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# Evaluation of the water weakening coefficient of sandstones by using non-destructive physical parameters

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**Introduction:** The presence of water significantly reduces the mechanical strength of rocks and induces various engineering geological hazards. The water weakening coefficient  $K_p$  is used to quantify this effect, defined as the ratio of wet uniaxial compressive strength to the dry value.

**Methods:** A comprehensive physico-mechanical test was conducted on fifteen sandstones under dry and saturated conditions to predict the water weakening coefficient using easily obtainable physical parameters. Multiple linear regression was employed to establish the relationship between these parameters and the saturated water weakening coefficient.

**Results:** The saturated water weakening coefficient decreases with increasing porosity and increases with higher Primary wave velocity (P-wave velocity). Rocks with higher porosity but lower P-wave velocity typically absorb more water. The P-wave velocity and clay mineral content were identified as the best predictors of the saturated water weakening coefficient ( $R^2 = 0.82$ ). Unsaturated water weakening coefficients at any water saturation level were well estimated using a previous exponential function.

**Discussion:** The roles of different clay minerals and P-wave velocity in the water weakening process of rocks are comprehensively discussed. This study enhances the understanding of the water weakening mechanism and provides an improved evaluation model for the water weakening coefficient of sandstones using physical parameters.

## KEYWORDS

water weakening coefficient, uniaxial compression strength, clay minerals, P-wave velocity, multiple linear regression

## 1 Introduction

Sandstone, as a kind of typical sedimentary rock, is widely distributed on the earth's surface and is often used as construction material due to its good cementation capacity and easy accessibility (Sun and Zhang, 2019). However, in rock engineering fields, sandstone inevitably comes into contact with water. The presence of water significantly reduces its mechanical properties, leading to geological disasters such as pillar instability (Lafrance et al., 2016), landslides (Song et al., 2018) and tunnel collapse (Yang et al., 2020). Additionally, most sandstones contain clay minerals. When these minerals absorb water, the resulting uneven stress distribution caused by the swelling of clay minerals will induce the deterioration of sandstones (Shen, 2014; Yuan et al., 2014). Therefore, it is essential to comprehensively investigate the strength change in sandstone after absorbing water in order to provide mechanical parameters for the safe design of rock engineering projects in water-prone areas.

Over the past few decades, extensive research has been conducted on the strength loss of sandstone from dry to saturated conditions. Hawkins and McConnell (1992) claimed that the maximum uniaxial compressive strength (UCS) loss at the fully saturated condition exceeded 70% after testing 35 sandstone samples. They held that the water weakening degree was primarily controlled by the mineral composition, particularly the content of quartz and clay minerals. Erguler and Ulusay (2009) further investigated the water weakening process of clay-bearing sandstones. The UCS of sandstones decreased by more than 90% after absorbing water. Tomor et al. (2024) investigated the reduction in UCS of sandstones under different moisture levels. They tested thirty-four UK Darney sandstone samples under six moisture conditions and evaluated moisture gain and loss over time. For 77 sandstones reviewed in the literature, UCS loss ranged up to 45% between oven-dry and saturated conditions, with an average loss of 20%. Wong et al. (2016) comprehensively summarized the variation of mechanical properties for different types of rocks exposed to water. They claimed that not only the strength but also the stiffness of rocks were reduced by the presence of water. Huang et al. (2022c) measured the UCS of four clay-bearing sandstones containing different water contents. The UCS of these sandstones decreased significantly when the water saturation increased from 0 to a critical water saturation, approximately 60%–80%, however, the reduction of UCS was not remarkable beyond this critical saturation. Li et al. (2019) also held that the strength of siltstones decreased from dry to saturated conditions. They concluded that the hydration of clay minerals reduced the cohesion of samples, and the hydrolysis of quartz in the crack tip region promoted the subcritical crack propagation during the loading process. In contrast, Reviron et al. (2009) found that water had no significant effect on the strength of sandstones composed almost entirely of quartz and lacking clay minerals. Chen et al. (2017) proposed that the reduction in strength and elastic modulus of siltstone after water absorption was caused by the dissolution of cementing minerals and subsequent increasing of distance between hard particles. Cai et al. (2019) addressed that a high expansion stress would arise due to the swelling of clay minerals, which should be responsible for the propagation of existing micro-cracks and generation of new cracks. Lu et al. (2017) discussed the roles of critical saturation and clay mineral content in the water weakening effect of sandstones by

using Computed tomography (CT), in which it was found that the montmorillonite had a much larger adverse effect on the internal structure and mechanical properties than low swelling clay minerals, such as kaolinite and chlorite. Siegesmund et al. (2003) investigated the damage mechanisms of water-saturated sandstone using X-ray diffraction (XRD), Cation exchange capacity (CEC), and Scanning electron microscope (SEM) experimental methods. They concluded that the intracrystalline swelling of expandable clay minerals and intercrystalline or osmotic swelling are the primary causes of damage to the sandstone. It can be concluded that the presence of water will cause the UCS reduction, and clay minerals have a significant influence on the water weakening degree of sandstones. However, the quantification relationship between the mineral component and UCS loss of sandstones after absorbing water is not fully built.

Traditional mechanical tests are time-consuming and laborious, therefore, some physical parameters by non-destructive test methods are usually adopted to estimate the UCS of rocks (Huang et al., 2022a; 2022b). Table 1 has summarized previous evaluation functions of UCS by using physical parameters in recent years. It can be found that the UCS increases with increasing the P-wave velocity and density, however, it decreases with increasing the porosity and water content. In addition, the sedimentary and mudstone with more clay mineral contents have a relatively smaller UCS according to predicted equations proposed by Gokceoglu et al. (2009) and Iyare et al. (2021). It illustrates that many physical parameters have significant influences on the UCS of rocks, including the P-wave velocity, density, porosity, clay mineral content and water content. In Table 1, the linear function, power function and exponential function are the most widely used functions to estimate UCS. However, most of the evaluation equations in Table 1 only use one physical parameter. The determination of the best subset of physical parameters to accurately predict the water weakening coefficient of sandstones after absorbing water need further study. In addition, the contribution of clay minerals to the water weakening degree is also not clear.

## 2 Experimental procedure

### 2.1 Sample preparation

Fifteen kinds of sandstones with different initial physico-mechanical properties were used in this study. They were collected from some rainy regions, including Dali in Yunnan Province (AAR = 870 mm), Hangzhou in Zhejiang Province (AAR = 1,930 mm), Xi'an in Shanxi Province (AAR = 1,067.9 mm), Zigong in Sichuan Province (AAR = 1,223 mm) and Yichang in Hubei Province (AAR=1,216 mm). All sandstone samples were drilled from large sandstone blocks in order to avoid the discreteness caused by geological formation. All sandstone samples were drilled by using a coring drill with an internal diameter of 50 mm, then cylindrical cores were cut to the height of 100 mm by using a cutter. According to the suggested method by ASTM, D4543-08, (2008), both ends of the sample were polished, and the flatness should be less than 0.025 mm. Therefore, these cylindrical samples are 50 mm in the diameter and 100 mm in the height.

TABLE 1 Representative evaluation functions of UCS by using different non-destructive physical parameters.

Rock type	Regions	Number of samples	Predicted function	R <sup>2</sup>	References
<b>P-wave velocity (Unit: km/s)</b>					
Granite	Türkiye	N = 19	$\sigma_c = 35.53V_p^{-55}$	0.80	Tuğrul and Zarif (1999)
48 rocks	Türkiye	N = 27	$\sigma_c = 9.95V_p^{1.21}$	0.83	Kahraman (2001)
Sandstone, etc	Türkiye	N = 150	$\sigma_c = 56.71V_p^{-192.93}$	0.67	Çobanoğlu and Çelik (2008)
Igimbrite	Türkiye	N = 264	$\sigma_c = 3.9V_p^{1.8}$	0.65	Binal (2009)
Sandstone	Iran	N = 70	$\sigma_c^{sa} = 0.0244\exp(0.0012V_p)$	0.83	Rezaei et al. (2019)
Flint	Europe	N = 7	$\sigma_c = 0.91V_p^{-4500.6}$	0.87	Aliyu et al. (2019)
Shale	Iran	N = 33	$\sigma_c = 2 \times 10^{-5}V_p^{1.624}$	0.93	Rastegarnia et al. (2021)
Calcarenite	Spain	N = 5	$\sigma_c^{sa} = 2.0365(V_p^{sa})^{-3502}$	0.96	Rabat et al. (2020)
Gypsum	Türkiye	N = 250	$\sigma_c = 3.9348\exp(0.6129V_p)$	0.82	Yilmaz and Yuksek (2009)
<b>Density (Unit: g/cm<sup>3</sup>)</b>					
Siltstone, etc	Türkiye	N = 67	$\sigma_c^{sa} = 0.13\exp(0.2134\rho^d)$	0.90	Erguler and Ulusay (2009)
Travertines	Hungary	N = 40	$\sigma_c^{sa} = 0.0001\exp(5.2435\rho^{sa})$	0.85	Török and Vásárhelyi (2010)
Sandstone, etc	India	N = 20	$\sigma_c = 287.7\rho^d - 615.9$	0.76	Mishra and Basu (2013)
Sandstone	United States	--	$\sigma_c^{sa} = 0.03\exp(3.41\rho^d)$	0.92	Kim and Changani (2016)
Flint	North-West Europe	N = 7	$\sigma_c = -6716.8(\rho^d)^2 + 35,905.6\rho^d - 47454.4$	0.90	Aliyu et al. (2019)
Calcarenite	Spain	N = 5	$\sigma_c^{sa} = 6 \times 10^{-8}\exp(1.889\rho^{sa})$	0.78	Rabat et al. (2020)
<b>Porosity (Unit: %)</b>					
Gypsum	Türkiye	N = 250	$\sigma_c = -28.429\ln(n) + 78.989$	0.80	Yilmaz and Yuksek (2009)
Sandstone, etc	India	N = 20	$\sigma_c = -55.7\ln(n) + 172.1$	0.88	Mishra and Basu (2013)
Mudstone	Trinidad	N = 7	$\sigma_c = -6.61n + 244.4$	0.70	Iyare et al. (2021)
Shale	Iran	N = 33	$\sigma_c = -0.26n + 7.5$	0.79	Rastegarnia et al. (2021)
<b>Water content (Unit: %)</b>					
Gypsum	Türkiye	N = 29	$\sigma_c = 16.68\exp(-0.8193W_a) + 24$	0.93	Yilmaz (2010)
Siltstone, etc	Türkiye	N = 67	$\sigma_c^{sa} = 67.1W_a^{-0.9951}$	0.87	Erguler and Ulusay (2009)
Sandstone	China	N = 16	$\sigma_c = 19.95\exp(-0.659W_a) + 46.8$	0.94	Zhou et al. (2016)
Sandstone	Australia	N = 25	$\sigma_c = 43.63\exp(-0.2W_a)$	0.89	Masoumi et al. (2017)
Sandstone	China	N = 41	$\sigma_c = 80.6\exp(-0.904W_a) + 43.17$	0.98	Tang (2018)
Siltstone	China	N = 12	$\sigma_c = 57.44\exp(-0.383W_a) + 17.71$	0.97	Li et al. (2019)
Shale	Iran	N = 33	$\sigma_c = -0.067W_a^2 + 0.058W_a + 7.081$	0.71	Rastegarnia et al. (2021)
<b>Clay content (Unit: %)</b>					
Sedimentary	Türkiye	N = 65	$\sigma_c/\sigma_{c(max)} = 1.134\exp[-1.1302CM/CM^{(max)}]$	0.79	Gokceoglu et al. (2009)
Mudstone	Trinidad	N = 7	$\sigma_c = -16.12CM + 218.47$	0.43	Iyare et al. (2021)

(Continued on the following page)

TABLE 1 (Continued) Representative evaluation functions of UCS by using different non-destructive physical parameters.

Rock type	Regions	Number of samples	Predicted function	R <sup>2</sup>	References
<b>Multivariate</b>					
Limestone, etc	Iran	N = 8	$\sigma_c^{sa} = 5.98 (\rho^{sa}/n) + 22.032$	0.65	Rajabzadeh et al. (2012)
Sandstone, etc	Türkiye	N = 13	$\log [\sigma_c (S_r)] = 1.368 + 0.794 \text{Log} (1 + V_p) - 0.201S_r - 0.056E_{cc}$	0.91	Karakul and Ulusay (2013)
Limestone	Iran	N = 105	$\sigma_c = 90 - 0.021V_p + 3 (\rho^d)^3 + 0.019n^3$	0.93	Torabi-Kaveh et al. (2015)
Limestone	Iran	N = 18	$\sigma_c = 20.54 + 0.013V_p - 3.27n$	0.92	Jamshidi et al. (2018)
Limestone	Chile	N = 13	$\sigma_c^{sa} = 2.0137 \exp (0.794V_p - 0.401n)$	0.85	González et al. (2019)
Travertine	Chile	N = 29	$\sigma_c = -13648 + 2407V_p + 5623\rho^d + 322n - 982V_p \times \rho^d - 10V_p \times n - 115 (\rho^d)^n$	0.84	Saldaña et al. (2020)

Note that:  $V_p$ -P-wave velocity,  $V_p^{sa}$ - P-wave velocity at saturation condition,  $\rho^d$ -Dry density;  $\rho^{sa}$ - Saturated density,  $\sigma_c^{sa}$ - Saturation uniaxial compressive strength,  $\sigma_c$ -Uniaxial compressive strength,  $N$ -Number of samples,  $CM$ -Clay mineral content,  $W_a$ -Water content,  $S_r$ -Water saturation,  $n$ -porosity of rock,  $E_{cc}$ -Effective clay mineral content.

In this experiment, both the dry and saturated UCS were measured. To avoid test errors caused by the discreteness of samples, three parallel tests were conducted on the same condition. Therefore, 90 standard cylindrical samples were prepared in total. First, the samples were dried in a forced convection drying oven (model 101-2B) at 105°C for 48 h. Subsequently, half of the standard specimens were placed in a forced saturator under a vacuum of -0.1 MPa for 48 h to achieve full saturation (ASTM, D4543-08 2008). To avoid moisture exchange between samples and the environment, all the fully dried samples were sealed in plastic bags and fully saturated samples were wrapped by plastic films before the test. The preparation procedure of cylindrical sandstone samples and powder are shown in Figure 1.

## 2.2 Petrographic analysis

Several fragments from fresh sandstone blocks were ground into powders by using an angle grinder (<45 um). Powders were dried in a heating oven at 105°C for 48 h, and used to analyze the minerals by a TTR III X-ray diffraction (XRD). The mineral composition was quantified according to the standard SY/T 5163-2018 (2018).

## 2.3 Physico-mechanical tests

Porosities of these sandstone samples were measured by using the vacuum saturation method. First, the drying mass was tested by using a high-precision electronic balance with an accuracy of 0.01 g. When these samples were completely saturated in a forced saturator, masses of them were measured again. Then the porosity can be calculated as follows:

$$n = \frac{M^{sa} - M^d}{\rho_w V_s} \times 100\% \tag{1}$$

In Equation 1  $n$  (%) is the porosity of rock,  $M^{sa}$  is the mass of completely saturated sample,  $M^d$  is the mass of completely dry sample, and  $V_s$  is the volume of standard sample.

After deriving the porosity, the dry density of rock can be calculated by Equation 2 as below:

$$\rho^d = \frac{M^d}{V_s} \tag{2}$$

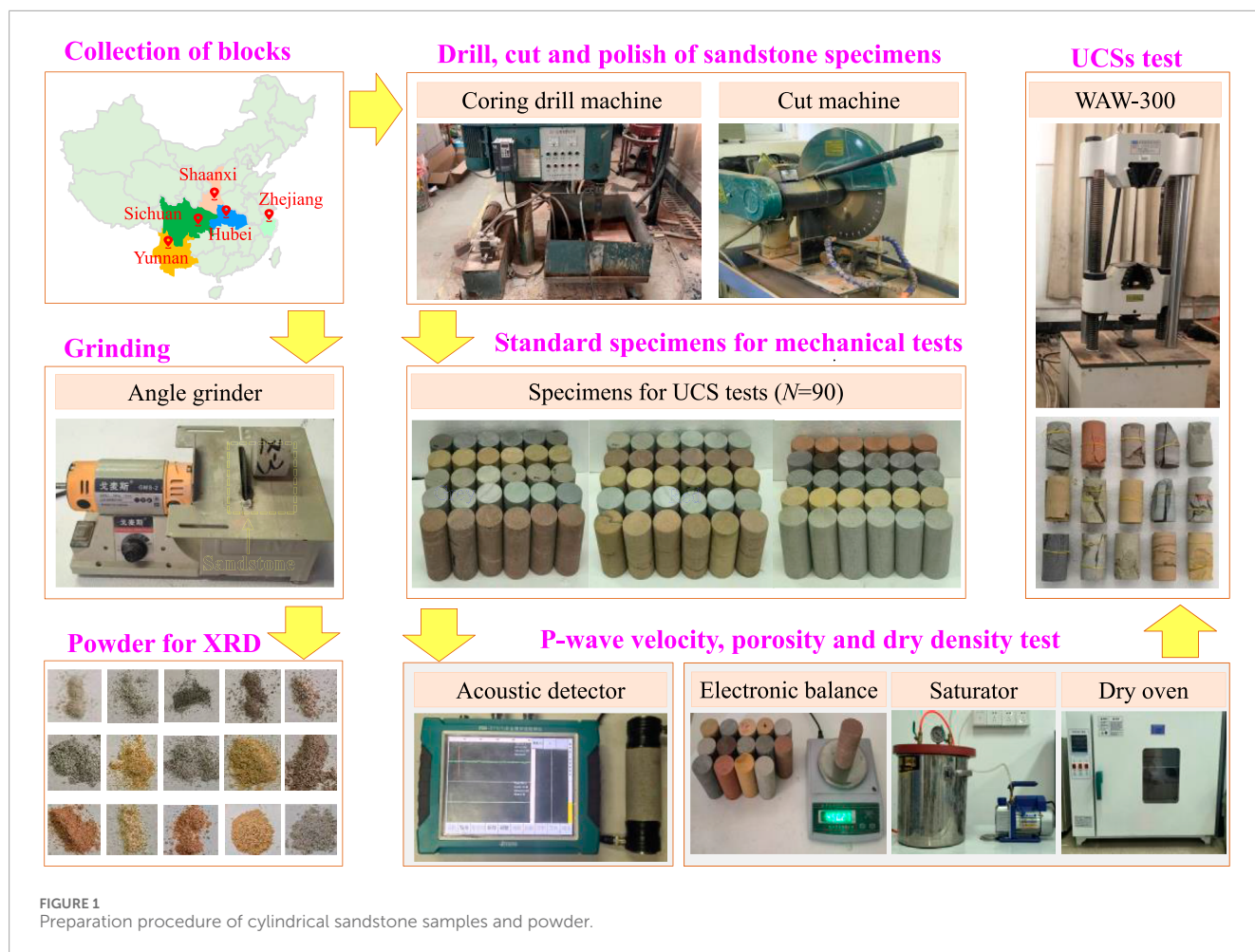
P-wave velocities at the completely dry and saturated conditions were also monitored by using a non-metallic acoustic detector (RSM-SY5T). The transmitters and receivers at both ends of the standard sandstone sample need to be interchanged and the average value was adopted in order to reduce the measurement error.

The UCS of these sandstones were tested after measuring the porosity and P-wave velocity. The UCS tests were performed on an electro-hydraulic servo-mechanical machine (WAW-300) with a loading rate of 0.24 mm/min according to the method recommended by ASTM D7012-10 (2010). The test machine and samples for UCS can be observed in Figure 1.

## 3 Experimental results

### 3.1 Petrographic characteristics

Mineral components of these sandstones were quantified by the XRD method. In addition, the particle size and their cemented structure were captured by using a 3D color optical microscope (Keyence, VHX-5000). These sandstones were divided into several geological types, according to the famous classification method based on the quartz-feldspar-rock fragments triangle as listed in Table 2 (Folk, 1968; Garzanti, 2019). It is evident that YB and SG are feldspatho-lithic sandstones, which have the debris contents more than feldspar. YR, YG, ZhP, ZhL, ShR, ZhG, HR and ShG are litho-feldspathic sandstones with more feldspar. YY, ShY and SW are the lithic quartz sandstones with quartz more than 75%. SB is the typical quartz sandstone with quartz more than 95%. SY is the feldspathic sandstone, because the ratio of feldspar to the debris is larger than 3:1. All of these sandstones contain some clay minerals, mainly including illite and chlorite. The quartz contents are from 28.4% to 95.4%, and the total clay mineral contents of these sandstones



are from 4.6% to 21.1%. Moreover, the red sandstone from Yunnan province (YR) has 4% montmorillonite. It should be noted that the montmorillonite is a kind of high expansion clay minerals. Above all, these 15 sandstones are representative and cover the general range of typical clay-bearing sandstones.

### 3.2 Physico-mechanical properties

Basic physico-mechanical properties of these sandstones are derived and listed in Table 3. Both the high porous sandstone and intact sandstone are used, which have porosities from 0.52% to 19.46%. The P-wave velocities of these sandstones at the dry state vary from 1,381 m/s to 4,787 m/s. At the saturated state, they have a significant increment ratio from 1.4% to 46.2%. After completely saturated, the largest increment is 46.2% for the YB and the smallest increment is only 1.4% for the HR (Figure 2A). The P-wave velocity of water is approximately 1,400 m/s, which is much larger than that of air (Williams, 1996). Therefore, when voids are occupied by the liquid water, the P-wave velocity of the porous sandstone will be improved. In addition, both of dry and saturated P-wave velocities display a reduction trend with increasing the porosity for these sandstones, however, the increment ratio of P-wave velocity

from dry to saturated conditions against the initial porosity is not remarkable.

Figure 2B shows that the mean UCS of these sandstones decreases rapidly from dry to fully saturated state due to the water weakening effect. The largest reduction is 64.4% for the SY and the smallest decrease is approximately 14.7% for the ZhL. The reduction ratio of UCS does not have a stable correlation with the porosity. Generally, a larger porosity implies more water will be absorbed into rocks and thus a greater water weakening damage occurs. However, not only the water absorption ability but also the mineral composition may influence the water weakening degree. Therefore, the relationship between the water weakening coefficient and potential influencing physical parameters should be investigated and built.

The saturated water weakening coefficient of sandstone is defined as follows:

$$K_p = \frac{\sigma_c^{sa}}{\sigma_c^d} \quad (3)$$

Where  $\sigma_c^{sa}$ - UCS of saturated sandstones,  $\sigma_c^d$ - UCS of dry sandstones,  $K_p$ -saturated water weakening coefficient.

The actual value of  $K_p$  is from 0 to 1. A smaller value of  $K_p$  represents a larger water weakening damage. The minimum saturated water weakening coefficient is 0.36 for SY and the

TABLE 2 Mineral components of the used sandstones.

Number	Location	Petrographic classification	Qua	Fel	Cal	Dol	Pyr	Others	Clay mineral						
									Kao	Ill	Chl	Mon	I/M	C/M	
YB	Yunnan	Fine-grained feldspatho-lithic sandstone	57.6	9.4	3.8	8.2	0	0	0	12.4	4.4	0	0	4.2	0
YR	Yunnan	Fine-grained litho-feldspathic sandstone	52.6	31.1	5.5	0	0.5	0	0	4.6	1.7	4	0	0	0
YY	Yunnan	Fine-grained lithic quartz sandstone	92.2	0	0	0	0	0	0	2.3	5.5	0	0	0	0
YG	Yunnan	Fine-grained litho-feldspathic sandstone	48.8	33.4	0	0	0.4	0	0	11.5	5.9	0	0	0	0
ZhP	Zhejiang	Fine-grained litho-feldspathic sandstone	41.6	35.6	0	9.4	0.6	0	0	12.8	0	0	0	0	0
ZhG	Zhejiang	Fine-grained Litho-feldspathic sandstone	33.7	34	4.6	0	2.7	5.0	0	8.6	11.4	0	0	0	0
ZhL	Zhejiang	Fine-grained litho-feldspathic sandstone	33.0	35.1	0	0	2.5	10.9	0	0	18.5	0	0	0	0
ShR	Shaanxi	Fine-grained litho-feldspathic sandstone	36.8	44.6	6.2	1.7	0.9	0	0	6.2	0	0	0	3.6	0
ShG	Shaanxi	Medium-grained litho-feldspathic sandstone	48.6	32.7	0	0	0	0	0	4.1	14.6	0	0	0	0
ShY	Shaanxi	Fine-grained lithic quartz sandstone	89.0	0	0	0	0	0	11	0	0	0	0	0	0
SB	Sichuan	Medium-fine-grained quartz sandstone	95.4	0	0	0	0	0	1.56	1.93	0.14	0	0	0.97	0
SY	Sichuan	Fine-grained feldspathic sandstone	28.4	64.6	0	0	0	0	0	0.77	0.28	0	0	0	5.95
SG	Sichuan	Fine-grained feldspatho-lithic sandstone	64.1	10.4	2.5	1.9	0	0	0	12.03	6.12	0	0	2.95	0
SW	Sichuan	Fine-grained lithic quartz sandstone	74.4	6.8	0	4.2	0	0	5.99	5.26	1.61	0	0	1.74	0
HR	Hubei	Medium-fine-grained Litho-feldspathic sandstone	63.2	21.7	1.2	2.3	1.0	0	8.69	0.64	0	0	0	1.27	0

Notes: Qua-Quartz; Fel-Feldspar; Cal-Calcite; Dol-Dolomite; Pyr-Pyrite; Kao-Kaolinite; Ill-Illite; Chl-Chlorite; Mon-Montmorillonite; I/M-Illite and Montmorillonite mixed layer; and C/M-Chlorite and Montmorillonite mixed layer; YB-Yunnan black sandstone; YR-Yunnan red sandstone; YY-Yunnan yellow sandstone; YG-Yunnan grey sandstone; ZhP-Zhejiang purple sandstone; ZhG-Zhejiang green sandstone; ZhL-Zhejiang light green sandstone; ShR-Shaanxi red sandstone; ShG-Shaanxi grey sandstone; ShY-Shaanxi yellow sandstone; SB-Sichuan brown sandstone; SY-Sichuan yellow sandstone; SG-Sichuan grey sandstone; SW-Sichuan white sandstone; HR-Hubei red sandstone.

TABLE 3 The basic physico-mechanical properties of present sandstones.

Type	$\sigma_c^d$ (Mpa)	$\sigma_c^{sa}$ (MPa)	$K_p$	$V_p^d$ (m/s)	$V_p^{sa}$ (m/s)	$\rho^d$ (g/cm <sup>3</sup> )	$n$ (%)	CM (%)
YB	63.96	48.83	0.76	2,659	3,888	2.58	4.93	21
YR	48.57	22.84	0.47	2,532	2,667	2.26	14.96	10.3
YY	74.09	51.63	0.66	2,818	3,031	2.21	16.23	7.8
YG	93.48	66.80	0.66	3,213	3,882	2.49	6.94	17.4
ZhP	149.2	106.3	0.71	3,636	4,305	2.63	2.14	12.8
ZhG	159.53	131.55	0.82	4,082	4,878	2.62	3.87	20
ZhL	201.2	171.62	0.85	4,787	5,120	2.65	0.52	18.5
ShR	49.76	29.42	0.57	2,176	2,225	2.22	16.43	9.8
ShG	44.52	27.50	0.62	2,712	3,046	2.19	17.01	18.7
ShY	47.62	31.78	0.67	2,658	2,985	2.33	12.98	11
SB	46.18	21.02	0.46	1702	2089	2.26	14.81	4.6
SY	32.71	11.64	0.36	1,381	1701	2.1	21.78	7
SG	94.69	47.47	0.50	2,845	3,178	2.57	4.53	21.1
SW	75.15	39.45	0.52	2,740	2,988	2.41	9.07	14.6
HR	63.55	28.75	0.45	2,779	2,817	2.4	12.94	10.6

maximum value is approximately 0.85 for ZhL. In Table 3, porosities of SY and ZhL are 21.78% and 0.52%, respectively. It indicates that the sandstone SY has absorbed more water than ZhL, although the total clay mineral content of ZhL is much larger. In addition, the sandstone YR has 4% expansive montmorillonite as shown in Table 2, which may be another reason for causing the remarkable reduction of UCS after completely saturated. The expansive montmorillonite can induce more serious water weakening damage than the non-expansive clay minerals, therefore, the saturated water weakening coefficient is only 0.47 for YR. It can be concluded that the mineral composition and absorbed water content have remarkable influence on the UCS loss of sandstones.

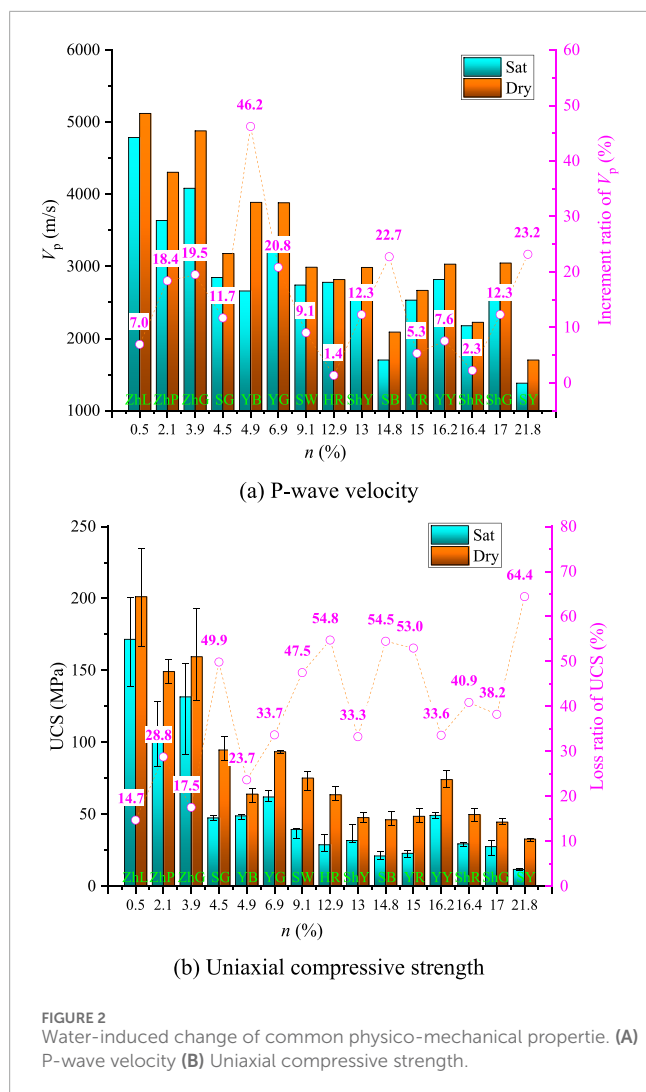
### 3.3 Correlation between the saturated water weakening coefficient with the physical parameter for sandstones

It has been summarized that the P-wave velocity, density, and porosity are usually used to estimate the strength of rocks in Table 1. The relationship between the  $K_p$  and single physical parameter is plotted in Figure 3. Figure 3A shows that  $K_p$  linearly increases with increasing the P-wave velocity, and the determination coefficient is 0.77. This implies that the P-wave velocity is a potential physical parameter to estimate the water weakening coefficient of sandstones. Although the saturated water weakening coefficient also displays a linear increasing trend against the dry density, the discreteness is a

little high and the determination coefficient is only 0.39 (Figure 3B). On the opposite,  $K_p$  linearly decreases with increasing the porosity (Figure 3C). It is evident that the sandstone with a high porosity usually has a low density and P-wave velocity, and more water will be absorbed inside the sandstone. Therefore, the high porosity sandstone will suffer much more serious water weakening, and thus causes a greater reduction of UCS. Figure 3D shows that the water weakening coefficient is positively correlated with the clay mineral content, which seems contrary to the popular expectation. Actually, only the wet clay minerals after absorbing water will cause the reduction of UCS. For instance, the ZhL Sandstone has a clay mineral content of 18.5% but a porosity of only 0.52%. The absorbed water is too low to cause the swelling and hydrolysis of all clay minerals. Therefore, only these water-contained clay minerals will contribute to the reduction of strength. Karakul and Ulusay (2013) proposed the concept of effective clay mineral content ( $E_{cc}$ ) to describe the coupling effect of porosity and clay mineral content on the strength loss of rocks as follows:

$$E_{cc} = n(\%) \times CM(\%) \tag{4}$$

In Equation 4,  $n$  is porosity,  $CM$  is the content of clay mineral. The statistical relationship between  $E_{cc}$  and  $K_p$  for present sandstones is plotted in Figure 3E. Although Figure 3 displays a linear relationship between the initial physical parameter with the water weakening coefficient, determination coefficients are very small. It is illustrated that only one physical parameter is not accurate enough to estimate the water weakening coefficient. Therefore, the multiple



linear regression method may be more suitable to determine the best combination of physical parameters.

## 4 Evaluation of water weakening coefficient by using physical parameters

### 4.1 Saturated water weakening coefficient

To identify the optimal subset of physical parameters for estimating the saturated water weakening coefficient, the multiple linear regression was adopted due to its simplicity, interpretability, ability to handle multiple independent variables, and strong predictive performance. Multiple linear regression analysis was carried out by combining with more experimental data from the previous studies (Table 4). In Table 4, the saturated UCS of sandstones are from 0.69 MPa to 88 MPa, and the clay mineral contents are in the range of 0 ~ 47%. Therefore, these sandstones are representative and cover a wide range from soft to hard ones. The adjusted  $R^2$  and Mallows'  $C_p$  values can be used to evaluate the

degree of correlation and determine the best subset. It is evident that the best fit has the highest adjusted  $R^2$  but the lowest  $C_p$ .

In Equation 5 adjusted  $R^2$  is used to eliminate the effect of independent variable number as below:

$$\hat{R}^2 = 1 - (1 - R^2) \times \frac{m - 1}{m - q - 1} \quad (5)$$

In Equation 6  $\hat{R}^2$  and  $R^2$  are the adjusted and original determination coefficients, respectively.  $m$  and  $q$  are the size of samples and number of independent variables, respectively.

$C_p$  is defined as a criterion for assessing the goodness of fit when comparing models with different parameters. It is defined as follows:

$$C_p = \frac{RSS_p}{\hat{\sigma}^2} + (2q + 2 - m) \quad (6)$$

where  $RSS_p$  represents the residual sum of square error for a model with  $q$  independent variables, and  $\hat{\sigma}^2$  denotes the mean square error based on the full model.

Table 5 was generated using multiple linear regression models constructed in Minitab software. By inputting the data from Table 4, various parameter combinations were selected based on the  $\hat{R}^2$  and  $C_p$ . The optimal multiple linear regression model can be expressed as

$$K_p = \beta_0 + \beta_1 * V_p^{sa} (Km/s) + \beta_2 * CM(\%) \quad (7)$$

In Equation 7  $\beta_0$ ,  $\beta_1$  and  $\beta_2$  are coefficients, which have been listed in Table 6.

Therefore, the final optimal linear evaluation function of the water weakening coefficient for sandstones can be expressed as

$$K_p = 0.134 + 0.168V_p^{sa} (km/s) - 0.536CM(\%) \quad (8)$$

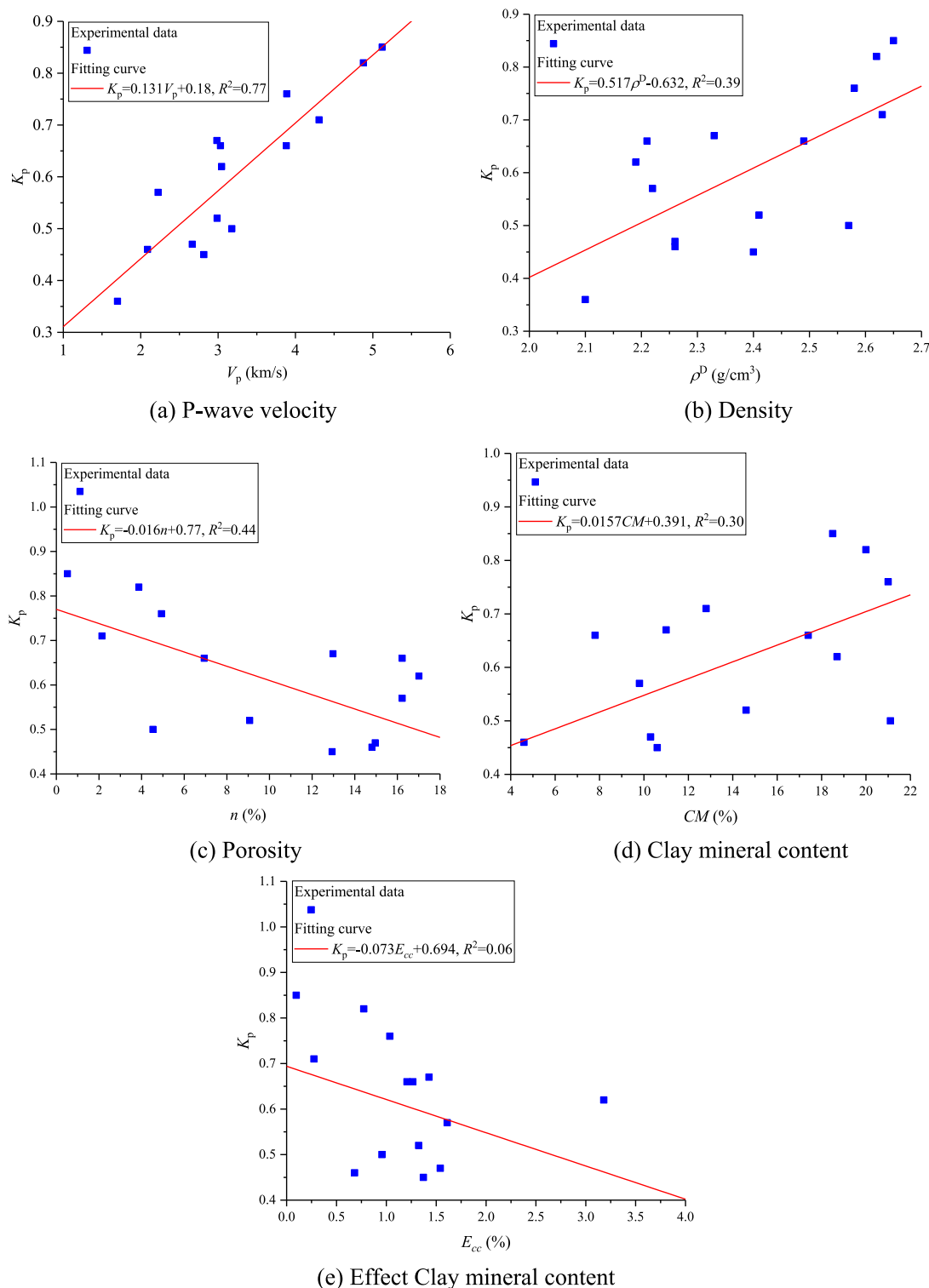
Equation 8 shows the water weakening coefficient of sandstone is proportional to the P-wave velocity and inversely proportional to the content of clay minerals. It means that the clay-bearing sandstone with a small P-wave velocity but high clay mineral content is more sensitive to water. Figure 4 shows that estimated values of  $K_p$  by using Equation 8 are in good agreement with actual measured values of  $K_p$ . The water weakening coefficients of these sandstones range from 0.35 to 0.86, but all evaluation errors are almost less than 20%, therefore, Equation 8 is applicable to estimate the saturated water weakening coefficient of clay-bearing sandstones.

### 4.2 Unsaturated water weakening coefficient

The traditional water weakening coefficient is used to estimate the UCS loss from dry to completely saturated conditions. However, the engineering rock mass may be not fully saturated in the field (Tang, 2018; Masoumi et al., 2017; Liu et al., 2020; Kim et al., 2017). Although some scholars have measured the UCS change of sandstones at different water saturations (Zhou et al., 2016; Jia et al., 2018; Huang et al., 2022b), how to estimate the unsaturated water weakening coefficient by using non-destructive physical parameters is still not clear. Huang et al. (2022c) developed an exponential function for estimating the UCS of sandstones with different water saturations as below:

$$\sigma_c = \frac{\sigma_c^d - \sigma_c^{sa}}{1 - e^{-A}} (e^{-A \cdot S_r} - 1) + \sigma_c^d \quad (9)$$





**FIGURE 3** Correlation of  $K_p$  with the physico-mechanical parameters. (A) P-wave velocity (B) Density (C) Porosity (D) Clay mineral content (E) Effect Clay mineral content.

If only physical parameters are used as the best subset, the unknown parameter  $A$  can be expressed by the porosity and clay mineral content based on the multiple linear regression method as follows (Huang et al., 2022c):

$$A = 0.749 + 6.82n(\%) + 5.69CM(\%) \tag{10}$$

It should be noted that the porosity is adopted in Equation 10 instead of the P-wave velocity, because the P-wave velocity is not

TABLE 4 Common physico-mechanical parameters for sandstones.

No.	$\sigma_c^d$ (Mpa)	$\sigma_c^{sa}$ (Mpa)	$K_p$	$V_p^{sa}$ (m/s)	$\rho^d$ (g/cm <sup>3</sup> )	$n$ (%)	$W_a$ (%)	$CM$ (%)	$E_{cc}$ (%)	References
1	66.75	46.8	0.70	3,141	2.37	9.3	3.46	4	0.37	Zhou et al. (2016)
2	71.91	50.48	0.70	3,615	2.37	8.50	2.29	13.77	1.17	Cai et al. (2019)
3	22.98	9.65	0.42	2,760	2.13	14.20	8.4	33.27	4.72	Karakui and Ulusay (2013)
4	65.40	34.66	0.53	3,540	2.50	3.20	1.26	47.00	1.50	
5	72.88	40.81	0.56	3,620	2.52	4.00	1.56	42.00	1.68	
6	46.99	32.94	0.60	3,167	2.37	8.87	3.5	4.89	0.43	Zhou et al. (2019)
7	32.69	14.04	0.43	2,703	2.32	12.69	5.81	9.91	1.26	Huang et al. (2021)
8	84.82	68.96	0.81	3,558	2.39	5.84	2.44	0.00	0.00	Chen (2011)
9	115.55	40.3	0.35	2,660	2.48	7.50	3.02	27.00	2.03	Zi et al. (2018) Jia et al. (2018)
10	30.11	14.86	0.49	2,331	2.71	12.12	4.47	9.00	1.09	Liao et al. (2019)
11	21.14	8.36	0.40	1864	2.68	13.69	5.11	10.00	1.37	
12	102.3	88.0	0.86	3,908	2.38	5.08	2.13	0.00	0.00	Cai et al. (2020)
13	71.26	46.89	0.66	3,165	2.42	5.59	3.01	0.00	0.00	Weng et al. (2020)
14	30.68	18.76	0.61	3,233	2.53	6.65	2.63	8	0.53	Xie et al. (2022)
15	1.69	0.69	0.41	1799	1.60	36.30	22.69	3.00	1.09	Verstrynge et al. (2014)
16	8.59	4.27	0.50	2,374	1.95	31.70	16.26	2.00	0.63	
17	12.09	7.23	0.60	2,740	1.98	21.70	10.96	2.50	0.54	

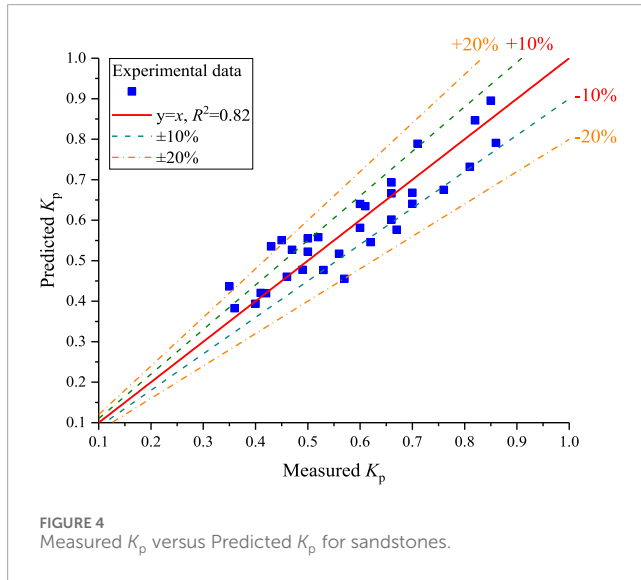
TABLE 5 Results of the best subset regression.

$\hat{R}^2$ (%)	$C_p$	$F$	$p$ -value	$\hat{S}S$	$\hat{M}S$	$V_p^{sa}$ (km/s)	$\rho^D$ (g/cm <sup>3</sup> )	$n$ (%)	$CM$ (%)	$E_{cc}$ (%)
65.9	25.4	61.01	$1.03 \times 10^{-8}$	0.437	0.437	√	--	--	--	--
24.9	89.8	11.25	$2.17 \times 10^{-3}$	0.178	0.178	--	--	√	--	--
<b>82.2</b>	<b>0.9</b>	<b>72.66</b>	<b><math>5.07 \times 10^{-12}</math></b>	<b>0.543</b>	<b>0.272</b>	√	--	--	√	--
72.1	16.3	41.03	$3.51 \times 10^{-9}$	0.481	0.241	√	--	--	--	√
82.0	2.4	47.93	$3.73 \times 10^{-11}$	0.545	0.182	√	√	--	√	--
81.7	2.8	47.17	$4.49 \times 10^{-11}$	0.544	0.181	√	--	--	√	√
81.5	4.1	35.20	$2.39 \times 10^{-10}$	0.547	0.137	√	√	√	√	--
81.3	4.3	34.74	$2.77 \times 10^{-10}$	0.545	0.136	√	√	--	√	√
80.9	6.0	27.19	$1.49 \times 10^{-9}$	0.547	0.109	√	√	√	√	√

Note:  $\hat{S}S$ - Adjusted sum of squared deviation,  $\hat{M}S$ - Adjusted mean squared deviation  $R^2$ . The bold values represent the optimal multiple linear regression models selected based on  $R^2$  and  $C_p$  for various parameter combinations.

TABLE 6 Values of the coefficients from the best subset regression.

$\beta_0$	$\beta_1$	$\beta_2$	$F$	$p$ -value	$\hat{R}^2$
0.134	0.168	-0.536	72.66	0	0.82



provided as the potential optimal parameter due to the lack of enough data in the previous literature (Huang et al., 2022c).

Substituting Equation 3 into Equation 9, yields

$$K_p^u(S_r) = \frac{\sigma_c}{\sigma_c^d} = \frac{1 - K_p}{1 - e^{-A}} (e^{-A \cdot S_r} - 1) + 1 \quad (11)$$

where  $K_p^u(S_r)$  is the water weakening coefficient for rocks with different water saturations, which is called unsaturated water weakening coefficient in this study. When  $S_r=1$ ,  $K_p^u(1) = K_p$  from Equation 11. The saturated water weakening coefficient  $K_p$  can be estimated by Equation 8.

In this study, the UCS of SG, SB, HR and SY sandstones with different water contents were measured, and essential parameters for these sandstones are listed in Table 3. Substituting values of porosity and clay mineral content into Equation 10, A can be derived. Then, the unsaturated water weakening coefficient can be further predicted by substituting the value of A into Equation 11. Figure 5 shows that predicted unsaturated water weakening coefficients are in good agreement with experimental values. They reduce with increasing the water saturation. In Tables 3, 4, it can be found that the UCS of these sandstones range from 11.64 MPa to 47.47 MPa, therefore, the water weakening degrees of soft and medium hard sandstones can be well estimated. The evaluation error of unsaturated water weakening coefficient against the water saturation is plotted in Figure 6. It shows that almost all the predicted errors are smaller than 20%. It should be noted that some evaluation errors may be a little large for some points, because the accurate quantification of some parameters is very hard. For instance, the determination of the clay mineral content by the XRD method is influenced by the analysis experience of the technician. Nevertheless, the quantitative correlation between

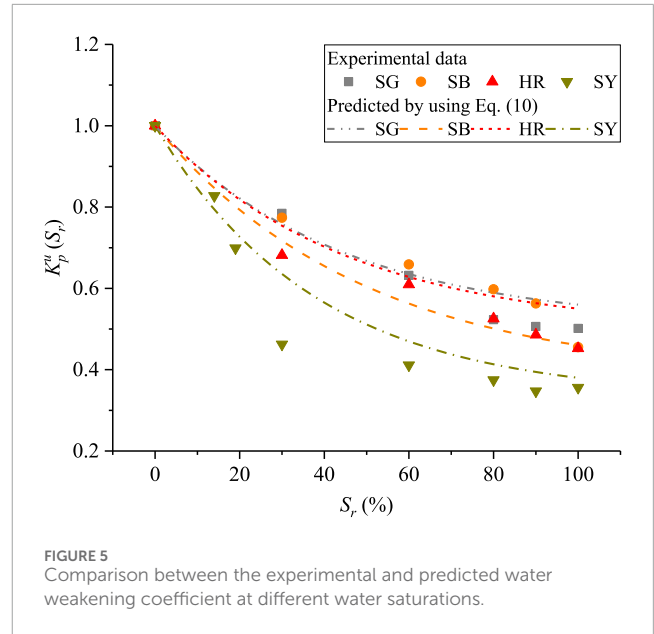


FIGURE 5 Comparison between the experimental and predicted water weakening coefficient at different water saturations.

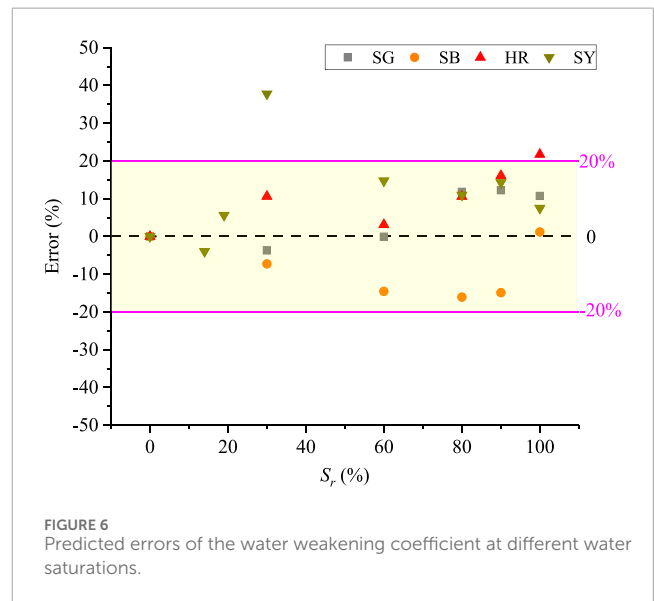


FIGURE 6 Predicted errors of the water weakening coefficient at different water saturations.

unsaturated water weakening coefficients at any water saturation with physical parameters is well built.

## 5 Discussion

### 5.1 Water weakening mechanism of clay minerals by microscopic simulation

It is evidenced that the saturated water weakening coefficient of sandstones can be estimated by using the saturated P-wave velocity and clay mineral content in this study. The weight coefficient for the clay mineral content is approximately -0.536. In Table 3, 4, the maximum clay mineral content is from 0% to 47% for these sandstones. 47% clay mineral content can cause the reduction of

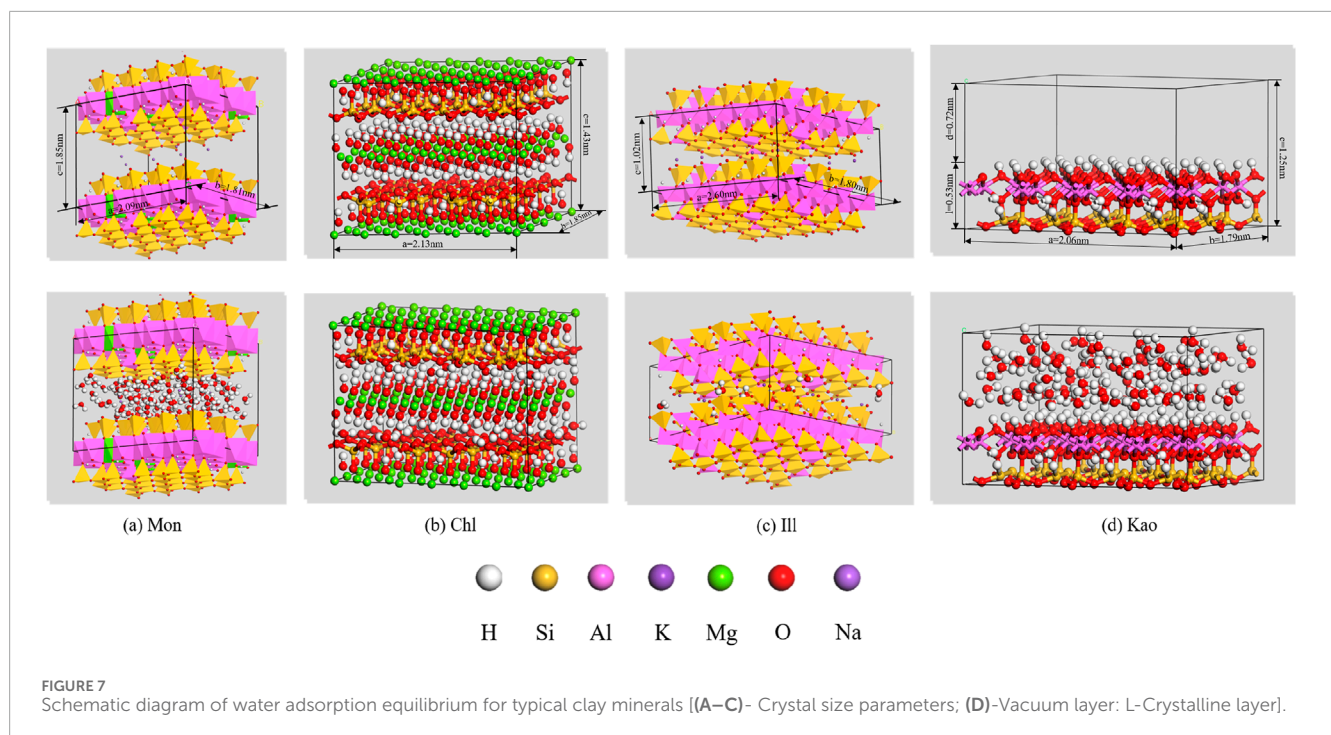


FIGURE 7 Schematic diagram of water adsorption equilibrium for typical clay minerals [(A–C)– Crystal size parameters; (D)–Vacuum layer: L-Crystalline layer].

$K_p$  by 0.25 from Equation 8. It illustrates that the presence of clay minerals is an important factor influencing the water weakening degree of sandstones. Although the statistical relationship between the strength loss and physical parameters already confirmed the critical role of clay minerals, the water weakening mechanism of different clay minerals in sandstones are not fully understood. The crystalline layer dissolution of clay minerals induced by water is in a nano-scale (layer spacing  $\leq 2$  nm), therefore, the existing measurement method is difficult to describe the swelling behavior in such a small spacing range (Pradhan et al., 2015). The molecular dynamics (MD) simulation method may be a suitable tool to investigate the hydration process of clay minerals, because it can explain the changes in lattice spacing and mechanical properties of clay minerals at a microscopic level after water absorption, and it also quantitatively helps us understand the swelling and softening mechanism of clay minerals when encountering water (Zhang et al., 2018; Ren et al., 2022). The response of mechanical strengths of crystals during the hydration process also can be analyzed to gain insight into the micro-kinetic mechanism of clay hydration.

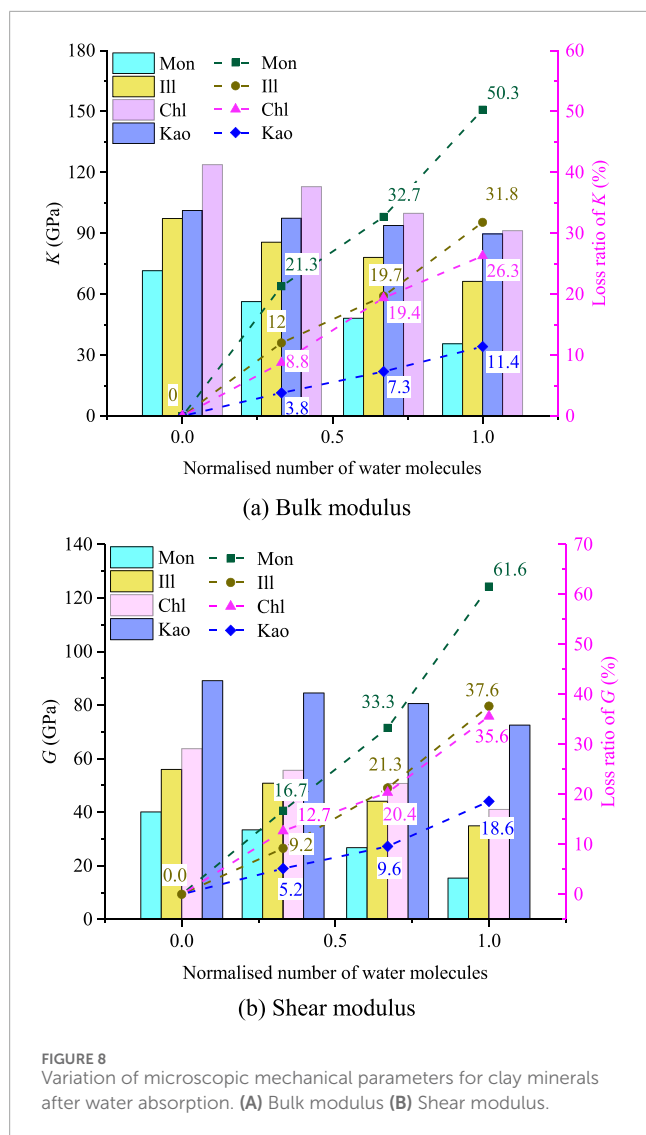
### 5.1.1 Construction of the molecular model

In order to simulate the water hydration process of typical clay minerals (montmorillonite, illite, kaolinite and chlorite), the specific parameters for molecular modelling are referred to Skipper et al. (1995), Drits et al. (2010), Bish (1993), and Joswig et al. (1989), respectively. In this study, water molecules are represented by the SPC/E water model (Berendsen et al., 1987). Some typical equilibrium diagrams containing clay molecule and adsorption water molecule are given in Figure 7. The bulk and shear module of clay mineral crystals after geometric optimization are calculated by the Forcite module.

### 5.1.2 Simulation results

By simulation, it is evidenced that the maximum number of water molecules absorbed inside the molecular interlayer are 96, 30, 12, and 0 for the montmorillonite, chlorite, illite and kaolinite, respectively. Therefore, the water adsorption capacity in different clay minerals decreases as the following order: montmorillonite > chlorite > illite > kaolinite. As shown in Figure 7, water molecules in the kaolinite structure are mostly concentrated in the vacuum layer, while only a small amount of water molecules are adsorbed on the surface of the crystal layer and no water molecule can enter into the kaolinite crystal. Therefore, the water weakening of kaolinite is only caused by the surface hydration, which is different from the other clay minerals. Liu et al. (2021) suggested that the radius of the silica-oxygen tetrahedral ring for illite was similar to the hydration radius of  $K^+$ , which usually occurs on the surface of the crystal. When  $K^+$  adsorbs a certain amount of water molecules, it can be firmly embedded in the pores of illite crystals. The illite has a relative smaller ability to absorb water molecules into illite crystals than the montmorillonite, which effectively reduces the degradation effect of hydration in illite.

Figure 8 shows that both of the microscopic bulk modulus ( $K$ ) and shear modulus ( $G$ ) for different clay minerals show a decreasing trend with the increasing of absorbed water molecules. The reduction ratios of the mineral moduli are montmorillonite > illite > chlorite > kaolinite. The montmorillonite has the largest reduction ratio of microscopic modulus, because it belongs to the expansive clay mineral, in which most of the water molecules will be absorbed inside the molecular interlayer. The expansive ratio is more than 20 times for the sodium montmorillonite. As a result, the microscopic bulk modulus and shear modulus have reduced by more than 50.3% and 61.6% after reaching the maximum water content, respectively. The reduction of mineral modulus of the kaolinite is the smallest, because the interlayer of molecules is too narrow to absorb



water molecules. The reduction ratio in mechanical parameters during the hydration of clay crystals almost is consistent with the macroscopic water absorption of clay minerals. The reduction ratios of mineral moduli for illite and chlorite are very close.

In Table 3, the first seven sandstones with the fastest reduction rate of water weakening coefficient are: SY>HR>SB>YR>SG>SW>ShR. All of these sandstones contain some montmorillonite (I/M or C/M) as shown in Table 2. However, the montmorillonite and its mixed layer are absent for almost all the other sandstones, which have higher water weakening coefficients. It further illustrates that the presence of montmorillonite can induce a much more water weakening degree and thus result in a greater reduction of UCS. It should be noted that the YB sandstone has 4.2% I/M but a high water weakening coefficient of 0.76. There may be two reasons for the low water weakening degree of YB. First, the porosity of YB is only 4.93%, therefore, only a little water will be absorbed into YB. In addition, the montmorillonite only occupies 5% of the total I/M mixed layer. It also illustrates that the montmorillonite plays a much more important role in the water weakening degree of sandstones.

## 5.2 Effect of the P- wave velocity

It is evidenced that the porous sandstone can absorb more water than intact sandstones at the completely saturated condition, because voids provide space for liquid water, and increase the contact area between liquid water and mineral particles, particularly the clay minerals. In Section 4.1, the P-wave velocity, instead of the porosity, is automatically selected as one parameter in the best subset by the linear regression method, which may be caused by two reasons:

First, P-wave velocity has a strong linear relationship with the porosity of sandstone. Figure 9 shows that the porosity linearly decreases with increasing saturated P-wave velocity for sandstones. In addition, the pore structure is very complex and the porosity cannot characterize the pore size distribution (Huang and Yu, 2022). It illustrates that the P-wave velocity may be a better parameter to reflect the compactness and water absorption ability of rocks than the porosity. Secondly, the P-wave velocity of porous rocks can reflect the mineral composition which has been interpreted in typical geo-acoustic models (Ji et al., 2003; Lyu et al., 2020). The mineral modulus and P-wave velocity of the main minerals in sandstones are listed in Table 7. The clay mineral and quartz are more sensitive to water, but they have much smaller P-wave velocities. Therefore, they can cause more serious damage in rocks after contacting with water. In addition, the cementation strength among the mineral particles also has a remarkable influence on the P-wave velocity of the rock matrix (Dvorkin et al., 1994; Jarrard et al., 2000). A weak cementation of mineral particles will cause the reduction of P-wave velocity and more water may be absorbed into the matrix to attack minerals. Actually, the P-wave velocity has a significant correlation with UCS as show in Figure 9. The sandstone with a higher P-wave velocity usually has a larger saturated UCS. Above all, the P-wave velocity may be a more comprehensive parameter to quantify the water weakening degree than the porosity.

## 5.3 Limitations of sandstones in this study

In this study, we selected 15 sandstone samples to represent a broad range of typical sandstones containing clay minerals. The quartz content of these sandstones ranges from 28.4% to 95.4%, while the total clay mineral content ranges from 4.6% to 21.1%. Additionally, these sandstones vary widely in hardness, including feldspathic litharenite, lithic quartz sandstone, and typical quartz sandstone. Therefore, these samples are somewhat representative, particularly for studying the impact of clay mineral content on sandstone mechanical properties.

Although it is widely accepted that clay mineral content can cause the mechanical weakening of rocks when in contact with water, the influence of specific clay mineral compositions remains underexplored (Cherblanc et al., 2016). Furthermore, the representativeness of these samples on a global scale is limited. Firstly, the clay minerals commonly found in Chinese sandstones include kaolinite, montmorillonite, illite, chlorite, and a small amount of randomly interstratified clays (Liu et al., 2003). In contrast, the clay mineral compositions of sandstones abroad exhibit greater diversity. For example, North American sandstones often

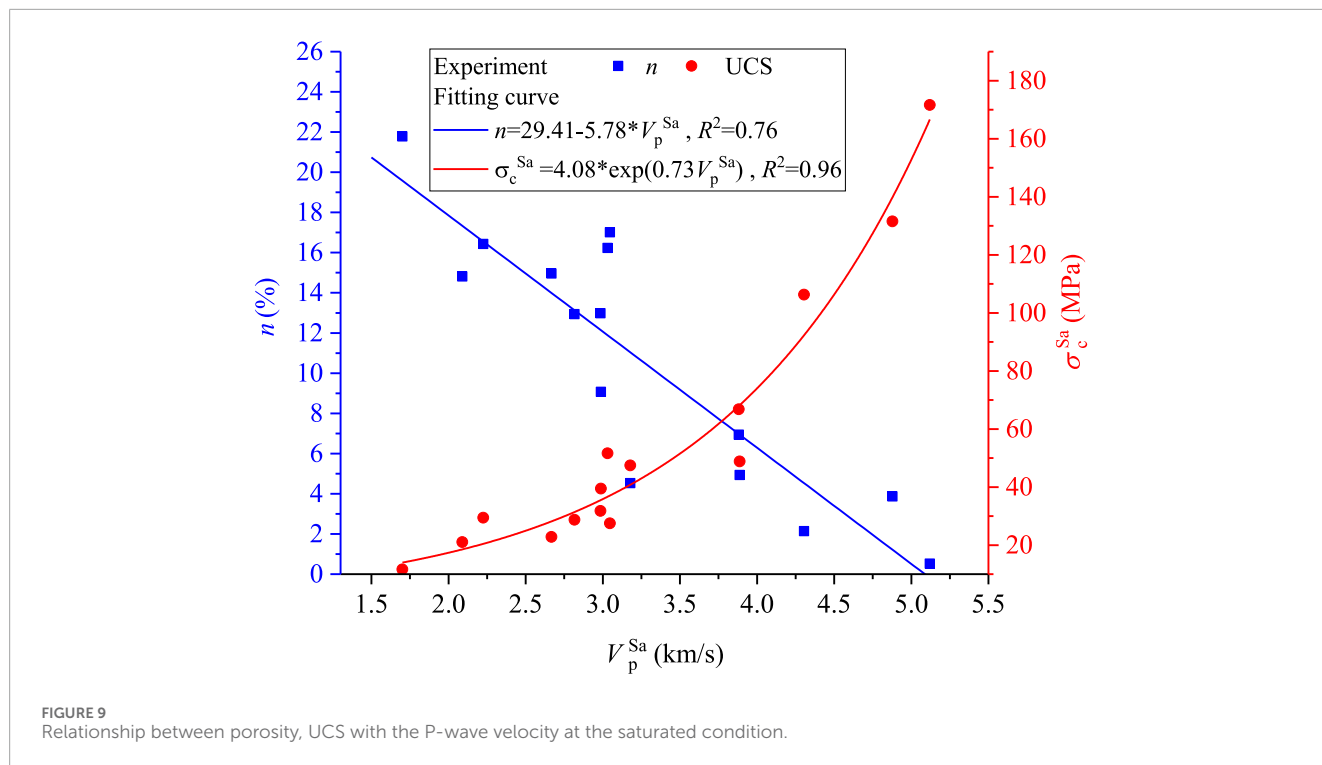


FIGURE 9 Relationship between porosity, UCS with the P-wave velocity at the saturated condition.

TABLE 7 The modulus and P-wave velocity of main minerals for sandstones.

Mineral	$K$ (GPa)	$G$ (GPa)	$\rho^d$ (g/cm <sup>3</sup> )	$V_p^m$ (m/s)	References
Dolomite	84.98	53.88	2.87	7,392	Yan et al. (2022)
Calcite	76.02	36.80	2.71	6,791	Ji et al. (2003)
K-feldspar	62.66	31.85	2.56	6,408	
Plagioclase (An9)	57.53	32.70	2.61	6,225	
Plagioclase (An53)	73.83	35.82	2.68	6,736	
Quartz	38.12	47.60	2.655	6,194	Chand et al. (2004)
Clay	20.90	6.85	2.58	3,412	

contain significant amounts of bentonite. The bentonite is a kind of swelling clay primarily composed of montmorillonite with excellent water absorption and plasticity, therefore, it provides unique industrial applications (Thair and Olli, 2008). These compositional differences result in notable variations in the chemical properties, adsorption capacity, and stability of clay minerals, therefore, the water weakening process by considering the composition of international clay minerals should be further investigated.

Secondly, the genesis of sandstones is closely related to their depositional environment. Chinese sandstones primarily form in river and delta environments, reflecting relatively stable sedimentary processes (Liu et al., 2003). In contrast, sandstones abroad, such as those in North America and Western Europe, are often derived from volcanic or glacial sediments, leading to significantly

different physical and chemical properties compared to Chinese sandstones (Thair and Olli, 2008). These genesis differences may cause variations in water weakening of sandstone.

Furthermore, there are significant differences in sedimentary structures between Chinese and foreign sandstones. China, located at the junction of several tectonic plates with frequent seismic activity, often exhibits seismic sedimentary structures in sandstone research. In regions with less seismic activity, such structures may be less prominent (Feng et al., 2016). Chinese sandstones typically show good sorting, meaning the grain size distribution is relatively uniform. This characteristic is common in river and lake sedimentary environments and helps sandstones remain stable during weathering and erosion. In contrast, sandstones from volcanic or glacial environments abroad may exhibit poorer sorting

and uneven grain size distribution (Collinson and Mountney, 2019). For example, in the Middle East, due to an arid climate and intense sedimentary processes, sandstones often have coarser layering and poorer sorting (Glennie, 2010). These structural differences can significantly impact sandstone stability and durability under various conditions and present challenges for cross-regional applications.

Currently, the sandstone samples used in our research mainly come from specific regions in China, making the results more applicable to Chinese sandstone characteristics. The international applicability of these findings still needs further validation. Differences in geological backgrounds, climate conditions, and sandstone formation processes across regions may lead to significant variations in physical, chemical, and mechanical properties. To address this limitation, future research will expand to other regions, exploring the performance of different sandstones in various applications and conducting a comparative analysis of the advantages and disadvantages of Chinese versus foreign sandstones in specific applications.

## 6 Conclusion

Based on this research, the following conclusions can be obtained.

- (1) The water weakening coefficient is an important index to evaluate the water weakening degree. It is time-saving and economic to estimate this critical coefficient by using non-destructive physical parameters. Although there is a certain statistical correlation between the saturated water weakening coefficient with the P-wave velocity, porosity, density and effective clay mineral content, only one physical parameter is not adequate to estimate the saturated water weakening coefficient.
- (2) The P-wave velocity and clay mineral content are automatically selected as the best subset to estimate the saturated water weakening coefficient by the linear regression method, in which the adjust  $R^2$  is 82%. The estimation errors are almost less than 20% for these 32 sandstones. Therefore, the equation we proposed (Equation 8) is applicable for estimating the saturation water weakening coefficient of clay-containing sandstone. Based on this, we believe that our findings are also applicable to other clay-containing sandstones.
- (3) It has been proved that clay minerals are seriously damaged after absorbing water by using the molecular dynamics (MD) simulation method, therefore, they should be responsible for the UCS loss of sandstones when contacting with water. The montmorillonite plays a much more important role in the water weakening degree of sandstones than the other clay minerals. In addition, the P-wave velocity may be a more comprehensive index to quantify the water weakening degree than porosity, because it can comprehensively reflect the effect of the pore volume, the cementation of mineral particles and their components.
- (4) The unsaturated water weakening coefficient at different water saturations are estimated by using the common physical

parameters based on an exponential strength function. The decreasing rate of unsaturated water weakening coefficient is dependent of the porosity and clay minerals. The water weakening coefficient of the sandstone with a large porosity and more clay minerals decreases more quickly against the water saturation.

## Data availability statement

The original contributions presented in the study are included in the article/supplementary material, further inquiries can be directed to the corresponding author.

## Author contributions

JX: Data curation, Investigation, Resources, Validation, Writing–original draft, Writing–review and editing. SH: Conceptualization, Data curation, Formal Analysis, Funding acquisition, Investigation, Methodology, Resources, Validation, Visualization, Writing–original draft, Writing–review and editing. SY: Data curation, Validation, Writing–original draft. SZ: Data curation, Project administration, Resources, Writing–original draft. JS: Conceptualization, Data curation, Methodology, Project administration, Writing–original draft.

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## Conflict of interest

The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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## Glossary

$\sigma_c^d$	Dry uniaxial compressive strength
$\sigma_c^{sa}$	Saturation uniaxial compressive strength
$\sigma_c$	Uniaxial compressive strength
$V_p^d$	P-wave velocity at the dry condition
$V_p^{sa}$	P-wave velocity at the saturated condition
$V_p$	P-wave velocity of the rock
$V_p^m$	P-wave velocity of the minerals
$V_s$	Volume of the standard sample
$\rho^d$	Dry density of rocks
$\rho^{sa}$	Saturation density of rocks
$\rho_w$	Density of water
$n$	Porosity of rock
$N$	Number of samples
$W_a$	Water content
$CM$	Clay mineral content
$S_r$	Water saturation
$M^{sa}$	Mass of completely saturated samples
$M^d$	Mass of dry samples
$K_p$	Saturated water weakening coefficient
$K_p^u(S_r)$	Water weakening coefficient for rocks with the water saturation of $S_r$
$E_{cc}$	Effective clay mineral content
$K$	Bulk modulus
$G$	Shear modulus
$A$	Fitting parameters
$\hat{R}^2, R^2$	The adjusted and original determination coefficients, respectively
$m, q$	The sample size and number of independent variables, respectively
$\beta_0, \beta_1, \text{ and } \beta_2$	Undetermined coefficients
$RSS_p$	The residual sum of square error
$\hat{\sigma}^2$	Mean square error
AAR	Average annual rainfall
$\hat{S}MS$	Adjusted sum of squared deviation and adjusted mean squared deviation