



A Study to Investigate the Viscosity Effect on Micro-Confined Fluids Flow in Tight Formations Considering Fluid–Solid Interaction

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Chen M, Li Q, Cheng L, Wang X, Lyu C and Fan Q (2021) A Study to Investigate the Viscosity Effect on Micro-Confined Fluids Flow in Tight Formations Considering Fluid–Solid Interaction. Front. Earth Sci. 9:795842. doi: 10.3389/feart.2021.795842 Understanding different fluids flow behavior confined in microscales has tremendous significance in the development of tight oil reservoirs. In this article, a novel semiempirical model for different confined fluid flow based on the concept of boundary layer thickness, caused by the fluid–solid interaction, is proposed. Micro-tube experiments are carried out to verify the novel model. After the validation, the viscosity effect on the flow rate and Poiseuille number considering the fluid–solid interaction is investigated. Furthermore, the novel model is incorporated into unstructured networks with anisotropy to study the viscosity effect on pore-scale flow in tight formations under the conditions of different displacement pressure gradients, different aspect ratios (ratio of the pore radius to the connecting throat radius), and different coordination numbers. Results show that the viscosity effect on the flow rate and Poiseuille number after considering the fluid–solid interaction induces a great deviation from that in conventional fluid flow. The absolute permeability is not only a parameter related to pore structures but also depends on fluid viscosity. The study provides an effective model for modeling different confined fluid flow in microscales and lays a good foundation for studying fluid flow in tight formations.

Keywords: flow rate, Poiseuille number, unstructured network, absolute permeability, aspect ratio, coordination number

INTRODUCTION

Tight oil reservoirs have played a dominant role in the development of the petroleum industry (Cui et al., 2020; Cui et al., 2021aCui et al., 2021b; Zhao et al., 2021). However, the flow regularity in tight formations differs a lot from that in conventional reservoirs due to large numbers of microscale or even smaller pore throats (Lyu et al., 2018a). Understanding different fluid flow behavior in microscale is of great significance for a better prediction and development of tight oil reservoirs. Recently, a practical investigation of confined fluid flow has been carried out due to the availability of new tools (Nie et al., 2004; Ren and E, 2005; Zhao and Yang, 2012; Zhao et al., 2018; Zhao et al., 2020a), and advances in micro-electromechanical systems have triggered the study of microscale fluid flow (Kumar et al., 2016; Yang et al., 2016).

Many investigations have indicated that properties of confined fluids in microscales differ dramatically from those of bulk fluids (Heuberger et al., 2001; Levinger, 2002; Scatena et al., 2001), owing to the varying structures and dynamics of confined fluids induced by the fluid–solid interaction (Wu K. et al., 2017). Some novel flow phenomena have been discovered (Fei et al., 2009;

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Li, 2001; Ling et al., 2002; Xiangan et al., 2010), which are helpful for theoretical investigations of the dynamics of confined fluids (Li and He, 2005; Liu et al., 2005; Wu et al., 2017c; Xu et al., 2007; Zhi, 2003). The flow rates measured by Pfahler et al. (1990) and Qu et al. (2000) for water flow through micro-tubes were found smaller than those calculated by the classic Hagen–Poiseuille equation. In addition, the relationship of the Reynolds number vs displacement pressure gradient no longer obeys the traditionally theoretical calculation in micro-confined fluid flow (Makihara et al., 1993).

The aforementioned huge differences may rise from the significantly different strengths of the fluid-solid interaction. With the decreased flow scale, the fluid-solid interaction effect on confined fluid flow becomes more severe (Gad-El-Hak, 1999; Sandeep Arya et al., 2013; Zhang et al., 2014). The fluid in the interface region is forced to stick on the wall surface due to the strong interaction and cannot move at a certain displacement pressure gradient. Jiang et al. (2006) carried out the deionized water flow experiment in micro-tubes made of quartz at high pressure under steady flow conditions and found that the deionized water cannot flow when the radius decreases to 2.32 µm, which validated the existence of the immovable layer. Mapxacin (1987) and Huang (1998) refer to this immovable fluid layer caused by the fluid-solid interaction as the boundary layer. Unlike the concept of the conventional boundary layer theory of hydromechanics (Schlichting and Gersten, 2003), the boundary layer here further shrinks the effective flow space of confined fluids and depends on the original throat radius, displacement pressure gradient, and fluid viscosity (Liu et al., 2005; Li, 2010). The emerging novel phenomena of the boundary layer should be included in order to accurately characterize confined fluid flow in microscale. Although many empirical correlations have been developed to represent boundary layer thickness (Li and He, 2005; Xu et al., 2007; Li et al., 2011; Liu et al., 2011; Cao et al., 2016; Wu et al., 2017a), most of them just take the displacement pressure gradient and original throat radius into account, while the factor of fluid viscosity is ignored, causing extreme limitation of their application when studying different fluid flow. Since multiphase flow usually occurs in tight formations (Lyu et al., 2018a), it is of great significance to take fluid viscosity into account to develop a novel model to represent the boundary laver thickness.

In this work, we first propose a novel model to represent the boundary layer thickness, which not only takes the displacement pressure gradient and throat radius into account but also the fluid viscosity. Then micro-tube experiments are used to validate the novel model. Subsequently, the viscosity effect on confined fluid flow in microscales is discussed in detail, including the flow rate and Poiseuille number. Furthermore, the novel model representing the boundary layer thickness is incorporated into unstructured networks with anisotropy to study the viscosity effect on pore-scale flow in tight formations, respectively, under the conditions of different displacement pressure gradients, different aspect ratios, and different coordination numbers. This study provides an effective model for modeling different micro-confined fluid flow and lays a good foundation for investigating fluid flow in tight formations.

REPRESENTATION OF THE BOUNDARY LAYER THICKNESS

The confined fluids in microscales possess different structural and dynamical properties from those of bulk fluids. Fluids in the inner region are attached on the wall surface and form an immovable layer due to a strong fluid–solid interaction. Since the boundary layer shrinks the flow space, the classic Hagen–Poiseuille equation is modified as **Eq. 1** according to the physical meaning (Chen et al., 2018):

$$Q = \frac{\pi (r-h)^4}{8\mu_b} \nabla P,$$
 (1)

where *Q* is the flow rate, 10^{-9} cm³/s; *r* and *h* are, respectively, the radius of micro-tubes and boundary layer thickness, μ m; μ _b is the bulk fluid viscosity, mPas; and ∇P is the displacement pressure gradient, MPa/m.

To characterize confined fluid flow in microscales, the boundary layer thickness needs to be accurately represented in advance. As summarized from previous literature on the boundary layer effect (Mazzoco and Jr, 1999; Pertsin and Grunze, 2004; Liu et al., 2005; Zhang et al., 2008; Cui et al., 2010; Zhu et al., 2013), the boundary layer thickness is affected not only by the micro-tube radius and displacement pressure gradient but also by the fluid viscosity. To obtain the relationship among them, the variable-by-variable analysis method is adopted here.

First, the relationship of the boundary layer thickness vs displacement pressure gradient needs to be obtained. It is clear that the flow rate is zero when no displacement pressure gradient is exerted on the fluid, which can be reckoned that the boundary layer thickness is equal to the original micro-tube radius (ratio of the boundary layer thickness h/r equals to 1). At the same time, the boundary layer thickness decreases with an increased displacement pressure gradient due to the novel equilibrium of shear force and the displacement pressure gradient (Wu et al., 2017b). Based on the experimental data of confined fluid flow in micro-tubes (**Figure 1**) (Li, 2010), it can be seen that ratio of the boundary layer thickness decreases exponentially with an increased displacement pressure gradient.

Therefore, the relationship between the boundary layer thickness and displacement pressure gradient can be expressed as **Eq. 2**:

$$h = r e^{-b\nabla P^c} , \qquad (2)$$

where b and c are related to tube radius and fluid viscosity, respectively, and their values are always positive.

Second, values of b and c at different micro-tube radii but with a fixed fluid viscosity (0.92 mPa s) are obtained based on Li's micro-tube experiments (**Figure 1A**) (Li, 2010), which are shown in **Figure 2**.

To guarantee that b and c are always positive, exponential functions are used to obtain the relationship of b and c vs microtube radii at a fixed fluid viscosity, as given in **Eq. 3**:

$$\begin{cases} b = me^{nr}, \\ c = ke^{-gr^{p}}, \end{cases}$$
(3)





where m, n, k, g, and p are related to the fluid viscosity.

Finally, relationships of parameters m, n, k, g, and p vs fluid viscosities are, respectively, obtained based on Li's confined fluid flow experiments in microscales with different viscosities (Figure 1B) (Li, 2010), using Eq. 1, Eq. 2, and Eq. 3. The results are relatively shown in Figure 3.

As can be seen from **Figure 3**, the relationships of m, n, k, g, and p vs fluid viscosities can be expressed as follows:

$$\begin{cases} m = 1.48\mu^{-0.1975}, \\ n = 0.03792e^{-1.127\mu} + 0.08604e^{-0.02816\mu}, \\ k = 0.3462\mu^{0.08706}, \\ g = 0.06592e^{0.02343\mu} - 0.07507e^{-0.4994\mu}, \\ p = -1.174e^{0.07147\mu} + 3.033. \end{cases}$$
(4)

Using the aforementioned variable-by-variable analysis method, the novel model to represent the boundary layer thickness with the consideration of displacement pressure gradient, micro-tube radius, and fluid viscosity is proposed. To validate the accuracy and reliability of the earlier novel model, Wu's (Wu et al., 2017b) experimental data of deionized water flow in different radial micro-tubes are used. Comparison results are shown in **Figure 4**. It can be seen that the calculated flow rates agree well with the experimental values, indicating the accuracy of the novel model.

Compared with other empirical correlations, the novel model not only involves more factors but also considers the variations of parameters along with the micro-tube radius and fluid viscosity. In addition, the calculated boundary layer thickness by the novel model will never exceed the original radii of micro-tubes, which



greatly broadens its application range. Since microscale and smaller scale pore throats possess similar flow mechanisms (Striolo, 2006; Thomas and Mcgaughey, 2009), the novel model may also be valid for modeling confined fluid flow in smaller scales. Furthermore, tight formations feature abundant micro-pore throats of different sizes, and the novel model lays a good foundation for studying fluid flow in tight formations. In the following sections, the viscosity effect on confined fluid flow from the perspective of flow rate and Poiseuille number in micro-tubes will be studied at first. Then the novel model will be incorporated into unstructured networks with anisotropy to investigate the viscosity effect on pore-scale flow in tight formations.

VISCOSITY EFFECT ON CONFINED FLUID FLOW IN MICRO-TUBES AND TIGHT FORMATIONS Viscosity Effect on Confined Fluid Flow in Micro-Tubes

Viscosity Effect on the Flow Rate

To study the effect of fluid viscosity on the flow rate due to the fluid–solid interaction, the decreasing factor, analogous to the enhancement one indicated by Mainak et al. (2005) and Holt et al. (2006), is defined as the ratio of the measured flow rate $Q_{exp}-Q_m$ predicted by the classic Hagen–Poiseuille equation. Since the measured flow rate can be well-predicted by our proposed novel model, it can be modeled by **Eq. 1**. Then, the decreasing factor can be expressed as follows:

$$\varepsilon = \frac{\mathcal{Q}_{\exp}}{\mathcal{Q}_n} = \left(1 - \frac{h}{r}\right)^4 = \left(1 - e^{-b\left(\mu, r\right)\nabla P^c\left(\mu, r\right)}\right)^4.$$
 (5)

Figure 5 shows the relationship of the decreasing factor vs the displacement pressure gradient at different radii and fluid viscosities, respectively, with and without considering the fluid-solid interaction. It is indicated that the decreasing factor keeps a constant (with its value 1) at any given displacement pressure gradient, pore throat radius, and fluid viscosity when the fluid-solid interaction is not included. However, great deviation occurs when the fluid-solid interaction is taken into consideration. The decreasing factor is no longer a constant, which gradually increases with the increased displacement pressure gradient. This phenomenon can be accounted for by the variation of the effective flow space. Due to the strong fluid-solid interaction, the fluid in the interface region is attached to the wall surface and cannot move, compressing the effective flow space, resulting in the smaller flow rate. With the increase in the displacement pressure gradient, the fluid-solid interaction gradually weakens, which enlarges the effective flow space. Therefore, the decreasing factor starts to increase and become more and more close to the one without considering the fluid-solid interaction.

In addition, the decreasing factor varies a lot at different fluid viscosities, which is quite different from its changing regularity without considering the fluid–solid interaction. The decreasing factor decreases with the increased fluid viscosity with its value being always smaller than 1. This phenomenon results from the fluid–solid interaction. With the increase in fluid viscosity, the Chen et al.



fluid-solid interaction grows more intense, resulting in more and more fluids attached to the wall surface. Eventually, the effective flow space is further compressed as the fluid viscosity increases, resulting in the smaller flow rate and decreasing factor. Meanwhile, the smaller the original radius, the stronger will be the fluid-solid interaction. Therefore, the fluid viscosity effect on confined fluid flow will be more serious in the smaller flow space. As a result, the fluid viscosity effect is needed to be considered in tight formations, which captures large numbers of micro-/nanopore throats.

Viscosity Effect on the Poiseuille Number

The Poiseuille number is an important parameter to characterize fluid flow, and it has been studied for many years (Damean and Regtien., 2001; Dutkowski, 2008; Hong et al., 2008; John et al., 2009; Park et al., 2002) (Krishnamoorthy and Ghajar, 2007). Churchill (Churchill, 1988) pointed out that the Reynolds number R_e is unsuitable for non-accelerating and viscous flow since density does not play a part. He suggested that the Poiseuille number P_o should be used, instead of R_e . Meanwhile, most of the initial work performed in determining P_o in microscales reported a variation from the classical theory. Several studies reported a higher value of P_o , while few reported a lower one (Krishnamoorthy and Ghajar, 2007). Even though enormous research has been performed on P_o , a complete understanding of it is still unavailable. In this part, P_o for the confined fluid flow in micro-tubes will be investigated.

Based on our proposed model, the expressions of the friction factor f and R_e in micro-tubes can be, respectively, obtained in Eq. 6 and Eq. 7:

$$f = \frac{2D}{\rho v^2} \nabla P = \frac{256r^5 \mu^2}{\rho \left(r - h\right)^8 \nabla P}.$$
(6)

$$R_e = \frac{\rho v D}{\mu} = \frac{\rho r \left(r - h\right)^4 \nabla P}{4 \left(\mu r\right)^2}.$$
(7)

Since the Poiseuille number P_o is the product of the friction factor and Reynolds number $f \times R_e$ (Churchill, 1988), it can be expressed as follows:

$$P_o = f \times R_e = \frac{64r^4}{(r-h)^4}.$$
 (8)

Figure 6 illustrates the relationship of P_o vs displacement pressure gradient at different fluid viscosities, with and without considering the fluid–solid interaction. It is noted that P_o induces







a significantly different changing rule from that in conventional fluid flow when the fluid-solid interaction is taken into consideration. P_o in consideration of the fluid-solid interaction is always larger than the one ignoring the interaction and decreases with the increased displacement pressure gradient. This deviation can be due to the variation of the effective flow space caused by the fluid-solid interaction. As a result of the strong interaction, fluid in the inner region sticks to the wall surface and cannot move at a certain displacement pressure gradient, compressing the effective flow space. However, the effective flow space enlarges gradually with the increasing displacement pressure gradient, making P_o more and more close to the value without considering the fluid-solid interaction.

At the same time, it can be seen that P_o also shows different values at different fluid viscosities. P_o stays at a constant value of 64 when no fluid–solid interaction is considered, indicating that the fluid viscosity has no effect on it. In contrast, P_o is no longer a constant after considering the fluid–solid interaction. With the increasing fluid viscosity, more and more fluid will be attached to the wall surface, reducing the effective flow space and resulting in larger flow resistance. Therefore, P_o at large fluid viscosity is always higher than that at small one when the fluid–solid interaction is involved.

Viscosity Effect on Pore-Scale Flow in Tight Formations

Construction of Pore Networks and Pore-Scale Flow Network Model

Fluid flow not only occurs in single tubes but also in tight formations with different pore throat radii and complex topologies (Lyu et al., 2019; Lyu et al., 2018c). In order to improve the recovery of tight oil reservoirs, fluid flow in tight formations should be studied correctly. In this section, the fluid viscosity effect on pore-scale flow in tight formations will be investigated.

For investigation, a platform which can represent the complex structures of tight formations is required to establish (Dong et al., 2017; Huaimin et al., 2019; Raeini et al., 2018; Wang and Sheng, 2018; Zhao et al., 2020b). Here, an unstructured stochastic network model with anisotropy is first constructed. The anisotropy here means that not all pores in the pore network possess the same coordination number. Each pore is assigned a coordination number based on the distribution of coordination numbers. Compared with other generation methods (Idowu, 2009; Raoof and Hassanizadeh, 2010), the method developed here can be applied to any coordination number distribution and is more flexible (Chalendar et al., 2018; Chen et al., 2019; Wang and Sheng, 2019). The detailed construction process is shown as follows:

- 1) An overall physical size of the network $L_x \times L_y \times L_z$ and resolution *Res* are given. Based on the parameters, numbers of lattices $[L_x/Res] \times [L_y/Res] \times [L_z/Res]$ are determined. Then the pore body of the network is randomly assigned on these lattices. Subsequently, the pore body radius is assigned based on the pore radius distribution. The following pore bodies are assigned on the remaining lattices, and the pore body radii are given one by one if the throat lengths between the pore body to be incorporated and incorporated pore bodies are all larger than the minimal pore radius of the pore radius distribution. The aforementioned operations are repeated until the overall porosity reaches the target (it is 0.12 in our study).
- 2) Coordination numbers are sampled from the probability distribution. We assume that the closer the distance of the pores, the easier they will be connected. Based on this assumption, we rank the pore bodies by their distances to the ninth most adjacent pores (since the largest coordination number in our study is 9) and assign the coordination number correspondingly.



- For every pore body, we connect its nearest pores one by one until the connectivity reaches the assigned coordination number in step (2).
- 4) We sample the throat radii from the input probability distribution and rank them in ascending order. Then we assign the ranked throat radii to the throats by ranking the mean radii of their connecting pore bodies.

The input data here are based on the extracted pore network of Berea 3D digital rock data by Dong and Blunt (Hu and Blunt, 2009). We reduce the throat radius distribution by a factor of 10 to make the pore throat radius in the range of tight formations. Visualization of the stochastic network along with its distributions of pore radii, throat radii, and coordination number is presented in **Figure 7**. It can be seen that generated distributions of the pore radii, throat radii, and coordination number agree well with the target data, illustrating the reliability of the aforementioned generation method.

When the network is fully saturated with a single-phase *p*, its flow rate at every pore satisfies the mass conservation as follows:

$$\sum_{j} q_{p,ij} = 0, \tag{9}$$

where j runs over all the throats connected to the pore i. The flow rate between two pores i and j is given as follows:

$$q_{p,ij} = g_{p,ij} \nabla P_{p,ij},\tag{10}$$

where $g_{p,ij}$ and $\nabla P_{P,ij}$ are, respectively, the conductance and displacement pressure gradient between the pore bodies *i* and *j*.

The conductance between two pore bodies $g_{p,ij}$ is taken to be the harmonic mean of each individual conductance as follows:

$$\frac{L_{ij}}{g_{p,ij}} = \frac{L_{p,i}}{g_{p,i}} + \frac{L_{p,t}}{g_{p,t}} + \frac{L_{p,j}}{g_{p,j}},\tag{11}$$

where *t* indicates the connecting throat. The pore body lengths, L_i and L_j , are the lengths from the pore–throat interface to the pore center.

Since the aspect ratio is large in tight formations (Zhao et al., 2015), the fluid–solid interaction in the pores is much smaller compared to that in the throats. Hence, the fluid–solid interaction will only be considered in the throats. Fluid conductance g of the pore and throat in single-phase laminar flow can be expressed as follows:





where g_t and r_t are, respectively, the throat conductance and radius.

Then a non-linear set of equations can be formed by combining **Eq. 9** and **Eq. 10**, which has to be solved in terms of pore pressures through repeated iterations. The absolute permeability K of the network is found from Darcy's law:

$$K = \frac{\mu_b q_t L}{A(P_{in} - P_{out})},\tag{13}$$

where *K* is the absolute permeability, um^2 ; q_t is the flow rate, cm^3/s ; P_{in} and P_{out} are respectively inlet and outlet pressures, 0.1 MPa; *A* and *L* are the cross-sectional area and length of the network, cm^2 and cm.

Based on the aforementioned constructed network and fluid flow calculation process, the viscosity effect on pore-scale flow in tight formations can be realized. In the following part, the viscosity effect on pore-scale flow in tight formations will be studied under three different conditions, which are, respectively, different displacement pressure gradients, different aspect ratios, and coordination numbers.

Viscosity Effect on Pore-Scale Flow at Different Displacement Pressure Gradients

Figure 8 shows the fluid viscosity effect on the effective throat radius and absolute permeability at different displacement pressure gradients, with and without considering the fluid-solid interaction.

It can be seen that the absolute permeability keeps a constant with the same value at a series of different displacement pressure gradients and fluid viscosities when the fluid-solid interaction is ignored. This phenomenon indicates that displacement pressure gradients and fluid viscosities have nothing to do with the absolute permeability which is in agreement with our common sense. However, the effective flow structures of tight formations are influenced when the fluid-solid interaction is taken into consideration, which results in a significantly different changing rule of the absolute permeability from that in conventional fluid flow. The absolute permeability no longer keeps the same constant and changes with the variation of displacement pressure gradient and fluid viscosity. As displacement pressure gradient decreases, part of the boundary fluid that can originally participate in pore-scale flow is attached on the wall surface and cannot move, reducing the effective flow space. As a result, the absolute permeability is smaller than that ignoring the fluid-solid interaction. With the displacement pressure gradient continuing to decrease, the effective flow space grows smaller and smaller, and the deviation of the absolute permeability with and without considering the fluid-solid interaction turns larger and larger. Meanwhile, with the increase in fluid viscosity, the number of molecules in the fluid becomes large, resulting in a larger fluid-solid interaction. More and more fluid is attached on the pore wall and increases the boundary layer thickness. The effective flow space becomes smaller, which results in larger flow resistance. As a result, the absolute permeability decreases with increased fluid viscosity. The larger the fluid viscosity, the smaller will be the absolute permeability.

Viscosity Effect on Pore-Scale Flow at Different Aspect Ratios

So as to investigate the fluid viscosity effect on pore-scale flow at different aspect ratios, we scale down the original throat radius distribution (**Figure 7C**) to a series of different values from 0.6 to 1 with the interval of 0.05, five of which are shown in **Figure 9A** in particular. Meanwhile, the other parameters in the aforementioned network (**Figure 7**) such as the distributions



of the pore radii and coordination number, positions of the pore bodies and the physical size stay unchanged.

Figure 9B shows the fluid viscosity effect on the absolute permeability at a series of the above different aspect ratios, with and without considering the fluid–solid interaction.

It is noted from Figure 9B that the effect of fluid viscosity on the absolute permeability considering the fluid-solid interaction differs significantly from that ignoring the interaction. The absolute permeability curves at different fluid viscosities overlap when the fluid-solid interaction is excluded, indicating that the fluid viscosity has no effect on the absolute permeability. This is in accordance with the common sense that the absolute permeability is only the function of pore structures, which has nothing to do with fluid properties. However, the absolute permeability curves separate with each other when the fluid-solid interaction is involved. The absolute permeability decreases with increased fluid viscosity at a certain aspect ratio. This special behavior can be accounted for from the perspective of the fluid-solid interaction. As the fluid viscosity increases, the number of molecules in the fluid increases, resulting in larger surface microscopic forces. More and more fluid which can be driven at smaller fluid viscosity are attached on the wall surface due to the strong interaction, further compressing the effective flow space and resulting in larger flow resistance. Therefore, the absolute permeability decreases with the increased fluid viscosity at a constant aspect ratio.

Viscosity Effect on Pore-Scale Flow at Different Coordination Numbers

For the sake of studying the fluid viscosity effect on pore-scale flow at different coordination numbers, the following process is developed to keep other structural parameters such as the distributions of the pore and throat radii, the positions of the pore bodies, and the physical size unchanged, except the coordination numbers.

1) We first generate the pore bodies including the radii and positions until the overall porosity reaches the target 0.12, as

mentioned in the first step of constructing a stochastic network in section 3.2.

- 2) Based on the established pore bodies, we, respectively, set the coordination number as 4, 6, 8, and 10 and assign them to each pore correspondingly as the rule indicated in the second step in section 3.2
- 3) The remaining steps are the same as the ones (steps 3) and 4) of constructing the network) listed in section 3.2.

Through the aforementioned construction process, four stochastic networks with different coordination numbers but the same positions and radii distributions of pore bodies and the physical size are established. The generated distributions of throat radii with four different coordination numbers are shown in **Figure 10A**. It can be seen that the generated distributions of throat radii agree well with each other, guaranteeing the reliability of studying the viscosity effect on pore-scale flow at different coordination numbers.

Figure 10B shows the fluid viscosity effect on the absolute permeability at different coordination numbers. It is clear that the viscosity effect on the absolute permeability differs a lot with and without considering the fluid–solid interaction. The absolute permeability curves overlap at different fluid viscosities when no fluid–solid interaction is taken into account, implying that the absolute permeability curves separate with each other when the fluid–solid interaction is involved. The larger the fluid viscosity, the smaller is the absolute permeability. This difference can also be due to the fluid–solid interaction. At a constant coordination number, the fluid–solid interaction grows more and more intense with the increased fluid viscosity. More and more fluid is attached on the wall surface, resulting in larger flow resistance and smaller absolute permeability.

CONCLUSION

In this work, a novel model considering the fluid-solid interaction is developed to characterize the confined fluid flow



in microscales based on the concept of boundary layer. Microtube experiments with different scales are used to verify the accuracy and reliability of the novel model. Subsequently, the fluid viscosity effect on confined fluid flow in micro-tubes and pore-scale flow in tight formations are, respectively, studied. The following conclusions are arrived:

- The viscosity effect on confined fluid flow in micro-tubes induces significant differences from that in conventional flow. With the increased fluid viscosity, the molecular density of the fluid increases which greatly strengthens the fluid-solid interaction. More and more boundary fluid is attached to the wall surface and cannot be driven at a certain displacement pressure gradient. Therefore, the effective flow space is narrowed and the flow resistance is magnified, which results in the smaller decreasing factor and larger Poiseuille number.
- 2) The absolute permeability is no longer a constant when considering the fluid-solid interaction into pore-scale flow in tight formations. The absolute permeability is not only related to pore structures of the porous media but also affected by the fluid viscosity, which is unlike our previous common sense.
- 3) The fluid-solid interaction grows with the increase in fluid viscosity, which compresses the efficient flow space. As a result, the absolute permeability decreases with increased fluid viscosity, respectively, under the conditions of different displacement pressure gradient, different aspect ratios, and different coordination numbers.

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DATA AVAILABILITY STATEMENT

The original contributions presented in the study are included in the article/supplementary material, and further inquiries can be directed to the corresponding author.

AUTHOR CONTRIBUTIONS

MC is responsible for the main work and writing of the manuscript; QL and LC are responsible for the guidance and modifications of the manuscript; XW provides the thoughts of constructing networks and modifications of the manuscript; and CL and QF helps to improve English grammar of the manuscript.

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Conflict of Interest: MC, QF, and QL are employed by the China National Offshore Oil Corporation (China).

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