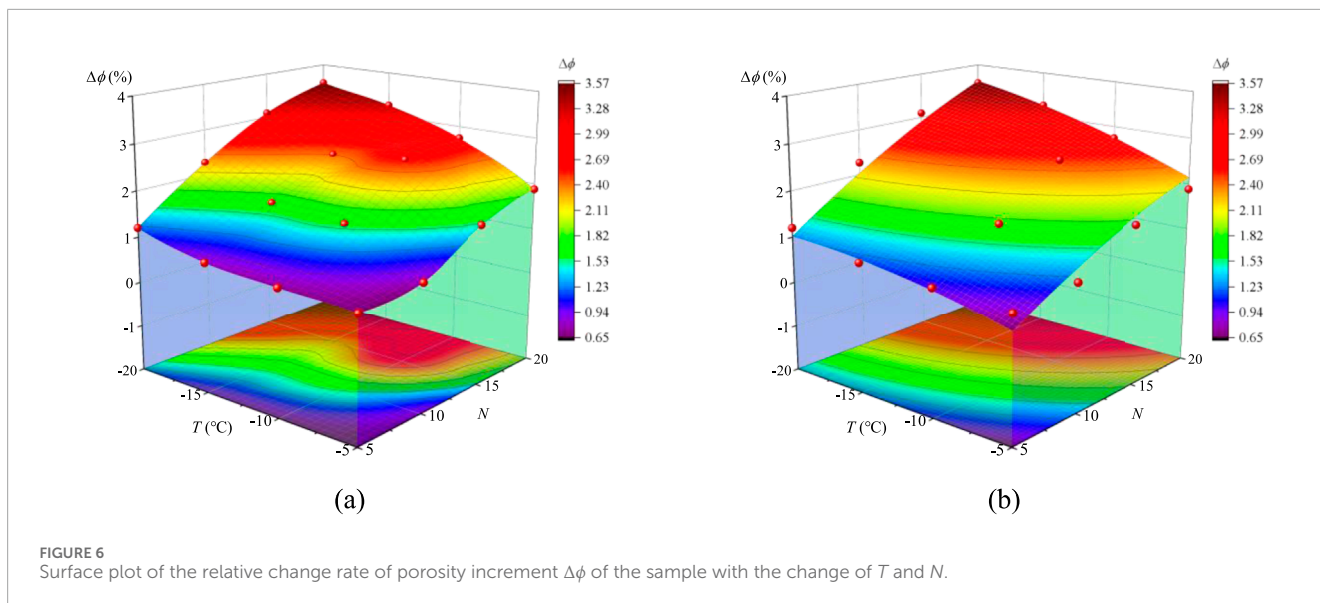
where $\Delta\Phi$ is the porosity increment of the sample; V_1 is the volume of the sample after freeze-thaw cycles; V_0 is the volume of the sample before freeze-thaw cycles.

To reduce the impact of discreteness on the test results, the measured data of eight samples in each group were averaged. The test results are shown in Table 3. To analyze the effects of freezing temperature and the number of freeze-thaw cycles on the changes in the P-wave velocity of sandstone, the change curves of porosity increment with freezing temperature and cycle numbers are drawn based on the data in Table 3, as shown in Figure 5.

TABLE 3 Sample volume and porosity increment before and after freeze-thaw cycles.

Sample group	Freezing temperature (°C)	Number of freeze-thaw cycles	V_0 ($\times 10^5 \text{mm}^3$)	V_1 ($\times 10^5 \text{mm}^3$)	$\Delta\Phi$ (%)
			Mean value	Mean value	Mean value
1	-5	5	1.9120	1.9250	0.68
2	-5	10	1.9310	1.9460	0.78
3	-5	15	1.9290	1.9580	1.50
4	-5	20	1.9270	1.9630	1.88
5	-10	5	1.9290	1.9430	0.74
6	-10	10	1.9280	1.9580	1.59
7	-10	15	1.9250	1.9740	2.58
8	-10	20	1.9350	1.9880	2.74
9	-15	5	1.9330	1.9500	0.84
10	-15	10	1.9320	1.9640	1.69
11	-15	15	1.9280	1.9750	2.41
12	-15	20	1.9330	1.9950	3.25
13	-20	5	1.9179	1.9409	1.20
14	-20	10	1.9210	1.9650	2.27
15	-20	15	1.9280	1.9880	3.10
16	-20	20	1.9270	1.9961	3.57





As shown in Figure 5 and Table 3, ① the volume V of the sample before and after freeze-thaw cycles increases as the freezing temperature T decreases or the number of freeze-thaw cycles N increases. ② When the freezing temperature T is constant, as the number of freeze-thaw cycles N increases, the average porosity increment of the sample exhibits an approximately linear increase, and its linear fitting correlation coefficient R^2 is greater than 0.93. ③ When the number of cycles N is fixed, as the freezing temperature T decreases, the average porosity increment of the sample rises approximately linearly, and its linear fitting correlation coefficients R^2 are greater than 0.8. ④ The slope a_N of the fitted straight line of changes with the number of freeze-thaw cycles, ranging from 0.0864 to 0.1590, and the slope a_T of the fitted straight line changes with the freezing temperature. The variation range of a_T is 0.0332–0.1116, and its absolute value is relatively small. This indicates that the number of freeze-thaw cycles N has a significant effect on the deterioration and damage of coal-bearing sandstone, while the freezing temperature T has a relatively small effect on the deterioration and damage of coal-bearing sandstone.

Figure 6 shows the surface plot of the sample porosity increment $\Delta\phi$ under the coupling effect of freezing temperature T and number of freeze-thaw cycles N . Figure 6A is the surface plot based on the $\Delta\phi$ data in Table 3 and Figure 6B shows the fitting surface plot of Figure 6A, and the fitting equation of $\Delta\phi$ can be expressed as follows:

$$\Delta\phi = 0.0026N^2 - 0.0022T^2 + 0.1407N - 0.0769T - 0.0047NT - 0.6500 \quad (4)$$

The fitting correlation coefficient R^2 of Equation 4 is 0.9617.

As shown in Figure 6 and Equation 4, ① The porosity increment $\Delta\phi$ increases with the decrease of freezing temperature and the increase of cycle numbers. This indicates that the damage and deterioration effect of freezing temperature and cycle numbers on coal-bearing sandstone is enhanced. ② The variation characteristics of the surface shape with freezing temperature and cycle numbers

are observed, and the coefficients of T^2 , T , N^2 and N in Equation 2 are compared. It can be found that the coefficient of variable N is larger than that of variable T , indicating that the number of freeze-thaw cycles has a stronger deterioration effect on coal-bearing sandstone than freezing temperature. ③ The coefficient of the NT term in Equation 2 reflects the coupling effect of the number of freeze-thaw cycles and freezing temperature on the porosity increment $\Delta\phi$ of the sample. It is noted that T is negative, and the NT term is always positive, indicating that the increase of the number of freeze-thaw cycles and the decrease of freezing temperature both enhance the damage and deterioration on coal-bearing sandstone.

3.3 Microscopic mechanism of sample pore structure change

Based on the P-wave velocity, volume and other physical parameters of the sample, the change law of the freeze-thaw damage and deterioration of the coal-bearing sandstone with the freezing temperature T and cycle number N is predicted in a macroscopic way. In this section, the pore structure evolution characteristics of coal-bearing sandstone under freeze-thaw cycles were discussed through high-resolution CT microscopy imaging technology to reveal the microscopic mechanism of freeze-thaw damage of coal-bearing sandstone. Table 4 shows the CT test results of sample porosity.

It can be seen from Table 4: ① When the number of freeze-thaw cycles N increases from 5 to 10, and 20 at the freezing temperature T of -10°C , the porosity ϕ of the sample increases by 1.52% and 3.22%, and the increasing amplitude is 12.4% and 23.4%; ② When the number of freeze-thaw cycles N increases from 5 to 10, and 20 at the freezing temperature T of -20°C , the porosity ϕ increases by 2.87% and 4.26%, with an increase of 22.2% and 26.9%; ③ When the number of freeze-thaw cycle N is fixed, the porosity ϕ increases with the decrease of the freezing temperature T . For example, when the number of freeze-thaw cycles N is 5 and the freezing temperature T is between -10°C and -20°C , the increasing amplitude of porosity is

TABLE 4 Porosity of samples.

Sample group	Freezing temperature (°C)	Porosity (%)		
		N = 5	N = 10	N = 20
CT-10	-10	12.24	13.76	16.98
CT-20	-20	12.92	15.79	20.05

5.6%; when the number of freeze-thaw cycles N is 20, the freezing temperature T is between -10°C ~ -20°C , the increasing amplitude of porosity 18.1%; ④ The sample porosity increment given in Table 3 is close to the CT test value, indicating that the data obtained from the freeze-thaw cycle test has high reliability.

Table 5 shows the cross-section and three-dimensional reconstruction of the pore structure of the sample by CT scanning. The black part in the picture represents the pores, and the other gray parts are the matrix structure. It can be seen from Table 5: ① When the freezing temperature is fixed, as the number of freeze-thaw cycles increases, the size and area of the pores in the sample section increase significantly, and the cracks on the surface of the three-dimensional reconstructed image increase significantly; ② When the number of freeze-thaw cycles is fixed, as the freezing temperature decreases, the size and area of the pores in the sample section also increase, and surface cracks in the three-dimensional reconstructed image also increase. It suggests that the freeze-thaw cycle leads to the progressive expansion and generation of internal cracks within the coal-bearing sandstone, resulting in the continuous deterioration of its deformation resistance and strength.

4 Discussion

4.1 Characterization methods of freeze-thaw damage

A large number of studies have shown that elastic modulus, mass density, porosity (ratio), resistivity, and other parameters can be used to describe or characterize material damage (Yani et al., 2019; Jiang et al., 2024; Liu M. et al., 2024; Liu J. et al., 2024). Elastic modulus is the most commonly used parameter, which is based on Lemaitre's Strain equivalence principle: the strain caused by the full stress acting on the damaged material is equivalent to the strain caused by the effective stress ε acting on the non-destructive material.

$$\varepsilon = \frac{\sigma}{E'} = \frac{\sigma'}{E} \quad (5)$$

As shown in Equation 5, E and E' are the elastic moduli of the undamaged material and the damaged material respectively. However, since rock materials all have initial damage, the elastic modulus E of undamaged rock cannot be obtained. Later, researchers proposed the generalized strain equivalence principle (Zhang et al., 2003):

$$\varepsilon = \frac{\sigma_1}{E_2} = \frac{\sigma_2}{E_1} \quad (6)$$

where E_1 and E_2 are the elastic moduli of the material in the two damage states; σ_1 and σ_2 are the stresses in the two damage states. In this study, the state of the sample before freeze-thaw cycles is regarded as the first state, and a certain state of the sample after freeze-thaw cycles is regarded as the second state. Assuming that the damage deterioration of the sample before freeze-thaw cycles and after freeze-thaw cycles can be expressed by the damage factor D_t ,

$$\sigma_2 = \frac{\sigma_1}{1 - D_t} \quad (7)$$

By substituting Equation 6 into Equation 7, we obtain:

$$D_t = 1 - \frac{E_2}{E_1} \quad (8)$$

Equation 8 indicates that the damage factor D_t can be obtained as long as the elastic moduli E_1 and E_2 of the sample before and after freeze-thaw cycles are determined through experiments.

It should be noted that E_1 and E_2 in Equation 8 represent the static elastic moduli of the sample before and after freeze-thaw cycles, respectively. However, it is challenging to obtain the deformation and failure process of rock samples during freeze-thaw cycle tests, as well as E_1 and E_2 . (Liu et al., 2015) suggested replacing the static elastic moduli E_1 and E_2 in Equation 8 with dynamic elastic moduli E_d and E_d' .

$$D_t = 1 - \frac{E_d'}{E_d} \quad (9)$$

In Equation 7, E_d and E_d' represent the dynamic elastic moduli of the sample before and after freeze-thaw cycles. The dynamic elastic moduli E_d and E_d' can be indirectly measured using non-destructive testing methods. Consequently, the damage and degradation characteristics of coal-bearing sandstone under freeze-thaw cycles can be obtained.

According to the theory of elastic dynamics, the dynamic elastic modulus E_d of a material has the following relationship with its P-wave velocity v_p , mass density ρ , and Poisson's ratio μ :

$$v_p = \sqrt{\frac{E_d(1 - \mu)}{\rho(1 + \mu)(1 - 2\mu)}} \quad (10)$$

From Equation 10, we can obtain:

$$E_d = \frac{\rho v_p^2 (1 + \mu)(1 - 2\mu)}{(1 - \mu)} \quad (11)$$

Equation 11 is substituted into Equation 9 to obtain the freeze-thaw damage factor, as shown in Equation 12:

$$D_t = 1 - \frac{\rho' v_p'^2 (1 + \mu')(1 - 2\mu')}{(1 - \mu')} \cdot \frac{(1 - \mu)}{\rho v_p^2 (1 + \mu)(1 - 2\mu)}$$

TABLE 5 Cross-section and three-dimensional reconstruction of the pore structure of the sample by CT scanning.

Number of freeze-thaw cycles	Cross-sectional view of pore structure		Three-dimensional reconstruction of the pore structure	
	$T = -10^{\circ}\text{C}$	$T = -20^{\circ}\text{C}$	$T = -10^{\circ}\text{C}$	$T = -20^{\circ}\text{C}$
$N = 5$				
$N = 10$				
$N = 20$				

$$= 1 - \frac{\rho' v_p'^2 (1 + \mu')(1 - 2\mu')}{\rho v_p^2 (1 - \mu')} \cdot \frac{(1 - \mu)}{(1 + \mu)(1 - 2\mu)} \quad (12)$$

Considering that the influence of Poisson's ratio is very small during the freeze-thaw cycles, it can be neglected. Therefore, Equation 13 is obtained:

$$D_t = 1 - \frac{\rho' v_p'^2}{\rho v_p^2} \quad (13)$$

It can be concluded from Equation 13 that if the P-wave velocity (v_p and v_p'), mass density (ρ and ρ') of the sample before and after freeze-thaw cycles are measured, the freeze-thaw damage factor D_t can be easily obtained.

$$\frac{\rho'}{\rho} = \frac{\frac{m'}{V'}}{\frac{m}{V}} \quad (14)$$

where m and m' are the mass of the sample before and after freeze-thaw cycles; V and V' are the volumes of the sample before and after freeze-thaw cycles, respectively. Considering that during the freeze-thaw cycle test, the sample is sealed with a thin film on the sides and wax on both ends, therefore, the mass of the sample changes little before and after freeze-thaw cycles. As shown in Equation 15,

$$\frac{m'}{m} \approx 1 \quad (15)$$

Then Equation 13 can be modified as follows:

$$D_t = 1 - \frac{V}{V'} \frac{v_p'^2}{v_p^2} \quad (16)$$

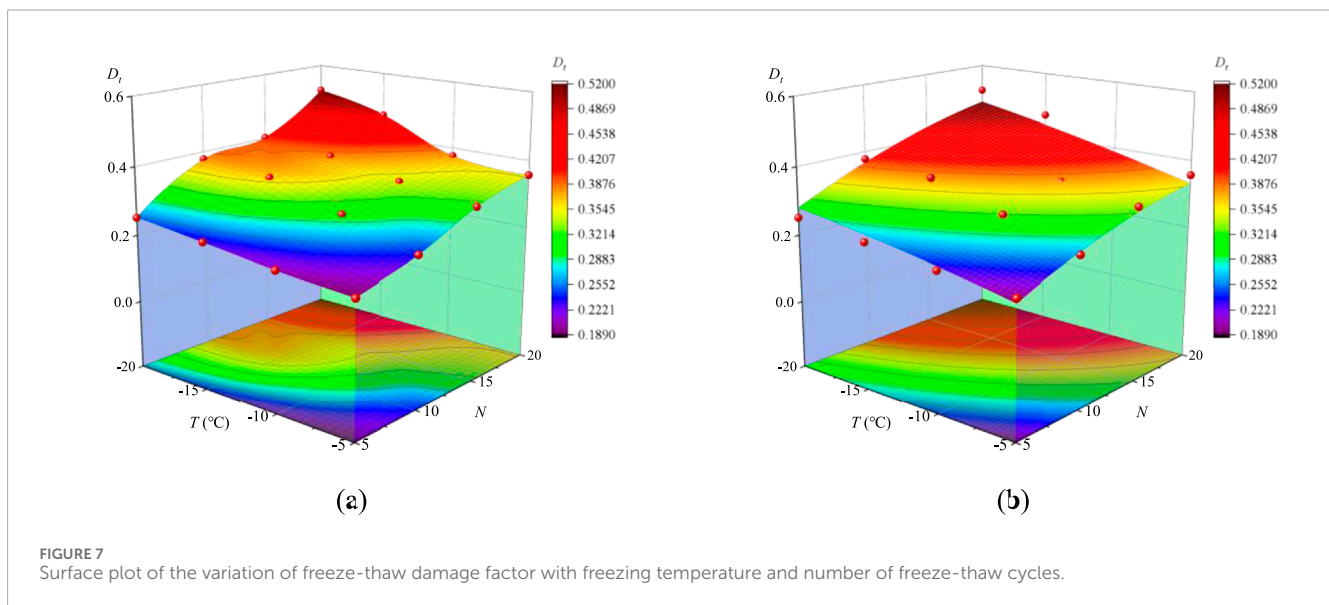
Based on the measured volume and P-wave velocity of the sample before and after the freeze-thaw cycles, the freeze-thaw damage factor D_t can be obtained using Equation 16. The number of freeze-thaw cycles and freezing temperature change the pore structure inside the rock through different degrees of frost heave action, which causes changes in rock volume and P-wave velocity before and after freeze-thaw. Consequently, differences in damage factors can be caused.

4.2 Variation law of freeze-thaw damage factor

By substituting the longitudinal wave velocities v_p , v_p' and volumes V , V' of the samples before and after freeze-thaw cycles from Tables 2 and 3 into Equation 14, the variation law of the average freeze-thaw damage factor D_t with the freezing temperature and cycle numbers can be obtained. As shown in Table 6, the average freeze-thaw damage factor is positively correlated with the number of freeze-thaw cycles. When the number of freeze-thaw cycles increases from 5 to 20, the average freeze-thaw damage factor D_t of the sample increases by 88.24% at each freezing temperature (0.1896–0.3569, $T = -5^{\circ}\text{C}$), 82.61%

TABLE 6 Variation of freeze-thaw damage factor D_t with freezing temperature and number of freeze-thaw cycles.

Sample group	Freezing temperature (°C)	Number of freeze-thaw cycles	Freeze-thaw damage factor	Sample group	Freezing temperature (°C)	Number of freeze-thaw cycles	Freeze-thaw damage factor
1	-5	5	0.1896	9	-15	5	0.2300
2	-5	10	0.2383	10	-15	10	0.3619
3	-5	15	0.3147	11	-15	15	0.3806
4	-5	20	0.3569	12	-15	20	0.4692
5	-10	5	0.2059	13	-20	5	0.2514
6	-10	10	0.2999	14	-20	10	0.3778
7	-10	15	0.3435	15	-20	15	0.4030
8	-10	20	0.3760	16	-20	20	0.5198



(0.2059–0.3760, $T = -10^{\circ}\text{C}$), 104.00% (0.2300–0.4692, $T = -15^{\circ}\text{C}$) and 106.76% (0.2514–0.5198, $T = -20^{\circ}\text{C}$). The average freeze-thaw damage factor D_t is negatively correlated with the freezing temperature. When the freezing temperature drops from -5°C to -20°C , the increasing amplitude in the average freeze-thaw damage factor of the sample under each freeze-thaw cycle is: 32.59% (0.1896–0.2514, $N = 5$), 58.54% (0.2383–0.3778, $N = 10$), 28.06% (0.3147–0.4030, $N = 15$) and 45.64% (0.3569–0.5198, $N = 20$).

According to the data in Table 6, a surface plot of the sample freeze-thaw damage factor D_t with respect to the freezing temperature T and the number of freeze-thaw cycles N is drawn, as shown in Figure 7. Figure 7A shows the surface distribution diagram of the damage factor based on Table 6 and Figure 7B reveals the

surface fitting diagram based on Figure 7A, and its fitting equation is described as follows:

$$D_t = -0.0003T^2 - 0.0006N^2 - 0.0164T + 0.0286N - 1.6 \times 10^{-5}TN - 0.0810 \tag{17}$$

The fitting correlation coefficient R^2 of Equation 17 reaches 0.9519. In other words, Equation 17 is approximately the damage evolution equation of coal-bearing sandstone with respect to freezing temperature T and number of freeze-thaw cycles N under freeze-thaw cycles.

From Equation 17, it can be observed that the coefficients of N^2 and N are larger than those of T^2 and T , indicating that the number of freeze-thaw cycles N has a higher effect on the freeze-thaw

damage and degradation of coal-bearing sandstone than the freezing temperature T ; the absolute value of the coefficient of the TN term is 1.6×10^{-5} , which is much smaller than the coefficients of other terms. This indicates that the coupling effect of the freezing temperature T and the number of freeze-thaw cycles N is relatively weak.

5 Conclusion

- (1) The results of the freeze-thaw cycle tests on coal-bearing sandstone show that the P-wave velocity of the sample decreases with the decrease of freezing temperature or the increase of the number of freeze-thaw cycles, and the relative change rate of the P-wave velocity of the sample before and after freeze-thaw cycles approximately linearly decreases with the decrease of freezing temperature or the increase of freeze-thaw cycles. The decrease in the P-wave velocity of the sample indicates that the P-wave propagation impedance in the sample increases. Therefore, the change in the P-wave velocity of the sample effectively reflects the damage degradation effects of freeze-thaw cycles on the coal-bearing sandstone.
- (2) The volume of the sample before and after freeze-thaw cycles increases as the freezing temperature decreases, or the number of freeze-thaw cycles increases, and the sample porosity increment increases approximately linearly as the freezing temperature decreases or the number of freeze-thaw cycles increases. The increase in sample volume and porosity reflects the continuous development of internal cracks in the sample, indicating the inherent nature of the damage and deterioration development of coal-bearing sand samples.
- (3) With the help of CT scanning imaging technology, the changing rules of porosity and pore structure characteristics of coal-bearing sandstone samples before and after freeze-thaw cycles were obtained. The results show that as the freezing temperature decreases and the number of freeze-thaw cycles increases, the porosity of the sample increases, the number of pores on the specimen cross section increases significantly, and the geometric size increases significantly. This reveals the microscopic mechanism of damage and deterioration of freeze-thaw cycles on coal-bearing sandstone to a certain extent.
- (4) Based on Lemaitre's strain equivalence principle and elastic dynamics theory, a calculation function for the freeze-thaw damage factor based on the P-wave velocity and volume of the sample before and after freeze-thaw cycles is proposed, and an evolution equation of freeze-thaw damage factors based on the freezing temperature and the number of freeze-thaw cycles is established, and the freeze-thaw damage degradation effect of coal-bearing sandstone is effectively characterized.

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Data availability statement

The datasets presented in this study can be found in online repositories. The names of the repository/repository and accession number(s) can be found in the article/supplementary material.

Author contributions

YM: Conceptualization, Writing–original draft, Writing–review and editing. ML: Conceptualization, Data curation, Funding acquisition, Writing–original draft, Writing–review and editing. PW: Funding acquisition, Writing–original draft, Writing–review and editing. SG: Conceptualization, Data curation, Writing–review and editing. FZ: Conceptualization, Data curation, Formal Analysis, Writing–review and editing.

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