



# Analysis of Energy Evolution Characteristics of Salt Rock Under Different Loading Rates

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The existing uniaxial compression test results of salt rock under different loading rates are used to study its energy evolution characteristics during deformation and failure in this study. First of all, the influence of loading rate on the total energy density, elastic energy density, and dissipated energy density is analyzed. Afterward, the relationship between the number and size of fragments, crushing intensity after rock destruction, and energy density of each part is discussed. The results show that the energy evolution process of salt rock during deformation and failure contains three stages, namely, energy accumulation stage, energy dissipation stage, and energy release stage. With the increase in loading rate, the total energy density and dissipated energy density gradually decrease, whereas the elastic energy density increases. When the volume of rock remains constant, the greater the dissipated strain energy, the more the number of fragments will be produced after rock failure. When the dissipated strain energy remains unchanged, the larger the dissipated strain energy (surface free energy) is, the smaller the number and the larger the size of fragments will be produced. When the total strain energy is constant, the splash rate of the fragments increases with increasing elastic strain energy ratio.

**Keywords:** salt rock, energy evolution, loading rate, rock fragment, crushing intensity

## INTRODUCTION

The deformation and failure process of rock under external loads is the generation and development process of new cracks. The generation of new cracks will absorb energy from the external environment, and the propagation and penetration process of cracks will consume energy. Namely, the process of rock deformation and failure is a process of energy accumulation and dissipation (Wang and Cui, 2018; Chen Z. et al., 2019; Wang et al., 2021a; Fan et al., 2022; Wang Y. et al., 2022). Therefore, studying the deformation and failure process of rocks from the perspective of energy is closer to its failure essence, and it is of great significance to reveal the mechanisms of rock failure and rock (body) engineering disasters (Carpinteri et al., 2004; Deng et al., 2016; He et al., 2018; Gong et al., 2021; Wang et al., 2021b; Wang et al., 2022b).

The deformation and failure of rocks under external load is the inevitable result of energy driving (Liu et al., 2019; Wang Y. et al., 2020; Li et al., 2021). Studying the deformation and failure process of rocks from the perspective of energy has always been a hot issue in the field of rock mechanics (Yang et al., 2019; Zhao et al., 2020; Li et al., 2022; Wang X. Y. et al., 2022; Zhang et al., 2022). Meng et al. (2019) carried out uniaxial cyclic loading tests on yellow sandstone, limestone, and marble under different loading rates, and analyzed the influence of loading rate on energy evolution during rock deformation and failure. Zhang and Gao (2015) analyzed the influence of water on energy evolution

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and distribution of sandstone based on the uniaxial cyclic loading and unloading test results. He et al. (2020) studied the evolution characteristics of the total energy, elastic energy, and dissipated energy for the fifteen rocks and then proposed a new method to determine the strength of rock using the dissipation energy coefficients. Gong et al. (2019) studied the relationship between total input energy and elastic strain energy under different unloading stress levels and proposed a new basis for judging rockburst tendency. Song et al. (2020) analyzed the influence law of loading mode on deformation characteristics, failure form, and energy evolution characteristics of the coal-rock combination. Wang et al. (2021c) and Yang D. et al. (2020) studied the energy evolution characteristics of rocks during fatigue deformation and pointed out that with the increase of load cycles, the elastic strain energy gradually increased, while the dissipated strain energy gradually decreased. Cao et al. (2020) studied the variation law of total strain energy, elastic strain energy, dissipated strain energy, and infrared radiation temperature of saturated sandstone under stress by using infrared thermal imaging technology. Zhang J. et al. (2021) studied the influence of joint inclination on the energy evolution characteristics of rock, the results showed that the total energy, elastic strain energy, and dissipated strain energy at the peak stress of rock first decreased and then increased with the increase of joint inclination. Zhang et al. (2017) studied the influence of confining pressure on the energy accumulation and dissipation of rocks and pointed out that confining pressure can promote energy input and accumulation and inhibit energy release. Huang and Li (2014) analyzed the influence of initial confining pressure and unloading rate on rock energy conversion and its failure characteristics based on the results of the triaxial cyclic loading test. Zhang et al. (2019) studied the energy evolution processes and mechanisms among three hard rocks using a strain energy analysis method under true triaxial compression. The results showed that the difference in the elastic and plastic deformation capacities, which influence the energy difference in different rocks, is influenced by the mineral compositions and microstructures of the different rocks when the external conditions are not considered. As aforementioned, a large number of research studies have been performed to examine the energy evolution characteristics of rocks under various experimental conditions for the past several years. However, there are only a few studies on the influence of loading rate on the energy evolution characteristics of salt rock.

The long-term operation process of salt cavern gas storage includes four stages: gas injection and pressurization, high-pressure operation, gas production, and depressurization, and low-pressure operation (Fan et al., 2019; Fan et al., 2020; Zhou et al., 2022). In the stage of gas production and depressurization stage, the pressure of the gas storage gradually decreases, and the unbalanced force of the surrounding rock gradually increases (Liu et al., 2020a; Wang et al., 2021d; Zhang X. et al., 2021; Wang et al., 2022d). With different gas recovery rates, the loading rates on the surrounding rock are also different. The energy evolution characteristics of salt rock under different loading rates exhibit some variation. Therefore, it is of great significance to study the energy evolution characteristics of salt rock under different

loading rates to ensure the safety and stability of the salt cavern gas storage (Liu et al., 2020b; Wang J. et al., 2020; Kang et al., 2021; Wang et al., 2021e; Wang X. et al., 2022).

To study the influence of loading rate on the energy evolution characteristics of salt rock during deformation and failure, the total energy density, elastic energy, and dissipated energy density are calculated using the existing test results mentioned in this study. Based on the calculation results, the relationship between the energy density of each part and the loading rate is studied. Then, the relationship between the number and size of fragments after deformation and failure, crushing intensity, and energy is discussed. The results can provide some theoretical guidance for the long-term stability analysis of salt cavern gas storage.

## ENERGY CALCULATION METHOD

According to the knowledge of thermodynamics, it is known that any physical process is the process of mutual conversion between various energies, such as mechanical energy and thermal energy, etc. Hence, the instability failure of an object under external loads is the inevitable result of energy driving. The whole process of deformation and failure of rock under external loads, such as compression density, elastic deformation, inelastic deformation, and post-peak damage stages is accompanied by the mutual conversion between various parts of energy. Therefore, it is conducive to understand the intrinsic mechanism of rock deformation and damage under external loads when thermodynamic knowledge is used to study the energy evolution process (Zhang et al., 2019).

Under the uniaxial or triaxial compression condition, the work done (total input energy) by the testing machine on the rock mainly includes three forms (as shown in **Figure 1**): 1) A part of the energy is stored inside the rock in the form of elastic strain energy, which can be released after unloading. Therefore, the elastic strain energy is reversible. 2) A part of the energy is mainly used for the closure of the original microcracks inside the rock, and the generation and development of new cracks. This part of energy is commonly called dissipated strain energy, which is irreversible. 3) A small part of the energy is released to the external environment in the form of heat and radiation energy (e.g., acoustic emission, infrared radiation, and electromagnetic radiation) due to the internal cracks, structural surfaces, and friction between mineral particles, which is also irreversible (Yang L. et al., 2020; Zhou et al., 2020).

The energy evolution process of rocks under external loads mainly undergoes three stages (as shown in **Figure 2**): namely, energy accumulation stage, energy dissipation stage, and energy release stage. 1) Energy accumulation stage: at the beginning of loading, the absorbed energy is mainly stored in the rock in the form of elastic strain energy, and only a small amount of energy is used to close the original defects inside the rock. Therefore, this stage is a process of energy accumulation. 2) Energy dissipation stage: after the external loads exceeds the yield stress of the rock, most of the absorbed energy is used for the nucleation, expansion, and penetration of microcracks, and only a small part of the absorbed energy is stored in the rock. Namely, the energy accumulation process also exists in this stage. However, the

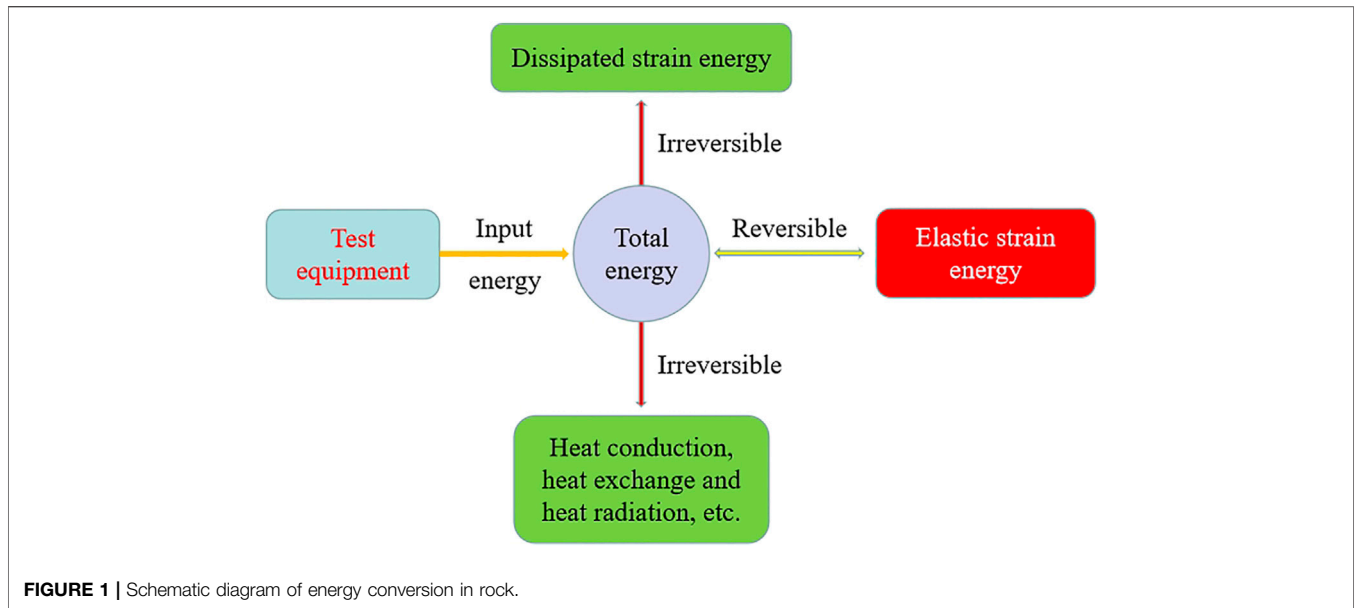


FIGURE 1 | Schematic diagram of energy conversion in rock.

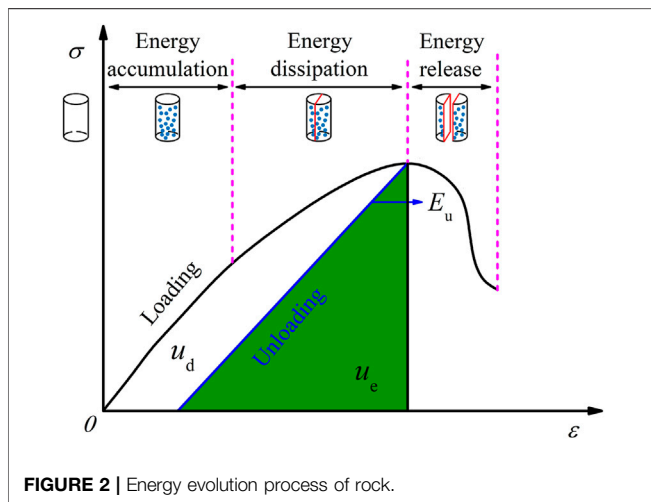


FIGURE 2 | Energy evolution process of rock.

accumulated energy in this stage accounts for only a small proportion of the total absorbed energy, which can be ignored. Hence, this stage can be considered a process of energy dissipation. 3) Energy release stage: when the absorbed energy is sufficient to overcome the frictional effect of the critical failure surface, the rock is destabilized, and the energy stored in the rock is released to the outside in the form of kinetic energy (Li et al., 2017; Zhang L. et al., 2021).

Assuming that no heat exchange occurs between the interior of the rock and the external environment during the entire loading process that is, the testing machine and the rock are considered to be a closed system. Then, according to the first law of thermodynamics, the work done by the testing machine on the rock can be expressed as (Wang C. L. et al., 2020):

$$U = U_e + U_d + U_h. \tag{1}$$

Here,  $U$  is the stored energy of rock (total input energy), in mJ;  $U_e$  is the elastic strain energy, in mJ;  $U_d$  is the dissipated strain energy, in mJ;  $U_h$  is the energy consumed in the form of heat conduction, heat exchange, and heat radiation, etc. in mJ.

In Eq. 1,  $U_h$  accounts for a relatively small proportion of  $U$ , and can be ignored (Chen X. et al., 2019). Consequently, we can get:

$$U = U_e + U_d. \tag{2}$$

For a rock mass unit, the energy evolution characteristics of rock under external loads are commonly characterized by energy density. Therefore, Eq. 3 is obtained according to Eq. 2, namely (Meng et al., 2016),

$$u = u_e + u_d, \tag{3}$$

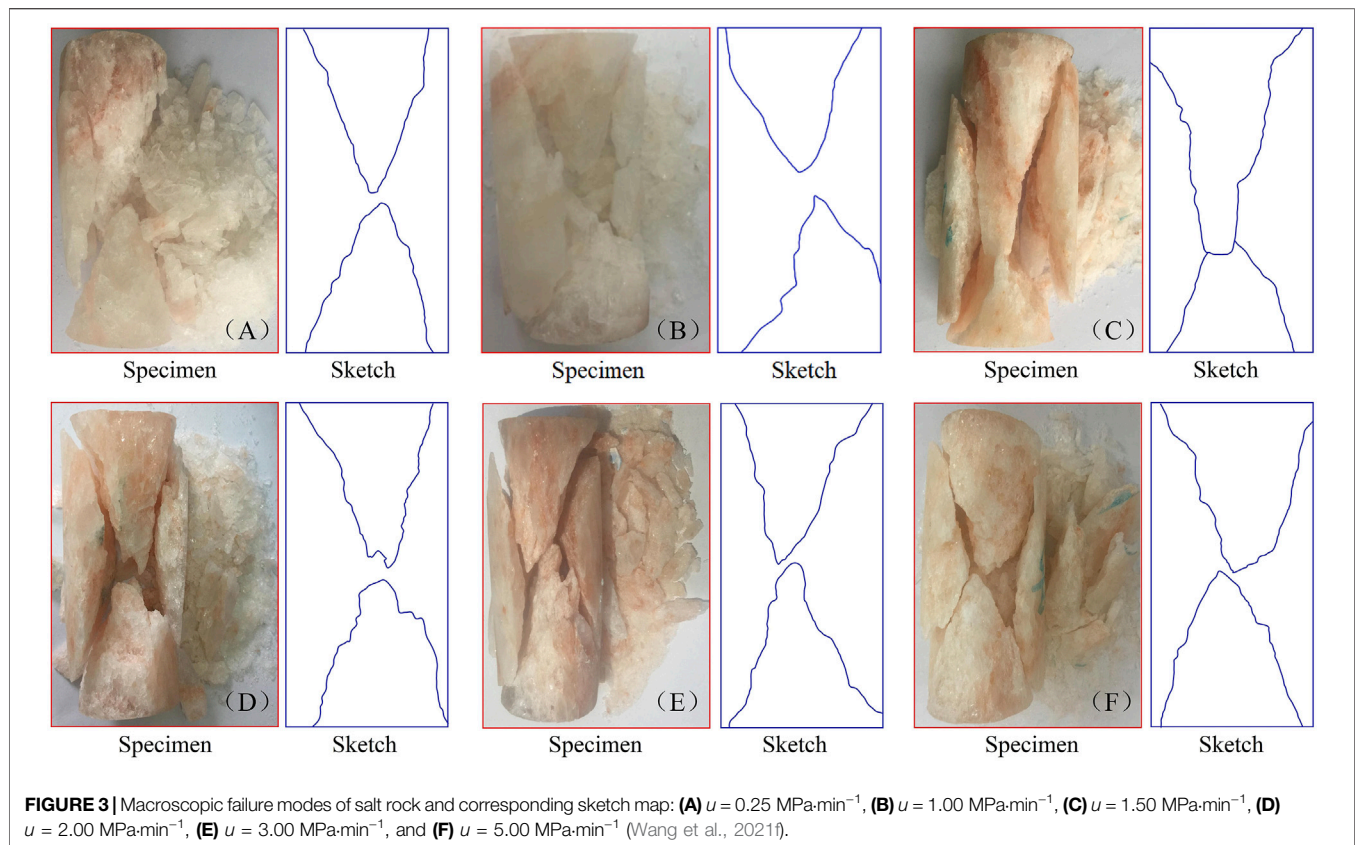
where  $u$  is the total energy density, in  $\text{mJ}\cdot\text{mm}^{-3}$ ;  $u_e$  is the elastic energy density, in  $\text{mJ}\cdot\text{mm}^{-3}$ ;  $u_d$  is the dissipated energy density, in  $\text{mJ}\cdot\text{mm}^{-3}$ .

The energy evolution relationship of rock mass units during deformation and failure is also exhibited in Figure 2. The area under the loading stress–strain curve represents the stored energy density  $u$ , which is the total work performed by the testing machine on the rock specimen. The area under the unloading stress–strain curve (the green zone) is the elastic energy density  $u_e$ , which is recoverable from the rock mass unit. The area between the loading and unloading stress–strain curves represents the dissipated energy density  $u_d$ , which causes irreversible plastic deformation and internal damage.

The total energy density  $u$  can be calculated using Eq. 4, namely (Xie et al., 2011):

$$u = \int \sigma_1 d\varepsilon_1 + \int \sigma_2 d\varepsilon_2 + \int \sigma_3 d\varepsilon_3, \tag{4}$$

where  $\sigma_1$ ,  $\sigma_2$ , and  $\sigma_3$  are the principal stresses in the three directions, in MPa;  $\varepsilon_1$ ,  $\varepsilon_2$ , and  $\varepsilon_3$  are the principal strains in the three directions, respectively.



**FIGURE 3** | Macroscopic failure modes of salt rock and corresponding sketch map: (A)  $u = 0.25 \text{ MPa}\cdot\text{min}^{-1}$ , (B)  $u = 1.00 \text{ MPa}\cdot\text{min}^{-1}$ , (C)  $u = 1.50 \text{ MPa}\cdot\text{min}^{-1}$ , (D)  $u = 2.00 \text{ MPa}\cdot\text{min}^{-1}$ , (E)  $u = 3.00 \text{ MPa}\cdot\text{min}^{-1}$ , and (F)  $u = 5.00 \text{ MPa}\cdot\text{min}^{-1}$  (Wang et al., 2021f).

The elastic energy density  $u_e$  is obtained according to Eq. 5, that is (Tang et al., 2022):

$$u_e = \frac{1}{2}\sigma_1\varepsilon_1 + \frac{1}{2}\sigma_2\varepsilon_2 + \frac{1}{2}\sigma_3\varepsilon_3. \quad (5)$$

For the uniaxial compression test ( $\sigma_2 = \sigma_3 = 0$ ), the total energy density  $u$  can be expressed as:

$$u = \int \sigma_1 d\varepsilon_1 = \sum_{i=1}^n \frac{1}{2} (\sigma_i + \sigma_{i-1}) (\varepsilon_i - \varepsilon_{i-1}), \quad (6)$$

where  $\sigma_i$  and  $\sigma_{i-1}$  are the stresses at any point on the stress–strain curve, in MPa;  $\varepsilon_i$  and  $\varepsilon_{i-1}$  are the strains corresponding to the stress points  $\sigma_i$  and  $\sigma_{i-1}$ , respectively.

The elastic energy density  $u_e$  can be expressed as:

$$u_e = \frac{1}{2}\sigma_1\varepsilon_1 = \frac{\sigma_1^2}{2E_u}, \quad (7)$$

where  $E_u$  is the unloading modulus, in MPa.

Here, the unloading modulus  $E_u$  can be replaced by the pre-peak elastic modulus  $E$  (Wang et al., 2017). Then Eq. 7 can be transformed as:

$$u_e = \frac{\sigma_1^2}{2E}. \quad (8)$$

Therefore, the concrete values of total energy density  $u$ , elastic energy density  $u_e$ , and dissipated energy  $u_d$  can be calculated by using Eqs 3, 6, 8.

## ANALYSIS OF ENERGY EVOLUTION CHARACTERISTICS OF SALT ROCK UNDER DIFFERENT LOADING RATES

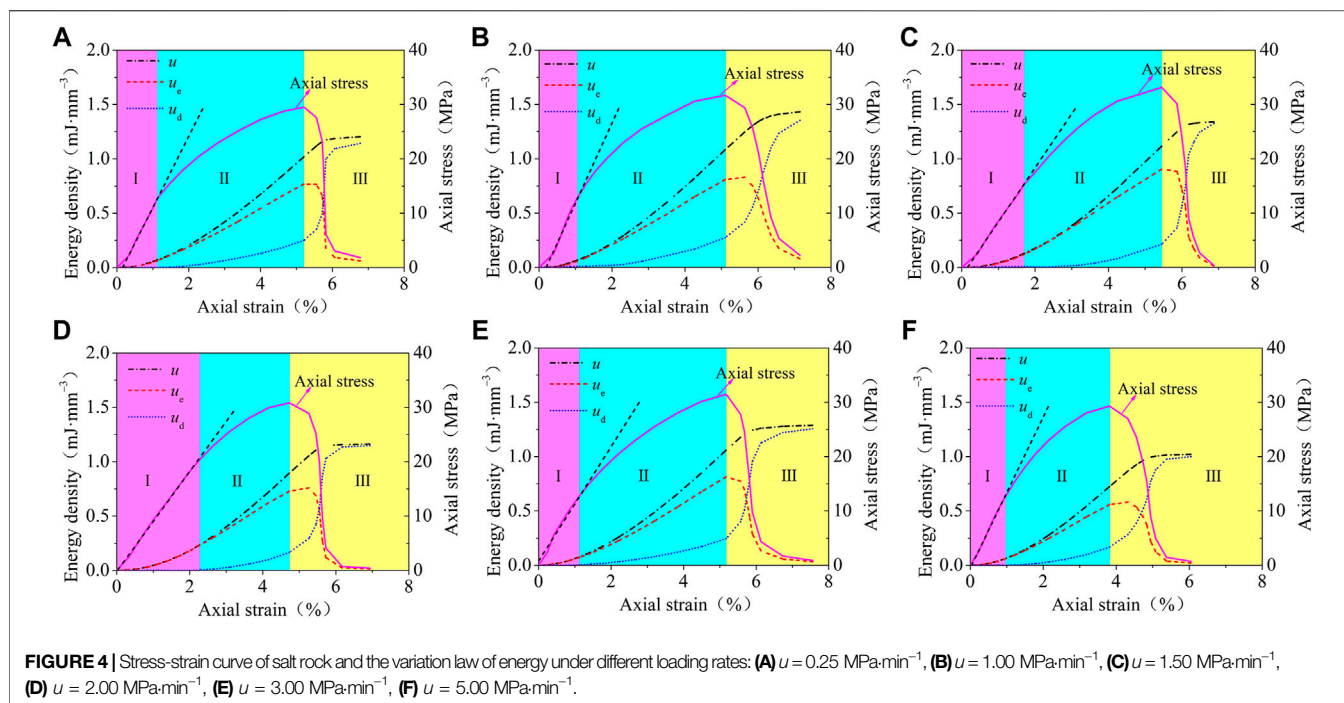
To study the influence of loading rate on the energy evolution characteristics of salt rock during deformation and failure, the uniaxial compression test results obtained by Wang et al. (2021f) is used to calculate the energy density of each part here. The loading rate selected in their study was  $u = 0.25, 1.00, 1.50, 2.00, 3.00,$  and  $5.00 \text{ MPa}\cdot\text{min}^{-1}$ , respectively.

Figure 3 shows the macroscopic failure modes of salt rock under different loading rates and the corresponding sketch map. Figure 3 reveals that the macroscopic failure modes of salt rock under different loading rates and all show “X”-type conjugate shear failure, accompanied by a debris formed by dilatancy and spalling. Therefore, the loading rate has no effect on the macroscopic failure mode of salt rock, but it is closely related to its fragmentation degree. When the loading rate is low, the fragmentation degree of salt rock is high, and the fragments produced in the process of failure are small in volume and large in quantity. With the increase in the loading rate, the fragmentation degree of salt rock gradually decreases, and the fragments produced in the process of failure are larger in volume and less in quantity.

## Energy Evolution Characteristics of Salt Rock During Deformation and Failure

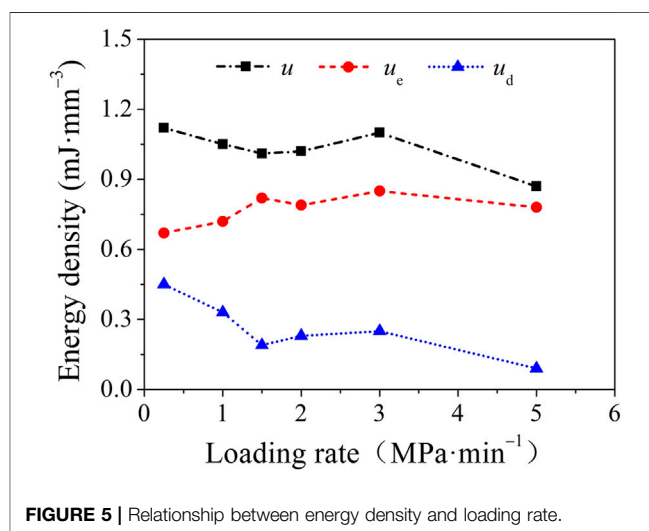
Figure 4 shows the variation in total energy density, elastic energy density, and dissipated energy density of salt rock with axial strain





under different loading rates. **Figure 4** reveals that with the increase in axial strain, the energy evolution process of salt rock during deformation and failure can be divided into the following three stages:

- 1) Energy accumulation stage (stage I), which corresponds to the compaction stage and elastic deformation stage of the axial stress–strain curve. In this stage, most of the absorbed energy is stored in salt rock in the form of elastic strain energy, and only a small amount of energy is used to close the initial defects. Generally speaking, the total energy density, elastic energy density, and dissipated energy density that occurred at this stage are all small. Through analysis, under different loading rates, the total energy density absorbed by salt rock is less than  $0.1 \text{ mJ}\cdot\text{mm}^{-3}$ ; Among them, the releasable elastic energy density stored in salt rock accounts for more than 90% of the total energy density.
- 2) Energy dissipation stage (stage II), which corresponds to the inelastic deformation stage of the axial stress–strain curve. At the beginning of this stage, new cracks began to appear in salt rock, and the growth rate of new cracks is relatively stable. The absorbed energy was still mainly stored in the salt rock in the form of elastic strain energy, and the dissipated strain energy increased slowly. With the further increase of axial strain, the internal cracks in salt rock develop into an unstable expansion stage. Although the elastic energy density increases with the increase of axial strain, the increasing rate gradually slows down. At this time, the absorbed energy is mainly used in the form of dissipated strain energy for the propagation of internal cracks in salt rock, and the dissipated energy density increases faster and faster.
- 3) Energy release stage (stage III), which corresponds to the post-peak failure stage of the axial stress–strain curve. With the increase



of axial strain, the internal cracks of salt rock expand and converge continuously, and then penetrate to form macroscopic cracks, which lead to the loss of bearing capacity of the salt rock. In this stage, the energy stored in salt rock is released to the outside in the form of kinetic energy and friction energy in a short time, and the elastic energy density rapidly decreases to zero, while the dissipated energy density increases rapidly.

### Effect of Loading Rate on Energy Density of Each Part

**Figure 5** shows the variation of total energy density, elastic energy density, and dissipated energy density of salt rock at peak point

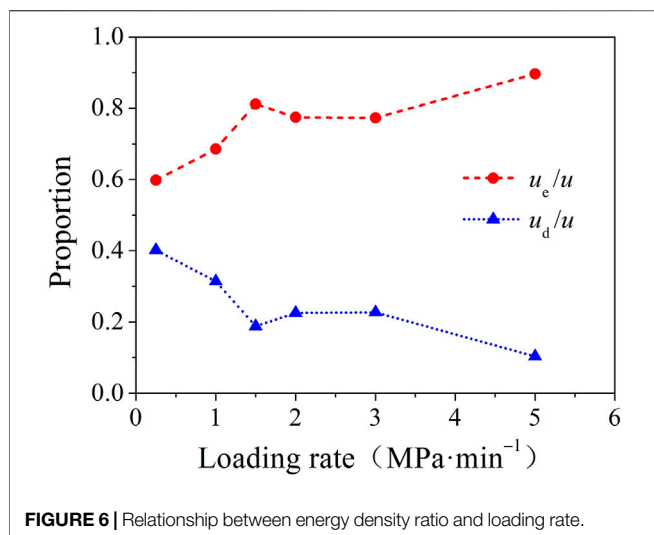


FIGURE 6 | Relationship between energy density ratio and loading rate.

with loading rate. **Figure 5** reveals that, in general, the total energy density and dissipated energy density gradually decrease with increasing loading rate, while the elastic energy density gradually increases. When the loading rate increased from 0.25 to 5 MPa·min<sup>-1</sup>, the total energy density decreased from 1.12 to 0.87 mJ·mm<sup>-3</sup>, a decrease of 22.32%. The dissipated energy density decreased from 0.45 to 0.09 mJ·mm<sup>-3</sup>, a decrease of 80%, while the elastic energy density increased from 0.67 to 0.78 mJ·mm<sup>-3</sup>, an increase of 16.42%.

**Figure 6** shows the variation of the ratios of elastic energy density to total energy density ( $u_e/u$ ) and dissipated energy density to total energy density ( $u_d/u$ ) at peak point with loading rate. **Figure 6** reveals that the ratio of elastic energy density to total energy density ( $u_e/u$ ) gradually increases with the increase of loading rate, while the ratio of dissipated energy density to total energy density ( $u_d/u$ ) gradually decreases. When the loading rate increased from 0.25 to 5 MPa·min<sup>-1</sup>, the ratio of  $u_e$  to  $u$  increased from 0.6 to 0.9, an increase of 50%, while the ratio of  $u_d$  to  $u$  decreased from 0.4 to 0.1, a decrease of 75%.

It is known from the previous analysis that during the deformation and failure of rock, the elastic strain energy is stored in the rock during the loading process, and this part energy will release to the outside environment after unloading. The dissipated strain energy is mainly used for the closure of the original microcracks, and the nucleation and expansion of new cracks. The larger the dissipated strain energy, the more the number of fracture surfaces are formed in rock, and the higher the degree of fragmentation after deformation and failure (Zhang et al., 2014). It can be seen from **Figure 5** that when the loading rate is slow, the dissipated strain energy used for the nucleation, expansion, and development of new cracks is relatively larger. In this case, the degree of the nucleation, expansion, and development of new cracks is adequate, the number of fracture surfaces formed in salt rock is relatively more, and the damage degree of salt rock is higher. Therefore, the fragmentation degree of salt rock is higher at lower loading rates, as shown in **Figure 3A**. With an increases of loading rate, on the whole, the

dissipated strain energy decreases gradually. At this time, the degree of the nucleation, expansion, and development of new cracks decreases, and the number of fracture surfaces formed gradually decreases, resulting in the decrease in damage degree of salt rock. Consequently, the fragmentation degree of salt rock under higher loading rate is relatively lower, as shown in **Figure 3F**. This is consistent with the conclusion obtained by Zhang (2013).

## Relationship Between the Number and Size of Fragments and Energy

The process of cracks expansion and development in the rock under external loads is the process from microscopic cracks to mesoscopic cracks, and then to macroscopic cracks. In the process of new cracks extension and development, it is necessarily accompanied by the increase of new free surfaces. Therefore, the dissipated strain energy  $U_d$  is mainly reflected in the form of surface free energy  $\delta_s$ , which is used for the addition of new cracks on the surface. Assuming that the fragments produced by a rock after destruction are equal volume spheres, then (Zhang, 2013):

$$U_d = \left( \sum 4\pi r^2 - \pi dh - \frac{1}{2} \pi d^2 \right) \delta_s, \quad (9)$$

where  $d$  and  $h$  are respectively the diameter and height of the cylindrical rock specimen, in mm;  $r$  is the radius of the equivalent sphere of the rock fragment, in mm; and  $\delta_s$  is the surface free energy, in mJ·mm<sup>-2</sup>.

Noted that the surface free energy  $\delta_s$  in **Eq. 9** refers to the energy consumed to form a unit crack area, and this parameter is also a physical quantity reflecting the ability of the rock to resist crack expansion.

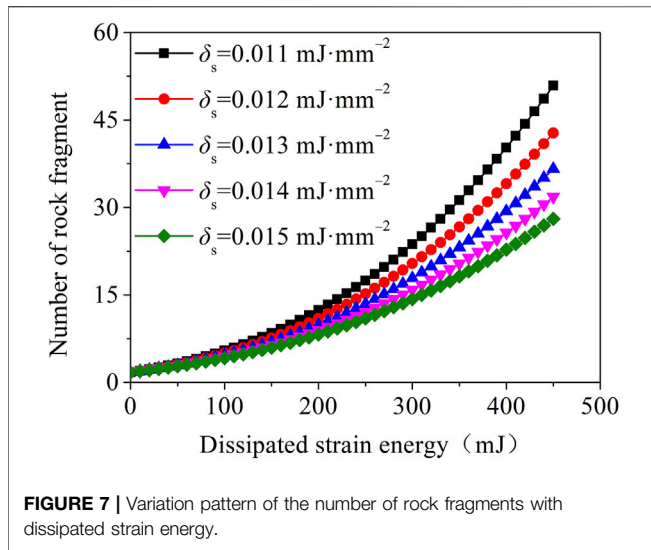
Since the volume of the rock before and after destruction is constant, we have:

$$\sum \frac{4}{3} \pi r^3 = \frac{1}{4} \pi d^2 h. \quad (10)$$

Assuming that the number of equal volume spheres formed after rock destruction is  $N$ , then according to **Eqs 9, 10**, we can get:

$$N = \frac{\left( \frac{U_d}{\delta_s} + \pi dh + \frac{1}{2} \pi d^2 \right)^3}{\frac{2}{3} \pi^3 d^3 h^2}. \quad (11)$$

With  $d = 50$  mm and  $h = 100$  mm, **Figure 7** shows the variation of the number of fragments produced after the rock failure with dissipated strain energy under different surface energies ( $\delta_s = 0.011, 0.012, 0.013, 0.014, \text{ and } 0.015$  mJ·mm<sup>-2</sup>). It reveals that under the condition of a certain rock volume, the greater the dissipated strain energy, the more fragments will be produced after rock failure, and the smaller the corresponding fragments will be. This is consistent with the macroscopic failure form of salt rock under different loading rates (as shown in **Figure 3A**). That is, the smaller the loading rate, the larger the dissipated strain energy, the more fragments produced after the salt rock failure, and the smaller the fragmented volume. Moreover, the larger the loading rate, the



smaller the dissipated strain energy, the smaller the number, and the larger the volume of fragments after the salt rock failure (as shown in **Figure 3F**). The main reason for this phenomenon is that the larger the dissipated strain energy is, the more cracks and fracture surfaces are produced in the rock, and the more fragments are produced after failure, and the smaller the corresponding fragments are. In addition, under the condition that the dissipated strain energy remains unchanged, the larger the surface free energy  $\delta_s$  is, the more energy is consumed to form the unit crack area, that is, the stronger the ability of the rock to resist crack propagation and development, the smaller the number of fragments produced after failure and the larger the fragment size.

### Relationship Between the Crushing Intensity of Rock and Energy

The crushing intensity of rock is closely related to the kinetic energy of the fragments at the time of destruction, which is converted from the elastic strain energy stored in the rock. For the same mass of fragments, the more the elastic strain energy stored inside the rock, the more kinetic energy the fragments have, and the faster the splash rate of the fragments when broken. In order to analyze the relationship between the crushing intensity of rock and the elastic strain energy, the following assumptions are made here: 1) the total energy  $U$  input to the rock by the testing machine is constant, and the ratio of conversion into elastic strain energy is  $x$ , then the ratio of conversion into dissipated strain energy is  $1-x$ ; 2) the dissipated strain energy is all used for the expansion and development of new cracks inside the rock that is, the dissipated strain energy can be approximated as the surface free energy of cracks, then:

$$\sum \frac{2}{3} \rho \pi r^3 v^2 = xU, \tag{12}$$

$$\left( \sum 4\pi r^2 - \pi dh - \frac{1}{2} \pi d^2 \right) \delta_s = (1-x)U, \tag{13}$$

where  $\rho$  is the density of the rock, in  $\text{g}\cdot\text{mm}^{-3}$ ;  $v$  is the splash rate of the fragments when the rock is damaged, in  $\text{mm}\cdot\text{s}^{-1}$ .

In addition, assuming that the fragments produced by the rock after destruction are equal volume spheres and the number of equal volume spheres formed is  $N$ , then according to **Eqs 10–13**, we get:

$$N = \frac{\left[ \frac{(1-x)U}{\delta_s} + \pi dh + \frac{1}{2} \pi d^2 \right]^3}{\frac{9}{4} \pi^3 d^4 h^2}, \tag{14}$$

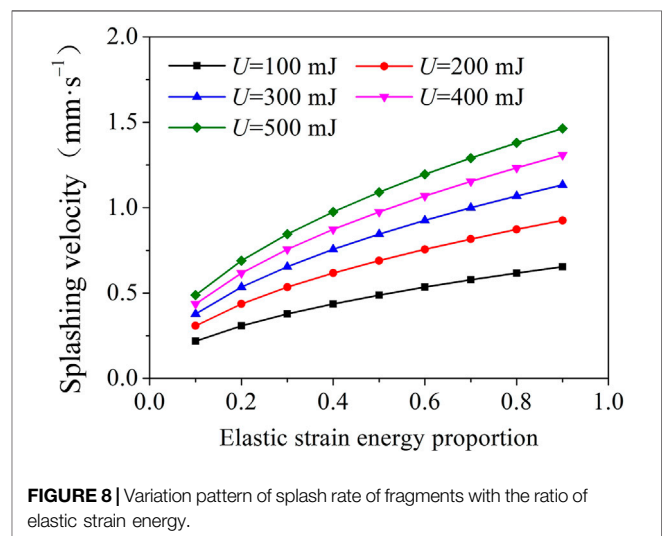
$$v = \left\{ \frac{x}{1-x} \frac{\left[ 4\pi \left( \frac{3}{16} d^2 h \right)^{2/3} N^{1/3} - \pi dh - \frac{1}{2} \pi d^2 \right] \delta_s}{\frac{1}{8} \pi \rho d^2 h} \right\}^{1/2}. \tag{15}$$

With  $d = 50 \text{ mm}$ ,  $h = 100 \text{ mm}$ ,  $\delta_s = 0.015 \text{ mJ}\cdot\text{mm}^{-2}$ , and  $\rho = 2.14 \times 10^{-3} \text{ g}\cdot\text{mm}^{-3}$ , **Figure 8** shows the variation law of fragment splash rate with elastic strain ratio under different total input energies ( $U = 100, 200, 300, 400, \text{ and } 500 \text{ mJ}$ ). It reveals that, under the condition of certain total input energy, with the increase of the proportion of elastic strain energy, the splash rate of fragments generally shows a changing trend in increase gradually, but the increasing range gradually decreases. In addition, when the proportion of elastic strain energy is constant, the greater the total input energy, the greater is the plastic strain energy, the smaller the mass of fragments produced after rock failure and the faster is the splash rate.

### CONCLUSION

Based on the existing uniaxial compression test results of salt rock under different loading rates, the energy evolution characteristics of salt rock during deformation and failure are studied. The influence of the loading rate on the total energy density, elastic energy density, and dissipated energy density of salt rock is analyzed, and the relationship between the number, size of fragments, crushing intensity, and energy of each part is discussed. The main conclusions are as follows:

- 1) The energy evolution process of salt rock deformation and failure contains the energy accumulation stage, energy



dissipation stage, and energy release stage. The energy accumulation stage corresponds to the compaction stage and the elastic stage of the stress–strain curve, the energy dissipation stage corresponds to the inelastic deformation stage of the stress–strain curve, and the energy release stage corresponds to the post-peak failure stage of the stress–strain curve.

- 2) With the increase in the loading rate, the total energy density and dissipated energy density of salt rock gradually decrease, while the elastic energy density gradually increases. At the same time, with the increase in the loading rate, the proportion of dissipated energy density to the total energy density gradually decreases, while the proportion of elastic energy density to the total energy density gradually increases.
- 3) When the volume of rock is constant, the greater the dissipated strain energy, the more the number of fragments produced after the rock failure and the smaller the size of the fragment. When the dissipated strain energy remains constant, the larger the surface free energy is, the smaller the number and the larger the size of fragments that will be produced after rock failure. When the total strain energy is constant, the splash rate of rock fragments increases with the increase of elastic strain energy ratio. When the proportion of elastic energy remains unchanged, the splash rate of rock fragments increases with the increase in total input energy.

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## DATA AVAILABILITY STATEMENT

The original contributions presented in the study are included in the article/supplementary material; further inquiries can be directed to the corresponding author.

## AUTHOR CONTRIBUTIONS

JW conceived and designed the methods for the study and economically supported the project. XL provided the experimental materials and completed the data collection. QZ completed the data analysis and the writing of the study manuscript. ZS provided the guide for experiment and theoretical research for the study.

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