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## A method of calculating water and soil loading on top of shallow shield tunnels near water areas

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Long-term water seepage in shield tunnels has a serious impact on water and soil loading on the outer surfaces of a shield segment near water areas. A theoretical analysis was used to obtain a formula to express the average vertical seepage gradient at the top of the tunnel. A formula for calculating the coefficient of lateral earth pressure for the principal stress arch effect was utilized. A model that takes into consideration the effects of long-term water seepage on the shield tunnel's water and soil load was designed. Based on this calculation model, the variation law of the water and soil loading on top of shield tunnel near water area with the internal friction angle in the soil body, the density of the soil, the tunnel depth-todiameter ratio, the water head of the external section, and the amount of water seepage per unit length is studied. Based on the geological conditions and field survey results of water and soil loading of two typical segments of the Maliuzhou Waterway section of the Henggin Tunnel, a comparative analysis of the theoretical results and field survey measurements was performed for different calculated conditions. The research shows that the proposed model is able to perform a reasonably effective evaluation of the water and soil pressure at the top of the shield tunnel for the marine and land segments of the shield tunnel; and, when compared with Dimitrios Kolymbas' effective stress method and Terzaghi's Principle, the method shown in this paper has fewer errors. The results of the associated research are sufficient to reasonably design and propose a theoretical basis for underwater shield tunnels.

#### KEYWORDS

tunnel engineering, terrestrial and marine shield tunnel, water seepage, water and soil load, soil arching effect, coefficient of lateral earth pressure

## **1** Introduction

With the implementation of strategies aimed at strengthening China's transportation infrastructure and as underwater shield tunnels gradually trend toward increased diameters and shallower overlying soils, the phenomenon of water seepage has begun occurring (Wang et al., 2019). The water and soil load on the top of shield tunnels contains two elements: soil pressure produced by the deformation of rock and soil and the water pressure from the effects of groundwater (Metro tunnel design specification, 2003). Tunnel water seepage will lead to changes in the surrounding seepage and stress fields, thus impacting the magnitude of water and soil load on the outer surface of the shield segment. A reasonably effective evaluation of the water and soil load on the outer surface of shallow shield tunnel segments has consistently been a hot topic and focal point both domestically and abroad as use of inaccurate values can lead to a series of problems, including tunnel deformation and instability, damage to the segment structure and increased project costs arising from material waste (Zhang et al., 2002).

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Therefore, extensive research has been conducted on the subject by researchers at home and abroad. On the aspect of water pressure calculation, Kyung-Ho. (2008), Fernandez. (2008), and Mohamed. (2010) took analytical approaches to the seepage field of a drained and circular tunnel. Du and Wang. (2011) proposed a method for the analysis of underwater tunnel fields for tunnels influenced by linings and grouting rings. Zhu et al. (2017), proposed an analytic solution for tunnel seepage fields in tunnels influenced by depth and linings. Li et al. (2020), analysed the effect of grouting rings on tunnel seepage fields under different conditions of outer lining drainage. Cui et al. (2019, 2017, 2015a, b) presented numerical solution of the surrounding rock mass pressure by considering the rock mass as strain softening and confining-stress-dependent. Liu et al. (2019), performed analyses of the seepage fields in surrounding rocks, grouting rings and liners of the Linhai Tunnel. Additionally, He et al. (2020) and Zhang et al. (2018), obtained analytical solutions for tunnel seepage fields by considering the impact of non-Darcy seepage flow while Zhang et al. (2020) and Fu et al. (2021), analysed tunnel seepage fields under the effect of far-field and near-fault water heads. On the aspect of soil pressure calculation, Terzaghi presented a sliding failure mode for overlying soil layers of shallow shield tunnels buried in sandy soils based on experimental results of the sliding door model and proposed a formula for calculating the vertical loose earth pressure on the top of a tunnel:

$$P_{\rm v} = \frac{B(\gamma - 2c/B)}{2K \tan \varphi} \left(1 - e^{-2KH \tan \varphi/B}\right) \tag{1}$$

where  $P_v$  is the vertical loose earth pressure on the top of the tunnel,  $\gamma$  is the density of the soil body, *c* is soil cohesion,  $\varphi$  is the angle of internal friction within the soil body, *K* is the lateral soil pressure coefficient for the sliding surface overlying the top of the tunnel with a suggested value of 1, *H* is tunnel depth and *B* is the width of the sliding section overlying the top of the tunnel, where  $B = 2R \cot(\pi/8 + \varphi/4)$  and *R* is the radius of the tunnel.

However, a large number of practical experiments have shown that there exists a definite discrepancy between the results of loose earth pressure calculations for sandy soils and the actual measured values in the field (Li et al., 2015), and researchers both at home and abroad have since performed revisions on the Terzaghi earth pressure theory and explored other ways of calculating soil pressure. Koyama. (2003) revised the value of the coefficient of lateral earth pressure. Li. (2014) proposed the concept of a small principal stress arch effect, thus formulating a new solution for vertical soil pressure at the top of a tunnel. Wang et al. (2019), conducted an analysis of the mechanisms of gradual arching in strata. Wan et al. (2019), separated the overlying soil body into three parts - the rectangular arching, the potential collapse, and the parabolic arching zones - and formulated a model for calculating the loose earth pressure of overlying soils. Li et al. (2020), conducted an inverse analysis of loads on the outer sections of underwater shield tunnel linings based on the results of field surveys. Zhang et al. (2019), performed a comparative analysis of the different calculation methods for vertical earth pressure on shield tunnels and their practicality based on the results of field surveys. Xiao et al. (2019), analysed the surrounding rock pressure of shield tunnels within composite strata. Zhang et al. (2016), investigated the soil arching effect and coefficient of lateral earth pressure at the top of tunnels and formulated a new type of predictive model for the height of developed soil arching. Chen and Peng. (2018), formulated a new type of soil pressure evaluation model, taking into consideration the

non-linear distribution characteristic of the height of developed soil arching and the soil pressure at the top of a tunnel based on the buoyancy of tunnels in Shanghai's soft soil region. Yu et al. (2019), performed a three-dimensional theoretical model analysis on the buoyant shear-slip model for deep tunnels.

In summary, there have already been numerous studies on the theory for calculating overlying water and soil loading on shield tunnels. Furthermore, there are relatively mature water pressure calculations and many theoretical calculation models. Moreover, the Terzaghi soil pressure principle is also in widespread use. All this information provides a theoretical basis for the design of underwater shield tunnels. However, it is not difficult to see that the current design theories and research conclusions are simply a superposition of soil and water pressures (Dimitrios, 2007; Zhao et al., 2017a; Zhao et al., 2017b; Maleki, 2018; Liu et al., 2019; Bi et al., 2020; Wang et al., 2020; Wei and Zhu, 2021; Bi et al., 2022; Liu et al., 2022). Therefore, when it comes to calculating water and soil loading for shallow shield tunnels near water areas, further discussion is still needed to account for the impact of changes in water level, actual flow field, value of the coefficient of lateral earth pressure and other problems. In light of this fact, this paper first presents an analysis of the seepage field for the marine and terrestrial segments of a tunnel, thus establishing a model with which to calculate water and soil loading on top of the tunnel. Then, with the Maliuzhou Waterway section of the Hengqin Tunnel as the object of research, in order to validate the efficacy of the calculation method proposed in this paper, a comparative analysis is performed using the results of the calculation methods proposed in this paper, actual field measurements and results of other theoretical calculations. This is done with the hope that the associated research will be able to provide a beneficial theoretical basis and support for underwater shield tunnel design.

## 2 Seepage field analysis for shallow underwater shield tunnels

An underwater shield tunnel can be divided into terrestrial and marine segments in the direction of a tunnel's central axis, as shown in Figure 1, where *R* is tunnel radius, *D* is the distance between the central



axis of the tunnel and the surface,  $d_1$  and  $d_2$  are distances between the water level and the surface of the marine and terrestrial segments, respectively and B is the width of the sliding section at the top of the tunnel. The water level is located above the surface in the marine segment and below the surface in the terrestrial section. Therefore, two sets of conditions exist for the underwater shield tunnel: underwater excavation and excavation in a semi-infinite aquifer. Under normal circumstances, surface water and groundwater levels of the Linjiang terrestrial segment are fixed and solutions are found using a fixed water head boundary condition without taking into consideration the complementary water flow conditions along the direction of the central axis of the tunnel. An analysis of the marine and terrestrial segments can be simplified into two dimensions using the calculation method shown in Figure 2 (where  $P_0$  is the support force at the top of the tunnel). Assuming that the rock surrounding the tunnel is a continuous, homogeneous medium of isotropic porosity, the seepage coefficient of the surrounding rock is k. Under conditions of long-term water seepage, the seepage field of the rock surrounding the outer section of the shield tunnel can be considered to have already reached a stable seepage state, and an analysis can be performed according to conditions of stable seepage.

According to Darcy's Law, the equation that governs stable groundwater seepage is:

$$\frac{\partial^2 \phi}{\partial x^2} + \frac{\partial^2 \phi}{\partial z^2} = 0 \tag{2}$$

where  $\phi(x,z)$  is the total water head at any point within the surrounding rock. Performing calculations with Eq. 2 based on the boundary conditions of the terrestrial and marine segments, an analysis of the tunnel seepage field can be obtained.

#### 2.1 Marine segment

With the plane of the ground surface as the datum of reference and ignoring the impact of atmospheric pressure, the seepage boundary condition at the ground surface is

$$\phi\big|_{z=0} = d_1 \tag{3}$$

With a fixed water head at the outer section of the shield tunnel, its water seepage boundary condition is

$$\phi\Big|_{x^2 + (z+D)^2 = R^2} = \phi_0 \tag{4}$$

where  $\phi_0$  is the fixed water head at the outer section of the shield tunnel. The method of images is one of the techniques commonly used to solve for the tunnel seepage field, and the key to using this method is to determine the source and the sink. Lei. (1997) disregarded the practice of fixing the centre of the tunnel as a sink, instead setting any point above the centre of the tunnel as the sink with the ground surface serving as the mirror surface. Determining the source according to the principle of the method of images provided a solution for tunnel seepage field analysis. This method avoids the fundamental assumed condition of  $R/D \ll 1$  and can be used to analyse seepage fields for deep and shallow tunnels. The equation to calculate the seepage field for the shallow marine segment of the shield tunnel  $\phi(x, z)$  and the water seepage volume per unit width q is

$$\phi(x,z) = \frac{d_1 - \phi_0}{2 \ln\left[\frac{D}{R} + \sqrt{\left(\frac{D}{R}\right)^2 - 1}\right]}$$

$$\ln\left[\frac{x^2 + \left(z + \sqrt{D^2 - R^2}\right)^2}{x^2 + \left(z - \sqrt{D^2 - R^2}\right)^2}\right] + d_1$$

$$q = \frac{2\pi k \left(d_1 - \phi_0\right)}{\ln\left[\frac{D}{R} + \sqrt{\left(\frac{D}{R}\right)^2 - 1}\right]}$$
(5)

The water pressure at any point in the rock surrounding the tunnel is represented by

$$p(x,z) = \gamma_{w} [\phi(x,z) - z]$$
(6)

where p(x,z) is the pore water pressure at any point in the surrounding rock below the water level,  $\gamma_w$  is the weight of the water, *z* is the location of



the water head, which is determined according to the distance between the datum plane and any point above or below the plane.

### 2.2 Terrestrial segment

Because ground water receives long-term replenishment from water at the surface, it is assumed that the groundwater level of the terrestrial segment is essentially equivalent to the water level at the surface and that the groundwater level does not change with tunnel seepage. With the plane of the groundwater level as the datum of reference and ignoring the impact of atmospheric pressure, the seepage boundary condition at the groundwater level is

$$\phi\Big|_{z=0} = 0 \tag{7}$$

The water head at the outer section of the shield tunnel is still assumed to be a fixed water head, and its seepage boundary condition is shown in Eq. 4. Under the special condition when the seepage field of the marine segment of the shield tunnel  $d_1 = 0$ , the seepage field of the terrestrial segment of the shield tunnel is solved using

$$\phi(x,z) = \frac{-\phi_0}{2 \operatorname{In} \left[ \frac{D - d_2}{R} + \sqrt{\left( \frac{D - d_2}{R} \right)^2 - 1} \right]}$$

$$\operatorname{In} \left[ \frac{x^2 + \left( z + \sqrt{(D - d_2)^2 - R^2} \right)^2}{x^2 + \left( z - \sqrt{(D - d_2)^2 - R^2} \right)^2} \right]$$

$$q = \frac{-2\pi k \phi_0}{\operatorname{In} \left[ \frac{D - d_2}{R} + \sqrt{\left( \frac{D - d_2}{R} \right)^2 - 1} \right]}$$
(8)

where  $d_2$  is the thickness of the strata above the groundwater level in the terrestrial segment.

## 3 Analysis of water and soil loading on top of a tunnel: The effect of long-term seepage

## 3.1 Soil pressure on top of the marine segment of the tunnel

According to the Terzaghi sliding failure mode for the overlying soil body of a shield tunnel, a rock body of thickness dz at a distance z below the ground surface is selected to serve as an object of research for this analysis as shown in Figure 2A. The following assumptions are made for the convenience of using these equations for theoretical analysis: (1) the sliding surfaces within the model are all in their ultimate state of strength, (2) the impact of the vertical seepage force within the sliding section on top of the tunnel is taken into consideration and (3) the vertical seepage gradient is evenly distributed within the rock surrounding the sliding section on top of the tunnel with an average seepage gradient of  $i_z$ . A tension-shear coupling effect with the phenomenon of ground surface tensile cracking exists, and its mechanisms are complex. Since this paper emphasizes the soil pressure on top of the tunnel, the destructive impact of the ground surface tensile forces is not discussed any further. The forces experienced by the object of research are separated into self-gravity as  $-\gamma_e Bdz$ , upper and lower stress as  $-B(\sigma'_Z + d\sigma'_z)$  and  $B\sigma'_Z$ , respectively, shear force as  $2\tau'dz$  and seepage force as  $-\gamma_w \bar{t}_z Bdz$ . When combined with the limit equilibrium analysis method, a differential equation that satisfies the equilibrium conditions can be obtained:

$$\frac{\mathrm{d}\sigma_z'}{\mathrm{d}z} = \frac{2\tau'}{B} - \gamma_{\mathrm{e}} - \gamma_{\mathrm{w}}\bar{i}_z \tag{9}$$

where  $\sigma'_z$  is the effective vertical stress in the rock surrounding the top of the tunnel,  $\gamma_e$  is the effective density of the rocky soil body,  $\bar{i}_z$  is the average vertical seepage gradient at the top of the tunnel and  $\tau'$  is the shear force on the sliding surface. The rock and soil body above the sliding surface obeys the Mohr failure criterion with a shear force of

$$\tau' = K'_c \sigma'_z \tan \varphi' + c' \tag{10}$$

where  $K'_c$  is the coefficient of lateral pressure for the sliding surface below the water level,  $\varphi'$  is the angle of internal friction within the rocky soil body below the water level and c' is the soil cohesion of the rocky soil body below the water level.

Substituting Eq. 10 into Eq. 9 based on the ground surface effective stress boundary condition  $\sigma_Z'|_{Z=0} = 0$ , an integration calculation can be performed to obtain

$$\sigma'_{\rm s} = \frac{B(\gamma_{\rm e} + \gamma_{\rm w} \bar{t}_z) - 2c'}{2K'_{\rm c} \tan \varphi'} \left[ 1 - \exp\left(\frac{2K'_{\rm c} \tan \varphi'}{B}z\right) \right]$$
(11)

Using Eq. 5 to directly solve for the seepage gradient  $\bar{t}_z$  within the sliding section at the top of the marine segment of the tunnel is relatively difficult. The seepage route is shortest at the top of the tunnel, and its seepage gradient is comparatively large. This paper presents calculations based on the most dangerous conditions so that the average seepage gradient  $\bar{t}_z$  within the sliding section is

$$\bar{i}_z = -\frac{1}{D-R} \int_{R-D}^0 \frac{\partial \phi(0,z)}{\partial z} dz = \beta_1 \left( \frac{d_1 - \phi_0}{D-R} \right)$$
(12)

where  $\beta_1$  is the water head influence coefficient calculated using the formula

$$\beta_{1} = -\frac{\ln\frac{\sqrt{D^{2}-R^{2}}+R-D}}{\ln\left[\frac{D}{R}+\sqrt{\left(\frac{D}{R}\right)^{2}-1}\right]}$$
(13)

Combining Eqs 11, 12 can solve for the soil pressure at the top of the marine segment of the shield tunnel (z = R - D):

$$\sigma'_{\rm v} = \frac{B(\gamma_{\rm e} + \gamma_{\rm w} \bar{t}_z) - 2c'}{2K'_{\rm c} \tan \varphi'} \left[ 1 - \exp\left(\frac{2K'_{\rm c} \tan \varphi'(R-D)}{B}\right) \right]$$
(14)

### 3.2 Soil pressure on top of the terrestrial segment of the tunnel

For the terrestrial segment, the groundwater level is beneath the ground surface, and for the terrestrial segment of the Linjiang Ocean Shield Tunnel, the groundwater level is generally located above the top of the tunnel. Not taking into consideration the effect of matrix suction

and finding separate solutions for the sections above and below the groundwater level, the analytical model shown in Figure 2B is obtained. The differential forces acting on the sliding section of the soil body above the groundwater level are self-gravity,  $-\gamma Bdz$ , upper and lower stresses,  $-B(\sigma_z + d\sigma_z)$  and  $B\sigma_z$ , respectively, and shear force,  $2\tau dz$ . The differential forces acting on the sliding section of the soil body below the groundwater level are self-gravity,  $-\gamma Bdz$ , upper and lower stresses,  $-B(\sigma'_z + d\sigma'_z)$  and  $B\sigma'_z$ , respectively, and shear force,  $2\tau dz$ . The differential forces acting on the sliding section of the soil body below the groundwater level are self-gravity,  $-\gamma Bdz$ , upper and lower stresses,  $-B(\sigma'_z + d\sigma'_z)$  and  $B\sigma'_z$ , respectively, shear force,  $2\tau' dz$  and seepage force,  $-\gamma_w \bar{i}_z Bdz$ . The equilibrium conditions for the two parts of the sliding section above and below the groundwater level are:

$$\frac{\mathrm{d}\sigma_z}{\mathrm{d}z} = \frac{2\tau}{B} - \gamma \text{ (Above the ground water level)} \\ \frac{\mathrm{d}\sigma_z^{'}}{\mathrm{d}z} = \frac{2\tau'}{B} - \gamma_{\mathrm{e}} - \gamma_{\mathrm{w}}\overline{t_z} \text{ (Below the ground water level)}$$

where  $\gamma$  is the natural density of the soil body above the water level.

The shear stress at the face of the sliding section below the groundwater level can be calculated according to Eq. 10 while the shear stress at the face of the sliding section above the groundwater level is

$$\tau = K_c \sigma_z \tan \varphi + c \tag{16}$$

where  $K_c$  is the coefficient of vertical earth pressure for the shear at the face of the slip surface above the groundwater level and *c* and  $\varphi$  are cohesion and angle of internal friction of the rock and soil body above the water level, respectively. Considering that the groundwater level in land next to the shore is generally higher and that there exists a capillary water effect, the values *c* and  $\varphi$  used in the calculations for the rocky soil body above the water level are selected according to their saturated state.

If the boundary conditions are  $\sigma_z (z = d_2) = 0$  and  $\sigma' (z = 0) = \sigma_z (z = 0)$  and Eqs 15, 16 are combined and then integrated, we can obtain:

$$\sigma_{z}^{'} = \frac{B\left(\gamma_{e} + \gamma_{w}\overline{i_{z}}\right) - 2c^{\prime}}{2K_{c}^{'}\tan\varphi^{\prime}} \left[1 - \exp\left(\frac{2K_{c}^{'}\tan\varphi^{\prime}}{B}z\right)\right] + \frac{\gamma B - 2c}{2K_{c}\tan\varphi} \left[1 - \exp\left(\frac{-2K_{c}\tan\varphi d_{2}}{B}\right)\right] \cdot \exp\left(\frac{2K_{c}^{'}\tan\varphi^{\prime}}{B}z\right)$$

$$(17)$$

According to Eq. 8, the average seepage force gradient  $i_z$  within the sliding section of the terrestrial segment of the tunnel is

$$\bar{i}_{z} = \frac{-1}{D - R - d_{2}} \int_{R + d_{2} - D}^{0} \frac{\partial \phi(0, z)}{\partial z} \, \mathrm{d}z = \frac{\beta_{2} \phi_{0}}{D - R - d_{2}}$$
(18)

where  $\beta_2$  is the influence coefficient of the water head, calculated using equation

$$\beta_2 = \frac{\ln \frac{\sqrt{(D-d_2)^2 - R^2 + R + d_2 - D}}{\sqrt{(D-d_2)^2 - R^2 + D - R - d_2}}}{\ln \left[\frac{D-d_2}{R} + \sqrt{\left(\frac{D-d_2}{R}\right)^2 - 1}\right]}$$
(19)

Combining Eqs 17, 18 can solve for the earth pressure on top of the tunnel for the terrestrial segment of the shield tunnel ( $z = R + d_2 - D$ ) as

$$\sigma_{z}^{'} = \frac{B(\gamma_{e} + \gamma_{w}\overline{i_{z}}) - 2c^{'}}{2K_{c}^{'}\tan\varphi^{'}} \cdot \left[1 - \exp\left(\frac{2K_{c}^{'}\tan\varphi^{'}(R + d_{2} - D)}{B}\right)\right] \\ + \frac{\gamma B - 2c}{2K_{c}\tan\varphi} \cdot \left[1 - \exp\left(\frac{-2K_{c}\tan\varphi d_{2}}{B}\right)\right] \\ \cdot \exp\left(\frac{2K_{c}^{'}\tan\varphi^{'}(R + d_{2} - D)}{B}\right)$$
(20)



For a medium load structure model, the water and soil loads  $P_{\text{water, soil}}^{\text{marine}}$  and  $P_{\text{water, soil}}^{\text{terrestrial}}$  for the top of the tunnel in the marine and terrestrial segments, respectively, are

$$P_{\text{water, soil}}^{\text{marine}} = \sigma_z' \big|_{z=R-D} + p_w \big|_{z=R-D}$$
(21a)

$$P_{\text{water, soil}}^{\text{terrestrial}} = \sigma_z' \Big|_{z=R+d_2-D} + p_w \Big|_{z=R+d_2-D}$$
(21b)

where  $p_w$  is the water pressure at the top of the tunnel, which can be solved for according to Eqs 5–7.

# 3.3 Investigating the coefficient of lateral earth pressure for the surface of the sliding section

The coefficient of lateral earth pressure is one of the key parameters of the Terzaghi loose earth pressure theory. However, a consensus has still not been reached in the calculation of the coefficient of lateral earth pressure *K*, with the primary point of controversy being the selection of the principal arch stress to be used in the calculation (Handy, 1985; Wan et al., 2019; Wang et al., 2019; Fan et al., 2022). Xu et al. (2018) and Dong et al. (2022) discovered that a convex principal stress arch is more aligned with actual circumstances and the principal stress arch traces adopt a circular arc form. In addition, the majority of past research and results are based on conditions of sandy strata, and, therefore, the applicability of the coefficient of lateral earth pressure formula to cohesive substrata has not been settled. On the basis of

prior research, this paper adopts assumed conditions for the principal stress arch and establishes an analytical model for the convex circular arc form shown in Figure 3. In Figure 3,  $P_A$  and  $P_B$  are two poles of the Mohr stress circle.

The rocky soil body of the sliding surface is in a limit equilibrium state. Based on the limit equilibrium conditions and the geometric relationship in Figure 3, the horizontal stress  $\sigma_h$  and  $\sigma_v$  the vertical stress within the sliding rocky soil body can be expressed as

$$\sigma_{\rm v} = \sigma_1 \left( \cos^2 \theta + K_{\rm a} \sin^2 \theta \right) \sigma_{\rm h} = \sigma_1 \left( K_a \cos^2 \theta + \sin^2 \theta \right)$$
(22)

where  $\sigma_1$  is the principal stress at any point within the soil body of the slip surface,  $\theta$  is the angle of rotation of the principal stress at any point within the soil body of the slip surface, expressing the angle between the direction of principal stress at a certain point and the horizontal while  $K_a$  is the coefficient of active earth pressure for the soil body.

*K*, the ratio of the horizontal earth pressure to the vertical earth pressure at any point, is expressed as

$$K = \frac{K_a \cos^2 \theta + \sin^2 \theta}{\cos^2 \theta + K_a \sin^2 \theta}$$
(23)

Because the rocky soil body within the sliding section is in an active fault state, the coefficient of active earth pressure in the equation is  $K_a = \sigma_3/\sigma_1$ ,  $K_a = tan^2 (\pi/4 - \varphi/2)$ .

The average vertical stress is

$$\bar{\sigma}_{\rm v} = \frac{1}{B} \int_{-B/2}^{B/2} \sigma_{\rm V} = \frac{\sigma_1}{2\sin\theta_0} \left[ \frac{1-K_{\rm a}}{2} \sin(2\theta_0) + (1+K_{\rm a})\theta_0 \right]$$
(24)

where  $\theta_0$  is the angle between the principal stress  $\sigma_1$  at point A in the shear-slip surface and the horizontal.

The distribution coefficient m for the vertical earth pressure is

$$m = \frac{\sigma_{\rm v}}{\bar{\sigma}_{\rm v}} = \frac{4\sin\theta_0\left(\cos^2\theta + K_{\rm a}\sin^2\theta\right)}{(1 - K_a)\sin2\theta_0 + 2(1 + K_{\rm a})\theta_0}$$
(25)

According to Figure 3, the shear stress  $\tau$  at point A of the shear-slip surface satisfies

$$\tau = K_A \sigma_{\rm vA} \tan \varphi + c \tag{26}$$

where  $K_A$  is the ratio of the horizontal earth pressure and  $\sigma_{vA}$  is the vertical earth pressure, respectively, at point A of the shear-slip surface. Substituting Eq. 25 into Eq. 26 simplifies the formula to

$$\tau = m_A K_A \bar{\sigma}_{\rm v} \tan \varphi + c \tag{27}$$

The coefficient of lateral earth pressure for the shear-slip surface is

$$K_{c} = m_{A}K_{A} = \frac{4(K_{a}\cos^{2}\theta_{0} + \sin^{2}\theta_{0})\sin\theta_{0}}{(1 - K_{a})\sin2\theta_{0} + 2(1 + K_{a})\theta_{0}}$$
(28)

According to the geometrical relationship between the Mohr stress circle and the extreme failure envelope of the  $\tau - \sigma$  plane, it is known that

$$\tan \theta_{0} = \frac{\sigma_{v} \tan \varphi + c}{\sigma_{v} - \sigma_{3}} 
\sigma_{3} = \frac{c (\sin \varphi - 1)}{\cos \varphi} - \frac{\sigma_{v} (\sin \varphi - 1)}{\cos^{2} \varphi}$$
(29)

Equation 29 can be simplified to obtain



$$\tan \theta_0 = \frac{\cos \frac{\varphi}{2} + \sin \frac{\varphi}{2}}{\left|\cos \frac{\varphi}{2} - \sin \frac{\varphi}{2}\right|} \tag{30}$$

Because of  $\varphi$ , the angle of internal friction within the soil body is typically less than 90° and  $\cos \frac{\varphi}{2} > \sin \frac{\varphi}{2}$ . Eq. 30 then becomes

$$\tan \theta_0 = \frac{\cos \frac{\varphi}{2} + \sin \frac{\varphi}{2}}{\cos \frac{\varphi}{2} - \sin \frac{\varphi}{2}} = \tan\left(\frac{\pi}{4} + \frac{\varphi}{2}\right)$$
(31)

from which can be obtained

$$\theta_0 = \pi/4 + \varphi/2 \tag{32}$$

It is clear from Eq. 32 that the formula for the angle of rotation of the principal stress obtained in this paper is consistent with the formula for the angle of rotation of the principal stress in sandy strata obtained by Handy (1985). Further, it can be seen that the angle of rotation of the principal stress in the soil body is only associated with the angle of internal friction within the soil body and that the coefficient of lateral earth pressure is a function of the angle of rotation of principal stress. This shows that this paper's model for calculating the coefficient of lateral earth pressure can be applied to both sandy and cohesive strata. By substituting Eq. 32 into Eq. 28 and simplifying, the coefficient of lateral earth pressure of the shear-slip surface can be obtained:

$$K_{\rm c} = \frac{2\left[(1+K_{\rm a})+(1-K_{\rm a})\sin\varphi\right]\sin\left(\frac{\pi}{4}+\frac{\varphi}{2}\right)}{(1-K_{\rm a})\cos\varphi+2(1+K_{\rm a})\left(\frac{\pi}{4}+\frac{\varphi}{2}\right)}$$
(33)

A comparative analysis has been performed using this paper's model for calculating the coefficient of lateral earth pressure and other existing formulas as shown in Figure 4. Through an analysis of the figure, when the results from this paper's model are placed alongside those from existing theoretical calculations, the validity of this paper's model for calculating the coefficient of lateral earth pressure is clear. Furthermore, it can also be seen from the figure that the coefficient of lateral earth pressure changes with increases in the angle of internal friction within the rocky soil body by first slightly decreasing and then increasing. This could be primarily due to the impact of the soil









arching effect during the soil deformation process, showing that there are certain conditions where the soil arching effect is a driving influence on the coefficient of lateral earth pressure. Before the soil arching effect begins, the coefficient of lateral earth pressure decreases slightly with an increase in the angle of internal friction. After the soil arching effect forms, soil arching is a driving influence on the changes in the coefficient of lateral earth pressure, and as the angle of internal friction increases, the coefficient of lateral earth pressure increases and the soil arching effect is more evident, which aligns with established facts.

## 4 Parameter impact analysis

## 4.1 The impact of the tunnel's depth - diameter ratio

When the distance between the water level and the ground surface is  $d_1 = d_2 = 10$  m, the cohesive strength of the rocky soil body is c = 20 kPa, the angle of internal friction  $\bar{\varphi} = 30^{\circ}$ , the tunnel is fully drained, and the saturated density of the rocky soil body is 19 kN/m<sup>2</sup>. The water and soil loading on the top of



#### FIGURE 9

Geological section of the construction section of the Hengqin Tunnel passing through the Maciuzhou Waterway.

#### TABLE 1 Physical parameters.

Surrounding	Seepage coefficient $k/m \cdot d^{-1}$	Compression modulus <i>E<sub>s</sub>/M</i> Pa	Saturation severity <i>y</i> /kN·m <sup>-2</sup>	Cohesion c/kPa	Internal friction <i>φ</i> /°
Silt	0.000 167	1.74	16.4	29.5	16.35
Fine clay	0.005	5.68	17.9	43.5	15.7
Medium-grade	0.71	20	19	10	28
Coarse	7	25	19	8.3	32
Fine sands	26.4	30	19.5	3.3	35
Weathered granite	7	60	22.1	12.6	38

the shield tunnel changes with different tunnel depth-diameter ratios D/R as shown in Figure 5. Through an analysis of the figure, it is clear that as D/R increases, the water and soil loading on the top of the shield tunnel consistently increases; and its rate of increase gradually lessens primarily due to the fact that as D/R increases, the impact of the soil arching effect becomes more evident. Under the same calculation conditions, the water and soil load on the marine segment is greater than that on the terrestrial segment primarily because the impact of the water level is higher on the marine segment, which aligns with known facts and reflects the rationality of this paper's method.

## 4.2 The impact of the density of the rocky soil body

When the distance between the water level and the ground surface is  $d_1 = d_2 = 10$  m, the cohesive strength of the rocky soil body is c =20 kPa, the angle of internal friction  $\varphi = 30^{\circ}$ , the tunnel is fully drained, the radius of the tunnel is R = 5 m, and the tunnel depth is D = 30 m. The water and soil loading on the top of the shield tunnel changes with different values of the saturated density  $\gamma$  of the rocky soil body, as shown in Figure 6. Through an analysis of the figure, it is clear that as the volumetric weight of the soil body increases, the water and soil load on the top of the tunnel experiences a gradual linear increase.



## 4.3 The impact of drainage conditions

When the distance between the water level and the ground surface is  $d_1 = d_2 = 10$  m, the cohesive strength of the rocky soil body is c = 20 kPa, the angle of internal friction  $\varphi = 30^\circ$ , the radius of the tunnel is R = 5 m, the tunnel depth is D = 30 m, the saturated density of the rocky soil body is 19 kN/m<sup>2</sup> and the coefficient of seepage for the rocky soil body is k = 0.001 m/d. The water and soil loading on the top of the shield tunnel changes with different values of the water head at the inner boundary of the tunnel as shown in Figures 7, 8. In the figures, *d* is the distance between the water level and the ground surface. Through an analysis of the figure, it is clear that as the water head at the outer edge of the section increases, the ability of the tunnel to seep water gradually decreases and the water and soil load on the top of the tunnel presents a consistent linear increase. As the volume of seepage water per unit width increases, the water and soil load on the top of the tunnel reveals a gradual linear decrease

## 5 Project applications and verifications

### 5.1 Project overview

The Maliuzhou segment of the Hengqin Tunnel is the object of our research. This tunnel is located in the section between Working Well No. Three and Financial Island. The Maliuzhou Waterway is in the YDK8 +  $100 \sim +700$  segment with a waterway width of 600 m and water depth of 5–8 m. The geological profile of the Maliuzhou Waterway shield construction segment of the Hengqin tunnel is shown in Figure 9. The strata surrounding the tunnel are primarily silt, fine clay, medium-grade, coarse and fine sands and weathered granite. According to the engineering geological conditions and engineering characteristics of Hengqin Tunnel, static penetration test, standard



penetration test and dynamic penetration test, pressure meter test and indoor soil test were carried out for the main soil layers. Through the statistical analysis of these test results, the paper obtains the values of cohesion and angle of internal friction of geotechnical masses. The primary physical and mechanical parameters are shown in Table 1. The shield construction section of the tunnel uses a total of four composite-style earth pressure equilibrium shields with linings of prefabricated reinforced concrete. The shield tunnel's inner diameter is 7.7 m, its outer diameter is 8.5 m, its segment width is 1.6 m and its segment liner thickness is 400 mm.

According to the preliminary geological exploration results of Hengqin Tunnel, two sections of the shield tunnel were selected to measure the changes in water and soil pressure on the outside of the shield tunnel in the direction of Well No. Three on the northern shore beneath the waterway and in the direction of Financial Island to the south. A basic overview of the measured sections is as follows:

Section I: YDK8 + 339.5 at a buried depth of 18.7 m and water depth of 5–8 m in the bottom section of the Maliuzhou Waterway. Overlying strata is composed of fluid plastic silt, fine plastic clay and a thin layer of silty clay. The tunnel passes through a stratum of moderate-density coarse sand.

Section II: YDK8 + 765.1 at a buried depth of 22.5 m and water depth of 5–8 m in the northern shore of the Maliuzhou Waterway. Overlying strata is composed of loose fine sand, fluid plastic silt, a thin layer of slightly dense fine sand, fine plastic clay and clay. The tunnel passes through an arched stratum of plastic clay, a middle



#### TABLE 2 Weighted value of stratum property parameters.

stratum of moderately dense sand and a bottom stratum of weatherized granite.

## 5.2 Analysis of field survey results

According to Figure 10, it is clear that the two measured sections located in B<sub>2</sub> are essentially located at the top of the tunnel and field measurements can be used to obtain the distributed changes in the pressure of water and soil in the outer B2 section at locations I and II as shown in Figures 11, 12. It can be seen that the initial water pressure of section II is higher than that of section I, which is mainly due to the different testing time of the two initial water pressures. Due to the limitation of on-site installation and testing conditions, the initial water pressure of section II is measured after the shield tail passes through about two ring segments. At this time, the underground water is affected by grouting and surrounding rock deformation, which will produce a certain water pressure on the outside of the segment. The initial water pressure of section I is measured when the shield tail almost passed section I, and the water pressure outside the segment is almost zero. After water and soil loading had essentially stabilized, the total soil pressure at the top of the tunnel in Section I was 0.309 MPa, the water pressure was 0.144 MPa and the effective soil pressure was 0.165 MPa. The total soil pressure at the top of the tunnel in Section II was 0.243 MPa, the water pressure was 0.174 MPa and the effective soil pressure was 0.068 MPa.

## 5.3 Theoretical calculations and comparative analysis

It is rather difficult to make a direct comparison between the water and soil pressures at the top of the tunnel in Sections I and II. The following formula can be used to find a weighted average of the physical parameters

Section		Saturation severity $\gamma/kN\cdot m^{-2}$	Cohesion c/kPa	Internal friction $arphi/^\circ$	Seepage coefficient <i>k</i> /m·d <sup>−1</sup>	
Ι		18.12	27.28	22.23	8.76	
Π	Below the water level	17.26	33.23	17.23	0.071 6	
	Above the water level (Medium-grade)	19	10	28		

#### TABLE 3 Comparative analysis of results.

	The value of the water and soil pressure at the top of the tunnel					
	Our method		DK method			
Section	Fully-drained /MPa	Non-drained /MPa	Fully-drained /MPa	Non-drained /MPa	Terzaghi method	Result
Ι	0.293	0.313	0.061	0.245	0.202	0.309
II	0.225	0.271	0.046	0.202	0.232	0.243



of the soil strata above the tunnel to achieve an effective simplification of the conditions of the strata where these sections of the tunnel lie:

$$\bar{x} = \frac{\sum_{i=1}^{4} x_i h_i}{\sum_{i=1}^{4} h_i}$$
(34)

where *x* is the weighted average of the physical parameters of the soil body,  $x_i$  is the value of the physical parameter at strata *i* and  $h_i$  is the thickness of strata *i*.

The strata above the top of the tunnel was selected to perform a weighted calculation. Segment I is located in strata completely below the water level with separate strata of coarse sand, silt and fine clay. Some of the strata above the tunnel in Segment II are located above the water level and require separate calculations. The strata located below the water level are comprised of fine clay, silt and fine sand. The strata above the water level are comprised of fine sand. The results of a weighted calculation of the physical parameters of the strata of segments I and II are shown in Table 2.

Based on the aforementioned parameters for the strata, different methods, including the Terzaghi method which does not take into consideration the impact of groundwater seepage, were used to perform a predictive analysis of the value of the water and soil pressure at the top of the tunnel. Calculations were performed according to the total stress method. The values for the water and soil pressure at the top of the tunnel obtained through these methods are shown in Table 3 and Figure 13. From an analysis of Figure 13, it is clear that the results from actual field measurements fall between the results of the fully-drained and non-drained conditions proposed in this paper while the results from calculations using the Dimitrios (2007) and Terzaghi methods have a small trend. For this project, the largest margin of error for the results obtained through this paper's calculation method is 5.17% while those of the DK and Terzaghi methods are nearly 80% and 34.63%, respectively. This shows that the calculation method proposed by this paper has good precision and validity and is able to effectively predict the water and soil load on the top of the tunnel.

## 6 Conclusion

The water and soil load on the top of the tunnel is an important parameter for the design of shield tunnels. This paper employs a theoretical analysis to construct a model for the water and soil load on the top of the marine segment of a shield tunnel under the conditions of long-term water seepage and applies it to evaluate the water and soil pressure on the Maliuzhou Waterway section of the Hengqin Tunnel. The following primary conclusions were obtained.

- The analytical model established by this paper for the water and soil load on the top of the tunnel is able to factor the effects of seepage force under conditions of long-term water seepage. Through a comparative analysis with actual field measurements, the Terzaghi total stress method, the DK effective stress method and other calculated results, it is clear that the margin of error for the results using this paper's calculation method is least, thus verifying the validity of our method.
- 2) A type of analytical model was established for the coefficient of lateral earth pressure that takes into consideration the principal stress arch effect. A verification through a comparative analysis with existing models indicates that this paper's model for the coefficient of lateral earth pressure is valid. Moreover, this paper reveals that as the angle of internal friction of the body of soil increases, the coefficient of lateral earth pressure first decreases then increases primarily due to the influence of the developing soil arching effect.
- 3) An impact analysis of relevant parameters shows that the water and soil load at the top of the tunnel has a positive correlation with the tunnel's depth-diameter ratio with a rate of increase that gradually falls off; it has a positive linear correlation with the density of the soil body and the water head at the outside of the shield segment and a negative linear correlation with the seepage volume per unit width.

## Data availability statement

The original contributions presented in the study are included in the article/supplementary material, further inquiries can be directed to the corresponding author.

## Author contributions

ZZ: Conceptualization, Methodology, Software. LC: Data curation, Writing—Original draft preparation. LMC: Software, Validation. QS: Writing—Reviewing and Editing.

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## Conflict of interest

The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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