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SPECIALTY SECTION
This article was submitted to
Geohazards and Georisks,
a section of the journal
Frontiers in Earth Science

RECEIVED 26 September 2022
ACCEPTED 27 October 2022
PUBLISHED 11 January 2023

CITATION
Yue L, Niu J, Ma Q, Zhao C, Cao M and
Yu B (2023), Research on direct shear
test of rock-like materials with two
closed pre-existing cracks of
different attitudes.
Front. Earth Sci. 10:1053630.
doi: 10.3389/feart.2022.1053630

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Research on direct shear test of rock-like materials with two closed pre-existing cracks of different attitudes

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To investigate the failure mode and strength characteristics of rock-like materials containing two non-coplanar closed discontinues, and the influence of crack attitude on the shear failure of rock mass, a series of direct shear tests are carried out on rock-like materials containing two pre-existing cracks of different attitudes, one of them is horizontal crack, and the other is inclined crack. The specimens containing pre-existing cracks of four inclinations (0°, 45°, 135°, and 180°) and three dip angles (30°, 60°, and 90°) are prepared, and the failure form and stress-displacement curve are recorded during the tests. The results show that the attitude of the crack has a significant effect on the failure form and strength characteristics. In positive shear, the shear stress increases slowly and the crack initiation of the crack occurs relatively late, and in negative shear, the shear stress increases rapidly and the crack initiation stage appears earlier. Under the normal stress of 1 MPa, the fracture surface fluctuates along the pre-existing cracks, and the difference in shear strength of each specimen is less than 1.0 MPa. Under the normal stress of 5 MPa, the fracture surface mostly distributes along the horizontal direction, and the difference in shear strength of each specimen is about 2.0 MPa. Under the same level of normal stress, the crack initiation and peak stress vary with the attitude of pre-existing crack, and the variation trend of peak stress is changed when the normal stress increased due to the difference in failure form. It is calculated that the ratio of crack initiation stress to peak stress ranges from 0.61 to 0.80.

KEYWORDS

direct shear test, two closed pre-existing cracks, attitude of crack, shear strength, crack initiation stress

Introduction

In rock engineering, the mechanical behavior of the structural plane has a significant influence on the deformation and failure of rock mass. The mechanism of discontinuity propagation and coalescence determines the failure form and strength characteristics of rock mass. Therefore, scholars began to deepen the study on the failure mechanism of rock mass with multiple cracks from the middle of the 20th century (Goodman et al., 1968; Toshikazu, 1988; Li and Zhu, 1992).

According to the shear failure theory of rock bridge proposed by Lajtai (1969), Shen et al. (1995) proposed two crack propagation modes, namely, wing crack caused by tensile stress and secondary crack caused by shear stress. It is pointed out that the relative position of the crack, that is, the angle between the connecting line of two adjacent ends of cracks and the shear direction, will have a great influence on the internal stress field and the failure mode of the rock mass. Wong et al. (1998, 2014) and Bobet et al. (1998) systematically classified the propagation and convergence modes of two fractures arranged at different positions under uniaxial compression.

A lot of laboratory experiments and numerical simulations have been carried out in the failure mechanism research of rock mass with multiple parallel cracks (Yang, 2013; Xiao, 2015). The results show that the peak strength and the final failure mode of rock mass will be affected by the dip angle, location and length of pre-crack and length of rock bridge, and a long rock bridge results in a complicated failure mode (Wong, 2015; Cao, 2016). Triaxial test results indicated that the initiation and propagation process of wing crack are controlled by confining pressure (Zhou, 2014). With the increase of confining pressure, the failure mode of cracked rock mass will change from tensile brittle failure to ductile failure (Zhou, 2015). Crack initiation mode transforms from shear crack to tensile crack as the brittleness index increases; the coalescence mode transforms from shear crack coalescence to the coalescence of tensile crack and shear crack; the failure mode transforms from shear failure to the mixed tension-shear failure, then to splitting failure as the brittleness index increases (Zhou, 2018). According to the slope of stress-displacement curve and the propagation process of cracks, the shear test can be divided into four or five stages: linear elastic stage, crack initiation stage, peak stage, post-peak stage, and residual stage. A serious compression-shear test research on rock mass with coplanar intermittent cracks are conducted by Hu et al. (2008), and shear strength calculation formulas of rock mass are established by weighted average method, considering the crack connectivity ratio as the weight. It is found that it is easier to form tensile failure when the rock bridge is relatively long, and easier to produce shear failure when it is short.

Direct shear tests of intermittent cracks are carried out, and the weakening laws of rock bridge in the shear process are revealed (Liu, 2010; Xia, 2010; Tang, 2012). Based on the direct shear test, a mechanical weakening model of rock

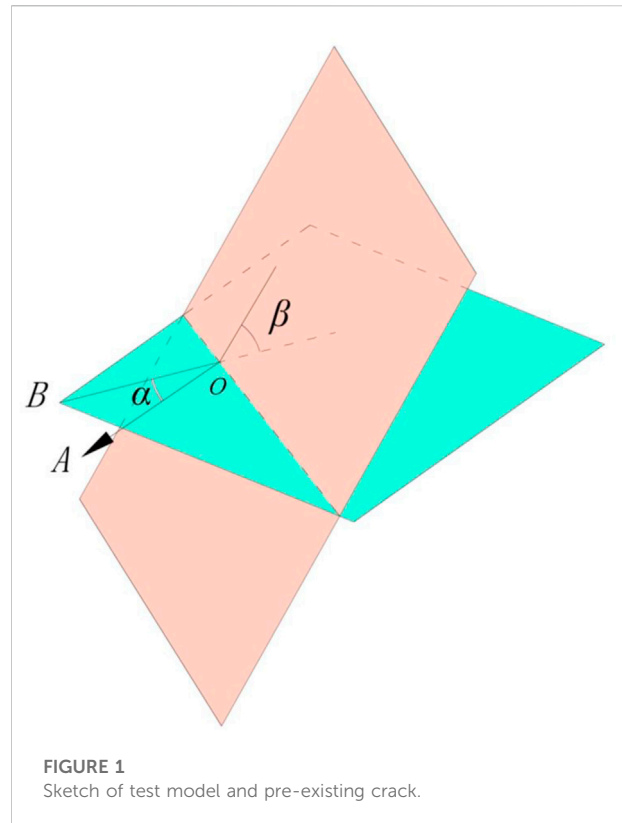
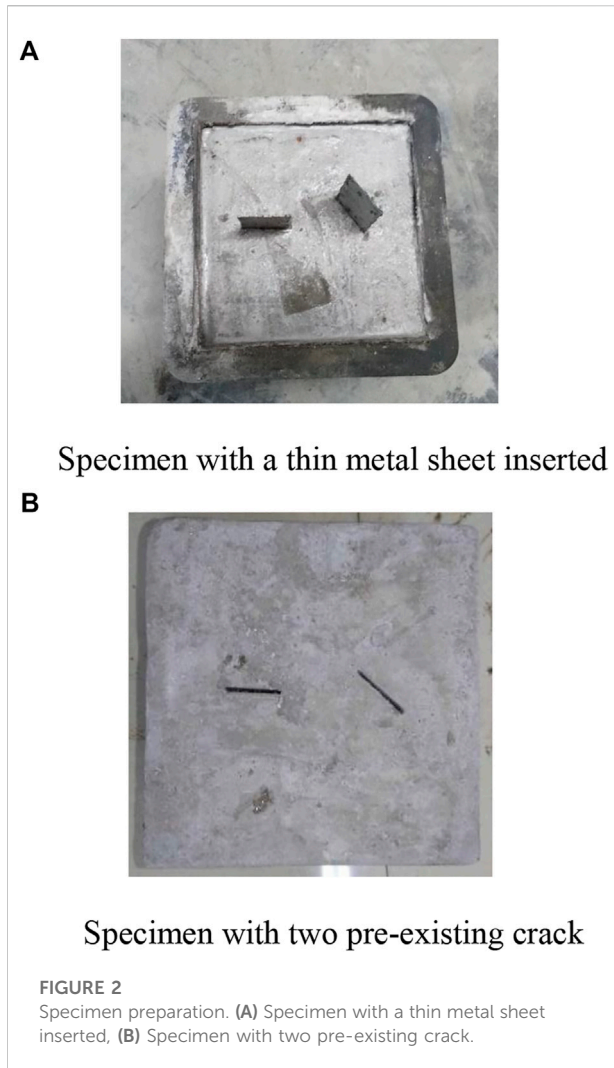


FIGURE 1
Sketch of test model and pre-existing crack.

bridge is established by introducing a weakening degree value δ to characterize the weakening degree of mechanical parameters of rock bridge. The calculation results are consistent with Jennings' internal friction strength criterion and the shear strength of non-cohesive rock bridge. The model not only explains the weakening mechanism of the rock bridge in microscopic view, but also corrects the Jennings shear strength criterion of non-persistent cracks by the parameters of equivalent cohesion and internal friction angle.

The fracture characteristics of anti-dip cracks under compression-shear load are studied in laboratory tests (Zhang et al., 2018). The results show that as the increase of pre-crack dip angle, three failure modes are obtained, and the shear strength first increases and then decreases. Uniaxial compression tests on rock-like materials with non-persistent cracks are carried out and stress-induced damage progression and acoustic emission (AE) are observed (Lee et al., 2011; Zhou, 2019; Cao et al., 2020; Zhou, 2021). The results show that the crack initiation stress and propagation path are affected by the included angle of pre-cracks. At the same time, it is found that multiple failure modes such as splitting, sliding, and mixing type are formed with the crack dip angle and length change. It is found that the process zone nucleation in granite are related to the clustering of grain-scale microcracks, and the clustering of microcracks is insignificant in the brittle failure of sandstone (Zhou, 2021). Triaxial compression tests on sandstone samples with pre-cracks



are carried out by [Huang et al. \(2016\)](#). It is obtained that the stress-strain curve of the samples fluctuant clearly; compared with the confining pressure, the distribution of pre-cracks has greater influence on the deformation, strength characteristics and failure mode of rock mass.

Furthermore, 3D cracking has been studied widely by a number of groups. Experimental studies of crack extension from flaws introduced into blocks of single-phase, dense resin materials were conducted by [Adams \(1978\)](#), the result suggest that the extension of secondary cracks may result in more damage. Fracture of rocks containing a multitude of pre-existing cracks is discussed by [Germanovich \(1994\)](#), and it is found that tear or shear type fracture mechanisms is related to the properties of the rock, the system of pre-existing cracks, and the type of loading. 3-D crack growth in compression was qualitatively different from the two-dimensional case. Several tests undertaken on samples with single internal cracks show that there are intrinsic limits on 3-D growth of wing cracks produced by a single pre-existing crack



FIGURE 3
Direct shear test equipment picture.

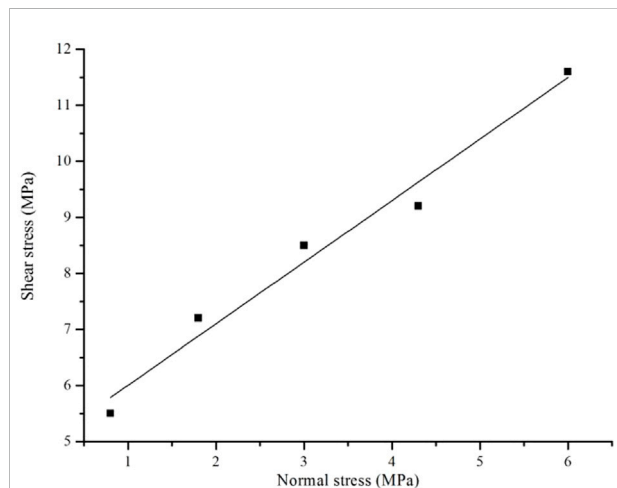


FIGURE 4
Shear stress-normal stress curve of intact specimen.

([Dyskin, 2003](#)). Dynamic laboratory tests are performed on normal-strength concrete and 3D-printed artificial rock samples with 3D embedded flaws, the results show that under high strain rate loading, wing cracks generated at 3D flaw tips lead to splitting failure of the sample, while shear cracks formed at 2D flaw tips result predominant shear failure of the sample ([Zhou et al., 2020](#)). The tests also show that higher strain rates produce smaller fragments due to specimen crushing ([Bi et al., 2020](#)).

A series of uniaxial compression experiments performed on sandstone specimens containing a pre-existing 3-D surface flaw indicate that, The generation of wing cracks, anti-wing cracks, and far-field cracks depend on the geometry of the pre-existing surface flaw, and flaw depth and flaw inclination influence the crack

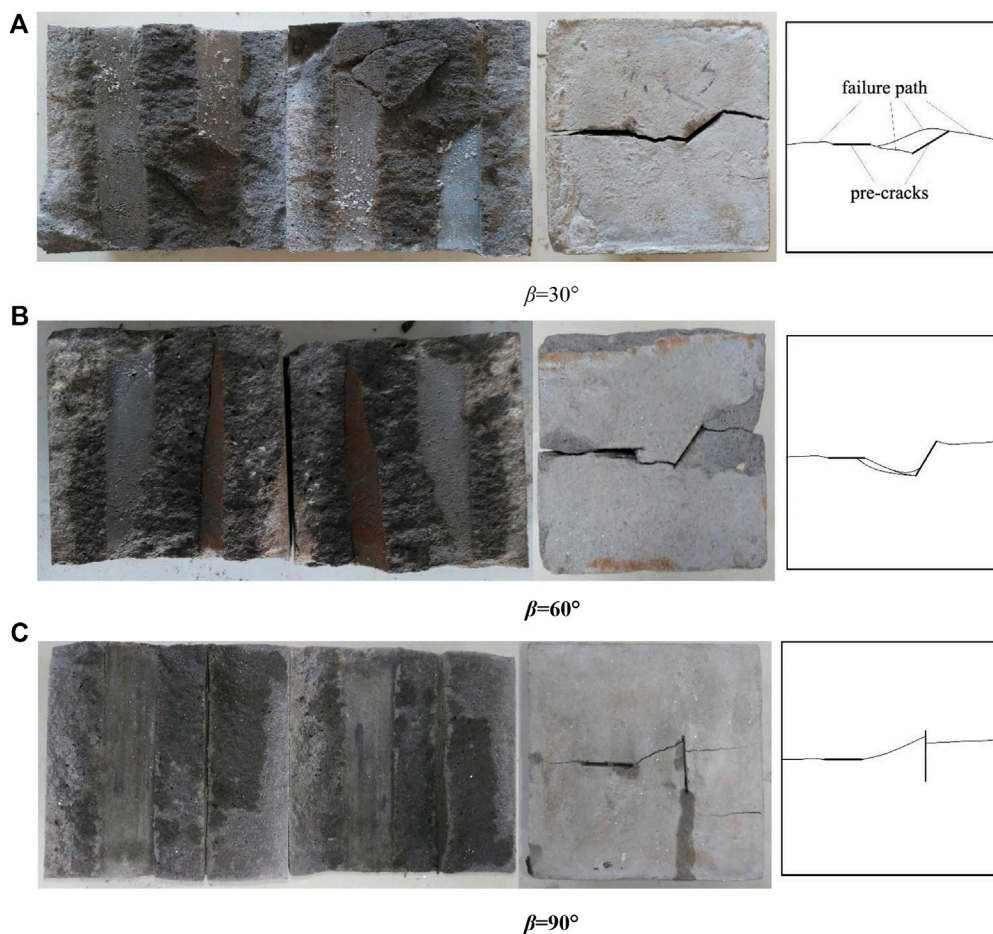


FIGURE 5
Shear failure surface and form of specimens under normal stress of 1 MPa ($\alpha = 0^\circ$). (A) $\beta = 30^\circ$, (B) $\beta = 60^\circ$, (C) $\beta = 90^\circ$.

initiation stress (Lu et al., 2015). Four modes of crack initiation and five modes of crack coalescence are observed in PMMA specimens with two 3D pre-existing cross-embedded flaws (Zhou, 2018). Three-dimensional printing (3DP) method was adopted to fabricate artificial rocks containing pre-existing 3D internal flaws, and the result show that the maximum crack propagation velocity in single flawed specimens is higher than that in double flawed samples. The continuous propagation of the secondary cracks developed after the peak stress lead to the failure of the flawed samples (Zhu, 2018; Zhou, 2019). In addition, crack propagation and coalescence behaviors in rock specimens containing pre-existing open flaws under uniaxial compression are investigated using the novel conjugated bond-based peridynamics (BB-PD), the BB-PD model is found to be effective for simulating rock fracture problems under compression, and the numerical results are in good agreement with the experimental observations (Wang, 2017).

The shear failure of rock mass with nonpersistent cracks is simulated with PFC^{2D} and PFC^{3D} by Yue et al. (2017). The

discrete element simulations demonstrate that the macro-scale shear zone resulted from the progressive failure of the tension-induced micro-cracks, and the proportion of rock bridge length on the shear plane has a significant effect on the failure mode; when the normal stress changes, different failure characteristics can be obtained in specimens; the generation rate of microcracks is significantly different at different loading stages.

Most of the researches on the shear failure of rock mass with multiple closed cracks focus on the propagation and connection law between multiple parallel cracks, and the influence of crack distribution on the failure mode.

When the rock mass contains multiple cracks of different inclinations and dip angles, the shear failure behavior and the propagation behavior of cracks need to be further studied, and the relationship between crack initiation shear stress and peak shear stress need to be fully discussed. In this study, the failure process of cracked rock mass with two pre-cracks of different attitudes under shear load is studied by laboratory direct shear test, and the influence of attitude on the shear failure mode and shear strength of rock mass

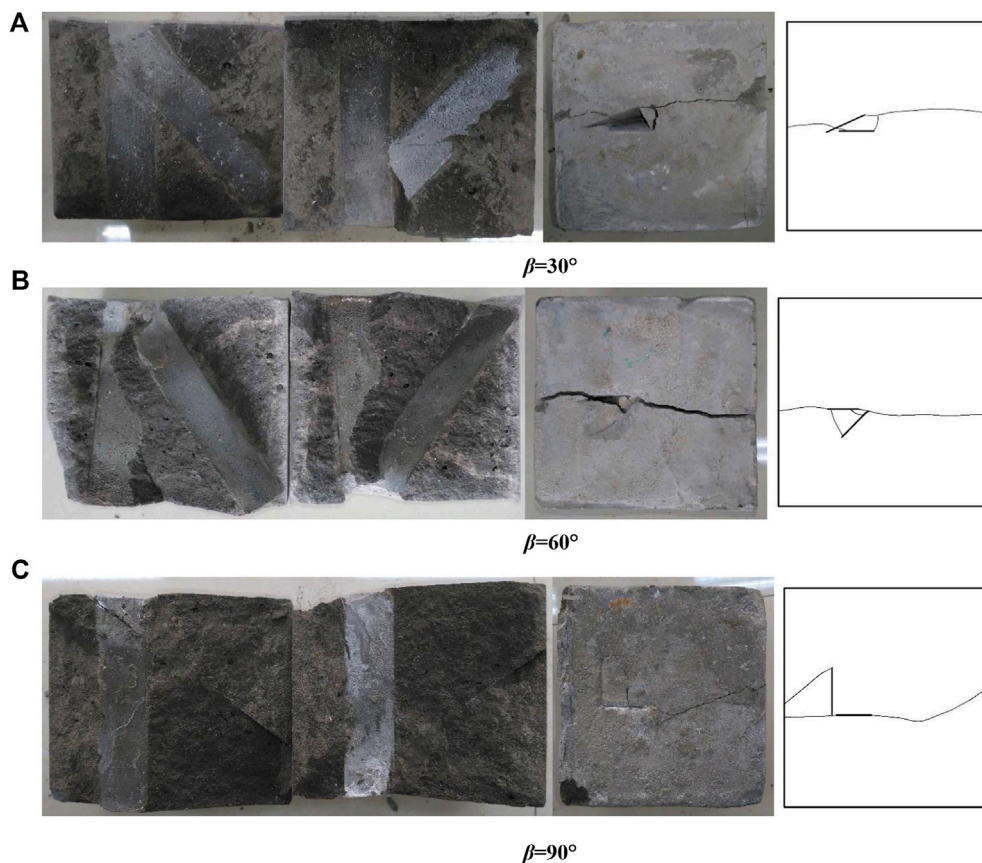


FIGURE 6
Shear failure surface and form of specimens under normal stress of 1 MPa ($\alpha = 45^\circ$). (A) $\beta = 30^\circ$, (B) $\beta = 60^\circ$, (C) $\beta = 90^\circ$.

is discussed. The ratio of crack initiation stress and peak shear stress in the tests will be obtained.

Laboratory test programs

Specimen design

The direct shear test is carried out on the specimen sized 150 mm \times 150 mm \times 150 mm with two pre-existing cracks. The length of the two pre-existing cracks is 30 mm, and the opening width is less than 1 mm. The first of them is a horizontal crack, the second is an inclined crack, and change the inclination and dip angle of the second crack in different specimens. As shown in Figure 1, O-A represents the loading direction of the upper shear box, as well as the 0° inclinations; O-B represents the inclination of the second crack, recorded as α ; the angle between the second crack and the horizontal plane is recorded as the dip angle β . The attitude of the second crack can be controlled by changing the value of α and β . Four angles of $\alpha = 0^\circ, 45^\circ, 135^\circ$, and 180° and three angles of $\beta = 30^\circ, 60^\circ$, and 90° are selected to study the influence of crack

attitude on the shear failure process. To study the effect of normal stress on the shear failure process of multiple cracks, two normal loads of 1.0 and 5.0 MPa are applied.

Specimen preparation

The two intermittent cracks are simulated by pre-cracks in specimens which are made of similar materials. By mixing cement, fine sand, and water in the ratio of 1:1:0.4 (Zhao, 2012), rock-like material specimens were made for laboratory test. Meanwhile, the closed pre-cracks of different attitudes can be made by the following two steps: 1) insert a thin metal sheet into the specimen during the initial setting period (as shown in Figure 2A); 2) Pull it out before the end of the initial setting. Then a rock-like specimen with two pre-cracks of different attitudes is accomplished (as shown in Figure 2B).

Direct shear tests are carried out on intact specimens under different normal stresses (as shown in Figure 3), and the shear strengths of each specimens are obtained and plotted in Figure 4. The linear equation in Figure 4 is obtained by fitting as follows:

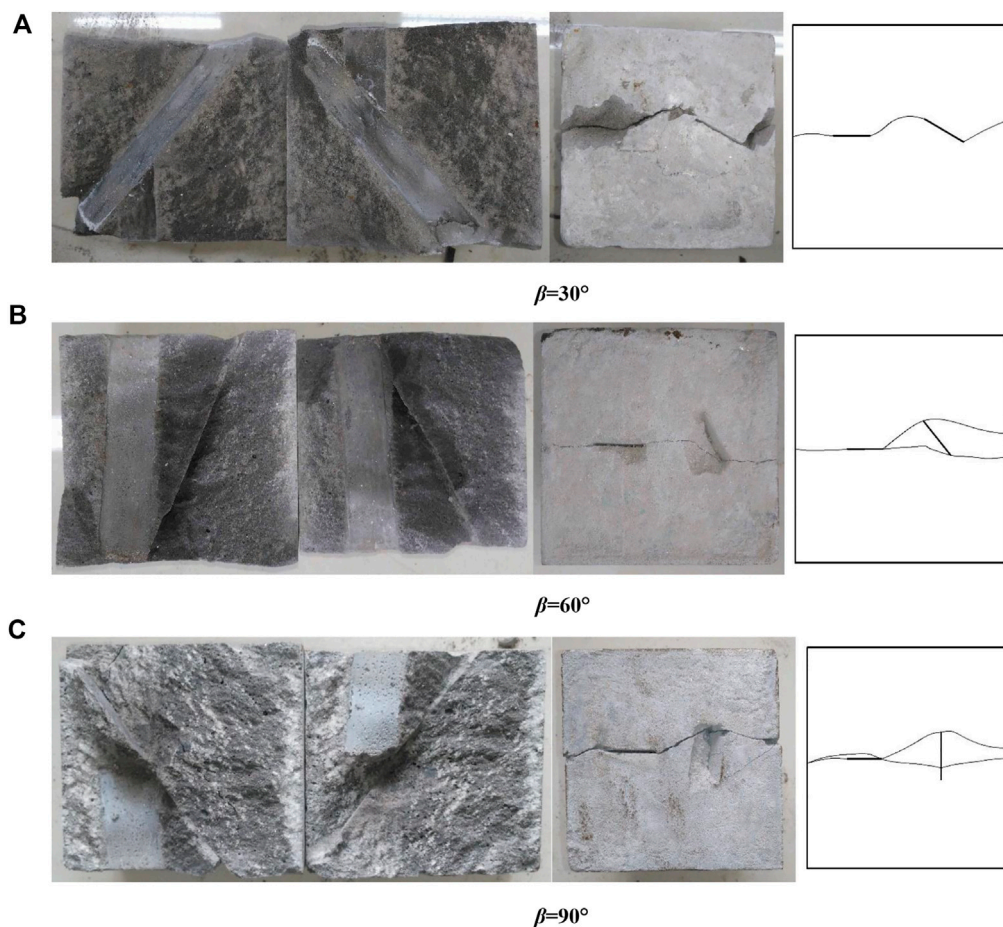


FIGURE 7
Shear failure surface and form of specimens under normal stress of 1 MPa ($\alpha = 135^\circ$). (A) $\beta = 30^\circ$, (B) $\beta = 60^\circ$, (C) $\beta = 90^\circ$.

$$\tau = 0.94\sigma + 4.70 \quad (1)$$

where σ is the normal stress, MPa; τ is the shear strength of specimens, MPa. The results show that the cohesion c is 4.70 MPa, and the internal friction angle φ is 43.2° for the intact specimen. The direct shear test equipment is shown in Figure 3, and shear stress and shear displacement are recorded and curves are drawn during the test.

The results of direct shear test

Direct shear test results under normal stress of 1 MPa

With the normal stress of 1 MPa, shear tests are carried out on specimens with two different attitude pre-cracks. The shear fracture surface and failure character of each specimen are

recorded, and the typical failure path sketches are drawn, as shown in Figures 5–8.

As shown in Figure 5, the failure forms of the horizontal crack of each sample are mostly the same, all specimens fractured along the horizontal cracks, and the fracture surface is relatively flat. On the other side, some different phenomena are obtained in the failure form of inclined pre-cracks. The failure modes, shear failure occurs along the two pre-cracks, are both observed in the specimens of $\alpha = 0^\circ$, $\beta = 30^\circ$, and $\alpha = 0^\circ$, $\beta = 60^\circ$. However, the fracture surface cut through the vertical crack in the specimen of $\alpha = 0^\circ$, $\beta = 90^\circ$. The failure surface of the rock bridge is comparatively rough in these specimens, and no obvious scratches and debris are observed, which indicates that the fracture in the rock bridge is mainly tension failure.

The fractured specimens of $\alpha = 45^\circ$ are shown in Figure 6. It can be observed that the specimens of $\alpha = 45^\circ$, $\beta = 30^\circ$ and $\alpha = 45^\circ$, $\beta = 60^\circ$ fracture along the two cracks, and the fluctuation of the failure surface is consistent with pre-cracks. Part of the rock bridge fracture surface is relatively rough, mainly tensile failure.

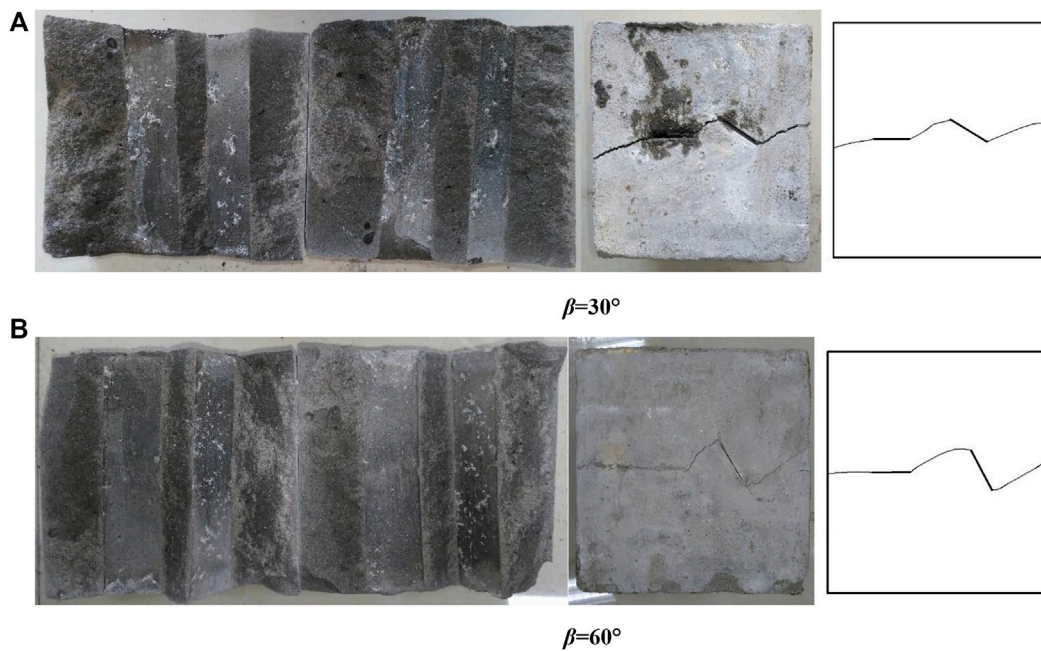


FIGURE 8 Shear failure surface and form of specimens under normal stress of 1 MPa ($\alpha = 180^\circ$). (A) $\beta = 30^\circ$, (B) $\beta = 60^\circ$.

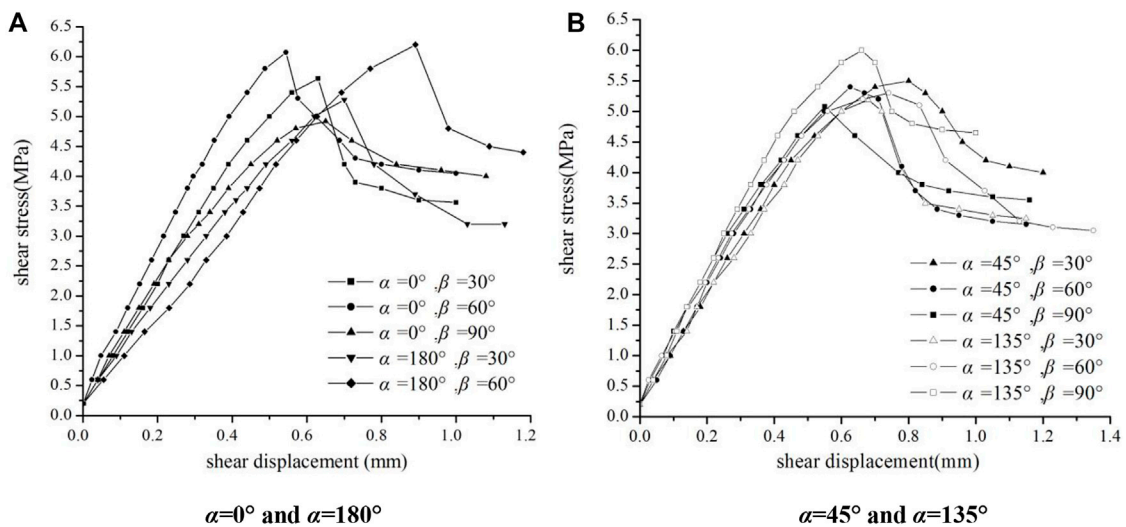


FIGURE 9 Shear stress-shear displacement curve (normal stress is 1 MPa). (A) $\alpha = 0^\circ$ and $\alpha = 180^\circ$, (B) $\alpha = 45^\circ$ and $\alpha = 135^\circ$.

The specimens of $\alpha = 45^\circ, \beta = 90^\circ$ fracture along the horizontal crack, and no separation and dislocation occurred in the vertical crack. The failure surface is relatively flat with slight fluctuations.

The fractured specimens of $\alpha = 135^\circ$ are shown in Figure 7. In the specimens of $\alpha = 135^\circ$, all fracture occurs along the inclined

pre-cracks. Obvious scratches are formed on the fracture surface of the rock bridge. Affected by the inclined crack, the horizontal crack is not separated completely, and the failure surface fluctuation is mainly controlled by the attitude of the inclined crack. For the samples of $\alpha = 135^\circ, \beta = 90^\circ$, part of the shear

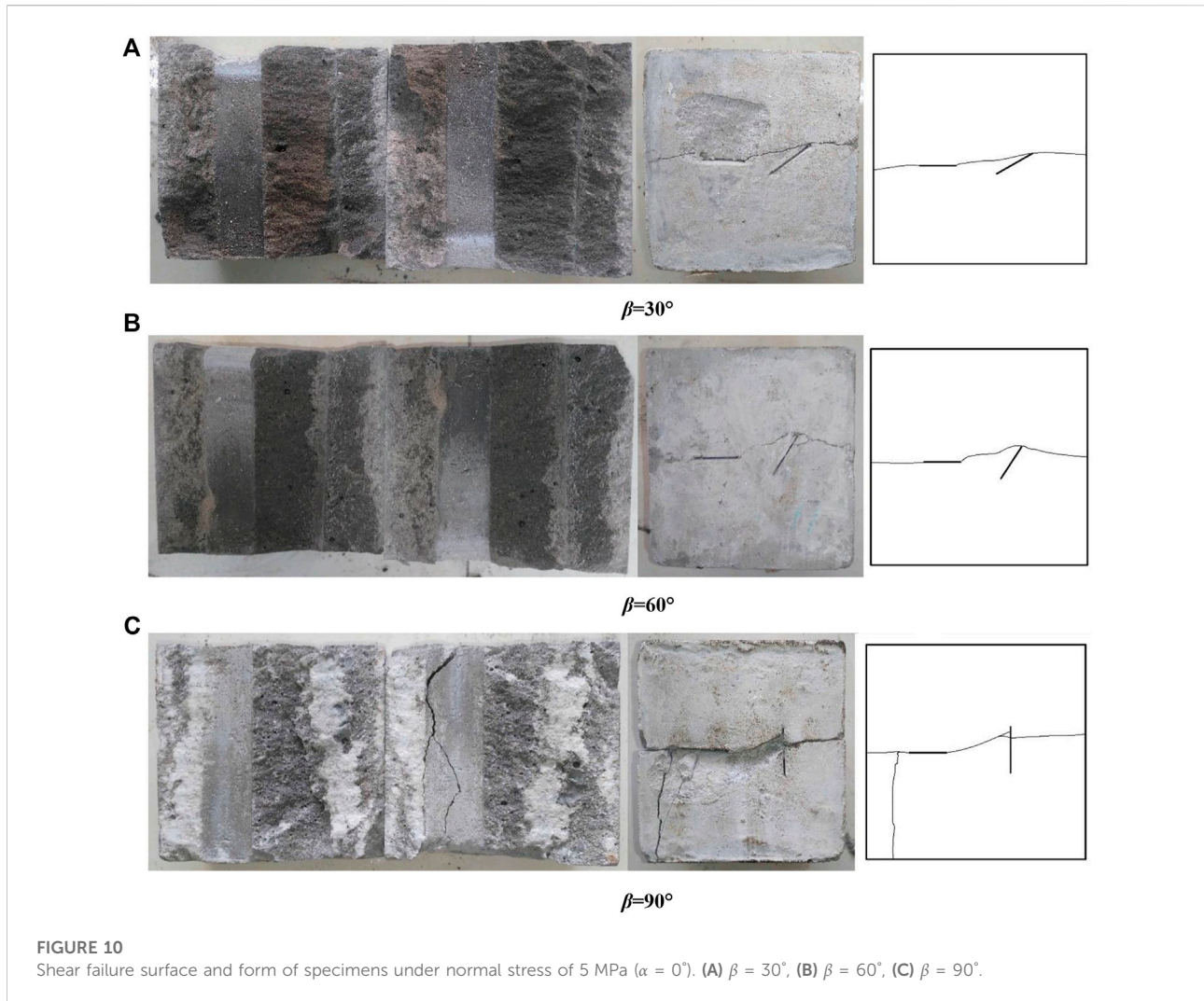


FIGURE 10
Shear failure surface and form of specimens under normal stress of 5 MPa ($\alpha = 0^\circ$). (A) $\beta = 30^\circ$, (B) $\beta = 60^\circ$, (C) $\beta = 90^\circ$.

surface is distributed along the horizontal and vertical cracks, while the other part is cut through the rock bridge *via* the end of the vertical crack, with some undulation on the fracture surface.

The fractured specimens of $\alpha = 180^\circ$ are shown in Figure 8. Shear failure modes of the two specimens are the same when $\alpha = 180^\circ$. The shear fracture surface distributes along the two pre-cracks, and no crush zone is observed on the surface, but there is an obvious appearance of scratch. The phenomenon of climbing effect occurs during the shear test. The rock bridge fractures along the connecting line of the adjacent ends of two cracks, and the failure surface fluctuates with the attitude of pre-cracks.

It is found that the strike of the inclined crack is perpendicular to the shear direction for the specimens of $\alpha = 0^\circ$ and $\alpha = 180^\circ$, and the shear failure process is quite different because of the attitude of crack. According to the fracture surface, the failure mode of negative shear is mainly tensile failure, while that of positive shear is mainly shear failure, with climbing and gnawing effect at the same time. According to the view of the

failure path, the failure mode of rock bridge is to connect the adjacent ends of two cracks with a straight path, and the failure path of specimens distribute along the two pre-existing cracks; the specimen will fracture along the horizontal direction when the inclined crack is upright.

In the specimens of $\alpha = 45^\circ$ and $\alpha = 135^\circ$, the propagation and coalescence form of the pre-existing crack is almost the same. According to the fracture surface, shear deformation is observed in both cracks when $\beta = 30^\circ$, and the scratch on the surface is obvious. The failure surface morphology is controlled by the attitude of the inclined crack when $\beta = 60^\circ$, and the specimen is deformed partially or wholly along the inclined crack. The scratch is less and the fracture mode of rock bridge is mainly tensile failure when $\beta = 60^\circ$. More scratches occur on the fracture surface of the specimens of $\beta = 90^\circ$, and the grinding effect is obvious. The fracture paths of these samples are relatively complex, and undulation of fracture surface is controlled by the inclined pre-crack. The difference of fracture paths between

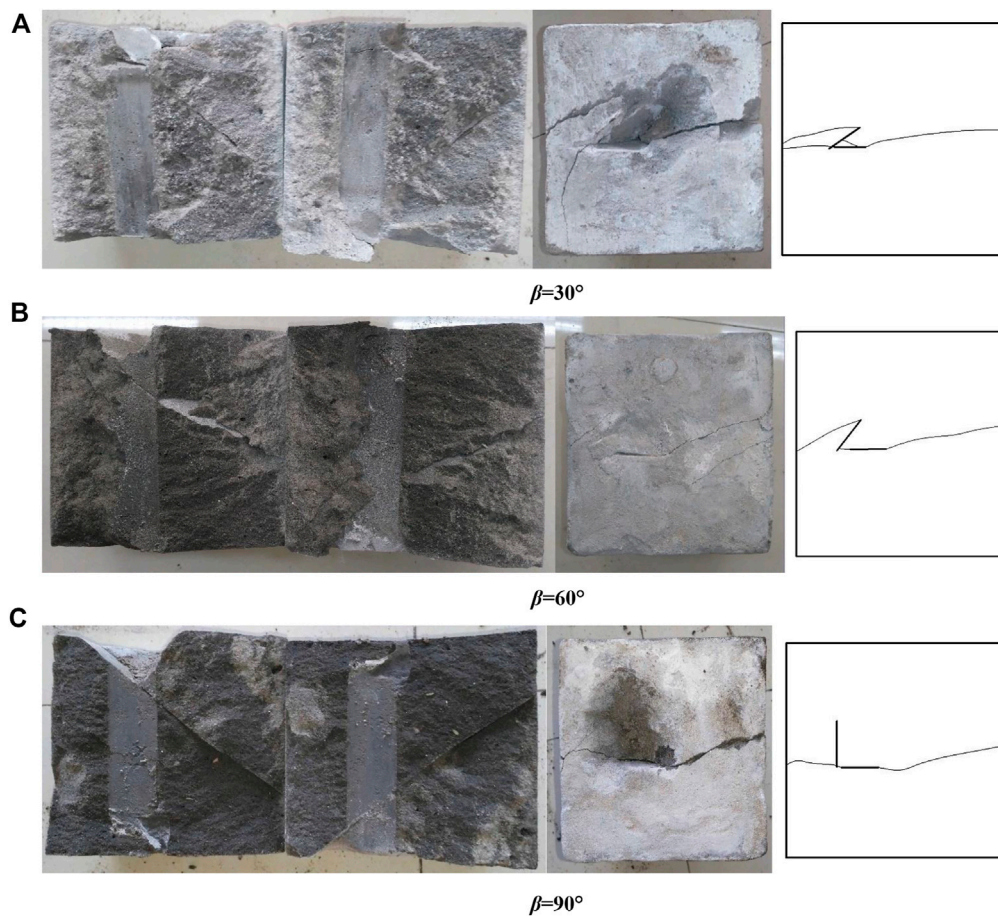


FIGURE 11

Shear failure surface and form of specimens under normal stress of 5 MPa ($\alpha = 45^\circ$). (A) $\beta = 30^\circ$, (B) $\beta = 60^\circ$, (C) $\beta = 90^\circ$.

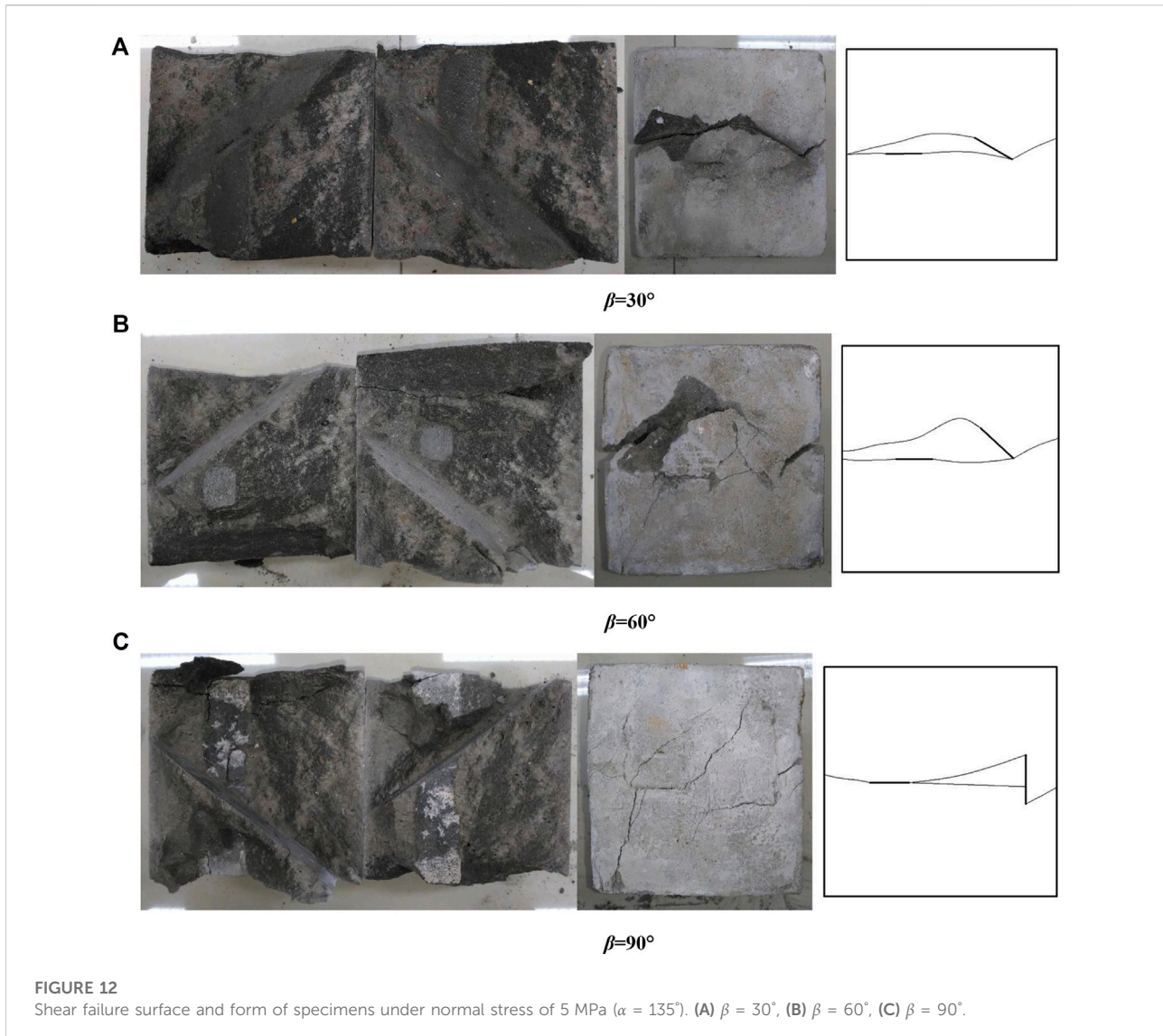
specimen of $\alpha = 45^\circ, \beta = 90^\circ$ and $\alpha = 135^\circ, \beta = 90^\circ$ is caused by the relative positions of loading boundary and structural plane.

With the normal stress of 1 MPa, the shear stress-shear displacement curve obtained from the test is shown in Figure 9. It is indicated that the curve of each specimen can be divided into four stages: elastic stage, crack initiation stage, peak stage, and residual stage. In elastic stage, the shear stress increases linearly with the shear displacement; then the slope of the curve gradually decreases in crack initiation stage, indicating that microcracks are generated in the sample; in the peak stage, the shear stress reaches the maximum, then decreases gradually; finally, shear stress reduced to residual strength, and the specimen is cut through by the fracture surface. When $\alpha = 0^\circ$ and $\alpha = 180^\circ$, the shear stress-shear displacement curves of the specimen are quite different, which is mainly reflected in the differences in the appearance of peak strength, and the slope of the curve in elastic stage. During elastic stage, the slope of the shear stress-shear displacement curve is lower when $\alpha = 180^\circ$, the shear stress increases slightly, and the crack initiation occurs

relatively late. On the contrary, the shear stress rises rapidly when $\alpha = 0^\circ$, and crack initiation occurs earlier. The crack initiation stage of $\alpha = 0^\circ, \beta = 60^\circ$ specimen is shorter, and the peak shear stress appears earlier. In addition, the crack initiation stage of $\alpha = 0^\circ, \beta = 30^\circ$ specimen is relatively longer. As shown in Figure 9A, the shear strength of specimens $\alpha = 180^\circ, \beta = 60^\circ$ and $\alpha = 0^\circ, \beta = 60^\circ$ is higher, while specimens $\alpha = 0^\circ, \beta = 90^\circ$ is lower.

The shear stress rises rapidly with the increasement of shear displacement when negative shear, while the slope of the curve in elastic stage is lower when positive shear. It is indicated that the pre-crack is further closed by the compression and shear stress in the case of positive shear, which leads to greater shear displacement in the elastic stage. In negative shear, part of the fracture surface does not cut through the pre-crack, but the inner of the rock-like material, so the slope of curve is larger during the elastic stage.

Compared with Figure 9A, the difference of shear stress-shear displacement curves between the specimens of $\alpha = 45^\circ$ and $\alpha = 135^\circ$ is smaller. The slope of the curve in elastic stage of the specimen $\beta = 90^\circ$ is smaller, and the peak stress appears earlier, while the peak



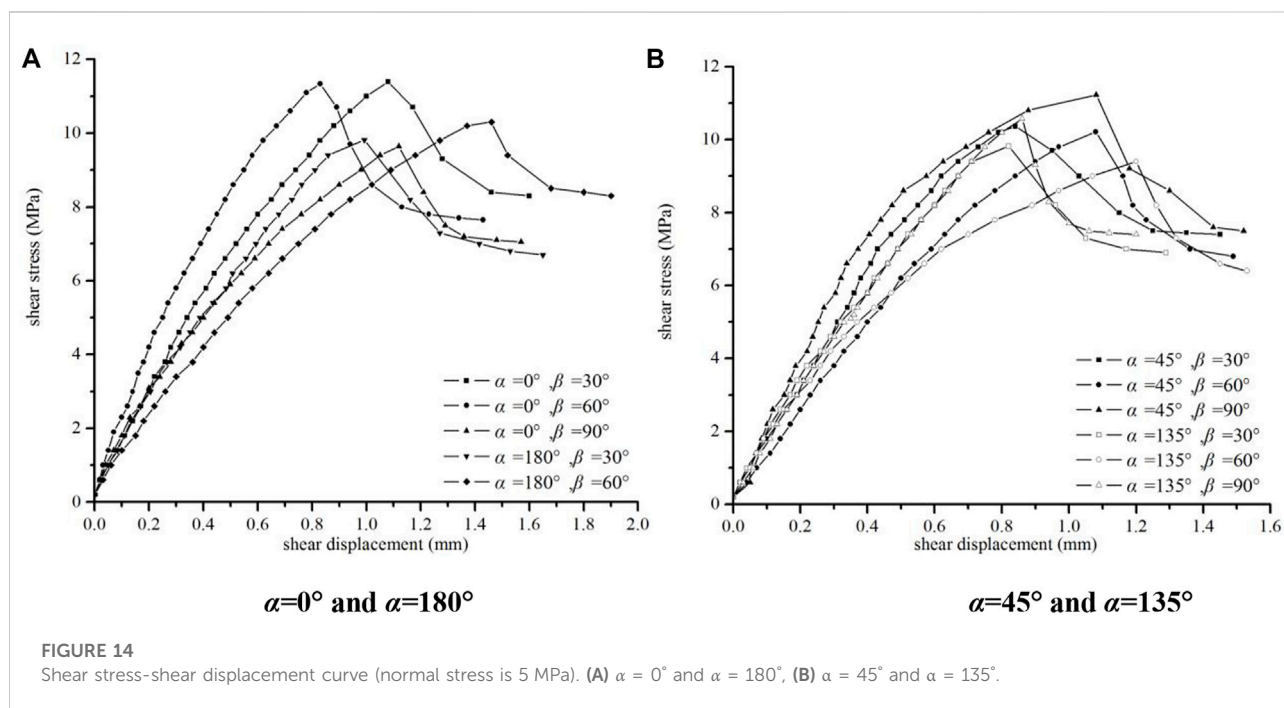
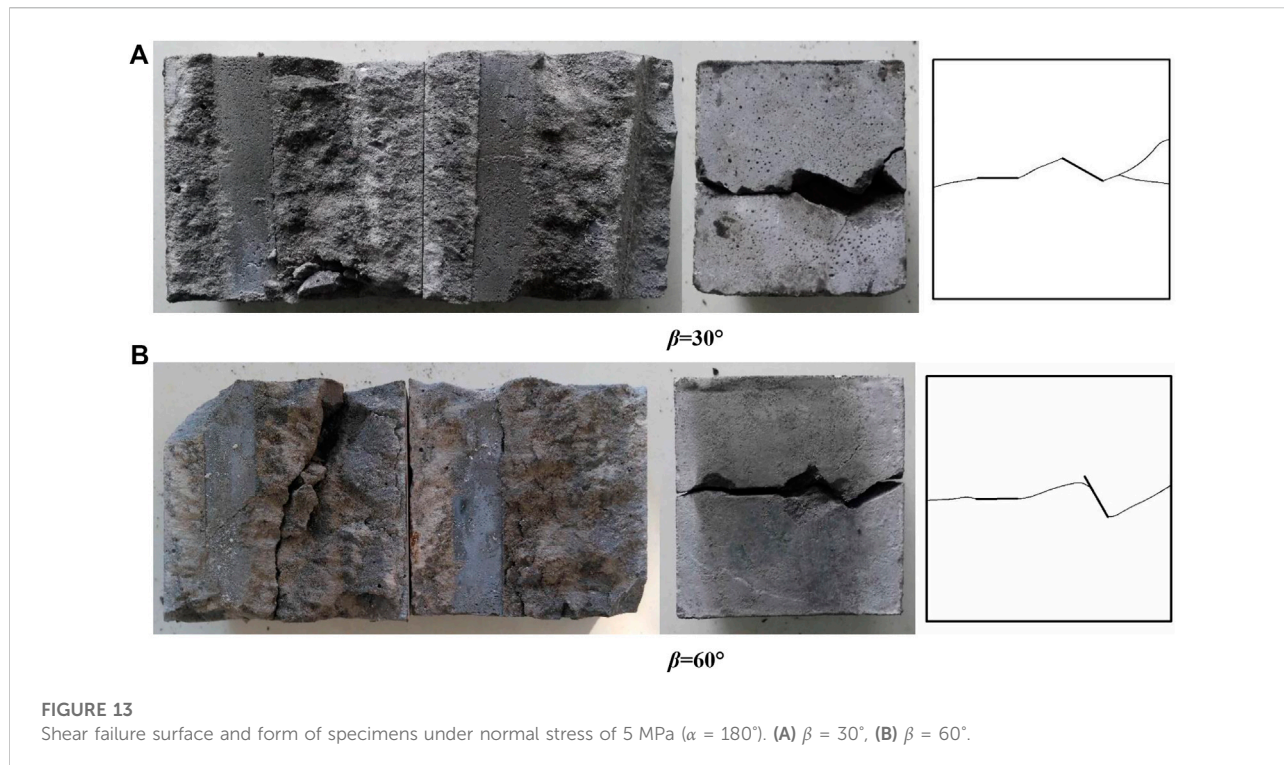
stress of the specimen $\beta = 30^\circ$ appears later. In terms of shear strength, the strength of each sample is similar in this group. With the normal stress of 1 MPa, the shear strength is 5.2–6.0 MPa, and the strength is higher when $\beta = 90^\circ$. The results show that the peak strength of each sample is almost the same, and the corresponding displacement range of each stage is slightly different. The influence of dip angle of pre-existing crack on the shear strength is weakened, but the influence of inclination is increased.

Direct shear test results with normal stress of 5 MPa

Direct shear tests are carried out on each specimen with the normal stress of 5 MPa, and the failure mode of the specimens obtained is shown in Figures 10–13.

The fractured specimens of $\alpha = 0^\circ$ are shown in Figure 10. With the increase of normal stress, the failure mode of the specimens $\alpha = 0^\circ$ is different from Figure 5. No relative displacement occurs along the inclined crack, and the failure path connects the farther end of the inclined crack and the horizontal crack. The fracture surface is nearly horizontal distribution without fluctuation overall. There are obvious scratches on the fracture surface, which are mainly concentrated near the pre-existing crack. Besides, a significant grinding effect is observed in the rock bridge.

The fractured specimens of $\alpha = 45^\circ$ are shown in Figure 11. The fracture surface of the specimen $\alpha = 45^\circ$ is nearly horizontal distribution, and no separation and displacement occur in the inclined crack. The attitude of the crack has little effect on the failure form in this group



specimen. There are obvious scratches on the failure surface, and some wedges are formed in the intersection of the two cracks.

The fractured specimens of $\alpha = 135^\circ$ are shown in Figure 12. The fracture surface is significantly affected by the inclined crack. Separation and displacement are both occurring within the two

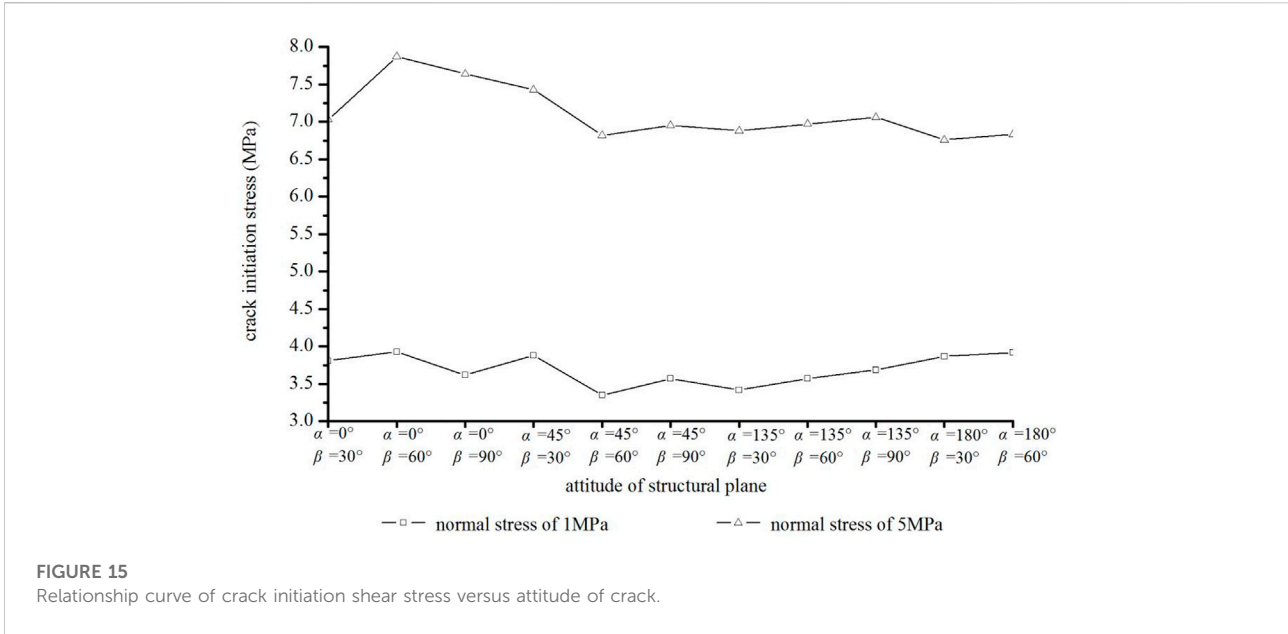


FIGURE 15
Relationship curve of crack initiation shear stress versus attitude of crack.

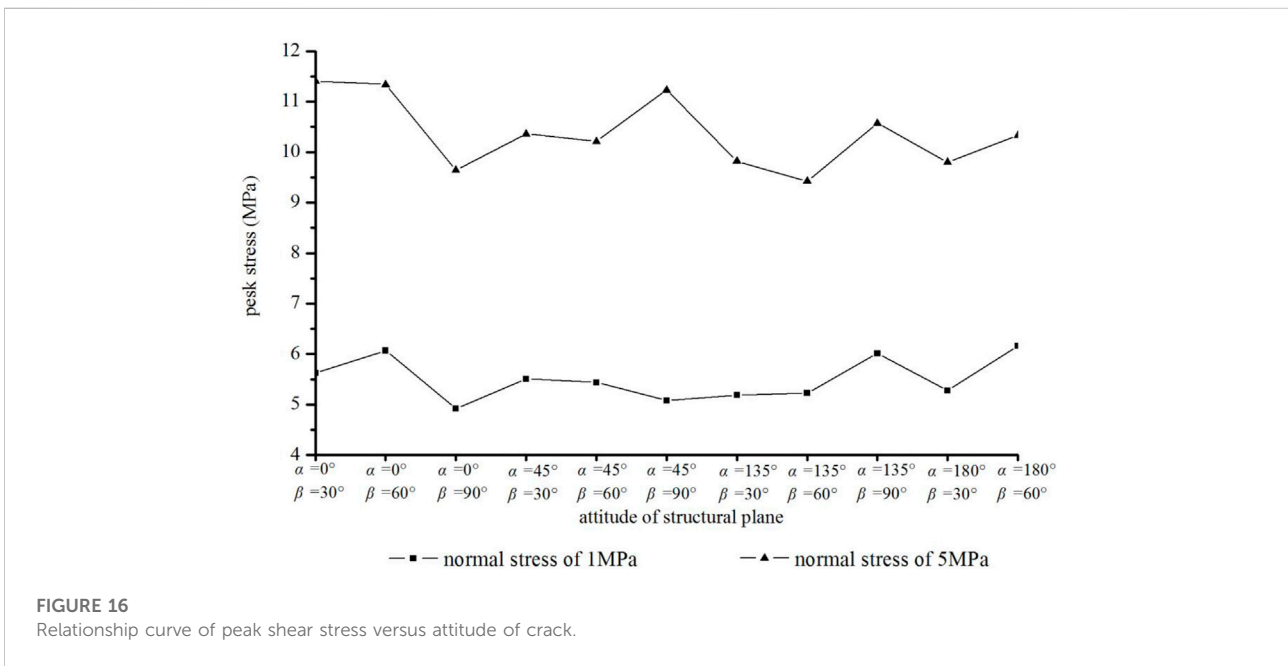


FIGURE 16
Relationship curve of peak shear stress versus attitude of crack.

pre-existing crack. The failure surface fluctuates along the attitude of the crack, and the scratches and crush zone are clearly observed on the failure surface.

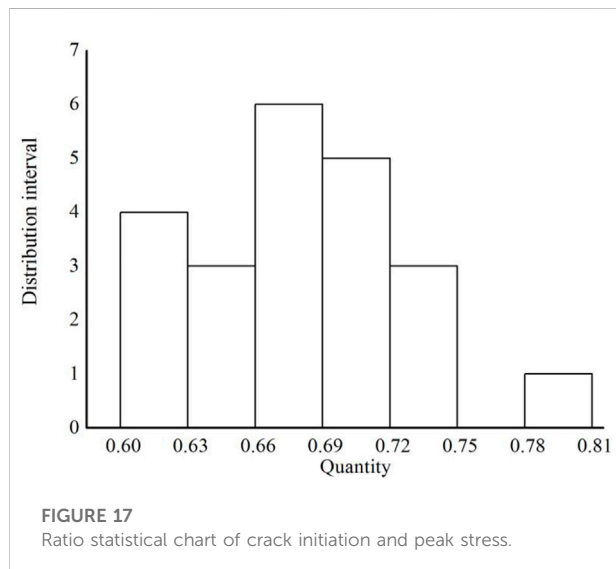
The fractured specimens of $\alpha = 180^\circ$ are shown in Figure 13. Under the normal stress of 5 MPa, the failure forms of the two specimens are similar. The failure form of the inclined crack is grinding and crushing rather than relative displacement, with a large number of scratches and obvious dilatancy. The failure path of the rock bridge is initially controlled by the inclined crack,

which has some fluctuation, and then gradually changes to the horizontal direction after grinding and crushing.

The shear stress-shear displacement curves of the specimens are shown in Figure 14 when the normal stress increases to 5 MPa. The curves of the specimens are similar to that of the specimens under normal stress of 1 MPa when $\alpha = 0^\circ$ and 180° , with the increasing in shear strength. The strength of specimens $\alpha = 180^\circ, \beta = 30^\circ$ and $\alpha = 0^\circ, \beta = 90^\circ$ is relatively low. As the specimen do not fracture along the inclined crack in negative shear, and the fracture path runs through

TABLE 1 Ratio of crack initiation and peak stress for each specimen.

Inclination α (°)	Dip angle β (°)	Normal stress (MPa)	
		1	5
0	30	0.677	0.617
	60	0.647	0.694
	90	0.736	0.793
45	30	0.704	0.717
	60	0.616	0.668
	90	0.703	0.619
135	30	0.659	0.701
	60	0.683	0.740
	90	0.614	0.668
180	30	0.733	0.690
	60	0.636	0.661



the inner of specimen, so the shear stress rises rapidly in elastic stage, and the crack initiation stage is relatively short, which result in an earlier appearance of the peak stress and a higher shear strength. In positive shear, the shear stress rises slowly and the peak stress appears relatively later after the displacement and grinding of the inclined crack. The shear strength of the specimens is 9.6–11.4 MPa.

The shear stress-shear displacement curves of specimens $\alpha = 45^\circ$ and $\alpha = 135^\circ$ are similar under the normal stress of 5 MPa, and the shear strength of specimens $\beta = 90^\circ$ is relatively high, which is due to the fact that no relative displacement occurs in the vertical crack, and the specimen fracture along the horizontal crack. From the shear strength curve and the fracture surface, it can be observed that the shear strength of $\alpha = 45^\circ$ specimen is

slightly higher than that of $\alpha = 135^\circ$, it is because that the area of the pre-crack on the fracture surface is larger in $\alpha = 135^\circ$ specimen, and the shear resistance to overcome is smaller, so the shear strength is relatively lower.

Comparison of crack initiation stress and peak strength under different normal stresses

Under the normal stresses of 1 and 5 MPa, the crack initiation and peak shear stress of the specimens are shown in Figures 15, 16. It is indicated that under the same level of normal stress, the crack initiation shear stress of each specimen is relatively close, and the difference is less than 1.0 MPa, while the difference of peak shear stress is 1.0–3.0 MPa. Furthermore, the relationship between the crack initiation stress and the peak stress of each sample varies with the attitude of the crack, that is, the peak stress of the specimen with larger crack initiation stress is not necessarily higher, and the strength relationship of each specimen is different under the two-level normal stress.

Figure 15 shows that under the same normal stress, the crack initiation shear stress of each sample is similar. The stress of $\alpha = 45^\circ$ and $\alpha = 135^\circ$ specimens is lower, while that of the specimen $\alpha = 0^\circ$ and $\alpha = 180^\circ$ is higher. It is because that the pre-crack intersects the shear direction at a small angle when $\alpha = 45^\circ$ and $\alpha = 135^\circ$, which conducive to shear failure. With the increment of normal stress, the variation trend of the curve is almost the same, but the fluctuation becomes more severe.

Figure 16 shows that the difference in peak stress of each sample is obvious. When the normal stress is 1 MPa, the strength of specimen $\alpha = 0^\circ$, $\beta = 30^\circ$, and 60° is higher, while the strength of specimen $\alpha = 0^\circ$ and $\beta = 90^\circ$ is lower, with a difference of about 1.2 MPa. When the normal stress rises to 5 MPa, the peak stress difference increases to 2.0 MPa due to the change in failure mode of some specimens, and the variation trend of peak stress curve is changed. In general, the shear strength of $\alpha = 45^\circ$ and $\alpha = 135^\circ$ specimens is slightly higher.

To study the relationship between crack initiation and peak stress of each specimen, the ratio of the above two stress for each specimen is calculated and listed in Table 1.

It can be found from the table that the ratio of crack initiation and peak shear stress of each specimen ranges from 0.61 to 0.80, the minimum value is 0.614, which appears in the specimen $\alpha = 135^\circ$, $\beta = 90^\circ$, and the maximum value is 0.793, which appears in the specimen $\alpha = 0^\circ$, $\beta = 90^\circ$. Drawing the above ratios into a columnar statistical chart (as shown in Figure 17), it can be found that the ratio of the initial crack stress to the peak stress is mainly concentrated between 0.60 and 0.75, which has a certain statistical law. According to the crack initiation stress of the rock-like material, the peak shear strength of can be estimated (Bobet and Einstein, 1998, Lajtai, 1969, Yin et al., 2014, Zhou et al., 2013).

Conclusion

Based on the laboratory direct shear test, the crack propagation and strength law of rock-like materials with two closed cracks under shear load are studied, and the failure form and load-displacement curves are recorded and compared. The conclusions of this research are listed as follows:

- (1) Under the normal stress of 1 MPa, the attitude of the crack has a significant effect on the shear failure form. In positive shear, with the increasing of shear displacement, the shear stress increases slowly and the crack initiation of the crack occurs relatively late, and the sliding of pre-cracks is the main failure form. Otherwise, in negative shear, the shear stress increases rapidly and the crack initiation stage appears earlier, and the tensile failure is dominant. The difference in shear strength is less than 1.0 MPa.
- (2) Under the normal stress of 5 MPa, the specimen $\alpha = 135^\circ$ fractures along the inclined crack, and the fracture surface fluctuates greatly. The rest of the specimens fracture along the horizontal direction. In negative shear, the shear stress rises rapidly and the peak stress appears early, and the crack initiation stage is relatively short. In positive shear, as the sliding and grinding of the crack, the dilatancy is distinct during the shear test. The difference in shear strength is about 2.0 MPa.
- (3) Under the same level of normal stress, the difference of crack initiation stress of each specimen is about 1.0 MPa, and the difference of peak stress is about 1.0–3.0 MPa. When the normal stress increases, the variation trend of crack initiation stress with the attitude of the crack is almost the same, but that of the peak strength is different due to the change in the failure form of specimen.
- (4) The ratio of crack initiation stress to peak stress ranges from 0.61 to 0.80, and the ratio is slightly different in each specimen under the same normal stress.

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Data availability statement

The original contributions presented in the study are included in the article/supplementary material, further inquiries can be directed to the corresponding author.

Author contributions

LY: Drafting the manuscript. JN: laboratory test. QM: data analysis. CZ: laboratory test. MC: laboratory test. BY: Reviewing and editing.

Funding

This work was supported by the Natural Science Foundation of Jiangsu Higher Education Institutions of China (Grant No. 19KJD410001), QingLan Project of Jiangsu Province, Campus-level research projects of Changzhou Vocational Institute of Engineering: 11130300121008.

Conflict of interest

The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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