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EDITED BY

Huaimin Dong,
Chang'an University, China

REVIEWED BY

Weichao Yan,
Ocean University of China, China
Haitao Wang,
Chongqing University of Science and
Technology, China

*CORRESPONDENCE

Haiyan Wang,
✉ haiyanwang7732@163.com

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Constructions of multi-scale 3D digital rocks by associated image segmentation method

Haiyan Wang*, Xuefeng Yang, Cong Zhou, Jingxu Yan, Jiaqi Yu
and Kui Xie

PetroChina Daqing Oilfield Co., Ltd., Daqing, China

Digital rocks constructed from micro-CT image at a single-resolution face limitations in accurately identifying the entire pore space and mineral components of tight sandstones, due to their high content of nanoscale pores and clay. Consequently, the porosity values derived from such digital rocks are significantly lower compared to those obtained through laboratory measurements, resulting in discrepancies between the measured and calculated petrophysical properties. This study introduces a multi-scale digital rock modeling method by integrating three-dimensional micro-CT images acquired at two distinct resolutions and two-dimensional SEM images. Plunger-shaped core samples and their corresponding sub-samples were scanned at resolutions of 13.99 $\mu\text{m}/\text{voxel}$ and 2.99 $\mu\text{m}/\text{voxel}$, respectively. The scale-invariant feature transform (SIFT) image registration technique was employed to accurately align the two sets of grayscale CT images. Correlation curves between the grayscale value in low-resolution CT images and various mineral contents were established based on the aligned regions, and utilized to construct multi-scale digital rock models. Intragranular pores, unresolvable by the micro-CT images, were identified using SEM imaging, enabling the incorporation of fine-scale features into the models. The resulting multi-scale digital rock models exhibited bulk porosity values that closely matched laboratory helium porosity measurements. Additionally, the elastic moduli calculated by the differential effective medium (DEM) model and the finite element method (FEM) demonstrated good correspondence with experimental results. These results validate the proposed multi-scale digital rock modeling method as an effective approach for accurately characterizing the porosity and mineral components of tight sandstone reservoirs.

KEYWORDS

digital rock, image registration, multi-scale, correlation segmentation, porosity, elastic modulus

1 Introduction

In modern society, the demand for fossil fuels continues to grow, while reserves of conventional oil and gas are gradually depleting. Consequently, the exploration and development of unconventional oil and gas resources have become increasingly important within the petroleum industry. In recent years, the production of oil and gas from unconventional resources has experienced significant growth (Tong et al., 2018; Wang et al., 2016). Among unconventional reservoirs, tight sandstone reservoirs are one of the major reservoirs for unconventional gas resources. Their pore structures and physical properties

are crucial for effective reservoir development (Guo et al., 2022; Li et al., 2017; Wang et al., 2017; Yin et al., 2017). However, tight sandstones are typically characterized by complex pore structures, a broad pore size distribution, and low porosity and permeability. These characteristics present significant challenges for conventional petrophysical experimental techniques when attempting to accurately determine their pore structure features and physical properties (Zhang et al., 2017).

Methods for measuring the porosity of low-permeability rock cores can be broadly classified into two categories: laboratory-based direct measurement techniques and indirect methods based on various downhole testing techniques. Laboratory techniques primarily include mercury intrusion porosimetry (MIP) and nitrogen gas adsorption (N₂GA). MIP functions on the principle that mercury, as a non-wetting liquid, infiltrates pores under applied pressure (Abell et al., 1999). However, this method risks damaging the pore structure, particularly in smaller pores, as mercury infiltration requires higher pressures (Clarkson and Marc Bustin, 1996). In contrast, N₂GA offers greater accuracy but is limited in its capacity to detect pores larger than 200 nm due to the experimental mechanism and sample size constraints. Indirect methods mainly predict core porosity from logging data, such as electrical imaging and sonic logging data (Alizadeh et al., 2015; Close et al., 2009; Newberry et al., 1996; Tixier et al., 1959; Yamada et al., 2013). Laboratory porosity measurements are not only time-consuming and costly but may also cause irreversible damage to the samples. Indirect methods are heavily dependent on the accuracy of the logging data and require a multitude of parameters. Variability in geological environments across different regions may further introduce uncertainties into these methods, affecting the reliability of these methods. Moreover, these traditional methods provide only average characteristics of the pore structure, lacking the capability to accurately delineate the microscopic features of the core pores. This limitation hampers their ability to comprehensively characterize the complexity of low-permeability rocks.

Digital rock technology, which digitizes actual rock cores using high-resolution imaging techniques such as X-ray computed tomography (CT) and scanning electron microscopy (SEM), offers an alternative approach. This technology provides detailed microscopic structural information at the pore scale, enabling the application of advanced numerical algorithms to simulate rock physics experiments. These simulations can effectively analyze the response of physical properties in rock samples. Digital rock technology simplifies the research process, reduces costs and time, enhances result repeatability, and avoids destructive testing of physical samples. It addresses challenges associated with measuring and quantitatively analyzing rock physical parameters, thereby overcoming the inherent limitations of conventional experimental techniques. In recent years, digital rock technology has become a pivotal tool for pore structure analysis and investigation of rock physical properties. Researchers have developed a variety of methods for constructing three-dimensional (3D) digital rock models, primarily focusing on direct modeling utilizing 3D CT images and reconstruction methods based on two-dimensional (2D) images (Bin et al., 2013; Hazlett, 1997; Liu et al., 2023; Liu et al., 2014; Quiblier, 1984; Wu et al., 2004; Yin et al., 2019; Zhao et al., 2007).

However, the unique characteristics of tight sandstones, such as low porosity, low permeability, wide pore size distribution, and

high clay content, may lead to inaccuracies in structure modeling when utilizing digital rock technology based on single-resolution CT scanning. These limitations often lead to significant discrepancies between numerical simulation results and experimental data. To address this issue, this study presents a multi-scale digital rock modeling method that integrates 3D micro-CT images acquired at different resolutions with nanoscale 2D images obtained via SEM. Using the constructed multi-scale digital rock, we calculated the porosity and elastic moduli of tight sandstone samples. The calculated results exhibit good agreement with the laboratory measurements, suggesting that the multi-scale digital rock model provides an accurate depiction of the porosity and mineral components of actual tight sandstones.

2 Samples and experimental measurements

To evaluate the performance of the multi-scale digital rock modeling method proposed in this study, two tight sandstone cores from Changqing Oilfield were selected for digital rock construction and elastic moduli calculations. These core samples, which are plunger-shaped and labeled as N1 and N2, have a diameter of 24.5 mm and were initially subjected to low-resolution CT scanning. To facilitate the construction of a multi-scale digital rock, a cylindrical sub-sample with a diameter of 5 mm was extracted from each original core sample for higher-resolution CT scanning. Figure 1 presents a schematic diagram and photographs of the test sample, illustrating the extraction of the smaller cylindrical sub-sample from the larger core.

To assess the accuracy of the proposed multi-scale 3D digital rock modeling method, laboratory measurements were performed to characterize various properties of the core samples. Helium porosity measurements yielded values of 11.75% for the N1 core and 12.17% for the N2 core. Acoustic properties of the cores were also measured. When saturated with water, the longitudinal wave velocities were 4,217.6 m/s for the N1 core and 4,327.8 m/s for the N2 core, and the corresponding shear wave velocities were 2,551.8 m/s and 2,235.8 m/s, respectively. XRD experiments were conducted to analyze mineral contents, with the results presented in Table 1. These results indicate that the mineral components and their content of the two cores are similar, with the clay content in the N2 core being slightly higher than that in the N1 core, which is similar to the difference in porosities, demonstrating that the clay pores play a significant role in contributing the overall porosity.

3 Multi-scale 3D digital rock modeling method

3.1 Multi-resolution images

Imaging techniques used in digital rock modeling commonly include X-ray CT, SEM, focused ion beam scanning electron microscopy (FIB-SEM), etc. In this study, X-ray CT imaging was employed to construct 3D digital rock models. X-ray CT imaging is a non-destructive testing technology widely utilized in medical and

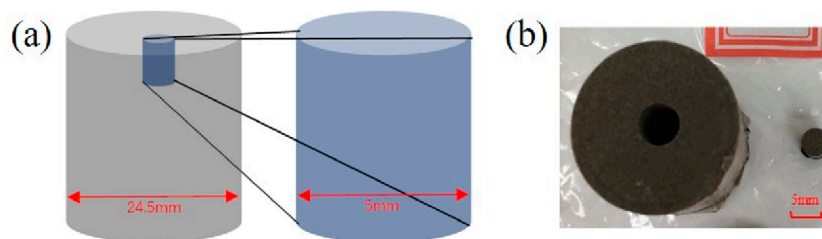


FIGURE 1
(A) Schematic diagram illustrating the extraction of a 5 mm diameter cylindrical subsample from a 24.5 mm diameter plunger core sample. **(B)** Photographs of the N1 core sample and its sub-samples.

TABLE 1 The contents of minerals in the core samples obtained from XRD experiments.

Sample	Quartz/%	Albite/%	Potash feldspar/%	Calcite/%	Dolomite/%	Siderite/%	Clay/%
N1	59	19	8	4	4	1	5
N2	59	20	9	1	3	1	7

industrial applications. The penetration of X-rays through an object causes attenuation, the extent of which depends on the material's properties, such as thickness and density. CT scans of cores taken from different angles generate attenuation maps (Dunsmuir et al., 1991), which are processed using reconstruction algorithms to produce 3D grayscale images. The grayscale values of pixels in these images correspond to the degree of X-ray attenuation, accurately reflecting the spatial distribution of different components.

Tight sandstone core samples and their sub-samples were imaged using CT scans of different resolutions. Initially, CT imaging with a resolution of 13.99 $\mu\text{m}/\text{voxel}$ was performed on two original tight sandstone core samples. After extracting sub-samples from the original cores, high-resolution (2.99 $\mu\text{m}/\text{voxel}$) CT imaging was conducted on the small sub-samples. The 3D CT images had a resolution of 1,920 \times 1,920 \times 1,536 voxels. Figure 2 shows the CT scan slice images for both N1 and N2 samples at the different resolutions, highlighting the level of detail achieved at each scanning resolution. To identify micropores beyond the resolution limit of CT scanning, broad ion beam scanning electron microscopy (BIB-SEM) with a resolution of 5 nm/pixel was employed. Furthermore, to create a 2D image of the core surface with a large field of view, the MAPS image stitching technique was utilized. This technique involves combining multiple high-resolution SEM images to form a single, expansive image (Lemmens and Richards, 2013). The resulting MAPS image was of a considerable size, measuring 105,000 \times 106,000 pixels, which provides a detailed and expansive view of the core's surface.

3.2 Image registration method

Image registration techniques aim to establish correspondence between corresponding positions in two different images through various operations such as rigid transformation, similarity transformation, affine transformation, projection transformation,

and polynomial transformation. This technology is widely applied in medical image processing, image analysis, remote sensing fusion, and computer vision.

Image registration methods can be broadly categorized into information-based registration and feature-based registration. Grayscale-based registration methods, which rely on the grayscale features of two images, have been extensively studied. The principle of this approach involves using the grayscale value information at each position for alignment. Because images typically contain vast amounts of grayscale data, this method requires substantial computational resources and often results in prolonged registration times. Furthermore, because the two images may not be captured simultaneously or with the same equipment, variations in grayscale information can significantly reduce the success rate of registration. In contrast, feature-based image registration methods offer lower computational requirements and faster processing speeds, effectively enhancing both the efficiency and accuracy of registration. Algorithms such as the Harris corner detection, Moravec algorithm, and scale-invariant feature transform (SIFT) have been developed to support feature-based image registration.

In this study, the SIFT algorithm was employed for image registration, a method based on feature points. This method was first introduced by Lowe at the International Conference on Computer Vision in 1999 (Lowe, 1999). SIFT algorithm is based on the scale space and ensures invariance to image translation, rotation, scaling, and even affine transformations. The algorithm represents image information across various scales using a Difference of Gaussian (DOG) pyramid and identifies key points by detecting extrema in the DOG images. The precise locations and scales of these key points are determined using an optimization algorithm, which also eliminates points with poor responses or edge responses, thereby yielding the image's feature points. By calculating the magnitude and orientation of gradients around the feature points, an orientation is assigned, ensuring the feature points remain invariant to scale and rotation. Local image information around each feature point

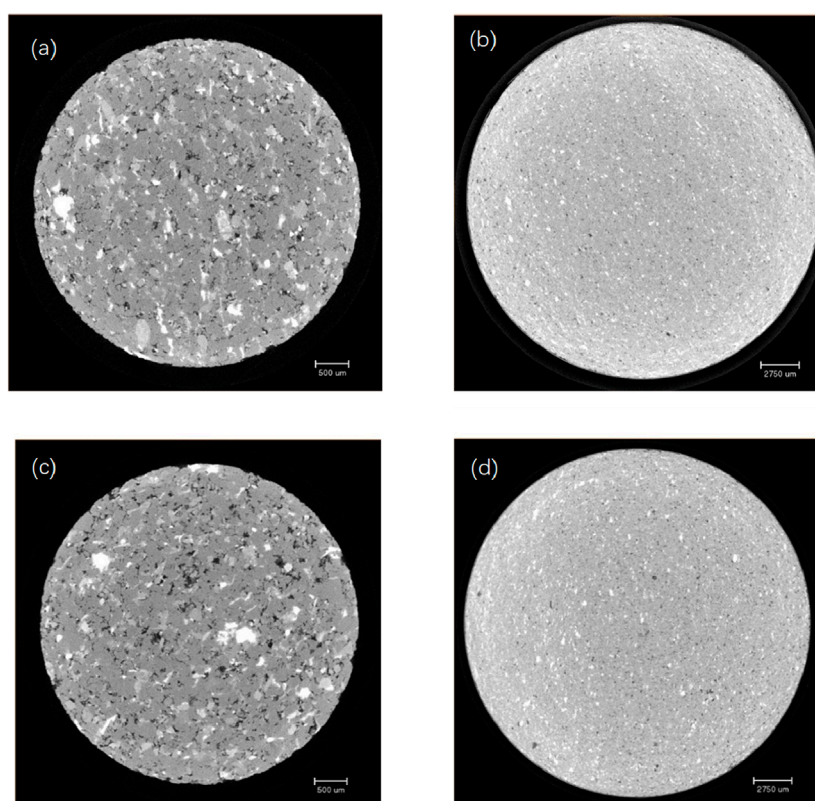


FIGURE 2 High-resolution (2.99 $\mu\text{m}/\text{voxel}$) CT scan slice images of the (A) N1 and (C) N2 sub-samples. Low-resolution (13.99 $\mu\text{m}/\text{voxel}$) CT images of the (B) N1 and (D) N2 origin samples.

is then used to generate distinctive descriptors, further enhancing the accuracy of feature matching. The positional information of matching feature points allows the calculation of the matching region between two images. Corresponding sections of images with varying resolutions can be aligned through operations such as rotation and cropping. These functions can be implemented using the open-source program “siftdemoV4” developed by Lowe (1999), Lowe (2004). Figure 3 illustrates the flowchart of the image registration process, detailing each step in the procedure.

3.3 Microporosity of mineral component

Based on the geometry of pores in the core samples, pore spaces can be categorized into intergranular pores, intragranular pores, intercrystalline pores, and cracks. CT imaging is capable of identifying large pores located between particles of various components in the core. However, it cannot resolve micropores due to its resolution limitation (Liu and Ostadhassan, 2017). Therefore, incorporating microporosity associated with different mineral components reflects the objective reality, thereby enabling a more accurate estimation of core porosity.

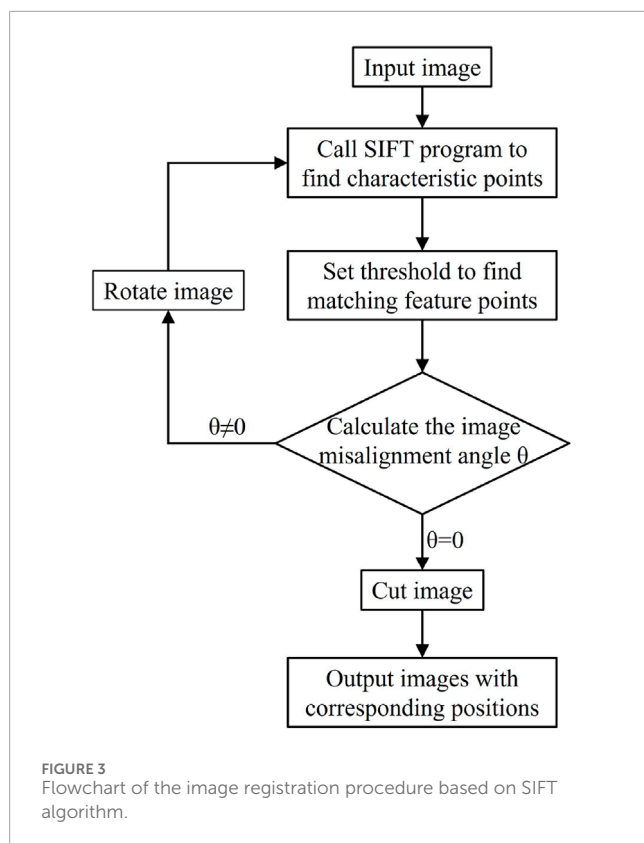
Nano-resolution 2D MAPS imaging enables identifying pore types and their spatial locations. Small pore clusters within the feldspar, quartz or calcite grains are classified as dissolved pores, while larger pore clusters located between quartz, albite, and

feldspar grains are categorized as intercrystalline pores. Clusters of small pores surrounded by clay minerals are identified as clay-dominated micropores. Statistical analysis of various pore types observed in the MAPS image facilitates the calculation of microporosity with each mineral component. The corresponding data are presented in Table 2.

3.4 Associated image segmentation

Coarse-scale digital rocks feature lower resolution, with each voxel potentially representing multiple mineral components. In contrast, fine-scale digital rocks offer more precise information but may lack broader representativeness due to their limited sample size. Consequently, an effective strategy for rock physics research involves integrating digital rocks at both scales and performing upscaling operations to bridge the discrepancies between scales.

Based on the scale relationship between the two resolutions in CT imaging, each voxel in the coarse-scale digital rock corresponds to a $5 \times 5 \times 5$ voxel grid in the fine-scale digital rock. Utilizing this relationship, the proportions of mineral components within each voxel can be extracted. By statistically analyzing all voxels with the same grayscale value in the coarse-scale digital rock, the average content of each mineral component can be determined, enabling the calculation of the mineral component proportions represented by that grayscale value. By using a program to perform



traversal statistics, a correlation curve between grayscale values and the mineral component proportions in the coarse-scale digital rock was generated (Figure 4). This curve establishes a direct mapping between image grayscale information and mineral component proportions.

The porosity of each voxel in the coarse-scale digital rock is calculated using the formula:

$$\vartheta_i = \sum_k f_k(g_i) \times \varphi_k \quad (1)$$

where ϑ_i is the porosity of the i th voxel, g_i is the grayscale value of the i th voxel, $f_k(g_i)$ is the proportion of the k th component corresponding to the grayscale value g_i which can be obtained from the correlation curves (Figure 4), and φ_k is the microporosity of the k th component (see Table 2). After calculating the porosity of all voxels within the coarse-scale image using Equation 1, the total porosity of the entire core sample is obtained by averaging all voxel porosities.

3.5 Elastic modulus calculation

The complexity of multi-component tight sandstone digital rocks, coupled with the inclusion of microporosity, makes the conventional single-mineral-component method for calculating the elastic modulus no longer applicable. To address this limitation, we developed an integrated approach that combines the differential effective medium (DEM) model with the finite element method (FEM). Figure 5 illustrates the step-by-step flowchart of the proposed calculation methodology.

In this study, CT imaging was utilized to segment the core into five distinct components: pores, clay, quartz (albite), potash feldspar, and dolomite. This segmentation is crucial for accurately modeling the rock's physical properties. The coarse-scale digital rock is represented by an 8-bit grayscale image consisting of 256 distinct grayscale values. The equivalent elastic modulus for each of these grayscale values was obtained using two-step DEM calculation process. In the first DEM step, each mineral component, assumed to be in its pure solid state, was designated as the matrix, with micropores incorporated to compute the component's equivalent elastic modulus (Berryman, 1980). The elastic moduli for pure mineral component were determined using the data in Table 3. Additionally, since the sound velocity measurements were conducted under water-saturated conditions, the elastic properties of water were considered during the addition of the pores. In the second DEM step, different components were sequentially added based on the correlation curve, enabling the calculation of the equivalent elastic modulus corresponding to each grayscale value, which represents different mineral mixtures. Following the DEM calculations, the FEM was applied to compute the overall elastic moduli of the coarse-scale digital rock. The employed FEM program is developed by Garboczi (1998). This program uses a hexahedral mesh with voxels as elements and has been validated for accuracy in multiple studies (Arns et al., 2005; Arns et al., 2002).

4 Results and discussions

4.1 Image registration

Figure 6 displays the registration images for CT images at varying resolutions, generated using the SIFT registration program. The figure reveals both correctly matched points and instances of mismatched points. These mismatched points can be corrected through manual intervention.

Once accurate registration information is obtained, the 3D images are adjusted through rotation, and corresponding cube images at different resolutions are extracted. Figures 7A, B present 3D comparison images of the N1 and N2 cores, respectively. The double arrows in these figures indicate corresponding feature points, demonstrating the precise alignment of the images across different resolutions.

4.2 Porosities

Core porosity is a crucial parameter for estimating reservoir oil and gas reserves as well as productivity. It represents one of the most important petrophysical characteristic in oilfield exploration and development. Generally, higher porosity in the reservoir cores correlates with greater oil and gas reserves and easier extraction. Enhancing the precision of core porosity calculations provides valuable guidance for the exploitation and development of oil and gas fields.

Table 4 presents the calculated porosity for the different digital rock models. For the single-scale N1 digital rock, porosities are 1.5% at 13.99 $\mu\text{m}/\text{voxel}$ resolution and 5.7% at 2.99 $\mu\text{m}/\text{voxel}$

TABLE 2 Microporosity of the mineral component in the tight sandstone samples.

Component	Pore	Clay	Quartz	Feldspar	Siderite
Microporosity φ	1	0.3	0.03	0.1	0

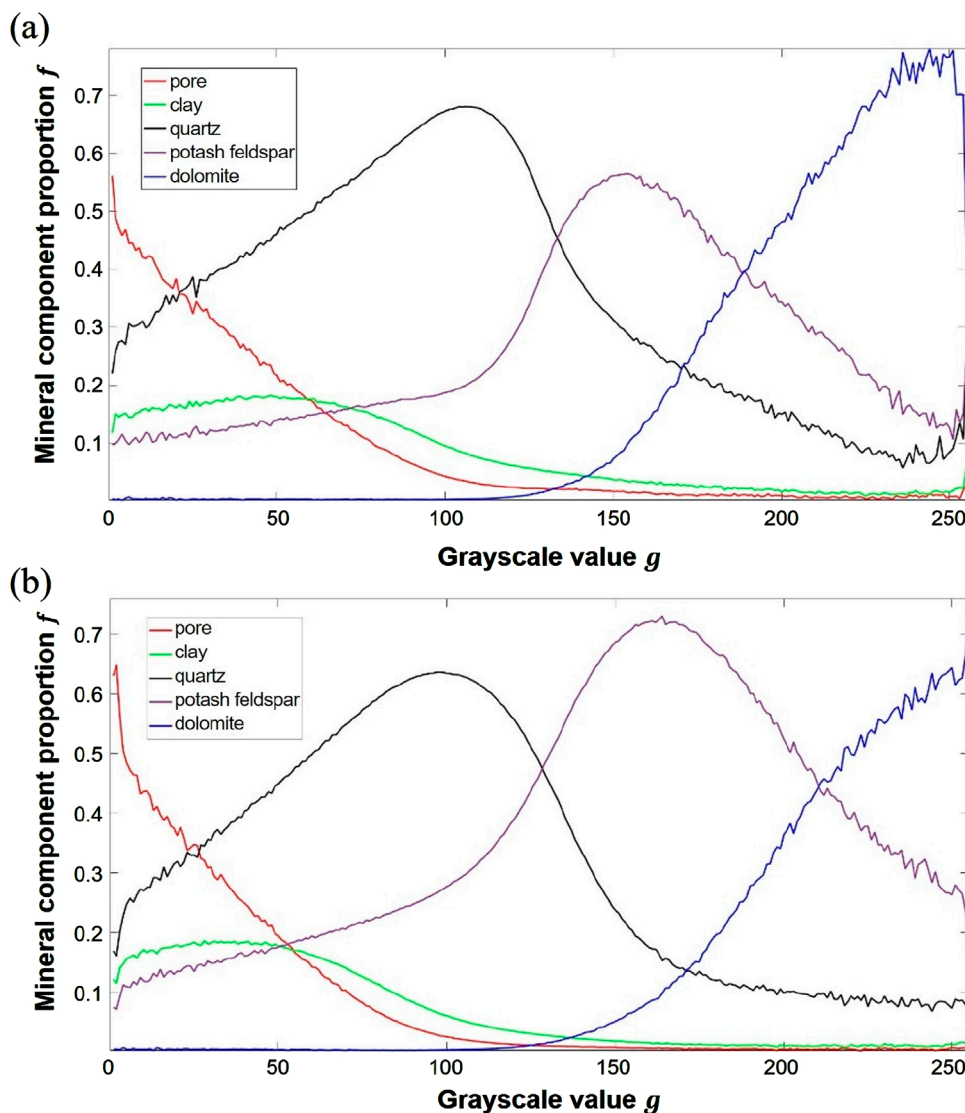


FIGURE 4 The correlation curves between grayscale value and mineral component proportion in the coarse-scale digital rocks of (A) N1 and (B) N2 based on low resolution CT grayscale images.

resolution, while for the N2 core, the corresponding values are 0.5% and 2.3%, respectively. In the multi-scale and multi-component models, incorporating microporosity results in porosities of 11.13% for N1 and 12.94% for N2, compared to 3.43% and 5.11% without considering microporosity. These results suggest that porosities derived from single-scale resolutions deviate significantly from experimental measurements, highlighting the limitations of such calculations in fully characterizing the pore structures of core samples.

Significantly, incorporating the microporosity of mineral components produces porosity estimates that closely match experimental gas porosities. The calculated porosity errors for the N1 and N2 rock cores are 5.28% and 6.33%, respectively, compared to experimental porosities. This highlights the substantial contribution of micropores to total porosity in tight sandstone cores. The use of multi-scale digital rocks for porosity calculations demonstrates improved accuracy, thereby enhancing the reliability of the results.

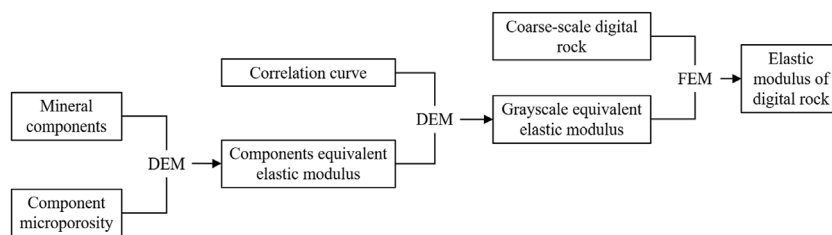


FIGURE 5 Flowchart of elastic modulus calculation method for upscaled digital rock based on the combination of DEM and FEM.

TABLE 3 The elastic moduli for each component when it is in a pure phase state.

Component	Bulk modulus/GPa	Shear modulus/GPa
Water	2.18	0
Clay	37.9	14.8
Quartz	37.7	44.5
Albite	55.1	29.7
Potash feldspar	56.2	29.3
Dolomite	95.5	11.4

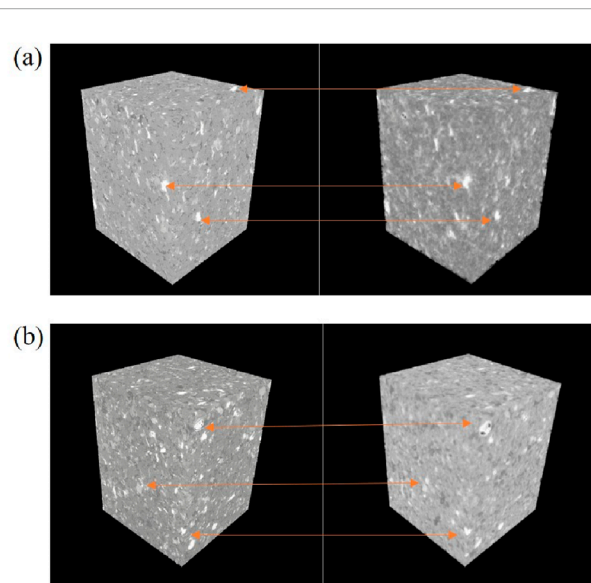


FIGURE 7 3D images of and core samples (A) N1 and (B) N2 at different resolutions, with high-resolution images on the left and corresponding low-resolution images on the right. The double arrows indicate corresponding feature points.

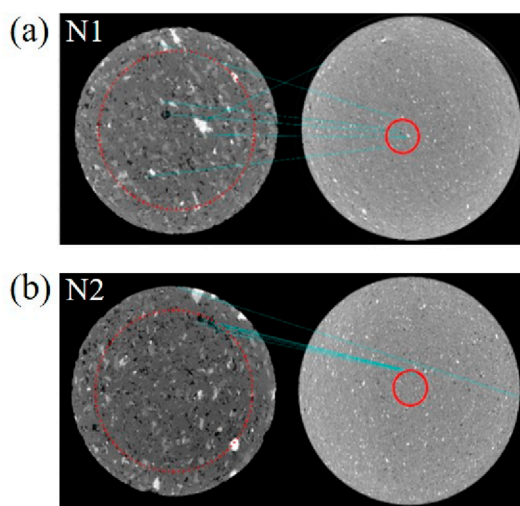


FIGURE 6 Registration images of and core samples (A) N1 and (B) N2 at different resolutions, with high-resolution images on the left and corresponding low-resolution images on the right. The blue line indicates the matching points.

Jin et al. (2018) constructed a digital rock model using CT images with a resolution of 0.7 μm/voxel and introduced component microporosity to calculate core porosity, achieving an error margin

within 5.20%. The accuracy of porosity calculations at a single-resolution digital rock depends on image resolution, with higher-resolution images yielding more precise results. In our study, despite using a maximum CT image resolution of 2.99 μm/voxel, which is significantly lower than the 0.7 μm/voxel used by Jin et al., the maximum calculation error is 6.33%, comparable to the reported 5.20%. This result suggests that establishing an upscaled digital rock model effectively reduces the resolution requirements while maintaining high calculation accuracy.

4.3 Elastic moduli

Based on the constructed multi-scale digital rock, the proportions of various mineral components in the low-resolution images can be accurately quantified. Table 5 provides a comparative analysis of the N2 core’s XRD experimental data and the corresponding statistical results derived from the multi-scale digital rock model. Since the differentiation of components in X-ray CT

TABLE 4 Porosities from lab measurements and digital rock samples at different scales.

Sample	Porosity calculated by digital rock/%				Helium porosity/%
	Single-scale digital rock		Multi-scale digital rock	Multi-scale digital rock with microporosity	
	13.99 μm	2.99 μm			
N1	1.5	5.7	3.43	11.13	11.75
N2	0.5	2.3	5.11	12.94	12.17

TABLE 5 Mineral components and contents of the N2 core sample from XRD measurements and the digital rock method.

Method	Clay/%	Quartz (plagioclase)/%	Potash feldspar (calcite)/%	Dolomite (siderite)/%
XRD	7.00	79.00	10.00	4.00
Digital rock	7.67	81.68	9.19	1.46

TABLE 6 Results of elastic moduli from the simulation based on the multi-scale digital rock method and the experimental measurements.

Sample	Multi-scale digital rock		Experimental measurements	
	Bulk modulus/Gpa	Shear modulus/Gpa	Bulk modulus/Gpa	Shear modulus/Gpa
N1	21.67	18.29	22.5	16.1
N2	27.85	13.56	29.7	12.3

images relies on variations in voxel grayscale values, minerals that exhibit minimal differences in grayscale value may be aggregated into a single phase, even though they represent distinct components.

Table 5 demonstrates that the mineral component analysis derived from correlation-based segmentation closely aligns with the XRD experimental data, although a notable disparity exists between the measurements for dolomite and siderite. This disparity is primarily attributed to misalignment during the image registration process, which disproportionately affects minerals with low abundance that are primarily distributed as discrete points within the core, rendering them more sensitive to registration inaccuracies.

Table 6 presents the elastic moduli results from the simulations based on the multi-scale digital rocks compared with the experimental measurements. The calculated elastic moduli exhibit good agreement with the experimental data, validating the accuracy of the multi-scale digital rock model. These results confirm that the constructed model effectively captures the distribution characteristics of minerals and pores within the core, providing a reliable modeling method for further digital rock physics research.

In unconventional oil and gas reservoirs, such as tight sandstones and shales, the reservoir rocks often exhibit a high degree of heterogeneity. Traditional digital rock technology, which relies on single-resolution imaging, faces challenges in balancing field of view and image resolution. In recent years, multi-scale

digital rock technology, which employs various resolutions and imaging techniques, has made significant progress. Walls et al. (2017) compared multi-scale digital rocks using SEM imaging at different resolutions, demonstrating that multi-resolution imaging significantly improves pore identification accuracy. Islam et al. (2019) conducted multi-scale imaging and numerical simulations on the permeability of heterogeneous carbonate rocks, establishing porosity-permeability curves and analyzing resolution impacts on porosity calculations. Liu et al. (2017) explored the pore characteristics of rock samples through fractal theory, revealing that pore complexity and fractal dimensions increase with magnification.

In the multi-scale digital rock techniques, upscaling methods have been developed to correlate data across scales effectively, enabling comprehensive analysis of core properties. These methods include the overlay method, representative elementary volume (REV), and integration of multiple computational approaches. The overlay method allows for the refinement of images and is commonly used in the upscaling construction of pore models. Yao et al. (2015) constructed multi-scale pore network models using different resolution SEM images and the Markov Chain-Monte Carlo method. The REV method involves partitioning the core to ensure that each section has similar properties, thus achieving upscaling from high to low resolution. Sun et al. (2019) proposed an upscaling porosity method using REV selection across CT-scanned samples. Suhrer et al. (2020) obtained multiple REV's based on

image complexity to achieve upscaling modeling. The integration of multiple computational methods utilizes the differences in scale between different computational methods. Ning et al. (2016) combined molecular dynamics (MD) and lattice Boltzmann methods to achieve nanoscale-to-microscale fluid transport simulations.

In this study, a two-step upscaling process was used to calculate the equivalent elastic moduli for the FEM simulations. Nano-resolution SEM data provided micro-porosity insights, integrated into mineral components. The precise registrations of high- and low-resolution CT images provide the relationship between mineral component proportions and grayscale value in the coarse-scale digital rocks, thereby obtaining the equivalent elastic moduli of each voxel. This approach maintains computational accuracy while significantly improving efficiency. It is noteworthy that due to the high sensitivity of the elastic modulus to porosity and mineral components, this upscaling method is particularly suitable for elastic modulus calculations. However, for flow characteristics and electrical properties, which depend on pore connectivity, fine-scale structural information loss during upscaling may impact the result accuracy, warranting further investigation.

5 Conclusion

This study introduces a method for constructing multi-scale digital rocks by integrating 3D micro-CT images at two different resolutions and 2D SEM-MAPS images. SIFT image registration was applied to align high- and low-resolution CT images, establishing a correlation curve between grayscale values in low-resolution images and mineral component proportions. To capture the microporosity of mineral components not identified by micro-CT, nanoscale SEM-MAPS scanning was employed. Using the correlation curve, microporosity of mineral components and low-resolution CT images, the multi-scale digital rocks were constructed. This multi-scale modeling method successfully produced digital rock models that accurately represent the porosity and minerals' content of tight sandstones. An upscaling method by calculating the equivalent elastic moduli of voxels of different grayscale value based on DEM theory was utilized and the FEM simulation was deployed to calculate the elastic moduli of the cores. The porosities and simulated elastic moduli of the multi-scale digital rocks exhibited good agreement the experimental data. These results confirm that the constructed model effectively captures the distribution characteristics of minerals and pores within the core, which helps to improve the efficiency and accuracy of subsequent rock physics simulation researches.

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Data availability statement

The original contributions presented in the study are included in the article/supplementary material, further inquiries can be directed to the corresponding author.

Author contributions

HW: Conceptualization, Data curation, Formal Analysis, Investigation, Methodology, Resources, Supervision, Validation, Visualization, Writing–original draft, Writing–review and editing. XY: Conceptualization, Data curation, Methodology, Writing–review and editing. CZ: Supervision, Validation, Visualization, Writing–review and editing. JXY: Data curation, Methodology, Investigation, Writing–review and editing. JQY: Supervision, Validation, Visualization, Writing–review and editing. KX: Supervision, Visualization, Writing–review and editing.

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Conflict of interest

Authors HW, XY, CZ, JnY, JaY, and KX were employed by PetroChina Daqing Oilfield Co., Ltd.

Generative AI statement

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