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Theoretical study on longitudinal deformation of adjacent tunnel subjected to pre-dewatering based on Pasternak-Timoshenko beam model

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In this research, under the disturbance of pre-dewatering, the analytical solution of vertical displacement of the adjacent tunnel is derived using the two-stage analysis method. In the first stage, the effective stress principle was used to calculate the additional stress of the adjacent tunnel caused by dewatering. In the second stage, the Pasternak-Timoshenko beam model was used to simulate the interaction between the tunnel and soil, taking the tunnel shear deformation into account. By referring to the calculation results of existing literature, the correctness of the proposed method is verified, and the influencing factors of the longitudinal displacement of the tunnel are further analyzed. The results show that with the increase of the distance from the dewatering well and soil elastic modulus, the vertical displacement of the tunnel is reduced. The deformation of the existing tunnel increases with the permeability coefficient. The decrease of the tunnel shear modulus can lead to the rapid increase of the tunnel's vertical displacement, so the shear stiffness should be considered in the analysis of its deformation. The increase in the dropping amplitude of the water level in the well will decrease the water level in the surrounding strata. According to the different relative positions of the tunnel and the water table, there are two forms of additional load on the tunnel. Before the water level drops to the tunnel axis, the tunnel's Additional load and displacement gradually increase.

KEYWORDS

excavation dewatering, effective stress principle, Timoshenko beam, Pasternak foundation, adjacent tunnel

1 Introduction

Foundation pit excavation is an effective means of underground space development. However, pre-dewatering is necessary for foundation pit engineering to improve construction conditions. In the process of dewatering, the effective stress of soil mass under the original water level will increase (Wang et al., 2013) to have a harmful effect on the existing tunnel, which is one of the main reasons for the long-term settlement of the tunnel (Zeng et al., 2019; DING et al., 2021). Therefore, investigating the longitudinal settlement of the adjacent tunnel subjected to pre-dewatering is crucial for operation safety.

At present, many scholars have studied the influence of pre-dewatering on the adjacent tunnel. For example, taking the excavation project of Shenzhen Kerry Construction Square Phase II as a research subject, (Zhang and Pan, 2013) found that the pre-dewatering of this project caused a settlement of 5.7 mm in the adjacent subway tunnel, which did not meet the requirements of metro track deformation. Liu (2013) established a numerical model to study the influence of dewatering on the adjacent subway tunnel in the excavation project of Tianjin West Railway Station. Taking an excavation project of Changsha Line 5 as an example, (Huang et al., 2018) studied the sensitivity of adjacent subway tunnels to excavation dewatering velocity by combining Biot consolidation theory and Midas GTS finite element software. Combining the finite difference method with fluid-structure coupling theory, (Jia et al., 2010) studied the stress and deformation law of the existing municipal tunnel in the process of dewatering for a new tunnel project in Chengdu. According to the geological characteristics of underground water in Shanghai, (Li, 2008) studied the influence of excavation dewatering on the longitudinal deformation of operating metro tunnels.

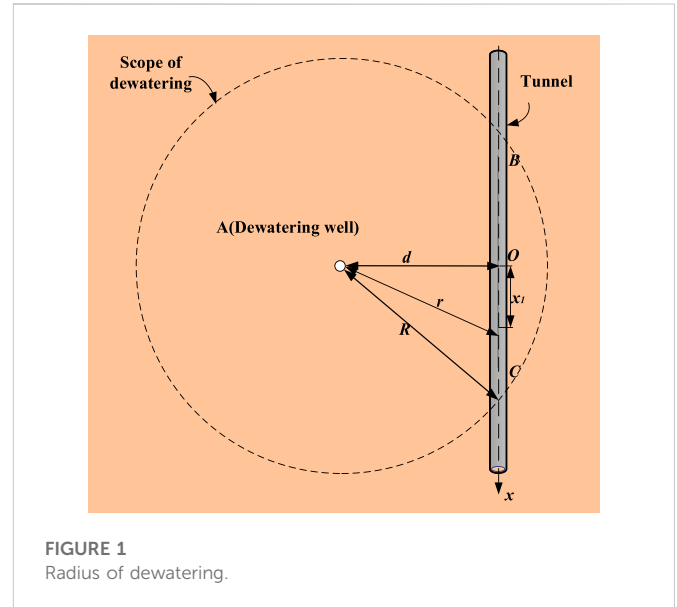
At present, there are few theoretical studies on the longitudinal deformation of adjacent tunnels caused by dewatering. Combining the effective stress principle with the Pasternak foundation model, (Xu et al., 2021) used the Euler-Bernoulli beam to simulate pipelines based on the two-stage theoretical method and deduced analytical solutions for the deformation of adjacent pipelines caused by dewatering. Under the influence of excavation and dewatering, (Zhang et al., 2017) used the two-stage theoretical method to study the deformation of the underlying tunnel and used the Euler-Bernoulli beam to simulate the tunnel, and found that the influence of excavation dewatering on the underlying tunnel should not be ignored.

In the existing studies on the deformation of shield tunnels, the shield tunnel is usually simplified as an Euler-Bernoulli beam (Zhang and Zhang, 2013; Liang et al., 2016; Liang et al., 2018). However, unlike pipelines, the shield tunnel is multi-segment ring-shaped segment splintering so that the Euler-Bernoulli beam will ignore the shear deformation generated by the tunnel. This will cause an error in the calculation. In recent years, some scholars have chosen to adopt the Timoshenko beam simulation tunnel (Li et al., 2015; Liang et al., 2017; Zhang et al., 2019; Liang et al., 2021) that can consider shear deformation.

To sum up, this paper is based on the two-stage method, the effective stress principle and Dupuit assumption are adopted in the first stage to calculate the additional stress of the adjacent tunnel caused by dewatering. In the second stage, the Timoshenko beam is used to simulate the tunnel while considering the shear deformation, and the Pasternak foundation model is used to simulate the interaction between the tunnel and soil. Then, the analytical solution of vertical displacement of adjacent tunnel caused by excavation dewatering is derived considering the shear deformation of the tunnel. Finally, the accuracy of the proposed method is verified by referring to the current literature results. The influence of the distance between the tunnel and the dewatering well, the tunnel shear modulus, the elastic modulus of soil, the permeability coefficient of soil, and the water level drawdown on the longitudinal displacement of the tunnel are studied.

2 Establishment of the equation

The influencing range of excavation pre-dewatering on the surrounding water level is defined as the dewatering radius, and



the existing shield tunnel within the dewatering radius will be affected by the dropping in the surrounding water level. As shown in Figure 1, A is the dewatering well, the dewatering radius is R, and the distance between the tunnel and the dewatering well is d. The X-axis is set along the tunnel direction, and the O point on the tunnel axis, that is, the nearest to the dewatering well is taken as the origin. Point B and point C are the intersection points between the dewatering radius and the tunnel.

2.1 Effective stress induced by pre-dewatering

Within the dewatering radius, the dewatering will cause a funnel-shaped dewatering curve in the soil; as shown in Figure 2, R_0 is the radius of the dewatering well, H_0 is the initial water level height of the phreatic aquifer, and H_t is the water level height in the well after dewatering. Based on Dupuit's assumption, the flow rate at different water levels is equal to the amount of water pumped from the well (Verruijt, 1982):

$$Q = 2\pi r h k_t \frac{dh}{dr} \tag{1}$$

where r is the horizontal distance from the well, h is the water level height at this position, and k_t is the permeability coefficient of soil. The dewatering curve $h(r)$ can be obtained by substituting the water level boundary conditions of the dewatering well $\begin{cases} h = H_0, r = R \\ h = H_t, r = R_0 \end{cases}$ and the dewatering radius into Eq. 1:

$$h(r) = \sqrt{H_0^2 - \frac{Q}{\pi k} \ln \frac{R}{r}} = \sqrt{H_0^2 - (H_0^2 - H_t^2) \frac{\ln \frac{R}{r}}{\ln \frac{R}{R_0}}} \tag{2}$$

According to Sakukin's formula, the dewatering radius can be calculated by $R = 2s_w \sqrt{kH_0}$ (Verruijt, 1982), $s_w = H_0 - H_t$.

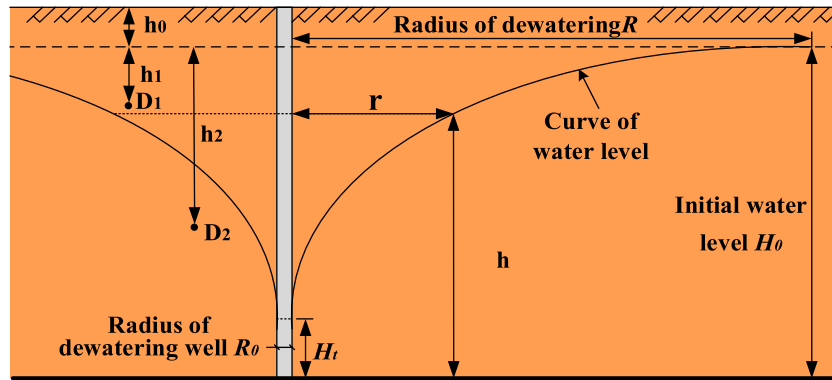


FIGURE 2
Curve of water level after dewatering.

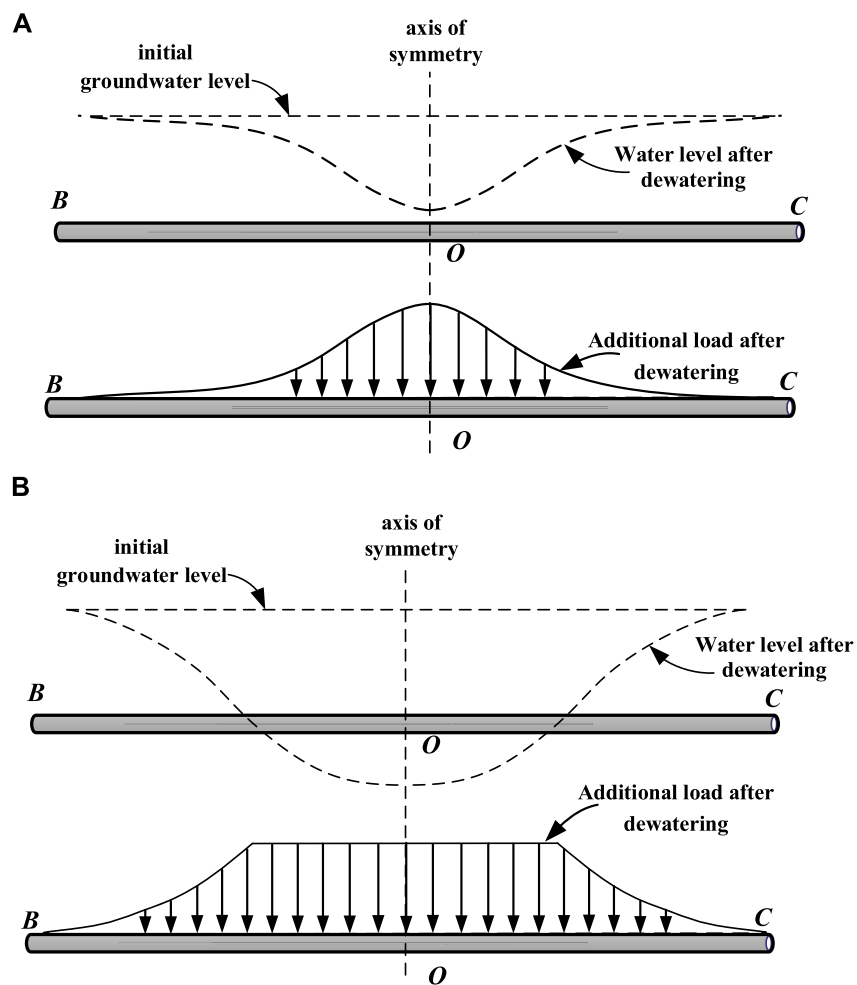


FIGURE 3
Water level and additional load distribution along tunnel length after dewatering: (A) water level is above the tunnel after dewatering; (B) part of the water level is below the tunnel after dewatering.

Within the dewatering radius, the decrease in water level will reduce pore water pressure in the soil, leading to an increase in effective stress, and this increased amplitude can be calculated according to the change in water level after dewatering; It can be

divided into two cases according to the relative position of the calculated point.

As shown in Figure 2, point D_1 is above the water level after dewatering, and point D_2 is below the water level after dewatering.

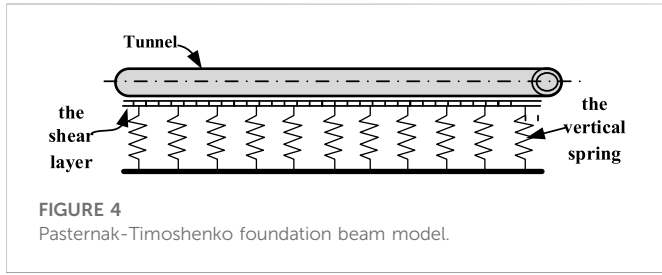


FIGURE 4 Pasternak-Timoshenko foundation beam model.

Therefore, the effective stress increment σ_1 and σ_2 of the two points can be calculated as follows:

$$\sigma_1 = \sigma_{t1} - \sigma_{o1} = (h_0 + h_1)\gamma - (h_0\gamma + h_1\gamma_s - h_1\gamma_w) = h_1(\gamma - \gamma_s + \gamma_w) \tag{3a}$$

$$\sigma_2 = \sigma_{t2} - \sigma_{o2} = [(h_0 + H_0 - h)\gamma + (h_2 - H_0 + h)(\gamma_s - \gamma_w)] - (h_0\gamma + h_2\gamma_s - h_2\gamma_w) = (H_0 - h)(\gamma - \gamma_s + \gamma_w) \tag{3b}$$

where σ_t and σ_o are the effective stresses of D_1 and D_2 points before and after dewatering, respectively; and h_0 is the buried depth of the initial water level from the ground surface; h_1 and h_2 are the elevation differences between D_1 and D_2 points and the initial water level, respectively; γ , γ_s and γ_w are unit weight and saturated unit weight of soil, and unit weight of water, respectively.

Above and below the water level, their effective stress increments after dewatering are different. According to the relative position of the tunnel and water level, the additional stress caused by dewatering is different. Therefore, the additional stress caused by dewatering can be calculated in two cases: all parts of the tunnel are below the water level after dewatering, and part of the tunnel is above the water level, as shown in Figure 3. Based on the coordinate system established in Figure 1, the additional stress on the tunnel under the two conditions is calculated as follows:

When the tunnel is below the water level, the distance between any point on the tunnel and the dewatering well $r = \sqrt{x^2 + d^2}$, after substituting it into Eq. 2 and Eq.3a can be obtained:

$$\sigma(x) = \left(H_0 - \sqrt{(H_0^2 - H_t^2) \frac{\ln \frac{R}{\sqrt{x^2 + d^2}}}{\ln \frac{R}{R_0}}} \right) \cdot (\gamma - \gamma_s + \gamma_w) \tag{4}$$

When the tunnel is partially located above the water level, the additional stress of the tunnel is divided into two parts. The additional stress of the tunnel above the water level is the same and is a fixed value.

$$\sigma = h_1(\gamma - \gamma_s + \gamma_w) \tag{5}$$

where h_1 is the height difference between the buried depth of the tunnel axis and the initial water level. The calculation of additional stress of other tunnels located below the water level is similar to Eq. 4. When $h(r) = H_0 - h_1$, it is the intersection point between water level and tunnel, so the coordinate of this point can be obtained as

$$x = \sqrt{\left(R \frac{(H_0 - h_1)^2 - H_t^2}{H_0^2 - H_t^2} \cdot R_0 \frac{(2H_0h_1 - h_1^2)}{H_0^2 - H_t^2} \right)^2 - d^2} \tag{6}$$

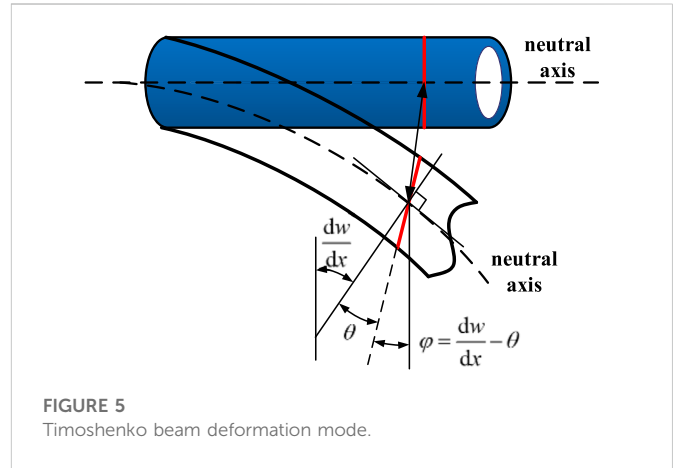


FIGURE 5 Timoshenko beam deformation mode.

In this review, when the tunnel part is located above the water level, the formula for calculating the additional stress of the tunnel is:

$$\sigma(x) = \begin{cases} \left(H_0 - \sqrt{(H_0^2 - H_t^2) \frac{\ln \frac{R}{\sqrt{x^2 + d^2}}}{\ln \frac{R}{R_0}}} \right) \cdot (\gamma - \gamma_s + \gamma_w), x^2 > \left(R \frac{(H_0 - h_1)^2 - H_t^2}{H_0^2 - H_t^2} \cdot R_0 \frac{(2H_0h_1 - h_1^2)}{H_0^2 - H_t^2} \right)^2 - d^2; \\ h_1(\gamma - \gamma_s + \gamma_w), x^2 \leq \left(R \frac{(H_0 - h_1)^2 - H_t^2}{H_0^2 - H_t^2} \cdot R_0 \frac{(2H_0h_1 - h_1^2)}{H_0^2 - H_t^2} \right)^2 - d^2 \end{cases} \tag{7}$$

2.2 Establishment of the governing equation of the timoshenko beam

The longitudinal deformation of the shield tunnel is composed of bending and shear deformation (Shen et al., 2014; Wu et al., 2015). When the traditional Euler-Bernoulli beam is used to simulate a shield tunnel, the tunnel is regarded as a structure with infinite shear strength, so the shear deformation of the tunnel is ignored. Since shield tunnels are composed of annular segments, unlike continuous structures such as pipelines, Euler-Bernoulli beams will underestimate the longitudinal deformation. The Timoshenko beam can take into account the shear deformation of the tunnel under additional loads (Li et al., 2015). In addition, the Pasternak foundation model can consider the continuity of foundation deformation and simulate the interaction between soil and tunnel well (Xu et al., 2021). Therefore, the tunnel is considered an infinitely long Timoshenko beam on the Pasternak foundation in this research to take into account the shear deformation generated by the tunnel, as shown in Figure 4. The section of the Timoshenko beam is no longer perpendicular to the neutral axis but crosses the normal direction of the neutral axis with an angle due to shear deformation. The stress deformation mode is more complex than the Euler-Bernoulli beam, as shown in Figure 5.

According to Timoshenko beam deformation theory, the relationship between tunnel bending moment M , shear force, and Q and displacement w is:

$$Q = (\kappa GA) \left[\frac{dw(x)}{dx} - \theta \right] \tag{8}$$

$$M = -E_t I_t \frac{d\theta}{dx} \tag{9}$$

where κ is the equivalent section coefficient, the tunnel is the annular section, $\kappa= 0.5$; G is the tunnel shear modulus, $G=E_t/2(1+\nu_t)$; ν_t is Poisson's ratio of tunnel; A is the annular section area of the tunnel; E_t is the elastic modulus of the tunnel; I_t is the moment of inertia of the tunnel. According to the equilibrium differential equation:

$$p(x)Ddx - q(x)Ddx - dQ = 0 \tag{10}$$

$$\frac{p(x)D}{2} dx^2 + Qdx - \frac{q(x)D}{2} dx^2 - dM = 0 \tag{11}$$

where $q(x)$ is the additional load generated by dewatering, $q(x)= \sigma(x)$; D is tunnel diameter. $p(x)$ is the ground reaction force. According to the Pasternak foundation model, $p(x)$ is obtained as

$$p(x) = kw(x) - g_s \frac{d^2w(x)}{dx^2} \tag{12}$$

where k and g_s are the elastic coefficient and shear coefficient of the foundation, respectively, which can be calculated as follows (Attewell et al., 1986; Tanahashi, 2004):

$$k = \frac{1.3E_s}{D(1-\nu^2)} \left(\frac{E_s D^4}{E_t I_t} \right)^{1/2} \tag{13}$$

$$g_s = \frac{E_s t}{6(1+\nu)} \tag{14}$$

where E_s soil elastic modulus; ν is Poisson's ratio of soil; t is the soil shear layer thickness, and $t=6D$ is used for calculation (Xu, 2005).

Through Eqs. 8–12, the governing equation of tunnel displacement $w(x)$ can be obtained as:

$$E_t I_t \left(\frac{g_s D}{\kappa G A} + 1 \right) \frac{d^4 w(x)}{dx^4} - \left(\frac{k D E_t I_t}{\kappa G A} + g_s D \right) \frac{d^2 w(x)}{dx^2} + k D w(x) = \left[q(x) - \frac{E_t I_t}{\kappa G A} \frac{d^2 q(x)}{dx^2} \right] D \tag{15}$$

3 Solving the governing equation

Based on the derivation process of Guan et al. (Guan et al., 2021), Eq. 15 was solved according to $q(x)=0$, and the general solution was obtained:

$$w(x) = e^{\alpha x} [A_1 \cos(\beta x) + A_2 \sin(\beta x)] + e^{-\alpha x} [A_3 \cos(\beta x) + A_4 \sin(\beta x)] \tag{16}$$

where $A_1, A_2, A_3,$ and A_4 are undetermined coefficients; $\alpha = \sqrt{\lambda^2/2 + \gamma/4}$; $\beta = \sqrt{\lambda^2/2 - \gamma/4}$; $\gamma = \frac{k D E_t I_t + g_s D \kappa G A}{(\kappa G A + g_s D) E_t I_t}$; $\lambda = \sqrt[4]{\frac{k D \kappa G A}{(\kappa G A + g_s D) E_t I_t}}$.

When the tunnel is subjected to concentrated load P at $x=0$, the boundary conditions of the tunnel are as follows:

$$u(\pm \infty) = 0 \tag{17a}$$

$$\left. \frac{dw(x)}{dx} \right|_{x=0} = 0 \tag{17b}$$

$$E_p I_p \left. \frac{d^3 w(x)}{dx^3} \right|_{x=0} = PD/2 \tag{17c}$$

After substituting Eqs. 17a–17c into Eq. 16, the calculation of the tunnel displacement under concentrated load P can be obtained as follows:

$$w(x) = \frac{P D e^{-\alpha x} (\beta \cos \beta x + \alpha \sin \beta x)}{4 E_t I_t \alpha \beta (\alpha^2 + \beta^2)} \tag{18}$$

It can be known from the literature (S Selvadurai, 1984) that the additional load caused by dewatering is regarded as many segments of tiny concentrated load by adopting the micro-element method and then superimposed according to Eq. 13. The additional deformation of the tunnel under the action of dewatering can be calculated by employing integration. According to Eq. 15, the right-hand side of the Equation is regarded as $Q(x)$, and the concentrated load $P(\xi)$ at any point ξ on the tunnel is

$$P(\xi) = Q(\xi) d\xi = \left[\frac{\kappa G A}{\kappa G A + g_s D} q(\xi) - \frac{E_p I_p}{\kappa G A + g_s D} \frac{d^2 q(x)}{dx^2} \right]_{x=\xi} d\xi \tag{19}$$

Substituting the distributed load $Q(x)$ into Eq. 18, the vertical displacement $dw(x)$ of the tunnel is:

$$dw(x) = \frac{Q(\xi) D e^{-\alpha|x-\xi|}}{4 E_p I_p \alpha \beta (\alpha^2 + \beta^2)} [\beta \cos(\beta|x-\xi|) + \alpha \sin(\beta|x-\xi|)] d\xi \tag{20}$$

In the influence range of pre-dewatering, the vertical displacement of the tunnel caused by dewatering can be obtained by integrating Eq. 20:

$$w(x) = \int_{-\sqrt{R^2-d^2}}^{\sqrt{R^2-d^2}} dw(x) \tag{21}$$

4 Verification

Under the impact of pre-dewatering in the excavation, the tunnel deformation of the existing subway line one of Xifeng Road of Chegongmiao Junction of Shenzhen Metro in reference (Zhang et al., 2017) is used to verify the proposed method. The initial water level of the project is $h_0=1$ m, the longitudinal length of the excavation $L=30$ m, transverse width $B=20$ m, and excavation depth is 8 m. The tunnel is vertically below the excavation and parallel to the excavation longitudinally, with a buried depth $h_2=14$ m, diameter $D=6$ m, and tunnel wall thickness is 0.3 m. The relative position of the tunnel and the excavation is shown in Figure 6. C50 concrete is generally used for the segment since its elastic modulus $E_t=34.5$ GPa, Poisson's ratio $\nu_t=0.3$, and the tunnel is in the gravel clay soil layer, the elastic modulus of soil is $E_s=60$ MPa, Poisson's ratio $\nu=0.3$, unit weight of soil $\gamma=19.9$ kN/m², and saturated unit weight of soil $\gamma_s=20.4$ kN/m². Other relevant parameters can be referred to literature (Zhang et al., 2017).

After pre-dewatering, the water level is dropped by $s_w=8$ m to be $h=9$ m, and the tunnel becomes to be under the water level. In addition, only the water falling within the scope of the excavation is considered in the literature (Zhang et al., 2017), but the dewatering radius is not considered. According to Eq. 4, the additional stress received by the tunnel in the pit range is 75.7 kPa.

Figure 7 compares the calculation results of the proposed method, the Winkler-Euler-Bernoulli model, and the results of reference (Zhang et al., 2017). The origin of the abscissa is located at the midpoint of the tunnel in the pit, so the tunnel subjected to additional load caused by dewatering is in the range $-15 \leq x \leq 15$.

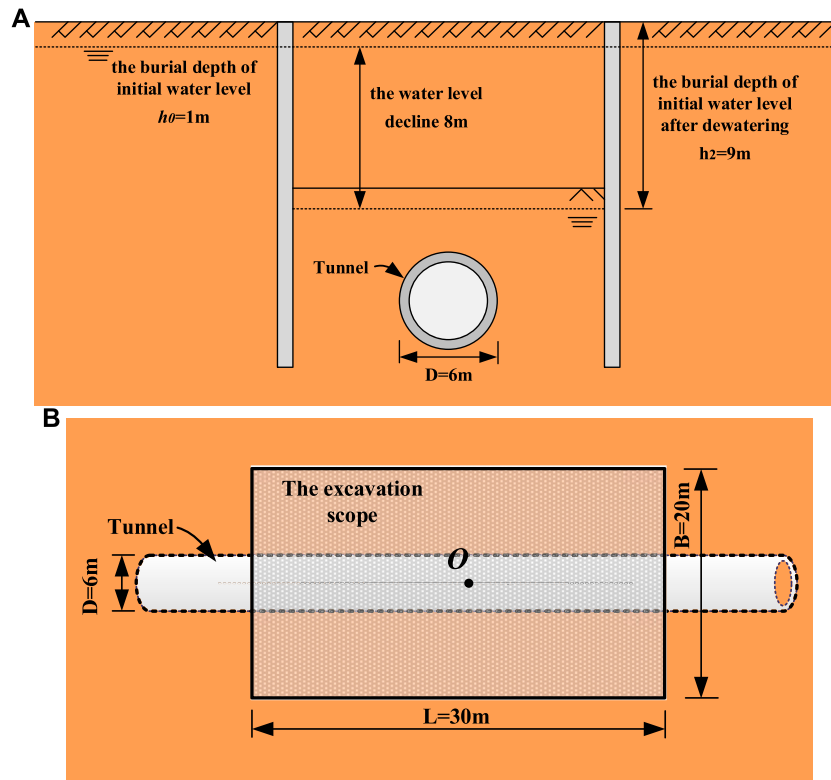


FIGURE 6 Engineering schematics: (A) sectional view; (B) plan view.

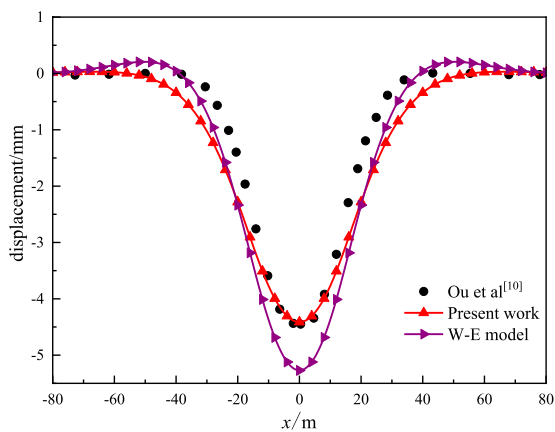


FIGURE 7 Comparison with existing literature.

It can be seen from Figure 7 that the maximum longitudinal deformation of the tunnel in the results of Reference 10 is -4.386 mm, and the maximum longitudinal deformation calculated by the method in this paper and the Winkler-Euler-Bernoulli model is -4.406 and -5.262 mm, respectively. In contrast, the calculated results in this paper are closer to those in reference 10. Because the Winkler-Euler-Bernoulli model cannot consider tunnel and foundation soil shear deformation, the Winkler calculation results

are too large. Therefore, it is proved that the calculation method of tunnel displacement considering shear deformation under the action of dewatering is correct.

5 Parameter analysis

The following calculation examples are designed for analyzing the influence of various factors on the displacement of the tunnel caused by dewatering, including initial water level $H_0=40$ m, initial water depth $h_0=1$ m, the radius of the dewatering well is $R_0=0.2$ m, the water level in the well $H_t=30$ m after dewatering, and dropping of water level $s_w=10$ m after pre-dewatering. Soil permeability $k_t=4.32$ m/d, soil elastic modulus $E_s=30$ MPa, Poisson's ratio $\nu=0.3$, unit weight of soil $\gamma=19$ kN/m³, saturated unit weight of soil $\gamma_s=20$ kN/m³. The nearest distance between tunnel and dewatering well is $D=10$ m, buried depth $z=10$ m, $h_2=9$ m, diameter $D=6$ m, the tunnel wall thickness is 0.3 m, elastic modulus $E_t=34.5$ GPa, Poisson's ratio $\nu_t=0.3$, shear modulus $G_p=13.27$ GPa.

5.1 Distance d between tunnel and dewatering well

Five groups of tests are designed to study the influence of the distance d between the tunnel and the dewatering well on the tunnel deformation while the other parameters remain unchanged, whose distances are 6, 8, 10, 12, and 14 m, respectively. It can be seen from

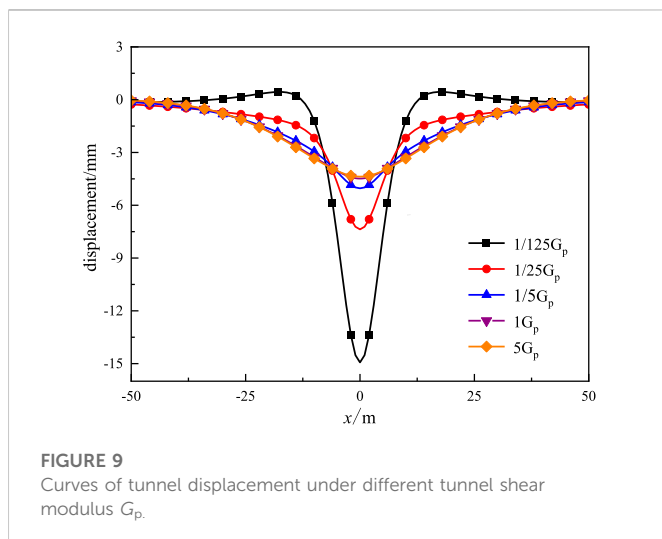
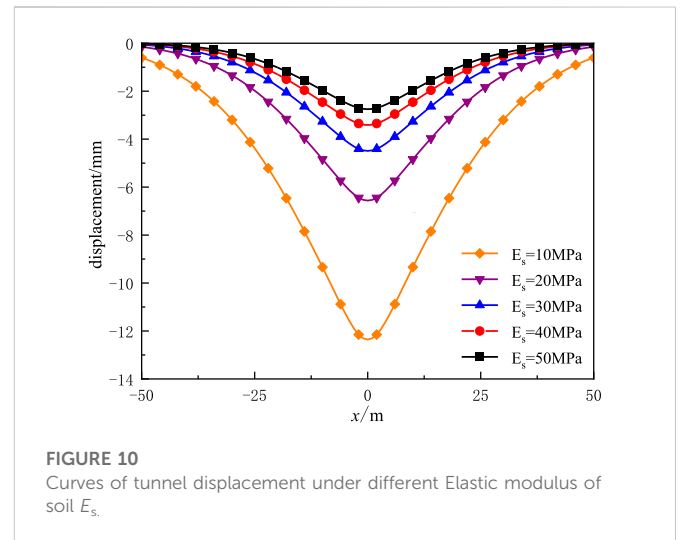
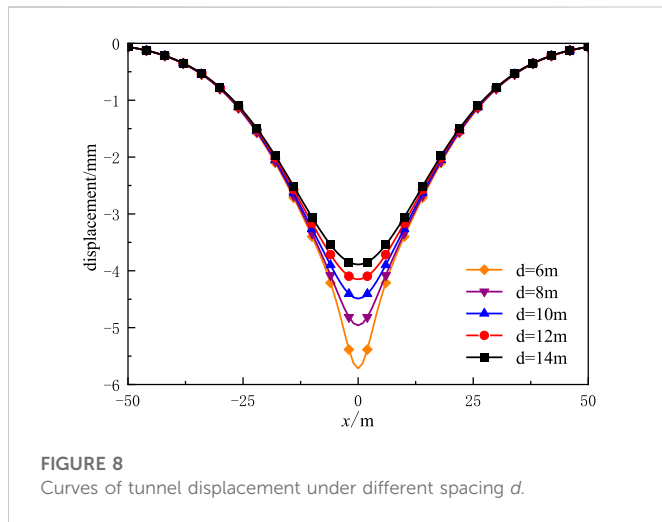


Figure 8 that when the spacing d increases from 6 to 14 m, the maximum vertical displacement of the tunnel decreases from 5.72 to 3.89 mm. This is because when the distance between the tunnel and the dewatering well gradually increases, the influence of dewatering on the tunnel is weakened. Therefore, the dewatering well should be as far away from the tunnel as possible to avoid excessive tunnel deformation in the project.

5.2 Tunnel shear modulus G_p

Five groups of tests with different tunnel shear modulus G_p were taken to study its influence on tunnel deformation while the other parameters remained unchanged, including $1/125$, $1/25$, $1/5$, and 5 times the original shear modulus. Figure 9 shows the tunnel displacement curves caused by pre-dewatering under different tunnel shear modulus G_p . As can be seen from Figure 9, when the tunnel shear modulus G_p decreases from $5 G_p$ to $1/125 G_p$, the maximum vertical displacement of the tunnel rapidly and significantly increases from 4.38 to 14.93 mm. This is because when the shear modulus G_p decreases, the ability of the tunnel to

resist the influence of dewatering is weakened. Therefore, strengthening the soil around the tunnel can reduce tunnel deformation.

5.3 Elastic modulus of soil E_s

Five groups of tests with different soil elastic modulus E_s were designed to study its influence on tunnel deformation while other parameters remained unchanged, which were 10, 20, 30, 40, and 50 MPa. It can be seen from Figure 10 that the maximum vertical displacement of the tunnel rapidly decreases from 12.36 to 2.75 mm as the soil elastic modulus E_s increases from 10 to 50 MPa. That is, because when the elastic modulus of soil E_s increases, the foundation is less likely to deform. On the other hand, when the tunnel bends, the foundation can provide a more significant reaction force to prevent tunnel deformation. Therefore, strengthening the soil around the tunnel can reduce tunnel deformation.

5.3.1 Permeability coefficient k_t

Five groups of tests with different permeability coefficient k_t were taken to study its influence on tunnel deformation, which were 4.32×10^{-3} , 4.32×10^{-2} , 0.432, 4.32, and 43.2 m/d. Figure 11 shows the tunnel displacement curves caused by pre-dewatering under different permeability coefficients k_t . It can be seen from Figure 11 that the maximum vertical displacement of the tunnel increases from 3.64 to 5.00 mm as the permeability k_t increases from 4.32×10^{-3} to 43.2 m/d. That is, because when the soil permeability k_t rises, the influence of dewatering on the surrounding stratum water level increases. Therefore, a water stop curtain can be constructed between the dewatering well and the tunnel to reduce the influence of dewatering on the tunnel.

5.4 Water level drawdown s_w

Five groups of tests with different H_t were designed to study its influence on tunnel deformation while other parameters remained unchanged, which were 30, 25, 20, 15, and 10 m, and the corresponding s_w was 10, 15, 20, 25, and 30 m respectively. Figure 12 shows the water level curve in the strata near the

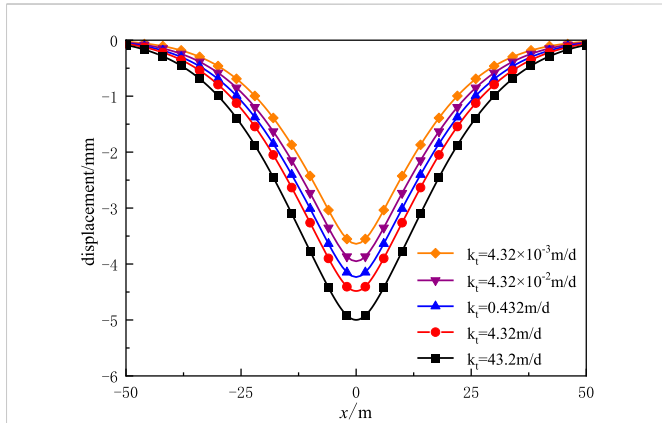


FIGURE 11
Curves of tunnel displacement under different permeability coefficients of soil k_t .

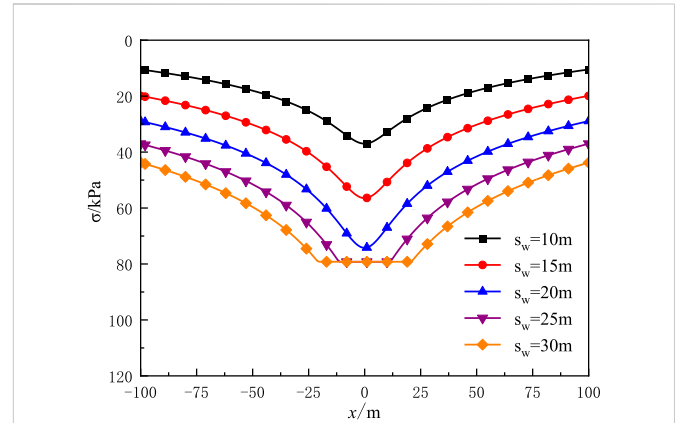


FIGURE 13
Curves of effective stress under different water level drawdown s_w .

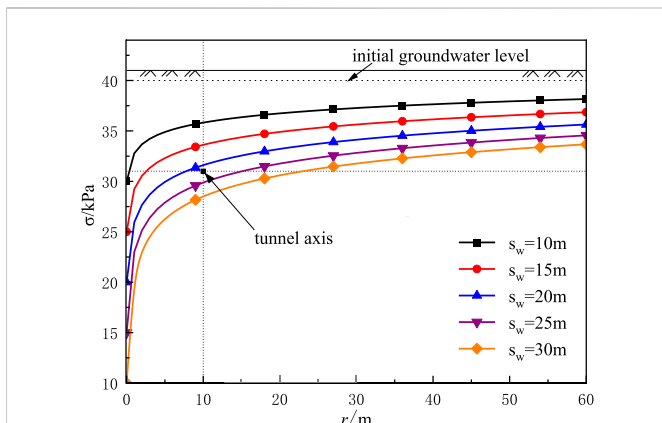


FIGURE 12
Curves of water level under different water level drawdown s_w .

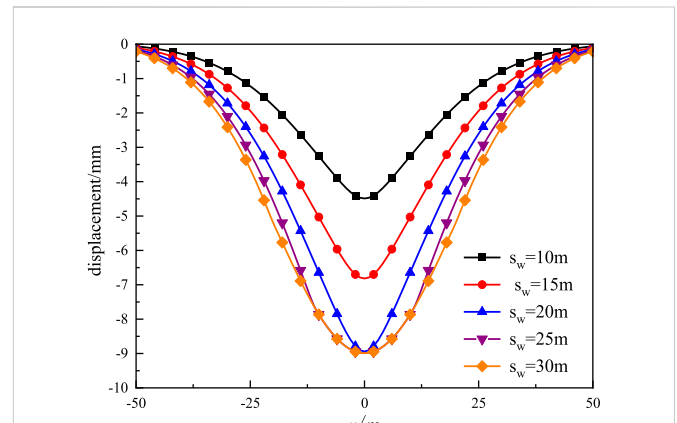


FIGURE 14
Curves of tunnel displacement under different water level drawdown s_w .

dewatering well under different water level dropping depths s_w . It can be seen that with the increase of the dropping depth of water level s_w in the well, the water level in the surrounding stratum also decreases, and the decreasing range gradually decreases. When the dewatering s_w reaches 20 m, the groundwater level is still above the buried depth of the tunnel axis, and the additional stress on the tunnel can be calculated by Eq. 4. However, when s_w of water level drawdown reaches 25 m, the part, that is, the closest to the dewatering well on the tunnel is already below the water level; In this case, the additional stress on this part is calculated by Eq. 5. Figure 13 shows the additional stress sustained by the tunnel under different water level drop depth s_w . It can be seen that the additional stress on the tunnel increases with the increase of s_w of the water level. This is because the more the water level drops, the less water buoyancy the soil above the tunnel receives. As shown in Figure 13, when s_w reaches 25 and 30 m, the maximum value of the additional stress on the tunnel will not increase, and the range of the whole deal of the additional stress will expand. This is because part of the tunnel is already above the water level as $s_w=25$ m. At the same time, as the s_w continues to increase, more of the tunnel is located above the water level. However, the additional stress on the tunnel will not increase when the water level is below the tunnel.

Therefore, the curves of $s_w=25$ and $s_w=30$ show inconsistent change trends compared with several other curves.

Figure 14 shows the tunnel displacement curve caused by pre-dewatering under different water level drop depth s_w . It can be seen from Figure 14 that the maximum vertical displacement of the tunnel increases from 4.49 to -8.99 mm when the water level drawdown s_w increases from 10 to 30 m, but the increased amplitude gradually weakens. That is, because when the water level drops depth s_w gradually increases, the influence of dewatering on the surrounding water level also increases, which leads to the increase of the effect of dewatering on the tunnel. Furthermore, the drop in water level causes the increase of additional loads on the tunnel. Therefore, with the increase of s_w , the tunnel displacement due to dewatering increases overall.

6 Conclusion

Based on the proposed two-stage method, a theoretical calculation method for the vertical displacement of adjacent existing tunnels under the impact of pre-dewatering of excavation is proposed in this paper. In the first

stage, the additional load induced by dewatering the tunnel was calculated. In the second stage, considering the shear effect, the Timoshenko beam model was used to simulate the deformation mode of the tunnel to derive the calculation of the tunnel displacement. After an in-depth Analysis, the following conclusions were drawn: DING et al., 2021.

- 1) With the increase in the distance between the tunnel and the dewatering well, the vertical displacement of the tunnel is reduced. The dewatering well should be as far away from the tunnel as possible to avoid excessive tunnel deformation in the project.
- 2) The decrease of the tunnel shear modulus G_p can lead to the rapid increase of the vertical displacement of the tunnel, so the influence of its shear stiffness should be considered when analyzing its deformation. Meanwhile, ensuring the shear stiffness of tunnels can effectively improve the ability of tunnels to resist external loads.
- 3) The growth of the elastic modulus of soil provides a more significant reaction force to prevent tunnel deformation. Therefore, strengthening the soil around the tunnel can reduce tunnel deformation.
- 4) When the soil permeability increases, the influence of dewatering on adjacent tunnels also increases. Therefore, a water stop curtain can be constructed between the dewatering well and the tunnel to reduce the influence of dewatering on the tunnel.
- 5) The increase of s_w will lead to the overall decrease in water level in the surrounding strata. According to the relative position of the tunnel and the water table, there are two forms of additional load on the tunnel. Before the water level drops to the tunnel axis, the additional load on the tunnel increases with the water level drop depth s_w , and the tunnel displacement also increases. When the water level drops below the tunnel axis, the additional load on the part above the water level is the same and does not increase with the increase of s_w . Therefore, excessive dewatering should be avoided to reduce the influence of dewatering on adjacent tunnels in foundation pit dewatering engineering.

Data availability statement

The data used to support the findings of this study are available from the corresponding author upon request.

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Conflict of interest

Author SY, RY, YJ, and ZL were employed by the company Jiangxi Transportation Institute Co., LTD.

The remaining authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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